

If the algorithm returns false, then there is at least one vertex  $U \in L$  such that  $\deg(U) = 0$  (not saturated) and hence  $U$  is not assigned to any projects. To show that the perfect assignment corresponds to max-flow: Let  $S$  be the perfect assignment in  $G$ . In  $G$ , for every edge  $e$  between  $L$  and  $R$ , assign  $f(e) = 1$  if  $e \in S$  and  $f(e) = 0$  otherwise. For  $U \in L$ , if  $U$  is involved in  $S$ ,  $f(s, U) = 1$  and  $f(U, t) = 0$ . For  $V \in R$ , if  $V$  is involved in  $S$ ,  $f(V, t) = 1$  and  $f(s, V) = 0$  otherwise.  $|f(A)| = 10 = f(t)$  and  $f$  is a valid flow.