

24.2 OPTICAL FIBRE

Definition: An optical fibre is a cylindrical wave guide made of transparent dielectric, (glass or clear plastic), which guides light waves along its length by total internal reflection. It is as thin as human hair, approximately $70\ \mu\text{m}$ or 0.003 inch diameter. (Note that a thin strand of a metal is called a wire and a thin strand of dielectric materials is called a fibre).



Optical Fibre.

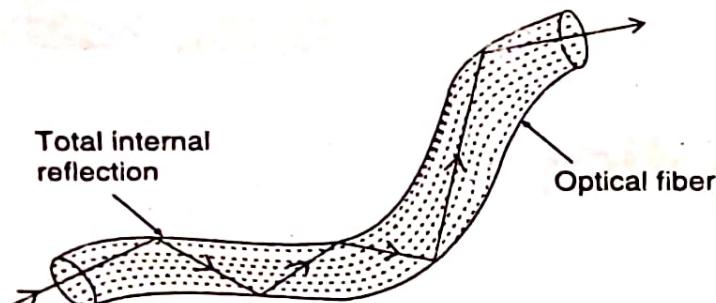
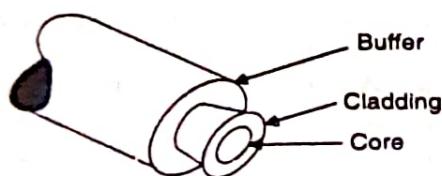
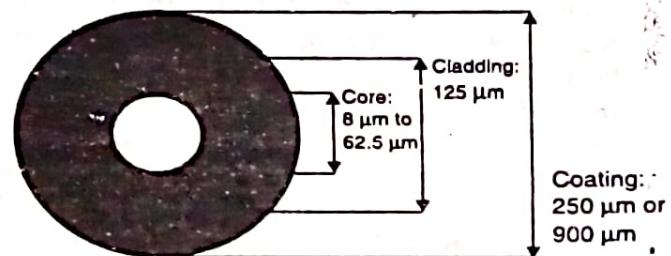


Fig. 24.1: Illustration of a transparent fibre guiding light along its length.

Principle: The propagation of light in an optical fibre from one of its ends to the other end is based on the principle of *total internal reflection*. When light enters one end of the fibre, it undergoes successive total internal reflections from sidewalls and travels down the length of the fibre along a zigzag path, as shown in Fig. 24.1. A small fraction of light may escape through sidewalls but a major fraction emerges out from the exit end of the fibre, as illustrated in Fig. 24.1. Light can travel through fibre even if it is bent.

Structure:

(a)



(b)

Fig. 24.2: Side view and cross sectional view of a typical optical fibre

A practical optical fibre is cylindrical in shape (Fig. 24.2a) and has in general three coaxial regions (Fig. 24.2b).

- The innermost cylindrical region is the light guiding region known as the **core**. In general, the diameter of the core is of the order of $8.5\ \mu\text{m}$ to $62.5\ \mu\text{m}$.
- It is surrounded by a coaxial middle region known as the **cladding**. The diameter of the cladding is of the order of $125\ \mu\text{m}$. The refractive index of cladding (n_2) is always lower than that of the core (n_1). Light launched into the core and striking the core-to-cladding interface at an angle greater than critical angle will be reflected back into the core. Since the

angles of incidence and reflection are equal, the light will continue to rebound and propagate through the fibre.

- (iii) The outermost region is called the **sheath** or a **protective buffer coating**. It is a plastic coating given to the cladding for extra protection. This coating is applied during the manufacturing process to provide physical and environmental protection for the fiber. The buffer is elastic in nature and prevents abrasions. The coating can vary in size from 250 μm or 900 μm . To sum up
 - Core is the inner light-carrying member.
 - Cladding is the middle layer, which serves to confine the light to the core.
 - Buffer coating surrounds the cladding, which protects the fibre from physical damage and environmental effects.

24.2.1 NECESSITY OF CLADDING

The actual fibre is very thin and light entering a bare fibre will travel along the fibre through repeated total internal reflections at the glass-air boundary. However, bare fibres are used only in certain applications. For use in communications and some other applications, the optical fibre is provided with a cladding. *The cladding maintains uniform size of the fibre, protects the walls of the fibre from chipping, and reduces the size of the cone of light that will be trapped in the fibre.*

- It is necessary that the diameter of an optical fibre remains constant throughout its length and is surrounded by the same medium. Any change in the thickness of the fibre or the medium outside the fibre (when the fibre gets wet due to moisture etc) will cause loss of light energy through the walls of the fibre.
- A very large number of reflections occur through the fibre and it is necessary that the condition for total internal reflection must be accurately met over the entire length of the fibre. If the surface of the glass fibre becomes scratched or chipped, the normal to the edge will no longer be uniform. As a result, the light traveling through the fibre will get scattered and escapes from the fibre. This also causes loss of light energy.
- Part of light energy penetrates the fibre surface. The intensity of the light decreases exponentially as we move away from the surface, as the light is able to penetrate only a very small distance outside the fibre. However, anytime the fibre touches something else, the light can leak into the new medium or be scattered away from the fibre. This effect causes a significant leakage of the light energy out of the fibre. Even a small amount of dust on the surface would cause a fair amount of leakage.
- If bare optic fibres are packed closely together in a bundle, light energy traveling through the individual fibres tends to get coupled through the phenomenon of *frustrated total internal reflection*. Cladding of sufficient thickness prevents the leakage of light energy from one fibre to the other.
- The fiber is provided with a cladding in order to prevent loss of light energy due to the above reasons.
- The cladding causes a reduction in the size of the cone of light that can be trapped in the fibre. Light entering the fibre at larger angles will strike the fibre walls at smaller angles (higher modes) and ultimately travel a longer distance. Such higher modes of a light signal will take longer time to reach the end of the fibre than the lower modes. Therefore, a pulse sent through optical fibre spreads out. The spreading would be larger, the larger the cone of acceptance. Such pulse spreading limits the rate of data transmission through the fibre. As fibers with a cladding have smaller cone of acceptance, they carry information at a much higher bit rate than those without a cladding.

Thus, the cladding performs the following important functions:

- Keeps the size of the fibre constant and reduces loss of light from the core into the surrounding air.
- Protects the fiber from physical damage and absorbing surface contaminants.
- Prevents leakage of light energy from the fibre through evanescent waves.
- Prevents leakage of light energy from the core through frustrated total internal reflection.
- Reduces the cone of acceptance and increases the rate of transmission of data.
- A solid cladding, instead of air, also makes it easier to add other protective layers over the fibre.

24.2.2 OPTICAL FIBRE SYSTEM

An optical fibre is used to transmit **light signals** over long distances. It is essentially a **light-transmitting medium**, its role being very much similar to a coaxial cable or wave-guide used in microwave communications. Optical fibre requires a **light source** for launching light into the fibre at its input end and a **photodetector** to receive light at its output end. As the diameter of the fibre is very small, the light source has to be dimensionally compatible with the fibre core. Light emitting diodes and laser diodes, which are very small in size, serve as the light sources. The electrical input signal is in general of digital form. It is converted into an optical signal by varying the current flowing through the light source. Hence, the intensity of the light emitted by the source is modulated with the input signal and the output will be in the form of light pulses. The light pulses constitute the signal that travels through the optical fibre. At the receiver end, semiconductor photodiodes, which are very small in size, are used for detection of these light pulses. The photodetector converts the optical signal into electrical form. Thus, a basic *optical fibre system* consists of a LED/laser diode, optical fibre cable and a semiconductor photodiode.

24.2.3 OPTICAL FIBRE CABLE

Optical fibre cables are designed in different ways to serve different applications. More protection is provided to the optical fibre by the "cable" which has the fibres and strength members inside an outer covering called a "jacket". We study here two typical designs: a single fibre cable or a multifibre cable.

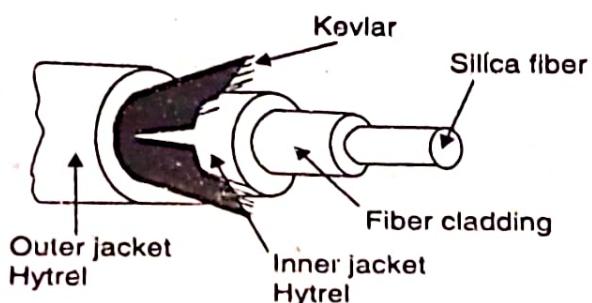


Fig. 24.3: Single fibre cable

- **Single Fibre Cable:** Around the fibre a tight buffer jacket of Hytrel is used (see Fig. 24.3). The buffer jacket protects the fibre from moisture and abrasion. A strength member is arranged around the buffer jacket in order to provide the necessary toughness and tensile strength. The strength member may be a steel wire, polymer film, nylon yarn or Kevlar yarn. Finally, the fibre cable is covered by a Hytrel outer jacket. Because of this arrangement fibre cable will not get damaged during bending, rolling, stretching or pulling and transport and installation processes. The single fibre cable is used for indoor applications.

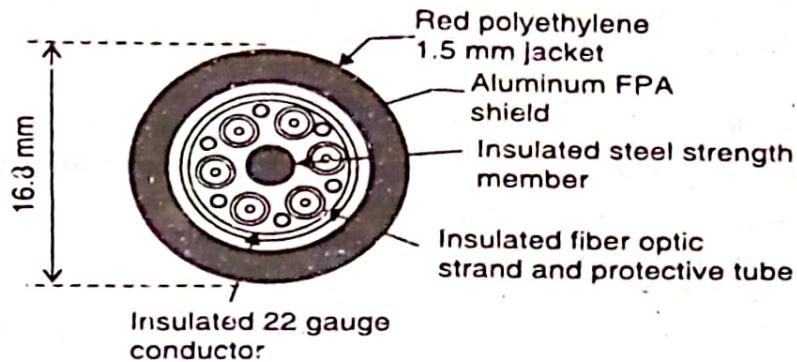


Fig. 24.4: Cross-sectional view of a typical multi fibre cable

- **Multifibre Cable:** A multifibre cable consists of a number of fibres in a single jacket. Each fibre carries light independently. The cross-sectional view of a typical telecommunication cable is shown in Fig.24.4. It contains six insulated optical fibre strands and has an insulated steel cable at the center for providing tensile strength. Each optical fibre strand consists of a core surrounded by a cladding, which in turn is coated with insulating jacket. The fibres are thus individually buffered and strengthened. Six insulated copper wires are distributed in the space between the fibres. They are used for electrical transmission, if required. The assembly is then fitted with in a corrugated aluminium sheath, which acts as a shield. A polyethylene jacket is applied over the top.

