

# REACT: The Riskmap Evaluation and Coordination Terminal

by

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Submitted to the Department of Electrical Engineering and Computer  
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## Abstract

The United Nations Office for Disaster Risk Reduction (UNDRR) states that economic losses due to natural disasters have risen 151 percent in the past 20 years. Of these disasters, floods are the most common. The Sendai Framework for Disaster Risk Reduction was created by the UNDRR in order to chart goals for future risk mitigation; among its seven global targets is increasing the availability of disaster risk information and assessment systems. Disaster information systems use state of the art techniques such as remote sensing in order to mitigate damages from natural and man made hazards.

It is common in developed countries utilize networks of advanced sensors and ahead of time mapping in order to facilitate emergency responses; however, such systems are not available in developing countries due to cost limitations. The widespread proliferation of smart phones and social media use in developing countries means that citizens can be used as sensors by reporting disaster information online. The Riskmap system was developed by the Urban Risk Lab at MIT in order to gather citizen report streams. Such citizen disaster reports have two issues: a large influx of reports can cause information overload in emergency operations centers, which makes it difficult to summarize the situation. Machine learning has previously been used in order to analyze and simplify information for human consumption. This work seeks to use novel machine learning techniques to fully utilize crowd-sourced social media reports gathered using the Riskmap system.

Thesis Supervisor: Miho Mazereeuw  
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# Chapter 1

## Introduction

Natural disasters are a constant threat to societies all over the planet. Among natural disasters, flooding is the most common calamity in the world [1]. Flood related deaths account for half of all deaths from natural disasters [2]. Although flooding impacts both developed and developing countries, developing nations face much higher mortality rates as a result of flooding since they lack resources to adequately mitigate hazards [3, 4]. Deltaic megacities in developing countries are particularly at risk because of unregulated urbanization, rising population, and climate change [1]. Moreover, there is little data that is available before, during, and after a disaster to help stakeholders respond to hazards [5].

Various stakeholders, such as humanitarian Nongovernmental Organizations (NGOs), government emergency responders and affected citizens, have different but overlapping interests with regards to disaster management. Government and NGOs work together to provide relief and mitigate damages from flooding [6], while citizens look for relevant information and try to reduce their risk by avoiding heavily affected areas [7]. Information is at the core of disaster management; however, data scarcity makes it hard for emergency personnel to optimize their use of resources, while citizens have an abundance of information about their surroundings but must be careful not to trust incorrect or outdated information about broader areas [8].

Disaster information systems can connect affected communities with Emergency Operations Centers (EOCs), thereby bridging the information gap between respon-

ders and citizens. Many such disaster information systems have been developed, but they often suffer from a lack of institutional buy-in [9]. The lack of engagement can be partly attributed to the difficulty of adding data gathering responsibilities to emergency personnel that have little time during crises. One solution to this problem is asking citizens to submit information; however, crowdsourcing brings its own issue: in times of crisis EOCs can suffer from information overload when they are presented with too much data [10].

In this work we present the REACT system, which uses novel machine learning and human computer interaction research to reduce information overload from crowd sourced data in EOCs, thereby decreasing data analysis time during disasters. It classifies reports as indicating heavy flooding or not through an ensemble model. It extracts key features from each of the parts of a report (text, picture, metadata) using domain specific techniques and then uses a small dense neural net to classify the citizen report.

First we establish the motivation for using citizens as sensors and provide an overview of the Riskmap System which allows for gathering of citizen reports. We then show the need for analyzing this noisy data using machine learning. A review of different machine learning techniques that have been used in crisis information systems, including those that also utilize social media is presented. Finally we describe REACT, a novel ensemble learning model that can accurately predict large urban flood events from noisy crowdsourced data.



# Chapter 2

## Background

Global climate change is ‘expected to increase the frequency and intensity of floods’ [4]. Developing urban areas that are undergoing unchecked development and rising population regularly experience flooding [1]. Nowhere is this more apparent than in South and Southeast Asia, where the severity of floods has been increasing over the past several decades [11].

Of the world’s 33 mega-cities with population over 10 million, more than 60 percent are located in developing Asian Countries [12]. These cities face a looming crisis as flood risk increases, but there are also unique opportunities for risk mitigation. Megacities are characterized by high population density, which leads to an increase in economic damages and loss of life during flood events, but it also means that there are large numbers of citizens that have disaster information they would like to share with others [1].

### 2.1 History of Disaster Informatics

One of the best known and earliest work in disaster informatics was John Snow’s use of maps to find the source of the 1857 Cholera outbreak in London[13]. This example is taught to all students of epidemiology and illustrates the need not only for up to date information, but for systems that ease the analysis of this information. In John Snow’s case, the map was the technology that allowed him to visualize the

spread of the disease and effectively take action that ended the outbreak; however, the computer revolution has drastically changed the way that scientists and responders analyze disaster information. John Snow used mapping technology to track the spread of disease, but now researchers are using artificial intelligence to predict cholera outbreaks before they happen [14].

In more recent times, the need for Information Technology (IT) in disaster management has been clear since the mid 1980s when computers became user friendly enough to be used during disasters [15].

Now many Emergency Operations Centers (EOCs) use Geographic Information Systems (GIS), inventory control systems, and online messaging systems among other technology in order to organize spatial data and analyze disaster information. For example, Mozambique used an integrated disaster management system to provide early warning during the 2007 Zambezi floods, while Guatemala’s inventory management helped to curb government bribes [9]. While technology has helped some EOCs to better respond to disaster events, researchers have often stated that ‘there are many reasons to remain skeptical about the idea that technology will provide a panacea for emergency management problems’ [16, 10, 17]. A number of potential negative effects associated with disaster management technology have been identified: primarily the potential of information overload and the dissemination of incorrect and outdated information [8, 18].

