

STAT5002 Lab10 Question Sheet

Introduction to Statistics

STAT5002

Two-sample T-tests

The Marrickville Golf Club has been collecting weather data (on and off) since 1904. Daily rainfall data may be downloaded by selecting the link “All years of data” from this page within the Bureau of Meteorology website (note: the actual URL of the “All years of data” link seems to change from day to day).

1 Data processing

In the first part of this lab, we demonstrate some basic data processing steps using the file `IDCJAC0009_066036_1800_Data.csv`. This section is intended solely to illustrate how to prepare the original dataset, so that you can use the processed data to generate additional examples for your own practice. **The questions begin on Page 6. The variables involved are loaded in the accompanying R markdown worksheet.**

```
mgc = read.csv("IDCJAC0009_066036_1800_Data.csv")
str(mgc)
```

```
'data.frame': 43980 obs. of 8 variables:
 $ Product.code           : chr  "IDCJAC0009" "IDCJAC0009" "IDCJAC0009"
 $ Bureau.of.Meteorology.station.number : int  66036 66036 66036 66036 66036 66036 66036 66036 66036 66036
 $ Year                   : int  1904 1904 1904 1904 1904 1904 1904 1904 1904 1904
 $ Month                  : int  1 1 1 1 1 1 1 1 1 1 ...
 $ Day                    : int  1 2 3 4 5 6 7 8 9 10 ...
 $ Rainfall.amount..millimetres. : num  NA NA NA NA NA NA NA NA NA NA ...
 $ Period.over.which.rainfall.was.measured..days.: int  NA NA NA NA NA NA NA NA NA NA ...
 $ Quality                 : chr  "" "" "" "" ...
```

The code below determines monthly totals of rainfall (note that `na.rm=T` ignores NAs, treating them as zero); rows are years, columns are months:

```
rf = mgc$Rainfall.amount..millimetres.
monthly.rf = tapply(rf, list(mgc$Year, mgc$Month), sum, na.rm = T)
monthly.rf
```

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1904 | 0.0 | 0.0 | 0.0 | 0.0 | 87.3 | 0.5 | 303.1 | 37.3 | 26.7 | 38.6 | 0.0 | 25.4 |
| 1905 | 42.0 | 68.1 | 227.2 | 151.1 | 162.3 | 52.6 | 9.1 | 7.6 | 35.5 | 46.3 | 6.4 | 77.9 |
| 1906 | 46.1 | 7.0 | 134.5 | 8.9 | 115.3 | 28.0 | 3.8 | 121.7 | 35.2 | 41.2 | 93.4 | 59.7 |
| 1907 | 67.9 | 84.5 | 192.6 | 29.7 | 31.8 | 195.5 | 4.5 | 6.3 | 5.1 | 7.2 | 26.6 | 50.7 |
| 1908 | 25.8 | 191.5 | 31.0 | 55.0 | 46.4 | 10.6 | 212.7 | 219.3 | 53.0 | 17.0 | 2.0 | 15.2 |
| 1909 | 17.8 | 148.0 | 19.1 | 30.5 | 20.6 | 110.0 | 15.1 | 29.6 | 104.0 | 35.8 | 72.8 | 91.5 |
| 1910 | 135.2 | 16.6 | 156.4 | 73.2 | 107.5 | 61.9 | 224.8 | 5.6 | 48.2 | 53.3 | 19.1 | 149.9 |
| 1911 | 348.0 | 121.3 | 55.9 | 61.0 | 38.1 | 2.5 | 163.8 | 164.4 | 46.2 | 19.5 | 39.3 | 53.4 |
| 1912 | 27.9 | 158.6 | 112.1 | 139.7 | 80.1 | 43.2 | 218.3 | 54.6 | 14.0 | 21.1 | 74.6 | 44.1 |
| 1913 | 13.8 | 34.3 | 257.1 | 173.1 | 411.2 | 0.0 | 199.7 | 0.0 | 42.6 | 34.3 | 10.9 | 8.9 |
| 1914 | 14.4 | 25.0 | 203.7 | 40.1 | 96.8 | 131.1 | 220.8 | 54.4 | 97.1 | 148.9 | 76.1 | 157.6 |
| 1915 | 23.4 | 26.8 | 92.2 | 222.6 | 96.8 | 26.2 | 122.0 | 26.7 | 28.6 | 16.7 | 0.0 | 63.8 |
| 1916 | 21.8 | 54.3 | 52.6 | 120.1 | 38.4 | 42.4 | 70.6 | 97.0 | 123.5 | 312.4 | 69.7 | 78.9 |
| 1917 | 56.5 | 169.9 | 8.7 | 319.0 | 82.8 | 131.8 | 9.0 | 39.6 | 101.4 | 97.7 | 186.4 | 40.6 |
| 1918 | 229.5 | 90.8 | 29.0 | 161.9 | 7.4 | 3.9 | 211.0 | 46.9 | 69.9 | 19.2 | 20.7 | 11.4 |
| 1919 | 28.9 | 96.1 | 84.8 | 57.4 | 416.7 | 32.4 | 31.7 | 4.6 | 79.8 | 46.6 | 80.1 | 63.6 |
| 1920 | 137.5 | 32.3 | 27.7 | 59.3 | 5.1 | 57.4 | 125.9 | 24.7 | 29.4 | 24.3 | 42.2 | 341.0 |
| 1921 | 67.4 | 23.9 | 75.6 | 154.3 | 145.6 | 17.1 | 152.0 | 24.4 | 84.1 | 55.4 | 73.3 | 145.0 |
| 1922 | 133.5 | 75.1 | 41.4 | 29.2 | 89.0 | 25.0 | 243.1 | 41.0 | 99.5 | 49.3 | 14.6 | 40.7 |
| 1923 | 51.6 | 13.8 | 20.0 | 150.7 | 26.7 | 101.2 | 174.2 | 139.4 | 42.5 | 33.2 | 26.7 | 41.4 |
| 1924 | 111.9 | 58.5 | 95.8 | 134.3 | 49.3 | 48.2 | 38.4 | 57.1 | 74.9 | 25.9 | 79.6 | 67.4 |
| 1925 | 70.7 | 41.3 | 44.1 | 29.4 | 430.8 | 154.0 | 4.1 | 86.4 | 18.0 | 16.3 | 99.7 | 16.0 |
| 1926 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1927 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1928 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1929 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1930 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1931 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1932 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1933 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1934 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1935 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1936 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1937 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

