



**Tecnológico
de Monterrey**

Control engineering

PhD. Enrique Aguayo

Third
Simulation Project

José Abraham Pérez Martínez
A01633926

System1

Lead Compensator

$G1 = \frac{17}{26s + 9}$

Continuous-time transfer function.

$C1Lead = \frac{11.912 (s+2)}{(s+5)}$

Continuous-time zero/pole/gain model.

System 1 Lead Compensator

$$G(s) = \frac{17}{26s + 9}$$

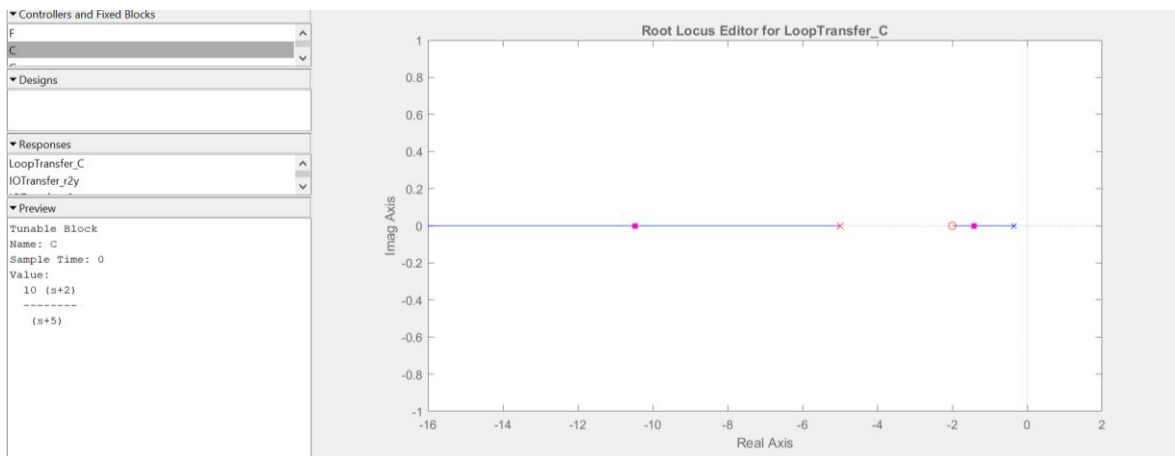
$$C(s) = \frac{10(s+2)}{s+5}$$

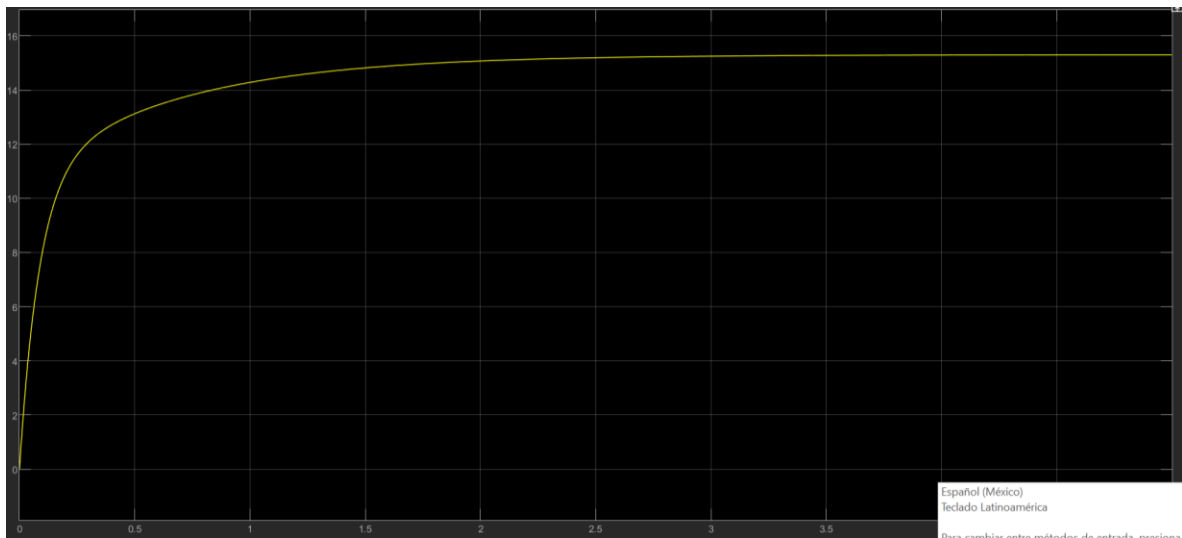
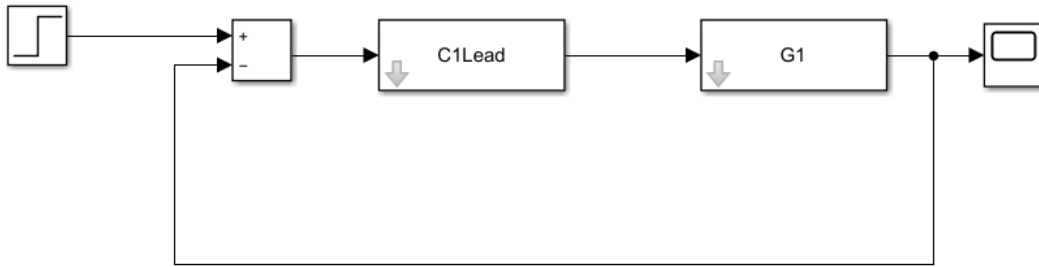
$$K_p G = \frac{17}{9}$$

$$ess = \frac{1}{1 + \frac{17}{9} \cdot \frac{2K}{5}} = .1$$

$$K = 11.9118$$

$$zpk = ([-2] [-5] 11.9118)$$





Lag Compensator

C1Lag =

$$\frac{26 (s+2) (s+0.9672)}{(s+5) (s+1)}$$

Continuous-time zero/pole/gain model.

