

B \bowtie Tree

A mechanism to drive existing B⁺Trees to do Join Internally.

RDBMS challenges

Performance has been always a challenge for relational databases. A major problem with relational database that a good schema requires many tables in relation between them, and in consequence the calculation of many joins to satisfy the queries.

DBA spends lots of time to tune the database. Some database schemas are not in BCNF just to avoid some joins. Also some materialized views are just to avoid it. Star Schema born from the fact that joining is complex and to simplify joins.

Standard indexes

The standard indexes used in relational databases are B+tree, hashed keys and bitmap indexes but the problem all suffers from some restrictions.

B+tree have among others the fact that it work just on one table.

Hashed keys are very fast but they require a full key lookup, a perfect match, and a unique identifying value.

Bitmap is also good but it has a limit on the number of different values a column can have.

Bitmap Join Index

Bitmap join index is efficient but is not general; it is based on Star Schema. Has a lots of bitmap arrays depending on the size of the dimensions tables.

Materialized Views are redundant. No one use Materialized View to order a table, because index is the more natural way. Also B⁺Tree index is the more natural way to get the join.

B[⋈]TREE Overview

B[⋈]tree is a new index technology that is based on B+tree that pre-join the tables inside it.

B[⋈]tree uses “Virtual Tables” and “Join Path Lists” to make pre-join internally, so it doesn't use the multidimensional index technique with the benefit of more easier and more concise algorithm, no limit for the number of tables in join and easy use: the same way as a native B+tree.

Given n Tables in join, scanning the B[⋈]tree return a set of pointers for the rows in join for any possible combination of tables in join.

B⁺TREE Index

To understand how B⁺TREE Index works let see what happens when we insert a new Row R_m from Table T_i into the database.

Suppose that table T_i is in Direct Join with a table T_k , we have to look for all the Rows $R_n \dots R_z$ in T_k that satisfy the join condition with R_m and insert Rows references to $R_m R_n \dots R_m R_z$ in the virtual table T_{ik} .

The process should be repeated for $R_m R_n \dots R_m R_z$ with a table in join at least with one of the base tables constituting the Virtual Join Table T_{ij} and so on until we scan a path in the sequence of tables in join.

Transformation of Existing B+Tree

- The internal definition for the creation of a B+Tree take in consideration the following:
 - Name of B+Tree index follow by an index
 - Number of base tables constituting the virtual table indexed by the B+Tree
 - Length and type of Keys
 - Length and type of Inherited Keys (They are supplementary fields inserted in the B+Tree but they are not part of the key and they are not used for comparison)
- Declare the page of B+Tree as a buffer of bytes and divide it as needed. Many existing B+Tree follow this technique to support different type of multiple columns Key.
- The Leaf Page structure consists of:
 - Pointer to the previous sibling page
 - number of elements in which everyone consists of:
 - Space for the columns forming the keys
 - Space for the Data Pointers (Row Ids) to reference the Row in every table
 - Space for the columns forming the Inherited Keys
 - Pointer to the next sibling Page

Transformation of Existing B+Tree (continue)

- The Non Leaf Page structure consists of:
 - Pointer to a child page which key values are smaller than all the keys in the page
 - number of elements in which everyone consists of:
 - Space for the columns forming the keys
 - Pointer to a child page which key values are bigger than the keys in the Element
- Due to the fact that many join keys are duplicates, change has been made for the duplicates in the sense when 2 keys are equals, we consider the data references for them. The B+Tree keeps these possibly duplicated keys separate internally by combining the unique sequence of data references with each key. The process of combination is done logically, and requires no additional space for key storage.

Many advanced B+Tree in the market use (Key, Data Reference) combination to refer to unique Row eliminating duplicates internally and use additional fields others than the one forming the key to avoid access to the table.

So for those B+Trees, the only modification is instead of space of one Data Reference is a space for multiple Data Reference Space.

Definitions

- Base Table:

Base tables are database objects whose structure and the data they contain are both on disk.

- Virtual Table:

Virtual tables are tables whose contents are derived from base tables. Only its definition (base tables Names constituting it) is stored on disk.

Definitions

Direct Join:

Two tables are in Direct Join if there is a link between them (in other sense if there is common columns between them).

Join Graph:

A graph representing direct join between tables.

Adjacency List:

List for every table T_i in the database all those tables in direct Join with it.

Generating Join Graph

- Base Tables represent the vertexes of the Join Graph.
- Due to the fact that join is commutative, for every pair of tables in direct join between them as defined by DBA create an undirected edge to link them.
- It is very easy to know which tables are in direct join with others tables from the definition of common columns between them.

The algorithm for generating the Linked List representation of the join Graph is the following:

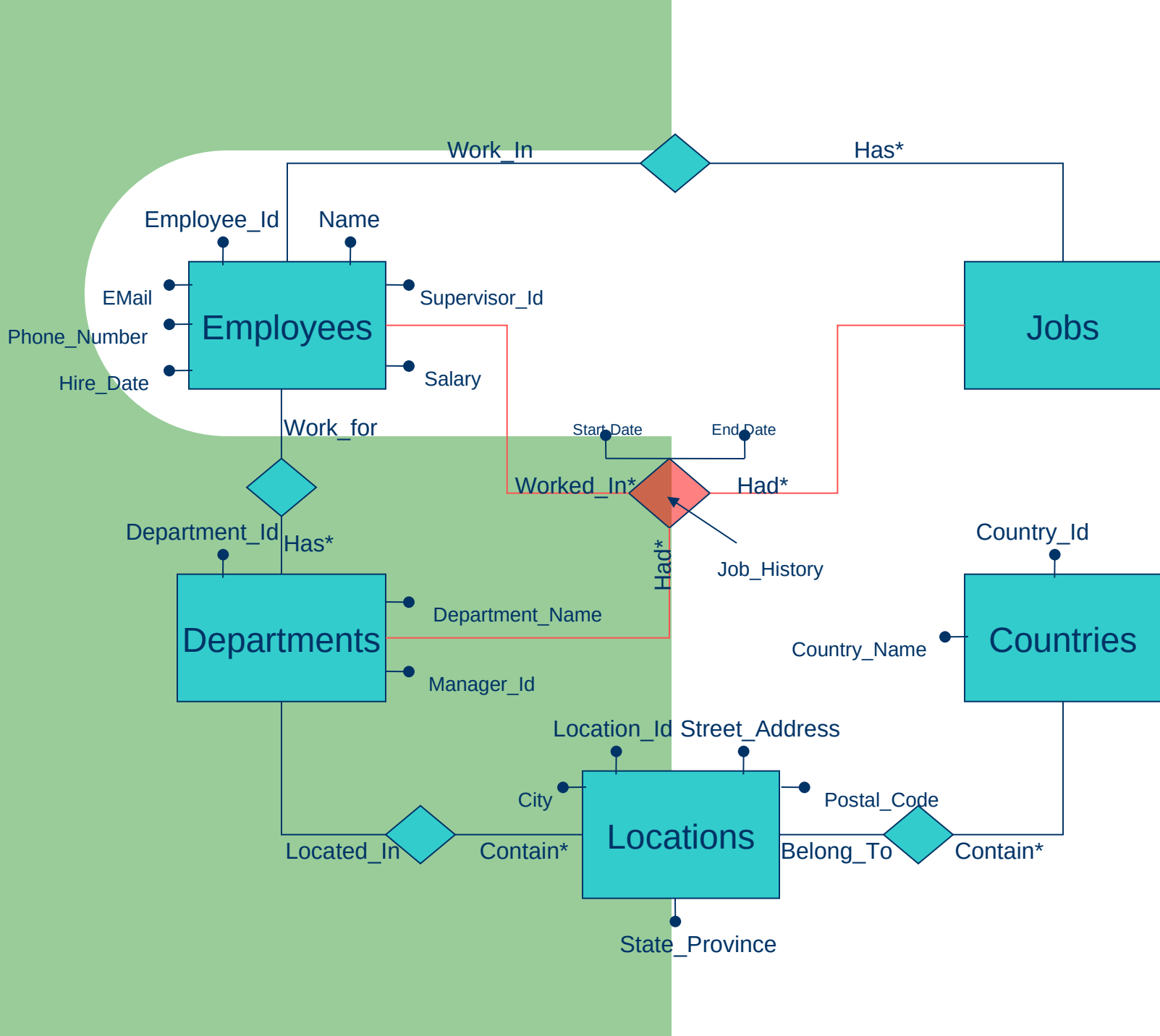
generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

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 AdjacentList[T_i] += T_k follow by the common key

 AdjacentList[T_k] += T_i follow by the common key



Transforming the entity relationship schema into the relational model, we get the following tables:

```
CREATE TABLE EMPLOYEES
```

```
(
```

```
    EMPLOYEE_ID INT NOT NULL,  
    EMPLOYEE_NAME VARCHAR(35),  
    EMAIL VARCHAR(25),  
    PHONE_NUMBER VARCHAR(20),  
    HIRE_DATE DATE,  
    JOB_ID VARCHAR(10),  
    SALARY NUMERIC(8,2),  
    DEPARTMENT_ID VARCHAR(3)
```

```
);
```

```
CREATE TABLE JOB_HISTORY
```

```
(
```

```
    EMPLOYEE_ID INT,  
    START_DATE DATE,  
    END_DATE DATE,  
    DEPARTMENT_ID VARCHAR(3),  
    JOB_ID VARCHAR(10)
```

```
);
```

```
CREATE TABLE JOBS
```

```
(
```

```
    JOB_ID VARCHAR(10),  
    JOB_TITLE VARCHAR(35),  
    MIN_SALARY DOUBLE,  
    MAX_SALARY DOUBLE
```

```
);
```

CREATE TABLE DEPARTMENTS

```
(  
    DEPARTMENT_ID VARCHAR(3),  
    DEPARTMENT_NAME VARCHAR(30),  
    MANAGER_ID INT,  
    LOCATION_ID INT  
);
```

CREATE TABLE LOCATIONS

```
(  
    LOCATION_ID INT,  
    STREET_ADDRESS VARCHAR(40),  
    POSTAL_CODE VARCHAR(12),  
    CITY VARCHAR(30),  
    STATE_PROVINCE VARCHAR(25),  
    COUNTRY_ID CHAR(2)  
);
```

CREATE TABLE COUNTRIES

```
(  
    COUNTRY_ID CHAR(2),  
    COUNTRY_NAME VARCHAR(40)  
);
```

The join for the example is the following:

List where every employee have been worked before along with the department that he is working now:

```
CREATE JOIN INDEX RECENT_IDX
```

```
ON      EMPLOYEES(LAST_NAME), DEPARTMENTS, JOBS, JOB_HISTORY, LOCATIONS, COUNTRIES
WHERE   EMPLOYEES.EMPLOYEE_ID = JOB_HISTORY.EMPLOYEE_ID
AND     JOBS.JOB_ID = JOB_HISTORY.JOB_ID
AND     EMPLOYEES.DEPARTMENT_ID = DEPARTMENTS.DEPARTMENT_ID
AND     DEPARTMENTS.LOCATION_ID = LOCATIONS.LOCATION_ID
AND     LOCATIONS.COUNTRY_ID = COUNTRIES.COUNTRY_ID;
```

```
SELECT EMPLOYEES.EMPLOYEE_NAME,
       JOBS.JOB_TITLE AS JOB_TITLE,
       DEPARTMENTS.DEPARTMENT_NAME AS DEPARTMENT_NAME,
       COUNTRIES.COUNTRY_NAME AS COUNTRY_NAME
FROM   EMPLOYEES, JOB_HISTORY, DEPARTMENTS,
       LOCATIONS, JOBS, COUNTRIES
WHERE  EMPLOYEES.EMPLOYEE_ID = JOB_HISTORY.EMPLOYEE_ID
AND    JOBS.JOB_ID = JOB_HISTORY.JOB_ID
AND    EMPLOYEES.DEPARTMENT_ID = DEPARTMENTS.DEPARTMENT_ID
AND    DEPARTMENTS.LOCATION_ID = LOCATIONS.LOCATION_ID
AND    LOCATIONS.COUNTRY_ID = COUNTRIES.COUNTRY_ID;
```


This is another join on the same table:

List where every employee have been worked before along with the department that he is working before:

```
CREATE JOIN INDEX HISTORY_IDX
```

```
ON      EMPLOYEES(LAST_NAME), DEPARTMENTS, JOBS, JOB_HISTORY, LOCATIONS, COUNTRIES
WHERE   EMPLOYEES.EMPLOYEE_ID = JOB_HISTORY.EMPLOYEE_ID
AND     JOBS.JOB_ID = JOB_HISTORY.JOB_ID
AND     JOB_HISTORY.DEPARTMENT_ID = DEPARTMENTS.DEPARTMENT_ID
AND     DEPARTMENTS.LOCATION_ID = LOCATIONS.LOCATION_ID
AND     LOCATIONS.COUNTRY_ID = COUNTRIES.COUNTRY_ID;
```

```
SELECT EMPLOYEES.FIRST_NAME +
```

```
    EMPLOYEES.LAST_NAME AS NAME,
```

```
    JOBS.JOB_TITLE AS JOB_TITLE,
```

```
    DEPARTMENTS.DEPARTMENT_NAME AS DEPARTMENT_NAME,
```

```
    COUNTRIES.COUNTRY_NAME AS COUNTRY_NAME
```

```
FROM   JOB_HISTORY, DEPARTMENTS,
```

```
        LOCATIONS, JOBS, COUNTRIES, EMPLOYEES
```

```
WHERE  EMPLOYEES.EMPLOYEE_ID = JOB_HISTORY.EMPLOYEE_ID
```

```
AND    JOBS.JOB_ID = JOB_HISTORY.JOB_ID
```

```
AND    JOB_HISTORY.DEPARTMENT_ID = DEPARTMENTS.DEPARTMENT_ID
```

```
AND    DEPARTMENTS.LOCATION_ID = LOCATIONS.LOCATION_ID
```

```
AND    LOCATIONS.COUNTRY_ID = COUNTRIES.COUNTRY_ID;
```

→ generateJoinGraph (in BaseTables; out JoinGraph)
insert the base tables as vertexes of the graph
for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do
 AdjacentList[T_i] += T_k follow by the common key
 AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
0	1	2	3	4	5

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Employees	→	Job_History	Employee_Id
Job_History			
Jobs			
Departments			
Locations			
Countries			