| | | | | | | | | | | | | |
|------|-------|-------|-------|-------|------|-------|------|-------|-------|------|-------|------|
| 1938 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1939 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1940 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1941 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1942 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1943 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1944 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1945 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1946 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1947 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1948 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 58.8 |
| 1949 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1950 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1951 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1952 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1953 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1954 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1955 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1956 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1957 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1958 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1959 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1960 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1961 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1962 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1963 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1964 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1965 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1966 | 18.8 | 113.9 | 203.3 | 183.7 | 50.1 | 113.3 | 11.4 | 67.6 | 50.6 | 38.0 | 140.2 | 68.2 |
| 1967 | 153.1 | 164.4 | 101.8 | 46.8 | 31.0 | 214.0 | 20.8 | 211.9 | 68.3 | 55.4 | 78.6 | 18.8 |
| 1968 | 109.5 | 15.0 | 86.1 | 11.2 | 85.8 | 20.3 | 47.8 | 22.2 | 3.1 | 4.2 | 17.5 | 76.1 |
| 1969 | 51.7 | 195.6 | 104.0 | 169.7 | 44.2 | 149.3 | 29.8 | 155.4 | 45.0 | 49.0 | 255.5 | 37.4 |
| 1970 | 94.1 | 60.4 | 140.1 | 58.7 | 15.2 | 27.2 | 0.0 | 31.9 | 132.9 | 18.1 | 0.0 | 0.0 |
| 1971 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1972 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1973 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1974 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1975 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1976 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1977 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1978 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1979 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1980 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