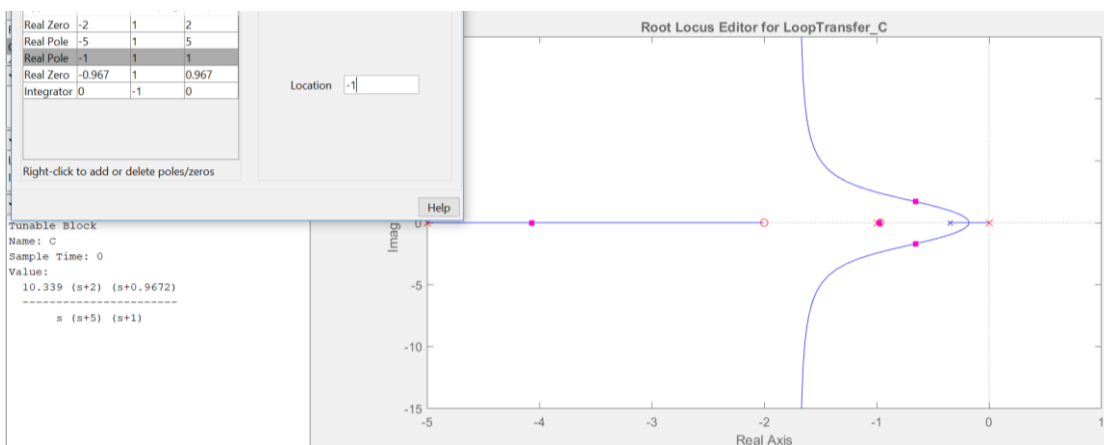
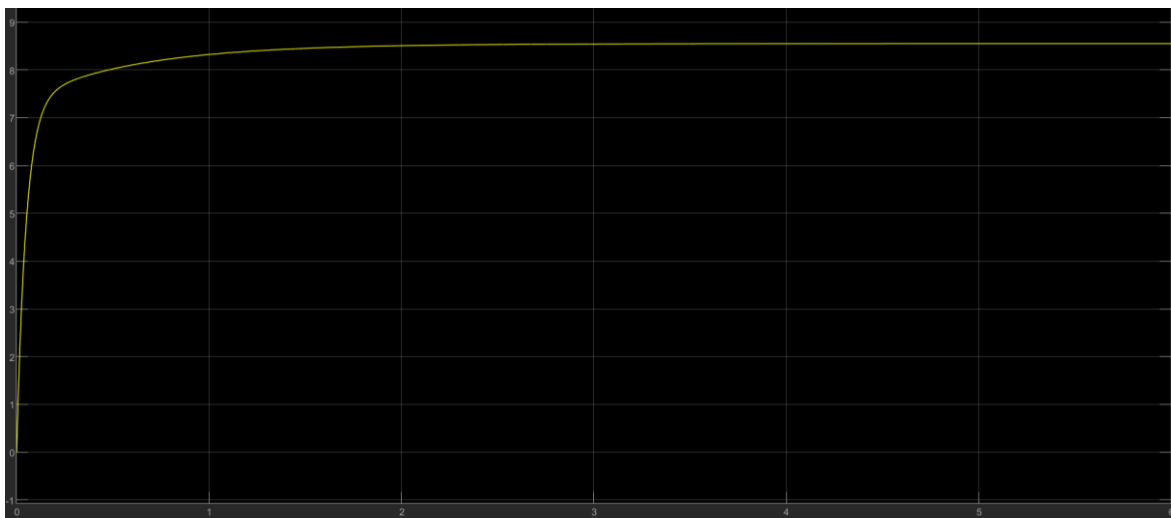
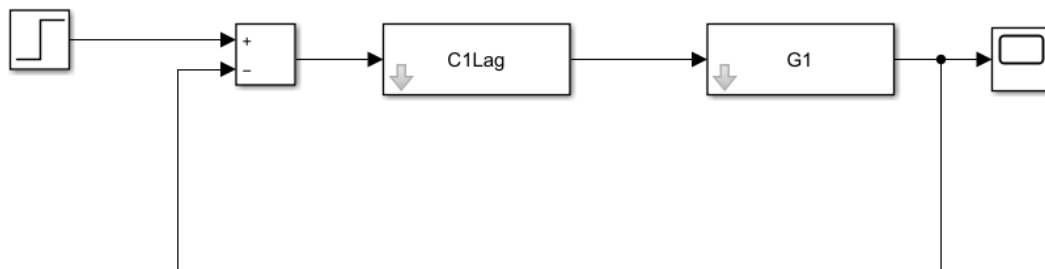
Lag Compensator

$$C(s) = \frac{26 (s+2) (s+0.9672)}{(s+5) (s+1)}$$

$$K_p G = \frac{17}{9} \quad \text{ess} = \frac{1}{1 + \frac{17}{9} \cdot \frac{52}{5} K} = .05$$

$$K = .967195$$

$$C(s) = \frac{26 (s+2) (s+0.967195)}{(s+5) (s+1)}$$



System 2

Lead Compensator

G2 =

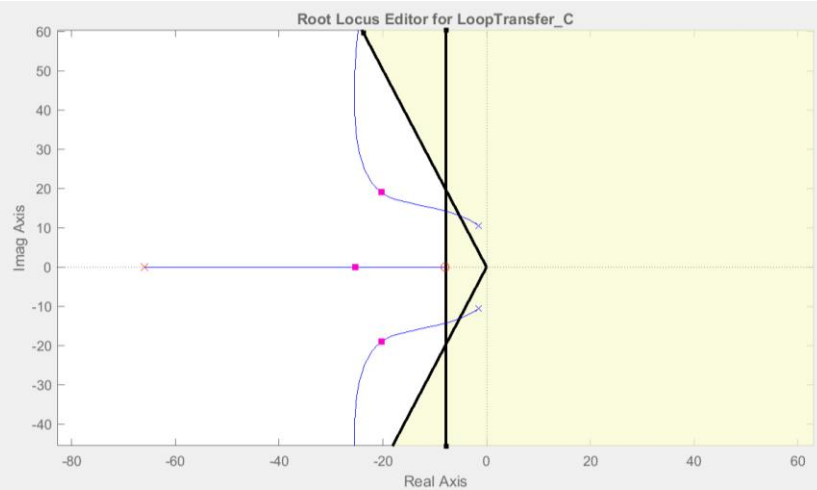
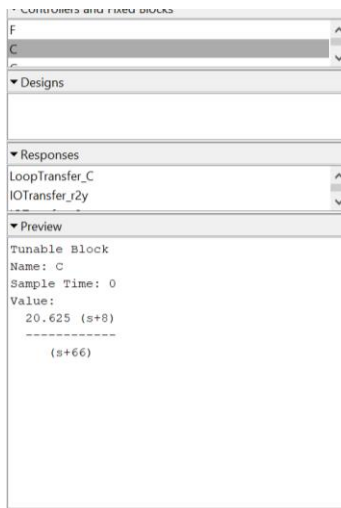
$$\frac{-0.884 s + 442}{6 s^2 + 17.58 s + 676}$$

Continuous-time transfer function.

C2Lead =

$$\frac{113.56 (s+8)}{(s+66)}$$

Continuous-time zero/pole/gain model.



System 2
Lead Compensator

$$G(s) = \frac{-0.884s + 442}{6s^2 + 17.58s + 676}$$

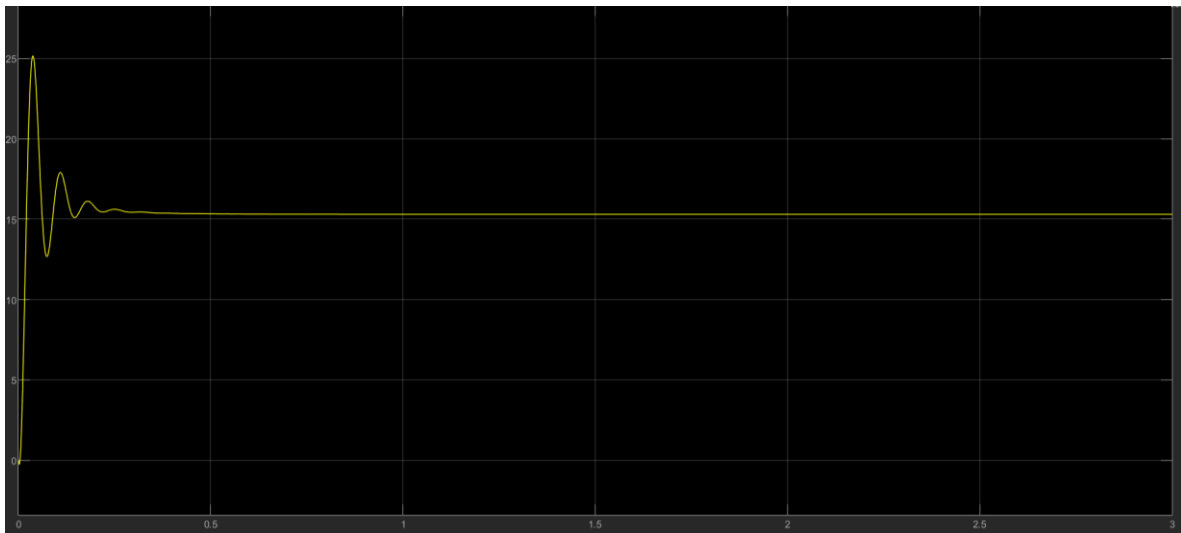
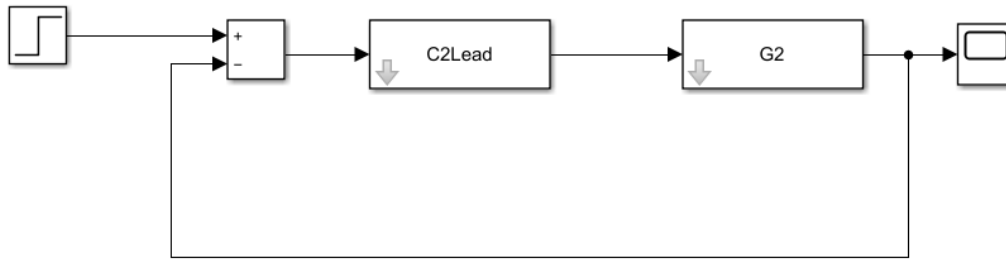
$$K_p G = \frac{446}{676} \quad G_8 = 0.34$$

$$C(s) = \frac{20.625 (s+8)}{(s+66)} \quad K_p C = 2.5 \quad 8 = 0.37 \text{ propose}$$

$$\frac{1}{1 + \left(\frac{446}{676}\right)\left(\frac{8}{66}\right)} = 0.1 \quad K = 113.559$$

$$\text{zpk} = (-8, -66, 113.559)$$

$\zeta_{ss} = 0.5$



Lag Compensator

C2Lag =

$$\frac{26 (s+8) (s+9.221)}{(s+66) (s+1)}$$

Continuous-time zero/pole/gain model.

