

# Generalizing discrete convolutions for unstructured point clouds

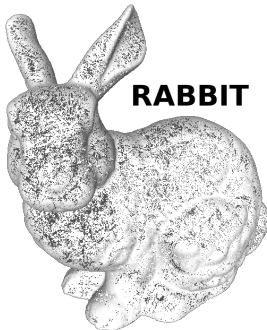
Eurographics 3DOR 2019

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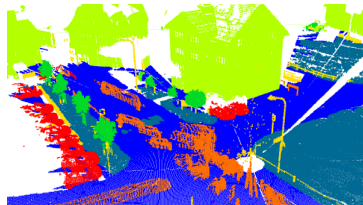
Alexandre Boulch

Image Vision Machine Learning team - ONERA

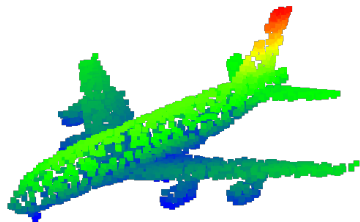
[www.boulch.eu](http://www.boulch.eu)



Classification



Semantic segmentation



A point cloud is

- unstructured : not sampled on grid
- unordered : invariant by permutation of points
- scale less : e.g. CAD, photogrammetry
- defined by point coordinates only

Previous works

Generalizing convolutions

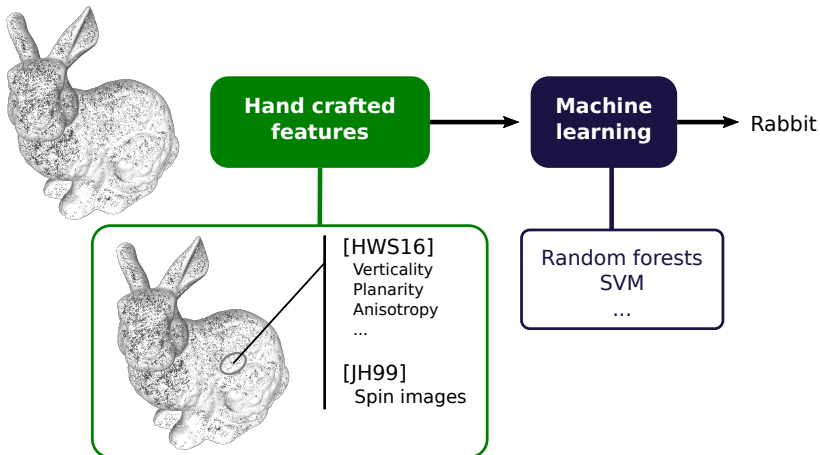
Implementation

Experiments

Perspectives and conclusions

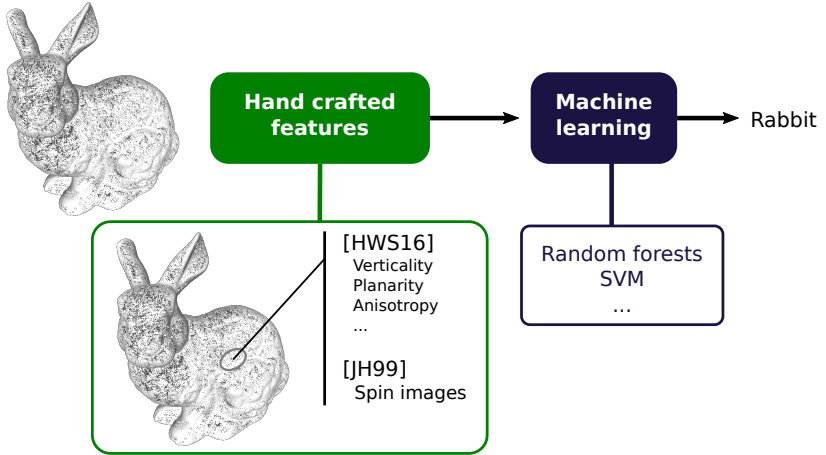
## Previous works

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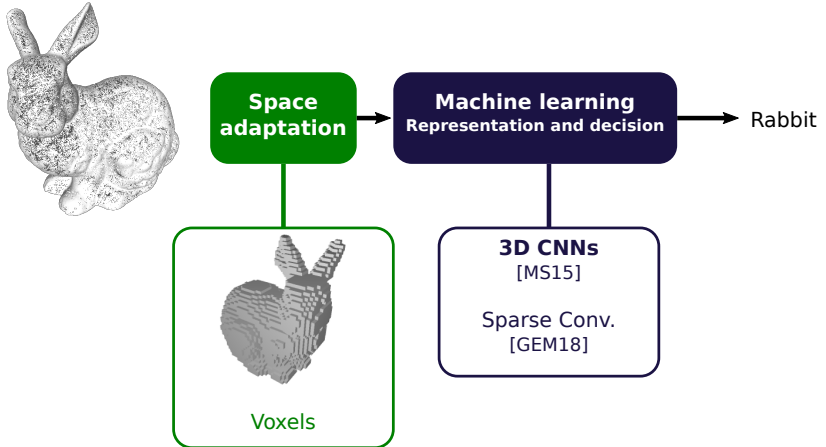