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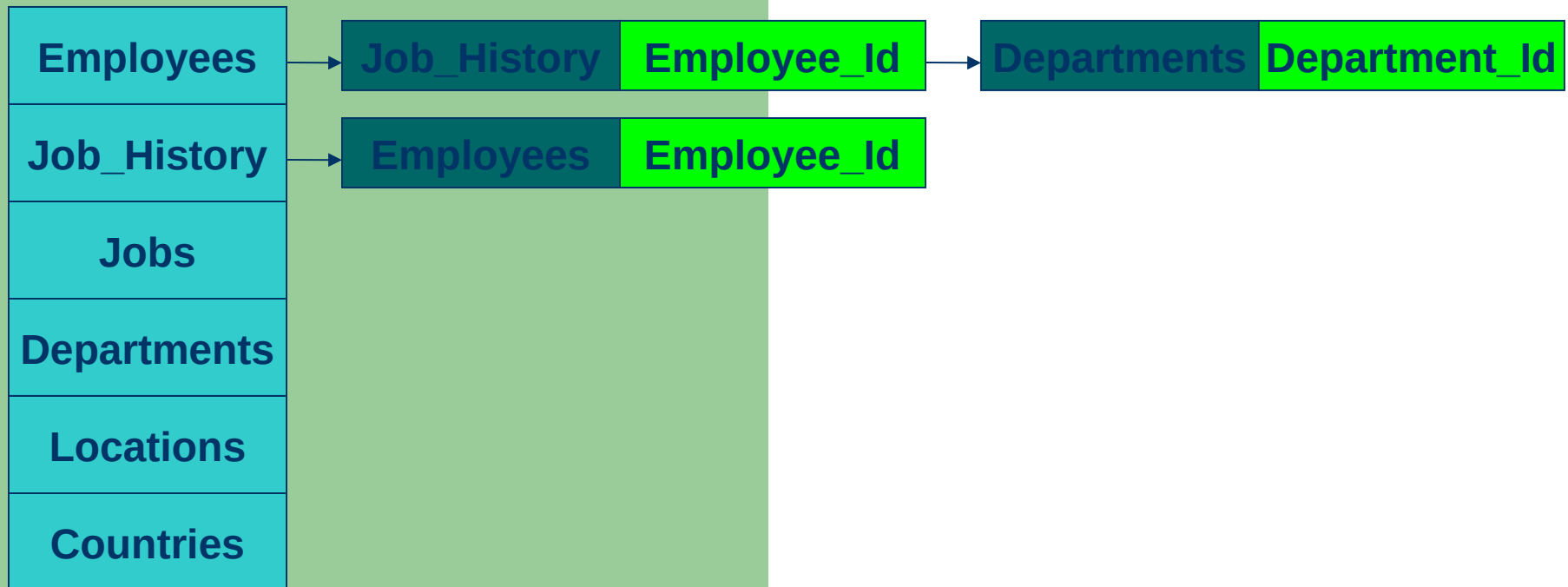
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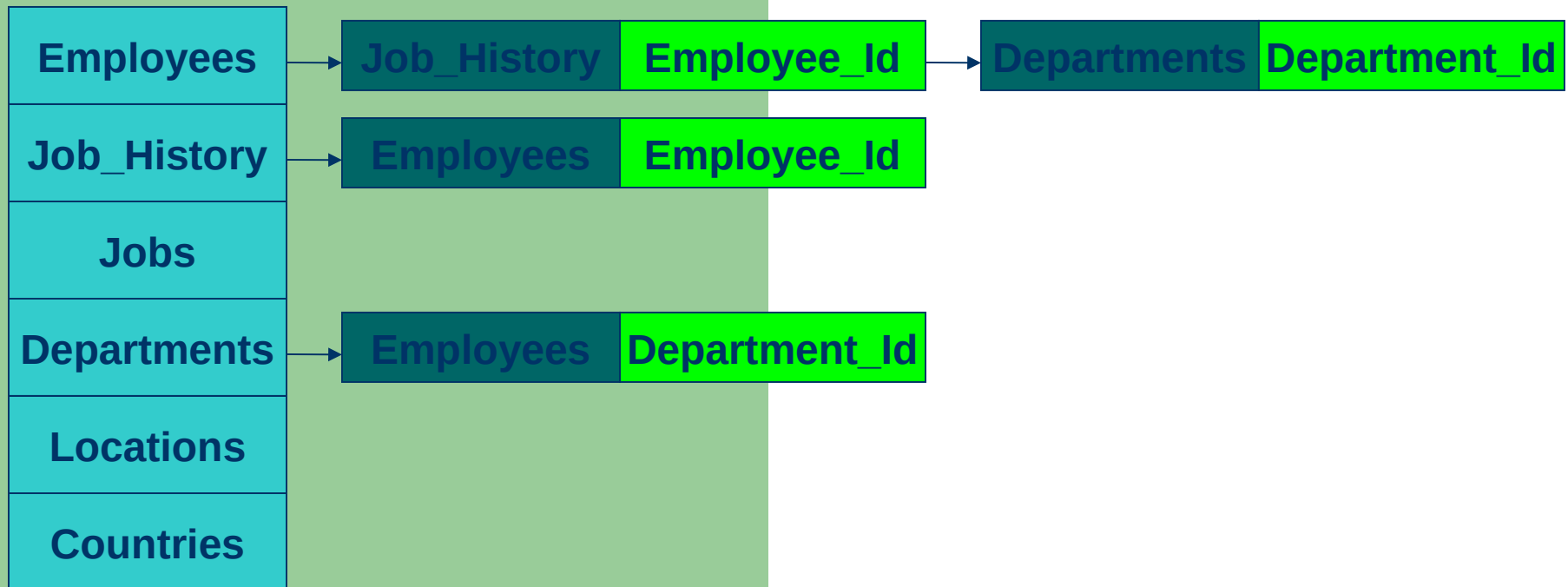
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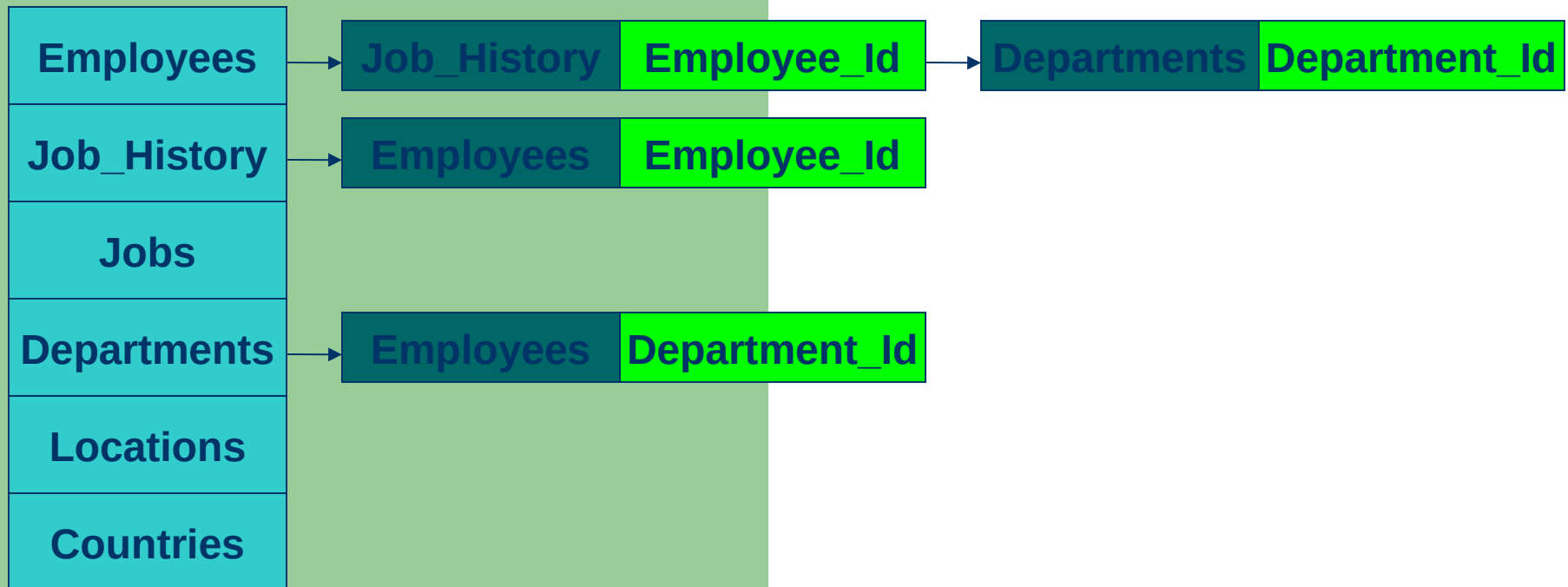
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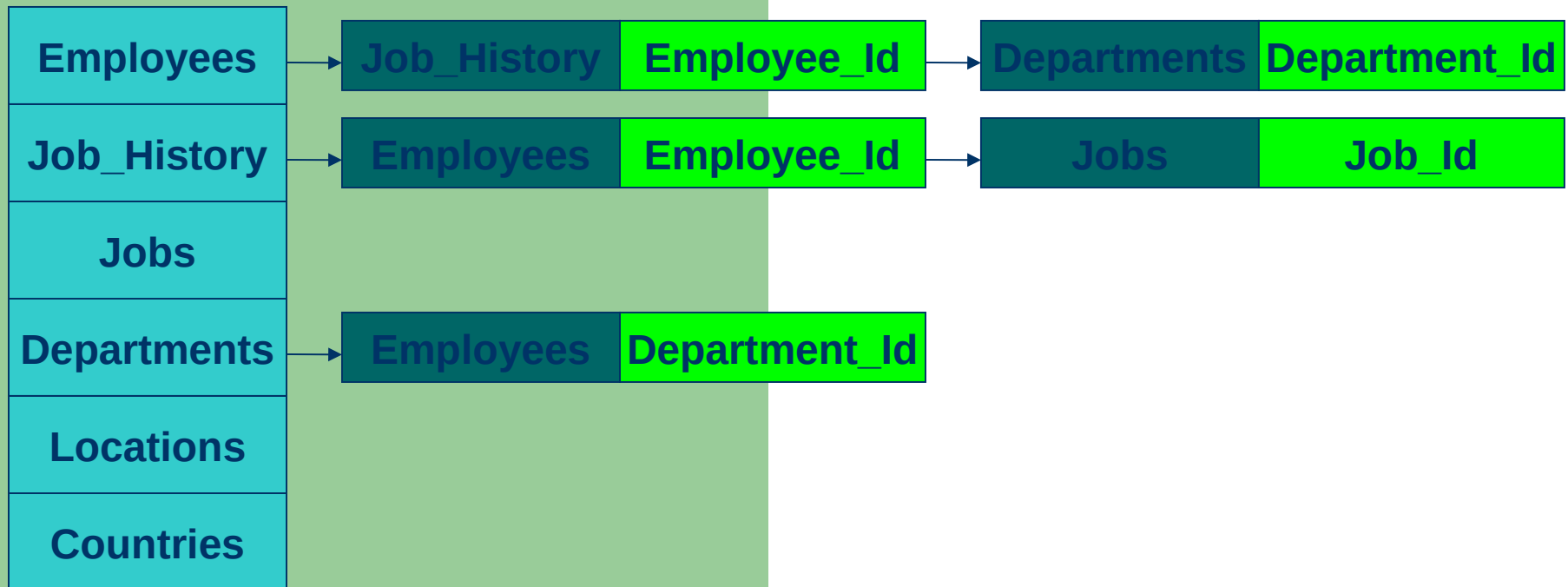
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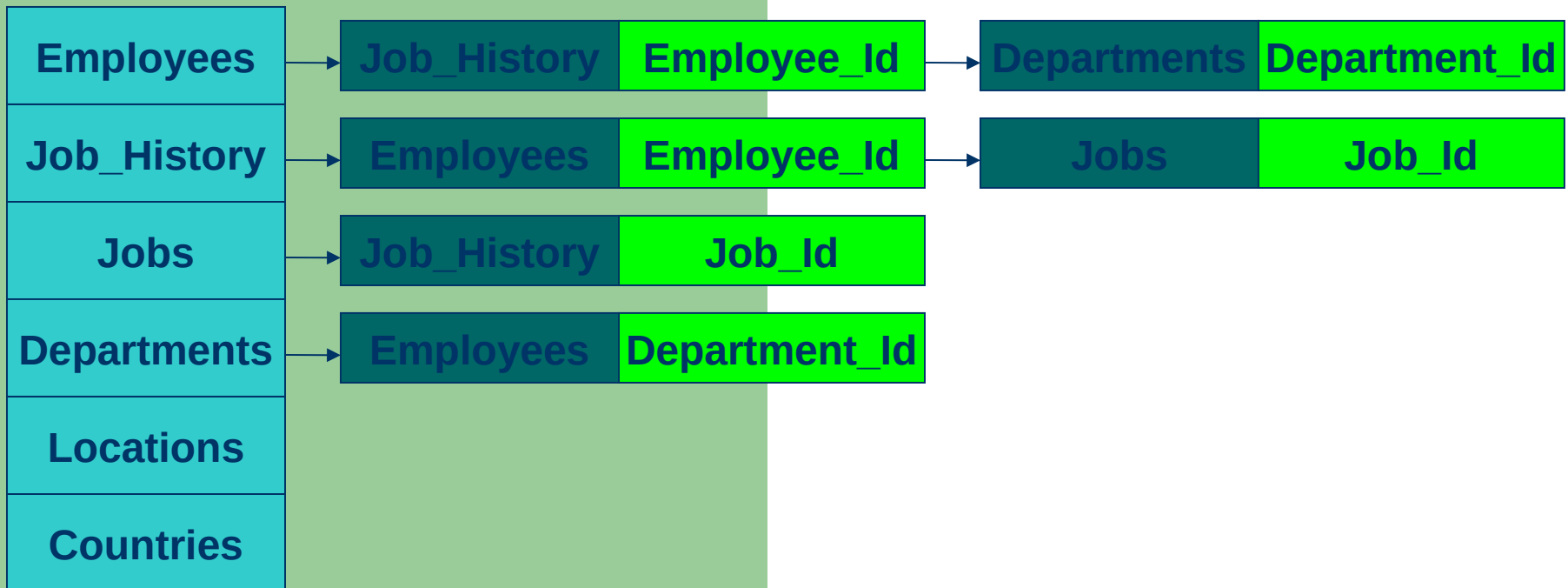
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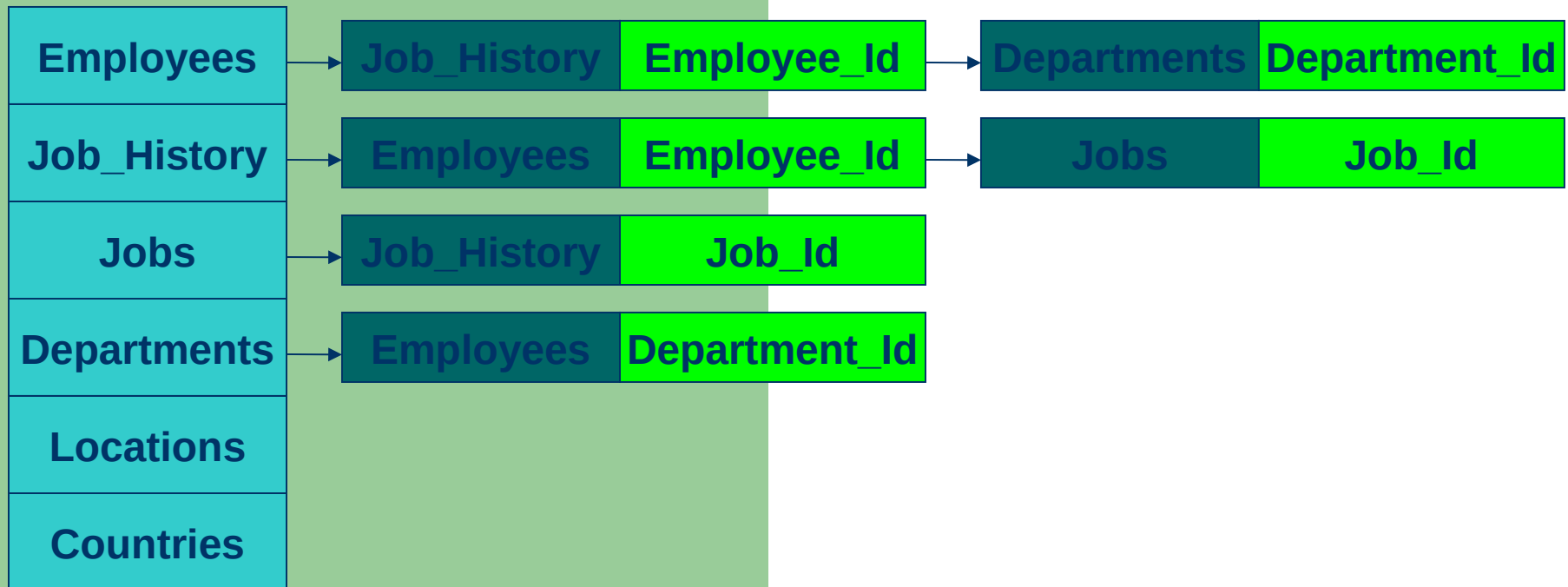
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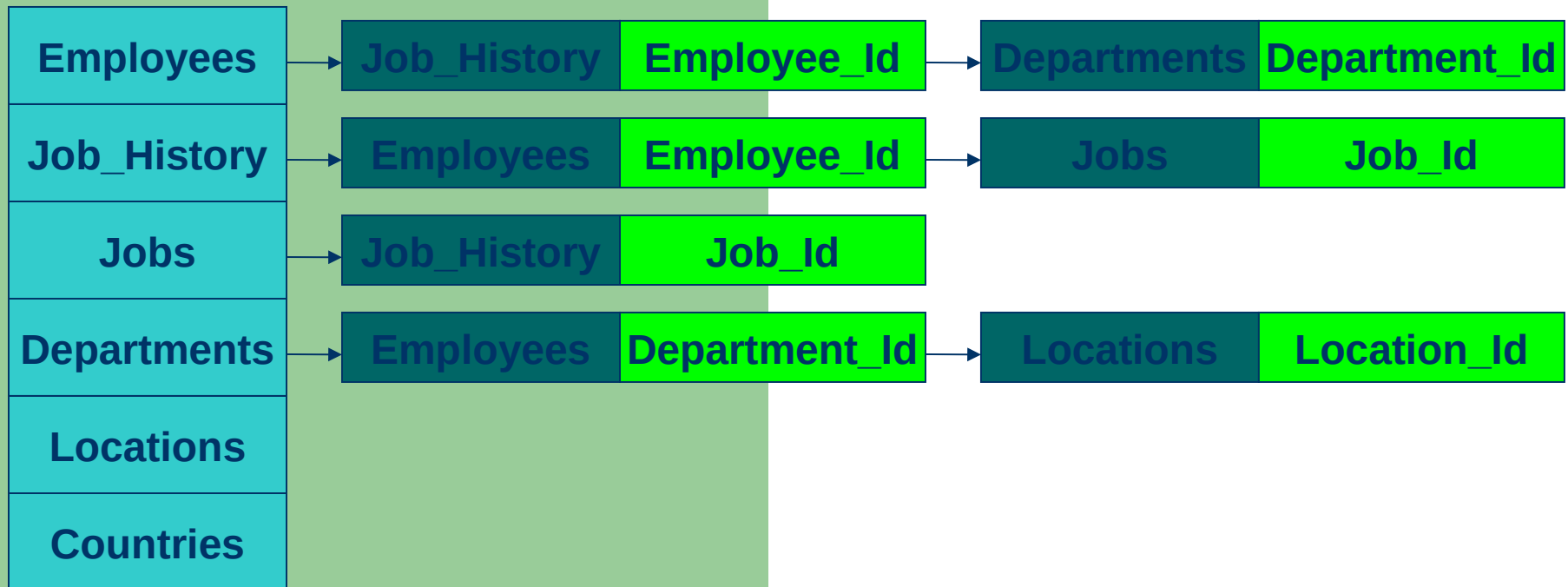
