

Types of SRT

S - Attributed SRT

- Based on synthesized attribute
- Use Bottom up Parsing
- Semantic rules always written at rightmost position in RHS

Example :-

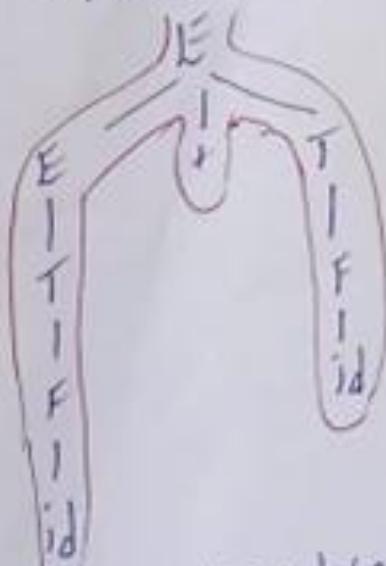
GRAMMAR

$$E \rightarrow E + T \mid T$$

$$T \rightarrow F$$

$$F \rightarrow id$$

input string : id + id



② The parent is taken the value from children it is called S-attributed

L - Attributed SRT

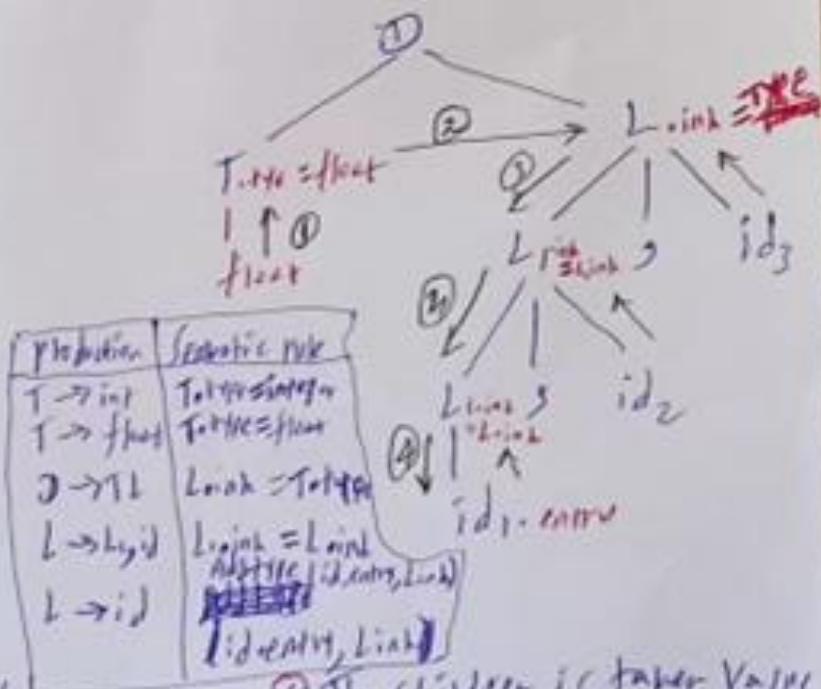
- Based on both synthesized and inherited attributes
 - Top Down parsing
 - Semantic rules anywhere in RHS
 - no cyclic dependency
- Example :-
- (grammar) | D: Declaration
 | T: Data type (int/float)
 | L: List of identifiers or identifier

$$D \rightarrow TL$$

$$T \rightarrow \text{int} \mid \text{float}$$

$$L \rightarrow L_1, id \mid id$$

input string : float id, id, id



③ The children is taken value from parent called L-attributed.

Add type()

- id_entry is a lexical value that points to the symbol table.
- L_inh is the type being assigned to every identifier in the list
- The function installs L_inh as the type of corresponding identifiers.