24.3 TOTAL INTERNAL REFLECTION

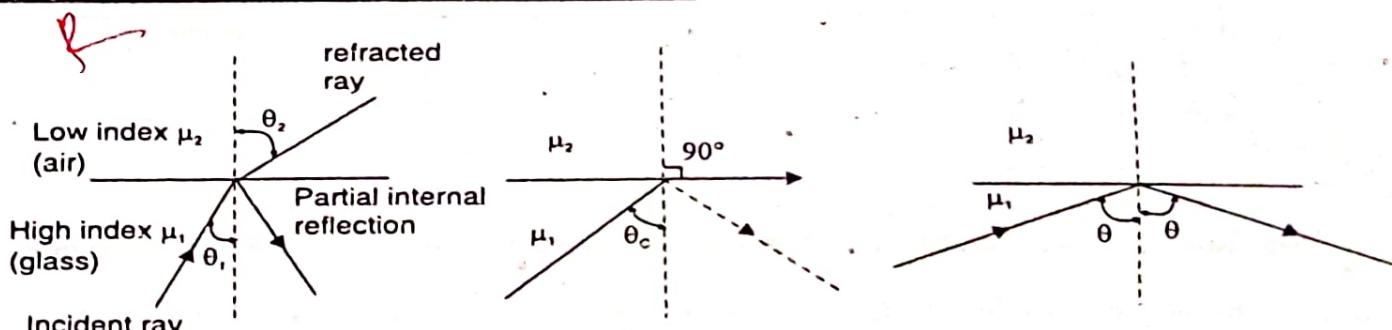


Fig. 24.5: Phenomenon of total internal reflection

A medium having a lower refractive index is said to be an optically **rarer medium** while a medium having a higher refractive index is known as an optically **denser medium**. When a ray of light passes from a denser medium to a rarer medium, it is bent away from the normal in the rarer medium (see Fig.24.5a). Snell's law for this case may be written as

$$\sin \theta_2 = \left(\frac{\mu_1}{\mu_2} \right) \sin \theta_1 \quad (24.1)$$

where θ_1 is the angle of incidence of light ray in the denser medium and θ_2 is the angle of refraction in the rarer medium. Also $\mu_1 > \mu_2$. When the angle of incidence, θ_1 in the denser medium is increased, the transmission angle, θ_2 increases and the refracted rays bend more and more away from the normal. At some particular angle θ_c the refracted ray glides along the boundary surface so that $\theta_2 =$

90° , as seen in Fig. 24.5(b). At angles greater than θ_c , there are no refracted rays at all. The rays are reflected back into the denser medium as though they encountered a specular reflecting surface (Fig. 24.5c). Thus,

- If $\theta_1 < \theta_c$, the ray refracts into the rarer medium
- If $\theta_1 = \theta_c$, the ray just grazes the interface of rarer-to-denser media
- If $\theta_1 > \theta_c$, the ray is reflected back into the denser medium.

The phenomenon in which light is totally reflected from a denser-to-rarer medium boundary is known as **total internal reflection**. The rays that experience total internal reflection obey the laws of reflection. Therefore, the critical angle can be determined from Snell's law.

When $\theta_1 = \theta_c$, $\theta_2 = 90^\circ$.

Therefore, from equ.(24.1), we get

$$\mu_1 \sin \theta_c = \mu_2 \sin 90^\circ = \mu_2$$

$$\therefore \sin \theta_c = \frac{\mu_2}{\mu_1} \quad (24.2)$$

When the rarer medium is air, $\mu_2 = 1$ and writing $\mu_1 = \mu$, we obtain

$$\sin \theta_c = \frac{1}{\mu} \quad (24.3)$$

24.4 PROPAGATION OF LIGHT THROUGH AN OPTICAL FIBRE

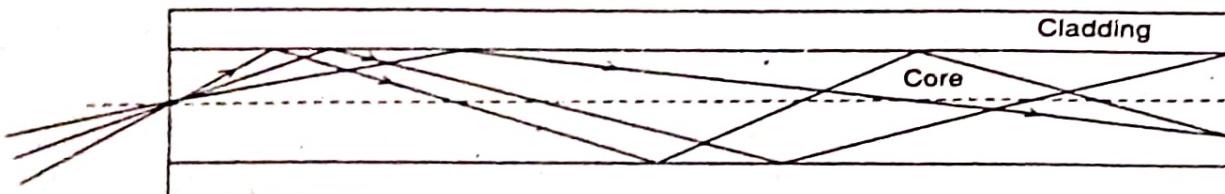


Fig. 24.6 : Propagation of light rays through an optical fibre due to total internal reflection.

The diameter of an optical fibre is very small and as such we cannot use bigger light sources for launching light beam into it. Light emitting diodes (LEDs) and laser diodes are the optical sources used in fibre optics. Even in case of these small sized sources, a focusing lens has to be used to concentrate the beam on to the fibre core. Light propagates as an electromagnetic wave through an optical fibre. However, light propagation through an optical fibre can as well be understood on the basis of *ray model*. According to the ray model, light rays entering the fibre strike the core-clad interface at different angles. As the refractive index of the cladding is less than that of the core, majority of the rays undergo total internal reflection at the interface and the angle of reflection is equal to the angle of incidence in each case. Due to the cylindrical symmetry in the fibre structure, the rays reflected from an interface on one side of the fibre axis will suffer total internal reflections at the interface on the opposite side also. Thus, the rays travel forward through the fibre via a series of total internal reflections and emerge out from the exit end of the fibre (Fig.24.6). Since each reflection is a total internal reflection, there is no loss of light energy and light confines itself within the core during the course of propagation. Because of the negligible loss during the total internal reflections, optical fibre can carry the light waves over very long distances. Thus, the optical fibre

acts essentially as a wave-guide and is often called a light guide or light pipe. At the exit end of the fibre, the light is received by a photo-detector.

Total internal reflection at the fibre wall can occur and light propagates down the fibre, only if the following two conditions are satisfied.

1. The refractive index of the core material, n_1 , must be slightly greater than that of the cladding, n_2 .
2. At the core-cladding interface (Fig. 24.7), the angle of incidence ϕ between the ray and the normal to the interface must be greater than the critical angle ϕ_c defined by

$$\sin \phi_c = \frac{n_2}{n_1} \quad (24.4)$$

It is to be noted here that only those rays, that are incident at the core-clad interface at angles greater than the critical angle will propagate through the fibre. Rays that are incident at smaller angles are refracted into the cladding and are lost.

24.4.1 CRITICAL ANGLE OF PROPAGATION

Let us consider a step index optical fibre into which light is launched at one end. The end at which light enters the fibre is called the **launching end**. Fig. 24.7 depicts the conditions at the launching end. In a step-index fibre, the refractive index changes abruptly from the core to the cladding. Now, we consider two rays entering the fibre at two different angles of incidence.

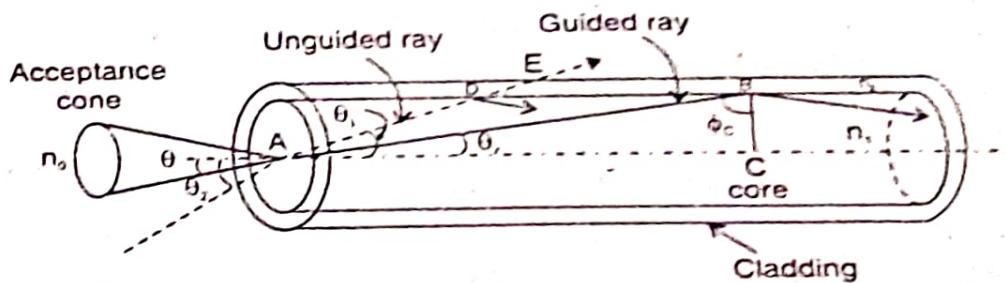


Fig. 24.7: Light rays incident at an angle smaller than critical propagation angle will propagate through the fibre.

The ray shown by the broken line is incident at an angle θ_2 with respect to the axis of the fibre. This ray undergoes refraction at point A on the interface between air and the core. The ray refracts into the fibre at an angle θ_1 ($\theta_1 < \theta_2$). The ray reaches the core-cladding interface at point D. At point D, refraction takes place again and the ray travels in the cladding. Finally, at point E, the ray refracts once again and emerges out of fibre into the air. It means that the ray does not propagate through the fibre.

Let us next consider the ray shown by the solid line in Fig. 24.7. The ray incident at an angle θ undergoes refraction at point A on the interface and propagates at an angle θ_1 in the fibre. At point B on the core-cladding interface, the ray undergoes total internal reflection, since $n_1 > n_2$. Let us assume that the angle of incidence at the core-cladding interface is the **critical angle** ϕ_c where ϕ_c is given by

$$\phi_c = \sin^{-1}(n_2/n_1) \quad (24.4a)$$

A ray incident with an angle larger than ϕ_c will be confined to the fibre and propagate in the fibre. A ray incident, at the core-cladding boundary, at the critical angle is called a **critical ray**. The critical ray makes an angle ϕ_c with axis of the fibre. It is obvious that rays with propagation angles

larger than θ_c will not propagate in the fibre. Therefore, the angle θ_c is called the critical propagation angle. From the Δ^{abc} , it is seen that

$$\frac{AC}{AB} = \sin \phi_c.$$

$$\text{Also, } \frac{AC}{AB} = \cos \theta_c.$$

From the relation (24.4a), $\sin \phi_c = n_2 / n_1$.

$$\cos \theta_c = n_1 / n_2 \quad (24.5)$$

$$\therefore \theta_c = \cos^{-1}(n_2/n_1) \quad (24.6)$$

Thus, only those rays which are refracted into the cable at angles $\theta_i < \theta_c$ will propagate in the optical fibre.

24.4.2 ACCEPTANCE ANGLE

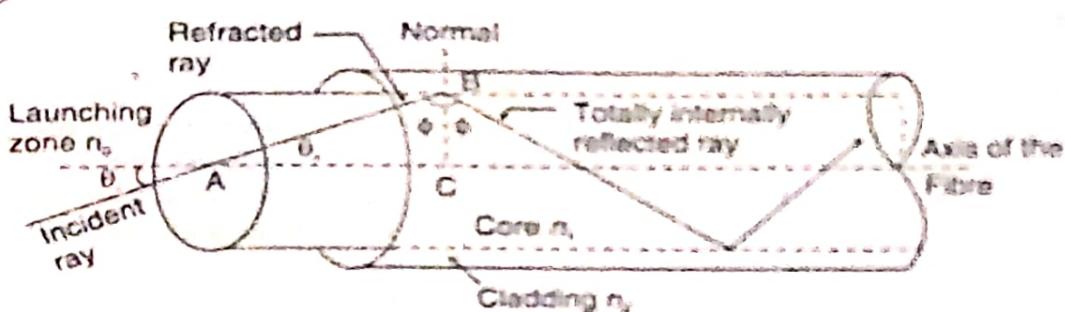


Fig. 24.8 : Geometry for the calculation of acceptance angle of the fibre.

Let us again consider a step index optical fibre into which light is launched at one end, as shown in Fig. 24.8. Let the refractive index of the core be n_1 and the refractive index of the cladding be n_2 ($n_2 < n_1$). Let n_o be the refractive index of the medium from which light is launched into the fibre.

Assume that a light ray enters the fibre at an angle θ_i to the axis of the fibre. The ray refracts at an angle θ_r and strikes the core-cladding interface at an angle ϕ . If ϕ is greater than critical angle ϕ_c , the ray undergoes total internal reflection at the interface, since $n_1 > n_2$. As long as the angle ϕ is greater than ϕ_c , the light will stay within the fibre.