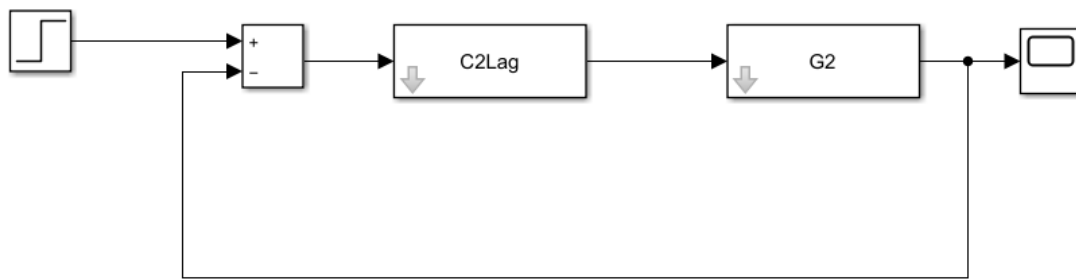
Lag Compensator

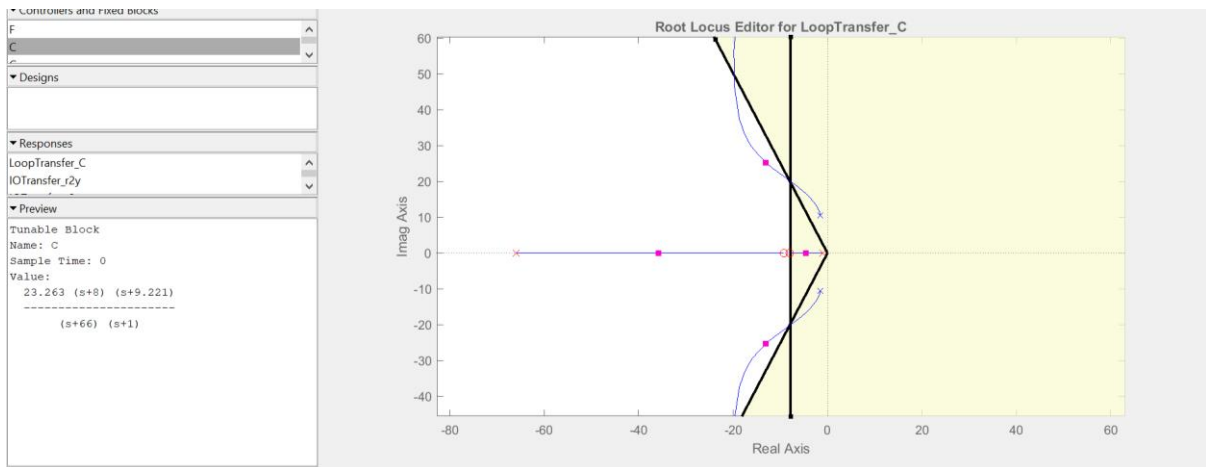
Maximum input = 26

$$K_p G = \frac{446}{676} \quad C(s) = \frac{26(s+8)(s+a_2)}{(s+66)(s+b_2)}$$

$$ess = \frac{1}{1 + \frac{446}{676} \cdot \frac{208K}{66}} = .05 \quad K = 9.22059$$

$$C(s) = \frac{26(s+8)(s+9.22059)}{(s+66)(s+1)}$$





System3

Lead Compensator

G3 =

$$\frac{-0.204 s + 68}{s^2 + 27 s + 162}$$

Continuous-time transfer function.

C3Lead =

$$\frac{54.794 (s+9)}{(s+23)}$$

Continuous-time zero/pole/gain model.

System 3
Lead Compensator

$$G(s) = \frac{-0.204s + 68}{s^2 + 27s + 162}$$

$$K_p G = \frac{68}{162}$$

$$G_8 = 1.06066$$

$$\gamma_{\text{proposed}} = 1.1$$

$$\zeta_{ss} = 0.5$$

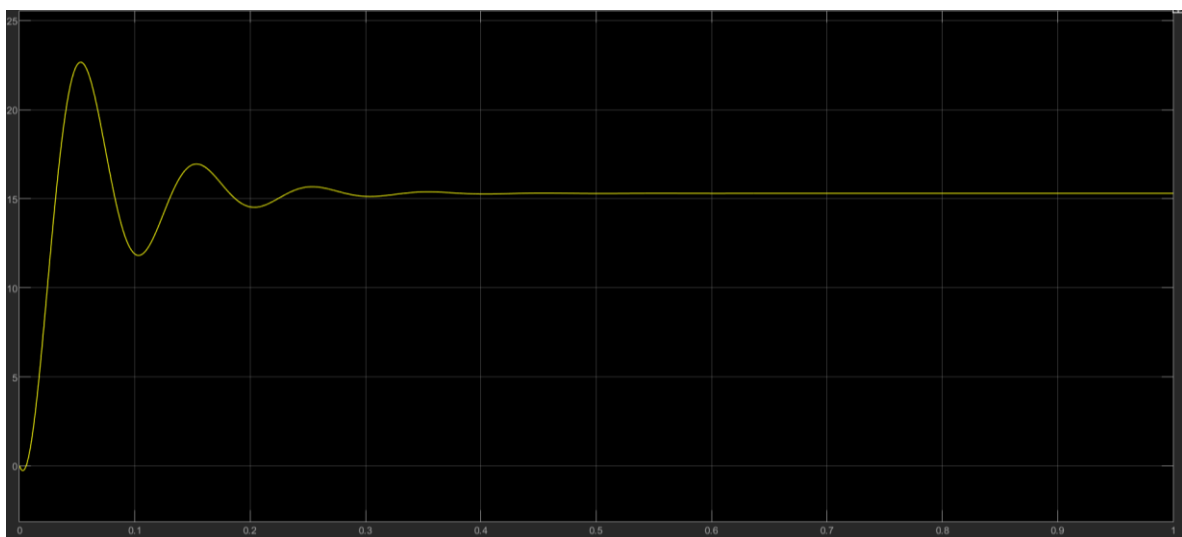
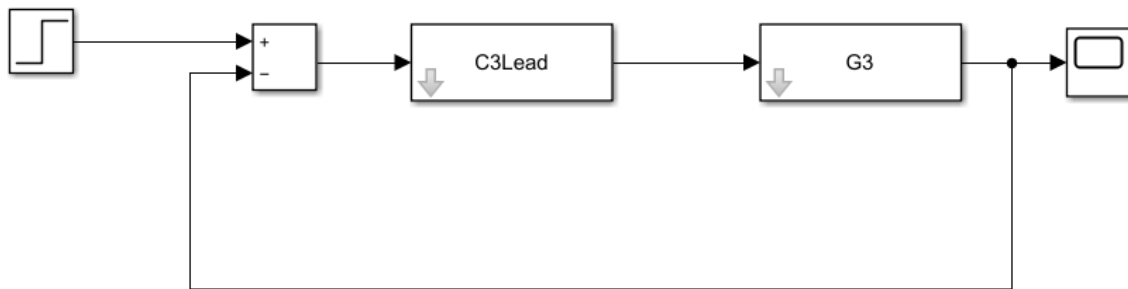
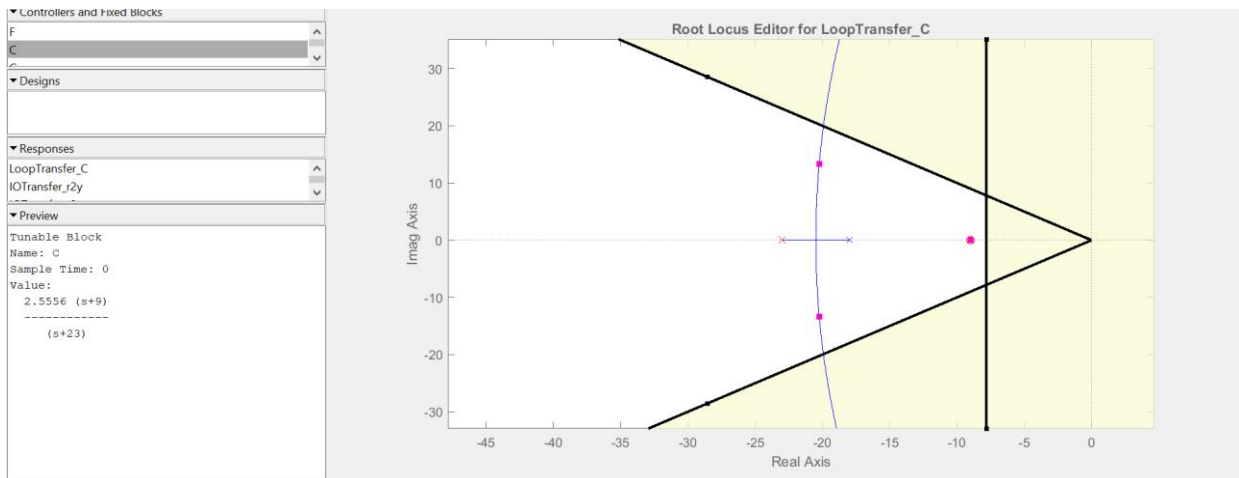
$$\text{ess} = \frac{1}{1 + \left(\frac{68}{162}\right) \frac{9K}{23}} = 0.1$$