Conflicts in Syntax Analysis

⊕ Bottom-up (LR-family)

- 1) Shift-Reduce Conflict
- 2) Reduce-Reduce Conflict
- 3) Conflict from insufficient lookahead (SLL(1) vs LR(0))

⊖ Top-down (LL-family)

- 1) First-Follow Conflict
- 2) First-Follow "
- 3) Left-recursion "
- 4) Top-down ambiguity "

⊗ Grammar level ambiguity

- 1) Inherent ambiguity condition

⊗ Lexer-pARSER interface

- 1) Token ambiguity

LALR(1), first table

| States | Action | | | # | Action | |
|-----------------|-----------------|-----------------|---|--------------------|--------|----|
| | c | d | * | | E | F |
| I ₀ | S ₃₆ | S ₄₂ | | | | |
| I ₁ | | | | A ₀₀₀₀₀ | | 5 |
| I ₂ | S ₃₆ | S ₄₂ | | | | 99 |
| I ₃₄ | S ₃₆ | S ₄₂ | | | | |
| I ₃₂ | P ₃ | P ₃ | | P ₃ | | |
| I ₅ | | | | P ₁ | | |
| I ₄₄ | P ₂ | P ₂ | | P ₂ | | |

10 years
W₂ states

LALR(1)

CLR(1) \rightarrow look ahead
value

LR(1) items

LR(1) items + look ahead value

$$\begin{array}{l} E \rightarrow BB \\ B \rightarrow cB/d \end{array} \Rightarrow \begin{array}{l} E \rightarrow \cdot E, \$ \\ E \rightarrow \cdot BB, \$ \\ B \rightarrow \cdot cB/d, c/d \end{array} \left. \begin{array}{l} \text{LR(1)} \\ \text{items} \end{array} \right\}$$

$\Rightarrow I_3, I_6 \Rightarrow I_{16}$ } same production
 $\Rightarrow I_4, I_7 \Rightarrow I_{47}$ } look ahead
 $\Rightarrow I_8, I_9 \Rightarrow I_{89}$ } value is different

LALR(1) parsing table

| state | Action | | | Factor |
|-----------------|-----------------|-----------------|----------------|--------|
| | c | d | \$ | i |
| I ₀ | S ₃₆ | S ₄₇ | ACCEPT | |
| I ₁ | S ₃₆ | | | 5 |
| I ₂ | S ₃₆ | S ₄₇ | | 89 |
| I ₃₆ | S ₃₆ | S ₄₇ | | |
| I ₄₇ | R ₃ | R ₂ | | |
| I ₅ | | | R ₂ | |
| I ₃₆ | S ₃₆ | S ₄₂ | | 89 |
| I ₄₂ | | | R ₃ | |
| I ₈₉ | R ₂ | R ₂ | | |
| I ₈₉ | | | R ₃ | |

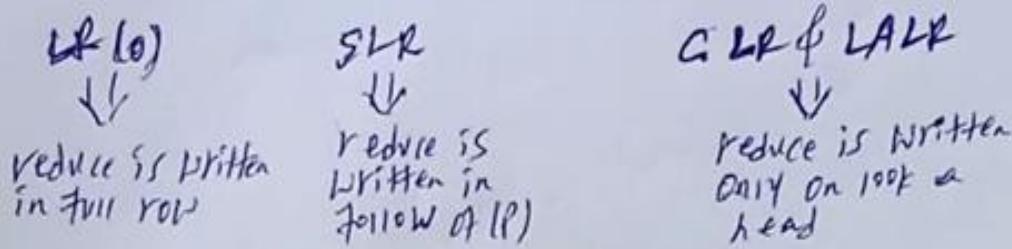
CLR(1) Parsing Table

| state | c | d | Action | E | Goto |
|----------------|----------------|----------------|----------------|---|------|
| I ₀ | S ₃ | S ₄ | | I | B |
| I ₁ | | | Accept | | |
| I ₂ | S ₆ | S ₇ | | | 5 |
| I ₃ | S ₃ | S ₄ | | | 8 |
| I ₄ | I ₃ | I ₃ | | | |
| I ₅ | | | I ₁ | | 9 |
| I ₆ | S ₆ | S ₇ | | | |
| I ₇ | | | I ₃ | | |
| I ₈ | I ₂ | I ₂ | | | |
| I ₉ | | | I ₂ | | |

CLR(1) and LALR(1)