Applying Snell's law to the launching face of the fibre, we get

$$\frac{\sin \theta_i}{\sin \theta_r} = \frac{n_1}{n_o} \quad (24.7)$$

If θ_i is increased beyond a limit, ϕ will drop below the critical value ϕ_c and the ray escapes from the sidewalls of the fibre. The largest value of θ_i occurs when $\phi = \phi_c$.

From the Δ^{abc} , it is seen that

$$\sin \theta_r = \sin (90^\circ - \phi) = \cos \phi \quad (24.8)$$

Using equation (24.8) into equation (24.7), we obtain

$$\sin \theta_i = \frac{n_1}{n_o} \cos \phi$$

When

$$\phi = \phi_c, \quad \sin [\theta_{i_{\max}}] = \frac{n_1}{n_o} \cos \phi_c \quad (24.9)$$

But

$$\sin \phi_c = \frac{n_2}{n_1}$$

$$\cos \phi_C = \frac{\sqrt{n_1^2 - n_2^2}}{n_1} \quad (24.10)$$

Substituting the expression (24.10) into (24.9), we get

$$\sin[\theta_i(\max)] = \frac{\sqrt{n_1^2 - n_2^2}}{n_0} \quad (24.11)$$

Quite often the incident ray is launched from air medium, for which $n_0=1$. Designating $\theta_i(\max)=\theta_a$, equation (24.11) may be simplified to

$$\begin{aligned} \sin \theta_a &= \sqrt{n_1^2 - n_2^2} \\ \theta_a &= \sin^{-1} \left[\sqrt{n_1^2 - n_2^2} \right] \end{aligned} \quad (24.12)$$

The angle θ_a is called the **acceptance angle** of the fibre. *Acceptance angle is the maximum angle that a light ray can have relative to the axis of the fibre and propagate down the fibre.* Thus, only those rays that are incident on the face of the fibre making angles less than θ_a will undergo repeated total internal reflections and reach the other end of the fibre. Obviously, larger acceptance angles make it easier to launch light into the fibre.

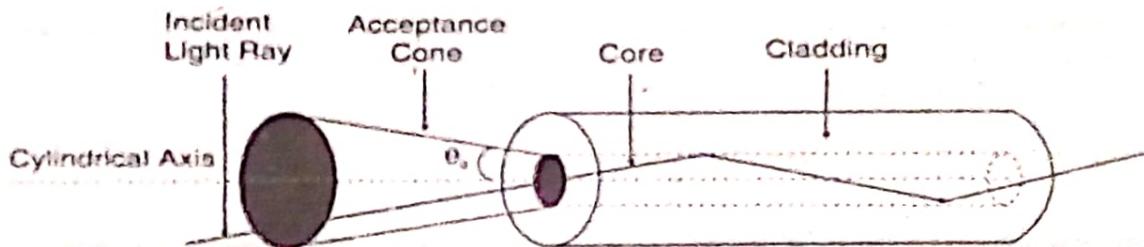


Fig. 24.9 Acceptance Cone

In three dimensions, the light rays contained within the cone having a full angle $2\theta_a$ are accepted and transmitted along the fibre (see Fig. 24.9). Therefore, the cone is called the **acceptance cone**.

Light incident at an angle beyond θ_a refracts through the cladding and the corresponding optical energy is lost.

24.5 FRACTIONAL REFRACTIVE INDEX CHANGE

The fractional difference Δ between the refractive indices of the core and the cladding is known as **fractional refractive index change**. It is expressed as

$$\Delta = \frac{n_1 - n_2}{n_1} \quad (24.13)$$

This parameter is always positive because n_1 must be larger than n_2 for the total internal reflection condition. In order to guide light rays effectively through a fibre, $\Delta \ll 1$. Typically, Δ is of the order of 0.01.

24.6 NUMERICAL APERTURE

The main function of an optical fibre is to accept and transmit as much light from the source as possible. The light gathering ability of a fibre depends on the numerical aperture. The acceptance angle and the fractional refractive index change determine the numerical aperture of fibre.

The numerical aperture (NA) is defined as the sine of the acceptance angle. Thus,

$$NA = \sin \theta_0$$

where θ_0 is the acceptance angle.

But:

$$\sin \theta_0 = \sqrt{n_1^2 - n_2^2}$$

$$NA = \sqrt{n_1^2 - n_2^2}$$

(24.14)

$$n_1^2 - n_2^2 = (n_1 + n_2)(n_1 - n_2) = \left(\frac{n_1 + n_2}{2} \right) \left(\frac{n_1 - n_2}{n_1} \right) 2n_1$$

Approximating $\frac{n_1 + n_2}{2} \approx n_1$, we can express the above relation as $(n_1^2 - r_2^2) = 2n_1^2 \Delta$. It gives

$$NA = \sqrt{2n_1^2 \Delta}$$

$$NA = n_1 \sqrt{2\Delta}$$

(24.15)

Numerical aperture determines the light gathering ability of the fibre. It is a measure of the amount of light that can be accepted by a fibre. It is seen from equ. (24.14) that NA is dependent only on the refractive indices of the core and cladding materials and does not depend on the physical dimensions of the fibre. The value of NA ranges from 0.13 to 0.50. A large NA implies that a fibre will accept large amount of light from the source (see Fig. 23.10).

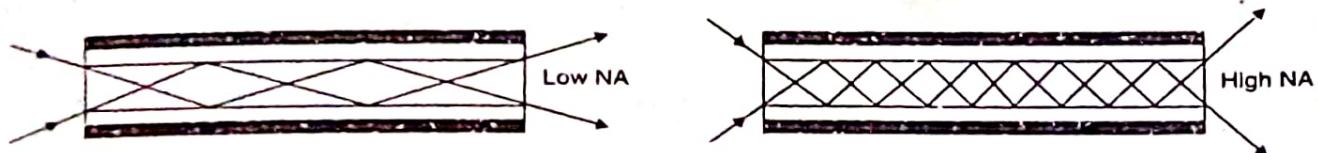


Fig. 24.10: Illustration of the propagation of light through low and high numerical aperture fibres.

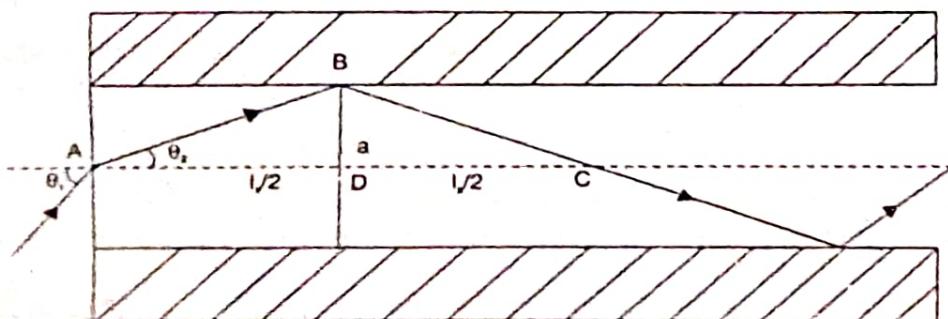
24.7 SKIP DISTANCE AND NUMBER OF TOTAL INTERNAL REFLECTIONS

Fig. 24.11 : Skip Distance l_s

We shall now calculate the number of total internal reflections that a light ray undergoes as it travels through an optical fibre of length L . Let a be the radius of the fibre. Let a light ray be incident on one end of the fibre at an angle θ_1 to the axis and refract into the fibre at an angle θ_2 , as shown in Fig. 24.11. The ray undergoes the first reflection at B. The distance $AC = l_s$ is known as the **skip distance** and represents the distance between two successive reflections of the ray. In the $\triangle ABD$,

$$AD = \frac{1}{2} AC = \frac{l_s}{2}, \quad BD = a \text{ and } \angle BAD = \theta_2.$$

$$\tan \theta_2 = \frac{BD}{AD} = \frac{a}{l_s/2}$$

$$\text{or} \quad l_s = \frac{2a}{\tan \theta_2} \quad (24.16)$$

In terms of the incidence angle θ_1 , the above equation may be rewritten as

$$l_s = 2a \left[\frac{\cos \theta_2}{\sin \theta_2} \right] \quad \text{or} \quad l_s^2 = (2a)^2 \left[\frac{1}{\sin^2 \theta_2} - 1 \right]$$

Using equ.(24.7) into the above expression, we obtain

$$l_s^2 = (2a)^2 \left[\left(\frac{n_1}{n_o \sin \theta_1} \right)^2 - 1 \right]$$

$$\text{or} \quad l_s = 2a \left[\left(\frac{n_1}{n_o \sin \theta_1} \right)^2 - 1 \right]^{1/2} \quad (24.17)$$

$$\text{In case of air, } n_o = 1 \text{ and } l_s = 2a \left[\left(\frac{n_1}{\sin \theta_1} \right)^2 - 1 \right]^{1/2} \quad (24.17a)$$

The number of total internal reflections in the total fibre length is given by

$$N = \frac{\text{Total length of the cable}}{\text{The distance travelled during one reflection}} = \frac{L}{l_s}$$

$$\therefore N = \frac{L \tan \theta_2}{2a} \quad (24.18a)$$

$$\text{Also, } N = \frac{L}{2a \left[\left(\frac{n_1}{\sin \theta_1} \right)^2 - 1 \right]^{1/2}} \quad (24.18b)$$

For example, if $n_1 = 1.50$, $\theta_1 = 30^\circ$ and $a = 25 \mu m$, equ.(24.18b) gives $l_s = 141 \mu m$. Alternately, computing the value of θ_2 and using it in equ.(24.18a), we obtain $l_s = 141 \mu m$. Therefore, if light travels through a length of 1 m of the optical fibre of the above specifications, it is reflected 7092 times.

24.8 MODES OF PROPAGATION

Light propagates as an electromagnetic wave through an optical fibre and its propagation is governed by Maxwell's equations. Complete understanding of propagation of light waves through optical fibres requires a thorough understanding of solution of these equations in the context of optical fibres. When a plane electromagnetic wave propagates in free space, it travels as a transverse electromagnetic wave. The electric field and magnetic field components associated with the wave are perpendicular to each other and also perpendicular to the direction of propagation. It is known as a TEM wave. When the light ray is guided through an optical fibre, it propagates in different types of modes. Each of these guided modes consists of a variety of electromagnetic field configurations, such as transverse electric (TE), transverse magnetic (TM) and hybrid modes. Hybrid modes are combination of transverse electric and magnetic modes.

In simple terms these modes can be visualised as the possible number of allowed paths of light in an optical fibre (see Fig. 24.6). The paths are all zigzag paths excepting the axial direction. Though the rays having propagation angles between $\theta = 0^\circ$ and $\theta = \theta_c$ will be in a position to undergo total internal reflections, all of them will not however propagate along the optical fibre. Only a certain ray directions are allowed. As a zigzag ray gets repeatedly reflected at the walls of the fibre, phase shift occurs. Consequently, the waves travelling along certain zigzag paths will be in phase and undergo constructive interference, while the waves coursing along certain other paths will be out of phase and diminish due to destructive interference. The light ray paths along which the waves are in phase inside the fibre are known as modes. Each mode is a pattern of electric and magnetic field distributions that is repeated along the fibre at equal intervals. The number of modes propagating in a fibre increases as θ_c or Δ increases. Increasing the core refractive index increases the number of propagating modes. On the other hand, increasing the clad refractive index decreases the number of propagating modes. The number of modes that a fibre will support depends on the ratio d/λ , where d is the diameter of the core and λ is the wavelength of the wave being transmitted. The zero order ray travels along the axis is known as the *axial ray*.

