18.01 EXAM 1 SEPTEMBER 18, 2003

Name:	_	
	Problem 1: /20	
	Problem 2: /25	
	Problem 3: /10	
	Problem 4: /20	
	Problem 5: /15	
	Problem 6: /10	
Please write the hour of your recitation. Hour:	Total: /100	

Instructions: Please write your name at the top of every page of the exam. The exam is closed book, calculators are not allowed, but you are allowed to use your prepared index card. You will have approximately 50 minutes for this exam. The point value of each problem is written next to the problem – use your time wisely. Please show all work, unless instructed otherwise. Partial credit will be given only for work shown.

You may use either pencil or ink. If you have a question, need extra paper, need to use the restroom, etc., raise your hand.

Date: Spring 2001.

Name:	Problem 1:	_ /20
Problem 1 (20 points) Use the limit definition of the for all points $x > 0$. Show all work.	derivative to compute the derivative of $y =$	$\frac{1}{x^2}$

Name:	Problem 2:	/25
Problem 2 (25 points) The point $P = (0,1)$ lies on two disting equation $y = x^2 + 2$. Find the equations of both tangent line answer.		
Extra credit (5 points) Let $Q = (x_0, y_0)$ and $R = (x_1, y_1)$ be		
above. There is a unique point $S = (x_2, y_2)$ which lies on both	oth the tangent line at Q and on the	;

tangent line at R. Show that for every pair of distinct points Q and R on the parabola, $2x_2 = x_1 + x_2$,

i.e., the line passing through S parallel to the y-axis bisects the line segment QR.

Name:	Problem 3:	/10

Problem 3(10 points) For each of the following functions, compute the derivative. Show all work, including each step in your derivation, but you do not need to state the rules you are using. Circle the final answer.

(a)(2 points)
$$y = \frac{1}{\sqrt{1+x^4}}$$

(b)(2 points)
$$y = x \ln(x) + \frac{1}{e^{-x}}$$

(c)(3 points)
$$y = (1 + x^{1000})^{\frac{1}{1000}}$$

(d)(3 points)
$$y = 10^x + \log_{10}(x^2 - x)$$

Name:		Problem 4:		_ /20	
Duahlam	$4(20 \text{ points})$ The point $T = (-4\sqrt{10} - \sqrt{10})$	ing on the ellings with as	wation		

Problem 4(20 points) The point $T = (\frac{-4\sqrt{10}}{5}, \sqrt{10})$ lies on the ellipse with equation $9(x+y)^2 + (x-y)^2 = 36$.

Using implicit differentiation, determine the equation of the tangent line to the ellipse at the point T; do not simply find the slope of the tangent line, you must write the equation of the tangent line. Show all work and circle the final answer.

Name:	Problem 5:	/15
Problem 5 (15 points) Let $u(x) = xe^{-x}$.		
(a)(5 points) Find the first, second and third deriva and circle the answers.	tives of $u(x)$ with respect to x . Show a	ll work
and effect the answers.		
(b) (10 points) Find a formula for the n^{th} derivative you do not need to <i>prove</i> your answer by induction. notation (depending on whether n is even or odd), o n odd.	In writing your final answer either use	e brace

Name:	Problem 6: /	10
after t seconds is given by	d from the edge of a cliff so that the height $s(t)$ in meters $s(t) = 80 - 5t^2$.	
(a)(5 points) Find the velocity v_f of the $t > 0$. Show all work and circle the final a	stone when it strikes the ground, i.e., when $s(t)=0$ and answer.	
(b)(5 points) Determine at what height final answer.	the stone has velocity $\frac{1}{2}v_f$. Show all work and circle the	