| | | | | | | | | | | | | |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1981 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1982 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1983 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1984 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1985 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1986 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1987 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1988 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1989 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1990 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1991 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1992 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1993 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1994 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1995 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1996 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1997 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1998 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1999 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 2000 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 2001 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 39.0 | 57.0 | 29.0 | 74.0 | 18.0 |
| 2002 | 67.0 | 313.0 | 33.0 | 26.0 | 75.0 | 18.0 | 9.0 | 13.0 | 20.0 | 19.0 | 19.0 | 88.0 |
| 2003 | 5.0 | 53.0 | 70.0 | 242.0 | 335.0 | 57.0 | 42.0 | 34.0 | 8.0 | 61.0 | 81.0 | 52.0 |
| 2004 | 51.0 | 43.0 | 4.0 | 2.0 | 8.0 | 27.0 | 28.0 | 86.0 | 54.0 | 200.0 | 42.0 | 71.0 |
| 2005 | 60.0 | 95.0 | 45.0 | 17.0 | 29.0 | 64.0 | 61.0 | 0.0 | 40.0 | 56.0 | 92.0 | 37.0 |
| 2006 | 61.0 | 33.0 | 29.0 | 2.0 | 20.0 | 157.0 | 98.0 | 68.0 | 147.0 | 8.0 | 22.0 | 13.0 |
| 2007 | 10.0 | 105.0 | 49.0 | 113.0 | 12.0 | 333.0 | 31.0 | 99.0 | 48.0 | 33.0 | 122.0 | 77.0 |
| 2008 | 53.0 | 325.0 | 64.0 | 155.0 | 4.0 | 109.0 | 55.0 | 34.0 | 73.0 | 44.0 | 44.0 | 73.0 |
| 2009 | 18.0 | 125.0 | 17.0 | 50.0 | 115.0 | 75.0 | 48.0 | 4.0 | 17.0 | 158.0 | 24.0 | 54.0 |
| 2010 | 24.0 | 164.0 | 50.0 | 32.0 | 149.0 | 93.0 | 30.0 | 18.0 | 46.0 | 79.0 | 165.0 | 75.0 |
| 2011 | 29.0 | 16.0 | 153.0 | 216.0 | 112.0 | 63.0 | 264.0 | 38.0 | 71.0 | 32.0 | 169.0 | 154.0 |
| 2012 | 112.0 | 140.0 | 221.0 | 163.0 | 23.0 | 211.0 | 52.0 | 8.0 | 20.0 | 24.0 | 48.0 | 38.0 |
| 2013 | 133.0 | 169.0 | 71.0 | 109.0 | 2.0 | 308.0 | 30.0 | 14.0 | 47.0 | 18.0 | 183.0 | 31.0 |
| 2014 | 7.0 | 41.0 | 117.0 | 61.0 | 9.0 | 84.0 | 12.0 | 243.0 | 48.0 | 131.0 | 18.0 | 161.0 |
| 2015 | 159.0 | 101.0 | 49.0 | 413.0 | 102.0 | 90.0 | 54.0 | 60.0 | 56.0 | 31.0 | 81.0 | 69.0 |
| 2016 | 251.0 | 29.0 | 117.0 | 86.0 | 13.0 | 300.0 | 108.0 | 82.0 | 0.0 | 27.0 | 34.0 | 66.0 |
| 2017 | 48.0 | 177.0 | 267.0 | 71.0 | 19.0 | 116.0 | 11.0 | 21.0 | 0.0 | 59.0 | 40.0 | 52.0 |
| 2018 | 25.0 | 116.0 | 77.0 | 15.0 | 14.0 | 146.0 | 8.0 | 6.0 | 80.0 | 181.0 | 110.0 | 93.0 |
| 2019 | 69.0 | 88.0 | 170.0 | 16.0 | 9.0 | 146.0 | 43.0 | 53.0 | 103.0 | 27.0 | 25.0 | 1.0 |
| 2020 | 66.0 | 435.0 | 138.0 | 25.0 | 99.0 | 82.0 | 140.0 | 60.0 | 6.0 | 4.0 | 45.0 | 89.0 |
| 2021 | 71.0 | 108.0 | 407.0 | 27.0 | 99.0 | 70.0 | 32.0 | 80.0 | 52.0 | 61.0 | 160.0 | 91.0 |
| 2022 | 91.0 | 394.0 | 626.0 | 221.0 | 178.0 | 4.0 | 348.0 | 42.0 | 79.0 | 173.0 | 43.0 | 42.0 |
| 2023 | 157.0 | 191.0 | 61.0 | 131.0 | 36.0 | 15.0 | 38.0 | 49.0 | 0.0 | 23.0 | 143.0 | 81.0 |

| | | | | | | | | | | | | |
|------|------|-------|------|-------|-------|----|----|----|----|----|----|----|
| 2024 | 76.0 | 180.0 | 51.0 | 249.0 | 163.0 | NA | NA | NA | NA | NA | NA | NA |
|------|------|-------|------|-------|-------|----|----|----|----|----|----|----|

