

## 2 **Draft: Constraints on Simplified Dark Matter Models** 3 **using Mono-X Collider Searches**

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8 ABSTRACT: The use of simplified models of dark matter is becoming increasingly prevalent  
9 in collider searches, and while early Run II results are beginning to appear, we look to see  
10 what further information can be extracted from Run I results. We consider three ‘standard’  
11 simplified models that couple quarks to fermionic singlet dark matter: an  $s$ -channel vector  
12 mediator with vector or axial-vector couplings, and a  $t$ -channel scalar mediator. Upper lim-  
13 its on the couplings are calculated, and compared across three alternate channels, namely,  
14 mono-jet, mono- $Z$  (leptonic) and mono- $W/Z$  (hadronic). The strongest limits are observed  
15 in the mono-jet channel, however the computational simplicity, and absence of significant  
16  $t$ -channel model width effects, in the mono-boson channels make these a straightforward  
17 and fast alternative.

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# 1 Introduction

Simplified models have emerged as a powerful tool for the interpretation of collider, direct and indirect detection signals of dark matter (DM). Previously, searches for DM were conducted within the context of both Effective Field Theories (EFTs) [1, 4, 5, 7, 32, 33] and full UV-complete theories such as Supersymmetry [8, 10–12, 40]. The latter approach, though well-motivated, is typified by a broad parameter space and generally yields results which are insensitive to the wider class of DM models. EFT constraints, in comparison, are applicable to a broad range of models and rely on the specification of only a small set of parameters, namely the suppression scale,  $M_\star$ , and the DM mass,  $m_{\text{DM}}$  [25]. In the EFT framework, interactions between the dark and Standard Model (SM) sector are parametrised by a set of higher-dimensional effective operators, that arise when the mass of the mediating particle is assumed to be significantly larger than the momentum transferred in a given interaction. Where this is not the case, the EFT prescription can produce constraints which detour dramatically from those of the associated UV-complete model [24–28]. This is not so important in direct detection experiments where the momentum transferred in the scattering of DM particles with heavy nuclei is generally of the order of tens of keV [13, 14], or in indirect searches where the annihilations of non-relativistic DM particles in the galactic halo occur with momentum transfers of order  $m_{\text{DM}}$  []. However, for hadron collider searches - where the accessible center of mass energy of two colliding baryons may be sufficient to produce the mediator on-shell - the range of validity of the EFT prescription is significantly diminished. Indeed, recent works have shown the EFT approach to be unreliable in certain cases for the interpretation of data collected during the  $\sqrt{s} = 8$  TeV Run I of the Large Hadron Collider (LHC) [15–17]. In light of this, simplified models have become the preferred tool for the interpretation of collider DM searches [18, 31, 53, 55, 56].

In a nutshell, a simplified model (SiM) arises when the heavy mediator which was integrated out in the EFT framework is reintroduced. Like EFTs, SiMs admit the comparison of results obtained in the different avenues of dark matter study [] and are defined by a relatively small set of parameters - namely  $m_{\text{DM}}$ , the mass of the mediator  $M_{\text{med}}$ , and the SM-mediator and DM-mediator coupling strengths,  $g_q$  and  $g_\chi$  (or  $g_{q\chi}$  in the case of a single, SM-DM-mediator coupling). Unlike EFTs, constraints calculated within the context of a SiM are valid across a broad energy range.

In this paper, we examine a phenomenologically distinct set of SiMs. In particular, we place constraints on the SiMs corresponding to the simplest UV-completions of the D5 (vector) and D8 (axial-vector) effective operators in the  $s$ -channel<sup>1</sup>. We also include a case in which a scalar mediator is exchanged in the  $t$ -channel, motivated by its analog of squark

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<sup>1</sup>The D5 and D8 operators form a nice starting point in the analysis of simplified models as they have been studied exhaustively in the past (see refs. [1, 4, 5, 7, 15–17, 32, 33] among others). This attention is motivated by the fact that collider limits for the D5 (D8) operator can be readily transformed into limits on spin-independent (spin-dependent) DM-nucleon scattering and vice versa. With the exception of D1 (see sec. ??), and D9 and D11 (which have no simple simplified model counterparts []), the remaining effective operators induce elastic scattering which is suppressed by powers of the DM velocity or the momentum transferred [19]. Hence, these operators are not often considered in the literature.

exchange in Supersymmetry. In the heavy mediator limit, this model is converted into a combination of the D5 and D8 EFTs via a Fierz transformation.

The models are constrained using public results from mono- $X$  + missing transverse energy ( $E_T^{\text{miss}}$ ) searches conducted by the ATLAS Collaboration. Specifically we focus on searches where  $X$  is either a parton (manifesting in the detector as a narrow-radius jet), a leptonically-decaying  $Z$  boson, or a hadronically-decaying  $W$  or  $Z$  boson (manifesting as a large-radius jet). The purpose of this work is to strengthen existing SiM limits [23, 57] using the full 20.3  $fb^{-1}$  of Run I ATLAS data, and to explore an enhanced phase space with respect to the mediator and DM masses and the relative strength of the couplings to the visible and dark sectors. We choose to treat the mediator width as the minimal value naturally arising, as an alternative to many past analyses which handle this as a fixed value []. We extend the study by providing a cross-check and comparison of the performance of the three targeted collider detection channels, and compare against relic density and direct detection constraints.

The remainder of the paper is organised as follows. Section 2 contains a compendium of the SiMs chosen for analysis and the associated collider phenomenology. Section 3 outlines the techniques used to recast mono- $X$  +  $E_T^{\text{miss}}$  limits on the visible cross-section for any new physics process into constraints on SiMs, and specifically on the couplings  $g_q$  and  $g_\chi$ . Lastly, our results are presented in Section 4 along with a discussion of the implications of this work. Appendices A and B include details of the limit setting and analysis validation procedures.

## 2 Simplified Model Phenomenology

### 2.1 Model Descriptions

We begin with a short set of assumptions: that the DM particle,  $\chi$ , is a weakly interacting Dirac fermion, that it is a singlet under the SM, and that it is the lightest stable new particle. Additionally the new sector is assumed to couple only to the SM quarks; while possible coupling to SM leptons [] or gluons [] has been studied elsewhere, it is beyond the scope of this paper. The nature of the mediating particle then results from these assumptions: in the  $s$ -channel it is chosen to be a vector particle and so must also be a SM singlet, denoted  $\xi$ , while in the  $t$ -channel it is identified as scalar and is necessarily charged and coloured, and labelled  $\phi$ .

The  $s$ -channel models chosen for analysis are characterised by vector ( $sV$ ) or axial-vector ( $sA$ ) couplings to both the dark and SM sectors. They are described by the following interaction Lagrangians:

$$\mathcal{L}_{sV} = -\xi_\mu \left[ \sum_q g_q \bar{q} \gamma^\mu q - g_\chi \bar{\chi} \gamma^\mu \chi \right], \quad (2.1)$$

$$\mathcal{L}_{sA} = \xi_\mu \left[ \sum_q g_q \bar{q} \gamma^\mu \gamma_5 q - g_\chi \bar{\chi} \gamma^\mu \gamma_5 \chi \right], \quad (2.2)$$

where the sum is over all quarks. For the couplings  $g_q$  and  $g_\chi$  to remain within the perturbative regime, they are required to satisfy  $g_q, g_\chi \leq 4\pi$ , though stronger perturbativity requirements do exist [15].

The  $t$ -channel model considered in this paper (abbreviated  $tS$ ) is characterised by a scalar mediator and is motivated by analogy with a common aspect of Supersymmetric models: neutralino DM interacting with the SM sector via  $t$ -channel exchange of a squark [20]. Note that in this Supersymmetric scenario the DM particle is a Majorana fermion. SiMs in which  $\chi$  is of Majorana type are kinematically identical to the corresponding Dirac cases (requiring multiplication of the cross-section by a simple factor in order to compute limits) and so are not covered here<sup>2</sup>. The exception to this rule is the  $s$ -channel vector mediator model, which vanishes if  $\chi$  is a Majorana fermion [21].

In the  $tS$  model, the mediator is allowed to couple to either the left or right-handed quarks as an SU(2) doublet or singlet respectively. Since the LHC is insensitive to the chirality of the quarks, we assume for simplicity that  $\phi$  couples to the left-handed quarks only, and is itself an SU(2) doublet, allowing radiation of a  $W$  boson. To avoid coupling quarks of different generations, and to remain in step with the DM forum recommendations [], we include three generations of mediator  $\phi$ , with equal masses and couplings. The interaction Lagrangian for this model is then:

$$\mathcal{L}_{tS} = \sum_Q g_{q\chi} \bar{Q} P_R \phi \chi + \text{h.c.}, \quad (2.3)$$

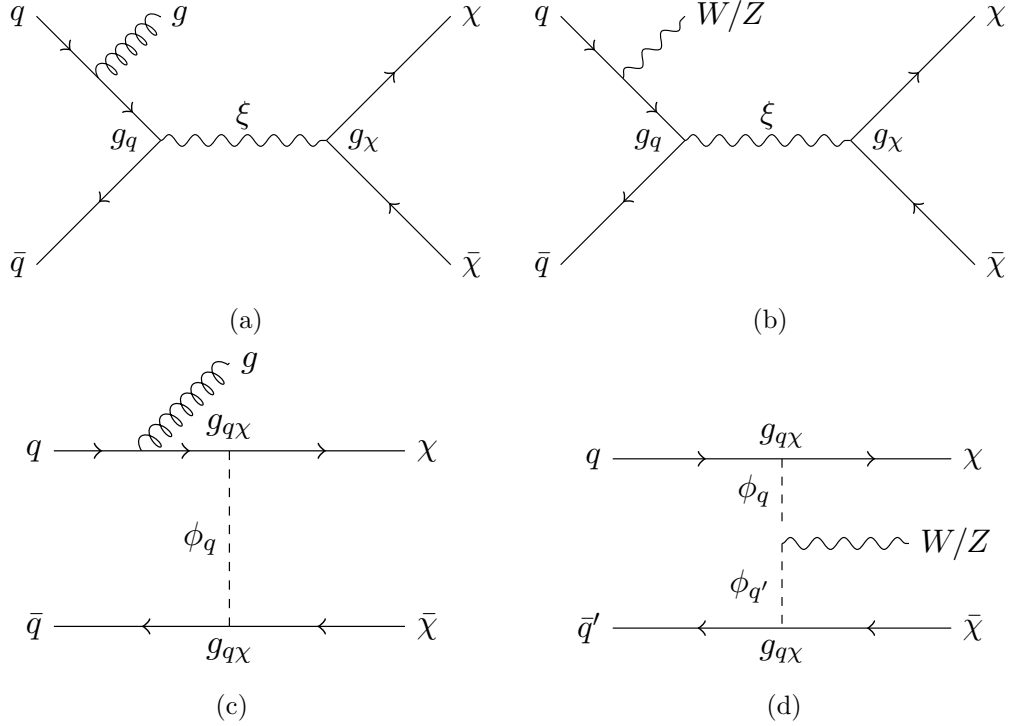
where the sum is over the three  $Q_L$  doublets,  $g_{q\chi}$  is the scalar coupling of the incoming quark,  $\phi$  and  $\chi$ , and  $P_R$  is the usual chiral projection operator.

