

## Deep learning

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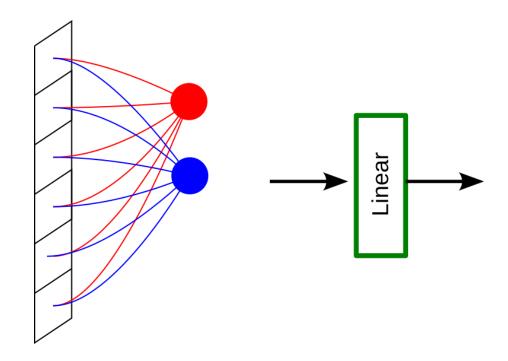
## **Outline**

- Back on last course
- Concept of deep learning
- Convolutional Neural Networks
- Attention and transformers

#### Back on neural networks

#### The linear layer

- Also called *fully connected* 
  - a neuron is connected to all the inputs
- High number of parameters ( $\mathbf{W}$  matrix): |inputs|\*|outputs|

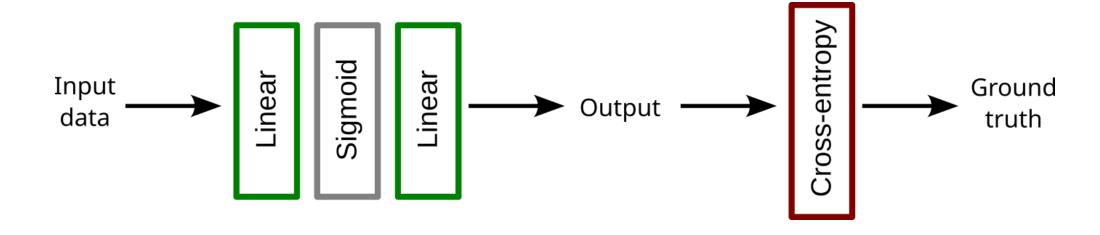




## Multi-layer perceptron

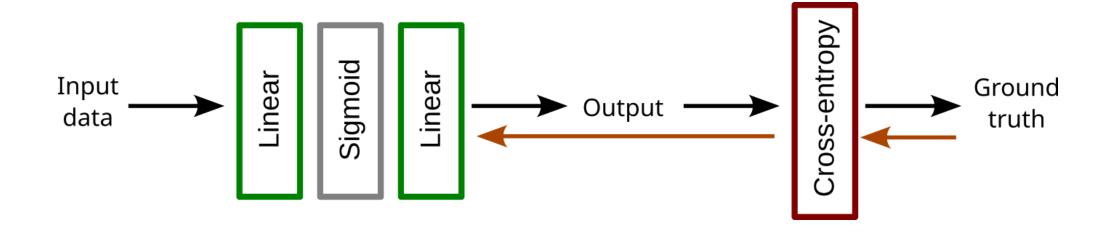
A stack of linear layers with activation functions (e.g., sigmoids)

Optimization with gradient descent.