[HWS16] Hackel et al., Fast semantic segmentation of 3D point clouds with strongly varying density, ISPRS Annals of Photogrammetry, Remote Sensing & Spatial Information Sciences, 2016

[JH99] Johnson et al., Using spin images for efficient object recognition in cluttered 3D scenes, IEEE PAMI 1999.



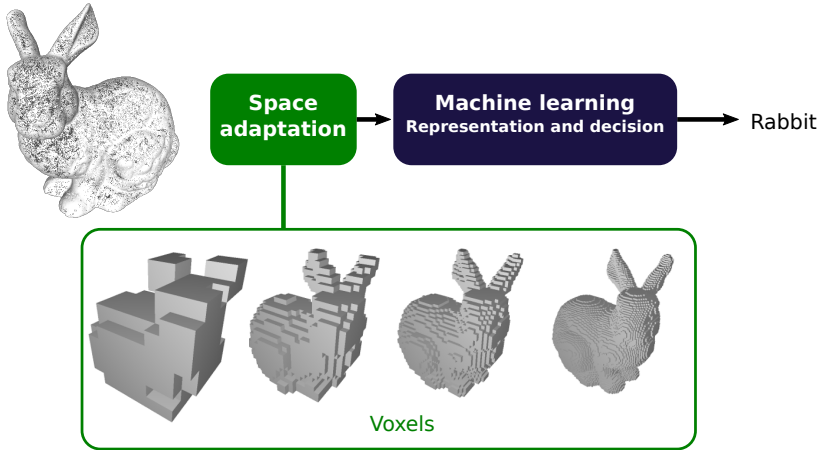
- Designing features is difficult → learn them with deep methods
- Exploit images processing approaches → adapt space



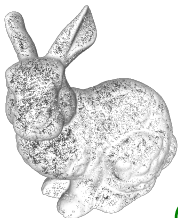
[MS15], Maturana and Scherer, Voxnet : A 3D convolutional neural network for real-time object recognition, IROS 2015

[GEM18] Graham et al. 3D semantic segmentation with submanifold sparse convolutional networks, CVPR 2018





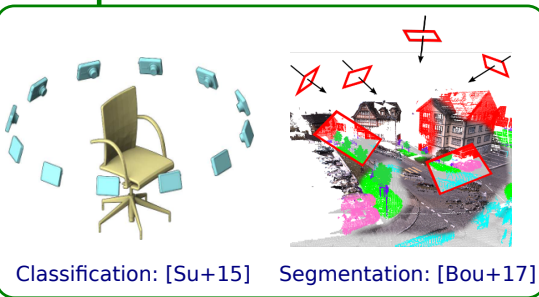
**Difficulties :** Voxel sizes ? Voxel orientation ?