$$K = 54.7941$$

$$z_{pK} = ([-9] \quad [-23], 54.7941)$$

$$C(s) = \frac{2.5556 (s+9)}{s+23}$$

$$K_p C = 1$$



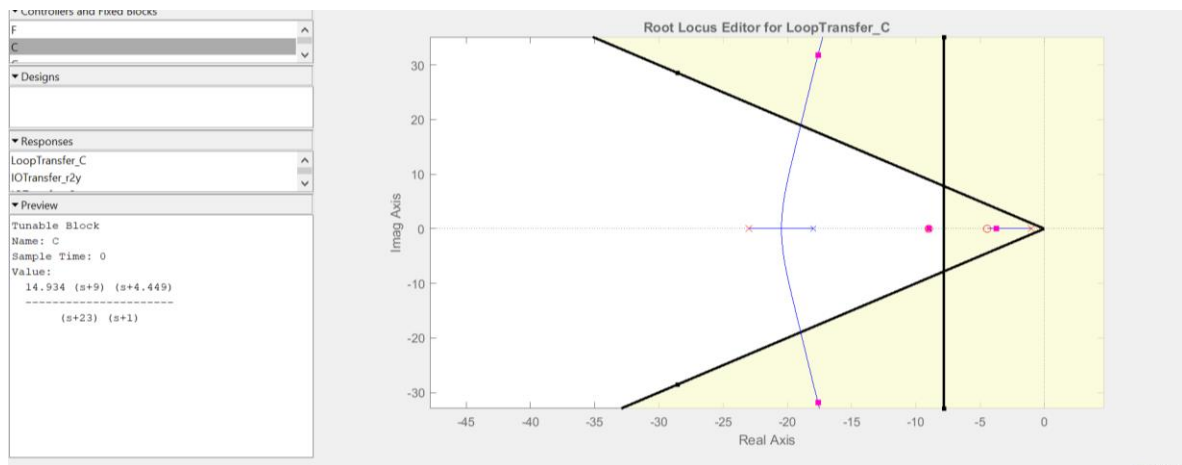
Lag Compensator

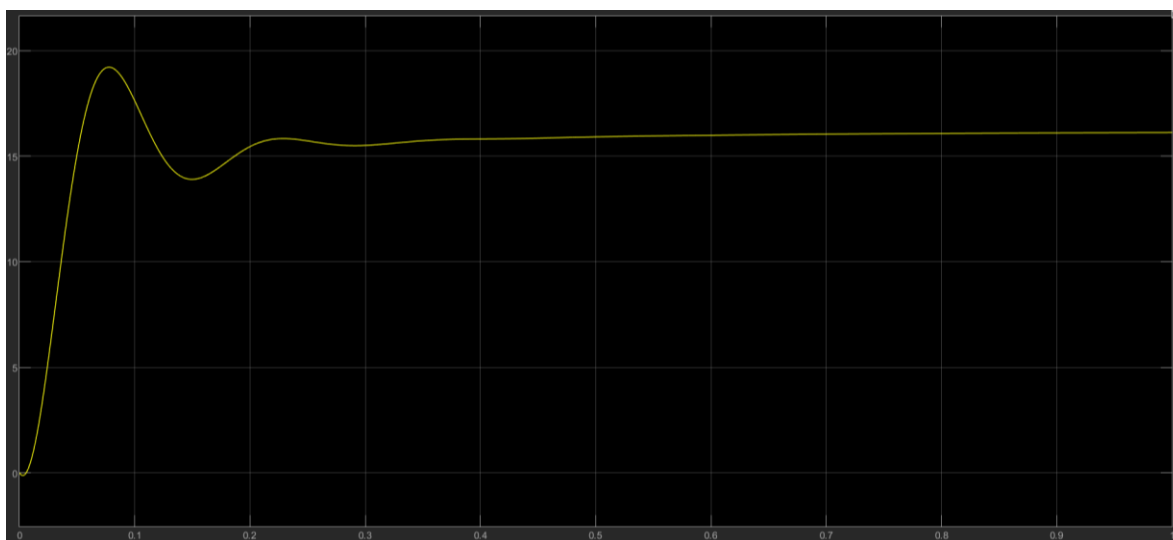
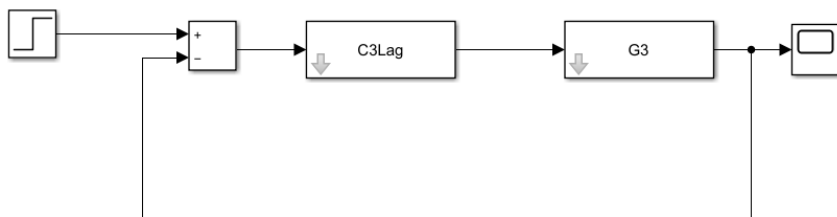
C3Lag =

$$\frac{26 (s+9) (s+4.449)}{(s+23) (s+1)}$$

Continuous-time zero/pole/gain model.