## Optimization: forward-backward algorithm





## Chain rule applied to neural networks

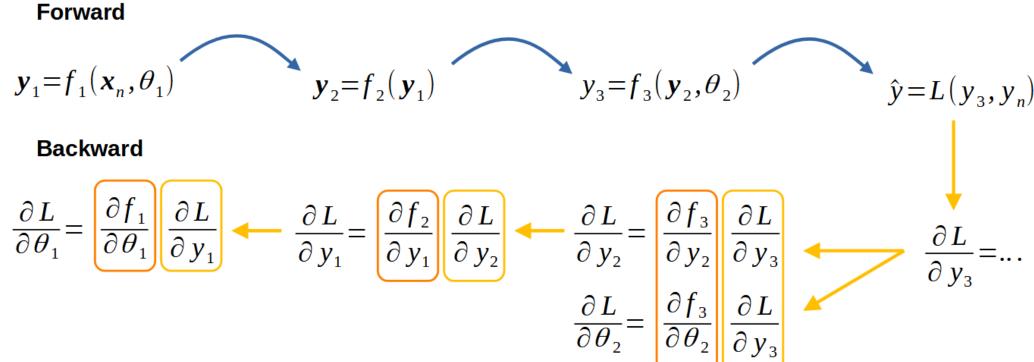
#### **Forward**





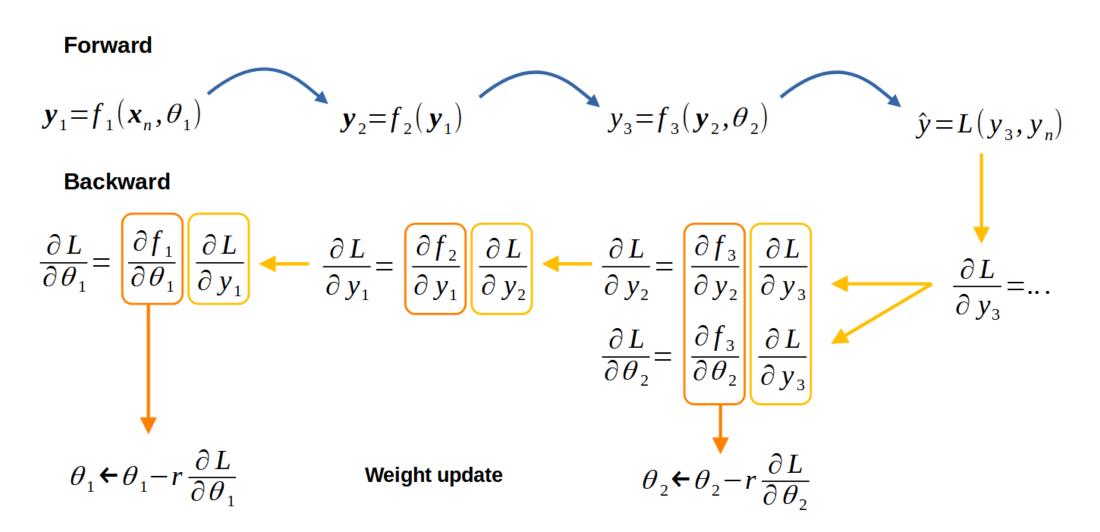
## Chain rule applied to neural networks

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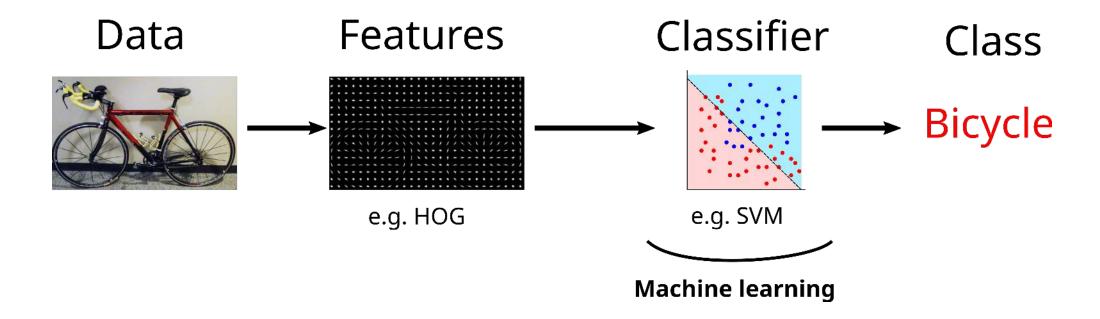