Canonical Collection of

$LR(k)$ items $\Rightarrow LR(0)$ item + Look-ahead



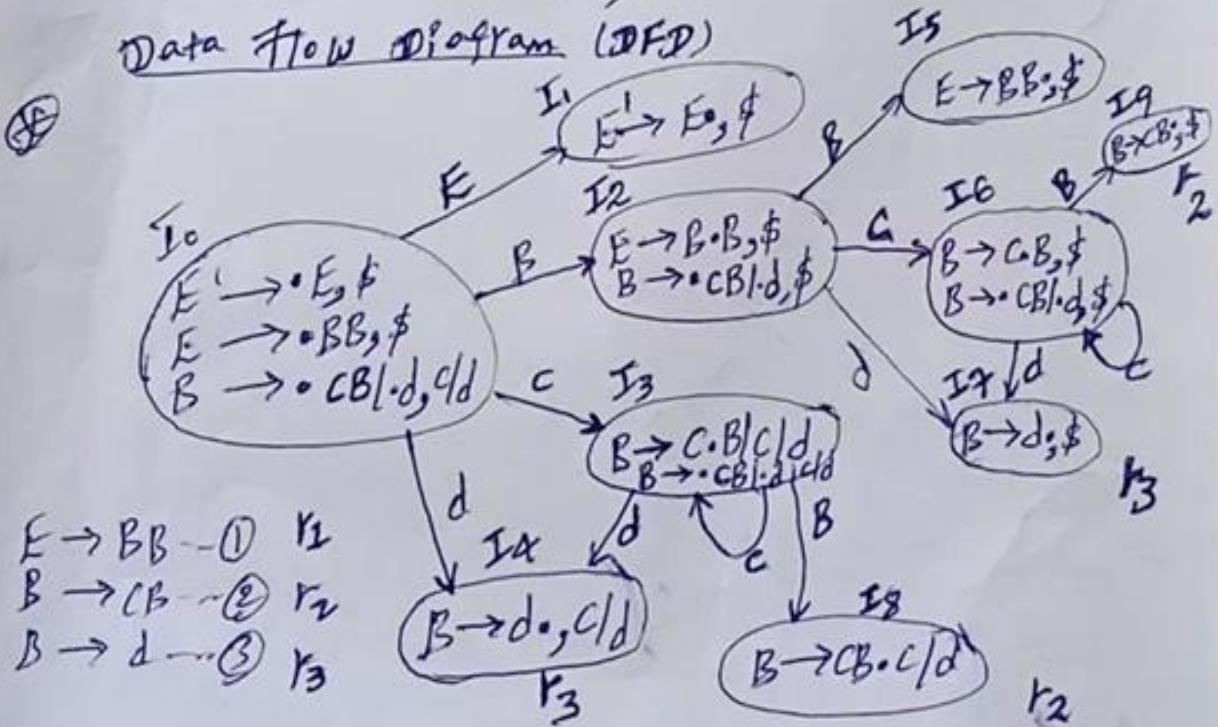
Example :-

$$\begin{array}{l} E \rightarrow BB \\ B \rightarrow CB/d \end{array}$$

* Argument grammar of $LR(1)$ items

$$\begin{array}{l} E^* \rightarrow \cdot E, \$ \leftarrow \text{look a head item} \\ E^* \rightarrow \cdot BB, \$ \leftarrow \text{look a head item} \\ B \rightarrow \cdot CB/d, c/d \leftarrow \text{look a head item} \end{array}$$

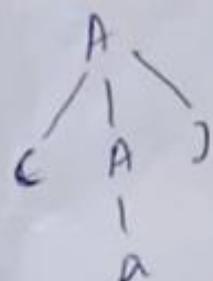
Data Flow Diagram (DFD)



IP stack parsing :- (a) #

| step | parsing stack | IP | Action |
|------|---------------|-------|----------------------|
| 1. | \$0 | (A) # | Add 2 |
| 2. | \$012 | 2) # | Add 3 |
| 3. | \$012A3 |) # | Reduce R. A → a |
| 4. | \$012A4 |) # | Add 5 |
| 5. | \$012A4E5 | E | Reduce R. A → (A) |
| 6. | \$0A1 | # | Accept |

