

```
-- Week 2, Activity 11:
-- a) Add a unary minus operator (negation) to the language.
-- b) Add comparison operators to the language with a lower priority than the
--     additive operators. The result of a comparison must be 1 (for true) or 0.
--     (The set of comparison operators comprises <, >, >=, <=, ==, and !=. Mind
--     the possessiveness of LPeg).
```

```
local lpeg = require "lpeg"
local pt = require "pt"
local loc = lpeg.locale()
```

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-- FRONTEND: PARSER
-- Our frontend is a parser that gets a source code as input and produces an
-- intermediate representation of the program in an AST
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```
-- Initial patterns:
local spc = loc.space^0
local vazio = -lpeg.P(1)
local sinal = lpeg.S("+~")^-1
local hexdig = lpeg.R("AF", "af", "09")
local hexpre = lpeg.P("0") * lpeg.S("Xx")
local opAS = lpeg.C(lpeg.S("+~")) * spc
local opMD = lpeg.C(lpeg.S("*/%")) * spc
local opE = lpeg.C(lpeg.P("^")) * spc
local lt = lpeg.C(lpeg.P("<")) * spc
local lte = lpeg.C(lpeg.P("<=")) * spc
local gt = lpeg.C(lpeg.P(">")) * spc
local gte = lpeg.C(lpeg.P(">=")) * spc
local eq = lpeg.C(lpeg.P("==")) * spc
local neq = lpeg.C(lpeg.P("!=")) * spc
local opRel = (lte + gte + lt + gt + eq + neq) * spc
local OP = lpeg.P("(") * spc
local CP = lpeg.P(")") * spc
```

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-- Function that get's a number and return a node of AST
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```
function node(numero)
    return {
        tag = "numero",
        val = numero
    }
end
```

```
-- What is a number? Note that an AST node is returned
```

```
local decnum = ((sinal * loc.digit^1) / tonumber) / node * spc
local hexnum = ((sinal * hexpre * hexdig^1) / tonumber) / node * spc
local numero = spc * (hexnum + decnum) * spc
```

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-- Function to fold a list and convert the list to an AST:
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```
-- input: list: {n1, "+", n2, "+", n3, ...}
-- output: AST: {...{ op = "+", e1 = {op = "+", e1 = n1, e2 = n2}, e2 = n3}...}
```

```
-- foldBinEsq = operators with left-associativity
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```
local function foldBinEsq(list)
    local tree = list[1]
    for i = 2, #list, 2 do
        tree = { tag = "binop", e1 = tree, op = list[i], e2 = list[i + 1] }
```

```

    end
    return tree
end

-- foldBinDir = operator with right-associativity
local function foldBinDir(list)
    local tree = list[#list]
    for i = #list - 1, 2, -2 do
        tree = { tag = "binop", e1 = list[i - 1], op = list[i], e2 = tree }
    end
    return tree
end

-- Our grammar for mathematic expression:
local factor = lpeg.V"factor"
local pot = lpeg.V"pot"
local term = lpeg.V"term"
local exp = lpeg.V"exp"
local rel = lpeg.V"rel"

grammar = lpeg.P{"rel",
    factor = spc * numero + OP * exp * CP,
    pot = lpeg.Ct(spc * factor * (opE * factor)^0) / foldBinDir,
    term = lpeg.Ct(spc * pot * (opMD * pot)^0) / foldBinEsq,
    exp = lpeg.Ct(spc * term * (opAS * term)^0) / foldBinEsq,
    rel = lpeg.Ct(spc * exp * (opRel * exp)^0) / foldBinEsq
}
grammar = spc * grammar * vazio

-- The parser per si:
local function parse(input)
    return grammar:match(input)
end

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-- BACKEND: CODE GENERATOR
-- Our backend is a code generator that get's an AST and generate the final
-- output of the compiler
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-- Function to add opcodes:
local function addCode(state, op)
    local code = state.code
    code[#code + 1] = op
end

-- Operators:
local ops = {["+"] = "add", ["-"] = "sub",
    ["*"] = "mul", ["/"] = "div", ["%"] = "rem",
    ["^"] = "exp",
    ["<="] = "lte", [">="] = "gte", ["=="] = "eq", ["!="] = "ne",
    [ "> "] = "gt", [ "< "] = "lt"}

-- Function to specify the operations by type (tag) of node:
local function codeExp(state, ast)
    if ast.tag == "numero" then
        addCode(state, "push")
    end
end

```

```

        addCode(state, ast.val)
    elseif ast.tag == "binop" then
        codeExp(state, ast.e1)
        codeExp(state, ast.e2)
        addCode(state, ops[ast.op])
    else
        error("invalid tree")
    end
end
end

```

```

-- The compiler per si:
local function compile(ast)
    local state = { code = {} }
    codeExp(state, ast)
    return state.code
end

```

-- INTERPRETER

-- Receives the intermediate code produced by the compiler and empty stack and,

-- when finished, leaves the result of the expression on the top of the stack.

```

-- The interpreter:
local function run(code, stack)
    local pc = 1 -- program counter
    local top = 0 -- top of stack
    while pc <= #code do
        if code[pc] == "push" then
            pc = pc + 1
            top = top + 1
            stack[top] = code[pc]
        elseif code[pc] == "add" then
            stack[top - 1] = stack[top - 1] + stack[top]
            top = top - 1
        elseif code[pc] == "sub" then
            stack[top - 1] = stack[top - 1] - stack[top]
            top = top - 1
        elseif code[pc] == "mul" then
            stack[top - 1] = stack[top - 1] * stack[top]
            top = top - 1
        elseif code[pc] == "div" then
            stack[top - 1] = stack[top - 1] / stack[top]
            top = top - 1
        elseif code[pc] == "rem" then
            stack[top - 1] = stack[top - 1] % stack[top]
            top = top - 1
        elseif code[pc] == "exp" then
            stack[top - 1] = stack[top - 1] ^ stack[top]
            top = top - 1
        elseif code[pc] == "gte" then
            stack[top - 1] = (stack[top - 1] >= stack[top]) and 1 or 0
            top = top - 1
        elseif code[pc] == "lte" then
            stack[top - 1] = (stack[top - 1] <= stack[top]) and 1 or 0
            top = top - 1
        elseif code[pc] == "gt" then
            stack[top - 1] = (stack[top - 1] > stack[top]) and 1 or 0
            top = top - 1
        end
        pc = pc + 1
    end
end

```

```
elseif code[pc] == "lt" then
    stack[top - 1] = (stack[top - 1] < stack[top]) and 1 or 0
    top = top - 1
elseif code[pc] == "eq" then
    stack[top - 1] = (stack[top - 1] == stack[top]) and 1 or 0
    top = top - 1
elseif code[pc] == "ne" then
    stack[top - 1] = (stack[top - 1] ~= stack[top]) and 1 or 0
    top = top - 1
else
    error("unknown instruction")
end
pc = pc + 1
end
end
```

-- Tests:

-- Get's the source code (only a number for now):

```
local input = io.read("a")
```

-- The frontend (parser) generates as AST:

```
local ast = parse(input)
```

```
print(pt.pt(ast))
```

-- The backend (code generator) compiles AST to intermediate code:

```
local code = compile(ast)
```

```
print(pt.pt(code))
```

-- We run the interpreter passing as arguments the

-- intermediate code and the stack:

```
local stack = {}
```

```
run(code, stack)
```

```
print(stack[1])
```