**Space  
adaptation**

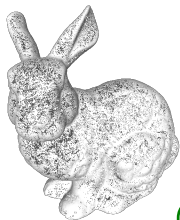
**Machine learning  
Representation and decision**

Rabbit



[Su+15] Su et al, Multi-view convolutional neural networks for 3D shape recognition, ICCV, 2015

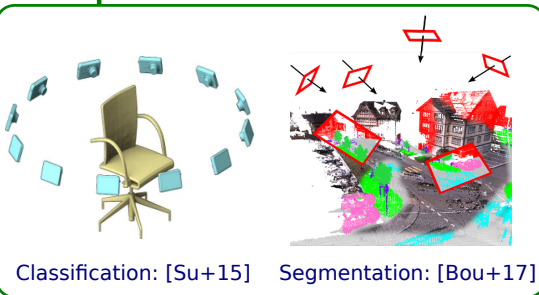
[Bou+17] Boulch et al, SnapNet : 3D point cloud semantic labeling with 2D deep segmentation networks, Computer & Graphics, 2017



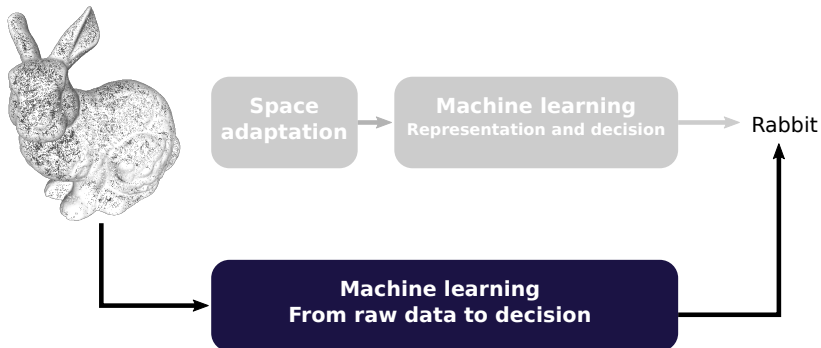
**Space  
adaptation**

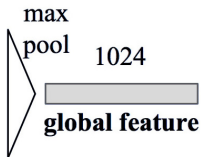
**Machine learning**  
Representation and decision

Rabbit



**Difficulties** : Snapshot strategies ?

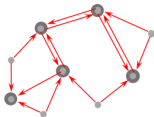




PointNet : Qi et al [Qi+17a]

Permutation inv. : Max pooling.

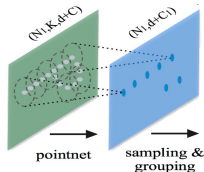
Use location as features.



PointCNN : Li et al [Li+18]

Input projection on kernel.

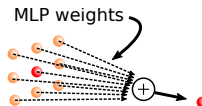
Use location as features.



PointNet++ : Qi et al [Qi+17b]

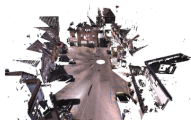
Hierarchical representation.

Use location as features.



PCCN : Wang et al [Wan+18a]

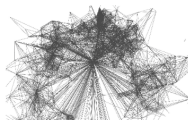
Feature weighting using MLP



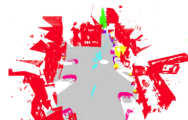
(a) RGB point cloud



(b) Geometric partition



(c) Superpoint graph



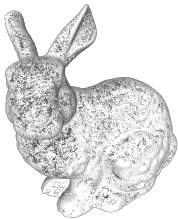
(d) Semantic segmentation

- Offline segmentation
- Network : PointNet on each primitive + GRU for message passing

[LS18] Landrieu et al., Large-scale point cloud semantic segmentation with superpoint graphs, CVPR, 2018

# Generalizing convolutions

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**Machine learning**  
**From raw data to decision**

→ Rabbit

CNNs have proved very efficient for image / voxel processing

## Objective

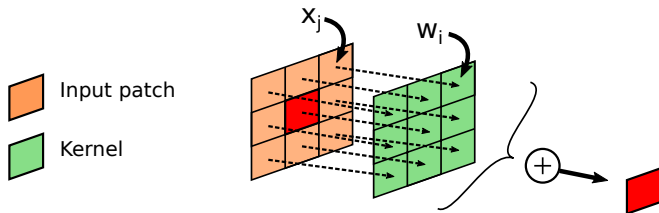
- Adapt convolutions to sparse, unstructured data
- Stick as much as possible to the original formulation