Note that each mode carries a portion of the light from the input signal.

Types of modes:

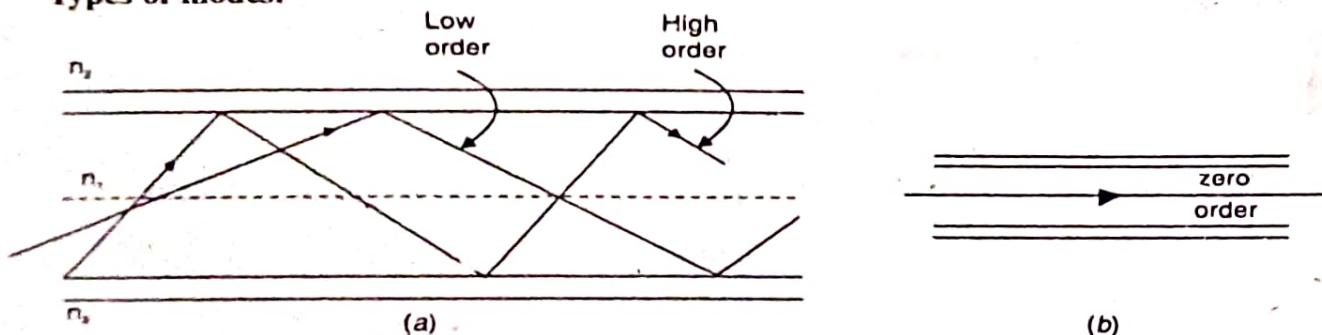


Fig.24.12 : (a) Low and High-order ray paths in a multimode fibre. (b) Axial ray in a single mode fibre

In a fibre of fixed thickness, the modes that propagate at angles close to the critical angle ϕ_c (i.e., critical propagation angle θ_c) are **higher order modes**, and modes that propagate with angles larger than the critical angle (i.e., lower than the critical propagation angle) are **lower order modes** (see Fig. 24.12). In case of lower order modes, the fields are concentrated near the center of the fibre. In case of higher order modes, the fields are distributed more towards the edge of the wave-guide and tend to send light energy into the cladding. This energy is lost ultimately. The higher order

- modes have to traverse longer paths and hence take larger time than the lower order modes to cover a given length of the fibre. Thus, the higher order modes arrive at the output end of the fiber later than the lower order modes.

24.9 TYPES OF RAYS

The rays that propagate through an optical fibre can be classified into two categories: (i) meridional rays and (ii) skewed rays.

1. Meridional ray: A ray that propagates through the fibre undergoing total internal reflection is called meridional ray. It passes through the longitudinal axis of the fibre core (Fig. 24.13a). The propagation of meridional rays is possible only in the TM or TE modes.

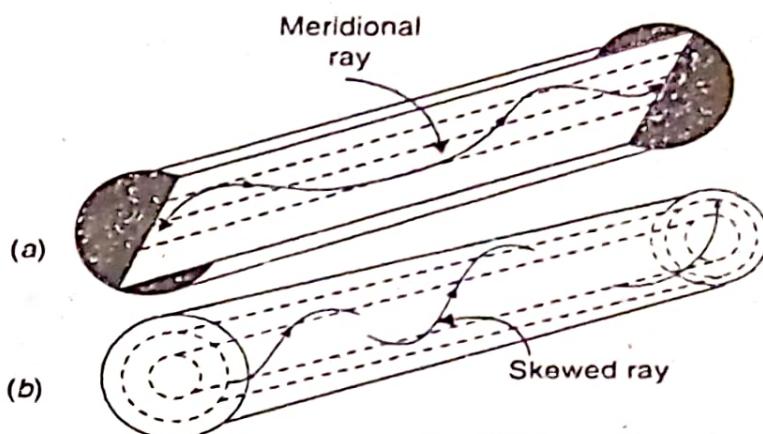
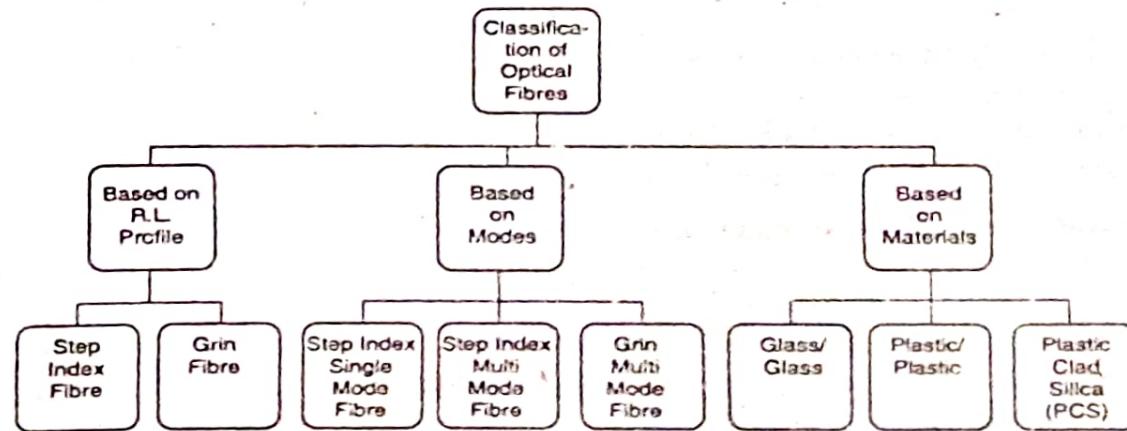


Fig. 24.13

2. Skew ray: The ray that describes angular helical path along the fibre is called a skew ray (see Fig. 24.13b). These rays do not pass through the axis of the core. These rays are propagated in either hybrid EH or HE modes. Some of these modes produce losses through leakage of radiation. In real situations, the skew rays constitute a substantial portion of the total number of guided rays. They tend to propagate only in the annular region near the outer surface of the core and do not fully utilize the core as the medium. However, they are complementary to the meridional rays and increase the light gathering capacity of the fibre.

24.10 CLASSIFICATION OF OPTICAL FIBRES

Optical fibres are differently classified into various types basing on different parameters.



A. Classification basing on refractive index profile:

Refractive index profile of an optical fibre is a plot of refractive index drawn on one of the axes and the distance from the core axis drawn on the other axis (see Fig. 24.14). Optical fibres are classified into the following two categories on the basis of refractive index profile.

1. Step index fibres
- and
2. Graded index (GRIN) fibres.

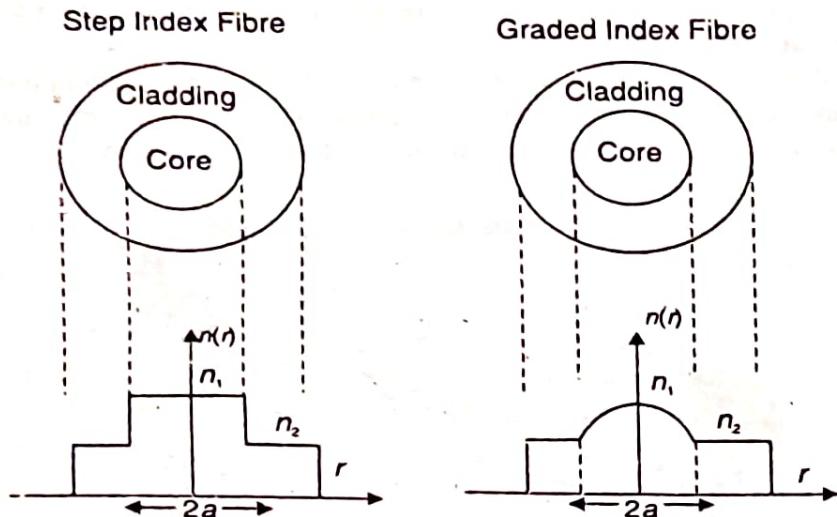


Fig. 24.14 : Classification of optical fibres based on R.I. profile (a) Step index fibre (b) GRIN fibre

Step index refers to the fact that the refractive index of the core is constant along the radial direction and abruptly falls to a lower value at the cladding and core boundary (see Fig. 24.14a). In case of GRIN fibres, the refractive index of the core is not constant but varies smoothly over the diameter of the core (see Fig. 24.14b). It has a maximum value at the center and decreases gradually towards the outer edge of the core. At the core-cladding interface the refractive index of the core matches with the refractive index of the cladding. The refractive index of the cladding is constant.

B. Classification basing on the modes of light propagation:

On the basis of the modes of light propagation, optical fibres are classified into two categories as

1. Single mode fibres (SMF)
- and 2. Multimode fibres (MMF).

A single mode fibre (SMF) has a smaller core diameter and can support only one mode of propagation. On the other hand, a multimode fibre (MMF) has a larger core diameter and supports a number of modes.

Thus, on the whole, the optical fibres are classified into three types:

- Single mode step-index (SMF) fibre
- Multimode step-index (MMF) fibre
- Graded index (multimode) (GRIN) fibre.

C. Classification basing on materials:

On the basis of materials used for core and cladding, optical fibres are classified into three categories.

1. Glass/glass fibres (glass core with glass cladding)
2. Plastic/plastic fibres (plastic core with plastic cladding)
3. PCS fibres (polymer clad silica)

24.11 THE THREE TYPES OF FIBRES

We now study the detailed structure and characteristics of the three types of optical fibres.

24.11.1 SINGLE MODE STEP INDEX FIBRE

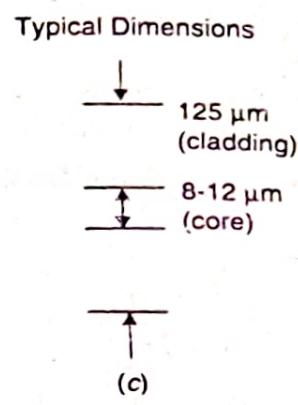
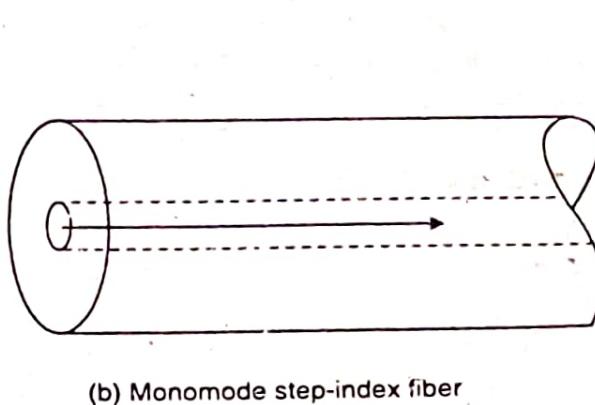
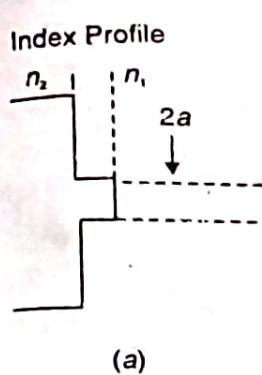


Fig. 24.15: Single mode step index fibre (a) R.I. profile (b) ray paths (c) typical dimensions

Structure

A single mode step index fibre has a very fine thin core of diameter of 8 μm to 12 μm (see Fig.24.15 c). It is usually made of germanium doped silicon. The core is surrounded by a thick cladding of lower refractive index. The cladding is composed of silica lightly doped with phosphorous oxide. The external diameter of the cladding is of the order of 125 μm . The fibre is surrounded by an opaque protective sheath. The refractive index of the fibre changes abruptly at the core-cladding boundary, as shown in Fig. 24.15 (a). The variation of the refractive index of a step index fibre as a function of radial distance can be mathematically represented as

$$\begin{aligned} n(r) &= n_1 [r < a \text{ inside core}] \\ &= n_2 [r > a \text{ in cladding}] \end{aligned} \quad (24.19)$$

Propagation of light in SMF

Light travels in SMF along a single path that is along the axis (Fig.24.15b). Obviously, it is the zero order mode that is supported by a SMF. Both Δ and NA are very small for single mode fibres. This relatively small value is obtained by reducing the fibre radius and by making Δ , the relative refractive index change, to be small. The low NA means a low acceptance angle. Therefore, light coupling into the fibre becomes difficult. Costly laser diodes are needed to launch light into the SMF.