## Chain rule applied to neural networks

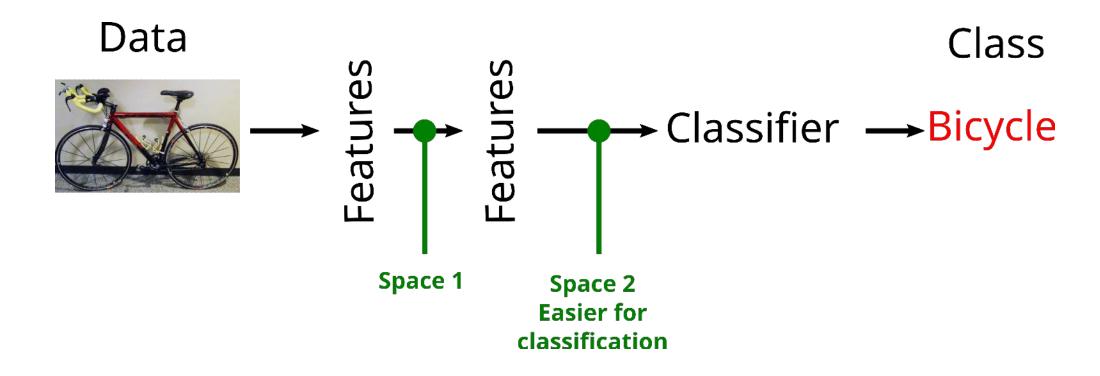


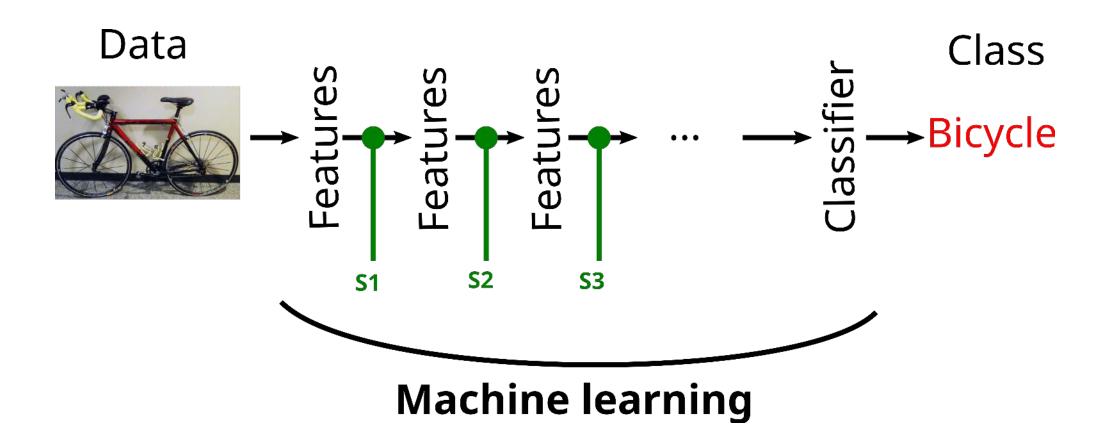






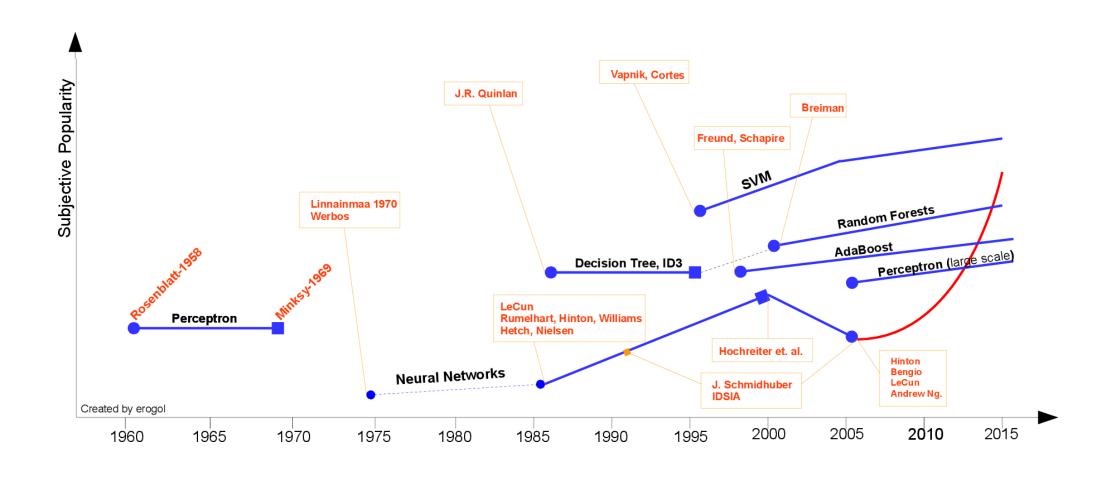








## Massively data driven approaches





## Convolutions and image processing

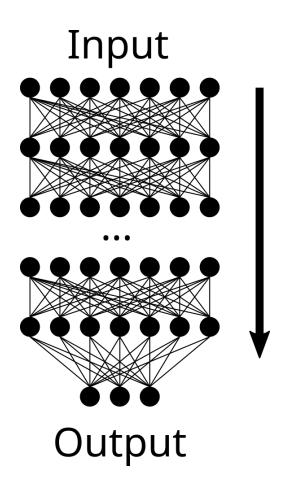
# Multi-layer perceptron (before 1990)