## 2.2 The Mono- $X + E_T^{\text{miss}}$ Signature

The mono- $X + E_T^{\text{miss}}$  (abbreviated to mono- $X$ ) is a popular collider signal in the search for new physics, particularly in the search for dark matter. Since DM particles are not expected to interact with detector material, they appear as missing transverse energy when balanced against a visible object,  $X$ , that is radiated from the initial or intermediate state (where the latter is permitted in the  $t$ -channel model). For the  $s$ -channel SiMs discussed above, only initial-state radiation is permitted; see figs. 1a and 1b for examples. For the  $tS$  model, radiation of a gluon or electroweak (EW) boson is permitted both from initial state partons (fig. 1c) or from the mediator (fig. 1d).

To fully exploit the potential of the ATLAS detector to record and identify a vast array of particle types, we consider for analysis three scenarios: 1.)  $X$  is a parton which hadronises to form a jet, 2.)  $X$  is a  $Z$  boson which decays into an  $\ell^+\ell^-$  pair, and 3.)  $X$  is a hadronically decaying  $W$  or  $Z$  boson. In the context of DM searches, these signatures are referred to as mono-jet, mono- $Z$ , and mono- $W/Z$  respectively. Note that the mono-jet scenario is the most likely scenario at the LHC owing to the strength of the strong coupling yet the mono- $Z$  channel has the advantage of a relative simple and clean signature. OR: Leptons are in general much cleaner and simpler than jets, so this channel is included here

<sup>2</sup>The exception being in the validation of the mono- $Z$  channel, see Sec. B.2.



**Figure 1:** Representative dark matter pair-production processes with a gluon or  $W/Z$  boson in the final state for the  $s$ -channel (a,b) and  $t$ -channel (c,d) models.

155 to investigate whether the reduction in systematic uncertainties can provide easily obtained  
 156 results that are comparable to the more complicated mono-jet channel. The inclusion of the  
 157 mono-WZ channel is motivated by its fundamentally different signature structure wherein  
 158 event selection is based on large  $R$  jets that are consistent with having come from an EW  
 159 boson.

160 NEW: The most likely scenario at the LHC is production of a jet alongside the in-  
 161 visible  $\chi$  pair, as a result of the strong coupling and prevalence of partons in the initial  
 162 state. However, to fully exploit the potential of the ATLAS detector to record and identify  
 163 a vast array of particle types, we can include the alternative mono-W/Z channels to po-  
 164 tentially glean further information. We can take advantage of the relative cleanliness and  
 165 simplicity of leptons in the leptonically-decaying mono-Z channel, or the large hadronic  
 166 branching fraction, and developing techniques to identify jets resulting from EW bosons,  
 167 in the hadronically-decaying mono-W/Z channel. In both cases, the large multi-jet back-  
 168 ground is reduced, and complications in jet production such as parton-matching can be  
 169 ignored, making these an interesting alternative where speed, efficiency and a reduction in  
 170 jet-associated uncertainties may make up for the loss in sensitivity.

### 171 2.3 Mass and Coupling Points

172 A representative set of dark matter and mediator masses, listed in table 1, are chosen for  
 173 study in each detection channel. DM masses of 3, 30 and 300 GeV were also included in the

$m_\chi$ [GeV]	$M_{\text{med}}$ [GeV]	$s$ -channel		$t$ -channel
		$g_q$	$g_\chi$	$g_{q\chi}$
1, (3), 10, (30), 100, (300), 1000	1, 2, 10, 20, 100, 200, 1000, 2000	1	0.2, 0.5, 1, 2, 5	1

**Table 1:** Mass and coupling points chosen for the analysis of simplified dark matter models. Values in brackets are only included in the mono- $Z$  channel. The mediator masses are primarily representative of three regimes: (near-)degenerate ( $M_{\text{med}} \approx m_\chi$ ), on-shell ( $M_{\text{med}} \geq 2m_\chi$ ), and EFT-like ( $\sqrt{s} \ll M_{\text{med}}$ ). For the  $t$ -channel model,  $M_{\text{med}} > m_\chi$  is also required.

174 mono- $Z$  channel, where ease of production can afford higher granularity. All ( $m_\chi, M_{\text{med}}$ )  
175 combinations are permitted in the  $sV$  and  $sA$  models, while in the  $tS$  model  $M_{\text{med}}$  must  
176 be greater than  $m_\chi$  to ensure stability of the DM particle. The couplings  $g_q$  and  $g_{q\chi}$  are  
177 set to unity, while the DM-mediator coupling in the  $s$ -channel models,  $g_\chi$ , was varied from  
178 0.2 to 5. The mediator masses are chosen to cover a broad range of parameter space and  
179 to coincide with predominantly three regimes: (near-)degenerate ( $M_{\text{med}} \approx m_\chi$ ), on-shell  
180 ( $M_{\text{med}} \geq 2m_\chi$ ), and EFT-like ( $\sqrt{s} \ll M_{\text{med}}$ )<sup>3</sup>. We also allow for the possibility of a light  
181 mediator/heavy WIMP scenario ( $M_{\text{med}} < m_\chi$ ) in the  $sV$  and  $sA$  models.

## 182 2.4 Width Effects

183 An important factor when considering simplified models is to ensure the mediator width is  
184 treated appropriately, as it impacts both the cross-section calculation and, in some cases,  
185 the kinematic behaviour of the model. In previous analyses (ref) it has been common to  
186 consider mediators of a fixed width such as  $\Gamma = M/8\pi$  (the minimal width possible with  
187 only a single quark helicity coupling to the mediator with  $g_q = 1$ ), to take advantage of  
188 the enhancement in cross-section as the width becomes small and on-shell.

189 In this work, the mediator widths are expanded to include coupling to all kinematically  
190 accessible quarks. We assume minimal flavour violation, which implies a universal coupling  
191 to all quark flavours. Following [(other minimum width papers)], the minimum on-shell  
192 kinetic width for each model is given by:

$$\begin{aligned}
\Gamma_{sV} = & \frac{g_\chi^2 M}{12\pi} \left(1 + \frac{2m_\chi^2}{M^2}\right) \left(1 - \frac{4m_\chi^2}{M^2}\right)^{\frac{1}{2}} \Theta(M - 2m_\chi) \\
& + \sum_q \frac{g_q^2 M}{4\pi} \left(1 + \frac{2m_q^2}{M^2}\right) \left(1 - \frac{4m_q^2}{M^2}\right)^{\frac{1}{2}} \Theta(M - 2m_q)
\end{aligned} \tag{2.4}$$

<sup>3</sup>A recent study by Alves et al. found that EFT results do not apply to mediators with a mass less than 2.5 TeV at the LHC during Run I [35].

$$\begin{aligned}\Gamma_{sA} = & \frac{g_\chi^2 M}{12\pi} \left(1 - \frac{4m_\chi^2}{M^2}\right)^{\frac{3}{2}} \Theta(M - 2m_\chi) \\ & + \sum_q \frac{g_q^2 M}{4\pi} \left(1 - \frac{4m_q^2}{M^2}\right)^{\frac{3}{2}} \Theta(M - 2m_q)\end{aligned}\tag{2.5}$$

$$\begin{aligned}\Gamma_{tS} = & \sum_q \frac{g_{q\chi}^2 M}{16\pi} \left(1 - \frac{m_q^2}{M^2} - \frac{m_\chi^2}{M^2}\right) \\ & \times \sqrt{\left(1 - \frac{m_q^2}{M^2} + \frac{m_\chi^2}{M^2}\right)^2 - 4\frac{m_\chi^2}{M^2}} \Theta(M - m_q - m_\chi)\end{aligned}\tag{2.6}$$

193 The above expressions are valid where the width is smaller than the mass of the  
194 mediator.

195 A recent paper [Tom+Karl, others?] demonstrated that the generator treatment of the  
196 mediator as a Breit-Wigner propagator, rather than a true kinetic propagator, is accurate  
197 only up to  $\Gamma \lesssim M/2$ . This was also shown to be a necessary requirement for the following  
198 approximations to hold:

$$\sigma \propto \begin{cases} g_q^2 g_\chi^2 / \Gamma & \text{if } M_{\text{med}} \geq 2m_{\text{DM}} \\ g_q^2 g_\chi^2 & \text{if } M_{\text{med}} < 2m_{\text{DM}} \end{cases}\tag{2.7}$$

199 in the  $sV$  and  $sA$  models, and

$$\sigma \propto g_{q\chi}^4\tag{2.8}$$

200 in the  $tS$  model. When valid, these approximations allow us to greatly simplify our limit  
201 calculations.

202 To simplify the procedure further, we can take advantage of the fact that (with the  
203 notable exception of the  $tS$  model in the mono-jet channel) for each point in  $(m_\chi, M_{\text{med}})$   
204 phase space, the mediator width (and therefore the couplings) do not greatly affect each  
205 model's kinematic behaviour. This is demonstrated in fig. 2, where for the  $sV$  (representing  
206 both the  $sV$  and  $sA$  models) and  $tS$  models, we plot a simplified  $E_{\text{T}}^{\text{miss}}$  distribution, as a  
207 proxy for the full selection in each analysis, for two mass points and a demonstrative set of  
208 couplings such that  $\Gamma < M_{\text{med}}/2$ . The  $E_{\text{T}}^{\text{miss}}$  distribution is predominantly independent of  
209 the mediator width for the  $s$ -channel models in the mono-jet channel, and all models in the  
210 mono- $Z$ <sup>4</sup> channel. However, there is a clear variation in the kinematic behaviour of the  $tS$   
211 model in the mono-jet channel, which can be attributed to additional diagrams (accessible  
212 only in this channel) featuring a gluon in the initial state and subsequently allowing the  
213 mediator to go on-shell. In this scenario, when the resulting quark and DM particle are

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<sup>4</sup>In this discussion, the mono- $W/Z$  channel can be assumed to follow the same logic as for the mono- $Z$  channel.