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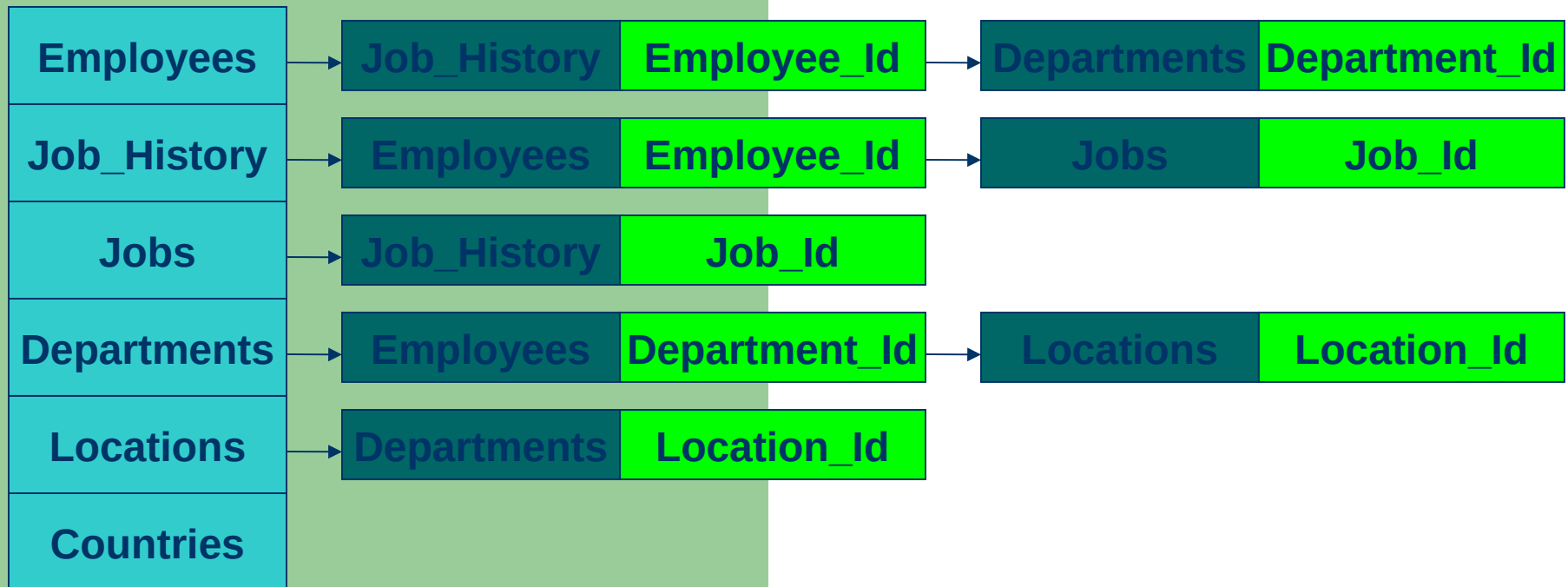
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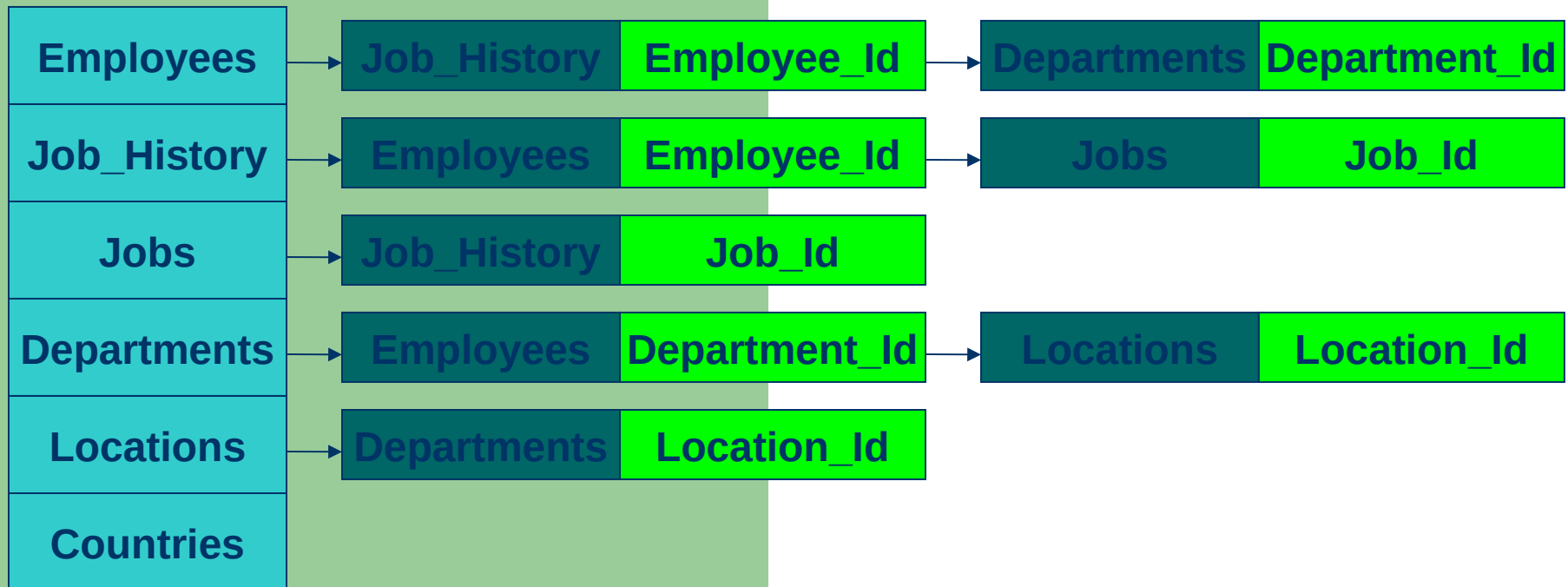
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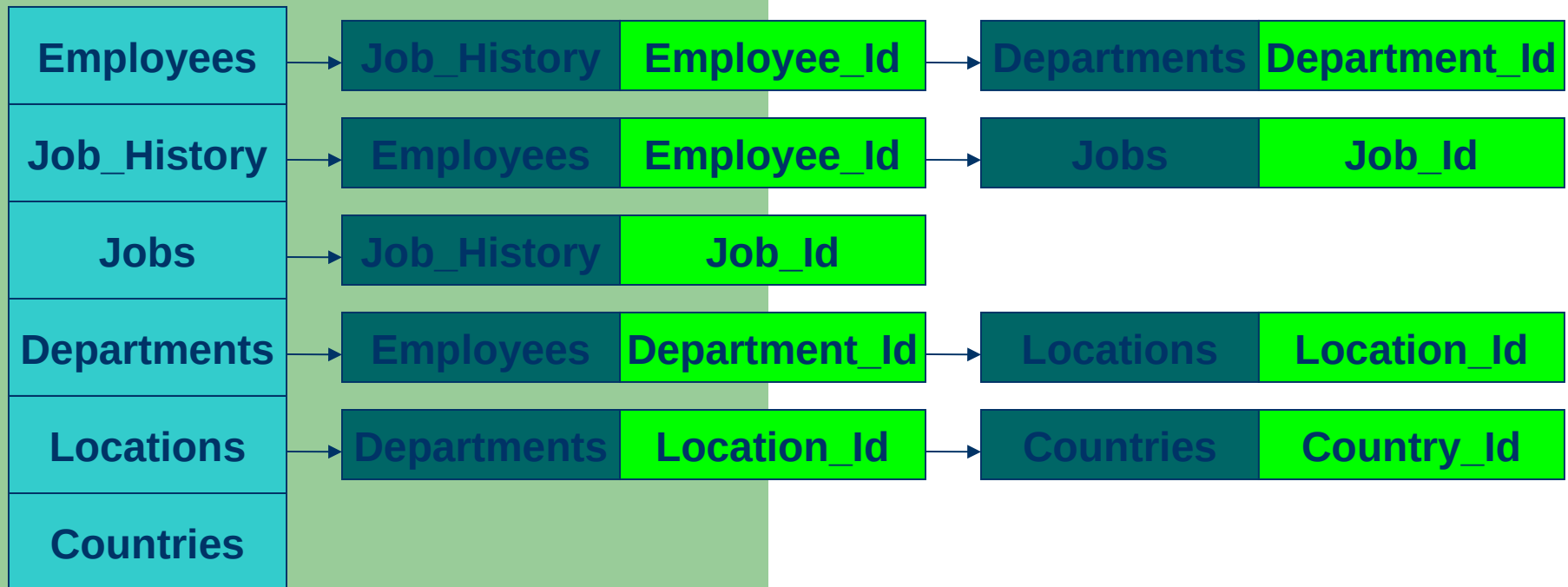
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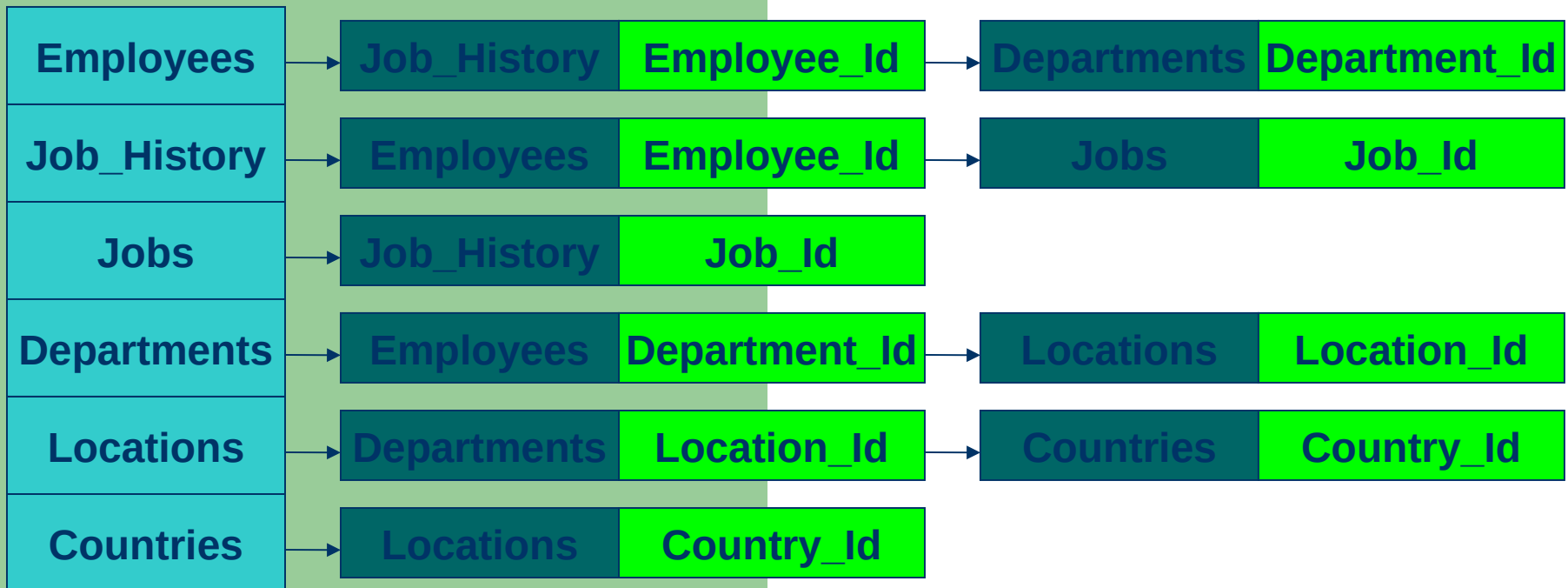
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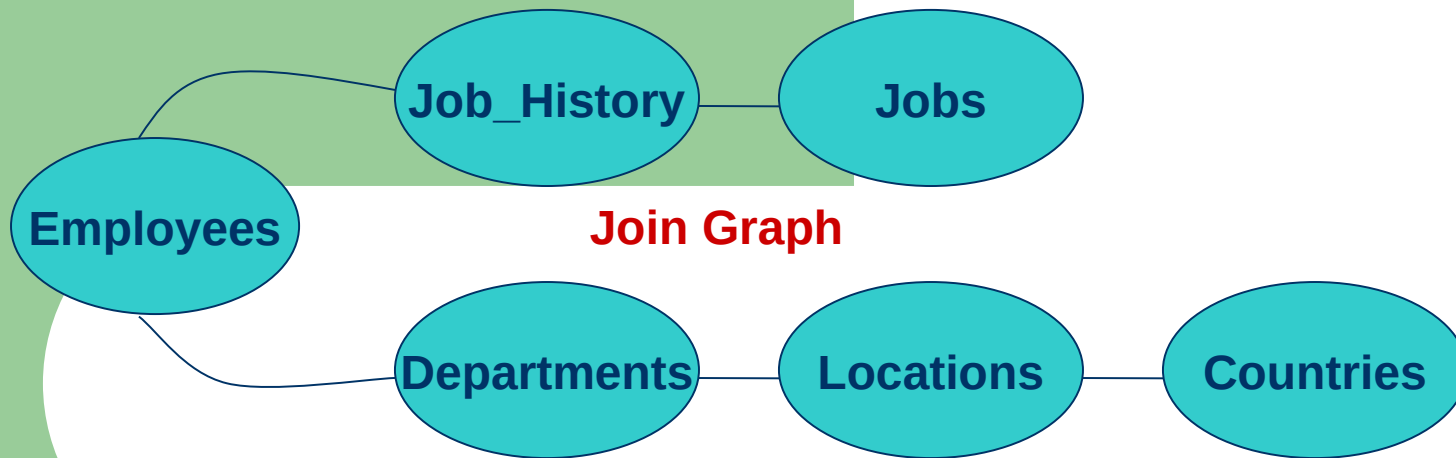
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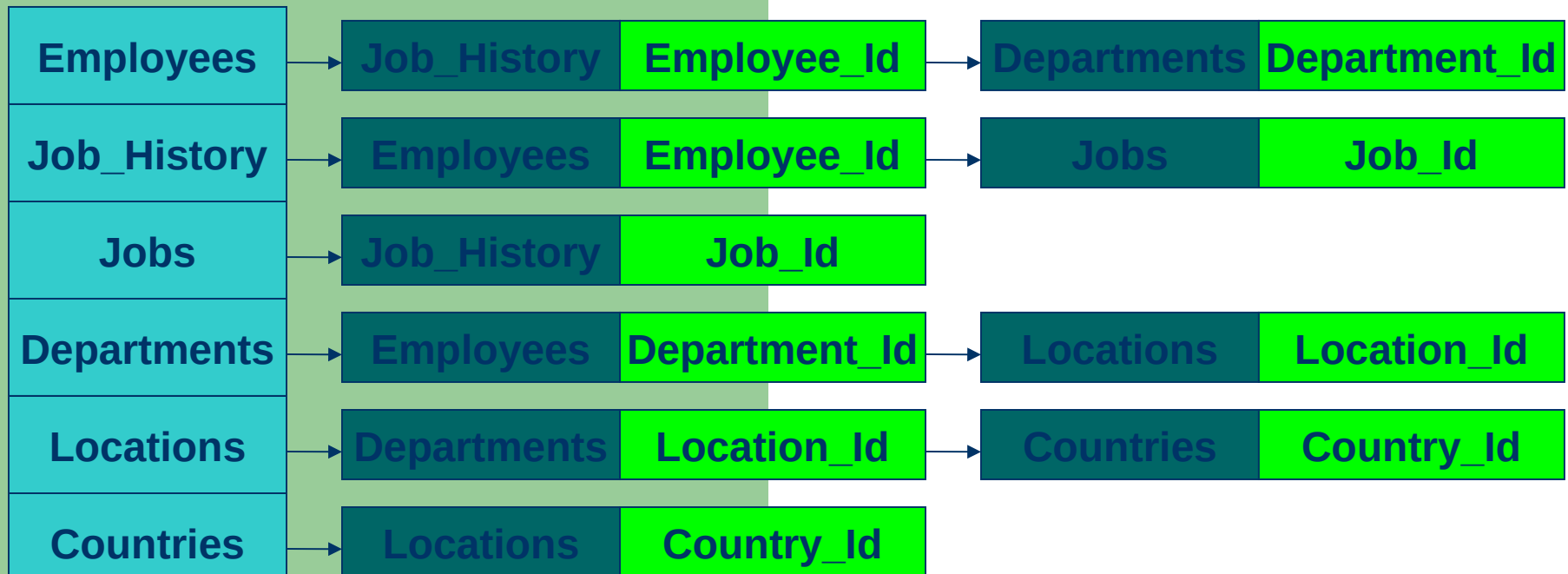
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Linked List representation of the Join Graph