#### MLP becomes larger and deeper

- difficult convergence
- few data
- very long training
- progessive loss of interest

#### **SVM**

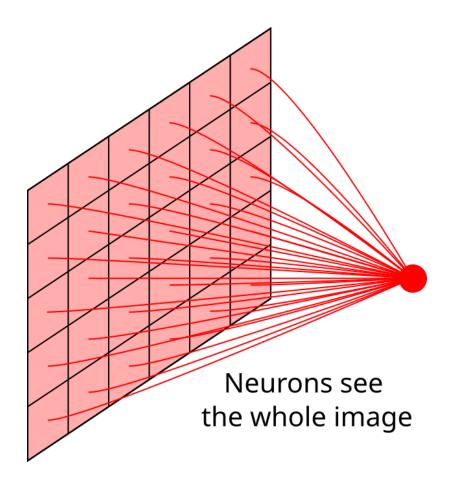
- simpe to use
- convergence proof
- fast



# Multi-layer perceptron for images

#### Using a linear layer?

Lots of weights! (at least one per pixel!)

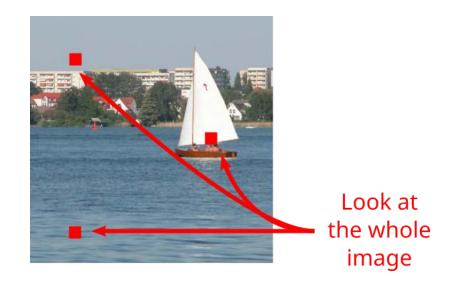


# Multi-layer perceptron for images

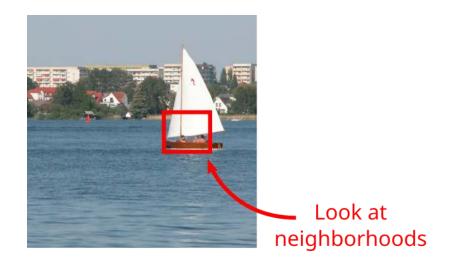
#### Using a linear layer?

Lots of weights! (at least one per pixel!)

Is it interesting to look at relations in the whole image?

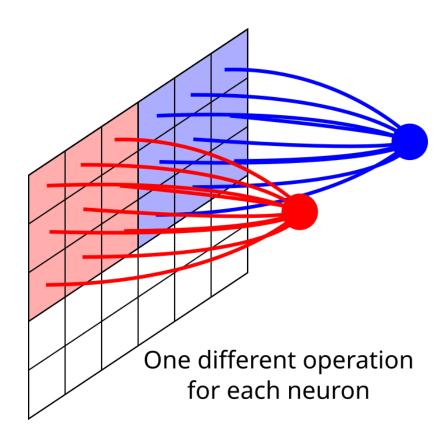


Look at small neighborhoods (where the objects are)



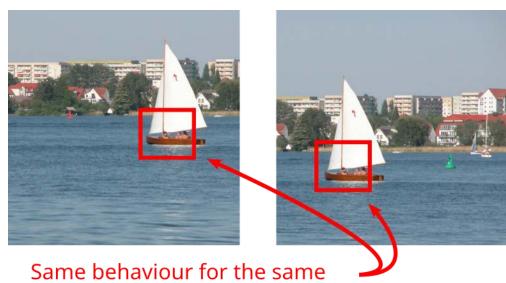
Look at small neighborhoods (where the objects are)

