

Show all your work. Late Homework will not be accepted without prior approval.

1. Continuing Hw3 Q2 in which balls are selected one at a time with replacement from a box containing 4 red and 6 white balls.
 - (a) If the third ball is red, what is the probability the first ball was red?
 - (b) If the third ball is red, what is the probability the first two balls were red?
2. Redo Q1 if the balls are selected without replacement.
3. One of a die and a coin (sides 0 and 1) is selected at random and tossed.
 - (a) If the outcome is 0, what is the probability the coin was chosen?
 - (b) If the outcome is 1, what is the probability the coin was chosen?
4. An HIV test is known to be 98% accurate (i.e. the probability of a correct diagnosis is 0.98) and 0.5% of the population is known to be HIV positive.
 - (a) What is the probability that a random person will test positive?
 - (b) If a person selected at random does test positive, what is the probability that he is infected?

Bonus. A gambler has three coins in his pocket, one is normal, one is head-head and the third is tail-tail. He picks one at random and tosses it and it shows heads. The gambler says that since you now know the coin is either head-head or head-tail the odds that the other side is tails is $1/2$. Is this true?