Adjacency List

Definitions

Join Path List:

A sequence of tables $T_0 \dots T_{n-1}$ is in the Join Path List if every T_i of them is at least in direct join with another table in the sequence.

Notation

- When index i is not between brackets like in T_i , it represent a base table T_i .

When index i is between brackets like in $T_{[i]}$, it represent a base table T_i or a virtual table in which index i represent a set of indexes for the base tables forming the virtual table.

Steps to generate function: $\text{Key}(T_{[j]})$ $\text{getFirstAdjacentListKey}(T_{[j]}, T_{[k]})$

for every Base Table T_i in $T_{[j]}$ do

Take one at a time

for every $T_{\text{Link}(l)}$ do

Take one at a time

if $T_{\text{Link}(l)}$ in $T_{[k]}$ then

return($\text{key}(T_i, T_{\text{Link}(l)})$)

Normally one of the 2 tables $T_{[j]}$ or $T_{[k]}$ is a base table this is why we stop after founding the key.

Key could be a one column key or multicolumn key that satisfy the join condition.

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

 for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

 if the Link Item is in the join sequence then

 if path doesn't contain the Link Item then

 insert Link Item into path

 insert Link Item into queue

 remove T_{Element} from queue

until queue is empty

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$ (continue)

insert all the names of base tables from path as vertexes in the JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{PathJoinAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{PathJoinAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]}^+ = T_i$

$\text{Insert NodeList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$ (continue)