**Figure 2:** The  $E_T^{\text{miss}}$  distribution of the  $sV$  and  $tS$  models in the mono-jet and mono- $Z$  channels, for some demonstrative masses. The parameter  $\mu$  is defined as  $\Gamma/M_{\text{med}}$ , and is used to demonstrate the impact of a changing width; in particular, the  $tS$  model in the mono-jet channel shows clear width-dependence. The widths are obtained with couplings of 0.1, 1, and 5 where  $\mu < 0.5$  remains true.

both small compared to the mediator mass, they share equally its energy leading to a peak in the  $E_T^{\text{miss}}$  distribution at approximately half the mediator mass.

In the cases where the model behaviour is independent of the width, we can greatly simplify the calculations by assuming the impact of the selection cuts in each channel is unchanged for each masspoint; that is, independent of the couplings. In this case, a simple rearrangement of eqns. 2.7 and 2.8 allows us to obtain upper limits on the model couplings (see App. A for further details of this calculation).

A proper study of the  $tS$  model within the mono-jet channel, where altering the coupling can lead to changed kinematic behaviour, has been performed elsewhere [23], and requires the production of individual samples for each coupling point. This, combined with the challenges associated with including differing orders of  $\alpha_s$ , make the generation process computationally expensive compared to the mono- $Z$  and mono- $W/Z$  channels. We therefore exclude an analysis of the  $tS$  model in the mono-jet channel in this work.

### 3 Recasting mono- $X$ constraints

The procedure for recasting existing mono- $X$  analyses to obtain SiM constraints follows a simple cut-and-count methodology. Firstly, signal events are simulated (described below in section 3.1) with object  $p_T$  smearing applied to approximate the detection efficiency of the ATLAS detector,  $\epsilon$ . The event selection criteria of the mono- $X$  analysis of interest is then applied to the simulated signal samples. Events surviving the selection criteria are counted to determine the likelihood of a dark matter event being observed (referred to as the acceptance,  $\mathcal{A}$ ), which is then used in combination with channel-specific model-independent limits on new physics events to limit the parameter phase space of a given model. For a comprehensive description of the recasting procedure, see appendix A.

In this paper, mono-jet constraints are derived from a search for new phenomena conducted by the ATLAS Collaboration using  $pp$  collisions at  $\sqrt{s} = 8$  TeV as described in ref. [41]. Similarly, the leptonic mono- $Z$  and hadronic mono- $W/Z$  constraints are derived from ATLAS dark matter searches originally optimised for the D1, D5 and D9 effective operators [47? ]. These analyses are described in further detail in sections 3.2, 3.3 and 3.4 respectively.

#### 3.1 Signal Simulation

Monte Carlo simulated event samples are used to model the expected signal for each channel and for each simplified model. Leading order matrix elements for the process  $pp \rightarrow X + \chi\bar{\chi}$  (where  $X$  is specifically one or two jets<sup>5</sup>, a  $Z(\rightarrow \ell^+\ell^-)$  boson or a  $W/Z(\rightarrow jj)$  boson) are first simulated using MADGRAPH5\_AMC@NLO v2.2.2 [49] with the MSTW2008lo68cl PDF [50]. During this stage, the renormalisation and factorisation scales are set to the default sum of  $\sqrt{m^2 + p_T^2}$  for all particles in the final state. Showering and hadronisation are then performed by PYTHIA 8.201 [ ] with the appropriate PDF and using the ATLAS UE Tune AU2-MSTW2008LO [51]. Reconstruction of small-radius jets (from hereon referred to just as ‘jets’) for the mono-jet channel is performed by FastJet [ ] using the anti- $k_T$  algorithm with radius parameter  $R = 0.4$ . Similarly, reconstruction of large-radius jets for the mono- $W/Z$  channel is performed using the Cambridge-Aachen algorithm with  $R = 1.2$ . The latter channel also includes a mass-drop filtering procedure with  $\mu = 0.67$  and  $\sqrt{y}$ <sup>6</sup> = 0.4 (see ref. [ ] for further details), which favours large- $R$  jets with two balanced subjets, consistent with the decay of an EW boson to a (potentially-boosted) dijet pair. Lastly, the detector response is approximated by applying a Gaussian smearing factor to the  $p_T$  of all leptons and jets.

##### 3.1.1 Parton Matching Scheme

In the ATLAS mono-jet analysis, matching of partons generated in MADGRAPH5 to jets generated in PYTHIA is performed using the MLM scheme, with two matching scales, or values of ‘QCUT’, per mass/coupling point. The QCUT values span a broad kinematic

<sup>5</sup>Jets are seeded by any parton excluding the (anti-)top quark.

<sup>6</sup> $\sqrt{y} = \min(p_{T_{j_1}}, p_{T_{j_2}})\Delta R/m_{jet}$  is the momentum balance of the two leading subjets.

range in combination with a cut placed on the leading jet  $p_T$  per event to avoid double-counting. This treatment aims to mitigate the impact of the matching scale on the shape of the  $p_T$  and  $E_T^{\text{miss}}$  distributions; that is, to reduce the uncertainty in those areas of phase space where the mediator mass is significantly larger or smaller than the QCUT value. For the analysis of SiMs, we use instead a single matching scale of 80 GeV. Though not ideal, this approach suitably reproduces the results of the ATLAS mono-jet analysis for the masses of interest (see Sec. B.1). Importantly, it also reduces the complexity and computational expense involved in estimating limits for the mono-jet channel.

We now move to a discussion of each of the mono- $X$  channels separately.

### 3.2 Mono-jet Constraints

The ATLAS mono-jet +  $E_T^{\text{miss}}$  analysis [41] was originally designed to set limits on three new physics scenarios, the most relevant of which is the production of WIMP DM within the context of seven (?) effective operators. The analysis also includes a brief study of a  $Z'$  DM model which is analogous to our  $sV$  model.

Signal selection is carried out based on at least one hard jet recoiling against missing energy. To ensure that the correct back-to-back jet +  $E_T^{\text{miss}}$  topology is selected events are required to have a leading jet,  $j_1$ , with  $p_T > 120$  GeV and  $|\eta| < 2.0$  satisfying  $p_T^{j_1}/E_T^{\text{miss}} > 0.5$ . Surviving events must then satisfy  $|\Delta\phi(j, \vec{E}_T^{\text{miss}})| > 1.0$ , where  $j$  is any jet with  $p_T > 30$  GeV and  $|\eta| < 4.5$ . This criterion reduces the multijet background contribution where the large  $E_T^{\text{miss}}$  originates mainly from jet energy mismeasurement. Note that there is no upper limit placed on the number of jets per event. The contribution from the dominant background processes,  $W/Z$ +jets, is managed with a veto on events containing muons or electrons with  $p_T > 7$  GeV. A further veto is placed on events containing isolated tracks<sup>7</sup> with  $p_T > 10$  GeV and  $|\eta| < 2.5$ , to reduce the contribution from non-identified leptons ( $e$ ,  $\mu$  or  $\tau$ ) in the final state. Lastly, nine separate signal regions are defined with increasing lower thresholds on  $E_T^{\text{miss}}$ , which range from 150 GeV to 700 GeV as shown in table 2.

The ATLAS mono-jet analysis revealed no significant deviation of observed events from the expected SM backgrounds in the Run 1 8 TeV dataset. Subsequently, model-independent limits on new physics signatures were provided in terms of the visible cross-section,  $\sigma \times \mathcal{A} \times \epsilon$ ; these are listed in table 2.

The signal simulation procedure outlined in sec. 3.1 and implementation of the selection criteria discussed above were validated for the mono-jet channel via reproduction of ATLAS limits on the suppression scale,  $M_\star \equiv M_{\text{med}}/\sqrt{g_q g_\chi}$ , for the  $Z'$  model. The details of this process are contained in appendix B.1. Importantly, we observe agreement within  $\sim 12\%$  for all samples.

### 3.3 Mono- $Z$ Constraints

The ATLAS mono- $Z(\rightarrow \ell^+ \ell^-)$  +  $E_T^{\text{miss}}$  analysis [47] was principally designed to constrain a set of EFT models of DM. As a secondary focus, it also includes a short study of a

<sup>7</sup>A track is considered isolated when no additional track with  $p_T > 3$  GeV lies within a cone of radius 0.4 around it.

Signal Region	$E_T^{\text{miss}}$ threshold [GeV]	$\sigma \times \mathcal{A} \times \epsilon$ [fb]
SR1	150	726 (935)
SR2	200	194 (271)
SR3	250	90 (106)
SR4	300	45 (51)
SR5	350	21 (29)
SR6	400	12 (17)
SR7	500	7.2 (7.2)
SR8	600	3.8 (3.2)
SR9	700	3.4 (1.8)

**Table 2:** The ATLAS mono-jet  $E_T^{\text{miss}}$  signal regions and corresponding observed (expected) model-independent upper limits on  $\sigma \times \mathcal{A} \times \epsilon$  at 95% confidence level. Adapted from Ref. [41].

$t$ -channel simplified model similar to our  $tS$  model.

The selection criteria for this analysis are summarised as follows (see the paper for a full description). Electrons (muons) are required to have a  $p_T$  greater than 20 GeV, and  $|\eta|$  less than 2.47 (2.5). Two opposite-sign, same-flavour leptons are selected, and required to have invariant mass and pseudorapidity such that  $m_{\ell\ell} \in [76, 106]$  GeV and  $|\eta^{\ell\ell}| < 2.5$ . The reconstructed  $Z$  boson should be approximately back-to-back and balanced against the  $E_T^{\text{miss}}$ , ensured with the selections  $\Delta\phi(\vec{E}_T^{\text{miss}}, p_T^{\ell\ell}) > 2.5$  and  $|p_T^{\ell\ell} - E_T^{\text{miss}}|/p_T^{\ell\ell} < 0.5$ . Events containing a jet with  $p_T > 25$  GeV and  $|\eta| < 2.5$  are vetoed. Events are also vetoed if they contain a third lepton with  $p_T > 7$  GeV. The signal regions are defined by increasing lower  $E_T^{\text{miss}}$  thresholds:  $E_T^{\text{miss}} > 150, 250, 350, 450$  GeV.