Lag Compensator
 Maximum input = 26
 $K_p G = \frac{68}{162}$ $C(s) = \frac{26(s+9)(s+4.2)}{(s+23)(s+6.2)}$
 $ess = \frac{1}{1 + \frac{68}{162} \cdot \frac{234}{23} K} = .05$ $K = 4.4491$





System 4

With the following script I obtain the transfer function

```
close all
t=zeros(); %arreglo de tiempo
k=zeros(); % arreglo de la ganancia
[fil,col]=size(Out); % declaro el arreglo para leer la posicion de los valores de la funcion
t=Out(:,1);%Datos del tiempo obtenidos de la tf G mediante simulink
k=Out(:,2);%Datos de la ganancia obtenidos de la tf G mediante simulink
figure;
plot(t,k); %grafica de la tf

%identificar el #orden del sistema
pico=max(k);
final=k(end);
if pico == final
    z = 1;

else
    z = 2;

end
%implementacion una vez conocido el orden del sistema
if z==1
    Orden=1
    for y=1:fil
        if Out(y,2) > final*0.9933 %Encontrar el valor de 5Tao
            pos=y %Posicion del arreglo donde esta 5tao
            break

            else
                end

            end

        Tss=Out(pos,1);
        Tao=Tss/5;
        ktf=final;
        G1=tf(ktf,[Tao 1])
        figure;
        plot(t,k);
        hold on
        step(G1)
    else
        Orden=2
        for y=1:fil
            if Out(y,2) == pico
                tpa=y;
                break

                else
                    end

                end

            tp=Out(tpa,1);
            wd=pi/tp;
            mp=((pico-final)/final);
            delta=-(log(mp))/(sqrt(log(mp)^2 + pi^2));
            wn=wd/sqrt(1-delta^2);
            ks2=final;
            G2=tf((ks2*wn^2),[1 (2*delta*wn) (wn^2)])
            figure;
            plot(t,k);
            hold on
            step(G2)
        end
    end
```

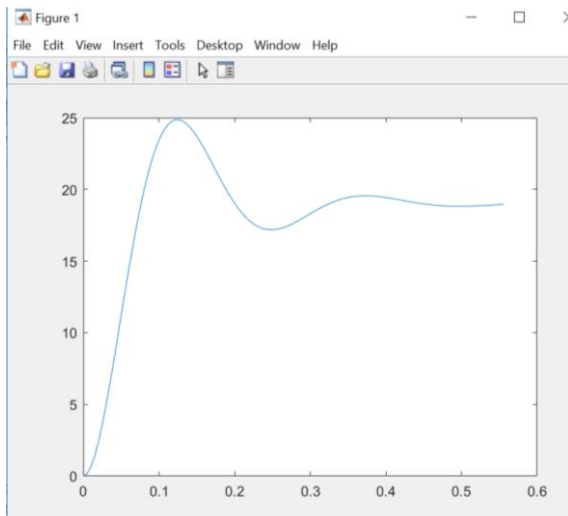
```
>> G4

G4 =

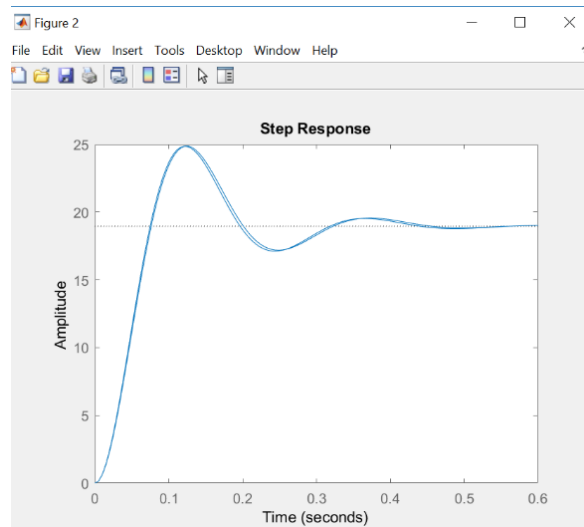
      14340
      -----
      s^2 + 19.14 s + 756.5

Continuous-time transfer function.
```

Original function



Approximate function



Lead Compensator

System 4
Lead Compensator

$$G(s) = \frac{14340}{s^2 + 19.14s + 756.5}$$

$$K_p G = \frac{14340}{756.5} \quad G\delta = .348$$

$$\delta = .349$$

$$\epsilon_{ss} = .5$$

$$e_{ss} = \frac{1}{1 + \frac{14340}{756.5} \frac{10K}{141}} = .1$$

$$C(s) = \frac{.3525(s+10)}{(s+141)}$$

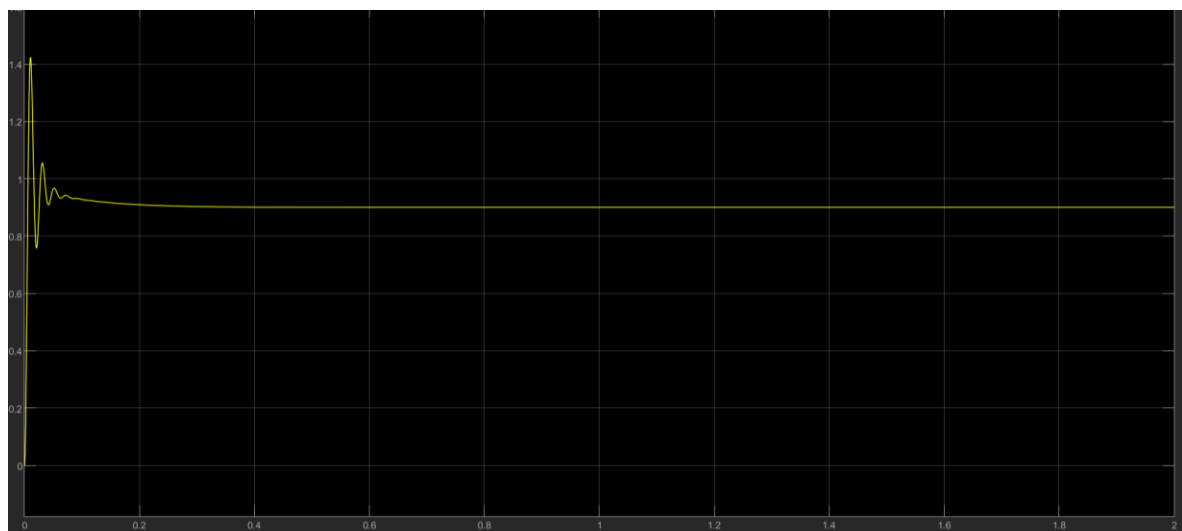
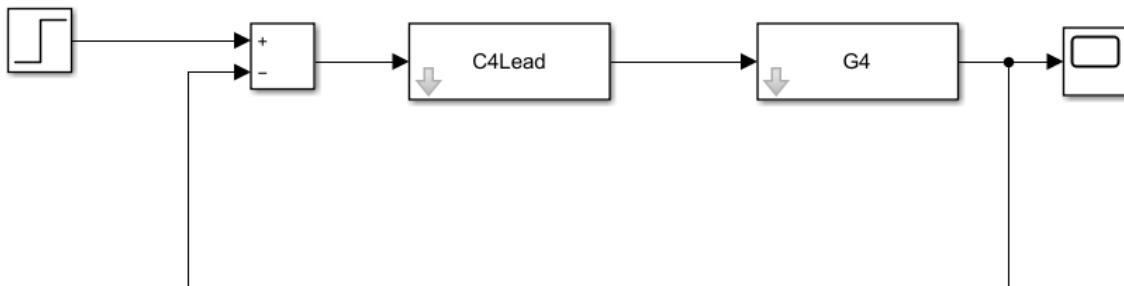
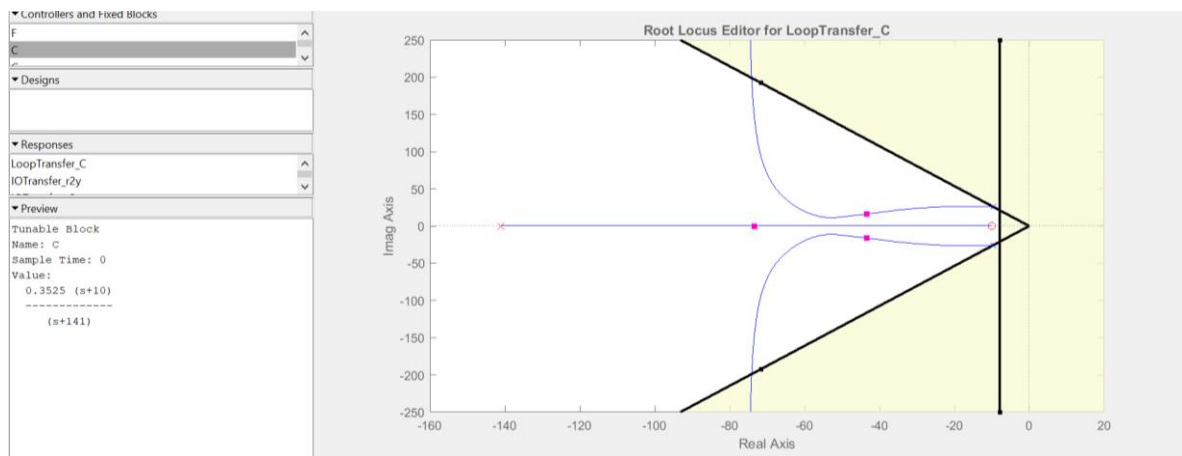
$$K = 6.69455$$

$$ZPK = ([-10] [-141] 6.69455)$$

C4Lead =

$$\frac{6.6945 (s+10)}{(s+141)}$$

Continuous-time zero/pole/gain model.