### **2.1.1 Social Media and Disasters**

The history of online communities is firmly linked to disasters. Internet Relay Chat (IRC) was one of the first truly global online communication systems; its adoption among internet connected citizens was ‘prompted by the First Gulf War’ [19]. Although radio and television broadcasts were halted by the Iraqi army shortly after the invasion, IRC communication continued for days afterward. IRC allowed users to communicate about conditions on the ground, including the Gulf War oil spill that grew to be the largest oil spill in history [20].

The history of social media and the hashtag is invariably linked to disaster com-

munication. It was during the San Diego bush fires of 2007 that the hashtag was first widely used on twitter [19].

Quarantelli emphasized that ‘management of hazards is fundamentally social in nature and not something that can be achieved strictly through technological upgrading’ [10] yet social media brings human behavior into a machine readable format can provide further information during disasters.

Work has been done in passively listening to social media streams in order to better understand how disasters unfold and how humans use social media as a communication tool during disaster events. Many of these studies use hand labeled tweets in order to classify what kind of information people talk about [21]. Further work has evolved to using artificial intelligence methods to automatically label new tweets using supervised learning. For example, Patrick Meier’s Haiti Crisis Map initially used volunteers to classify large number of tweets, but his more recent projects focus on the use of AI for tackling big data problems [5].

### 2.1.2 Crowdsourcing vs. Passive Listening

As Patrick Meier points out in *Digital Humanitarians*, ‘since humanitarian organizations don’t ask eyewitnesses on social media to report information’, they must passively wait and ‘rely on witnesses sharing relevant information by chance’ [5]. Listening to twitter data streams and hoping that someone posts relevant disaster information is not always a winning strategy. Past solutions have paid workers to collect information and enter it into disaster information systems. The government of Mozambique used this technique during flooding in 2007; however, this method was found to be expensive and unscaleable [9]. An analysis of the system found that ‘data processing and consolidation [were] difficult’ and that ‘the few data entry clerks struggled to keep up’ [9].

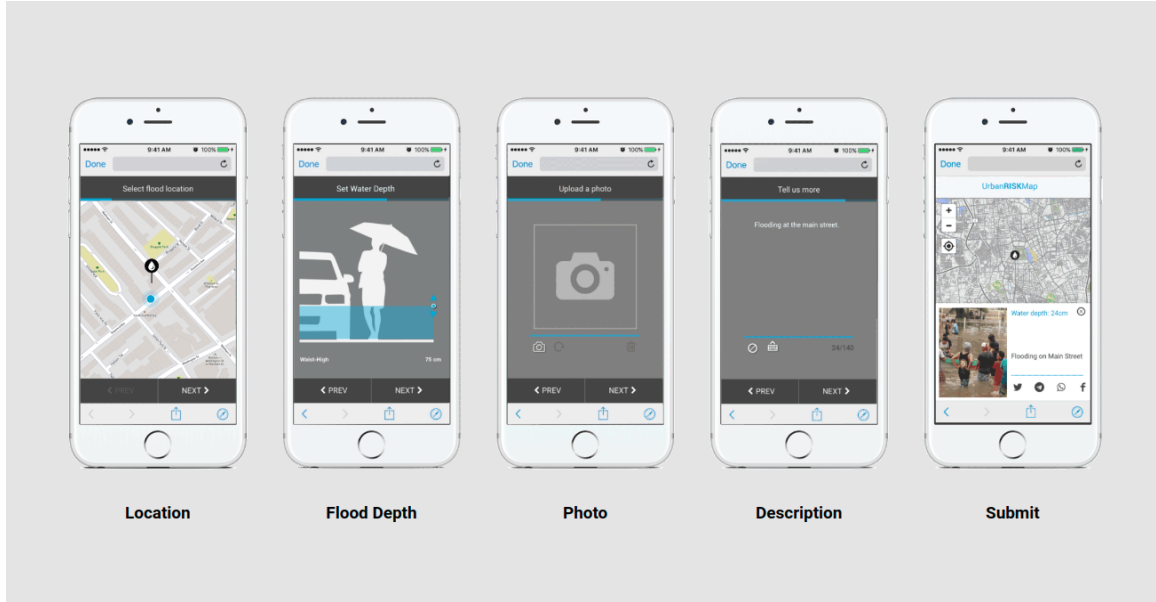


Figure 2-1: Submitting a flood report card. Graphic by MIT-URL

## 2.2 The Riskmap System

The Riskmap system alleviates the load on emergency managers by centralizing reports from many social media sources. It also makes it easy not only for reports to come into the response center, but also for emergency managers to indicate which areas of a city are most affected at any one time. The data gathered during an event is persistent and available under the Creative Commons license, which allows researchers to track the flood over time and pinpoint areas that are particularly vulnerable to flooding, thus fulfilling the need for open data [22, 23].

The system has been in place in Jakarta and Chennai since 2016, and has seen hundreds of thousands of views during flood events [24, 25].

### 2.2.1 Social Media Outreach

Riskmap consists of many different social media bots that are actively filtering social media streams and looking for citizens that might be reporting flooding events, it then reaches out to those users and asks them to submit a flood report that consists of a GPS location, the estimated flood height at that location, a picture, and a textual description. The user interface for submitting these reports is shown in Figure 2-1.

These reports are displayed on a public map for other citizens to inform themselves. Furthermore, EOC personnel are able to access the Risk Evaluation Matrix (REM), a special dashboard that allows them to give even more information to citizens.

### **2.2.2 Need for open data**

Creating bespoke information systems at the beginning of disasters has been the norm [9]; however this means that disaster response organizations must become acclimated with the system at the same time that they are dealing with disaster situations. Researchers have shown the need to create open sourced crowdsourced emergency systems that provide open data [26]. The Riskmap System was created to fill that need.

