18.01 EXAM 4 NOVEMBER 4, 2003

Name:	_	
	Problem 1:	/25
	Problem 2:	/25
	Problem 3:	/25
	Problem 4:	/25
Please write the hour of your recitation.	TT-4-1.	/100
Hour:	Total:	/100
Instructions: Please write your name at the top book, calculators are not allowed, but you are allowed approximately 50 minutes for this exam. The the problem – use your time wisely. Please show all will be given only for work shown.	wed to use your prepared index e point value of each problem is	card. You will written next to
You may use either pencil or ink. If you have a quest etc., raise your hand.	tion, need extra paper, need to u	se the restroom
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Date: Fall 2003.

Name:	Problem 1:
Problem 1(25 points) (a):(20 points) Find the volume of the solid of revolution the region in the first quadrant of the xy-plane bounded by the solid of the solid of revolution the region in the first quadrant of the xy-plane bounded by the solid of th	
$y = h \left(\frac{x}{r}\right)^3$.	
Here r and h are positive constants.	
(b):(5 points) This solid is contained in a cylinder with bas of the volume of the cylinder is taken up by the solid in (a)?	=

/25

Name:	Problem 2:	_ /25
Problem 2 (25 points) Compute the surface area of the	he surface of revolution obtained by revolving	ng
about the y -axis the curve,		

$$y = \frac{1}{2}x^2, \ 0 \le x \le 1.$$

Name:	Problem 3:	/25

Problem 3(25 points)

(a): (10 points) Sketch the curve with polar equation,

$$r = \sin(2\theta), \ 0 \le \theta \le \frac{\pi}{2}.$$

In particular, label the following on your graph,

- (i) in which quadrant or quadrants the curve is contained,
- (ii) the endpoints of the curve,
- (iii) the two slopes of the tangent lines at the endpoints of the curve,
- (iv) and the angle or angles θ at which $r(\theta)$ is a maximum.

(b):(15 points) Compute the area of the region enclosed by the curve in (a). As a hint, recall the half-angle formulas,

$$\begin{cases}
\cos^2\left(\frac{\alpha}{2}\right) &= \frac{1}{2}(1+\cos(\alpha)), \\
\sin^2\left(\frac{\alpha}{2}\right) &= \frac{1}{2}(1-\cos(\alpha)).
\end{cases}$$

Name:			

Problem 4: ______ /25

Problem 4(25 points)

(a):(15 points) A curve is given by parametrically by,

$$\begin{cases} x = \cos(t) + t\sin(t), \\ y = \sin(t) - t\cos(t), \end{cases} 0 \le t \le \pi.$$

Compute the arclength of the parametrized curve.

(b):(10 points) Let f(x) be a solution of the differential equation with side equation,

$$\frac{dy}{dx} = \sqrt{x^2 - 1}, \ y(2) = 0,$$

on the interval $2 \le x \le 3$. Compute the arclength of the curve y = f(x) on the interval $2 \le x \le 3$. DO NOT ATTEMPT TO SOLVE THE DIFFERENTIAL EQUATION!