Create neurons that take a patch input



#### **Problem**

Translation of the object must lead to same behaviour of the neurons



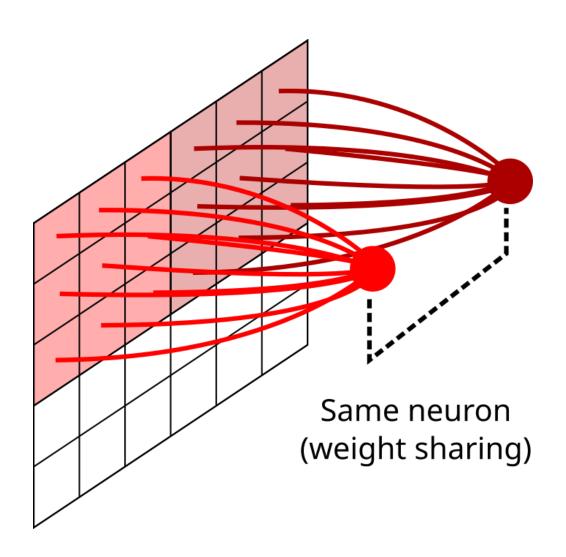
Same behaviour for the same pattern at different location

#### **Problem**

Translation of the object must lead to same behaviour of the neurons

#### **Solution**

Use the same neuron (i.e. all the neurons of the layer share weights)



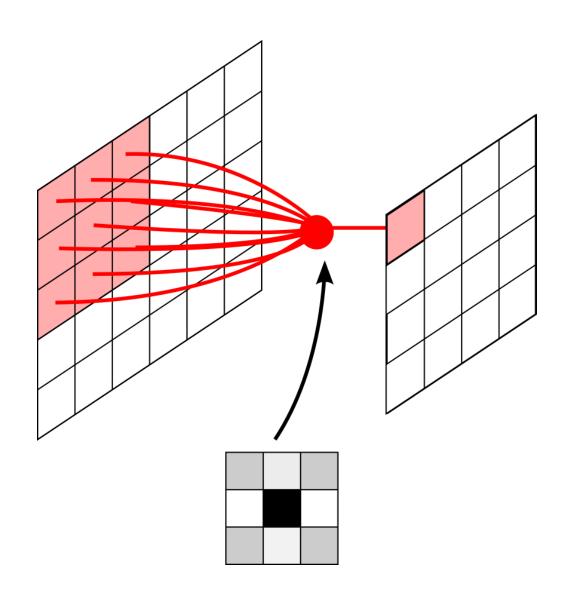
#### **Forward**

Let (i, j) be the coordinates in the input map.

(k,l) be the size of the patch (size of the kernel, usually k=l)

Then:

$$y_{i,j} = \sum_k \sum_l w_{k,l} x_{i+k,j+l} + b$$



Backward weight update

$$rac{\partial y_{i,j}}{\partial w_{k,l}} = x_{i+k,j+l}$$

Let y be the output map and  $\Delta y$  be the gradient coming back:

$$rac{\partial y}{\partial w_{k,l}} = \sum_i \sum_j x_{i+k,j+l}$$

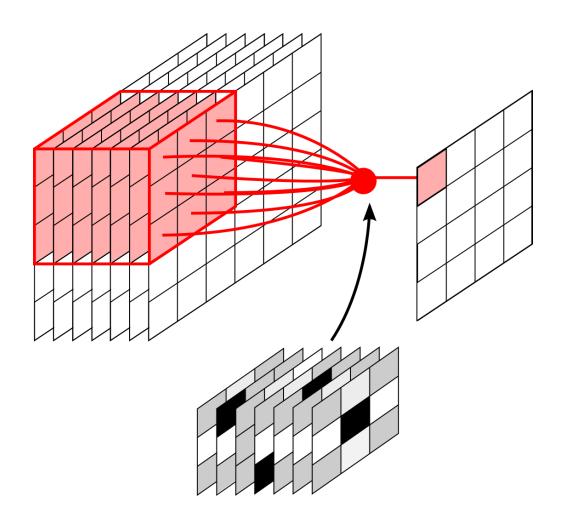
Finally, the update rule:

$$egin{aligned} w_{k,l} \leftarrow w_{k,l} - lpha rac{\partial y}{\partial w_{k,l}} \Delta y \ \leftarrow \sum_i \sum_j x_{i+k,j+l} \Delta y_{i,j} \end{aligned}$$