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
    take one  $T_{[i]}$  at a time
    for all Base Tables in  $T_{[i]}$  do
        take one  $T_k$  at a time
        for every buf.Table =  $T_k$  do
            if (buf.key != Key( $T_{[i]}$ ) ) and (buf.Key not in InheritedKey( $T_{[i]}$ )) then
                InheritedKey( $T_{[i]}$ ) += buf.key
        if  $T_i$  is the table from which comes Key( $T_{[i]}$ ) then
            buf.Table =  $T_i$ 
            buf.key = Key( $T_{[i]}$ )
```

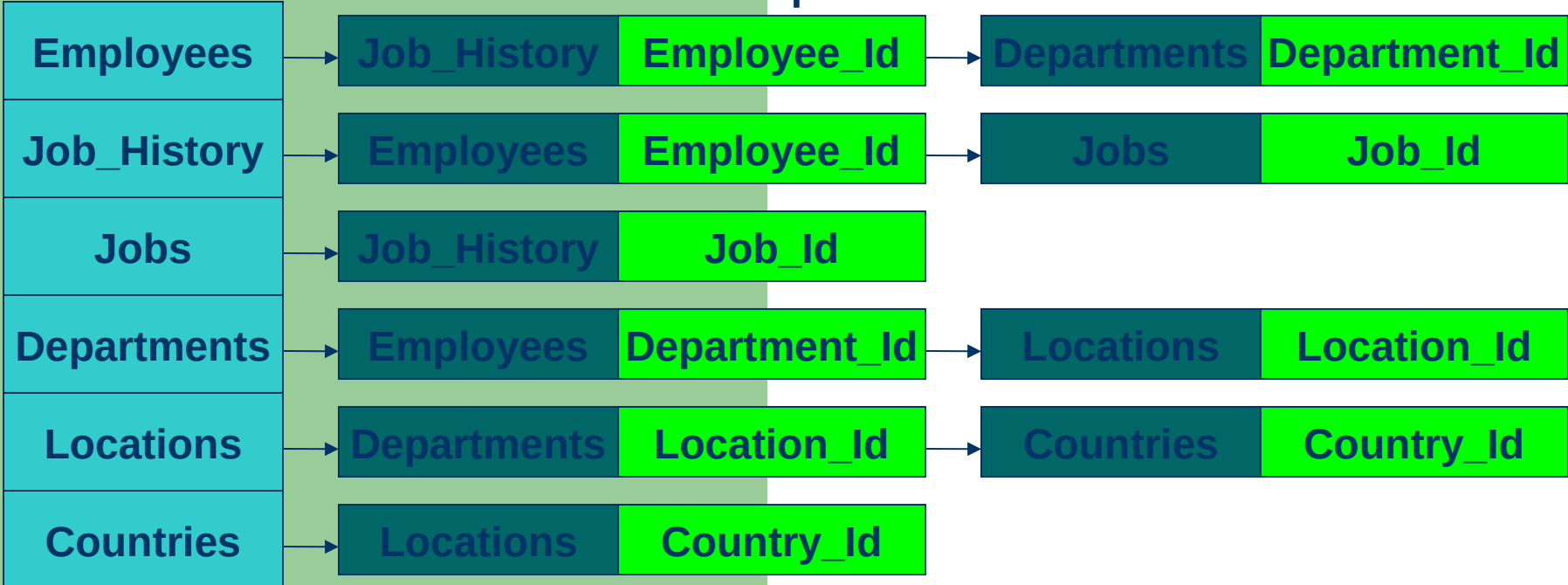
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Join Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
-----------	-------------	------	-------------	-----------	-----------

Join Graph



until queue is empty

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remove T_{Element} from queue
until queue is empty

Join Base Tables

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T_0	T_1	T_2	T_3	T_4	T_5

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

→ create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

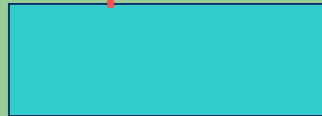
insert Link Item into path

insert Link Item into queue

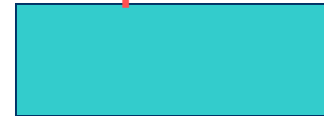
remove T_{Element} from queue

until queue is empty

queue



path



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

→ insert T_0 into path

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repeat

T_{Element} = First Table in queue

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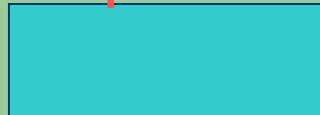
insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

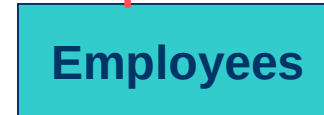
until queue is empty

queue



path

Employees



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

→ insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

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if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue

Employees

path

Employees

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

until queue is empty

queue

Employees

path

Employees

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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remove T_{Element} from queue

until queue is empty

queue



Employees

path

Employees

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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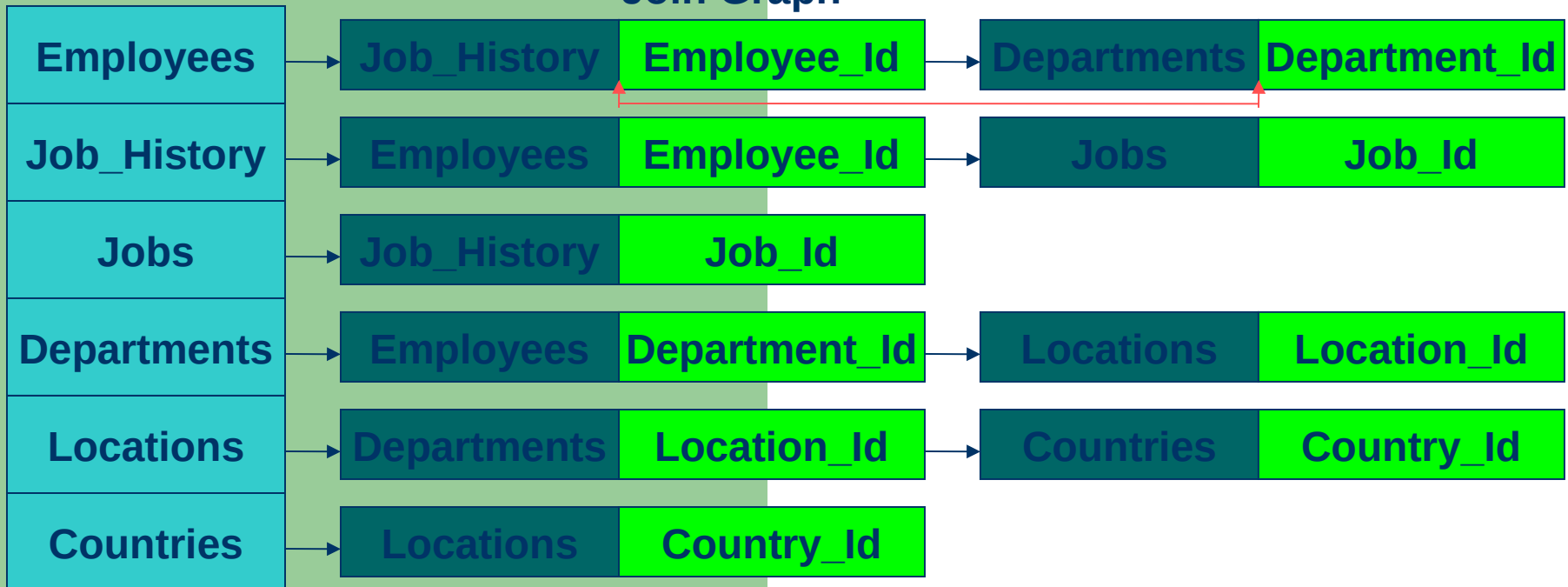
insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

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repeat

T_{Element} = First Table in queue

 for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

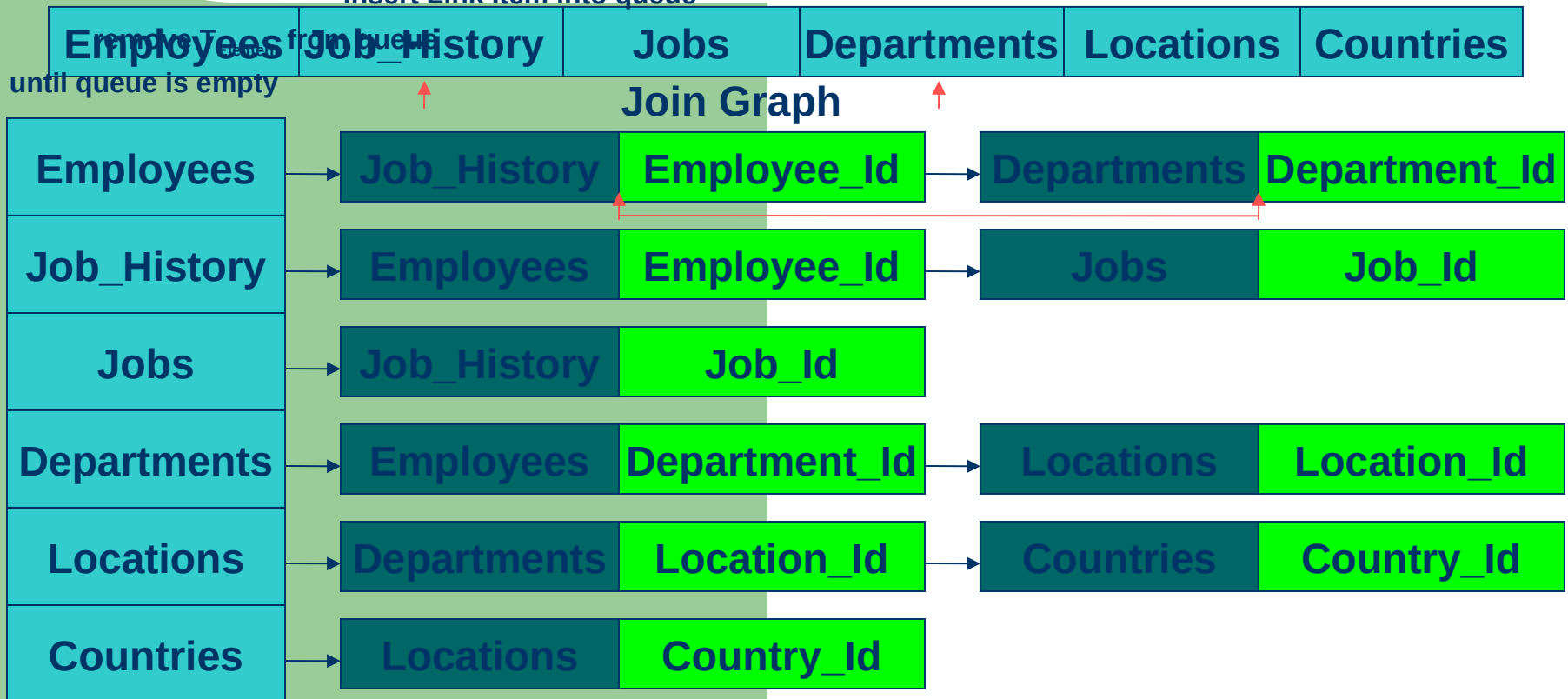
 if the Link Item is in the join sequence then

 if path doesn't contain the Link Item then

 insert Link Item into path

 insert Link Item into queue

 remove T_{Element} from queue
until queue is empty



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue
until queue is empty

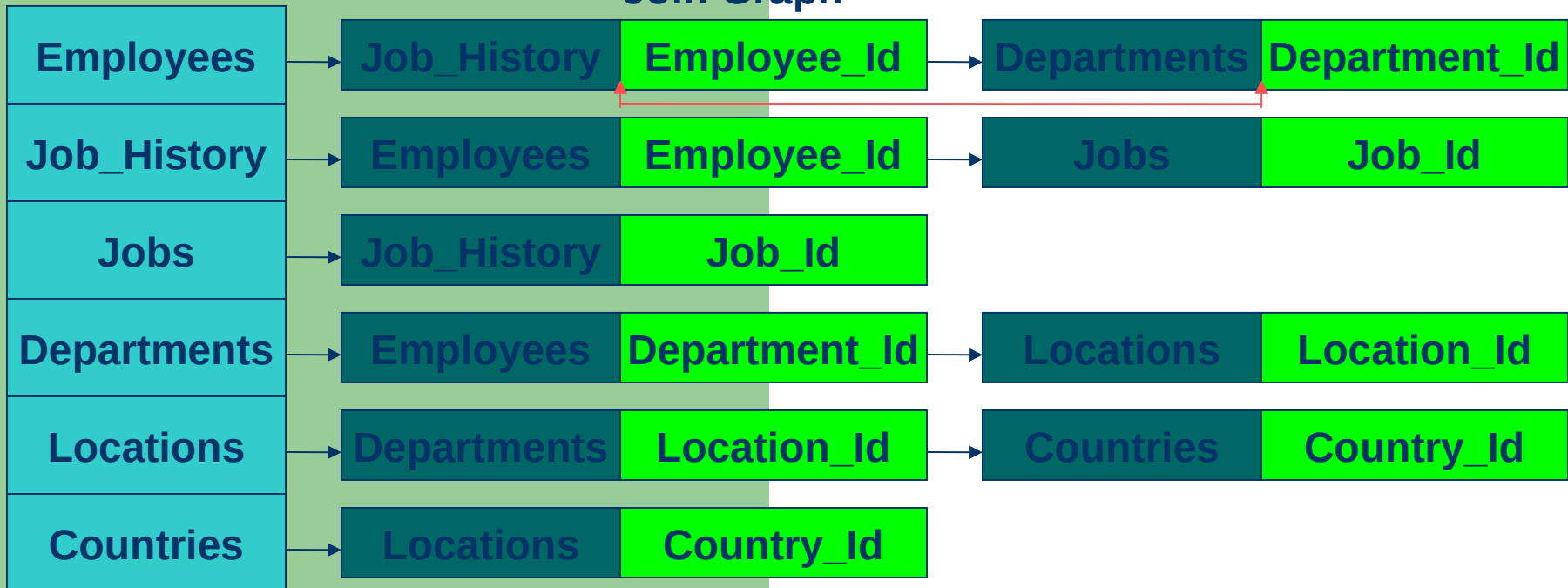
path

Employees

Join Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
-----------	-------------	------	-------------	-----------	-----------

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

until queue is empty

queue



Employees

path

Employees

Job_History

Departments

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Employees
Job_History
Departments

path

Employees
Job_History
Departments

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

until queue is empty

queue

Job_History

Departments

path

Employees

Job_History

Departments

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

until queue is empty

queue



Job_History

Departments

path

Employees

Job_History

Departments

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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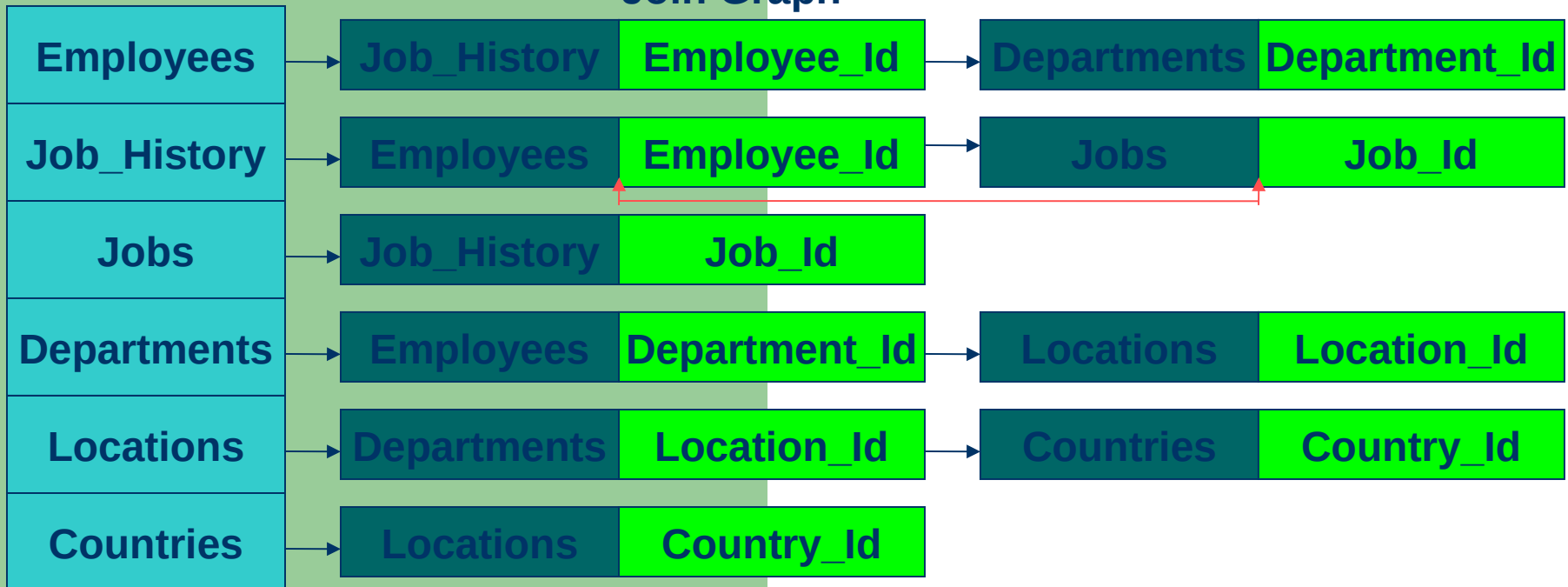
insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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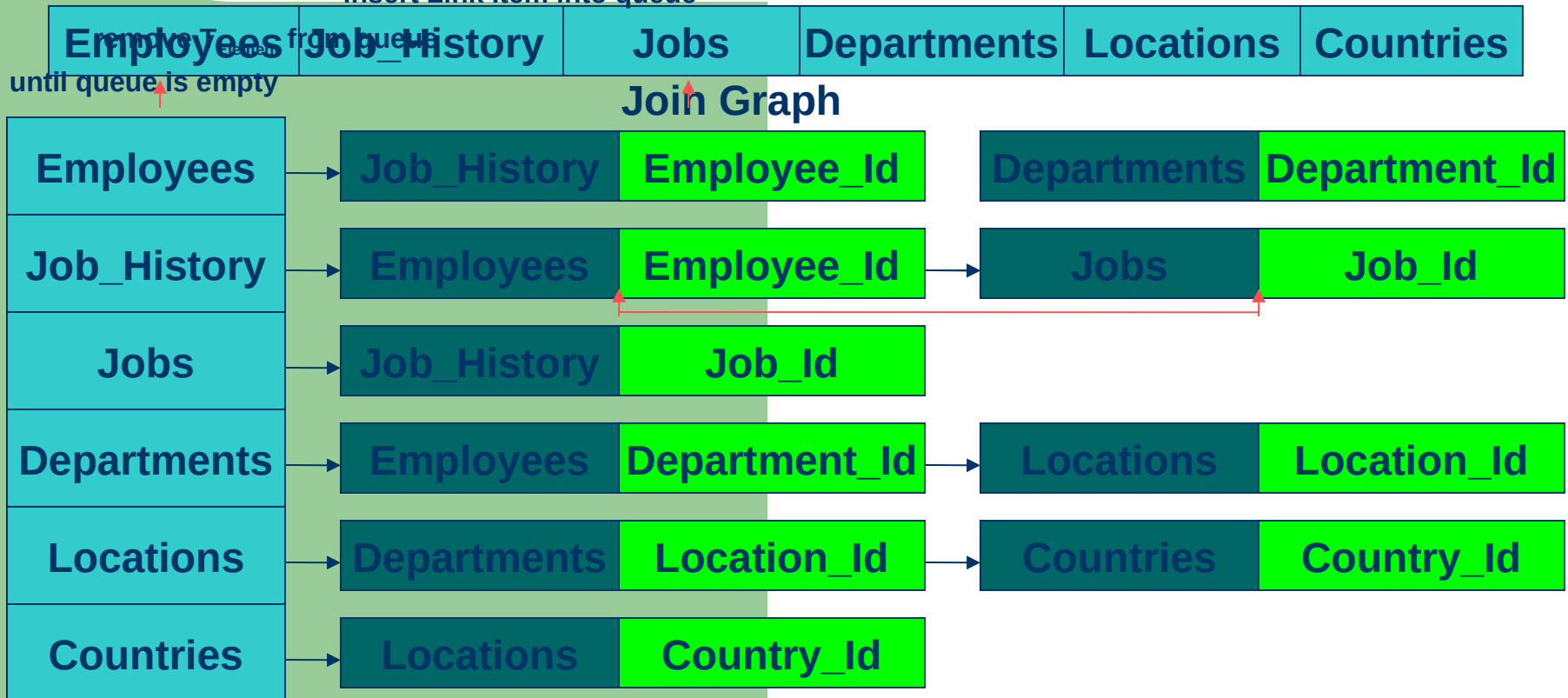
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if path doesn't contain the Link Item then

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until queue is empty



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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if path doesn't contain the Link Item then

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insert Link Item into queue

until queue is empty

path

Employees

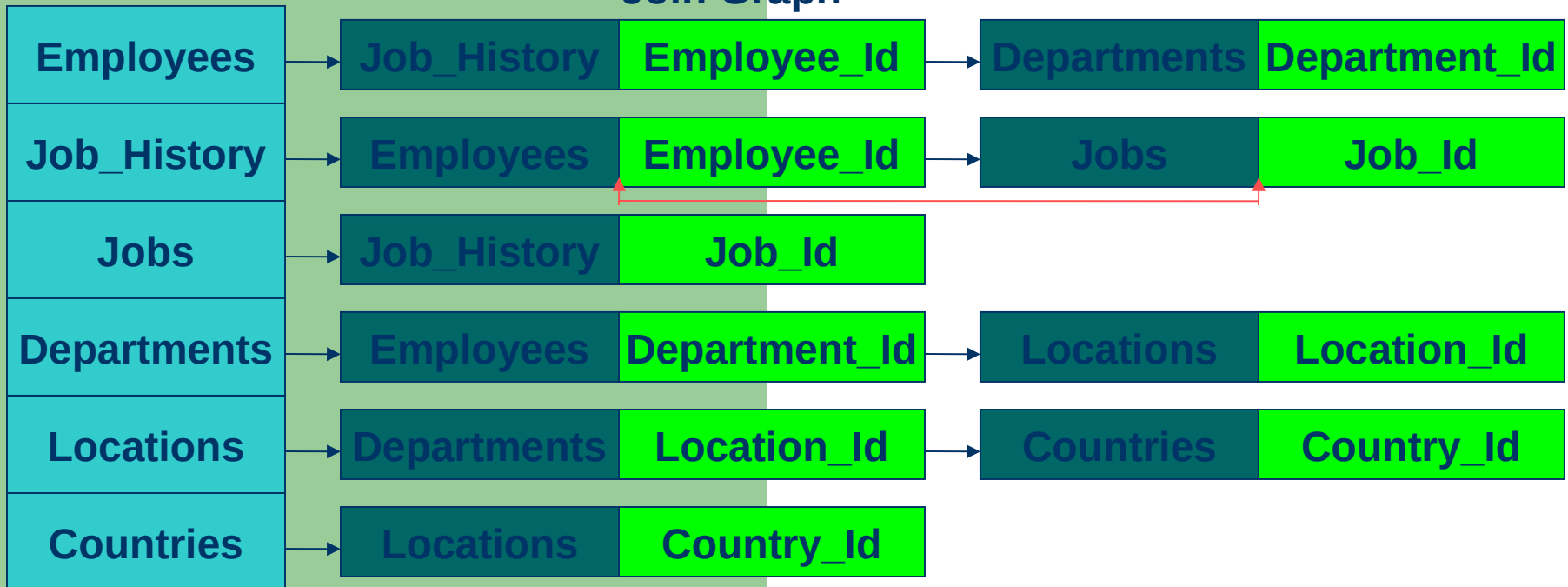
Job_History

Departments

Join Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
-----------	-------------	------	-------------	-----------	-----------

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Job_History

Departments

path

Employees

Job_History

Departments

Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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remove T_{Element} from queue

until queue is empty

queue



Job_History

Departments

Jobs

path

Employees

Job_History

Departments

Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

until queue is empty

queue

Departments

Jobs

path

Employees

Job_History

Departments

Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

until queue is empty

queue



Departments

