## 18.01 EXAM 5 NOVEMBER 20, 2003

Name:	-	
	Problem 1:	/20
	Problem 2:	/15
	Problem 3:	/25
	Problem 4:	/20
	Problem 5:	/20
Please write the hour of your recitation.	Total:	/100
Hour:		
Instructions: Please write your name at the top of book, calculators are not allowed, but you are allow have approximately 50 minutes for this exam. The the problem – use your time wisely. Please show all will be given only for work shown.  You may use either pencil or ink. If you have a questi etc., raise your hand.	ved to use your prepared index capoint value of each problem is wrork, unless instructed otherwise.	ord. You will eitten next to Partial credit

Date: Fall 2003.

Name:	Problem 1:	/20
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**Problem 1**(20 points) Compute the partial fraction decomposition of  $f(z) = \frac{1}{(z^2-1)^2}$ . Show all your work.

**Hint**: Use Heaviside's method to determine 2 of the 4 undetermined coefficients. Is f(z) an even function or an odd function? What does this tell you about the 2 remaining coefficients? Combine this with a substitution to determine the 2 remaining coefficients (or use any other method you like to determine the 2 coefficients).

Name:	/1-
<b>Problem 2</b> (15 points) Use polynomial divisi $x > 1$ ).	on to compute the following indefinite integral (for
- '	$\frac{x^3-1}{(x-1)^2}dx.$
Show all your work.	

Name:	Problem 3:	/25
Problem 3(25 points) This problem computes a re (a)(10 points): Compute the derivative of sec <sup>n</sup> -using a trigonometry identity in order to express t your work.	$-2(\theta)\tan(\theta)$ . Eliminate $\tan(\theta)$ from your answer	•
(b)(10 points): Write your answer from (a) in the	ne form of an integral identity, and then solve for	:
$\int \sec^n(\theta) d\theta$ to find a recursive formula of the form	ſ	
$\int \sec^n(\theta) d\theta = F(\sec(\theta), \tan\theta)$	$\operatorname{h}(\theta) + A \int \sec^{n-2}(\theta) d\theta.$	
Show all your work.		
(c)(5 points): Use your recursive formula to comwork.	pute the antiderivative of $\sec^4(\theta)$ . Show all your	

Name:	Problem 4:	/20
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**Problem 4**(20 points)

(a)(15 points): Use a trigonometric substitution of the form  $x = f(\theta)$  to express the following indefinite integral in terms of the variable  $\theta$  (assume x > 1).

$$\int \frac{1}{x^2 \sqrt{x^2 - 1}} dx.$$

Show all your work.

<sup>(</sup>b)(5 points): Using trigonometry identities, back-substitute to express the indefinite integral in terms of the original variable x. Show all your work (do not simply copy a formula from your index card).

Name:	Problem 5:	/20

**Problem 5**(20 points) In each of the following, use completing the square and a trigonometric substitution to evalute the indefinite integral.

substitution to evalute the indefinite integral.

(a)(10 points)  $\int \frac{1}{\sqrt{5x-x^2}} dx$  (assume that  $5x-x^2>0$ ). Show all your work.

(b)(10 points)  $\int \frac{1}{x^2-6x+18} dx$ . Show all your work.