24.11.2 MULTIMODE STEP INDEX FIBRE

Structure

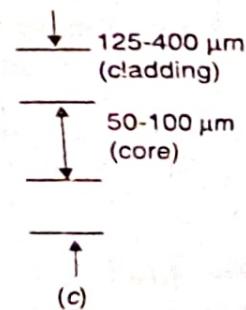
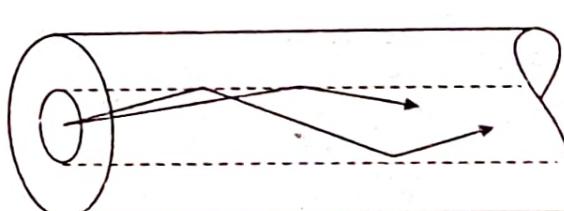
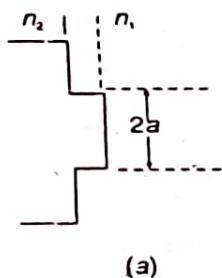


Fig. 24.16: Multimode step index fibre (a) R.I. Profile (b) Ray paths (c) typical dimensions.

A multimode step index fibre is very much similar to the single mode step index fibre except that its core is of larger diameter. The core diameter is of the order of 50 to 100 μm , which is very large compared to the wavelength of light. The external diameter of cladding is about 150 to 250 μm (Fig. 24.16 c).

Propagation of light in MMF

Multimode step index fibres allow finite number of guided modes. The direction of polarization, alignment of electric and magnetic fields will be different in rays of different modes. In other words, many zigzag paths of propagation are permitted in a MMF. The path length along the axis of the fibre is shorter while the other zigzag paths are longer. Because of this difference, the lower order modes reach the end of the fibre earlier while the high order modes reach after some time delay (Fig. 24.16b).

24.11.3 GRADED INDEX (GRIN) FIBRE

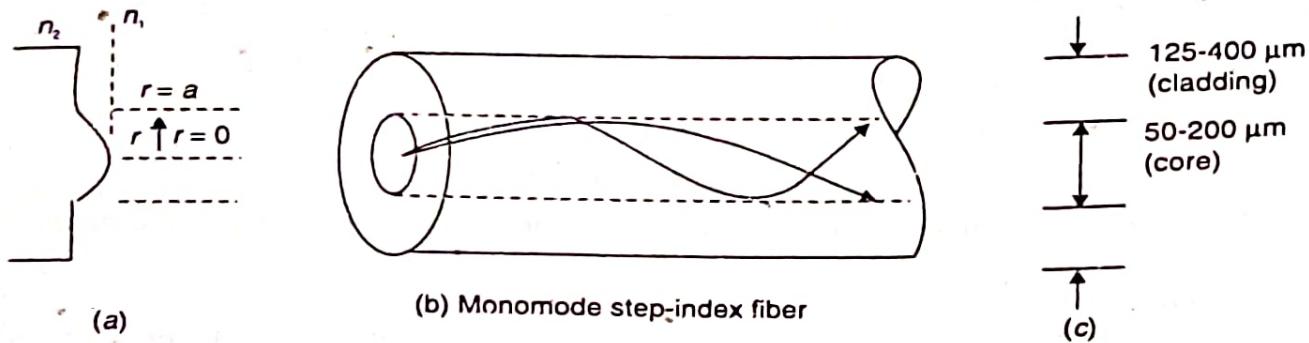


Fig. 24.17 : GRIN fibre (a) R.I. Profile (b) Ray paths (c) typical dimensions

A graded index fibre is a multimode fibre with a core consisting of concentric layers of different refractive indices. Therefore, the refractive index of the core varies with distance from the fibre axis. It has a high value at the centre and falls off with increasing radial distance from the axis. A typical structure and its index profile are shown in Fig. 24.17 (a). Such a profile causes a periodic focussing of light propagating through the fibre. The size of the graded index fibre is about the same as the step index fibre. The variation of the refractive index of the core with radius measured from the center is given by

$$n(r) = \begin{cases} n_1 \sqrt{1 - \left[2\Delta \left(\frac{r}{a} \right)^\alpha \right]}, & r < a \text{ inside core} \\ n_2, & r > a \text{ in cladding} \end{cases} \quad (24.20)$$

where n_1 is maximum refractive index at the core axis, a the core radius, and α the grading profile index number which varies from 1 to ∞ . When $\alpha = 2$, the index profile is parabolic and is preferred for different applications.

Propagation of light

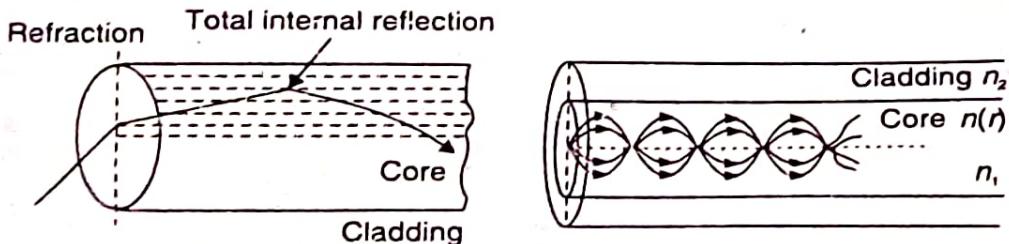


Fig.24.18 : (a) An expanded ray diagram showing refraction at the various high to low index interfaces within graded index fibre, giving an overall curved ray path. (b) Light transmission in a graded index fibre.

As a light ray goes from a region of higher refractive index to a region of refractive index, it is bent away from the normal. The process continues till the condition for total internal reflection is met. Then the ray travels back towards the core axis, again being continuously refracted (Fig. 24.18a). The turning around may take place even before reaching the core-cladding interface. Thus, continuous refraction is followed by total internal reflection and again continuous refraction towards the axis. In the graded index fibre, rays making larger angles with the axis traverse longer path but they travel in a region of lower refractive index and hence at a higher speed of propagation. Consequently, all rays traveling through the fibre, irrespective of their modes of travel, will have almost the same optical path length and reach the output end of the fibre at the same time (see Fig. 24.18b).

In case of GRIN fibres, the acceptance angle and numerical aperture decrease with radial distance from the axis. The numerical aperture of a graded index fibre is given by

$$\begin{aligned} NA &= \sqrt{n_1^2(r) - n_2^2} = n_1(2\Delta)^{\frac{1}{2}} \sqrt{1 - \left(\frac{r}{a}\right)^2} \\ &= n_1 \sqrt{2\Delta \left[1 - \left(\frac{r}{a}\right)^2\right]} \end{aligned} \quad (24.21)$$

24.12 MATERIALS

Optical fibres are fabricated from glass or plastic which are transparent to optical frequencies. Step index fibres are produced in three common forms – (i) a glass core cladded with a glass having a slightly lower refractive index, (ii) a silica glass core cladded with plastic and (iii) a plastic core cladded with another plastic. Generally, the refractive index step is the smallest for all glass fibres, a little larger for the plastic clad silica (PCS) fibres and the largest for all plastic construction.

24.12.1 ALL GLASS FIBRES

The basic material for fabrication of optical fibres is silica (SiO_2). It has a refractive index of 1.458 at $\lambda = 850 \text{ nm}$. Materials having slightly different refractive index are obtained by doping the basic silica material with small quantities of various oxides. If the basic silica material is doped with germania (GeO_2) or phosphorous pentoxide (P_2O_5), the refractive index of the material increases. Such materials are used as core materials and pure silica is used as cladding material in these cases. When pure silica is doped with boria (B_2O_3) or fluorine, its refractive index decreases. These materials are used for cladding when pure silica is used as core material. Examples of fiber compositions are

- SiO_2 core – $\text{B}_2\text{O}_3, \text{SiO}_2$ cladding
- $\text{GeO}_2, \text{SiO}_2$ core – SiO_2 cladding

The glass optical fibres exhibit very low losses and are used in long distance communications.

24.12.2 ALL PLASTIC FIBRES

In these fibres, perspex (PMMA) and polystyrene are used for core. Their refractive indices are 1.49 and 1.59 respectively. A fluorocarbon polymer or a silicone resin is used as a cladding material. A high refractive index difference is achieved between the core and the cladding materials. Therefore, plastic fibres have large NA of the order of 0.6 and large acceptance angles up to 77° . The main advantages of the plastic fibres are low cost and higher mechanical flexibility. The mechanical flexibility allows the plastic fibres to have large cores, of diameters ranging from 110 to 1400 μm . However, they are temperature sensitive and exhibit very high loss. Therefore, they are used in low cost applications and at ordinary temperatures (below 80°C). Examples of plastic fiber compositions are

• Polyester core	$n_1 = 1.60$	NA = 0.60
- Methyl methacrylate cladding	$n_2 = 1.49$	
• Polymethyl methacrylate core	$n_1 = 1.49$	NA = 0.50
- cladding made of its copolymer	$n_2 = 1.40$	

24.12.3 PCS FIBRES

The plastic clad silica (PCS) fibres are composed of silica cores surrounded by a low refractive index transparent polymer as cladding. The core is made from high purity quartz. The cladding is made of a silicone resin having a refractive index of 1.405 or of perfluorinated ethylene propylene (Teflon) having a refractive index of 1.338. Plastic claddings are used for step-index fibres only. The PCS fibres are less expensive but have high losses. Therefore, they are mainly used in short distance applications.

24.13 V-NUMBER

Let us consider a narrow beam of monochromatic light launched on the front end of a step-index fibre, at an angle less than the acceptance angle of the fibre. Let the wavelength of the light be λ , and the diameter of the fiber be d . It appears to us from the ray concept that all the rays contained in the beam propagate along the fibre, such that there can be infinite modes of propagation. However, in practice, only a limited number of modes of propagation are possible in an optical fibre. To understand the reason for this behaviour, we have to recall that phase changes occur as the light waves travel forward. The phase shift takes place due to two reasons – (i) due to optical path length traversed and (ii) due to total internal reflection at the core-cladding interface.