Parse tree



$\Rightarrow (a)$

SLR(1) Parsing



simple LR

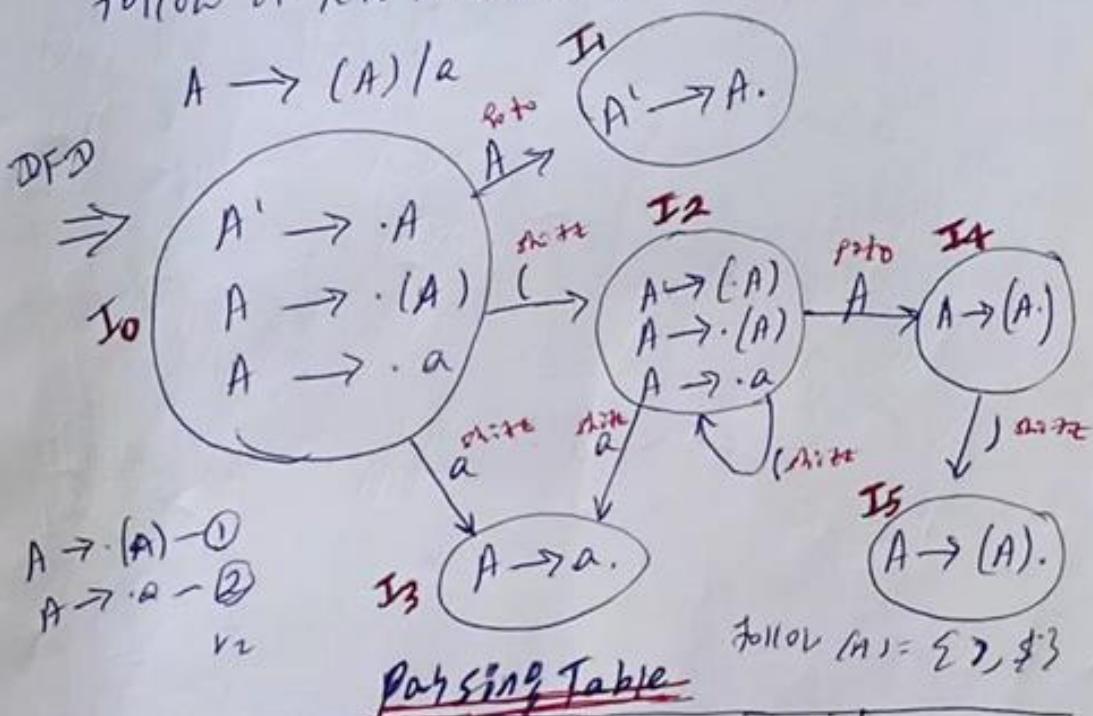
$$\begin{aligned} LR(0) &\supset LR(0) \\ SLR(1) &\supset \text{items} \\ CLR(1) &\supset LR(1) \\ LALR(1) &\supset \text{items} \end{aligned}$$

⇒ Works on smallest class of grammar

⇒ few no. of states

⇒ simple & fast to reconstruct

* In SLR we place the reduce move ONLY in the follow of left hand side not to entire row.



| State | a | (|) | \$ | goto |
|-------|----|----|----|--------|------|
| 1 | s3 | s2 | | | A |
| 2 | s3 | s2 | | Accept | 4 |
| 3 | | | r2 | r2 | |
| 4 | | | s5 | | |
| 5 | | | r1 | r1 | |

$r \rightarrow \text{reduce}$

Step-7:- Construct Parsing Table LR(0)

| States | Action (Terminal) | | | Go to | |
|----------------|-------------------|----------------|----------------|-------|---|
| | a | b | \$ | A | S |
| I ₀ | s ₃ | s ₄ | | 2 | 1 |
| I ₁ | Accept | Accept | Accept | | |
| I ₂ | s ₃ | s ₄ | | 5 | |
| I ₃ | s ₃ | s ₄ | | 6 | |
| I ₄ | r ₃ | r ₃ | r ₃ | | |
| I ₅ | r ₁ | r ₁ | r ₁ | | |
| I ₆ | r ₂ | r ₂ | r ₂ | | |