Jobs

path

Employees

Job_History

Departments

Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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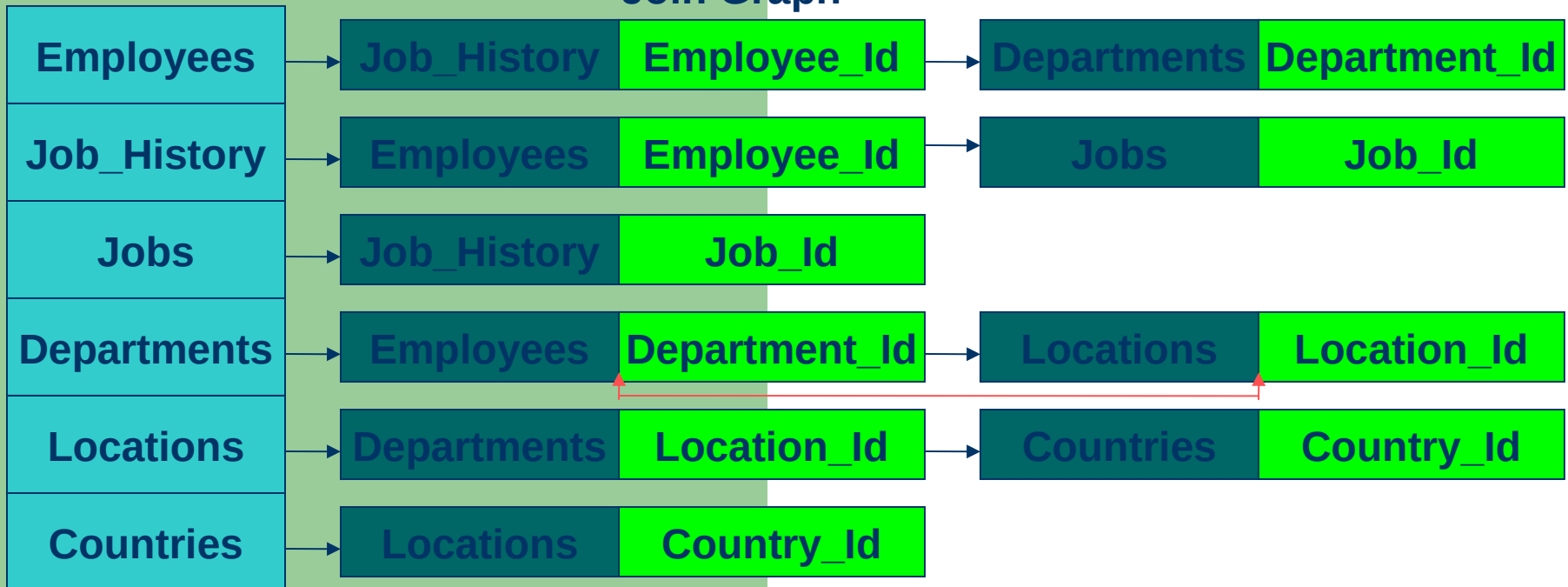
insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

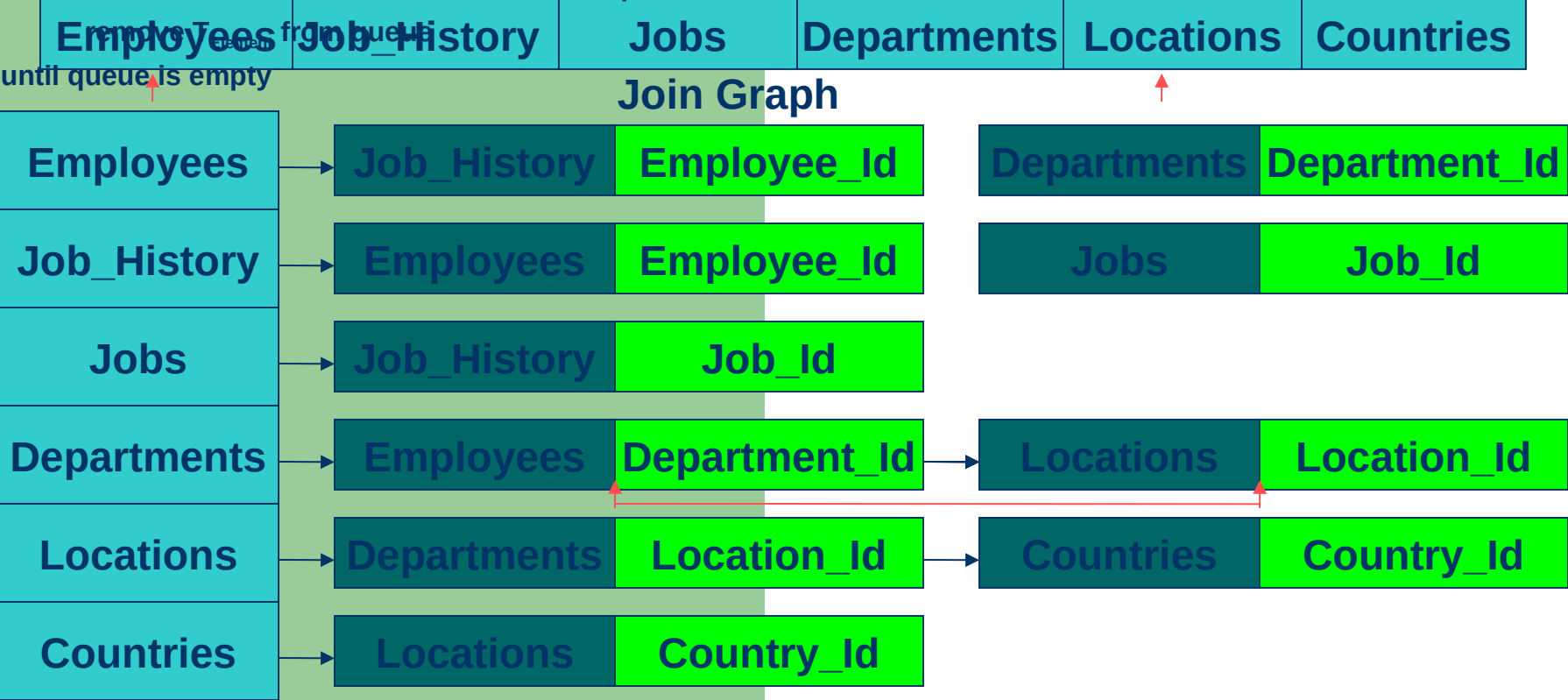
Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path
insert T_0 into path
insert T_0 into queue
repeat

T_{Element} = First Table in queue
for every Link Item in Adjacent Link of T_{Element} from the Join Graph do
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insert Link Item into queue

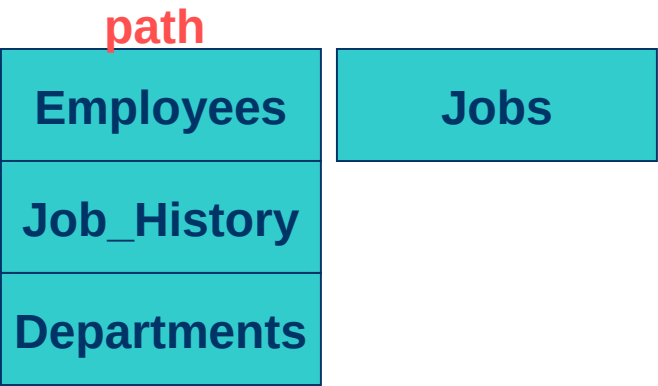


generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path
insert T_0 into path
insert T_0 into queue
repeat

T_{Element} = First Table in queue

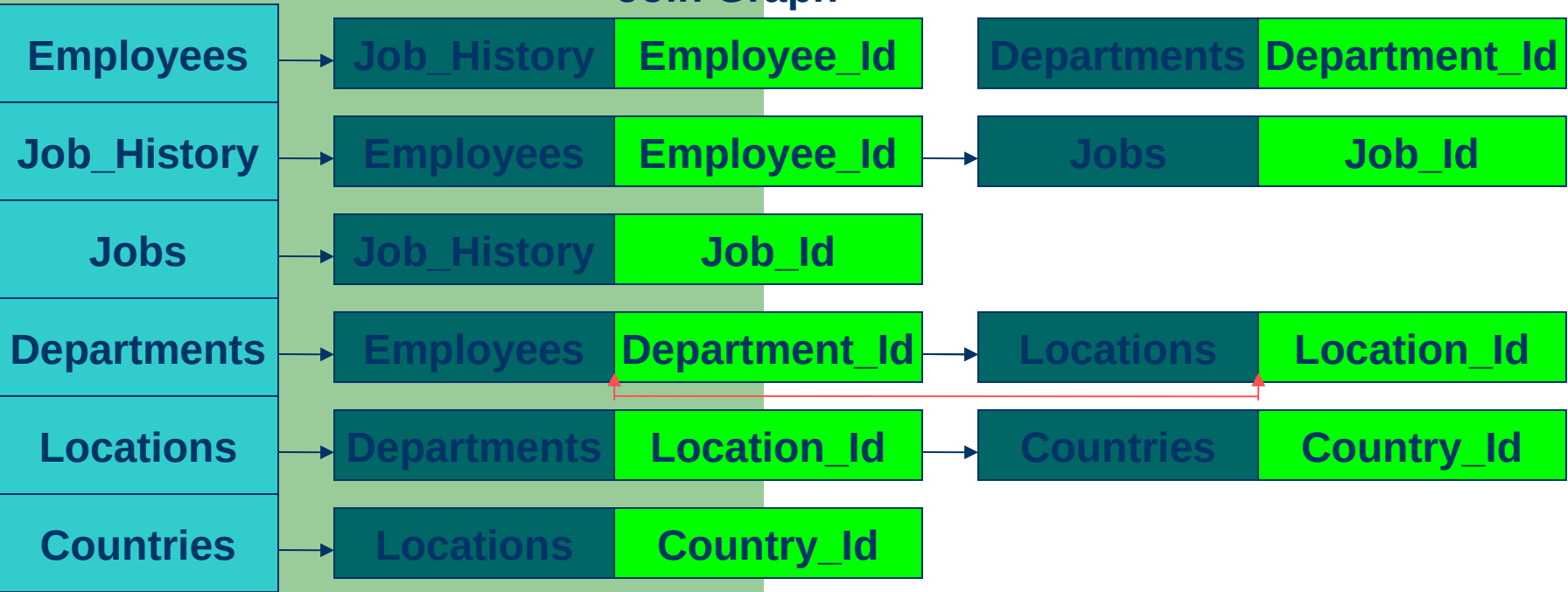
for every Link Item in Adjacent Link of T_{Element} from the Join Graph do
if the Link Item is in the join sequence then
if path doesn't contain the Link Item then
insert Link Item into path
insert Link Item into queue



Join Base Tables



Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Departments

Jobs

path

Employees

Job_History

Departments

Jobs

Locations

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

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T_{Element} = First Table in queue

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if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Departments

Jobs

Locations

path

Employees

Job_History

Departments

Jobs

Locations

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue

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queue

Jobs

Locations

path

Employees

Job_History

Departments

Jobs

Locations

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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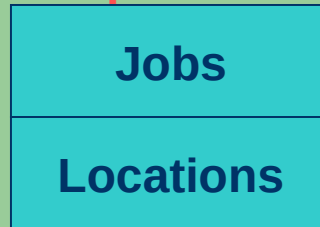
insert Link Item into path

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remove T_{Element} from queue

until queue is empty

queue



path



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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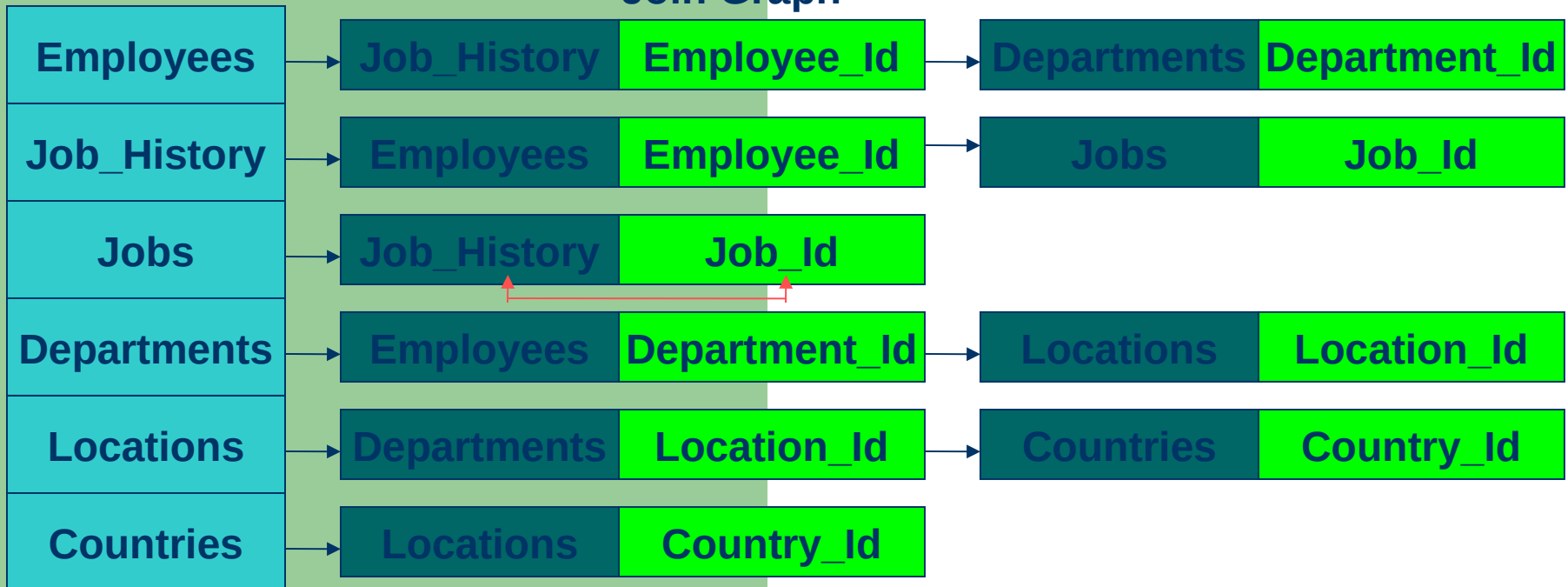
insert Link Item into path

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remove T_{Element} from queue

until queue is empty

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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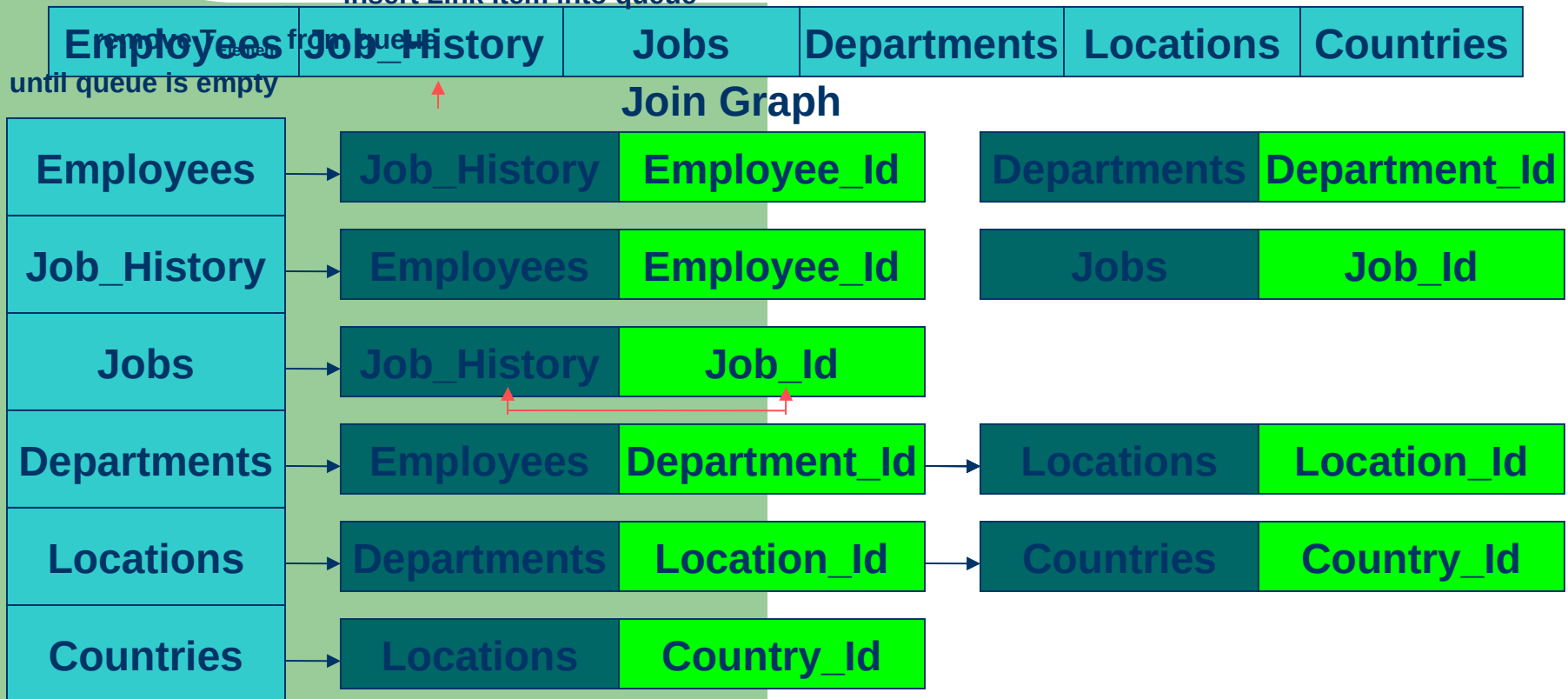
 if the Link Item is in the join sequence then

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generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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until queue is empty

path

Employees

Jobs

Job_History

Locations

Departments

Join Base Tables

Employees Job_History

Jobs

Departments

Locations

Countries

Join Graph

Employees

Job_History

Employee_Id

Departments

Department_Id

Job_History

Employees

Employee_Id

Jobs

Job_Id

Jobs

Job_History

Job_Id

Departments

Employees

Department_Id

Locations

Location_Id

Locations

Departments

Location_Id

Countries

Country_Id

Countries

Locations

Country_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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queue

Locations

path

Employees

Job_History

Departments

Jobs

Locations

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Locations

path

Employees

Job_History

Departments

Jobs

Locations

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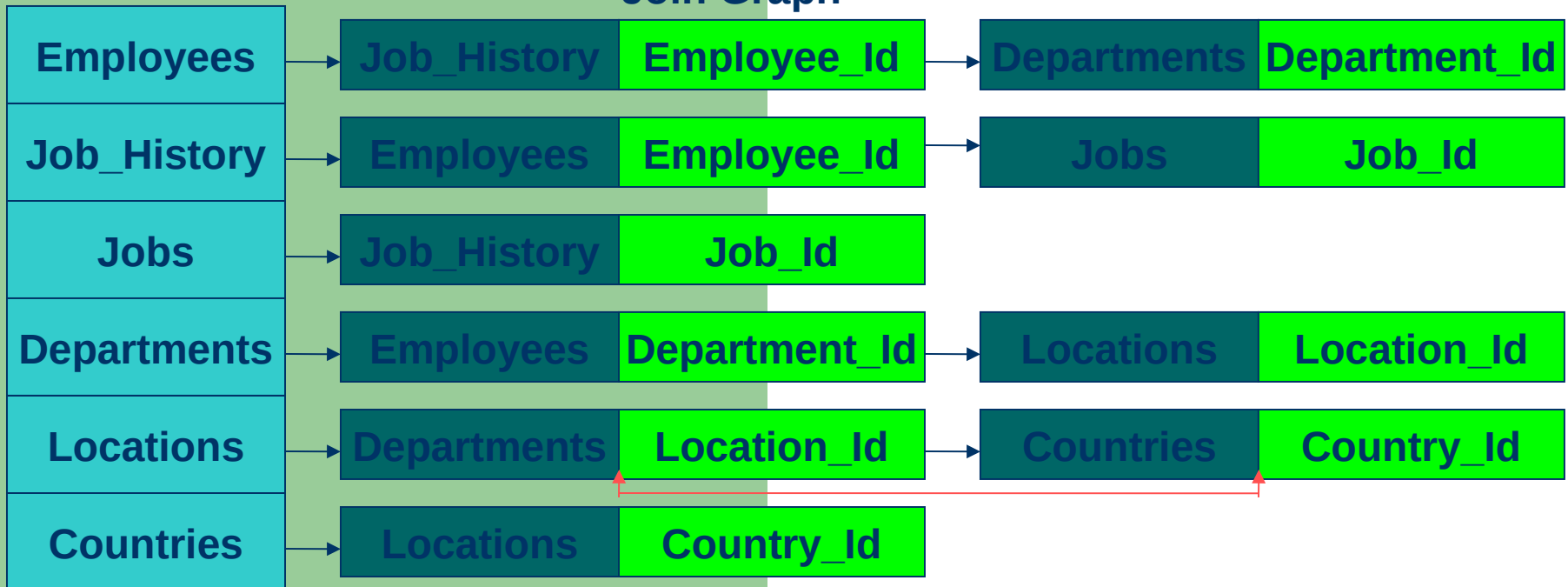
insert Link Item into path

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remove T_{Element} from queue

until queue is empty

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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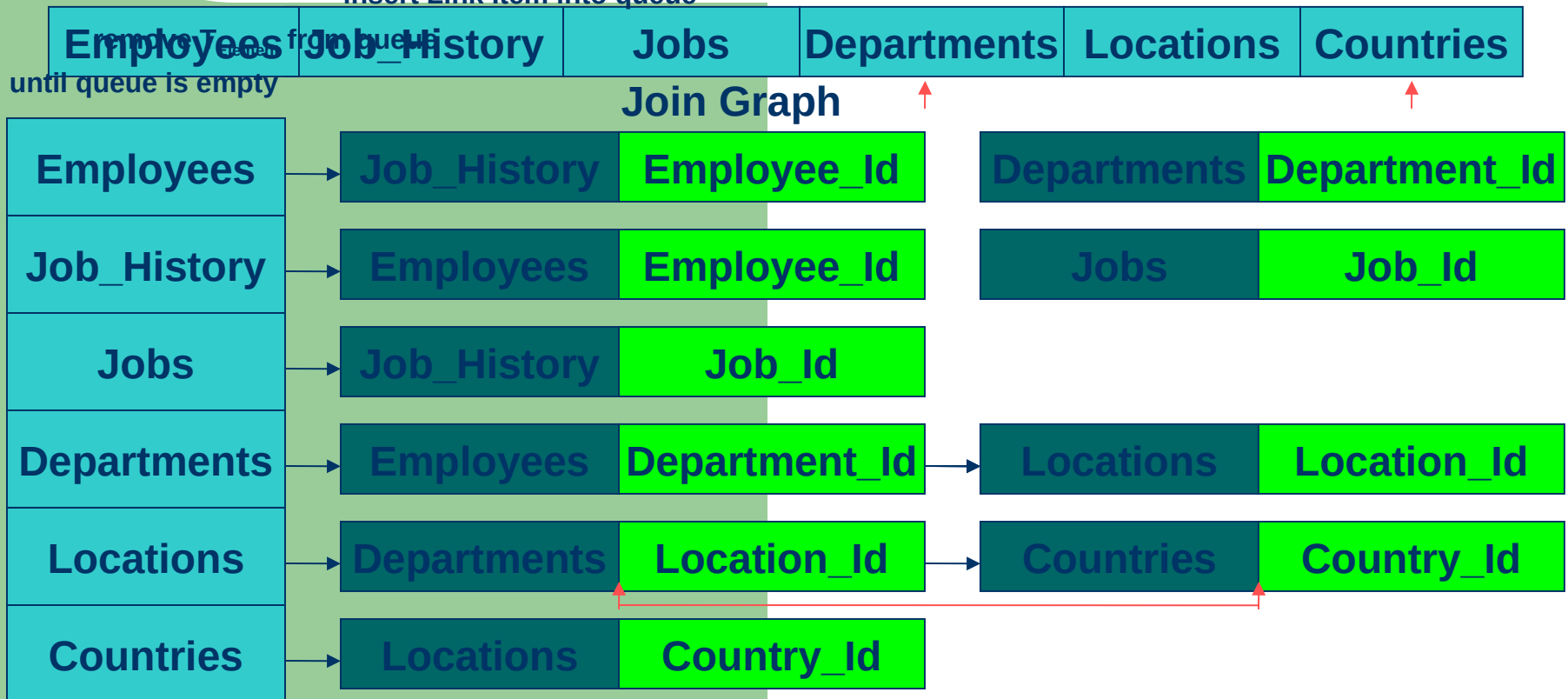
if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue
until queue is empty



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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remove T_{Element} from queue
until queue is empty

path

Employees

Jobs

Job_History

Locations

Departments

Join Base Tables

Employees Job_History

Jobs

Departments

Locations

Countries

Join Graph

Employees

Job_History

Employee_Id

Departments

Department_Id

Job_History

Employees

Employee_Id

Jobs

Job_Id

Jobs

Job_History

Job_Id

Departments

Employees

Department_Id

Locations

Location_Id

Locations

Departments

Location_Id

Countries

Country_Id

Countries

Locations

Country_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

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Locations

path

Employees

Job_History

Departments

Jobs

Locations

Countries

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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Locations

Countries

path

Employees

Job_History

Departments

Jobs

Locations

Countries

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Employees

Job_History

Departments

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Locations

Countries

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

→ repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Countries

path

Employees

Job_History

Departments

Jobs

Locations

Countries