- (i) When a wave travels a distance l in a medium of refractive index n_1 , it undergoes a phase change δ_1 given by

$$\delta_1 = k n_1 l = \frac{2\pi l n_1}{\lambda} \quad (24.22)$$

where k is the propagation constant.

- (ii) Whenever, a wave with component normal to the reflecting surface undergoes total internal reflection, the phase shift, δ_2 , is given by

$$\delta_2 = 2 \tan^{-1} \frac{\sqrt{n_1^2 \cos^2 \phi - n_2^2}}{n_1 \sin \phi} \quad (24.23)$$

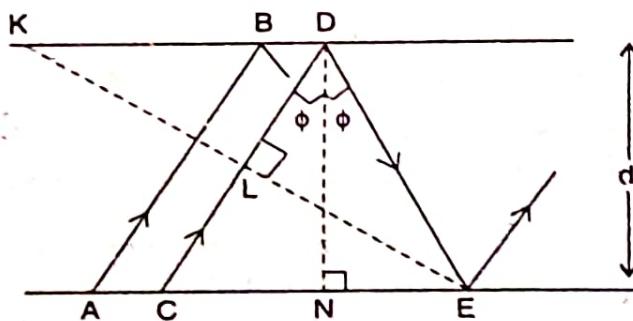


Fig. 24.19

In Fig. 24.19, AB and CD are parallel rays in an incident beam. The line KL is perpendicular to the propagation path of the rays AB, CD and hence represents a plane wavefront. The points K and L

lying on the same wavefront will be in phase with each other. As the point E, which is on the reflected ray DE, lies on the wavefront KL, the points L and E must be in phase with each other. However, moving from the point L to E along the ray, we find that there occurs a phase shift given by

$$\delta = (LD + DE) \frac{2\pi n_1}{\lambda_0} - 2\delta_2 \quad (24.24)$$

The factor 2 in the above equation takes into account the two total internal reflections at D and E. In the $\Delta^L DNE$

$$\frac{DN}{DE} = \cos \phi. \text{ Therefore, } DE = \frac{DN}{\cos \phi} = \frac{d}{\cos \phi}$$

Further, in the $\Delta^L LDE$

$$\frac{LD}{DE} = \cos 2\phi. \text{ Therefore, } LD = DE \cos 2\phi$$

$$LD + DE = DE (1 + \cos 2\phi) = 2 DE \cos^2 \phi.$$

$$\text{Therefore, } LD + DE = 2 \frac{d}{\cos \phi} \cos^2 \phi = 2d \cos \phi$$

Using the above expression into equ.(24.23), we obtain

$$\delta = \frac{4d\pi n_1 \cos \phi}{\lambda_0} - 2\delta_2$$

Now the condition for the wave associated with the ray CD to propagate along the optical fibre is that the phase of the twice reflected wave must be the same as that of the incident wave. That is, the wave must interfere constructively with itself. If this phase condition is not satisfied, the wave would interfere destructively with itself and just die out. It means that the total phase shift must be equal to an integer multiple of 2π radians. Thus

$$\frac{4d\pi n_1 \cos \phi}{\lambda_0} - 2\delta_2 = 2\pi m$$

$$\text{or } m = \frac{2d n_1 \cos \phi_m}{\lambda_0} - \frac{\delta_2}{\pi} \quad (24.25)$$

where m is an integer that determines the allowed ray angles for propagation of the wave and ϕ_m is the value of ϕ corresponding to a particular value of m . In order to sustain total internal reflection,

$$\begin{aligned} \sin \phi_m &\geq \frac{n_2}{n_1} \\ \therefore \cos \phi_m &\leq \frac{\sqrt{n_1^2 - n_2^2}}{n_1} \\ \therefore m &\leq \frac{2d \sqrt{n_1^2 - n_2^2}}{\lambda_0} - \frac{\delta_2}{\pi} \end{aligned} \quad (24.26)$$

$$\text{or } m \leq \frac{2V}{\pi} - \frac{\delta_2}{\pi} \quad (24.27)$$

where V is given by

$$V = \frac{\pi d}{\lambda_0} \sqrt{n_1^2 - n_2^2} \quad (24.28)$$

V -number is more generally called normalized frequency of the fibre. Each mode has a definite value of V -number below which the mode is cut off. Equ.(24.28) can be written as

$$V = \frac{\pi d}{\lambda_0} (NA) \quad (24.29)$$

or

$$V = \frac{\pi d}{\lambda_0} n_1 \sqrt{2\Delta} \quad (24.30)$$

The maximum number of modes N_m supported by an SI fibre is given by

$$N_m = \frac{1}{2} V^2 \quad (24.31)$$

Thus, for $V = 10$, N_m is 50. When the normalized frequency V is less than 2.405, the fibre can support only one mode, which propagates along the axial length of the fibre, and the fibre becomes a single mode fibre. It means that for single mode transmission in a MMF, V must be less than 2.405. The wavelength at which the fibre becomes single mode is called **cutoff wavelength**, λ_c of the fibre. Using eqn.(24.29), we can write

$$\lambda_c = \frac{\pi d}{2.405} (NA) \quad (24.32)$$

It is seen from the above equation that single mode property can be realized in a multimode fibre by decreasing the core diameter and/or decreasing Δ such that $V < 2.405$.

In case of GRIN fibres, for larger values of V ,

$$N_m \equiv \frac{V^2}{4} \quad (24.33)$$

24.14 FABRICATION

A number of techniques are available to produce all glass fibres. In one of the methods, known as the double crucible method, fibres are directly produced from the melt.

Double Crucible Technique

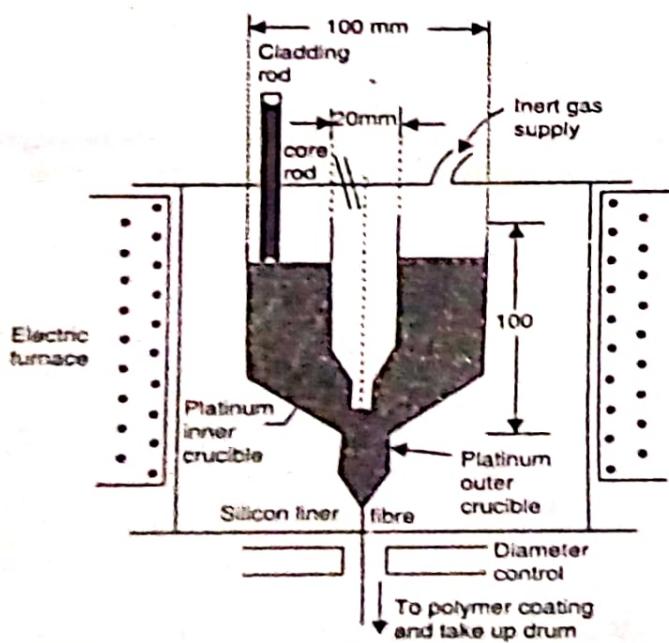


Fig. 24.20

The double crucible consists of two concentric platinum crucibles having thin orifices at the bottom. Raw material for the core-glass is placed in the inner crucible and the raw material for cladding is fed to the outer crucible. The double crucible arrangement is mounted vertically (Fig. 24.20) in a furnace. The furnace is maintained at a suitable temperature to take the raw material into molten state. The fibres are drawn through the thin orifices at the bottom of the crucibles. As both the materials are drawn simultaneously, a filament of core glass surrounded by a tube of cladding glass is obtained in the process. The thickness of the fibre is monitored and the fibre is then coated with a polymer. Subsequently, it is passed through a plastic extrusion die to form a plastic sheath over the fibre.

24.15 LOSSES IN OPTICAL FIBRE

As a light signal propagates through a fibre, it suffers loss of amplitude and change in shape. The loss of amplitude is referred to as *attenuation* and the change in shape as *distortion*.

24.15.1 ATTENUATION

When an optical signal propagates through a fibre, its power decreases exponentially with distance. The loss of optical power as light travels down a fiber is known as **attenuation**. The attenuation of optical signal is defined as *the ratio of the optical output power from a fibre of length L to the input optical power*. If P_i is the optical power launched at the input end of the fibre, then the power P_o at a distance L down the fibre is given by

$$P_o = P_i e^{-\alpha L} \quad (24.34)$$

where α is called the **fibre attenuation coefficient** expressed in units of km^{-1} . Taking logarithms on both the sides of the above equation, we obtain

$$\alpha = \frac{1}{L} \ln \frac{P_i}{P_o} \quad (24.35)$$

In units of dB / km , α is defined through the equation

$$\alpha_{\text{dB/km}} = \frac{10}{L} \log \frac{P_i}{P_o} \quad (24.36)$$

In case of an ideal fibre, $P_o = P_i$ and the attenuation would be zero.

24.15.2 DIFFERENT MECHANISMS OF ATTENUATION

There are several loss mechanisms responsible for attenuation in optical fibres. They are broadly divided into two categories: *intrinsic* and *extrinsic* attenuation. Intrinsic attenuation is caused by substances inherently present in the fiber, whereas extrinsic attenuation is caused by external forces such as bending.

A. Intrinsic Attenuation

Intrinsic attenuation results from materials inherent to the fiber. It is caused by impurities present in the glass. During manufacturing, there is no way to eliminate all impurities. When a light signal hits an impurity in the fiber, either it is scattered or it is absorbed. Intrinsic attenuation can be further characterized by two components:

- Material absorption
- Rayleigh scattering

The intermodal distortion can be reduced if graded index fibre is used. In case of a graded index fibre, the refractive index is larger at the center and it gradually decreases away from the center. A pulse traveling along the axis of the fibre, travels along a shorter path but it takes longer time to reach the end of the fibre since it is traveling through a medium of higher refractive index. On the other hand, the pulse traveling away from the axis travels a longer distance but takes lesser time since it is traveling through a medium of lower refractive index. As a result both the pulses reach the end of the fibre simultaneously. Thus, using a GRIN fibre can reduce the problem of intermodal dispersion. Low NA fibres exhibit smaller dispersion. Dispersion may be restricted by a careful selection of low NA fibre and a narrow spectral width fibre.

In a MMF, all three pulse spreading mechanism exist simultaneously. In case of SMF, only material and wave-guide dispersion exist.

24.16.3 TOTAL DISPERSION

All the above three dispersions contribute pulse spreading during signal transmission through an optical fibre. The total dispersion introduced by an optical fibre is given by the root mean square value of all the three dispersions. Thus,

$$(\Delta t)_T = \sqrt{(\Delta t)_{\text{inter modal}}^2 + (\Delta t)_{\text{mat}}^2 + (\Delta t)_{\text{wg}}^2} \quad (24.49)$$

24.17 BANDWIDTH

It is learnt in the above section that various dispersion mechanisms cause broadening of the information signal in time domain. If the pulses spread more, they can interfere with the adjacent pulses resulting in *Inter Symbol Interference* or ISI in short and there can be so much of ISI that it becomes impossible to distinguish between the individual pulses. Therefore, for a given broadening, the pulses have to be separated by a minimum time interval in order to avoid overlapping of the pulses. This would determine the ultimate information-carrying capacity of the system. When the pulse separation is increased, the data transfer rate decreases. Thus, broadening of pulses puts an upper limit on the rate of pulse transmission. To a first approximation, it may be taken that the

bandwidth in hertz is equal to the digital bit rate. Thus, $B_T = \frac{1}{\tau} = B$, where τ is the input pulse duration. In other words, the maximum allowable transmission rate is called **bandwidth**. In practice, the fibre bandwidth is expressed in terms of MHz.km, a product of frequency and distance. This is known as **bandwidth-distance** product, which specifies the usable bandwidth over a definite distance. With the increase in distance, different dispersion effects would increase in the optical fibre and as a result the usable bandwidth reduces. The attenuation per kilometer and the bandwidth-kilometer product are the important performance parameters of optical fibres.