I₄, I₅, I₆ all contains final states

$$S \rightarrow AA \quad \textcircled{1}$$

$$A \rightarrow aA \quad \textcircled{2}$$

$$A \rightarrow b \quad \textcircled{3}$$

LR (0) Parsing

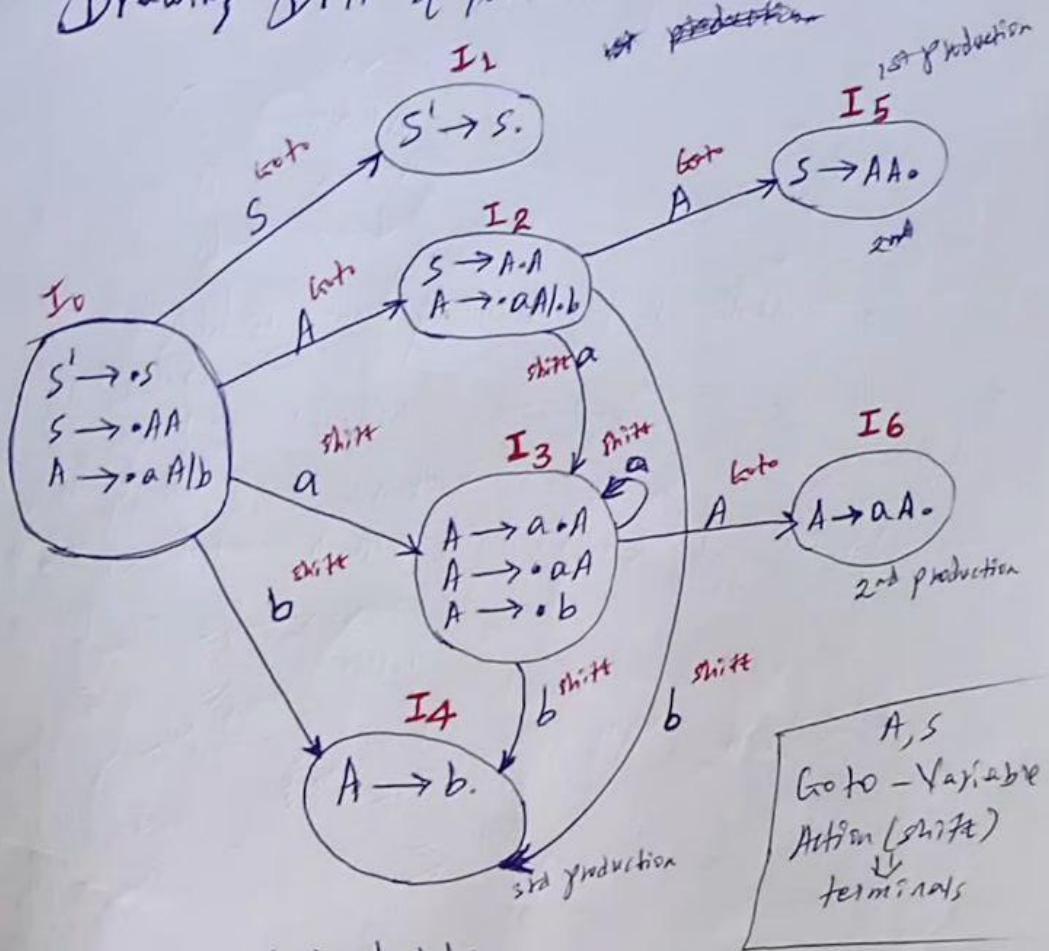
$$S' \rightarrow S$$

$$S \rightarrow AA \quad \textcircled{1}$$

$$A \rightarrow aA \quad \textcircled{2}$$

$$A \rightarrow b \quad \textcircled{3}$$

Drawing DFA & contains 7 states I₀ to I₆



Step 6 :- LR(0) table

* If a state is going to some other state on a terminal it is correspond to a shift move.

* If a state is going to some other state on a Variable it is correspond to goto move

* If a state contain the final item in the particular row then write the reduce node completed.

B⁺

$$\begin{aligned} S' &\rightarrow \cdot S \\ S &\rightarrow \cdot A A \\ A &\rightarrow \cdot a A \\ A &\rightarrow \cdot b \end{aligned}$$

{ Add Agument production to I₀ state & compute
closure }
 $I_0 = \text{closure} \{ S' \rightarrow \cdot S \}$

all productions starting with S' into I₀ state b/s
"•" is followed non terminal. So I₀ state becomes

$$\begin{aligned} I_0 &= S' \rightarrow \cdot S \\ &S \rightarrow \cdot A A \end{aligned}$$

all productions starting with "A" in modified I₀
state b/s

State

$$I_1 = \text{Goto}(I_0, S) = \text{closure}(S^1 \rightarrow \cdot S.) = \underline{S^1 \rightarrow S.}$$