```

let T0...Tm be the base tables
create 2 dynamic arrays queue and path
insert T0 into path

```

```
create 2 dynamic arrays queue and path
insert  $T_0$  into path
```

```

insert  $T_0$  into queue
repeat

```

repeat

T_{Element} = First Table in queue

T_{Element} = First Table in queue
for every Link Item in Adjacent Link of T_{Element} from t

for every Link Item in Adjacent Link of T_{Element} from t
 if the Link Item is in the join sequence then

- if the Link Item is in the join sequence then
 - if path doesn't contain the Link Item then

```

if path doesn't contain the Link Item then
    insert Link Item into path

```

insert Link Item into path
insert Link Item into queue

insert Link Item into queue

Join Gr

queue is empty

Join Group

Employees	→	Job_History	Empl



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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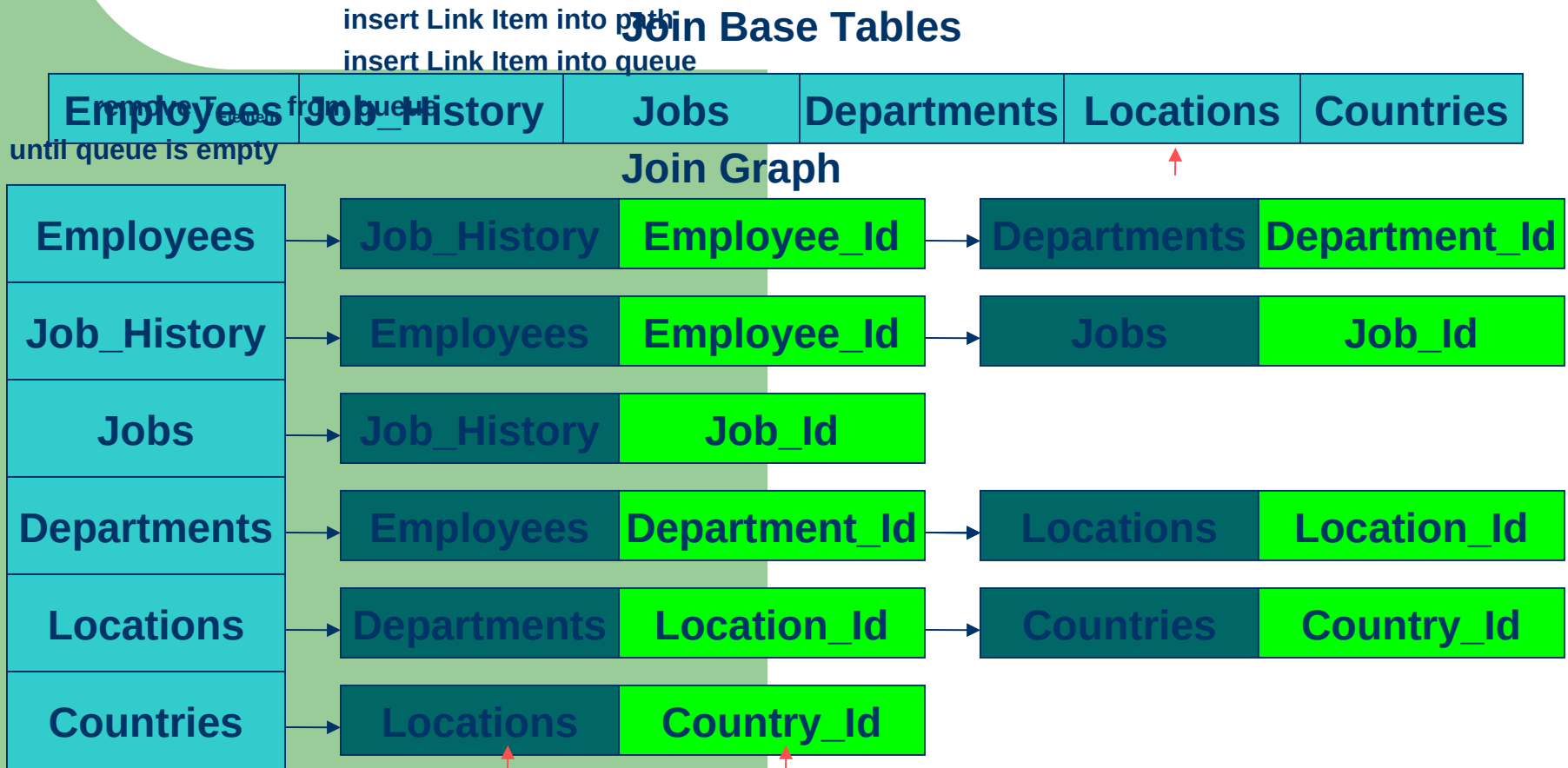
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until queue is empty



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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path

Employees

Jobs

Job_History

Locations

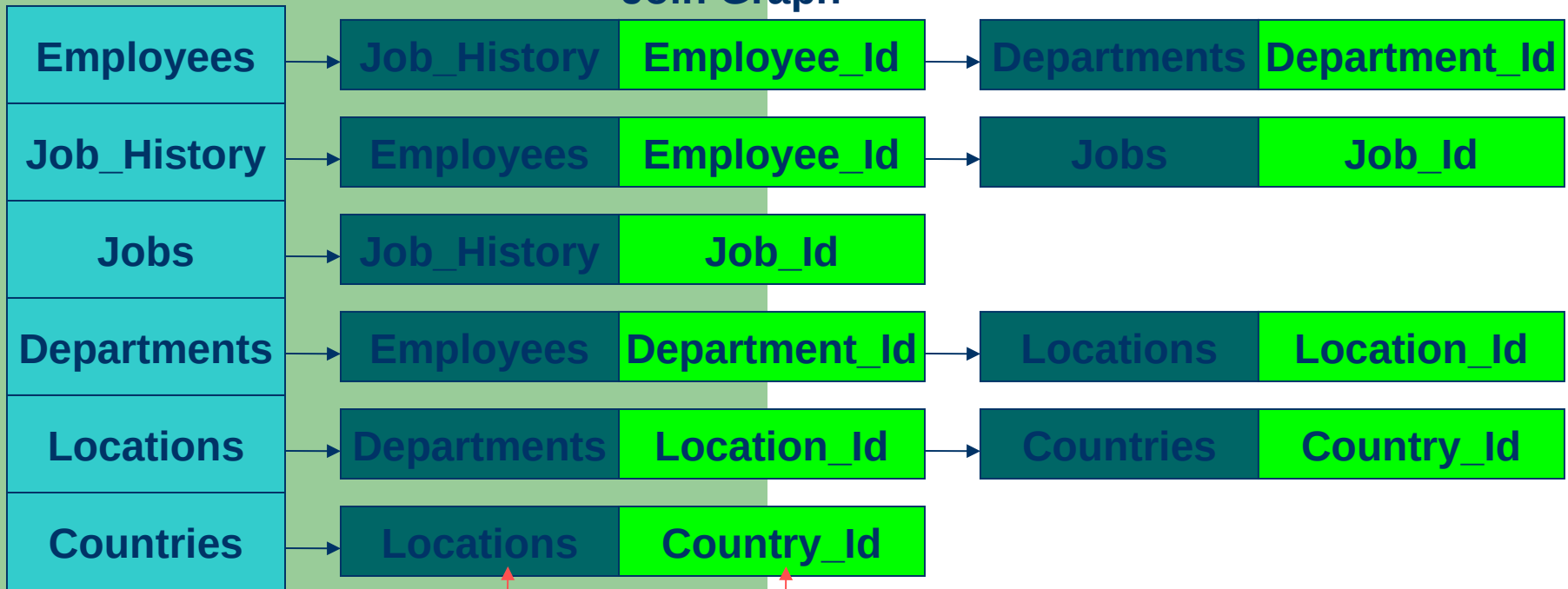
Departments

Countries

Join Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
-----------	-------------	------	-------------	-----------	-----------

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

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if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

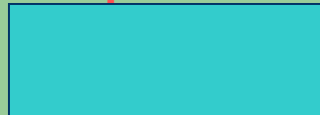
insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



path

Employees
Job_History
Departments
Jobs
Locations
Countries

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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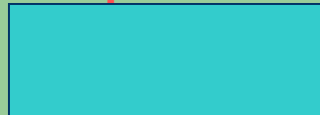
insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



path



vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries

→ insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

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$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path

→ Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes



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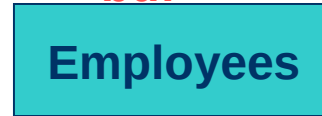
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buf



path



vertexes

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buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries

Employees

Job_History

Deparments

Jobs

Locations

Countries

Job_History

Employees

Employee_id

vertexes

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$T_{[buf]} += T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries



Employees
Job_History
Deparments
Jobs
Locations
Countries

Job_History
Employees

Employees	Employee_id
-----------	-------------

vertexes

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$



buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries



Employees
Job_History
Deparments
Jobs
Locations
Countries

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

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$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees
Job_History

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

Employees
Job_History
Deparments
Jobs
Locations
Countries
Employees
Job_History

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

insert all the names of base tables from path as vertexes in JoinPathList
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for all the remainder entries in path do

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 $T_{[buf]} += T_i$
 $Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

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$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees
Job_History
Deparments
Jobs
Locations
Countries
Employees Job_History

Job_History
Employees
Employees Job_History

Employees	Employee_Id
Job_History	Employee_Id

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries



vertexes

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$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History		

Departments

Employees
Job_History

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History

Employees
Job_History
Departments
Jobs
Locations
Countries



Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History		



Departments	Employees	Department_Id
-------------	-----------	---------------

Employees
Job_History
Deparments
Jobs
Locations
Countries
Employees Job_History

vertexes

insert all the names of base tables from path as vertexes in JoinPathList

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$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History		

Departments	Employees	Department_Id
-------------	-----------	---------------

vertexes

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees
Job_History
Deparments
Jobs
Locations
Countries
Employees
Job_History
Employees
Job_History
Departments

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History		

Departments	Employees	Department_Id
-------------	-----------	---------------

vertexes

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$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

buf

path

Employees
Job_History
Deparments
Jobs
Locations
Countries
Employees
Job_History
Employees
Job_History
Departments

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History		

Departments	Employees	Department_Id
-------------	-----------	---------------

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

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$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History Employees
Job_History Departments

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History Employees		
Job_History Departments		

Departments	Employees	Department_Id
-------------	-----------	---------------

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees
Job_History
Employees
Job_History
Departments

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History	Employees	
Job_History	Jobs	Job_Id
Departments		

Departments	Employees	Department_Id
-------------	-----------	---------------

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

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$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History Employees
Job_History Departments

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History Employees	Departments	Department_Id
Job_History Departments	Jobs	Job_Id

Departments	Employees	Department_Id
Jobs		

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
	Departments		

Locations			
Countries			
Employees	Departments	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Employees			
Job_History			
Departments			

buf

Employees
Job_History
Departments

path

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

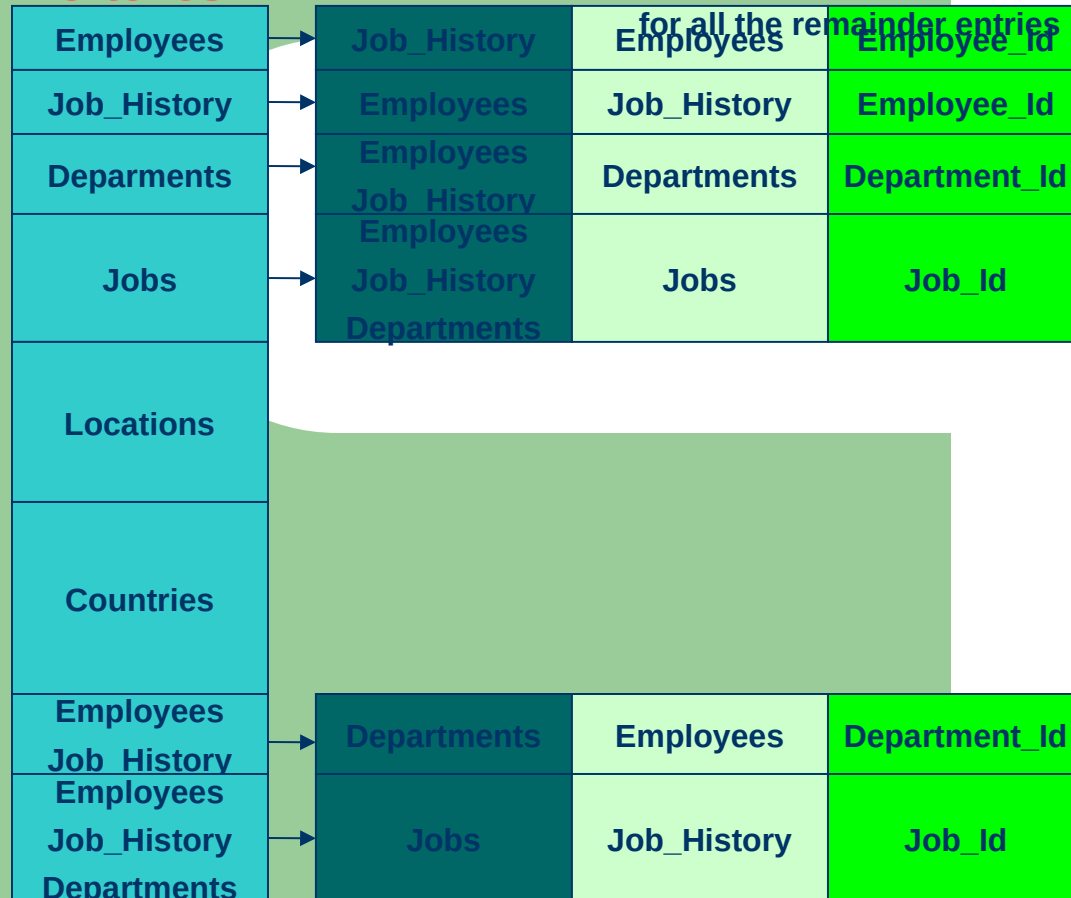
$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path



vertexes

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History
Departments
Jobs

path

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History Employees
Job_History Departments Employees
Job_History Departments Jobs

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History Employees	Departments	Department_Id
Job_History Departments	Jobs	Job_Id

Departments	Employees	Department_Id
Jobs	Job_History	Job_Id

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path

vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History Employees
Job_History Departments Employees
Job_History Departments Jobs

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History	Departments	Department_Id
Employees Job_History Departments	Jobs	Job_Id

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History
Departments
Jobs

path

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

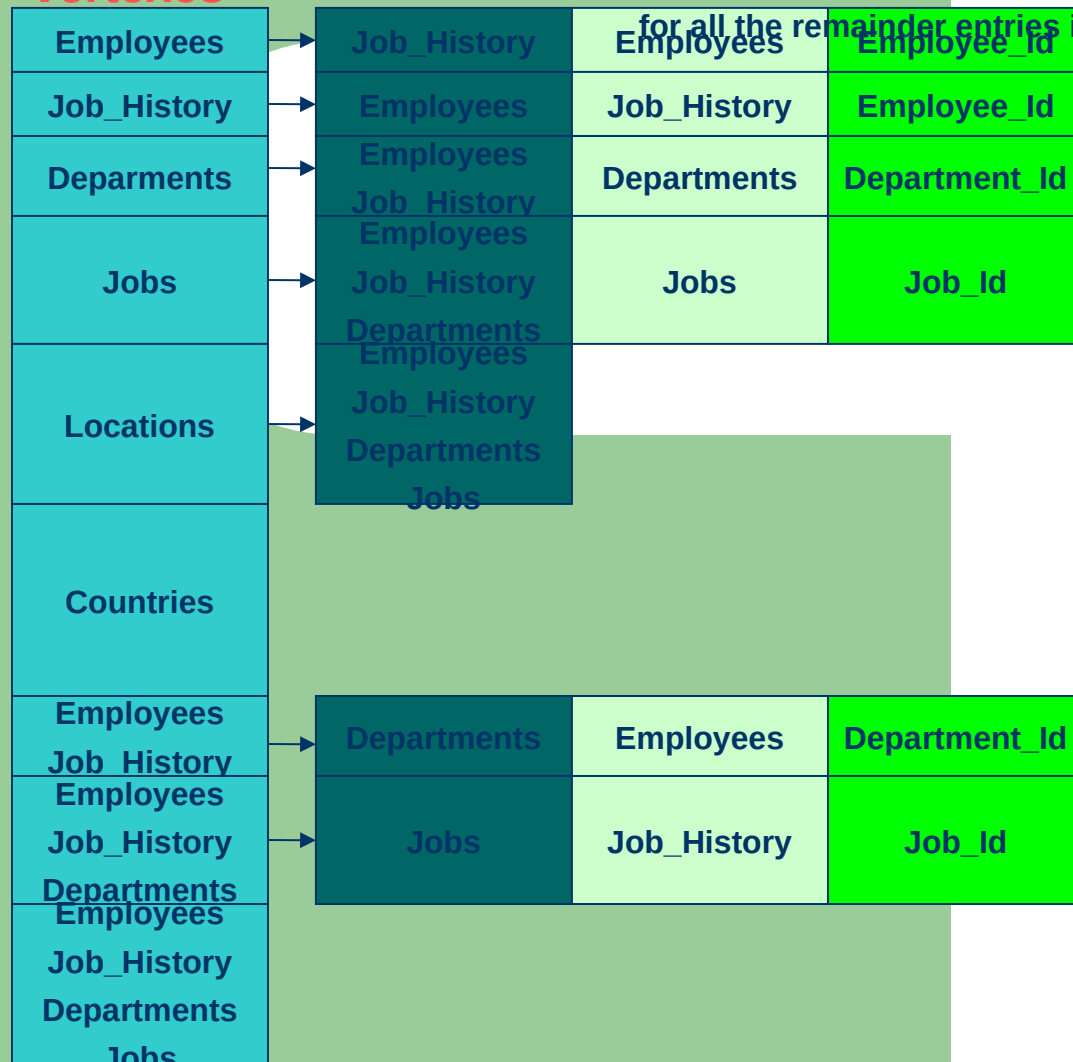
$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path



vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs

Employees
Job_History
Departments
Jobs
Locations
Countries



Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees	Departments	Department_Id
Job_History	Jobs	Job_Id
Employees	Locations	Location_Id

Departments	Employees	Department_Id
Jobs	Job_History	Job_Id

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees
Job_History
Employees
Job_History
Departments
Employees
Job_History
Departments
Jobs

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

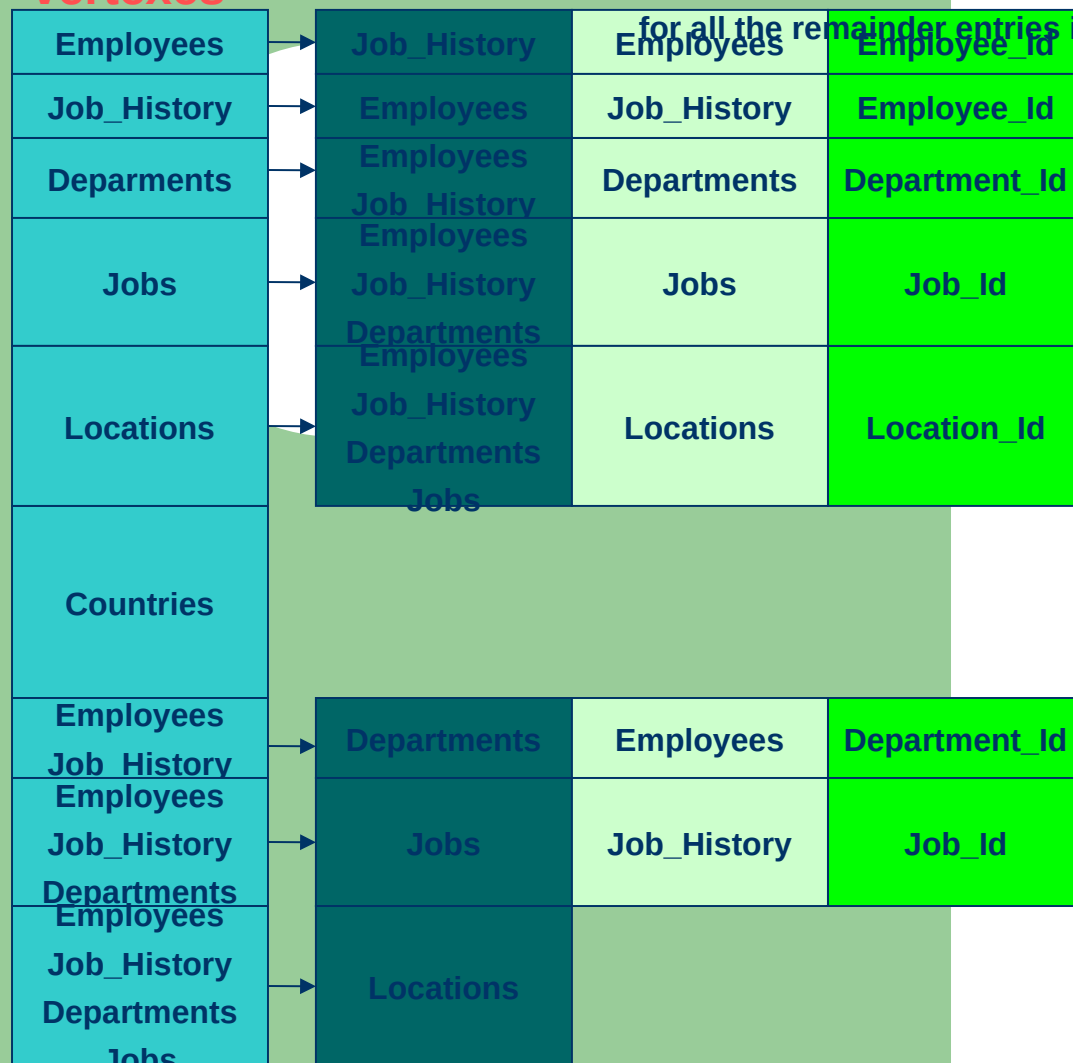
$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

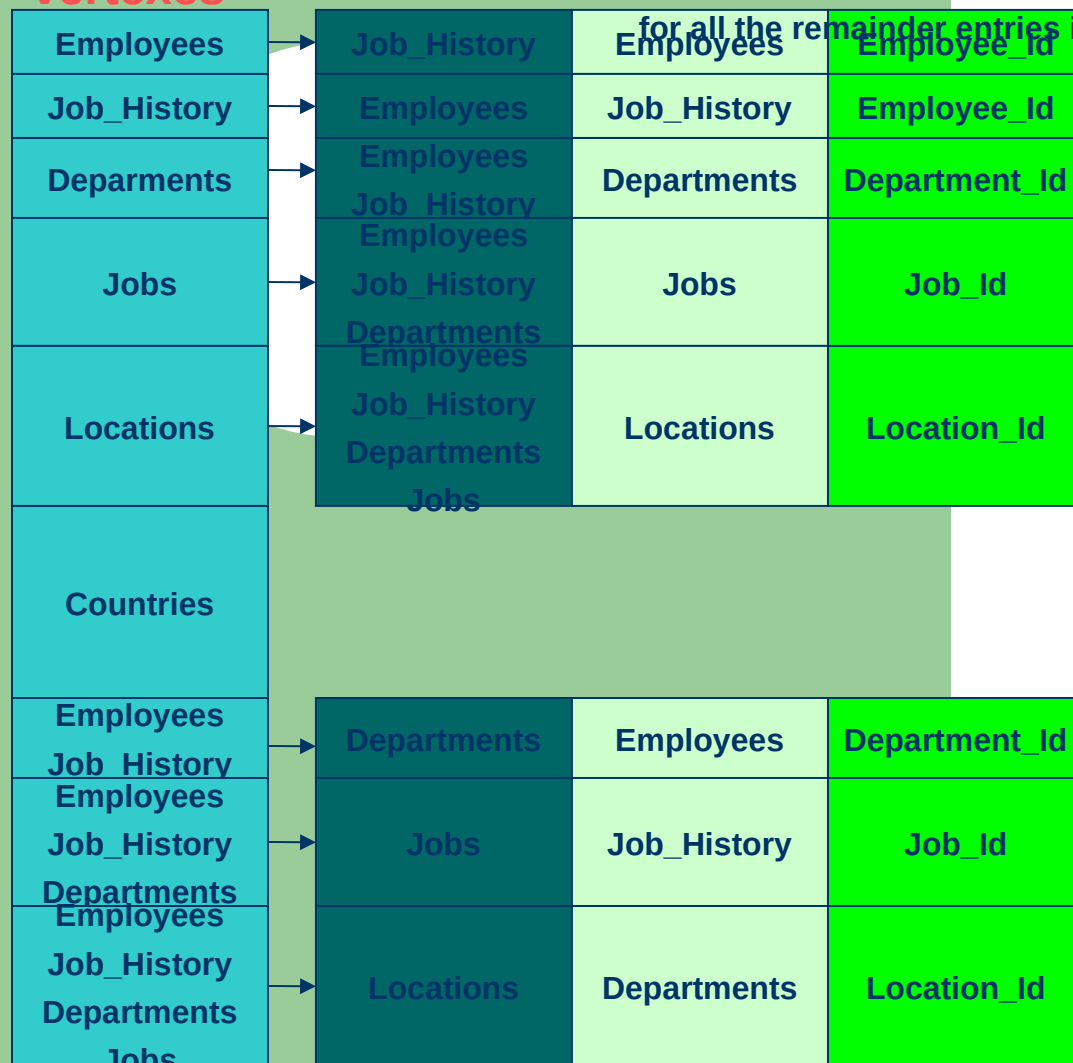
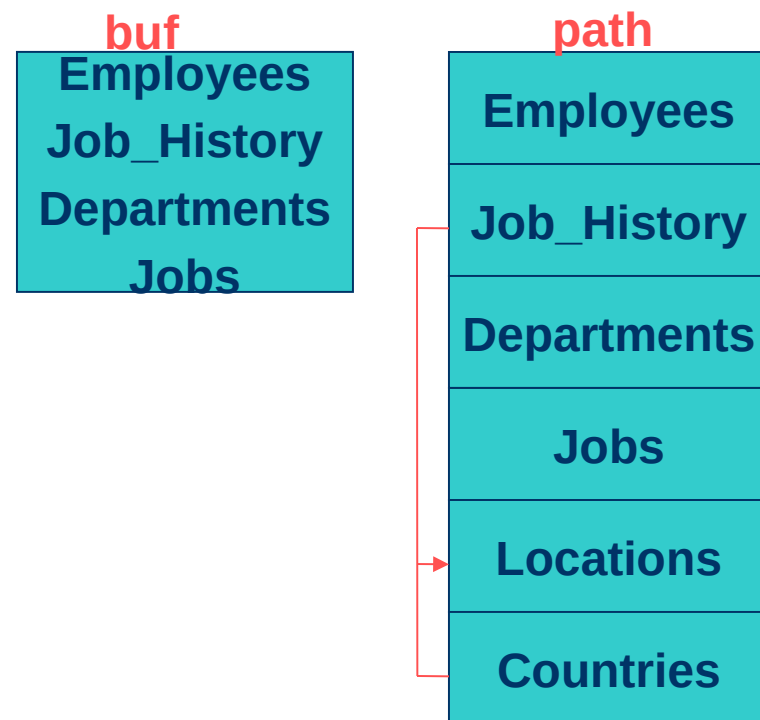
$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$



insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path

vertexes

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
Locations	Job_History	Locations	Location_Id

take one T_i at a time

$JoinPathAdjacentList(T_i) = T_{[buf]}$

$Key(T_i) = getFirstAdjacentListKey(T_i, T_{[buf]})$

$JoinPathAdjacentList(T_{[buf]}) = T_i$

$Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

Countries			
Employees	Departments	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Employees	Locations	Departments	Location_Id

buf

Employees
Job_History
Departments
Jobs
Locations

path

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path

vertexes

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
Locations	Job_History	Locations	Location_Id

take one T_i at a time

$JoinPathAdjacentList(T_i) = T_{[buf]}$

$Key(T_i) = getFirstAdjacentListKey(T_i, T_{[buf]})$