24.18 CHARACTERISTICS OF THE FIBRES

A. Step-index single-mode fibre

- It has a very small core diameter, typically of about $10 \mu\text{m}$.
- Its numerical aperture is very small.
- It supports only one mode in which the entire light energy is concentrated.
- A single mode step index fibre is designed to have a V number between 0 and 2.4.
- Because of a single mode of propagation, loss due to intermodal dispersion does not exist. With careful choice of material, dimensions, and wavelength, the total dispersion can be made extremely small.

- The attenuation is least.
- The single mode fibres carry higher bandwidth than multimode fiber.
- It requires a monochromatic and coherent light source. Therefore, laser diodes are used along with single mode fibres.

Advantages

- No degradation of signal
- Low dispersion makes the fibre suitable for use with high data rates. Single-mode fiber gives higher transmission rate and up to 50 times more distance than multimode.
- Highly suited for communications.

Disadvantages

- Manufacturing and handling of SMF are more difficult.
- The fibre is costlier.
- Launching of light into fibre is difficult.
- Coupling is difficult.

Applications

- Used as under water cables

B. Step-index multi-mode fibre

- It has larger core diameter, typically ranging between 50-100 μm .
- The numerical aperture is larger and it is of the order of 0.3.
- Larger numerical aperture allows more number of modes, which causes larger dispersion. The dispersion is mostly intermodal.
- Attenuation is high.
- Incoherent sources like LEDs can be used as light sources with multimode fibres.

Advantages

- The multimode step index fibre is relatively easy to manufacture and is less expensive.
- LED or laser source can be used.
- Launching of light into fibre is easier.
- It is easier to couple multi-mode fibres with other fibres.

Disadvantages

- Has smaller bandwidth.
- Due to higher dispersion data rate is lower and transmission is less efficient.
- It is less suitable for long distance communications.

Applications

- Used in data links.

C. Graded-index multi-mode fibre

- Core diameter is in the range of 50-100 μm .
- Numerical aperture is smaller than that of step-index multimode fibre.
- The number of modes in a graded index fibre is about half that in a similar multimode step-index fibre.
- Has medium attenuation.
- Intermodal dispersion is zero, but material dispersion is present.
- Has better bandwidth than multimode step-index fibre.

Advantages

- Either an LED or a laser can be used as the source of light with GRIN fibres.

parts of a human body. It is also called a fiberopticscope. It requires about 10,000 fibres forming a bundle of 1 mm diameter and it can resolve objects with a separation of 70 μm . By allowing direct viewing of what was formerly hidden, a fiberopticscope has become a vital diagnostic tool for industry and medicine. The broncho-fiberopticscope, gastrointestinal fiberopticscope, laparoscope etc are the endoscopes used in medical diagnosis.

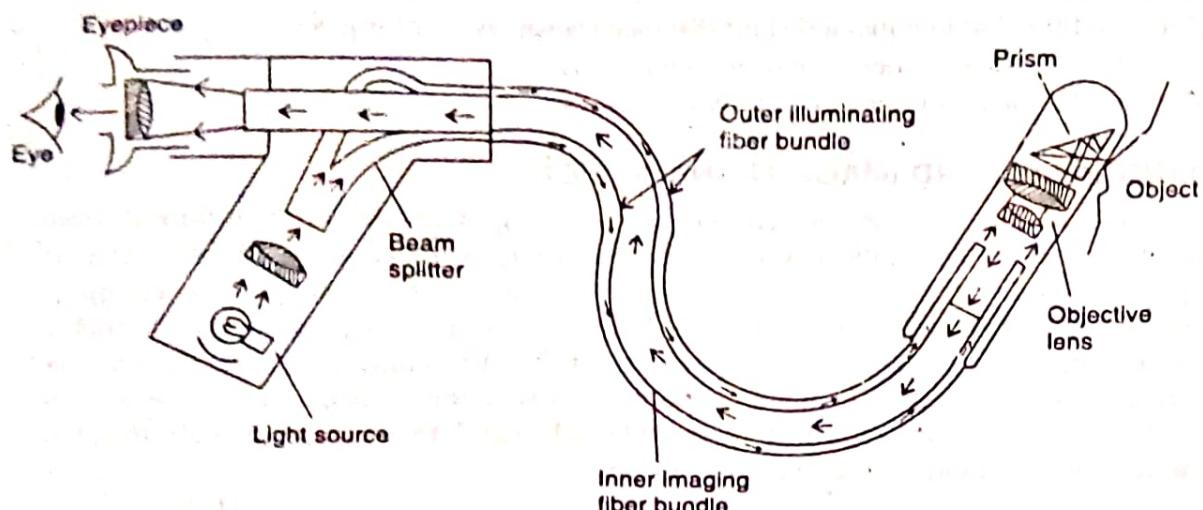


Fig. 24.33

Fig. 24.33 shows the schematic diagram of a flexible endoscope. The endoscopes are designed using low quality, large diameter and short silica fibres. There are two fiber bundles in an endoscope. One of them is used to illuminate the interior of the body and the other is used to collect the reflected light from the illuminated area. A telescope system is added in the internal part of endoscope for obtaining a wider field of view and better image quality. At the object end, there is an assembly of objective lens and prism which are kept in a transparent glass cover and at the viewing end, there is an eye lens. The input end of the endoscope contains a powerful light source. The light rays are focused and coupled to the illuminating fiber bundle. The light rays are finally incident on the surface of the object under study. The light rays reflected from the object surface are received by the objective lens through a prism and are transmitted through the imaging fibre bundle to the viewing end of the scope. Here the eye piece reconstructs the image of the object and one can view the image of the surface of the object. Endoscope pictures can be recorded on a videotape recorder.

24.20.2 OPTICAL COMMUNICATIONS

Traditionally, electronic communications were carried out by sending electrical signals through copper cables, coaxial cables or waveguides. In recent years optical fibres are being used, where light signals replace electrical signals. A basic communications system consists of a transmitter, a receiver and an information pathway. Normally, the information to be communicated is a non-electrical message, which is to be converted first into an electrical form. The conversion is done by a transducer. For example, a microphone converts sound waves into currents. Similarly, a video camera converts images into currents. These electrical messages are of low frequency and cannot be transmitted directly. Therefore, they are superposed on a carrier wave of very high frequency. The process of imposing a message signal on a carrier wave is called modulation. Two different techniques of modulation are available. In analog modulation a continuous wave carries the message. In digital modulation message is transmitted in discrete form using binary digits. The message travels along the transmission channel and is received at the receiver. The receiver demodulates the modulated

wave and separates out the message and feeds to a transducer such a loud speaker. The bandwidth requirement of the message and the bandwidth of the carrier determine the number of messages that can be simultaneously transmitted on an information channel. For example, a bandwidth of 4 kHz is required for voice transmission while 6 MHz bandwidth is required for TV signal transmission. When signals are transmitted in analog form the carrier should have double the above bandwidth. The normal TV communications has a bandwidth of 250 MHz and therefore, it can simultaneously transmit 20 TV programmes. However, instead of microwaves if light waves are used as carrier wave, the bandwidth will be about 10^8 MHz and can therefore transmit about 10^6 TV programs at a time. Thus, the use of the light waves expands our communication capabilities tremendously.

24.20.3 MEDICAL APPLICATIONS

Fibre optic technology is used in medical diagnostics as well as in medical procedures. The fibre optic endoscope is used to inspect internal organs for diagnostic purposes.

In ophthalmology, a laser beam guided by optical fibres is used to reattach detached retina and to correct defective vision.

In cardiology, optical energy transmitted through a optical fibre is used to evaporate built-up plaque that is blocking an artery.

In the treatment of cancer also the optical fibre technology is used. The process involves injection of special chemicals that penetrate only the cancerous cells. Infra red energy transmitted via the fibre illuminates the affected area and is absorbed by the special chemical in the cancerous cells. The heat generated destroys the cancerous cells.

24.20.4 MILITARY APPLICATIONS

An aircraft, a ship or a tank needs tons of copper wire for wiring of the communication equipment, control mechanisms, instrument panel illumination etc. Use of optical fibre in place of copper reduces weight and further maintains true communication silence to the enemy. For example, a shipboard radar system requires about 250 m of coaxial cable, with a weight of 7 tons and a diameter of 45 cm. These cables can be replaced by optical fibre weighing 20 kg and measuring 2.5 cm in diameter.

Fibre guided missiles are used in recent wars. Sensors mounted on the missile transmit video information through the optical fibre to a ground control van and receive commands from the van again. The control van continuously monitors the course of the missile and if necessary corrects its course to ensure that the missile precisely hits the target.

24.21 FIBRE OPTIC COMMUNICATION SYSTEM

A fibre optic communication system is very much similar to a traditional communications system and has three major components. A **transmitter** converts electrical signal to light signals, an **optical fibre** transmits the signals and a **receiver** captures the signals at the other end of the fibre and converts them to electrical signals.

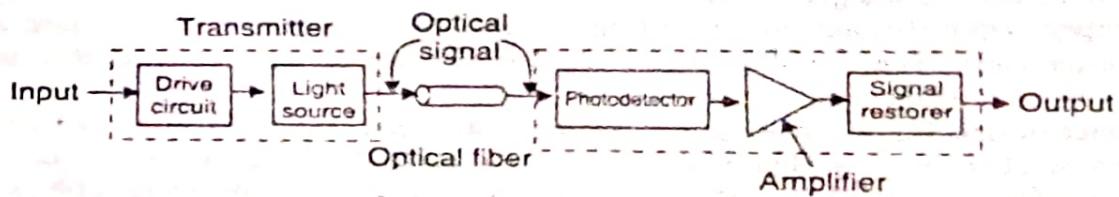


Fig. 24.34: Illustration of a typical fibre optic communication link.

The block diagram Fig. 24.34 illustrates a typical communications system. The transmitter consists of a light source supported by necessary drive circuits. A transducer converts a non-electrical message into an electrical signal and is fed to a light source. The light source is a miniature source, either a light emitting diode or a semiconductor laser. In either case, light is emitted in the IR range with a wavelength of 850 nm (0.85 μm), 1300 nm (1.3 μm) or 1550 nm (1.55 μm). The light waves are modulated with the signal. By varying the intensity of the light beam from the laser diode or LED, analog modulation is achieved. By flashing the laser diode or LED on and off at an extremely fast rate, digital modulation is achieved. A pulse of light represents the number 1 and the absence of light at a specified time represents zero. A message can be transmitted by a particular sequence of these 1s or 0s. If the receiver is programmed to recognize such digital patterns, it can reconstruct the original message. Though the digital modulation requires more complicated equipment such as encoders and decoders and also more bandwidth than analog modulation, it allows greater transmission distance with the same power. This is a great advantage and hence digital modulation has become popular and widely used nowadays. The transmitter feeds the analog or digitally modulated light wave to the transmission channel, namely optical fibre link. The optical signal travelling through the fibre will get attenuated progressively and distorted due to dispersion effects. Therefore, repeaters are to be used at specific intervals to regenerate the signal. At the end of the fibre, an output coupler directs the light from the fibre onto a semiconductor photodiode, which converts the light signals to electrical signals. The photodetector converts the light waves into electrical signals which are then amplified and decoded to obtain the message. The output is fed to a suitable transducer to convert it into an audio or video form.

