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-- Week 2, Activity 10:
-- Parenthesized Expressions

local lpeg = require "lpeg"
local pt = require "pt"
local loc = lpeg.locale()

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-- FRONTEND: PARSER
-- Our frontend is a parser that gets a source code as input and produces an
-- intermediate representation of the program in an AST
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-- Initial patterns:
local spc = loc.space^0
local vazio = -lpeg.P(1)
local sinal = lpeg.S("+~")^-1
local hexdig = lpeg.R("AF", "af", "09")
local hexpre = lpeg.P("0") * lpeg.S("Xx")
local opAS = lpeg.C(lpeg.S("+~")) * spc
local opMD = lpeg.C(lpeg.S("*/%")) * spc
local opE = lpeg.C(lpeg.S("^")) * spc
local OP = lpeg.P("(") * spc
local CP = lpeg.P(")") * spc

-- Function that get's a number and return a node of AST
function node(numero)
    return {
        tag = "numero",
        val = numero
    }
end

-- What is a number? Note that an AST node is returned
local decnum = ((sinal * loc.digit^1) / tonumber) / node * spc
local hexnum = ((sinal * hexpre * hexdig^1) / tonumber) / node * spc
local numero = spc * (hexnum + decnum) * spc

-- Function to fold a list and convert the list to an AST:
-- input: list: {n1, "+", n2, "+", n3, ...}
-- output: AST: {...{ op = "+", e1 = {op = "+", e1 = n1, e2 = n2}, e2 = n3}...}

-- foldBinEsq = operators with left-associativity
local function foldBinEsq(list)
    local tree = list[1]
    for i = 2, #list, 2 do
        tree = { tag = "binop", e1 = tree, op = list[i], e2 = list[i + 1] }
    end
    return tree
end

-- foldBinDir = operator with right-associativity
local function foldBinDir(list)
    local tree = list[#list]
    for i = #list - 1, 2, -2 do
        tree = { tag = "binop", e1 = list[i - 1], op = list[i], e2 = tree }
    end
    return tree
end
```

end

-- Our grammar:

```
local factor = lpeg.V"factor"
local pot = lpeg.V"pot"
local term = lpeg.V"term"
local exp = lpeg.V"exp"
```

```
grammar = lpeg.P{"exp",
  factor = spc * numero + OP * exp * CP,
  pot = lpeg.Ct(spc * factor * (opE * factor)^0) / foldBinDir,
  term = lpeg.Ct(spc * pot * (opMD * pot)^0) / foldBinEsq,
  exp = lpeg.Ct(spc * term * (opAS * term)^0) / foldBinEsq
}
grammar = spc * grammar * vaziao
```

-- The parser per si:

```
local function parse(input)
  return grammar:match(input)
end
```

-- BACKEND: CODE GENERATOR

-- Our backend is a code generator that get's an AST and generate the final
-- output of the compiler

-- Function to add opcodes:

```
local function addCode(state, op)
  local code = state.code
  code[#code + 1] = op
end
```

-- Operators:

```
local ops = {[ "+" ] = "add", [ "-" ] = "sub",
  [ "*" ] = "mul", [ "/" ] = "div", [ "%" ] = "rem",
  [ "^" ] = "exp" }
```

-- Function to specify the operations by type (tag) of node:

```
local function codeExp(state, ast)
  if ast.tag == "numero" then
    addCode(state, "push")
    addCode(state, ast.val)
  elseif ast.tag == "binop" then
    codeExp(state, ast.e1)
    codeExp(state, ast.e2)
    addCode(state, ops[ast.op])
  else
    error("invalid tree")
  end
end
```

-- The compiler per si:

```
local function compile(ast)
  local state = { code = {} }
  codeExp(state, ast)
```

```

    return state.code
end

```

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-- INTERPRETER
-- Receives the intermediate code produced by the compiler and empty stack and,
-- when finished, leaves the result of the expression on the top of the stack.
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-- The interpreter:

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local function run(code, stack)
    local pc = 1 -- program counter
    local top = 0 -- top of stack
    while pc <= #code do
        if code[pc] == "push" then
            pc = pc + 1
            top = top + 1
            stack[top] = code[pc]
        elseif code[pc] == "add" then
            stack[top - 1] = stack[top - 1] + stack[top]
            top = top - 1
        elseif code[pc] == "sub" then
            stack[top - 1] = stack[top - 1] - stack[top]
            top = top - 1
        elseif code[pc] == "mul" then
            stack[top - 1] = stack[top - 1] * stack[top]
            top = top - 1
        elseif code[pc] == "div" then
            stack[top - 1] = stack[top - 1] / stack[top]
            top = top - 1
        elseif code[pc] == "rem" then
            stack[top - 1] = stack[top - 1] % stack[top]
            top = top - 1
        elseif code[pc] == "exp" then
            stack[top - 1] = stack[top - 1] ^ stack[top]
            top = top - 1
        else
            error("unknown instruction")
        end
        pc = pc + 1
    end
end
end

```

```

-- Tests:
-- Get's the source code (only a number for now):
local input = io.read("a")

```

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-- The frontend (parser) generates as AST:
local ast = parse(input)
print(pt.pt(ast))

```

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-- The backend (code generator) compiles AST to intermediate code:
local code = compile(ast)
print(pt.pt(code))

```

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-- We run the interpreter passing as arguments the intermediate code and AST:
local stack = {}
run(code, stack)
print(stack[1])

```