Here, the production is reduced so close the stat

State

$$I_2 = \text{Goto}(I_0, A) = \text{closure}(S \rightarrow A \cdot A)$$

Add all productions starting with A into I_2 states

b/c " " follow

Non terminal. So, the I_2 state becomes,

$$I_2 = S \rightarrow A \cdot A$$

$$A \rightarrow \cdot aA$$

$$A \rightarrow \cdot b$$

$$\text{Goto}(I_2, a) = \text{closure}(A \rightarrow a \cdot A)$$

states

$$\begin{aligned} I_0 :& \quad S^1 \rightarrow \cdot S \\ & \quad S \rightarrow \cdot AA \\ & \quad A \rightarrow \cdot aA \\ & \quad A \rightarrow \cdot b \\ & \quad \text{goto}(I_0, S) \end{aligned}$$

$$\begin{aligned} I_1 :& \quad S^1 \rightarrow S. \\ & \quad \text{goto}(I_0, A) \end{aligned}$$

$$\begin{aligned} I_2 :& \quad S \rightarrow A \cdot A \\ & \quad A \rightarrow \cdot aA \\ & \quad A \rightarrow \cdot b \\ & \quad \text{goto}(I_2, a) \end{aligned}$$

$$\begin{aligned} I_3 :& \quad A \rightarrow a \cdot A \\ & \quad A \rightarrow \cdot aA \\ & \quad A \rightarrow \cdot b \end{aligned}$$

$$\text{goto}(I_2, b)$$

$$I_4 : \quad A \rightarrow b.$$

$$\text{goto}(I_2, A)$$

$$I_5 : \quad S \rightarrow AA.$$

$$\text{goto}(I_3, A)$$

$$I_6 : \quad A \rightarrow aA.$$

LR(0) Parsing :-

Various steps involved in parsing

- for the given input string write context free grammar
- check ambiguity of the grammar
- Add augment production in the given grammar
- Create Canonical collection of LR(0) items
- Draw a state flow diagram (DFA)
- Construct LR(0) parsing table.

E.g:-

$$\begin{array}{l} S \rightarrow AA \\ A \rightarrow aA/b \end{array}$$

$$\begin{array}{l} S^0 \rightarrow S \\ S \rightarrow AA \\ A \rightarrow aA \\ A \rightarrow b \end{array}$$

} Augment production

Step-3 :- Add Augment production

$$\begin{array}{l} S^0 \rightarrow S \\ S \rightarrow AA \\ A \rightarrow aA/b \end{array}$$

} Given grammar.

Step-4 :- Create Canonical collection of LR(0) items

* An LR(0) items is a production $G \rightarrow \cdot L$ with dot at some position in the right hand side of production.

* LR(0) items is useful to indicate that how much of string has been scanned up to a given point in the process of parsing

* In LR(0), we place the reduce node in entire row.

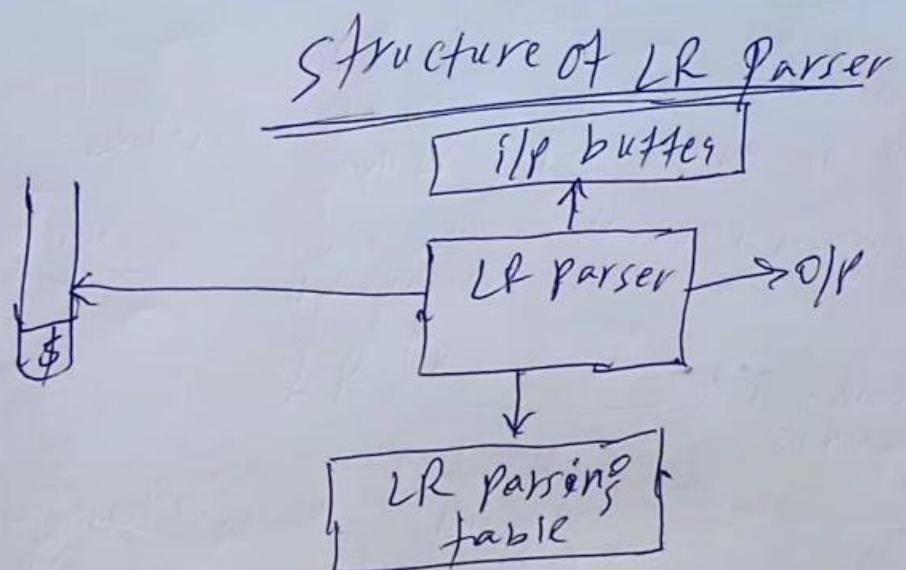
$$\boxed{\begin{array}{l} S^0 \rightarrow \cdot S - \text{LR}(0) \text{ item} \\ S \rightarrow \cdot AA \\ A \rightarrow \cdot aA/b \end{array}}$$



