Data Structures

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Introduction

1.1 What is a Data Structures Course

Data Structures is all about defining the different ways we can organize data.

1.2 Why This Book?

1.2.1 Where Does This Book Fit Into a Computer Science Curriculum

Education in Computer Science is based around three core topics: translating the steps of solving a problem into a language a computer can understand, organizing data for solving problems, and techniques that can be used to solve problems. These courses typically covered in a university's introductory course, data structures course, and algorithms course respectively, although different universities decide exactly what content fits in which course. Of course, there is are lot more concepts in computer science, from operating systems and low level programming, to networks and how computers talk to each other. However, all these concepts rely on the knowledge gained in the core courses of programming, data structures, and algorithms.

This textbook is all about Data Structures, the middle section between learning how to program and the more advanced problem solving concepts we learn in Computer Science. Here, we focus on mastering the different ways to organize data, recognize the internal and performative differences between each structure, and learn to recognize the best (if there is one) for a given situation.

1.2.2 What Are My Base Assumptions about the Reader?

This textbook assumes that the student has taken a programming course that has covered the basics. Namely: data types such as ints, doubles, booleans, and strings; if statements, for and while loops; and object orient programming. The first writeup of the textbook will be done in Java, but I will try to add as much Python into the book as well.

- 1.3 To The Instructor
- 1.4 To The Student

The Array

- 2.1 Array Operations
- 2.2 Finding Values in an Array

Analyzing Algorithms

3.0.1 Cost

 \mathbf{Time}

Space

Energy

Other costs - Bandwidth

- 3.1 Big O Notation
- 3.1.1 Space Complexity
- 3.2 The Formal Mathematics of Big O Notation
- 3.3 Other Notations

Lists

The first data structure we will be studying is the list. The list is by far the most relatable data structure, as humans deal with lists on a regular basis.

4.1 What is a list?

When you get right down to it, lists are defined by order.

```
public static <E> boolean isPermutation(List<E> listA, List<E> listB) {
        if(listA.size() != listB.size()) {
                return false;
        for(int i = 0; i < listA.size(); i++){</pre>
                E item = listA.get(i);
                int countA = 0;
                int countB = 0;
                for (E element : listA) {
                        if(item.equals(element)){
                                countA++;
                }
                for (E element : listB) {
                        if(item.equals(element)){
                                countB++;
                        }
                if(countA != countB) {
                        return false;
                }
        return true;
}
```

4.2 ArrayLists

- 4.2.1 Generics
- 4.2.2 Building an ArrayList
- 4.2.3 More Restrictive or Permissive Generics

4.3 LinkedLists

I will be presenting the directions to building a fully functional singly-linked list and doubly-lined list. These directions will differ from the mechanics of how your programming language of choice implements them, but have the same time complexity for their operations. My implementation is constructed with the goal of making the code easy to understand and the decisions that need to be for adding and removing reflect each other. Finally, my code aims to minimize the number of null-pointer exceptions and their ilk a programmer would make.

The full implementations ca be found at the end of the Chapter.

4.3.1 Building a Singly LinkedList

We open up our linked list with a class declaration. If our language uses generics, we specify it there. I'll be choosing not to inherit from the built-in list so we can focus solely on our own code and no external distractions.

In Java, our code looks like this.

```
public class LinkedList<E> {
    In Python
    class LinkedList(object):
```

Instance Variables

4.3.2 The Node

In a s

We want the Node class to be a private/internal class, so that the Node we write for a singly linked list and doubly linked list won't get mixed up in our coding environments. This also applies for other data structures that will be using nodes.

Adding

To add an item to a linked list, we need to

4.4 Analysis

Stacks

- 5.1 Building a Stack
- 5.2 Mazes Stacks and Backtracking
- 5.3 Discrete Finite Automata

Queues

A Queue (pronounced by saying the first letter and ignoring all the others) is a data structure which emulates the real word functionality of standing in a line (or queue, for those from Commonwealth nations). In a Queue, items are processed in the order they are inserted into the Queue. So if Alice enters the Queue, followed by Bob, followed by Carla, Alice would be the first to leave the Queue, then Bob, and then Carla.

The use cases for Queues are fairly obi

6.1 Linked Based Implementation

6.2 Array Based Implementation

We could use

Recursion

- 7.1 Recursive Mathematics
- 7.2 Recursive Problem Solving
- 7.2.1 Recursive Backtracking
- 7.2.2 Recursive Combinations
- 7.3 Recursion and Puzzles
- 7.4 Recursion and Art
- 7.5 Recursion and Nature

Trees

8.1 Binary Search Trees

A diagram of a binary search tree. It is made up of nodes, represented by circles, and edges (also called links or branches), represented by arrows.

- 8.2 Heaps
- 8.2.1 Priority Queues
- 8.3 Trees and Heaps in Java

Sorting

9.1 Quadratic-Time Algorithr	ic-Time Algorith	ıms
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- 9.1.1 Bubble Sort
- 9.1.2 Selection Sort
- 9.1.3 Insertion Sort
- 9.2 Log-Linear Sorting Algorithms
- 9.2.1 Tree Sort
- 9.2.2 Heap Sort
- 9.2.3 Quick Sort
- 9.2.4 Merge Sort
- 9.3 Unique Sorting Algorithms
- 9.3.1 Shell Sort
- 9.3.2 Radix Sort
- 9.4 State of the Art Sorting Algorithms
- 9.4.1 Tim Sort
- 9.4.2 Quick Sort
- 9.4.3 Distributing and Parallelization

Sets and Maps

- 10.1 Sets
- 10.2 Maps
- 10.3 Hash Tables
- 10.3.1 Creating a Hash Function
- 10.4 Map Reduce

Graphs

11.1	Introduction	and	History

- 11.2 Qualities of a Graph
- 11.2.1 Undirected Edges
- 11.2.2 Directed Edges
- 11.2.3 Weighted Edges
- 11.3 Directed Acyclic Graphs
- 11.4 Building a Graph
- 11.4.1 Adjacency List
- 11.4.2 Adjacency Matrix
- 11.5 Graph Algorithms
- 11.5.1 Searching and Traversing

Breadth First Search

Depth First Search

- 11.5.2 Shortest Path
- 11.5.3 Topological Sorting
- 11.5.4 Minimum Spanning Trees
- 11.6 Graphs, Humans, and Networks
- 11.6.1 The Small World

The Milgram Experiment

The Less-Known Milgram Experiment

- 11.6.2 Scale Free Graphs
- 11.7 Graphs in Art and Nature Voronoi Tessellation
- 11.8 Distributed Hash Tables



Figure 11.1: The wings of a dragonfly. Credit: Joi Ito (CC BY 2.0)

Other Data Structures

12.1 Skip Lists