## **2.3 Conquering Information Overload**

When researchers have tried using social media to track real-time disasters, they often suffer from information overload. For example, Meier states that the Haiti Crisis map was ‘constantly overwhelmed with the vast amount of information that needed to be monitored and processed’ and that the team never ‘managed to catch up’ with the backlog of social media activity [5].

It is not enough to create an advanced system for consuming citizen reports, it is also necessary to ensure that this system does not consume resources that are already scarce during a disaster event, for example the time of emergency workers [9]. Furthermore, it is also important to reduce the resources needed to create insights because if analyzing data is too difficult, then decision makers will make decisions without having fully analyzed the data [3].

Using computers to automatically make sense of disaster data has long been a goal in disaster informatics, but only recently have machine learning techniques become advanced enough to be implemented in production emergency systems [5]. Image recognition algorithms can provide summaries of objects and scenes found in user submitted photos [27, 28]. Natural language processing can estimate the probability that a textual document is overall negative or positive and thereby give EOCs a

shorthand way to summarize thousands of reports in short amounts of time [27, 29]. Finally, ensemble learning methods can learn relationships between disparate datasets and synthesize a single result [30].

In this work we will experiment with different machine learning techniques for image recognition, finally showing that transfer learning at the output layer can turn off the shelf multi—label classification algorithms into classifiers for flood image classification. For textual analysis, we will show the performance of bag of words, bigrams, and a combination of both techniques to classify report texts into heavy flooding/ no heavy flooding classes. Flood height will first be assessed as a raw numerical feature but will then be joined with nearby reports through a one dimensional convolutional filter in order to draw out temporal patterns. Finally, the output of these disparate techniques will be combined by using a small deep neural network to classify a report into one of two classes: ‘heavy flooding’ or ‘no heavy flooding’

Finally, the output of these disparate techniques will be combined by using a small deep neural network. In order to allow better interpretability, the most important labels from feature extraction machine learning algorithms are presented to the user so that they can understand what drove the machine’s choice.

## Chapter 3

# Previous Work for Machine Learning in Crisis Informatics

As discussed in Section 2.1.1, researchers have enviously eyed the panacea of information present in social media streams since the inception of the medium. Social media datasets are often very large, often hundreds of thousands or millions of data points can be collected during a single event. For example more than 1.5 million disaster related tweets were created during the 2011 Tohoku earthquake [31] and over 20 million during hurricane Sandy [5]. While all of these tweets concern the natural disaster and citizen’s reaction to the event, only a few have actionable intelligence that can help Emergency Operations Systems to better respond to an event— filtering out these actionable tweets and thus better understanding the ground truth is at the core of much research.

### 3.1 Passive Collection after Event

Because of the large number of data points and because of the difficulty of using humans to label all of the data set, researchers have turned to keyword searches to whittle down the volume of data [31]. Researchers then either hand label a small subset of the data or use keywords to aggregate data points and examine statistics on those aggregates.

### 3.1.1 Keyword Searches and Hand Labeling

Many studies of social media disaster data focused around post-event analysis using manual labeling. In [32] Starbird and Palen explore the uptake of the Tweek the Tweet (TtT) microsyntax, where citizens are encouraged to use a specific syntax in order to request or offer help during a crisis event. The adoption of the syntax by citizens on the ground was very low. Only 39 out of a total of 2,911 tweets in the TtT dataset originated within the affected areas; however, the authors saw many more tweets that were translated into the TtT syntax by other users. The authors also point out that social media enable new forms of volunteerism where humans can be used to manually ‘translate’ user tweets.

Other studies have analyzed social media behavior by using key word searches only and creating aggregate statistics. For example, Vieweg et al. state that they ‘reduced the data sets to those user streams that included more than three tweets containing the search terms’ in order to ‘make samples manageable’ [7]. The team then looked at easily machine readable features such as the inclusion of geotags.

## 3.2 Artificial Intelligence

While it is possible to gather some intelligence by using key words and digital volunteers to label data, artificial intelligence has two main advantages. Machine learning algorithms can handle much larger volumes of data than can be consumed by even a large team of people, and they can do it in a much shorter amount of time.

### 3.2.1 On Text Data

Nagy et al. used SentiWordNet, a lexical embedding for sentiment analysis, in order to classify tweets as mainly containing positive or negative feelings [29]. A dataset of 3698 tweets created during the 2010 San Bruno, CA fires was used in this study. The authors did manually label the tweets in order to find the performance of their method and found a precision score of 90% on a held out set. After validation, the



authors can use this process to classify tweets with little human interaction, allowing them to process much larger datasets.

In 2013, Chowdhury et al. used feature extraction to classify tweets into pre-incident, during-incident, and post-incident categories [33]. They showed the importance of treating crisis messages as distinct from other text based machine classification tasks. The precision score of this method was at least 96% [33].

Caragea et al. and Imran et al. compared the performance of Support Vector Machines (SVMs) and Convolutional Neural Networks (CNNs) at classifying tweets into two classes: informative, and not informative [34, 35]. The teams found that CNNs performed much better at the classification task because they were better able to learn the relationships between tokens and did not require much feature engineering in order to have good performance.

In addition to methods for classifying disaster messages, there has recently been work on creating textual datasets to help researchers conduct machine learning research. The Qatar Computing Research Institute has created the CrisisNLP datasets that contain thousands of tweets that have been human labeled [27].

### **3.2.2 On Image Data**

In the past decade there have been very promising results to using Convolutional Neural Networks for image recognition tasks, however training these large neural nets traditionally requires very large datasets. In 2014, the DeCAF team showed how to conduct transfer learning on deep neural nets in order to reduce the number of training images required without sacrificing performance [28]. Following this result, Nguyen et al. used transfer learning with an online component to classify social media disaster images into 3 classes: severe, mild, and little damage [36].