3) LALR(1) :- Look A head LR parser.

* Works on intermediate size of grammar

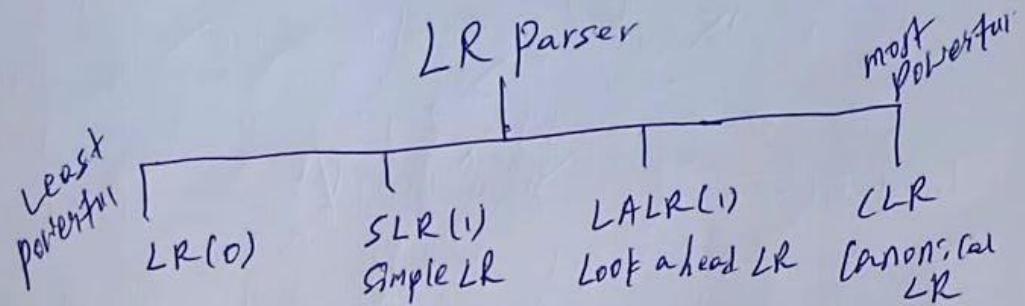
* No of States are same as SLR(1)



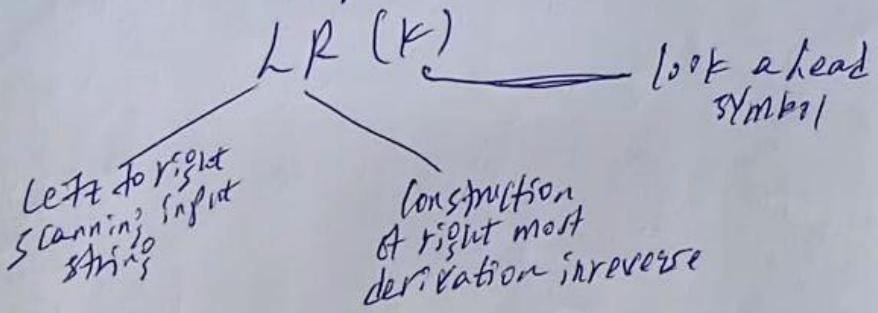
LR(0) -
SLR(1) -
LALR(1) - } the only difference
is parsing table

- * To construct LR(0) and SLR(1) tables we use Canonical Collection of LR(0) items.
- * To construct LALR(1) & CLR(1) tables we use Canonical Collection of LR(1) items.

parsers - Compiler Design



LR parser :- \Rightarrow Non recursive shift reduce bottom up parser.



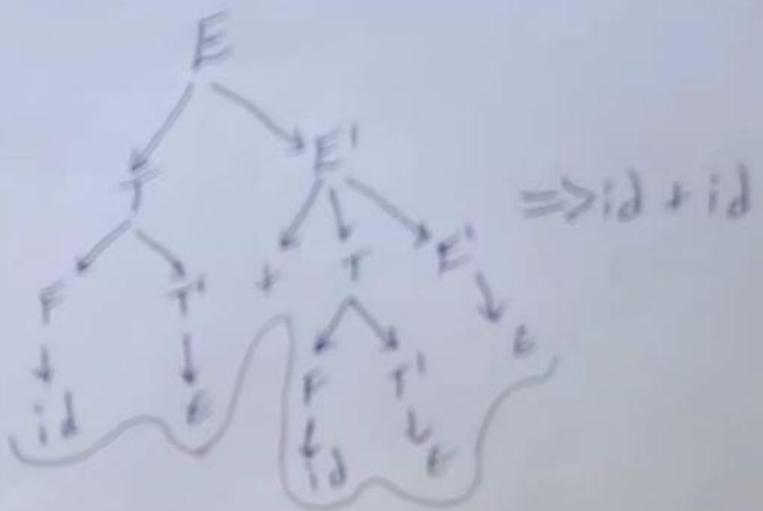
1) SLR(1) :- Simple LR parser

- * Work on smallest class of grammar
- * Few no of states
- * Simple & fast construction.