#### **Forward**

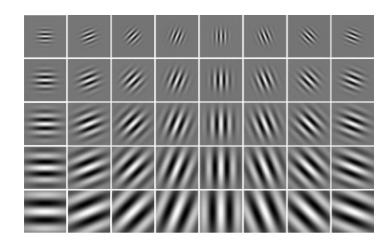
Same with term to term multiplication:

$$y_{i,j} = \sum_a \sum_b \mathbf{w}_{a,b} \mathbf{x}_{i+a,j+b}$$

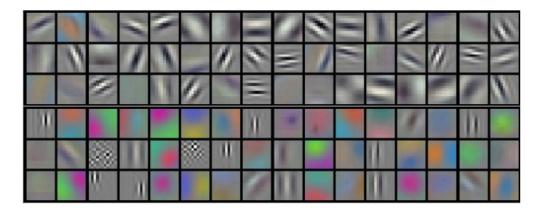




#### Convolution: what do convolutions learn?



Gabor filters.



First layer of AlexNet.



#### **Dimension reduction**

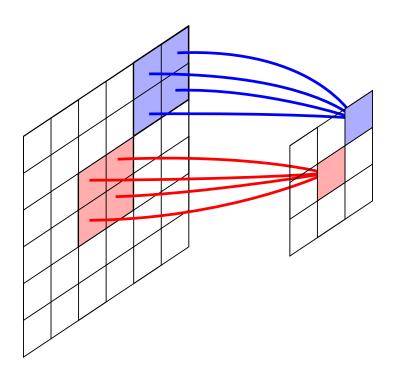
With the previous convolution, the output dimension is the same as the output dimension.

For classification: only one label, need for \textbf{dimension reduction}.

- convolution stride: do not look at all the pixels of the input (one every two, one every three...)
- Max Pooling

## **Max Pooling**

- dimension reduction
- relative translation invariability



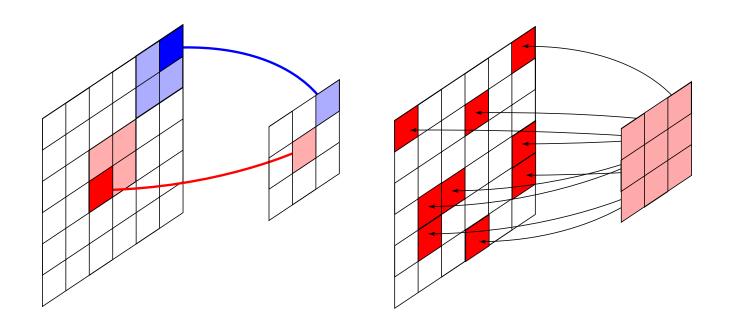
## **Max Pooling**

#### **Forward**

Max signal

#### **Backward**

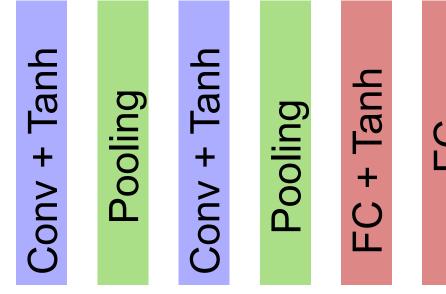
Gradient transmission to max signal origin, zero otherwise





## Convolutional Neural Netowkrs - LeNet (1990

LeNet (1990) Images 28x28





#### Isues

#### **Issues**

- Learning speed
- Exploding or vanishing gradients
- Overfitting
- Local minima

#### Limitations

- Architecture
- Initialization
- Computing power
- Data
- Optimization

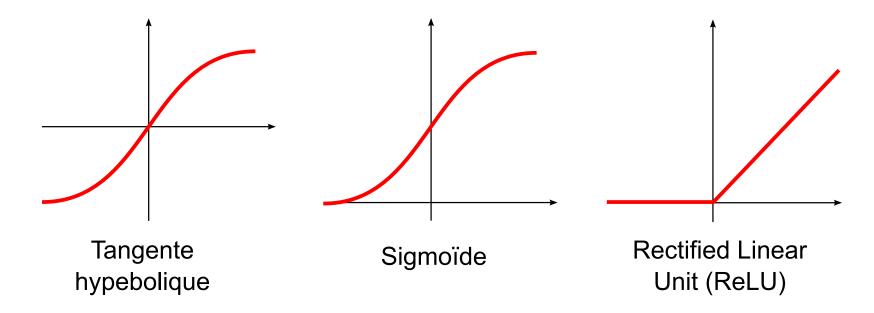


## **Solutions**

- activations
- mini-batches
- batch norm
- good weight initialization
- better optimization