A cut-and-count strategy is used to estimate the total observed yields and expected SM backgrounds in each signal region. The limits on  $\sigma \times \mathcal{A} \times \epsilon$  are not publicly available, so we take the numbers of expected and observed events, along with the associated uncertainties, and convert these into model-dependent upper limits with a single implementation of the HistFitter framework [54] using a frequentist calculator and a one-sided profile likelihood test statistic (the LHC default). The results of this process are displayed in table 3. Note that we use signal regions 1 and 2 only, as our simplified HistFitter approach is inadequate to handle the very low statistics of signal regions 3 and 4. These upper limits are also used for the validation of the mono- $Z$  signal generation and selection procedures (see app. B.2).

### 3.4 Mono- $W/Z$ Constraints

The ATLAS mono- $W/Z + E_T^{\text{miss}}$  search [48] was aimed at constraining the spin-independent effective operators C1, D1, and D5, and the spin-dependent operator D9. The search was originally designed to exploit the constructive interference of  $W$  boson emission from opposite-sign up-type and down-type quarks, leading to DM production wherein the mono- $W$  channel is dominant. Recent studies [ ] have revealed this scenario to violate unitarity and so we ignore it in this analysis. (should we not add some motivation on why we include

Signal Region	$E_T^{\text{miss}}$ threshold [GeV]	$\sigma \times \mathcal{A} \times \epsilon$ [fb]
SR1	150	1.59 (1.71)
SR2	250	0.291 (0.335)

**Table 3:** The ATLAS mono- $Z$   $E_T^{\text{miss}}$  signal regions and corresponding observed (expected) model-independent upper limits on  $\sigma \times \mathcal{A} \times \epsilon$  at 95% confidence level. Adapted using HistFitter from ref. [47].

it? Millie, you commented out these parts, maybe you could pick your favourite sentence or so and put it back in, in case you agree?)

The mono- $W/Z$  event selection is carried out as follows. Large-radius jets are selected using a mass-drop filtering procedure (see sec. 3.1) to suppress non- $W/Z$  processes. Events are required to contain at least one large- $R$  jet with  $p_T > 250$  GeV,  $|\eta| < 1.2$  and a mass,  $m_{\text{jet}}$ , within a 30-40 GeV window of the  $W/Z$  mass (i.e.  $m_{\text{jet}} \in [50, 120]$  GeV). In order to reduce the  $t\bar{t}$  and multijet backgrounds, a veto removes events containing a small- $R$  jet with  $\Delta\phi(\text{jet}, E_T^{\text{miss}}) < 0.4$ , or containing more than one small- $R$  jet with  $p_T > 40$  GeV,  $|\eta| < 4.5$ , and  $\Delta R(\text{small-}R \text{ jet}, \text{large-}R \text{ jet}) > 0.9$ . Electrons, muons and photons are vetoed if their  $p_T$  is larger than 10 GeV and they lie within  $|\eta| < 2.47$  (electrons), 2.5 (muons), 2.37 (photons). Two signal regions were defined with  $E_T^{\text{miss}} > 350$  GeV and  $E_T^{\text{miss}} > 500$  GeV.

The ATLAS analysis used a shape-fit of the mass distribution of the large- $R$  jet to estimate the background yields in the two signal regions, along with the associated statistical and systematic uncertainties. As in the mono- $Z$  case, we do not take the shapes into account but convert the published number of expected and observed events into upper limits on the expected and observed number of new physics events using the HistFitter framework. For the  $E_T^{\text{miss}} > 500$  GeV signal region, we obtain the limits shown in table 4. We do not consider the first signal region with  $E_T^{\text{miss}} > 350$  GeV in the recasting procedure, since the cut-and-count limits extracted could not be convincingly validated. The high  $E_T^{\text{miss}}$  signal region was found to be optimal for most operators studied by the ATLAS analysis. (add that in other cases the two perform similar?)

Signal Region	$E_T^{\text{miss}}$ threshold [GeV]	$\sigma \times \mathcal{A} \times \epsilon$ [fb]
SR2	500	1.35 (1.34)

**Table 4:** The ATLAS mono- $W/Z$   $E_T^{\text{miss}}$  signal region considered in this work and corresponding observed (expected) model-independent upper limits on  $\sigma \times \mathcal{A} \times \epsilon$  at 95% confidence level. Adapted using HistFitter from ref. [47].

## 350 4 Limits on the coupling $\sqrt{g_q g_\chi}$

351 The 95% confidence level upper limits on the sV and sA model couplings,  $\sqrt{g_q g_\chi}$ , and  
 352 the tS model coupling,  $g_{q\chi}$ , which are obtained from each of the mono- $X$  channels, are  
 353 presented in figs. 3 - 8. These quantities were evaluated as described in appendix A and  
 354 correspond to the best limits of each signal region tested.

355 In each plot, the grey region represents the phase space where no meaningful limit was  
 356 obtained, that is, where the limit of at least one of the couplings was found to be greater  
 357 than  $4\pi$  (and thus well out of the perturbative region). The white (hatched) regions  
 358 coincide with those mass points which yield an initial (final) value of  $\sqrt{g_q g_\chi}$  which fails to  
 359 satisfy  $\Gamma < M_{\text{med}}/2$ . Note that only the mono-jet channel produced limits which survive  
 360 this requirement when  $g_\chi/g_q = 0.2$ , as shown in fig. 7. We subsequently omit the plots  
 361 containing the associated limits for the mono- $Z$  and mono- $W/Z$  channels.

362 We note here that values of  $\sqrt{g_q g_\chi}$  and  $g_{q\chi}$  smaller than our hard upper limit of  $4\pi$ ,  
 363 beyond which any results are considered meaningless, may also become increasingly invalid  
 364 as they become less perturbative. Additionally, values for which the width is just within  
 365 our upper validity bound of  $M_{\text{med}}/2$  may be pushed over into the invalid range with the  
 366 addition of new particles, not considered here, which would serve to increase the mediator  
 367 width.

368 Large DM masses: small cross sections, limited by ATLAS analysis optimisation, re-  
 369 quires more data or further optimisation. Small DM masses: have low  $E_T^{\text{miss}}$ , would require  
 370 more statistics. (True for mono- $Z$  and I assume monojet also.)

371 The results are discussed according to channel below.

### 372 4.1 Mono-jet channel

373 The upper limits on the coupling combination  $\sqrt{g_q g_\chi}$  (calculated at 95% confidence interval)  
 374 of the sV and sA models, obtained in the mono-jet channel, are displayed in the left-hand  
 375 column of figs. ??, for  $g_q/g_\chi = 0.5, 1, 2$  and 5 respectively. Additional results for the  
 376  $g_q/g_\chi = 0.2$  case are also shown separately in fig. 7, as these limits are only meaningful  
 377 within the mono-jet channel.

378 Examining first the sV model, we see stronger limits in the region of phase space where  
 379  $M_{\text{med}} > m_\chi$  (why?), and weaker limits where  $M_{\text{med}} < m_\chi$  (due to small cross sections).  
 380 The weakest limits result for large  $m_\chi$  or large  $M_{\text{med}}$ , and in fact are so weak that they  
 381 are pushed into the region of invalidity where  $\Gamma > M_{\text{med}}/2$ ; this is because although the  
 382 acceptance is considerably higher in these regions compared to low masses, the cross section  
 383 is sufficiently small that this effect prevails. Within the valid region ( $m_\chi \in [1, 100]$  GeV  
 384 and  $M_{\text{med}} \in [1, 200]$  GeV), the limit on  $\sqrt{g_q g_\chi}$  generally ranges from 0.1 to 0.7, with a  
 385 handful of on-shell masses reaching a limit of  $\sim 0.05$  in the large  $g_\chi/g_q$  case.

386 As the ratio  $g_\chi/g_q$  varies, the coupling limits tend to remain approximately constant,  
 387 as is expected when the coupling (and hence the width) has been demonstrated to have  
 388 little effect on kinematic behaviour (and using the assumptions of eq. 2.7). As the ratio  
 389 increases, points in the region  $M_{\text{med}} > m_\chi$  disappear as the initial condition,  $g_q = 1$ , leads  
 390 to failure of the width condition. However, one could easily have chosen a smaller initial

value of  $g_q$  to recover these points, and we suggest that the limits in this region would be quite similar to those seen in the  $g_\chi/g_q = 0.2$  and  $0.5$  cases.

In the large ratio scenario, limits for  $m_\chi = 1000$  GeV start to become valid. This is because if  $\sqrt{g_q g_\chi}$  remains constant but the  $g_\chi/g_q$  increases then the value of  $g_q$  is pushed downward and so the width, which is dominated by decays to SM particles, decreases.

The uncertainties on the limits displayed here generally range from ??% to ??%, and are dominated by X.

Moving next to the sA model within this channel, we find that the strongest limits are obtained when  $m_\chi > M_{\text{med}}$ , thanks to both an improved acceptance and a higher cross section. Similarly to the sV model, as the couplings ratio increases, the limit remains approximately constant, and the high  $m_\chi$  points move back into the valid region. The uncertainties for this model are dominated by X and are within the range  $X \sim Y\%$ .

## 4.2 Mono-Z channel

The simplicity of the mono-Z channel relative to the mono-jet channel, and the speed of its production within MADGRAPH5, allowed us to study a finer granularity of points in the mass phase space. The resulting limits on the sV and sA models are shown in the central column of figs. ???. The behaviour of the limits as  $g_\chi/g_q$  varies is similar to that within the mono-jet channel, and overall the limits are weaker compared to that channel by a factor of a few.

The total relative uncertainties on  $\sqrt{g_q g_\chi}$  are generally within 10%, but can range up to 80% in a few cases.

The advantage of the mono-boson channels is in the study of the tS model; since this was not included in the mono-jet channel the strongest limits are obtained with the mono-Z analysis, and are shown in the left-hand side of fig. 8. In general the tS model limits are weaker than the corresponding s-channel points (why?), note that the scale here is increased by a factor of 10. We find stronger limits for smaller  $m_\chi$  and  $M_{\text{med}}$  masses, where larger cross sections compensate for lower acceptances at these points.