Another technique that researchers have used is the visual bag of words approach. In this method, each image is associated with a collection of labels for objects that are found in that scene. The collection of labels is then treated in the same way as text using a bag of words embedding scheme. Both humans and automatic means can be used to label images [37].

### 3.2.3 Ensemble Learning Models

The prospect of using many learning models and combine them has driven many research goals. Bagging, the practice of using many simple learners on different subsets of the training data has shown to be particularly useful [38]. Boosting is a related technique where an ensemble of simple classifiers are trained in succession, with data points misclassified by the  $n$ th classifier are weighed as more important for classifier  $n + 1$ . In a disaster data context, Furlanello et al. used boosting to train decision trees and geospatially predict the risk of tickborne illnesses [39].

#### Multimodal data

Ensemble models are not only attractive because they can increase precision on a single type of data, but also because they can enable classifiers to process many types of data. For example, Mouzannar et al. used two different CNNs to process image and text data. The team then used a variety of simple classifiers as the ensemble learners to produce a final result, classification into one of 6 classes [30]. In this manner, they were able to achieve higher than 90% accuracy with a dataset of 35,000 data points.

Researchers have also used neural networks as the ensemble learners. These models enable much more flexibility because the learner is able to encode a much more complex function and can therefore learn more information about the latent features between learners [40].

## 3.3 Challenges

### 3.3.1 Small Datasets

Although a limited number of larger datasets have recently become available, there has historically been a scarcity of training and validation data available for Deep learning models that are trained on small datasets tend to overfit on the training data and do not generalize well to the validation dataset [41, 27].

In many early studies only hundreds of data points were considered— combined

with the small size of those data points (for example, twitter microblogs of 140 or 280 characters) and effectively using deep learning becomes very difficult. For example [29] only uses 3,698 tweets in order to train their classifier.

### **3.3.2 Cold Start**

At the beginning of a disaster, there is not much data available in order to train a classifier.

### **3.3.3 Task Subjectivity**

Task subjectivity is an incredibly common issue [36, 3]. While most humans can agree on whether an object is or is not an apple, this task does not translate to defining if a picture indicates a severe event or a minor one. In other words, people’s perception of risk varies widely from region to region and from citizen to citizen [3].

Houses look different in different built environments, so cross location transfer might not work as well as we think it will.

### **Focus on technology rather than whole system design**

A series of UN case studies on six disaster information systems found that while engineering and system design were essential, it was the hidden wiring of support networks that allows for technology to succeed.

There have been some notable projects that attempt to provide complete systems that can be used for different disasters. Most notably are the Sahana and the Artificial Intelligence for Digital Response (AIDR) projects; however, both of these systems have faced trouble getting on the ground attention. The Sahana foundation suspended its on the ground disaster response team that helped to mobilize volunteers to respond to disasters [42].

An important message emerges from the case studies: an effective disaster information management system requires a good technological platform,

but also much more. Software programs for storing, sharing, and manipulating data for disasters are being developed or patched together at a steady pace, often in the aftermath of disasters. The real difficulty lies in anchoring these technological approaches in an appropriate institutional context where they are supported by relevant and effective operating procedures, agreed terminology and data labeling, and a shared awareness of the benefits of proper handling of disaster information. Clearly, a disaster information management system must be supported by accepted rules, procedures, and relationships that encourage, facilitate, and guide the production, sharing, and analysis and use of data in response to disaster. In these case studies, the institutional dimension—the hidden wiring—determined the effectiveness of the systems. [9]

# Chapter 4

## Methodology and Results

The Riskmap system allows citizens to easily submit disaster reports. From 2016 to date, the system has allowed the Urban Risk Lab at MIT (MIT-URL) to gather 2229 reports before, during, and after flood emergencies in Jakarta. Similarly the Riskmap platform has also gathered 356 reports in Chennai. Figure 4-1 demonstrates that these data points include traffic reports, indications that an area is unsafe, and advice for other citizens in the area. Images attached to reports include a wide variety of scenes, from daylight highways with cars and motorcycles to night time deserted alleys. The data points include not only textual and image data but also an estimated flood height.

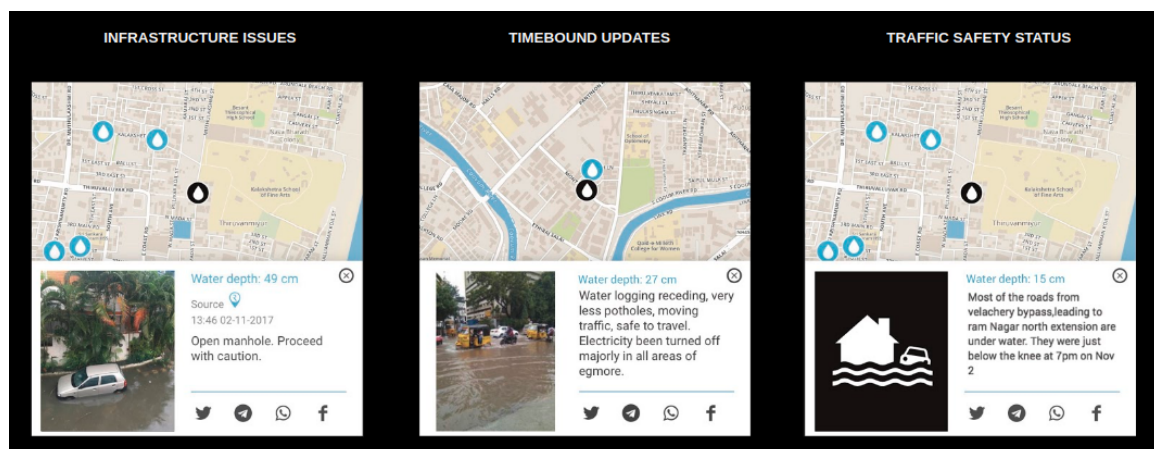


Figure 4-1: Representative reports of heavy flooding in Chennai during Nov. 2017 Monsoon

The disparate datasets contained in the Riskmap System motivate the creation of REACT in order to process and summarize results in real time.