#### **Activations**

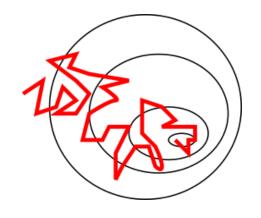


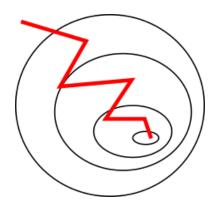
#### Rectified linear unit}

- Faster gradient computation
- Similar convergence



## Mini-batches



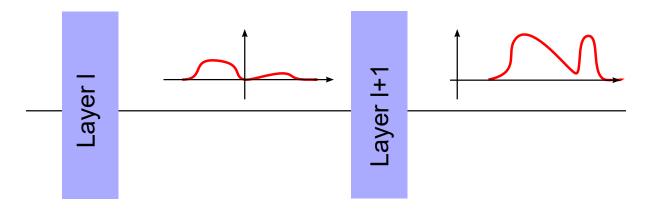


## **Gradient smoothing**

Smoother gradient converges faster.



#### **BatchNorm**



Changes in the signal dynamic make the model more difficult to optimize: exponential or vanishing gradients.

**Objective**: control the signal distribution:

$$y^{l*} = rac{y^l - \mu}{\sqrt{\sigma^2 + \epsilon}} \gamma + eta$$

 $\gamma$  and  $\beta$  are learnt,  $\mu$  and  $\sigma$  are computed (mean and standard deviation).

Learning is faster (iteration number) but slower (statistics computation).



## Weight initialization}

Weights have great influence on convergence speed.

They are randomly initialized.

- too small weigths: vanishing signal
- to high: exploding signal

Conservation of signal properties.

$$Var(Y) = Var(X)$$

## Weight initialization

#### **Xavier initialization**

 $X \in \mathbb{R}^n$ , weights W and output  $Y \in \mathbb{R}$ 

$$Y = W_1 X_1 + W_2 X_2 + \dots + W_n X_n$$

 $X_i$  and  $W_i$  independent:

$$Var(W_iX_i) = E[X_i]^2 Var(W_i) + Var(X_i) Var(W_i) + Var(X_i) E[W_i]^2$$

 $E[X_i] = 0$  and  $E[W_i] = 0$ :

$$Var(W_iX_i) = Var(X_i)Var(W_i)$$

finally  $\ Var(Y) = n Var(X_i) Var(W_i) \ and we chose$ 

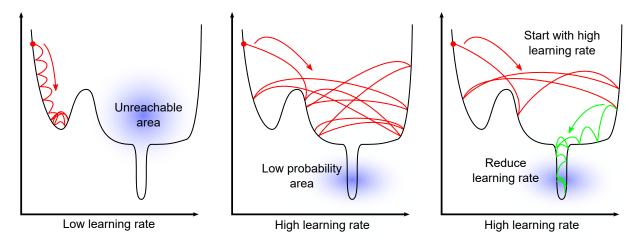
$$Var(W_i) = rac{1}{n}$$



## **Optimization - Stochastic Gradient Descent**

#### See neural network class

Update rule:  $w_{t+1} = w_t + \alpha \Delta w$  (learning rate lpha)



- Step decrease
- Exponential decrease
- Cosine annealing ...

## **Optimization - SGD with Momentum**

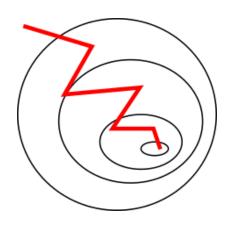
Same idea as mini batch: smooth gradient in the good direction

#### Momentum

Use previous gradient to ponderate the direction of the new gradient.