## Formulation for images

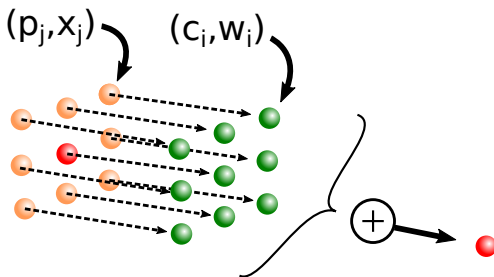
$$y = \beta + \sum_{i=1}^N \mathbf{w}_i \mathbf{x}_i = \beta + \sum_{i=1}^N \sum_{j=1}^{|X|} \mathbf{w}_i \mathbf{x}_j \mathbf{1}(i, j)$$

with  $X$  the input patch and  $\mathbf{1}(i, j)$  the indicator function.

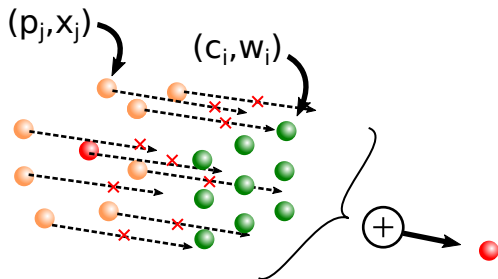


## Formulation with points

$$y = \beta + \frac{1}{|X|} \sum_{j=1}^{|X|} \sum_{i=1}^N \mathbf{w}_i \mathbf{x}_j \mathbf{1}(\mathbf{c}_i, \mathbf{p}_j)$$



Valid for structured inputs.



Unstructured inputs would lead to zero value almost all the time.

*Indicator function* is not the right function for unstructured inputs.

$$y = \beta + \frac{1}{|X|} \sum_{j=1}^{|X|} \sum_{i=1}^N \mathbf{w}_i \mathbf{x}_j \phi_i(p_j, C)$$

- Interpolation to neighbors

Somehow suppose a grid for the kernel.

Hang SU et al. "SPLATNet : Sparse Lattice Networks for Point Cloud Processing". In : *arXiv preprint arXiv :1802.08275* (2018)

$$y = \beta + \frac{1}{|X|} \sum_{j=1}^{|X|} \sum_{i=1}^N \mathbf{w}_i \mathbf{x}_j \phi_i(p_j, C)$$

$\phi$  construction :

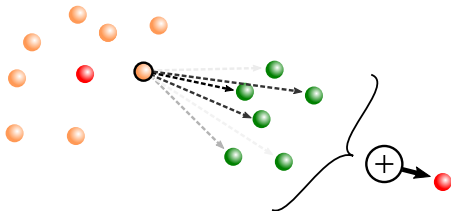
- decrease with the a distance
- deal with relative positions of kernel elements

Inverse  $\ell_2$  distance ? Gaussian functions ? ...

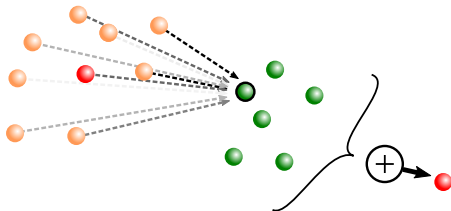
**How to tune parameters ?**

Use a MLP for  $\phi$  function [Li+18; Wan+18a] :

$$y = \beta + \frac{1}{|X|} \sum_{j=1}^{|X|} \sum_{i=1}^N \mathbf{w}_i \mathbf{x}_j \text{MLP}_i(p_j - C)$$



Each input influences  
each kernel elements



Each kernel element sees  
the whole input

Use a MLP for  $\phi$  function [Li+18; Wan+18a] :