Lag Compensator

Lag Compensator

$$C(s) = \frac{.26 (s+10) (s+0.2)}{(s+141) (s+0.2)}$$

Maximum input = 26

$$K_p G = \frac{19340}{756.5}$$

$$ess = \frac{1}{1 + \frac{19340}{756.5} \cdot \frac{260}{141} K} = .05$$

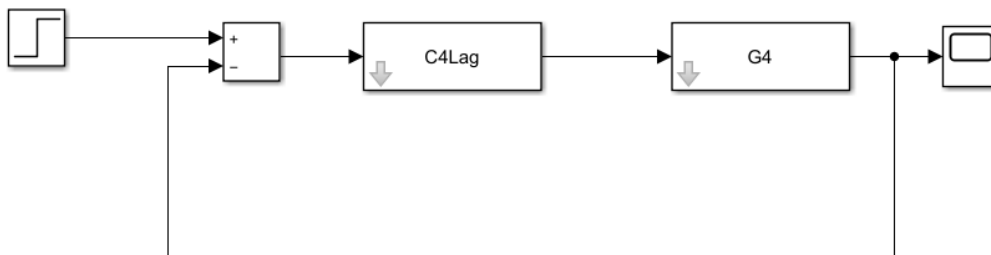
$$K = .543575$$

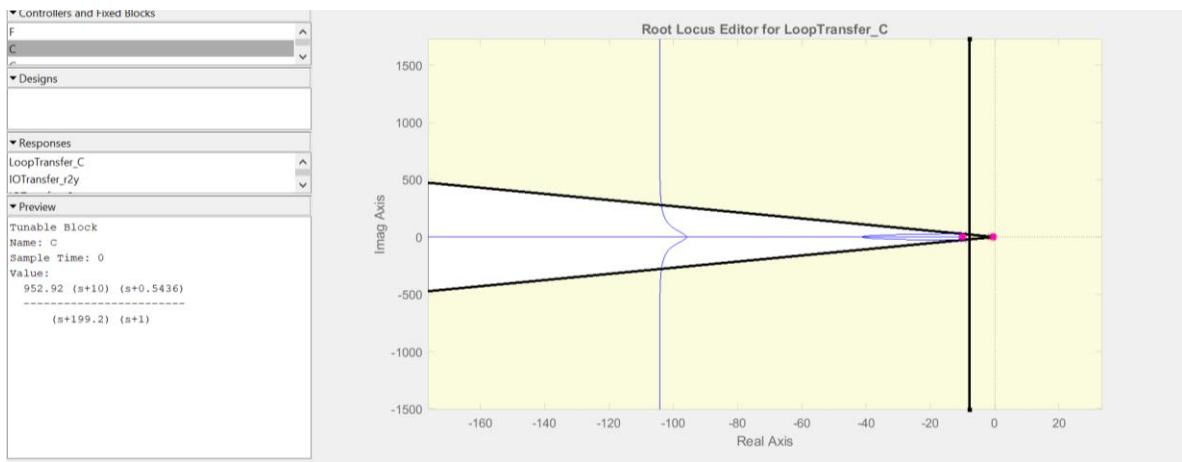
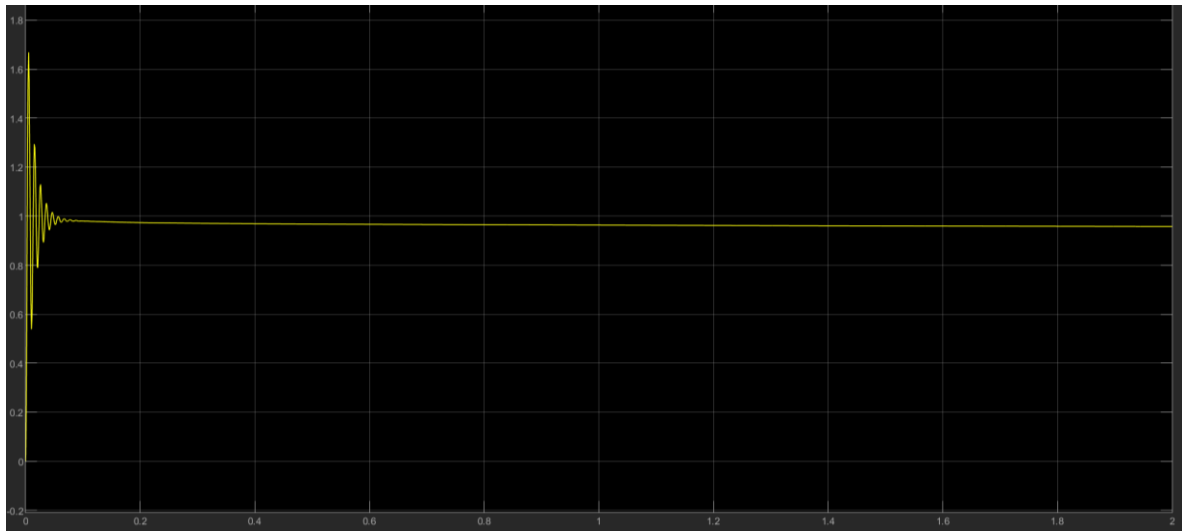
$$C(s) = \frac{.26 (s+10) (s+.543575)}{(s+141) (s+1)}$$

C4Lag =

$$\frac{26 (s+10) (s+0.5436)}{(s+141) (s+1)}$$

Continuous-time zero/pole/gain model.





System5

{n = 21}

Tank 1

Symbolic transfer function

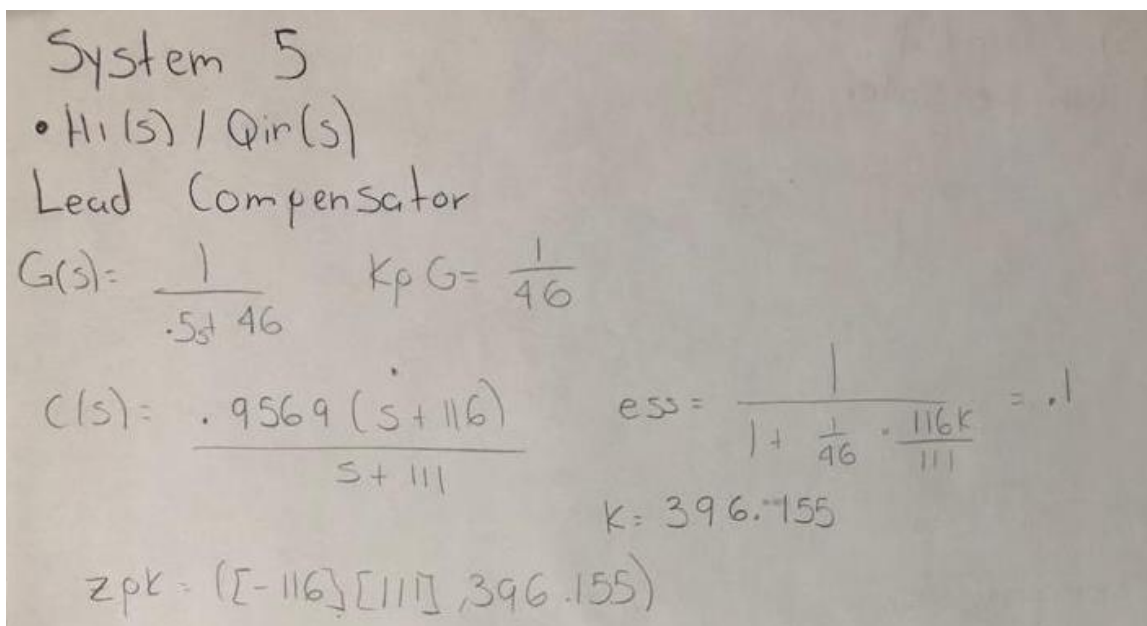
$$\frac{1}{Area1 + \frac{s}{R1}}$$

G5_H1 =

$$\frac{1}{0.5 s + 46}$$

Continuous-time transfer function.