## **4.1 System Design**

It is paramount for disaster systems to be highly available and scalable during events. The REACT system has been designed such that it is modular and ready to scale. A simple but expandable configuration file interface serves as a singleton for sharing global environment variables such as database connections and logging capabilities. The DataLoader interface allows for flexibility in the data source that is used, while the Labeler construct allows one to use different services to create embeddings of that data. Finally, any class that follows the Learner specification is able to train and validate on those embeddings.

### **4.1.1 Configuration**

A single configuration file allows for easy customization of the underlying training data. Figure 4-2 shows two default configurations that include all of the data from Chennai and Jakarta in 2017. Other configurations allow the opportunity to choose only those reports that include an image, or those that come from a specific social network.

### **4.1.2 Data Loaders**

Data Loaders are constructed by passing a configuration that implements the GenericConfig interface. They are then responsible for implementing methods that allow for retrieving the three kinds of data that the REACT system uses for prediction: text, image, and flood depth estimation. While the RiskmapLoader is the only Loader that is currently implemented, it was important to separate data loaders in order to make REACT ready for future change.

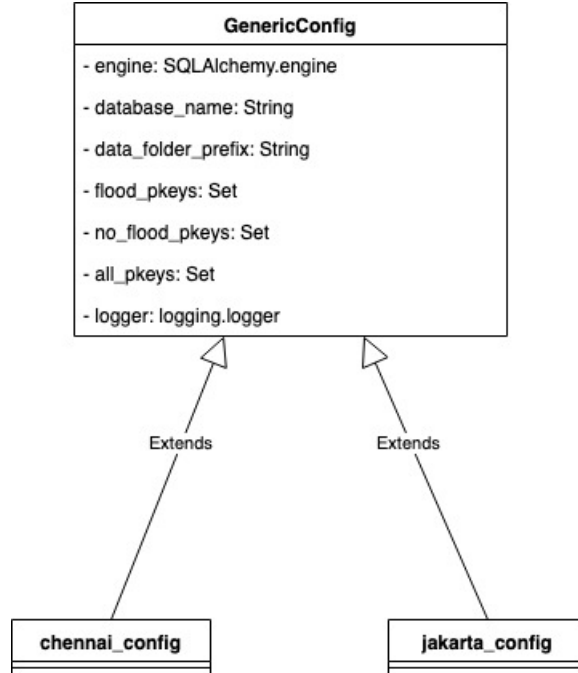


Figure 4-2: Configuration Abstraction

### 4.1.3 Labelers

Data embeddings, or labels, turn human recognizable data into feature vectors that can be used for machine learning. There are many choices for how to label the disaster data in REACT, as such any Labeler that implements the GenericLabeler interface can be used seamlessly in the system as shown in Figure 4-4. The AwsLabeler uses AWS Rekognition to create feature vectors, while the BowLabeler uses a bag of words approach to encode textual information. An IdentityLabeler is provided in order to facilitate the passing of raw features.

### 4.1.4 Learners

Different learning methods are represented by different implementations of the GenericLearner interface as shown in Figure 4-4. The perceptron algorithm and the Support Vector Machine method are implemented in REACT as simple linear classifiers. An IdentityLearner is also provided to act as a pass through in case raw features are desired.

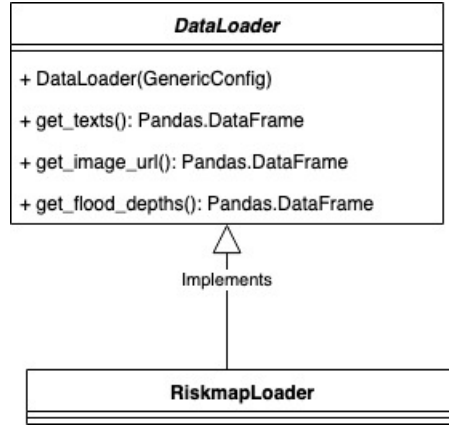


Figure 4-3: Adaptable Data Loaders

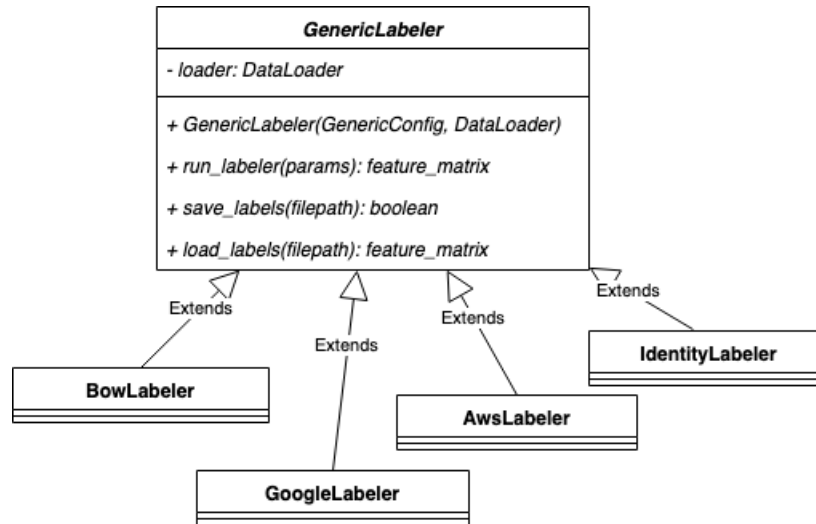


Figure 4-4: Many different labelers can be used to encode data in REACT

## 4.2 Ground Truth

We explored two different methods in order to decide whether a particular report was indicative of heavy flooding or not. We first classified a report as heavy flooding if it was submitted during a time range when we knew there to be heavy flooding in the corresponding city. These shall be referred to as time-classified. Although we expected this classification to be very coarse, we hoped that it would be specific enough to create an accurate predictor. In order to test this theory we also hand labeled reports by inspecting the images that accompanied them; these will be referred to as hand-classified.