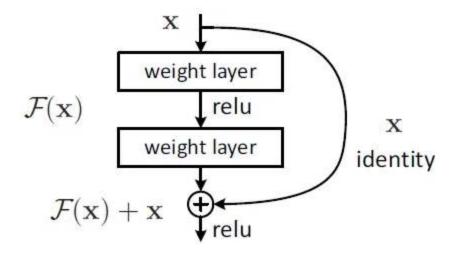
$$v_t = \gamma v_{t-1} + \alpha \Delta w$$
  
 $w_t = w_{t-1} - v_t$ 

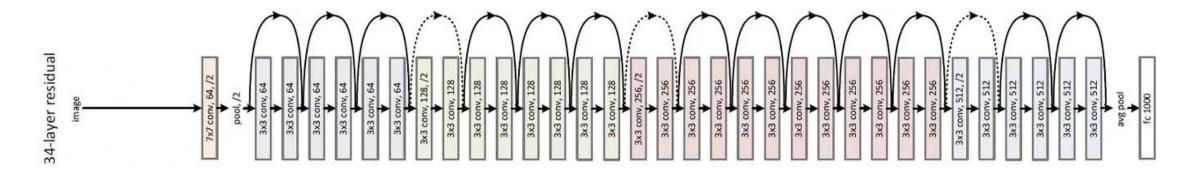
 $\gamma$  is the momentum.





#### **ResNet**







## Do not forget the classics



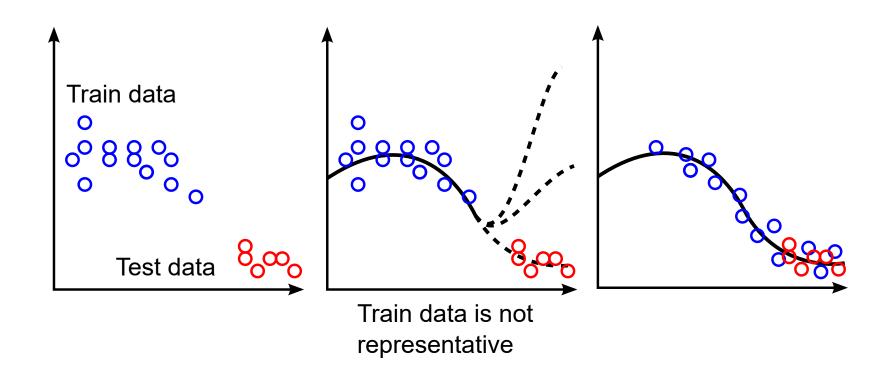
## Data

- Representative
- Data augmentation
- Data normalization



## Data

Train data must be representative of the problem}





#### **Data**

#### **Data normalization**

- -Compute mean  $\mu$  and standard deviation  $\sigma$  on the train set.
- -Normalize input I (train and test):

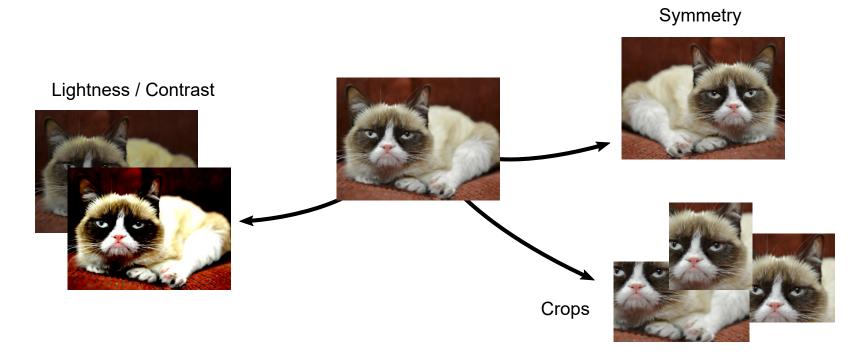
$$\hat{I} = \frac{I - \mu}{\sigma}$$



## Data - data augmentation

Random variations of input parameters (images: lightness, contrast \dots)

- train on a more representative set
- avoid learning on unwanted features





## Problems and partial solutions

#### **Problems**

- Small amount of data
- Low computational power

#### Solutions?

• Use classical approaches (Perceptron, SVM, ...)