## 4.3 Mono-W/Z channel

The limits on the couplings of the sV, sA and tS models, obtained within the mono-W/Z channel, are shown in the right-hand column of figs. ???. This channel was studied to compare with the leptonic mono-Z channel in particular, but a coarser selection of masses was chosen as the limits were initially found to be somewhat weaker. Additionally, further estimates were made: a) as the kinematic behaviour is reasonable independent of the couplings, a single acceptance was found for each  $(m_\chi, M_{\text{med}})$  combination and applied to each value of  $g_\chi/g_q$ , and b) complete systematic uncertainties were generated for a subset of masses and compared to those from the mono-Z channel; from this comparison the mono-Z systematic uncertainties were multiplied by 3 and then applied to the mono-W/Z limits. As a result, the limits obtained in this channel are not intended to be rigorously testable; rather, they are used more to indicate qualitatively how the channel compares.

The ATLAS mono-W/Z analysis was not optimised for a simplified model interpretation, and much of the phase space produced insignificant numbers of events passing the



event selection, with up to 200 thousand events generated. Generally, the limits are a factor of a few weaker again than those from the mono- $Z$  channel, which is both consistent with the limits on the EFT models studied in the ATLAS analyses, and expected following the use of a cut-and-count interpretation of the mono- $W/Z$  public results (can we say this? Point is to compare with them probably doing a shape analysis to improve their limits). Some exceptions do exist however - the low- $M_{\text{med}}$  region of the sA model shows limits comparable to those within the mono- $Z$  channel.

Overall, the uncertainties from this channel lie within the range XXX.

## 5 Conclusion

### 5.1 Comparison with Relic Density Constraints

In Figs. ?? we show lines where the constraint on the coupling corresponds to the coupling strength that would reproduce the correct DM density if DM is a thermal relic of the early universe. For points above the line, the LHC constraints naively rule out the couplings leading to the correct relic density. Below this line the relic density coupling is still allowed.

In this scenario, the measured abundance is approximately related to the unknown self-annihilation cross-section via

$$\Omega_{\text{DM}} h^2 \simeq \frac{2 \times 2.4 \times 10^{-10} \text{ GeV}^{-2}}{\langle \sigma v \rangle_{\text{ann}}}. \quad (5.1)$$

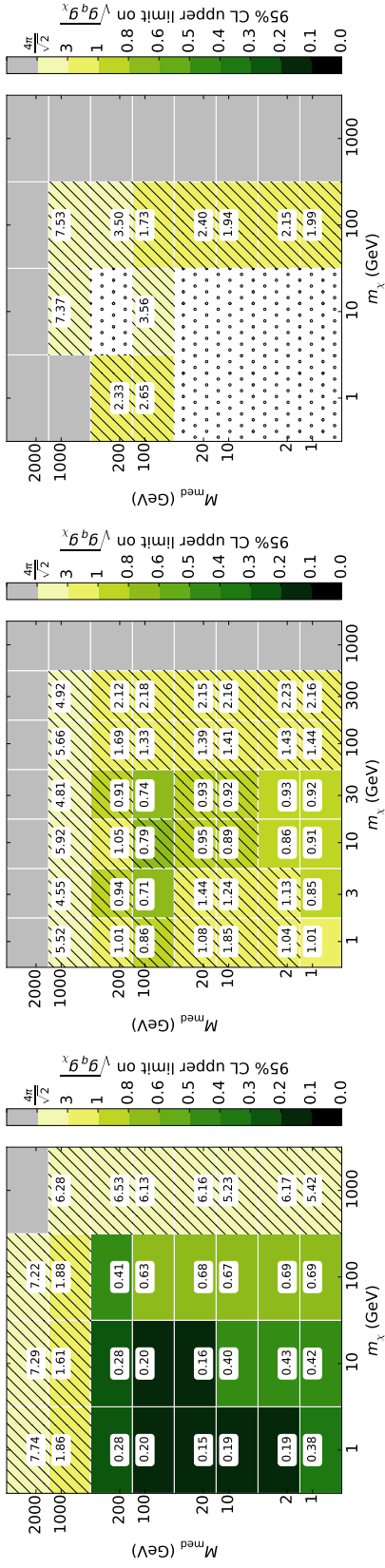
This is used with measurements of the DM abundance by Planck,  $\Omega_{\text{DM}}^{\text{obs}} h^2 = 0.1199 \pm 0.0027$  [36], to find  $\langle \sigma v \rangle_{\text{ann}} \simeq 4.0 \times 10^{-9} \text{ GeV}^{-2}$  for thermal relic DM. This relation is only approximately accurate, and so we use the Micromegas code [52] to determine the coupling strength leading to the correct relic density for each model. We verified this technique against the semi-analytic technique outlined in e.g. Ref. [37].

If the DM mass lies at the electroweak scale, the thermal relic scenario provides a natural explanation for the observed DM density, and so the coupling strengths leading to the correct relic density are a natural benchmark with which to compare constraints from other DM searches, indicating the scale at which we expect the couplings may lie. However the relic density couplings should by no means be treated as a constraint. If the DM was not produced thermally or if there is some unknown effect which modifies the evolution of the density with temperature, then these relations break down. Further, even if DM is a thermal relic, then the relationship no longer holds if there are other annihilation channels not taken into account, or if there are other beyond-SM particles contributing to the DM abundance.

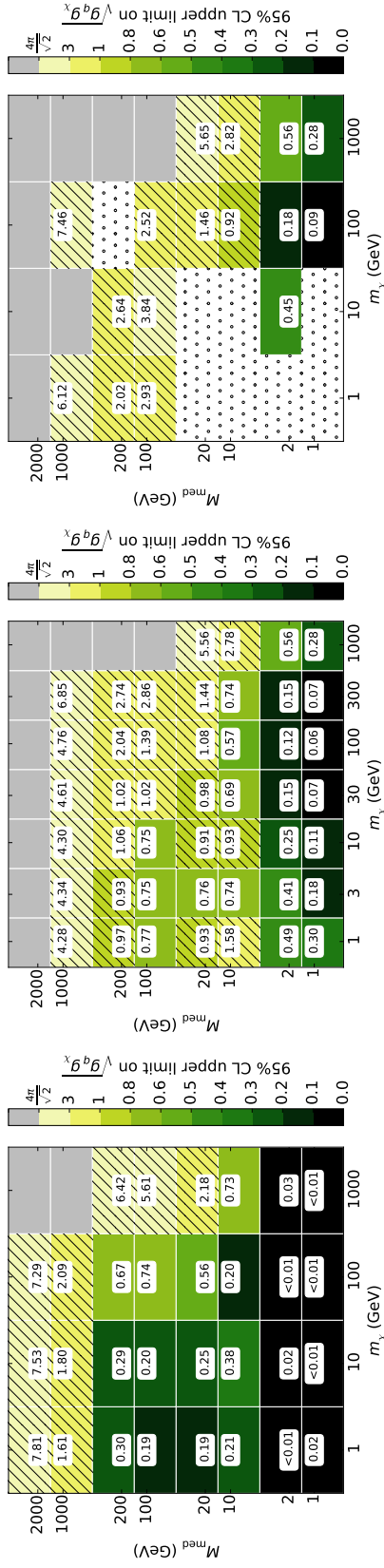
### 5.2 Comparison with Direct Detection Constraints

Normally DD is better for vector and LHC is better for Axial vector, but in our case DD is better in both cases until you get to around  $m_{\text{DM}} = 5 \text{ GeV}$  at which point our interpolation has broken down.



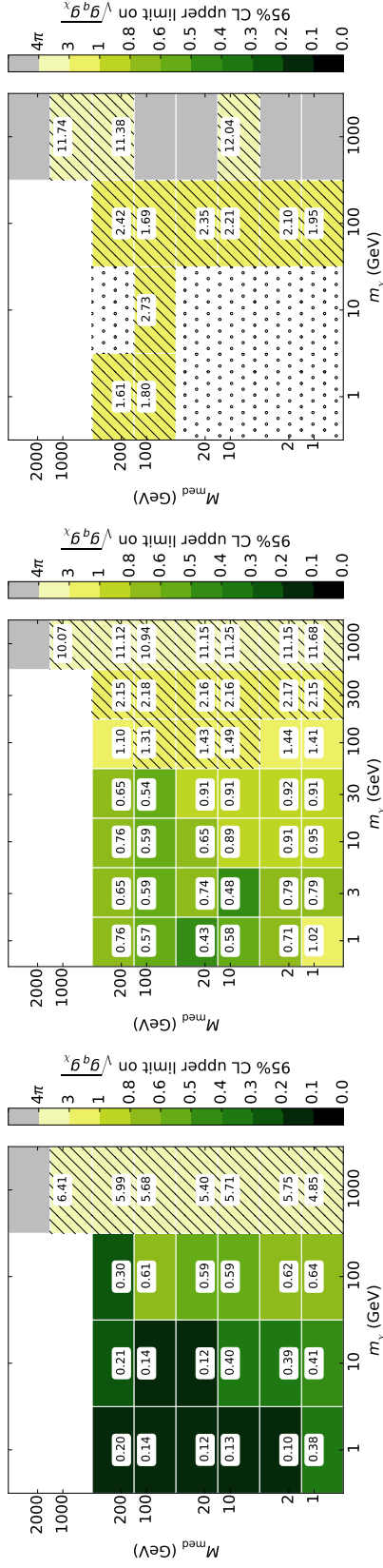


(a) sV model,  $g_q/g_\chi = 0.5$ , mono-jet channel. (b) sV model,  $g_q/g_\chi = 0.5$ , mono-Z channel. (c) sV model,  $g_q/g_\chi = 0.5$ , mono- $W/Z$  channel.

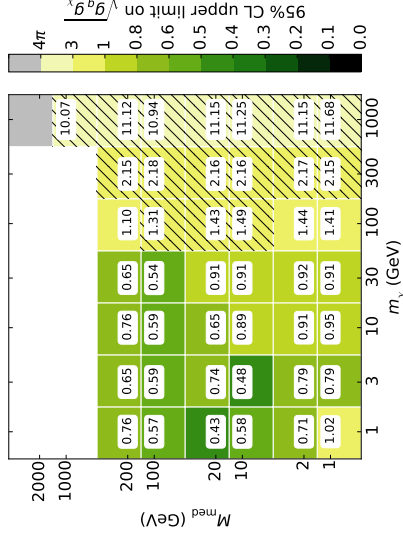


(d) sA model,  $g_q/g_\chi = 0.5$ , mono-jet channel. (e) sA model,  $g_q/g_\chi = 0.5$ , mono-Z channel. (f) sA model,  $g_q/g_\chi = 0.5$ , mono- $W/Z$  channel.