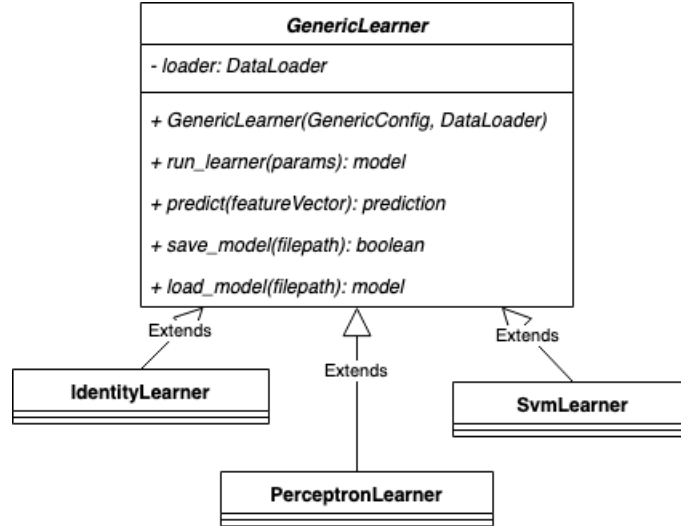


Figure 4-5: The Learner abstraction makes it easy to switch from one method to another

## 4.3 Text

As shown in Section 2.2, the Riskmap system allows citizens to provide a textual description to emergency managers. In Indonesia, most of the reports are provided in Bahasa, the local language; however, in Chennai all reports were submitted in English even though the system also supports Tamil. In both Chennai and Jakarta these reports are quite brief, with the longest reports having 140 characters. In this manner, they are quite similar to tweets which were initially 140 characters but this limit was doubled in 2017. Helpfully, this means that much of the work described in Section 3.2.1 applies to the Riskmap text corpus.

Table 4.1 contains a sample of ten reports that are indicative of those found in the Riskmap textual descriptions.

### 4.3.1 Preprocessing

We first remove test reports, which are reports submitted in order to ensure that the system is working. The following POSTGRESQL query was executed to remove reports that were only used to test the system:

```
SELECT    pkey ,
```

pkey	text
169	Waterlogging near cathedral road flyover
171	1st street Engineers avenue
173	Not that much water safe only
174	50cm water stagnant on the road
176	Water level rising slowly
177	Water logging
178	Model school road is completely flooded, with water almost knee deep
179	Heavy rain in West mambalam flood
180	Water on roads. Stay safe
182	4cm rainfall.. still continuing.. hope for safe .. dont come outside in night time
181	Luz signal flooded knee deep water

Table 4.1: A representative selection of report texts

```

text
FROM riskmap.all_reports
WHERE text IS NOT NULL
AND Length (text) > 0
AND text NOT similar TO '%%(T|t)(E|e)(S|s)(T|t)%%'
ORDER BY created_at;

```

We then use python to remove punctuation and split along whitespace, thus splitting the source text into individual words without any spaces.

```

def prepare_text(report_text):
    """
    returns a list of strings where each string is a different word
    """
    import string
    exclude = set(string.punctuation)
    s = "".join(ch for ch in inp if ch not in exclude )
    return s.lower().split()

```

### 4.3.2 Sentiment analysis

Since each report in the Chennai dataset includes a textual description in English, we could use off the shelf sentiment analysis to gauge how negatively citizens are feeling. It might be the case that a highly negative sentiment corresponds to heavy flooding and that a positive sentiment corresponds to lighter or no flooding. We can investigate the relation between a negative sentiment and heavy flooding by using conditional probability. We set the threshold for negative sentiment at .5 and then use the AWS Rekognition API in order to classify texts into heavy flooding when negative sentiment is greater than .5 and into light or no flooding otherwise.

We use bayes' rule in order to analyze the true positive rate— the probability that a report represents heavy flooding given a negative sentiment:

$$P(HeavyFlooding|negative) = \frac{P(negative|HeavyFlooding) * P(HeavyFlooding)}{P(negative)} = .65$$

The false positive rate, which is the probability that there is no heavy flooding given a negative sentiment is given by:

$$P(NoFlooding|negative) = \frac{P(negative|NoFlooding) * P(NoFlooding)}{P(negative)} = .34$$

These probabilities show that while there is some relation between a negative sentiment and flooding, it is not a very strong signal. Furthermore, there are no off the shelf sentiment analysis tools for the Indonesian language, so a model based on AWS Rekognition or Google Cloud Natural Language API would not translate to the Jakarta dataset.

### 4.3.3 Bag Of Words

While sentiment analysis might not be a strong enough signal of heavy flooding/no heavy flooding, our experiment shows that the textual data contains important information. In order to train a machine learning algorithm on textual data one must first create an embedding that maps natural language into feature vectors. There are many ways of creating embeddings as discussed in Section 3.2.1, but many of them require large datasets or do not support Indonesian. For example, word2vec is a popular embedding model that produces floating point vectors and has achieved remarkable performance; however, the size of its training vocabulary is 962,000 unique words [43]. It is possible to download a pre-trained word2vec model and use it to encode new texts, but such a pre-trained model doesn't exist for Indonesian. We could train it using a different dataset of Indonesian texts, but there is no guarantee that our domain specific words would have a good embedding after having trained with a different corpus.

