Inequalities Notes

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1 Algebraic Inequalities

Theorem 1 (AM-GM). Let a_1, \ldots, a_n be non-negative real numbers. Then:

$$\frac{a_1 + \dots + a_n}{2} \ge \sqrt[n]{a_1 \dots a_n}$$

with equality if and only if $a_1 = a_2 = \cdots = a_n$.

Theorem 2 (Cauchy-Schwarz). Let $a_1, \ldots, a_n, b_1, \ldots, b_n$ be real numbers. Then:

$$(a_1^2 + \dots + a_n^2)(b_1^2 + \dots + b_n^2) \ge (a_1b_1 + \dots + a_nb_n)^2$$