Lead Compensator



System 5

- $H_1(s) / Q_{in}(s)$

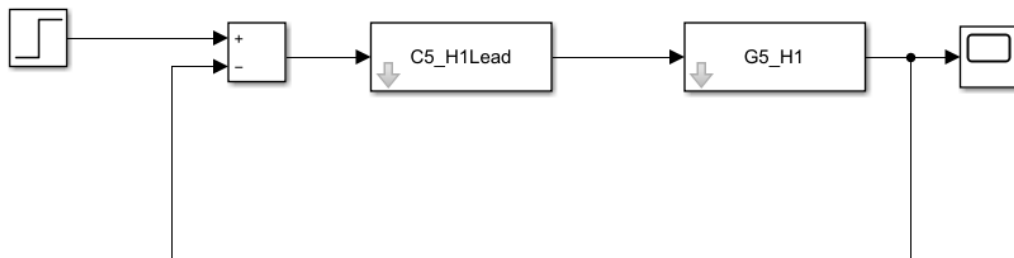
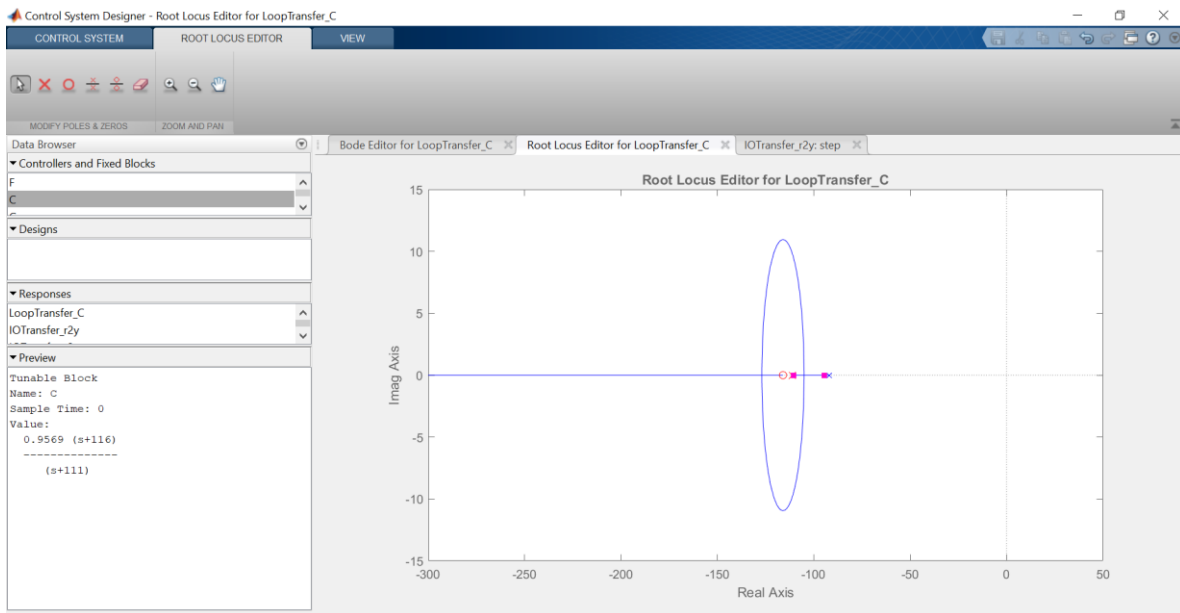
Lead Compensator

$$G(s) = \frac{1}{0.5s + 46} \quad K_p G = \frac{1}{46}$$
$$C(s) = \frac{0.9569(s + 116)}{s + 111}$$
$$ess = \frac{1}{1 + \frac{1}{46} \cdot \frac{116K}{111}} = 0.1$$
$$K = 396.155$$
$$zpk = (-116, 111, 396.155)$$

C5_H1Lead =

$$\frac{396.15 (s+116)}{(s+111)}$$

Continuous-time zero/pole/gain model.





Lag Compensator

Lag Compensator

Maximum input = 10

$$C(s) = \frac{10 (s+116) (s+0.2)}{(s+111) (s+1)}$$

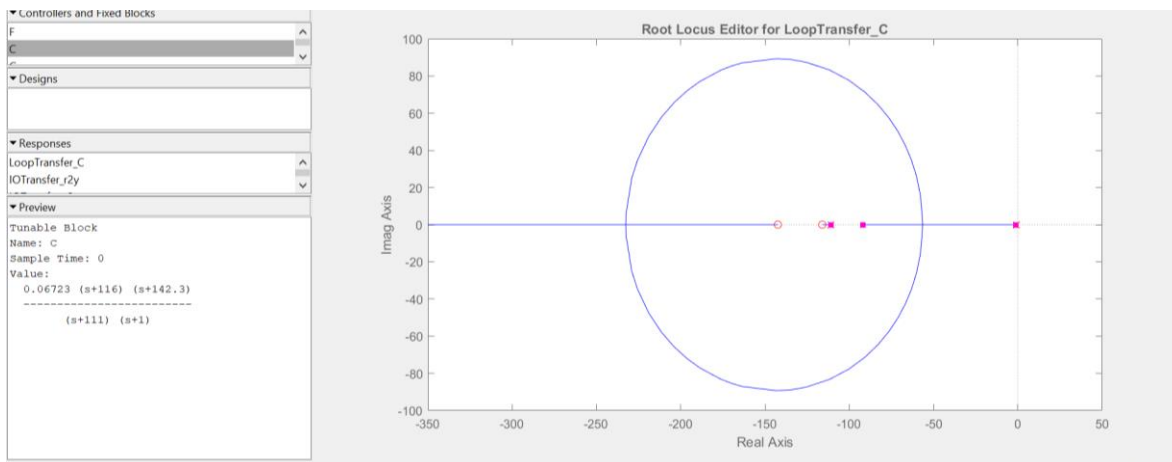
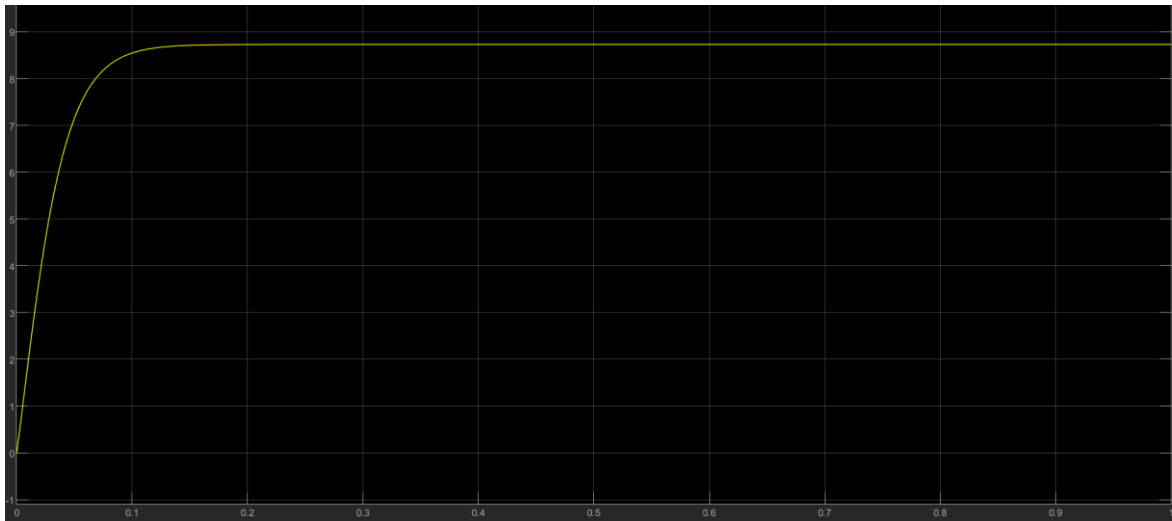
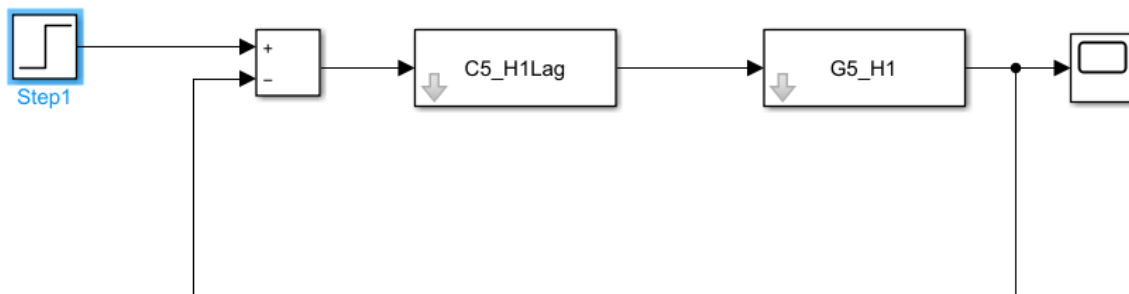
$$ess = \frac{1}{1 + \frac{1160K}{111} \left(\frac{1}{96}\right)} = 0.03 \quad K = 142.322$$