The bag of words encoding is particularly attractive to the Riskmap dataset because it language agnostic and can therefore work on both the Chennai and Jakarta datasets. The bag of words approach to classifying texts consists of first creating a vocabulary that maps from a token  $t$  to a unique index  $i$ . Each report text is then encoded into a feature vector by setting the  $i$ th element to 1 if the token  $t$  exists in the report text [44].

The bag of words model correctly classifies 67 percent of reports in the Chennai corpus under 5 fold cross validation. Examining the data, we see that there are many instances of reports such as 'no flooding here' which are being misclassified because the embedding is not able to understand relationships between adjacent words.

### 4.3.4 Bigrams

Bigrams are an embedding that allows the separator to learn relationships between adjacent words. The vocabulary is created by using pairs of adjacent words, such that 'no flooding here' would turn into 2 tokens: 'no flooding' and 'flooding here'.

Embedding the text data from the Riskmap system into a bigram vector creates a very large vector (over 3 times the size of the unitary approach), and only improves accuracy by .02 on average, as such we chose not to use a bigram embedding.

## 4.4 Images

Visual cues are integral disaster mitigation because they allow Emergency Operations Centers (EOCs) to quickly assess the situation in different parts of the city. The Riskmap system gathered 2159 images in Jakarta and 143 in Chennai during 2017. While not every report has an image, every image contains a multitude of information that can help EOCs better understand the situation in different parts of the city. Because reports are submitted at different times and from different places the images accompanying them vary widely, from bright daylight scenes of puddles and water stagnation to barely illuminated nighttime pictures of heavily inundated alleyways. Appendix B-1 contains a representative sample of images labeled ‘heavy flooding’ from the Jakarta 2017 dataset. Appendix B-2 shows a sample of images that are labeled ‘no heavy flooding’.

### 4.4.1 Transfer Learning

Image classification as described in Section 3.2.2 traditionally uses a deep convolutional neural network and requires millions of images. Since both the Chennai and Jakarta datasets are quite small (<5000 images), it would not be feasible to create and train our own CNN. Transfer learning uses a pretrained image classifier trained on a different dataset in order to assign labels that the original network was not trained on. We used the Resnet18 architecture pretrained on ImageNet in order to experiment with transfer learning.

dataset	method	best validation acc.
Jakarta 2017	Full net	0.60
Jakarta 2017	Feature extractor	0.61
Chennai 2017	Full net	0.62
Chennai 2017	Feature extractor	0.62

#### 4.4.2 Using Machine Learning as a Service

Results from popular machine learning as a service providers have a ‘flooding’ label whereas publicly available pretrained networks do not. As Google and Amazon Web Services (AWS) improve their own models, a classifier based on these results will also improve without the need to invest large compute resources.

##### AWS Image Rekognition

The boto3 python library is used to create a detect\_labels API call to AWS Rekognition, which then responds with a list of (label, confidence\_score) tuples. For example, AWS provides 1,319 unique labels for the Chennai 2017 dataset and 2,436 for the Jakarta 2017 images. For example, the heavy flooding report image with the unique identifier 272 shown in Figure 4-6 is labeled with upwards of 99% confidence as containing ‘Nature’, ‘Human’, and ‘Flood’<sup>1</sup>.

The report image with id 1 from the Jakarta 2017 dataset was not taken during heavy flooding. It depicts a drain that needs to be cleared ahead of the monsoon season. Labeling the image shows that the labels are quite different and that AWS correctly identifies the image as a ditch.

##### Google Cloud Vision AI

Figure 4-8 shows report image 272 as labeled by the Google Cloud Vision AI API<sup>2</sup>.

---

<sup>1</sup>the ‘Instances’ parameter is not included here for readability, but it contains bounding boxes for certain objects. It is unused in the training of the classifier.

<sup>2</sup>The ‘mid’ and ‘topicality’ properties have been redacted for brevity



```
[{'Confidence': 99.967,
  'Name': 'Nature',
  'Parents': []},
 {'Confidence': 99.811,
  'Name': 'Human',
  'Parents': []},
 {'Confidence': 99.735,
  'Name': 'Flood',
  'Parents': [{'Name': 'Nature'}]},
 {'Confidence': 41.318,
  'Name': 'Rural',
  'Parents': [{'Name': 'Countryside'},
               {'Name': 'Outdoors'},
               {'Name': 'Nature'}]},
 {'Confidence': 41.318,
  'Name': 'Outdoors',
  'Parents': []}]
```

Figure 4-6: Report image 272 and its top 5 AWS provided labels from Chennai 2017 Dataset, Riskmap India



```
[{'Confidence': 99.723,
  'Name': 'Ditch',
  'Parents': []},
 {'Confidence': 91.929,
  'Name': 'Path',
  'Parents': []},
 {'Confidence': 91.877,
  'Name': 'Soil',
  'Parents': []},
 {'Confidence': 91.503,
  'Name': 'Vegetation',
  'Parents': [{'Name': 'Plant'}]},
 {'Confidence': 91.503,
  'Name': 'Plant',
  'Parents': []}]
```

Figure 4-7: Report image 1 and its top 5 AWS provided labels from Jakarta 2017 Dataset, Petabencana

Whereas the top 5 labels from AWS are very distinct between Jakarta report 1 and Chennai report 272, the label annotations are quite similar for the response from the Google API as shown in Figure 4-9

## Results

When the dataset size is limited and it is difficult to gather new data, it is possible to estimate future true error rates by using cross validation. Cross validation consists of splitting the dataset into  $k$  many groups. The learning model is then trained on  $k-1$  groups and tested against the held out group. The average error over all  $k$  groups is