Applications

Optical fibre communications systems can be broadly classified into two groups: (i) local and intermediate range systems where the distances involved are small and (ii) long-haul systems where cables span large distances.

(i) **Local area networks:** The local area network (LAN) is a computer oriented communication system. LAN operates over short distances of about 1 to 2 km. It is multiuser oriented system. In LAN, a number of computer terminals are interconnected over a common channel allowing each computer to use data and programs from any other. An optical data bus offers a great reduction in cost and increases enormously the information handling capacity.

(ii) **Long-haul communication:** One of the most important applications of fibre optic communication is long-haul communication. Long-haul communication systems are used for long distances, 10 km or more. Telephone cables connecting various countries come under this category. A rather sophisticated long-haul network is the NSFNET which links six supercomputer centres throughout U.S.A.

24.22 MERITS OF OPTICAL FIBRES

Optical fibres have many advantageous features that are not found in conducting wires. Some of the important advantages are given here.

1. Cheaper: Optical fibres are made from silica (SiO_2) which is one of the most abundant materials on the earth. The overall cost of a fibre optic communication is lower than that of an equivalent cable communication system.

2. Smaller in size, lighter in weight, flexible yet strong: The cross section of an optical fibre is about a few hundred microns. Hence, the fibres are less bulky. Typically, a RG-19/U coaxial cable weighs about 1100 kg/km whereas a PCS fibre cable weighs 6 kg/km only. Optical fibres are quite flexible and strong.

3. Not hazardous: A wire communication link could accidentally short circuit high voltage lines and the sparking occurring thereby could ignite combustible gases in the area leading to a great damage. Such accidents cannot occur with fibre links since fibres are made of insulating materials.

5. Immune to EMI and RFI: In optical fibres, information is carried by photons. Photons are electrically neutral and cannot be disturbed by high voltage fields, lightening, etc. Therefore, fibres are immune to externally caused background noise generated through electromagnetic interference (EMI) and radiofrequency interference (RFI).

6. No cross talk: The light waves propagating along the optical fibre are completely trapped within the fibre and cannot leak out. Further, light cannot couple into the fibre from sides. In view of these features, possibility of cross talk is minimized when optical fibre is used. Therefore, transmission is more secure and private.

7. Wider bandwidth: Optical fibres have ability to carry large amounts of information. While a telephone cable composed of 900 pairs of wire can handle 10,000 calls, a 1mm optical fibre can transmit 50,000 calls.

8. Low loss per unit length: The transmission loss per unit length of an optical fibre is about 4 dB/km. Therefore, longer cable-runs between repeaters are feasible. If copper cables are used, the repeaters are to be spaced at intervals of about 2 km. In case of optical fibres, the interval can be as large as 100 km and above.

24.22.1 DISADVANTAGES

Installation and maintenance of optical fibres require a new set of skills. They require specialized and costly equipment like optical time domain reflectometers etc. All this means heavy investment.

24.23 FIBRE OPTIC SENSORS

Fibre optic sensors are transducers, which generally consist of a light source coupled with an optical fibre and a light detector held at the receiver-end. The fibres used could be either multimode or single mode type. The sensors can be used to measure pressure, temperature, strain, the acoustic field, magnetic field, etc physical parameters. The advantages of these sensors are that they are lighter, occupy lesser volume and are cheaper.

The optical fibre merely carries the light beam in some of the sensors and in others the fibre itself acts as the sensor. We study here a few typical examples of the sensors.

24.23.1 TEMPERATURE SENSORS

(a) Intensity modulated sensor

Principle: In this type of sensor, temperature is measured by the modulation of intensity of the reflected light from a target, a silicon layer. The operation of the temperature sensor is based on the $1 \mu\text{m}$ wavelength light-absorption characteristics of silicon as a function of temperature. Depending on the temperature, the amount of light absorbed by the silicon layer varies. The change in intensity of the reflected light is proportional to the change in temperature.

Construction: Fig. 24.35 illustrates a temperature sensor with a multimode fibre. The fibre is coated at one end with a thin silicon layer.

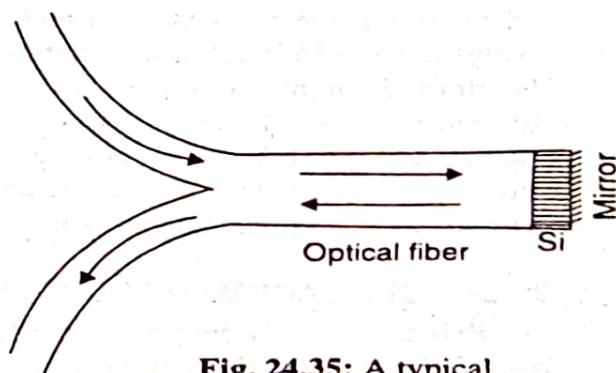


Fig. 24.35: A typical temperature sensor

WORKED-OUT EXAMPLES

Example 24.1: In an optical fibre, the core material has refractive index 1.43 and refractive index of clad material is 1.4. Find the propagation angle.

Solution: $\cos \theta_C = \frac{n_2}{n_1} = \frac{1.40}{1.43} = 0.979$

Therefore, propagation angle $\theta_C = \cos^{-1}(0.979) = 11.8^\circ$

Example 24.2: In an optical fibre, the core material has refractive index 1.6 and refractive index of clad material is 1.3. What is the value of critical angle? Also calculate the value of angle of acceptance cone.

Solution: Critical angle is given by $\sin \phi_c = \frac{n_2}{n_1} = \frac{1.3}{1.6} = 0.8125$
 $\therefore \phi_c = 54.3^\circ$

Acceptance angle $\theta_o = \sin^{-1} \left[\sqrt{n_1^2 - n_2^2} \right] = \sin^{-1} \left[\sqrt{1.6^2 - 1.3^2} \right]$
 $= \sin^{-1}(0.87)$
 $= 60.5^\circ$

Angle of acceptance cone $= 2\theta_o = 121^\circ$

Example 24.3: Calculate the numerical aperture and acceptance angle of an optical fibre from the following data:

$$\mu_1(\text{core}) = 1.55 \text{ and } \mu_2(\text{cladding}) = 1.50$$

Solution: $NA = \sqrt{n_1^2 - n_2^2} = \sqrt{1.55^2 - 1.50^2} = \sqrt{0.153} = 0.391.$

Acceptance angle $\theta_o = \sin^{-1} \left[\sqrt{n_1^2 - n_2^2} \right] = \sin^{-1} \left[\sqrt{1.55^2 - 1.50^2} \right] = 23.02^\circ$

Example 24.4: What is the numerical aperture of an optical fibre cable with a clad index of 1.378 and a core index of 1.546?

Solution: $NA = \sqrt{n_1^2 - n_2^2} = \sqrt{1.546^2 - 1.378^2} = \sqrt{0.491} = 0.70$

Example 24.5: A fibre cable has an acceptance angle of 30° and a core index of refraction of 1.4. Calculate the refractive index of the cladding.

Solution: $\sin \theta_o = \sqrt{n_1^2 - n_2^2}$
 $\therefore \sin^2 \theta_o = n_1^2 - n_2^2$
 $n_2^2 = n_1^2 - \sin^2 \theta_o = (1.4)^2 - \sin^2 30^\circ = 1.96 - 0.25$
 ≈ 1.71
 $n_2 = 1.308$

Example 24.6: Calculate the angle of acceptance of a given optical fibre, if the refractive indices of the core and the cladding are 1.563 and 1.498 respectively.

Solution:

$$\sin \theta_o = \sqrt{n_1^2 - n_2^2} = \sqrt{(1.563)^2 - (1.498)^2} = 0.4461$$

$$\theta_o = \sin^{-1}(0.4461) = 26.49^\circ$$

Example 24.7: Calculate the fractional index change for a given optical fibre if the refractive indices of the core and the cladding are 1.563 and 1.498 respectively.

Solution: Fractional index change $\Delta = \frac{n_1 - n_2}{n_1} = \frac{1.563 - 1.498}{1.563} = \frac{0.065}{1.563} = 0.0415$

Example 24.8: Calculate the refractive indices of the core and the cladding material of a fiber from the following data:

Numerical aperture (NA) = 0.22 and $\Delta = 0.012$

where Δ is the fractional refractive index change.

Solution: $NA = n_1 \sqrt{2\Delta}$

$$0.22 = n_1 \sqrt{2 \times 0.012} = 0.155 n_1$$

$$\therefore n_1 = \frac{0.22}{0.155} = 1.42$$

$$\Delta = \frac{n_1 - n_2}{n_1} \therefore \frac{1.42 - n_2}{1.42} = 0.012 \therefore n_2 = 1.42 - 1.42 \times 0.012 = 1.403$$

Example 24.9: Find the fractional refractive index and numerical aperture for an optical fibre with refractive indices of core and cladding as 1.5 and 1.49 respectively.

Solution: $\Delta = \frac{n_1 - n_2}{n_1} = \frac{1.5 - 1.49}{1.5} = 0.0067$

$$NA = n_1 \sqrt{2\Delta} = 1.5 \sqrt{2 \times 0.0067} = 0.174$$

Example 24.10: A step-index fibre is made with a core of refractive index 1.52, a diameter of 29 μm and a fractional difference index of 0.0007. It is operated at a wavelength of 1.3 μm . Find the V-number and the number of modes that the fibre will support.

Solution: $V = \frac{\pi d}{\lambda_o} n_1 \sqrt{2\Delta} = \frac{3.143 \times 29 \times 10^{-6} \text{ m}}{1.3 \times 10^{-6} \text{ m}} \times 1.52 \sqrt{2 \times 0.0007} = 4.049$

$$\therefore \text{Number of modes, } N = \frac{1}{2} V^2 = \frac{1}{2} (4.049)^2 = 8 \text{ modes}$$

Example 24.11: A step-index fibre is with a core of refractive index 1.55 and cladding of refractive index 1.51. Compute the intermodal dispersion per kilometer of length of the fibre and the total dispersion in a 15 km length of the fibre.

Solution: $\Delta t = \frac{n_1 L}{c} \left[\frac{n_1}{n_2} - 1 \right] = \frac{1.55 \times 10^3 \text{ m}}{3 \times 10^8 \text{ m/s}} \left[\frac{1.55}{1.51} - 1 \right] = 138 \text{ ns/km}$

$$\text{Total dispersion for 15 km length} = \Delta t \times 15 \text{ km} = (138 \text{ ns/km}) \times 15 \text{ km} = 2.07 \mu\text{s}$$