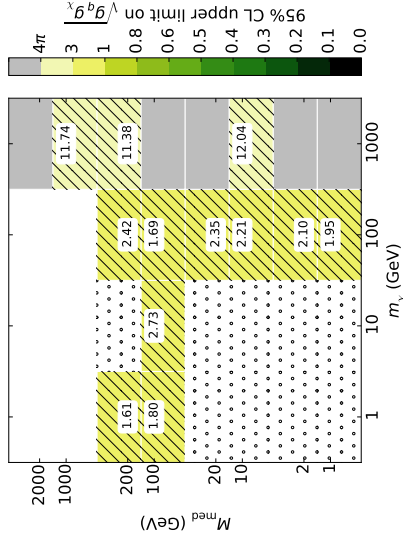
**Figure 3:** Upper limits on the coupling for the  $s$ -channel models in the mono-jet (left), mono-Z (centre) and mono- $W/Z$  (right) channels, for  $g_\chi/g_q = 0.5$ . The grey region represents the phase space where no meaningful limit was obtained. The hatched region represents a limit which leads to a width greater than  $M_{\text{med}}/2$ , so the validity of the calculation begins to fail. The dotted region represents phase space where insufficient statistics were available.



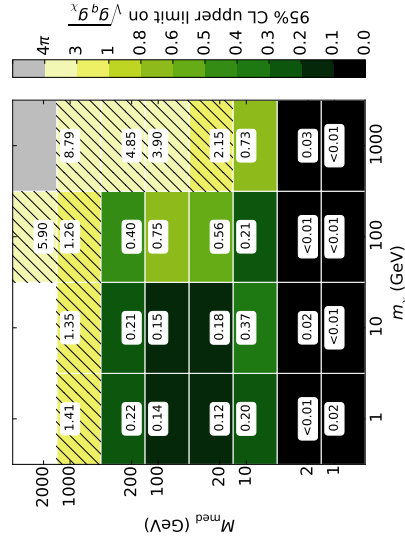
(a) sV model,  $g_q/g_\chi = 1$ , mono-jet channel.



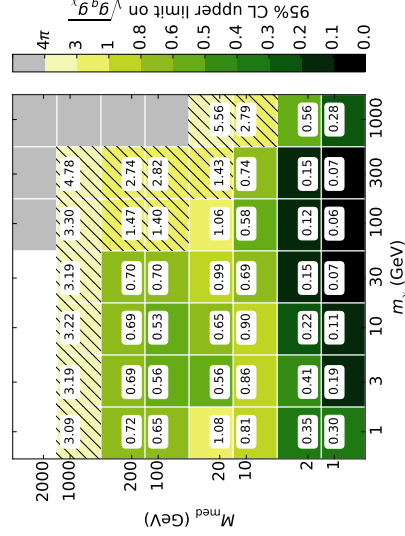
(b) sV model,  $g_q/g_\chi = 1$ , mono-Z channel.



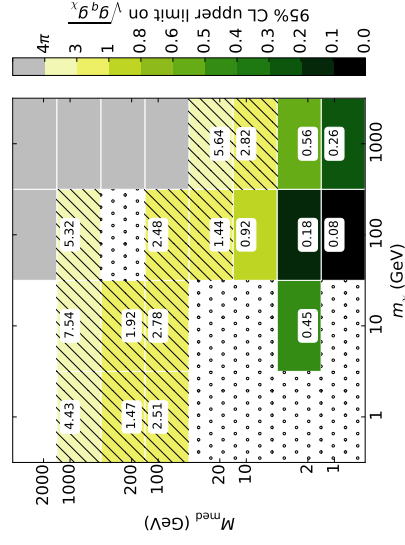
(c) sV model,  $g_q/g_\chi = 1$ , mono-W/Z channel.



(d) sA model,  $g_q/g_\chi = 1$ , mono-jet channel.

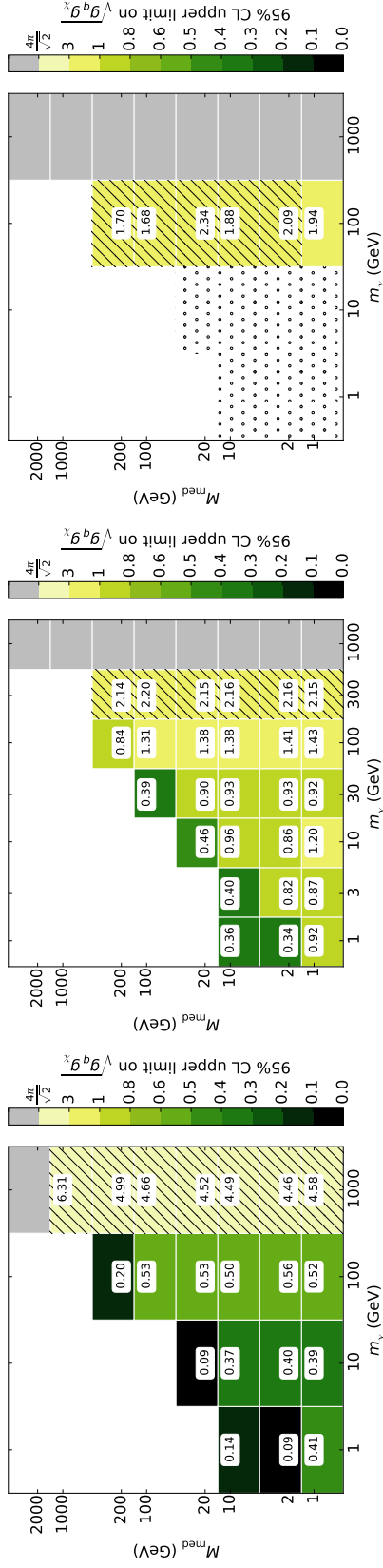


(e) sA model,  $g_q/g_\chi = 1$ , mono-Z channel.

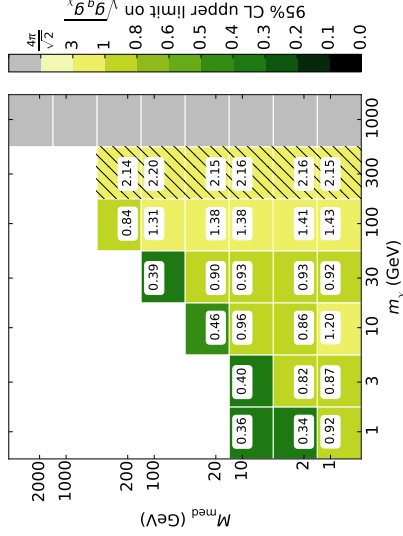


(f) sA model,  $g_q/g_\chi = 1$ , mono-W/Z channel.

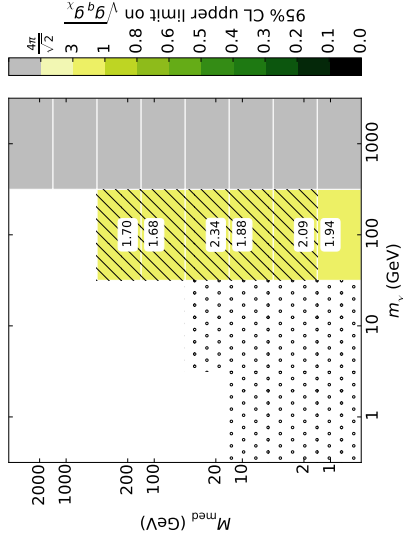
**Figure 4:** Upper limits on the couplings for the s-channel models in the mono-jet (left), mono-Z (centre) and mono-W/Z (right) channels, for  $g_\chi/g_q = 1$ . Refer to fig. 3 for details.



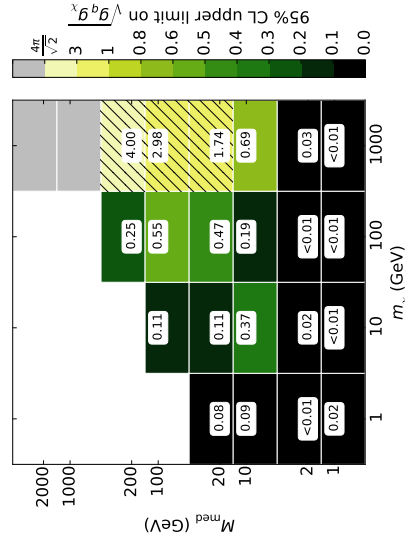
(a) sV model,  $g_q/g_\chi = 2$ , mono-jet channel.



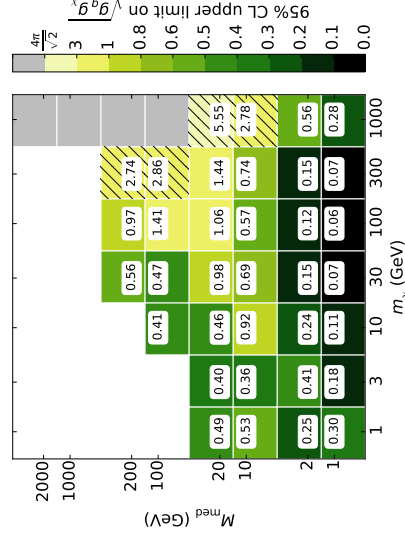
(b) sV model,  $g_q/g_\chi = 2$ , mono-Z channel.



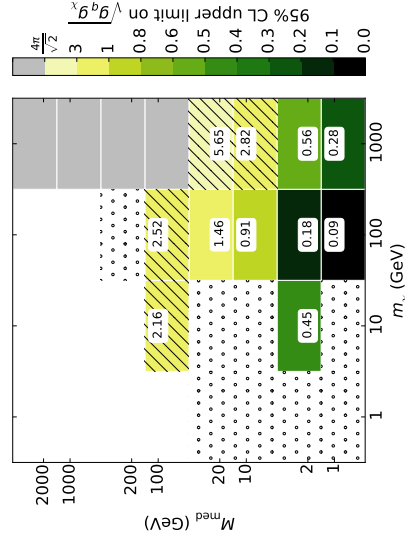
(c) sV model,  $g_q/g_\chi = 2$ , mono-W/Z channel.