$$C(s) = \frac{10 (s+116) (s+142.322)}{(s+111) (s+1)}$$

C5_H1Lag =

$$\frac{10 (s+116) (s+142.3)}{(s+111) (s+1)}$$

Continuous-time zero/pole/gain model.



Tank 2

Symbolic transfer function

$$\frac{Q_{in1}}{\frac{A2s}{R1} + A2A1 + \frac{s^2}{R1R2} + \frac{A1s}{R2}}$$

G5_H2 =

$$\frac{3.5}{0.1428 s^2 + 23.14 s + 920}$$

Continuous-time transfer function.

Lead Compensator

• $H_2(s) / Q_{in}(s)$
Lead Compensator

$G(s) = \frac{3.5}{0.1428s^2 + 23.14s + 920}$

$K_p G = \frac{3.5}{920}$

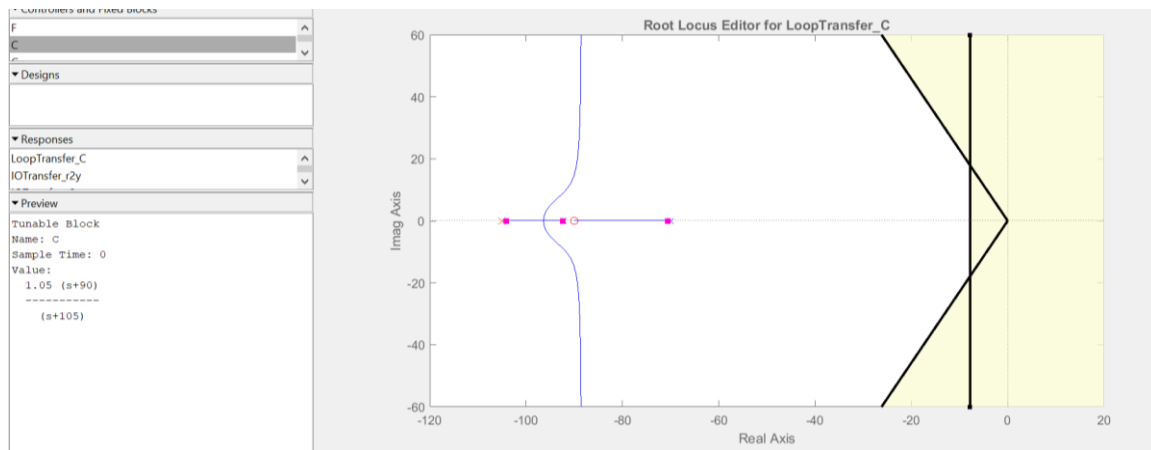
$ess = \frac{1}{1 + \frac{3.5}{920} \left(\frac{90}{105} \right)} = .1$

$K = 2760$

$C(s) = \frac{1.05(s+90)}{s+105}$

$G_8 = .3814$
 $\delta = .9$
 $Css = .5$

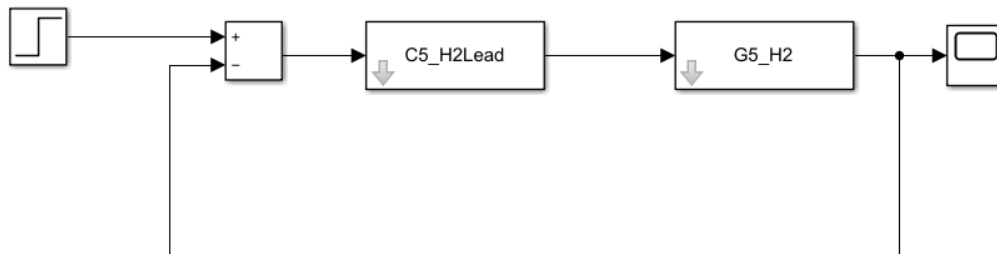
$zpk = [-90], [-105], 2760$

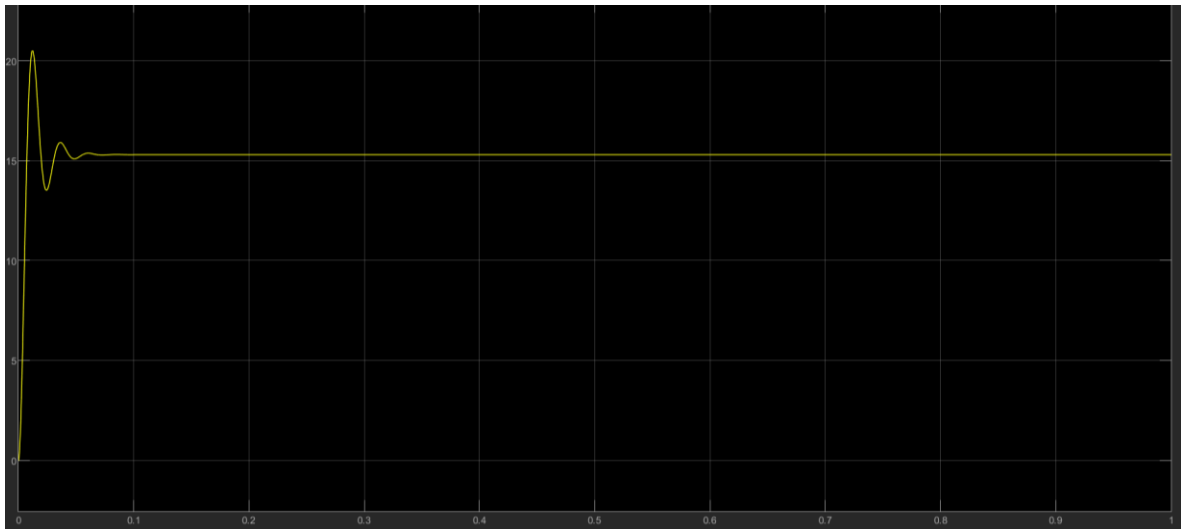


C5_H2Lead =

$$\frac{2760 (s+90)}{(s+105)}$$

Continuous-time zero/pole/gain model.





Lag Compensator

Lag Compensator

Maximum input = 10

$$K_p G = \frac{3.5}{920}$$

$$C(s) = \frac{10 (s+90) (s+a_2)}{(s+105) (s+b_2)}$$

$$ess = \frac{1}{1 + \frac{3.5}{920} \cdot \frac{900k}{105}} = .03$$

$$k = 991.556$$

$$C(s) = \frac{10 (s+90) (s+991.556)}{(s+105) (s+1)}$$

C5_H2Lag =

$$\frac{10 (s+90) (s+991.6)}{(s+105) (s+1)}$$

Continuous-time zero/pole/gain model.