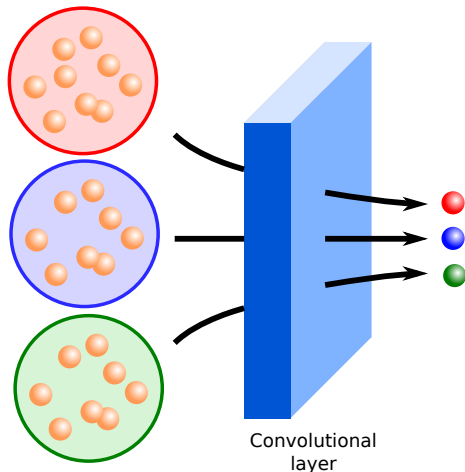
$$y = \beta + \frac{1}{|X|} \sum_{j=1}^{|X|} \sum_{i=1}^N \mathbf{w}_i \mathbf{x}_j \text{MLP}_i(p_j - C)$$

## Properties

- **Permutation invariance** :  $\phi$  function of  $p_j$  and  $C$
- **Translation invariance** :  $C$  centered on the neighborhood
- **Low sensibility to input size** : normalized by  $|X|$
- **Low sensibility to input scale** :  $X$  normalized to unit ball

Input point sets

Output points



## Input

Point sets  
(neighborhoods) :  
locations + features

## Output

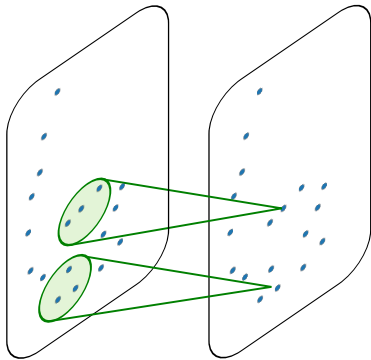
Features at given  
output locations (center  
of neighborhoods)



One neighborhood for each point of the input cloud.

**Images :**

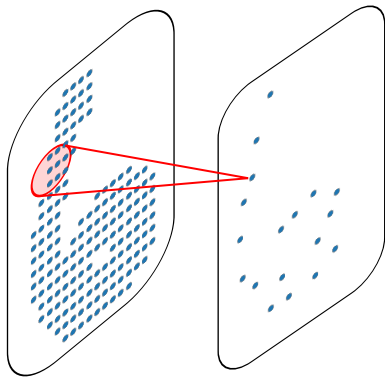
Convolution with stride 1.



Number of neighborhoods lower  
than input cloud size.

## Images :

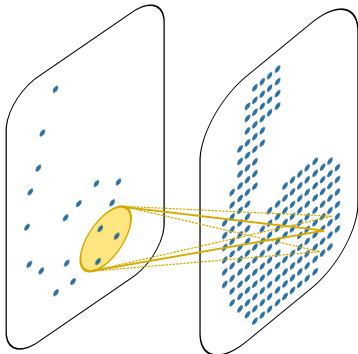
Convolution with stride  $\geq 2$ .



Output point cloud size greater than input cloud size.

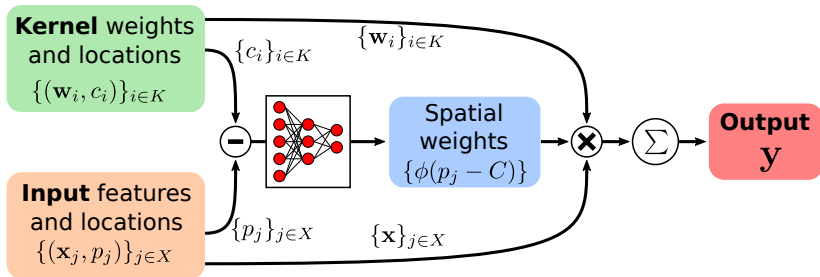
**Images :**

Convolution transpose.



# Implementation

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## Python

## implementation

Only differentiable operations  
Autograd usage (PyTorch or Tensorflow)

```
# Neighborhoods
features = input.view(-1, input.size(2))[indices]
pts = points.view(-1, points.size(2))[indices]

# Relative positions
pts = pts - next_points.unsqueeze(2)

# Normalization
if normalize:
    maxi = torch.sqrt((pts**2).sum(3).max(2)[0])
    maxi[maxi==0] = 1
    pts = pts / maxi.view(maxi.size()+(1,1))

# weighting MLP
dists = pts.view(pts.size()+(1,)) - centers
dists = dists.view(dists.size(0), dists.size(1),
                  dists.size(2), -1)
dists = F.relu(l1(dists))
dists = F.relu(l2(dists))
dists = F.relu(l3(dists))
dists = dists.unsqueeze(3)

# Features
features = features.view(features.size()+(1,)) * dists
features = features.mean(2)
features = features.view(features.size()+(1,)) * weight
features = features.sum([2,3])

# Bias
features = features + bias
```

Computed using search trees  
from Scikit-learn.