(d) sA model,  $g_q/g_\chi = 2$ , mono-jet channel.

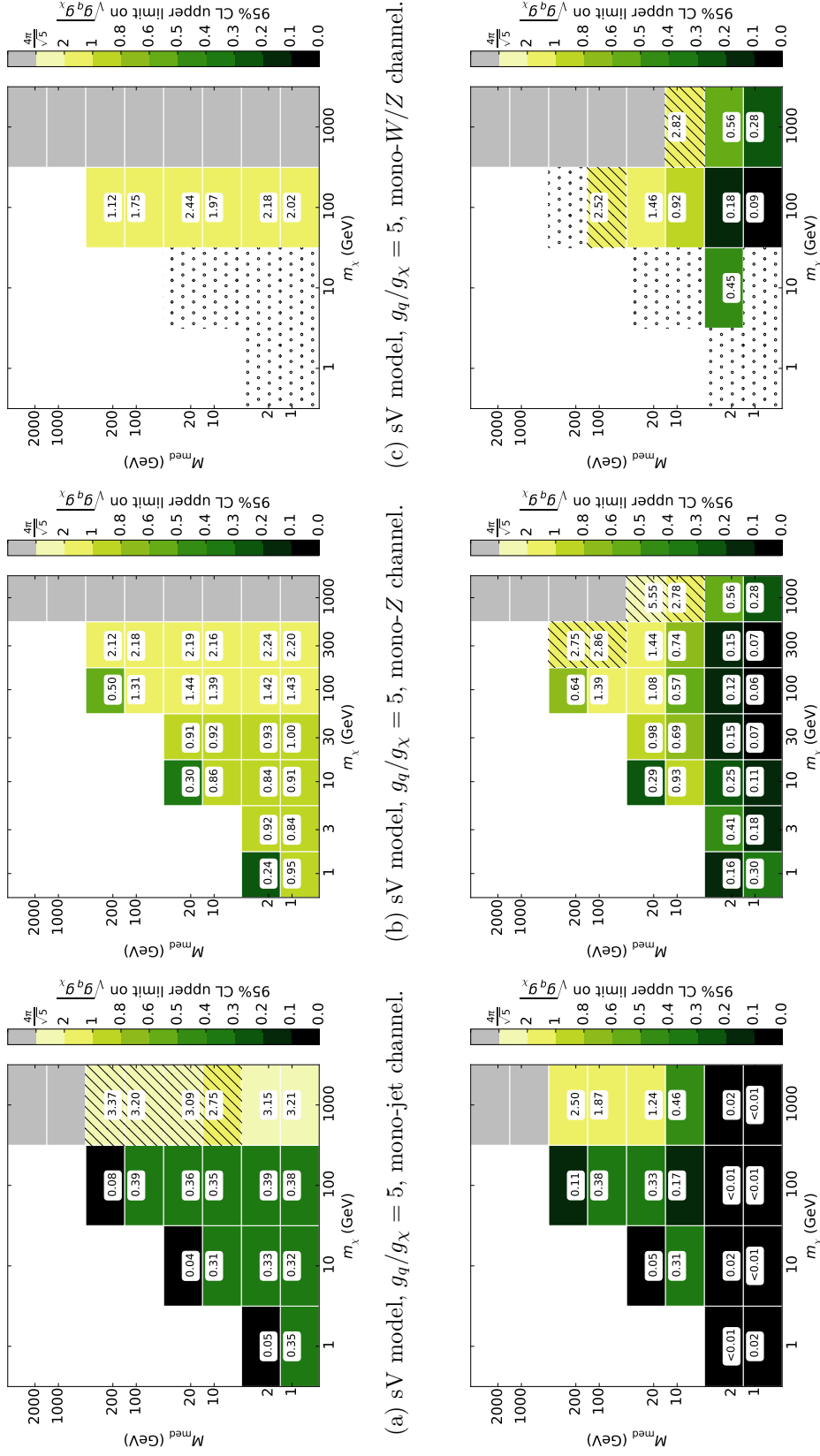


(e) sA model,  $g_q/g_\chi = 2$ , mono-Z channel.

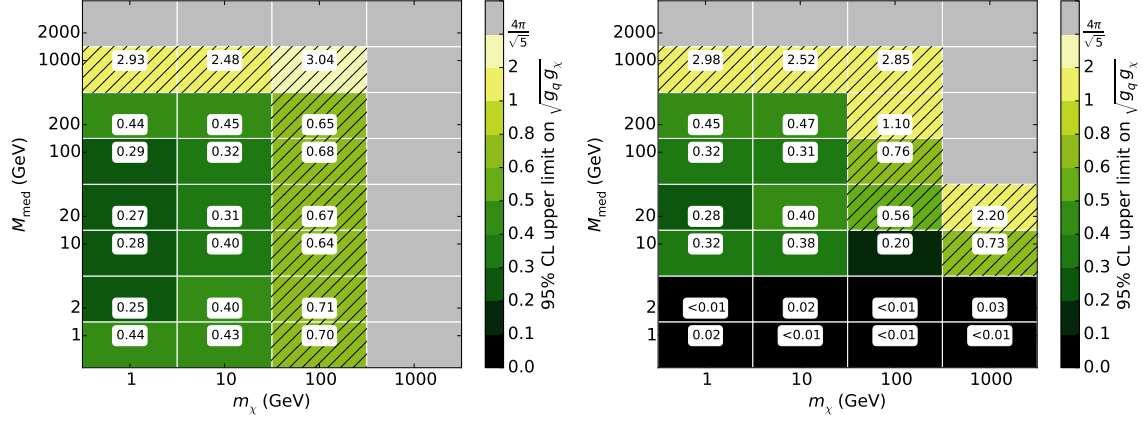


(f) sA model,  $g_q/g_\chi = 2$ , mono-W/Z channel.

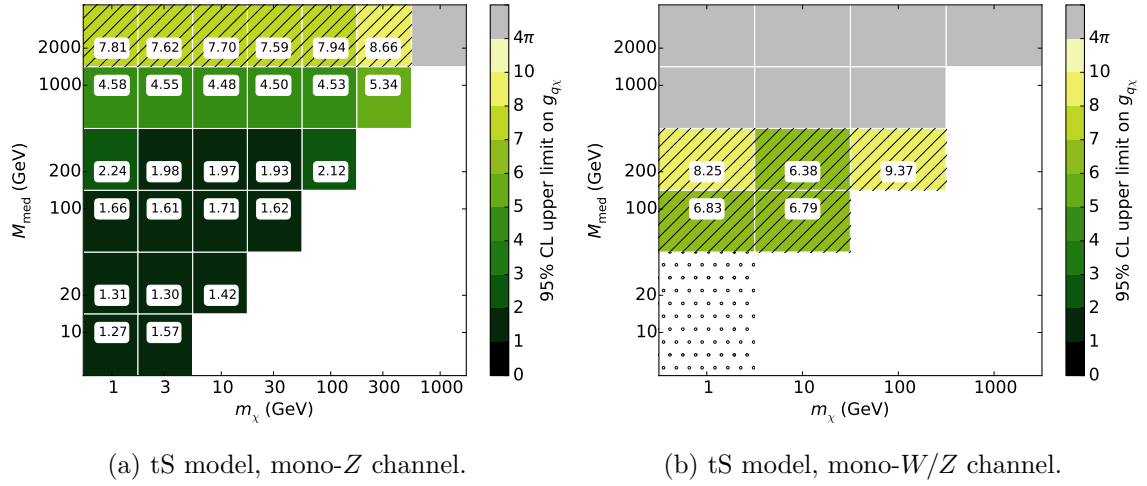
**Figure 5:** Upper limits on the coupling for the  $s$ -channel models in the mono-jet (left), mono-Z (centre) and mono-W/Z (right) channels, for  $g_\chi/g_q = 2$ . Refer to fig. 3 for details.



**Figure 6:** Upper limits on the coupling for the  $s$ -channel models in the mono-jet (left), mono-Z (centre) and mono-W/Z (right) channels, for  $g_\chi/g_q = 5$ . Refer to fig. 3 for details.



**Figure 7:** Upper limits on the coupling for the  $s$ -channel models in the mono-jet channel, for  $g_\chi/g_q = 0.2$ . Refer to fig. 3 for details.



**Figure 8:** Upper limits on the coupling  $g_{q\chi}$  for the  $t$ -channel model in the mono-Z (left) and mono-W/Z (right) channels. Refer to fig. 3 for details.

### 5.3 Discussion

- Comparison to direct mediator searches: dijet gives strongest constraints on mediator especially for small  $r$ . Missing ET still good for large  $M$  but in this region EFT is fine
  - Comparison to non-grid searches, e.g. McCullough et al
  - Comparison to grid searches e.g. Zurek et al, Jacques and Nordstrom
- MonoX searches dominate.

## 6 Acknowledgements

### A Limit setting strategy

In this appendix we present a summary of the procedure employed to calculate the 95% confidence level (CL) limits on the coupling parameter  $\sqrt{g_q g_\chi}$ , where this parameter can be replaced with  $g_{q\chi}$  for the tS model, and  $M_\star$  in the validation of the mono-jet analysis.

#### A.1 Nominal Values

For each simplified model, the nominal value for the observed limit on the cross-section for the process  $pp \rightarrow X + \chi\bar{\chi}$  is calculated using the formula:

$$\sigma_{obs}^{lim}(pp \rightarrow X + \chi\bar{\chi}) = \frac{N_{obs}}{\mathcal{L} \times \mathcal{A} \times \epsilon} \quad (\text{A.1})$$

where  $N_{obs}$  is a calculated 95% CL upper limit on the number of signal events in the channel and signal region of interest; it is a model-independent quantity.  $\mathcal{L}$  is the integrated luminosity,  $\mathcal{A}$  is the acceptance (the fraction of signal events passing the channel/SR-specific selection criteria) and  $\epsilon$  is the efficiency of the ATLAS detector for selecting channel/SR-specific signal events. For all channels the total luminosity is  $20.3 \text{ fb}^{-1}$  and  $\mathcal{A} \times \epsilon$  is regarded as a single variable.

In the following discussion,  $\sqrt{g_q g_\chi}$  is assumed to also represent  $g_{q\chi}$  from the tS model.