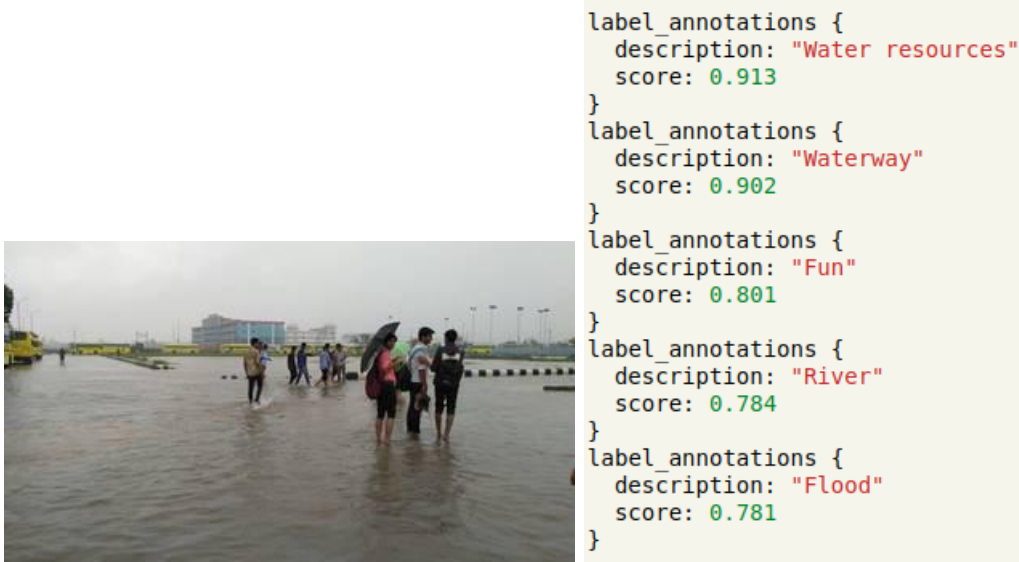


Figure 4-8: Report image 272 and its top 5 Google Cloud Vision AI provided labels from Chennai 2017 Dataset, Riskmap India

then taken as an estimate of the true error rate of the model.

With a balanced hold out set comprising of ten percent of the data points, the Support Vector Machine (SVM) linear classifier achieves a score upwards of 70 as shown in Table 4.2. Labels from AWS Rekognition were used because AWS returned many more labels than Google did for the same image. More labels means that there are more dimensions for the classifier to differentiate between heavy flooding and no heavy flooding images.

Table 4.2: Image Classification Accuracy

Dataset	Method	Validation Method	Validation Acc.
Jakarta 2017	Perceptron	held out validation set	0.70
Jakarta 2017	SVM	held out validation set	0.71
Chennai 2017	Perceptron	five fold cross validation	0.83
Chennai 2017	SVM	five fold cross validation	0.84

#### 4.4.3 Visual Bag of Words

[45]





Figure 4-9: Report image 1 and its top 5 Google Cloud Vision AI provided labels from Jakarta 2017 Dataset, Petabencana

## 4.5 Flood Height

### 4.5.1 Raw

### 4.5.2 Normalized

## 4.6 Ensemble with Neural Net

In [40], Jordan and Jacobs showed that neural networks can be effectively used to vote between different classifiers that are effective only in their specific domain of the overall space. They present a case for using the Estimation Maximization (EM) algorithm for optimizing the weights of the neural network. Hierarchical mixtures of experts and the EM algorithm [40] + bishop p. 673 [46]

It has been shown that ensemble learning methods that pick between several experts can provide accurate prediction even if the experts have low accuracy. By combining weak experts, we were able to achieve upwards of 85% accuracy on a

randomly sample held out validation set comprised of ten percent of the data points.

.74 all data .77 with picture

with pic plus report

#### **4.6.1 Validation Scores**

# Chapter 5

## Future Work

### 5.1 Image Data

#### 5.1.1 Using transfer learning

As the time goes on and the Riskmap System registers more flood events, more data will be collected, thereby increasing the amount of training data available. With more training data, transfer learning will become more and more accurate.

### 5.2 Text Data

#### **word2vec**

As outlined previously, we did not experiment with word2vec embeddings because of the difficulty of handling multilanguage datasets; however, it would be possible to create a word2vec embedder for Indonesian by using publicly available texts such as Wikipedia. The short coming of using Indonesian Wikipedia is that there are only 500 thousand articles compared to 5.9 million in English Wikipedia.

## 5.3 Location Information

Location information was not used because we aimed to create a per report heuristic for the whole city rather than concentrate on spatially disparate areas. In order to use spatial data it would be necessary to counteract the sampling bias present in the dataset. Richer neighborhoods have much higher rates of ownership of smart phones, which means citizens in those areas are more likely to report flooding than poorer areas— even if flooding is accruing at the same levels in both neighborhoods.

## 5.4 Ensemble Methods

### 5.4.1 Bigger network

Our current bagging network is very small so as to reduce over fitting on the small datasets we currently have. As the Riskmap System collects more data, it is likely that we can use a larger network with a decreased risk of over fitting.

### 5.4.2 Data Augmentation

It might be possible to use generative adversarial learning in order to create new example reports that fit into the distribution of user submitted reports. This would increase the size of the dataset without having to deploy the Riskmap system to more locations. One of the challenges related to generating new reports would be the multi-language problem and validating that generated report texts in other languages fit the distribution of user submitted reports in that language.

## Chapter 6

## Conclusion



# Appendix A

## Tables

Place tables here.





# Appendix B

## Figures

Figure B-1: Examples of Jakarta 2017 reports gathered by the Riskmap System labeled 'heavy flooding'



(a) Dark Alley



(b) Daylight street



(c) Heavy flooding and heavy traffic



(d) Car submerged in water

Figure B-2: Examples of Jakarta 2017 reports gathered by the Riskmap System labeled 'no heavy flooding'



(a) Small puddle



(b) Drain in need of cleaning



(c) Stagnant water on the road



(d) Trash by the roadside



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