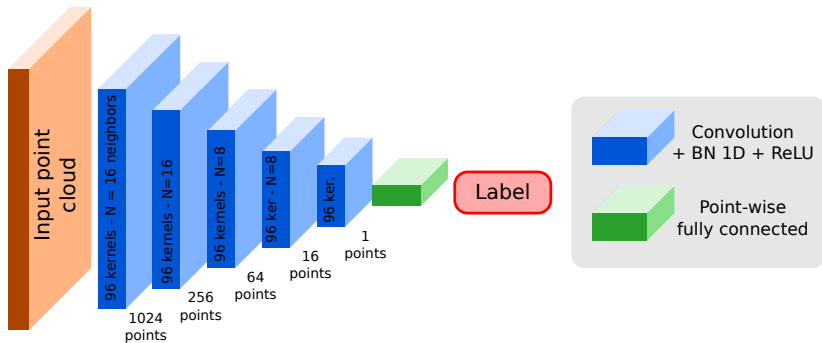
**Precomputation** for efficiency,  
all neighborhoods are computed  
in the data loader.



# Experiments

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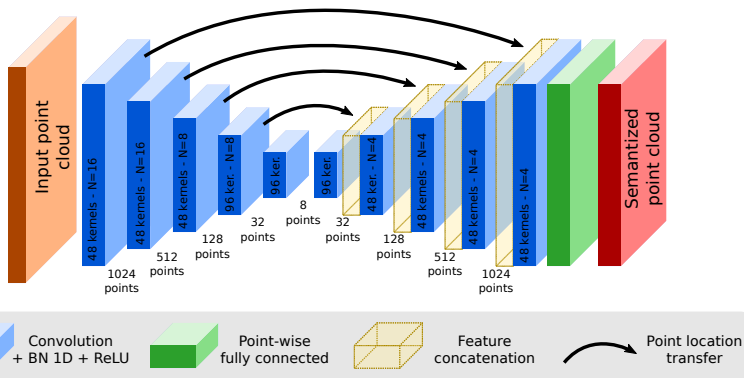


*MNIST dataset*

Methods	OA
NiN [LCY13]	99.53
PointNet++ [Qi+17b]	99.49
PointCNN [Li+18]	99.54
<i>Ours</i>	
16 samplings	<b>99.61</b>

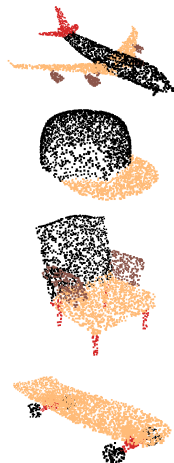
*ModelNet40 dataset*

Methods	OA	AA
DGCNN [Wan+18c]	92.2	<b>90.2</b>
PointNet++ [Qi+17b]	90.7	
PointCNN	<b>92.2</b>	88.1
<i>Ours</i>		
16 samplings	91.6	88.1



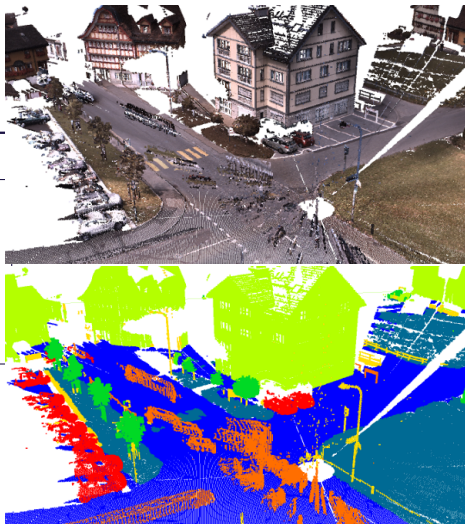
*Shapenet dataset*

Method	pIoU	mIoU
SPLATNet [Su+18]	85.4	83.7
DGCNN [Wan+18c]	85.1	82.3
PointNet [Qi+17a]	83.7	80.4
PointNet++ [Qi+17b]	85.1	81.9
SGPN [Wan+18b]	85.8	82.8
PointCNN [Li+18]	86.14	<b>84.6</b>
<i>Ours 1024 pts</i>		
16 trees	<b>93.1</b>	82.6

