

```
-- Week 2, Activity 9:
-- Adding more operators.
-- a) Add a remainder operator (%) to the language with the same priority as the
--    multiplicative operators.
-- b) Add an exponential operator (^) to the language with a higher priority
--    than the multiplicative operators.
```

```
local lpeg = require "lpeg"
local pt = require "pt"
local loc = lpeg.locale()
```

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-- FRONTEND: PARSER
-- Our frontend is a parser that gets a source code as input and produces an
-- intermediate representation of the program in an AST
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```
-- Initial patterns:
local spc = loc.space^0
local vazio = -lpeg.P(1)
local sinal = lpeg.S("+~")^-1
local hexdig = lpeg.R("AF", "af", "09")
local hexpre = lpeg.P("0") * lpeg.S("Xx")
local opAS = lpeg.C(lpeg.S("+~")) * spc
local opMD = lpeg.C(lpeg.S("*/%")) * spc
local opE = lpeg.C(lpeg.S("^")) * spc
```

```
-- Function that get's a number and return a node of AST
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```
function node(numero)
    return {
        tag = "numero",
        val = numero
    }
end
```

```
-- What is a number? Note that an AST node is returned
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```
local decnum = ((sinal * loc.digit^1) / tonumber) / node * spc
local hexnum = ((sinal * hexpre * hexdig^1) / tonumber) / node * spc
local numero = spc * (hexnum + decnum) * spc
```

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-- Function to fold a list and convert the list to an AST:
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```
-- input: list: {n1, "+", n2, "+", n3, ...}
-- output: AST: {...{ op = "+", e1 = {op = "+", e1 = n1, e2 = n2}, e2 = n3}...}
```

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-- foldBinEsq = operators with left-associativity
```

```
local function foldBinEsq(list)
    local tree = list[1]
    for i = 2, #list, 2 do
        tree = { tag = "binop", e1 = tree, op = list[i], e2 = list[i + 1] }
    end
    return tree
end
```

```
-- foldBinDir = operator with right-associativity
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```
local function foldBinDir(list)
    local tree = list[#list]
    for i = #list - 1, 2, -2 do
        tree = { tag = "binop", e1 = list[i - 1], op = list[i], e2 = tree }
    end
end
```

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    end
    return tree
end

```

```

-- Exponentials, Multiplications and Summations:
local pot = lpeg.Ct(spc * numero * (opE * numero)^0) / foldBinDir
local term = lpeg.Ct(spc * pot * (opMD * pot)^0) / foldBinEsq
local exp = lpeg.Ct(spc * term * (opAS * term)^0) / foldBinEsq

```

```

-- The parser per si:
local function parse(input)
    return exp:match(input)
end

```

```

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-- BACKEND: CODE GENERATOR
-- Our backend is a code generator that get's an AST and generate the final
-- output of the compiler
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-- Function to add opcodes:
local function addCode(state, op)
    local code = state.code
    code[#code + 1] = op
end

```

```

-- Operators:
local ops = { ["+"] = "add", ["-"] = "sub",
              ["*"] = "mul", ["/"] = "div", [%] = "rem",
              ["^"] = "exp"}

```

```

-- Function to specify the operations by type (tag) of node:
local function codeExp(state, ast)
    if ast.tag == "numero" then
        addCode(state, "push")
        addCode(state, ast.val)
    elseif ast.tag == "binop" then
        codeExp(state, ast.e1)
        codeExp(state, ast.e2)
        addCode(state, ops[ast.op])
    else
        error("invalid tree")
    end
end

```

```

-- The compiler per si:
local function compile(ast)
    local state = { code = {} }
    codeExp(state, ast)
    return state.code
end

```

```

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-- INTERPRETER
-- Receives the intermediate code produced by the compiler and empty stack and,

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-- when finished, leaves the result of the expression on the top of the stack.
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-- The interpreter:
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```
local function run(code, stack)
    local pc = 1 -- program counter
    local top = 0 -- top of stack
    while pc <= #code do
        if code[pc] == "push" then
            pc = pc + 1
            top = top + 1
            stack[top] = code[pc]
        elseif code[pc] == "add" then
            stack[top - 1] = stack[top - 1] + stack[top]
            top = top - 1
        elseif code[pc] == "sub" then
            stack[top - 1] = stack[top - 1] - stack[top]
            top = top - 1
        elseif code[pc] == "mul" then
            stack[top - 1] = stack[top - 1] * stack[top]
            top = top - 1
        elseif code[pc] == "div" then
            stack[top - 1] = stack[top - 1] / stack[top]
            top = top - 1
        elseif code[pc] == "rem" then
            stack[top - 1] = stack[top - 1] % stack[top]
            top = top - 1
        elseif code[pc] == "exp" then
            stack[top - 1] = stack[top - 1] ^ stack[top]
            top = top - 1
        else
            error("unknown instruction")
        end
        pc = pc + 1
    end
end
```

```
-- Tests:
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-- Get's the source code (only a number for now):
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```
local input = io.read("a")
```

```
-- The frontend (parser) generates as AST:
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```
local ast = parse(input)
```

```
print(pt.pt(ast))
```

```
-- The backend (code generator) compiles AST to intermediate code:
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```
local code = compile(ast)
```

```
print(pt.pt(code))
```

```
-- We run the interpreter passing as arguments the intermediate code and AST:
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```
local stack = {}
```

```
run(code, stack)
```

```
print(stack[1])
```