2) CLR(1) :- LR parser

- * Works on complete set of LR(1) grammar
- * Large no of states
- * Slow construction

Step 4: parse tree



Step-2 :- Parsing Table

| | id | + | * | (|) | \$ |
|------|---------------------|-----------------------|-----------------------|---------------------|--------------------|----------------------|
| E | $E \rightarrow TE'$ | | | $E \rightarrow TE'$ | | |
| E' | | $E' \rightarrow +TE'$ | | | $E' \rightarrow E$ | $E' \rightarrow \#E$ |
| T | $T \rightarrow FT'$ | | | $T \rightarrow FT'$ | | |
| T' | | $T' \rightarrow E$ | $T' \rightarrow *FT'$ | | $T' \rightarrow E$ | $T' \rightarrow E$ |
| F | $F \rightarrow id$ | | | | | |

Step-3 :- Stack Implementation

$i/p = id + id$

| Stack | i/p | Action |
|------------|-------------|--|
| $E\#$ | $id + id\#$ | $E \rightarrow TE'$ |
| $TE'\#$ | $id + id\#$ | $T \rightarrow FT'$ |
| $FT'E'\#$ | $id + id\#$ | $F \rightarrow id$ |
| $idT'E'\#$ | $id + id\#$ | pop id |
| $T'E'\#$ | $+id\#$ | $T' \rightarrow E$ |
| $E'\#$ | $+id\#$ | $E' \rightarrow +TE'$ |
| $+TE'\#$ | $+id\#$ | pop + |
| $TE'\#$ | $id\#$ | $T \rightarrow FT'$ |
| $FT'E'\#$ | $id\#$ | $\#F \rightarrow id$ |
| $idT'E'\#$ | $id\#$ | pop + |
| $T'E'\#$ | $\$$ | $T' \rightarrow E$ |
| $E'\$$ | $\$$ | $E' \rightarrow E$ |
| $\$$ | $\$$ | Accept |

Construction of predictive parser LL(1)

Example 2 :-

$$\begin{array}{l} E \rightarrow E + T T \\ T \rightarrow T * F F \\ F \rightarrow (E) / id \end{array}$$

$$\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow +TE'/E \\ T \rightarrow FT' \\ T' \rightarrow *FT'/E \\ F \rightarrow (E)/id \end{array}$$

- ① first follow
- ② parsing table
- ③ stack implementation
- ④ parse tree

Step - 1 :-

FIRST Function

$$\begin{aligned} \text{first}(F) &= \{c, id\} \\ \text{first}(T') &= \{\$, E\} \\ \text{first}(T) &= \{c, id\} \\ \text{first}(E') &= \{+, E\} \\ \text{first}(E) &= \{c, id\} \end{aligned}$$

FOLLOW Function

$$\begin{aligned} \text{follow}(E) &= \{\$\} \\ \text{follow}(E') &= \{\$\} \\ \text{follow}(T) &= \{\text{first}(E') - E \vee \text{follow}(E)\} \\ &= \{+, \$\} \\ \text{follow}(T') &= \{+, \$\} \\ \text{follow}(F) &= \{+, *, \), \$\} \end{aligned}$$

Step 3 :- Stack Implementation by using parse table

Input string abd\$

| <u>Stack</u> | <u>input</u> | <u>Production</u> |
|--------------|--------------|---|
| \$ \$ | abd \$ | $S \rightarrow A$ |
| A \$ | abd \$ | $A \rightarrow aBA'$ |
| aBA' \$ | abd \$ | pop a |
| BA' \$ | bd \$ | $B \rightarrow b$ |
| bA' \$ | d \$ | pop b |
| A' \$ | | $A' \rightarrow dA'$ |
| dA' \$ | | pop d |
| A' \$ | | $A' \rightarrow e$ |
| \$ | | Accept if the input is properly parsed |

Step 4 :- Generate Parse tree using implementation
Following top down approach.