The nominal value for the observed limit  $Y$ , where  $Y$  is the suppression scale  $M_\star$  in the validation of the mono-jet analysis, or the coupling values  $\sqrt{g_q g_\chi}$  in the general case, is then calculated using

$$Y_{obs}^{lim} = Y^{gen} \left( \frac{\sigma_{obs}^{lim}}{\sigma^{gen}} \right)^{\frac{1}{4}}. \quad (\text{A.2})$$

(Note: this section needs to be re-written to account for the on-shell case as well.)

The signal region in each case is chosen based on where the best ‘expected’ limit exists, where that limit is calculated assuming that exactly the expected SM background is observed.

main systematic sources	PDF/tune	factorisation and renormalisation scales	matching scale (mono-jet only)
variation ‘up’	NNPDF2.1LO + Monash tune	2	160 GeV
nominal	MSTW2008lo68cl + ATLAS UE AU2-MSTW2008LO	1	80 GeV
variation ‘down’	CTEQ6L1 + ATLAS UE AU2-CTEQ6L1	0.5	40 GeV

**Table 5:** The sources of systematic uncertainty considered in this analysis. Each point in phase space is varied up or down by one of these sources, and the systematic uncertainty is taken to be the average difference in  $\mathcal{A}'$  from the nominal value.

## A.2 Uncertainty Estimation

Our nominal limits on  $M_\star$ ,  $\sigma(pp \rightarrow X + \chi\bar{\chi})$  and  $\sqrt{g_q g_\chi}$  rely on both  $\sigma_{gen}$  and  $\mathcal{A} \times \epsilon$  and so are subject to systematic uncertainties which derive from our choice of MC generation procedure. For our MC samples, there are three key sources of systematic uncertainty: the factorisation and renormalisation scales, the strong coupling constant ( $\alpha_s$ ) and the parton distribution function (PDF).

Firstly, the factorisation and renormalisation default scales are varied simultaneously by factors of 2 (‘up’) and 0.5 (‘down’). The systematic effects of the strong coupling constant and the PDF are difficult to separate and so are treated in tandem. We assume that the systematic uncertainty introduced by  $\alpha_s$  at matrix-element level is negligible when compared to the PDF uncertainties, as demonstrated to be valid in Ref. [42]. The variation of  $\alpha_s$  in conjunction with a PDF is done with the use of specific tunes in PYTHIA, which we change simultaneously with the PDF choice to estimate the uncertainty on  $\Delta\sigma_{gen}$ . The nominal choices of PDF and tune are varied ‘up’ to NNPDF2.1LO PDF + Monash tune, and ‘down’ to CTEQ6L1 PDF and ATLAS UE AU2-CTEQ6L1 tune. **Millie: put discussion of matching scale systematic here.** These systematic uncertainty sources are summarised in table 5.

Following eqns. A.1 and A.2, the relative uncertainty in the limit on  $\sqrt{g_q g_\chi}$  (or on  $M_\star$ ) is given by (to be updated with on-shell case also)

$$\frac{\Delta\sqrt{g_q g_\chi}}{\sqrt{g_q g_\chi}} = \frac{1}{4} \sqrt{\left(\frac{\Delta\sigma_{gen}}{\sigma_{gen}}\right)^2 + \left(\frac{\Delta(\mathcal{A} \times \epsilon)}{\mathcal{A} \times \epsilon}\right)^2 + \left(\frac{\Delta\mathcal{L}}{\mathcal{L}}\right)^2} \quad (\text{A.3})$$

For  $P = \sigma_{gen}, \mathcal{A} \times \epsilon$ , the relative error  $\Delta P/P$  is found by summing in quadrature the separate sources of uncertainty, according to

$$\left(\frac{\Delta P}{P}\right)_{\text{total}}^2 = \left(\frac{\Delta P}{P}\right)_{\text{scale}}^2 + \left(\frac{\Delta P}{P}\right)_{\text{PDF+tune}}^2 + \left(\frac{\Delta P}{P}\right)_{\text{matching}}^2 \quad (\text{A.4})$$

where  $\Delta P$  is taken as the average distance from the nominal value  $P$  when the systematic source is varied up and down. The statistical uncertainty is taken into account rather conservatively by using the 95%CL *lower* limit on  $\mathcal{A} \times \epsilon$  as calculated with the Wald approximation, i.e.  $\mathcal{A} \times \epsilon \rightarrow (\mathcal{A} \times \epsilon) - \Delta(\mathcal{A} \times \epsilon)$ . The uncertainty on the luminosity is less than 3%, so is considered to be negligible in comparison to other systematic sources.

## B Validation of signal simulation and event selection procedures

### B.1 Monojet Channel

The MC generation and signal selection procedures for the mono-jet channel are validated via reproduction of the ATLAS limits on  $M_\star \equiv M_{\text{med}}/\sqrt{g_q g_\chi}$ , for the  $s$ -channel vector simplified model. A comparison of SR7 limits for a representative sample of mediator masses with  $m_\chi = 50$  GeV,  $\Gamma = M/8\pi$  and  $\sqrt{g_q g_\chi} = 1$  is presented in Table 6. In general, good agreement is observed between the ATLAS and reproduced limits, with a maximum difference (with respect to the ATLAS limit) of <23%. We note that a discrepancy of a few percent is expected and allowed for three reasons. Firstly, the MC generation procedure employed in this analysis does not include a full simulation of the ATLAS detector. Instead, reconstruction effects are simulated by applying a Gaussian smearing of the jet  $p_T$  by a conservative factor of 5%. Next, the matching procedure employed in this analysis (and discussed in detail in Section 3.1.1) is largely simplified. This introduces a substantial uncertainty when compared to the matching procedure utilised by the ATLAS mono-jet group. For example, where the ATLAS group observe a maximum matching scale uncertainty of 5% for events with  $E_T^{\text{miss}}$  above 350 GeV, we observe an uncertainty of  $\sim 30\%$ . Lastly, the 95% CL uncertainties on  $M_\star$  for this work are estimated in a non-identical fashion to that used in the ATLAS analysis. In particular, where the ATLAS limits are estimated using the HistFitter package, we use the approach described in appendix A. As our results are consistently more conservative than those of the ATLAS analysis, we consider this approach acceptable.

### B.2 Mono-Z Channel

The ATLAS mono- $Z$  analysis result includes an upper limit on the coupling  $g_{q\chi}$  for a  $t$ -channel simplified model that is very similar to the model investigated here, and so is used for validating our signal generation and selection procedure. The most significant differences are in the number of mediating particles — the ATLAS model includes just two mediators (*up*- and *down*-type) compared to our six — and in the nature of the DM particle, which is taken to be Majorana. This latter choice does not impact the kinematic behaviour, but does scale the cross section by a simple factor. Additionally, while we use a



$M$ [TeV]	$M_{\star}^{\text{ATLAS95}}$ [GeV]	$M_{\star}^{95}$ [GeV]	Difference [%]
0.05	91	89	2.16
0.3	1151	1041	7.3
0.6	1868	1535	11.8
1	2225	1732	12.0
3	1349	1072	6.8
6	945	769	8.5
10	928	724	10.6
30	914	722	9.6

**Table 6:** Comparison of the 95% CL upper limits on  $M_{\star}$  from this work ( $M_{\star}^{95}$ ) and from the ATLAS mono-jet analysis ( $M_{\star}^{\text{ATLAS,95}}$ ) [41]. The values shown in the second and third columns are for the processes  $pp \rightarrow j\chi\bar{\chi}$  and  $pp \rightarrow jj\chi\bar{\chi}$  for the  $s$ -channel vector mediator model with  $m_{\chi} = 50$  GeV,  $\Gamma = M/8\pi$ ,  $\sqrt{g_q g_{\chi}} = 1$  and QCUT = 80 GeV.

$m_{\chi}$ [GeV]	$M_{\text{med}}$ [GeV]	$g_{q\chi}^{95\% \text{CL}}$ (ATLAS)	$g_{q\chi}^{95\% \text{CL}}$ (this work)	Difference [%]
10	200	1.9	2.0	5.3
	500	2.8	3.2	14.3
	700	3.5	4.4	25.7
	1000	4.5	5.2	15.6
200	500	3.4	4.0	17.6
	700	4.2	4.5	7.1
	1000	5.2	5.3	1.9
400	500	5.5	5.7	3.6
	700	6.1	6.5	6.6
	1000	7.2	7.4	2.8
1000	1200	23.3	24.1	3.4

**Table 7:** Comparison of the upper limit on  $g_{q\chi}$  from the ATLAS analysis [47] and this work.

universal coupling  $g_{q\chi}$  to all three quark generations, the analysis used a model which set  $g_{t,b\chi} = 0$ .

Table 7 shows the 95% CL upper limits on  $g_{q\chi}$  that we calculate using the same  $t$ -channel model and our own generation procedure (using the values in table ??), compared with the limits on this same variable taken from the ATLAS analysis. The difference as a percentage of the ATLAS limit is also shown in the table. We see reasonable agreement; most of the 11 points in parameter space are within 10% of the ATLAS limits, and all are within 26%. Additionally, our results are consistently more conservative, which is to be expected due to the less sophisticated nature of our generation procedure. Similarly to the

$m_\chi$ [GeV]	$M_\star^{90\%CL}$ (ATLAS) [GeV]	$M_\star^{95\%CL}$ (this work) [GeV]	Difference [%]
1	570	499	12.5

**Table 8:** Comparison of the upper limit on  $M_\star$  from the ATLAS analysis [48] and this work.

mono-jet validation, the dominant effects are due to the use of  $p_T$  smearing applied to the leptons, rather than considering the full reconstruction effects, and the simple systematic treatment that was used with HistFitter.

### B.3 Mono-W/Z Channel

The signal generation as well as event selection for the mono- $W/Z$  channel are validated by reproducing the published limit on  $M_\star \equiv M_{\text{med}}/\sqrt{g_q g_\chi}$  for the D5 EFT operator at a dark matter mass of 1 GeV. The comparison is not straight-forward for the following reasons: the D5 limits are only published for the low- $E_T^{\text{miss}}$  signal region, whereas we use the high- $E_T^{\text{miss}}$  signal region only in this recast; the ATLAS analysis uses a shape fit to extract the limit on the number of new physics events, whereas we use a cut-and-count approach; their limit is quoted at 90% CL, ours at 95% CL. Nevertheless, the value of the limit agrees within 12.5 %, where the result of this work is weaker, as expected for the above reasons.

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