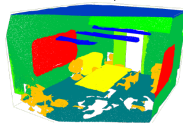
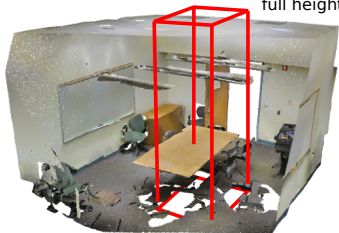


*Semantic8 dataset*

Method	AvIoU	OA
TML-PC [MZ+14]	0.391	0.745
TMLC-MS [HWS16]	0.494	0.850
PointNet++ [Qi+17b]	0.631	0.857
SnapNet [Bou+17]	0.674	0.910
SPGraph [LS18]	<b>0.762</b>	<b>0.929</b>
Ours	0.666	0.898
<i>ranking</i>	3	3



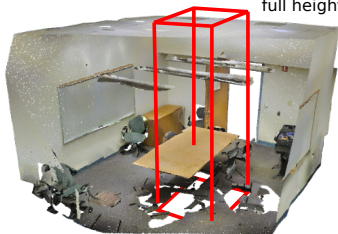
**Box:**  
2 meter based  
full height



*S3DIS dataset*

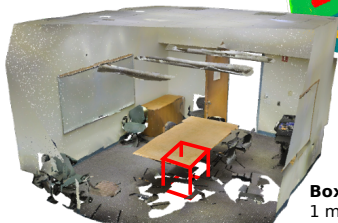
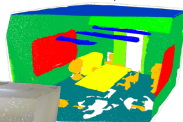
Method	OA	mAcc	mIoU
PointNet [Qi+17a]	78.5	66.2	47.6
SPGraph [LS18]	85.5	73.0	62.1
RSNet [HWN18]	-	66.45	56.47
PCCN [Wan+18a]	-	67.01	58.27
PointCNN [Li+18]	<b>88.14</b>	<b>75.61</b>	<b>65.39</b>
<i>Ours</i>			
1 scale 2m	84.05	-	55.36

**Box:**  
2 meter based  
full height

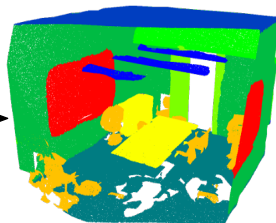


*S3DIS dataset*

Method	OA	mAcc	mIoU
PointNet [Qi+17a]	78.5	66.2	47.6
SPGraph [LS18]	85.5	73.0	62.1
RSNet [HWN18]	-	66.45	56.47
PCCN [Wan+18a]	-	67.01	58.27
PointCNN [Li+18]	<b>88.14</b>	<b>75.61</b>	<b>65.39</b>
<i>Ours</i>			
1 scale 2m	84.05	-	55.36
2 scales 2m,1m	84.93	-	58.54



**Box:**  
1 meter side



## Perspectives and conclusions

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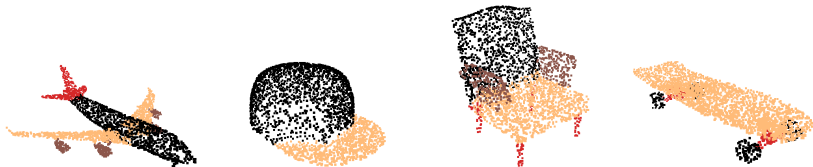


- Work on architecture design
- Training strategy : multiscale, layer initialization ...
- Extend layers

- Competitive results
- A single architecture on all datasets
- Trained on a 12G NVidia Titan GPU

## Code available

<https://github.com/aboulch/ConvPoint>



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