As can be seen, the rainfall was only recorded May 1904 – Dec 1925, then Jan 1966 – Oct 1970, then Aug 2001 to the present. Let us extract the rainfall for the month of May in the two periods 1904-1925 and 2002-2024:

```
yrs = as.numeric(rownames(monthly.rf))
yrs
```

```
[1] 1904 1905 1906 1907 1908 1909 1910 1911 1912 1913 1914 1915 1916 1917 1918
[16] 1919 1920 1921 1922 1923 1924 1925 1926 1927 1928 1929 1930 1931 1932 1933
[31] 1934 1935 1936 1937 1938 1939 1940 1941 1942 1943 1944 1945 1946 1947 1948
[46] 1949 1950 1951 1952 1953 1954 1955 1956 1957 1958 1959 1960 1961 1962 1963
[61] 1964 1965 1966 1967 1968 1969 1970 1971 1972 1973 1974 1975 1976 1977 1978
[76] 1979 1980 1981 1982 1983 1984 1985 1986 1987 1988 1989 1990 1991 1992 1993
[91] 1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006 2007 2008
[106] 2009 2010 2011 2012 2013 2014 2015 2016 2017 2018 2019 2020 2021 2022 2023
[121] 2024
```

```
yr.19 = (yrs < 1926)
yr.20 = (yrs > 2001)
may.19 = monthly.rf[yr.19, 5]
may.19
```

| | | | | | | | | | | | | |
|------|-------|-------|------|-------|------|-------|------|-------|-------|------|------|------|
| 1904 | 1905 | 1906 | 1907 | 1908 | 1909 | 1910 | 1911 | 1912 | 1913 | 1914 | 1915 | 1916 |
| 87.3 | 162.3 | 115.3 | 31.8 | 46.4 | 20.6 | 107.5 | 38.1 | 80.1 | 411.2 | 96.8 | 96.8 | 38.4 |
| 1917 | 1918 | 1919 | 1920 | 1921 | 1922 | 1923 | 1924 | 1925 | | | | |
| 82.8 | 7.4 | 416.7 | 5.1 | 145.6 | 89.0 | 26.7 | 49.3 | 430.8 | | | | |

```
may.20 = monthly.rf[yr.20, 5]
may.20
```

| | | | | | | | | | | | | | | | |
|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 |
| 75 | 335 | 8 | 29 | 20 | 12 | 4 | 115 | 149 | 112 | 23 | 2 | 9 | 102 | 13 | 19 |
| 2018 | 2019 | 2020 | 2021 | 2022 | 2023 | 2024 | | | | | | | | | |
| 14 | 9 | 99 | 99 | 178 | 36 | 163 | | | | | | | | | |

We will use `may.19` and `may.20` in the rest of sections to investigate if the differences in mean rainfall significant. To address this question we assume that

- the 1904-1925 May rainfall totals are like a random sample X_1, \dots, X_{22} taken with replacement from a box with mean μ_X ;
- the 2002-2024 May rainfall totals are like a random sample Y_1, \dots, Y_{23} taken with replacement from a box with mean μ_X ;
- both samples are taken independently of each other.

2 Classical two-sample T-test

2.1 Hypotheses

Formally state the hypotheses being considered here. (Hint: is this a one-sided or two-sided test?)

2.2 Checking assumptions

State the additional assumptions underlying the use of the Classical two-sample T-test, and check the assumptions using graphical summaries.

2.3 Pooled estimates

First determine the sample sizes, sample means, and sample SDs for `may.19` and `may.20`. Then determine the pooled estimated standard deviation and the standard error of the difference.

2.4 Test statistic

Determine the test distribution and the observed value of T-statistic.

2.5 P-value and conclusion

Is the apparent mean difference significantly different from zero at the 5% significance level?

2.6 Critical region of rejection

What is the critical region of rejection for a 5% significance level?

3 Welch test

3.1 Assumption

This test relaxes one of the assumptions of the Classical two-sample T-test. Which one exactly?

3.2 Standard error

This test uses a different estimate of the standard error of the mean difference, compared to the Classical two-sample T-test. Determine the value of this estimated standard error.

3.3 T-test

Use the built-in R function `t.test()` to perform Welch's test with the 10% significance level. Note that you can set this by choosing the confidence level `conf.level = 0.90`. What is the P-value? how does it compare with the classical two-sample T-test?

4 Simulation-based two-sample T-test

4.1 Simulate test statistics

- Use a bootstrap simulation to simulate 10,000 samples of the Welch statistic, plot the histogram of the test statistics, and compare with the Student's T distribution with d.o.f. 34.859 (which is the one used in Welch's test).
- Note that we need to define two surrogate boxes `box.19 = may.19 - mean(may.19)` and `box.20 = may.20 - mean(may.20)`. Why are the means subtracted off?
- You can write your code in the accompanying R markdown worksheet.

4.2 P-value

We use the simulated values of the Welch statistic to approximate the distribution of the test statistic when the null hypothesis is true. What is a simulation-based P-value? You can use an observed Welch statistic 1.4473 here (obtained by `t.test()`).