$JoinPathAdjacentList(T_{[buf]}) = T_i$

$Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

Countries			
Employees	Departments	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Employees	Locations	Departments	Location_Id
Job_History			
Departments			
Employees			
Job_History			
Departments			
Jobs			
Locations			

buf

Employees
Job_History
Departments
Jobs
Locations

path

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

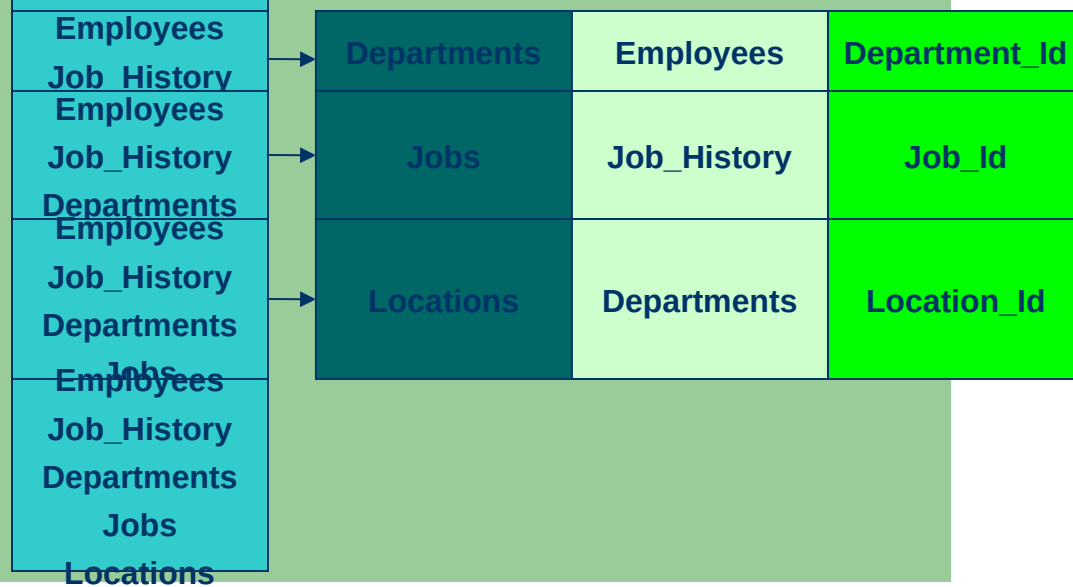
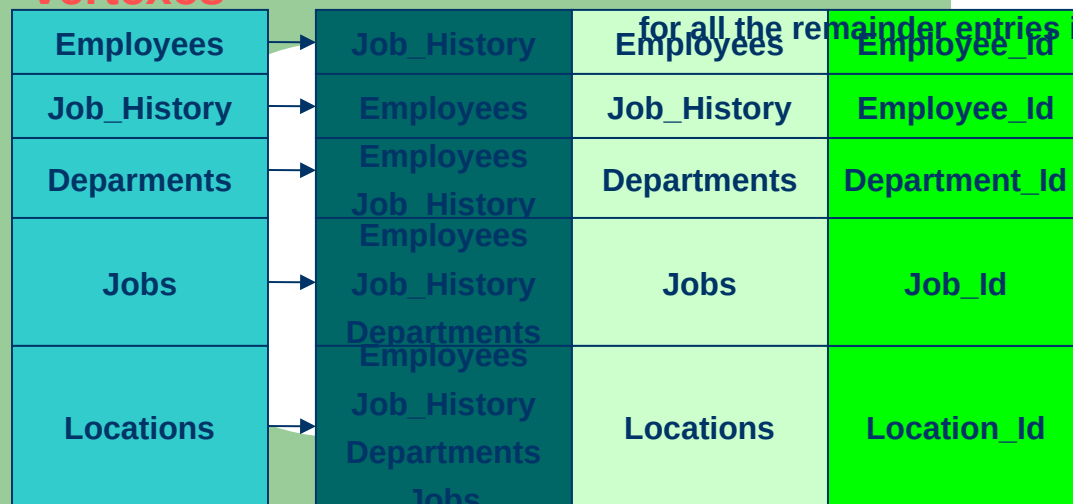
$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	→	Job_History	Employees	for all the remainder entries	Employee_Id
Job_History	→	Employees	Job_History		Employee_Id
Departments	→	Employees	Departments		Department_Id
Jobs	→	Job_History	Jobs		Job_Id
		Departments			
Locations	→	Job_History	Locations		Location_Id
		Departments			
Countries	→	Jobs			
		Job_History			
		Departments			
Employees	→	Locations	Employees		Department_Id
		Departments			
Job_History	→	Jobs	Job_History		Job_Id
Employees					
Job_History	→	Locations	Departments		Location_Id
Departments					
Employees	→				
Job_History					
Departments					
Jobs					
Locations	→				

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path

vertexes

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
	Job_History		
Jobs	Job_History	Jobs	Job_Id
	Departments		
Locations	Job_History	Locations	Location_Id
	Departments		
	Jobs		
Countries	Job_History	Countries	Country_Id
	Departments		
	Jobs		
Employees	Locations		
Job_History	Departments	Employees	Department_Id
Employees			
Job_History		Jobs	Job_Id
Departments			
Employees			
Job_History		Locations	Location_Id
Departments		Departments	
Jobs			
Locations			

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History
Departments
Jobs
Locations

path

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
Locations	Job_History	Locations	Location_Id
Countries	Job_History	Countries	Country_Id
Employees	Departments	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Departments	Locations	Departments	Location_Id
Jobs	Countries		

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path

vertexes

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
Locations	Job_History	Locations	Location_Id
Countries	Departments	Countries	Country_Id
Employees	Job_History	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Departments	Locations	Departments	Location_Id
Employees	Countries	Locations	Country_Id

take one T_i at a time

$JoinPathAdjacentList(T_i) = T_{[buf]}$

$Key(T_i) = getFirstAdjacentListKey(T_i, T_{[buf]})$

$JoinPathAdjacentList(T_{[buf]}) = T_i$

$Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

$Insert\ NodesList[T_{[buf]}] = T_{[buf]}$

buf

Employees
Job_History
Departments
Jobs
Locations

path

Employees
Job_History
Departments
Jobs
Locations
Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

vertexes

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
Locations	Job_History	Locations	Location_Id
Countries	Departments	Countries	Country_Id
Employees	Job_History	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Departments	Locations	Departments	Location_Id
Jobs	Countries	Locations	Country_Id

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

vertexes

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees	Departments	Department_Id
Jobs	Job_History	Jobs	Job_Id
Locations	Job_History	Locations	Location_Id
Countries	Departments	Countries	Country_Id
Employees	Job_History	Employees	Department_Id
Job_History	Jobs	Job_History	Job_Id
Departments	Locations	Departments	Location_Id
Jobs	Countries	Locations	Country_Id

Vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries

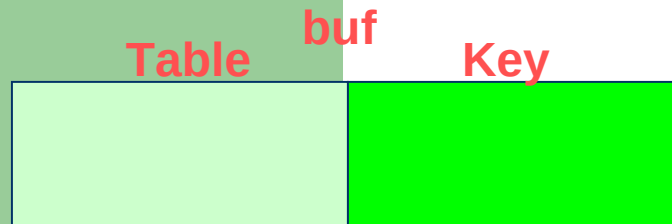
path

Employees
Job_History
Departments
Jobs
Locations
Countries

Join Path List

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Departments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Job_History Employees Departments	→	Jobs	Job_History	Job_Id
Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

→ create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
 take one $T_{[i]}$ at a time
 for all Base Tables in $T_{[i]}$ do
 take one T_k at a time
 for every buf.Table = T_k do
 if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
 InheritedKey($T_{[i]}$) += buf.key
 if T_i is the table from which comes Key($T_{[i]}$) then
 buf.Table = T_i
 buf.key = Key($T_{[i]}$)



→ create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do

→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

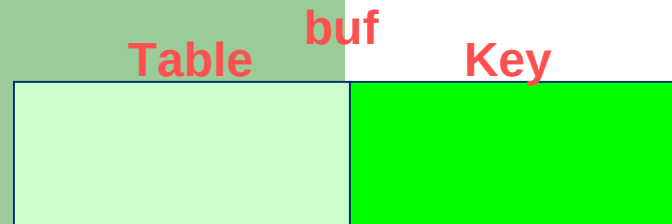
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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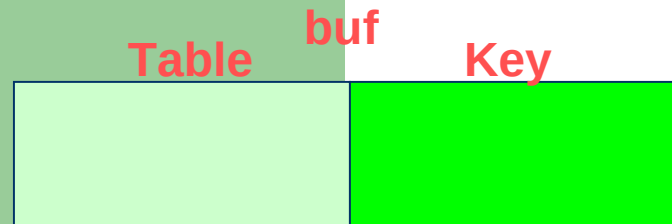
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Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

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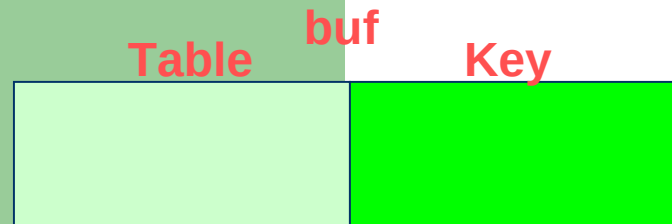
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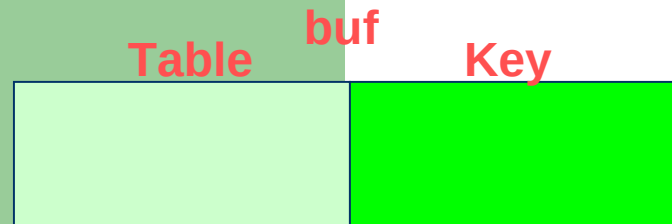
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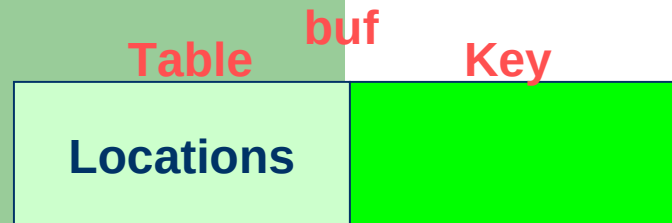
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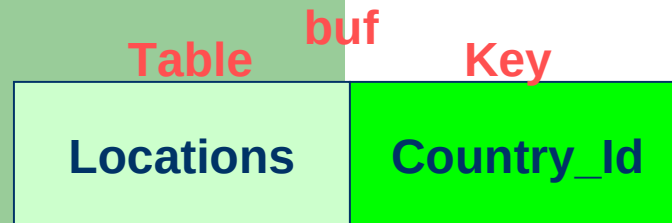
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Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

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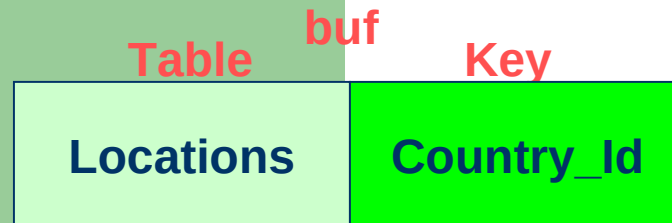
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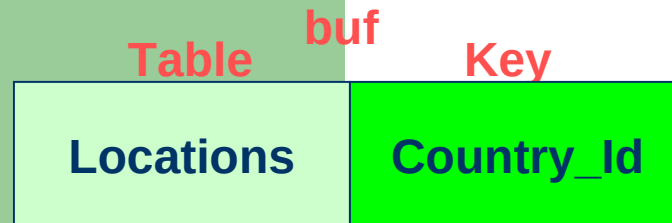
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Table	Key
Locations	Country_Id
Departments	



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Table	Key
Locations	Country_Id
Departments	Location_Id



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Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

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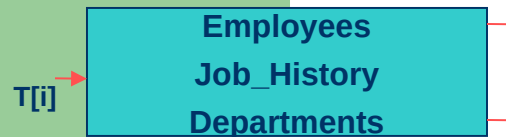
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Table	Key
Locations	Country_Id
Departments	Location_Id



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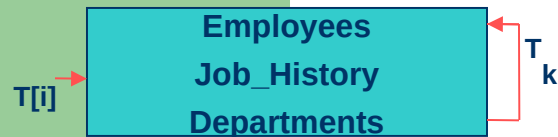
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Table	Key
Locations	Country_Id
Departments	Location_Id



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Table	Key
Locations	Country_Id
Departments	Location_Id

$T_{[i]}$	Employees Job_History Departments	T_k
-----------	---	-------

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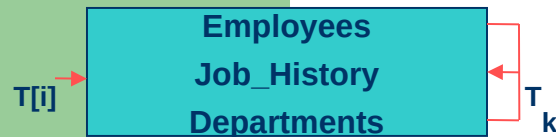
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Table	Key
Locations	Country_Id
Departments	Location_Id



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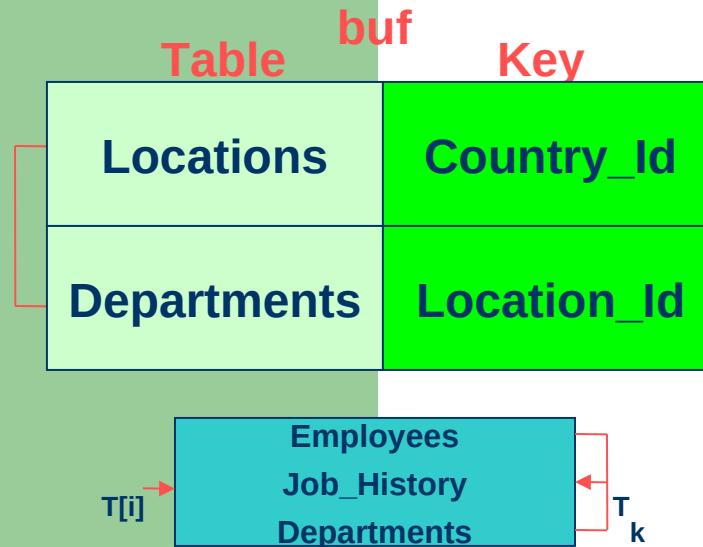
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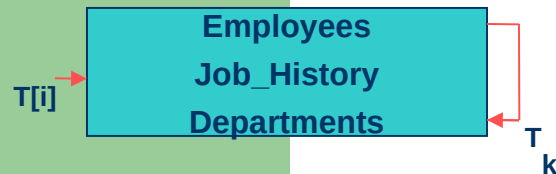
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Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
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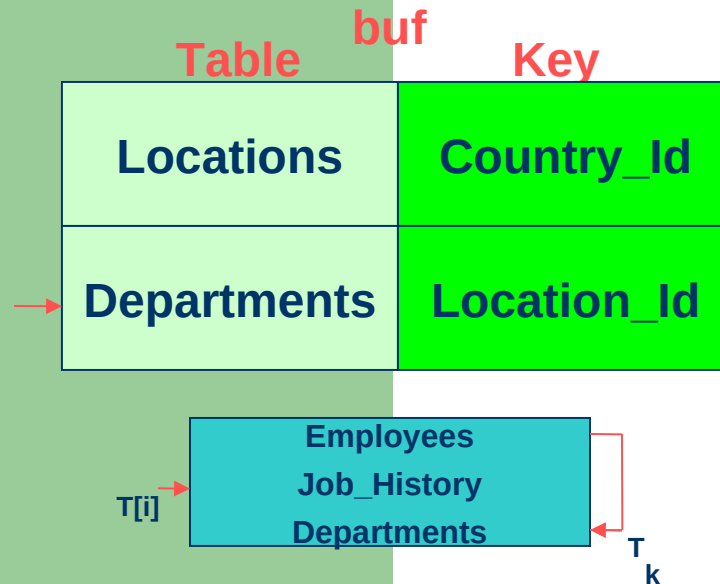
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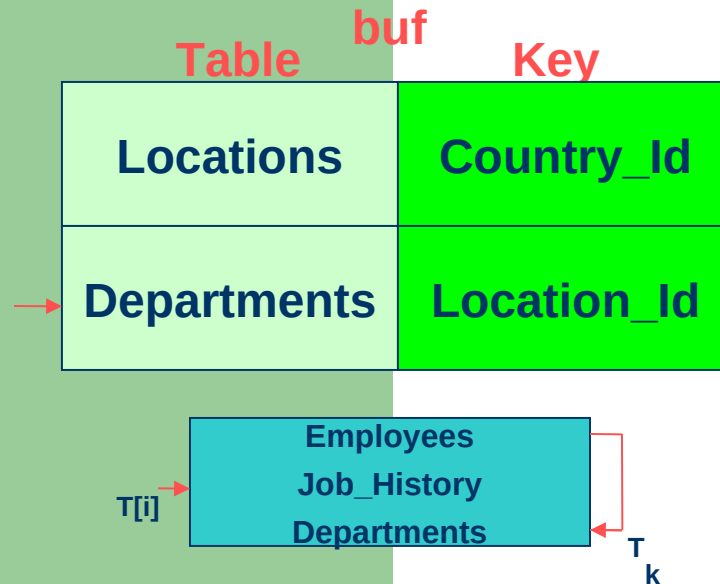
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Join Path List

T
[i]

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Deparments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments	Locations	Location_Id
Countries	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History Employees	Locations Departments	Employees	Department_Id
Job_History Departments Employees	Jobs	Job_History	Job_Id
Job_History Departments Jobs	Locations	Departments	Location_Id
Locations Employees Job_History Departments Jobs Locations Countries	Countries	Locations	Country_Id

Departments	Location_Id
-------------	-------------

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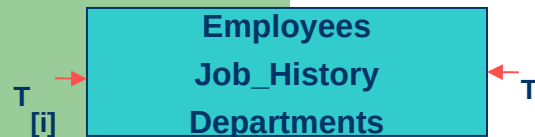
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Table	Key
Locations	Country_Id
Departments	Location_Id



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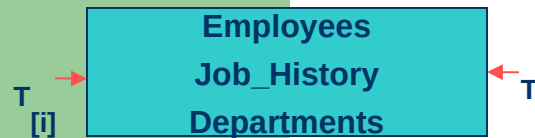
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	



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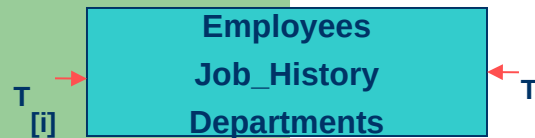
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



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Join Path List

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Employees	Job_History	Employees	Employee_Id
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Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments	Locations	Location_Id
Countries	Employees Job_History Departments Jobs	Countries	Country_Id
Employees Job_History Employees	Departments	Employees	Department_Id
Job_History Departments Employees	Jobs	Job_History	Job_Id
Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries			

Departments	Location_Id
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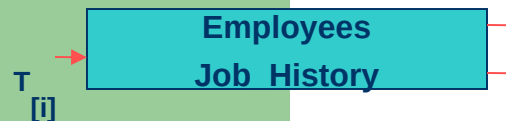
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



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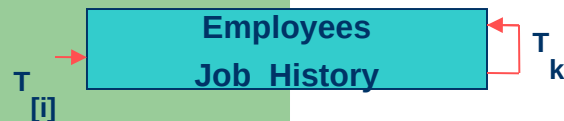
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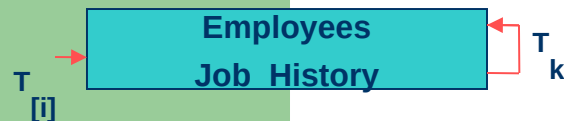
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



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take one T_k at a time

for every buf.Table = T_k do

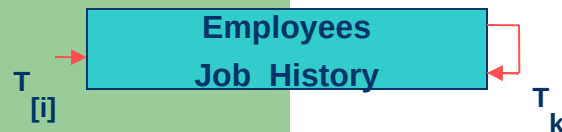
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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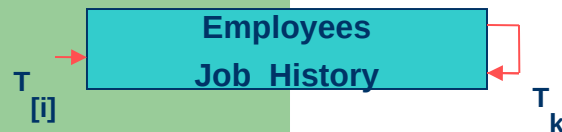
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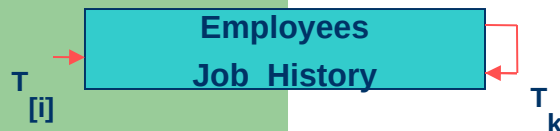
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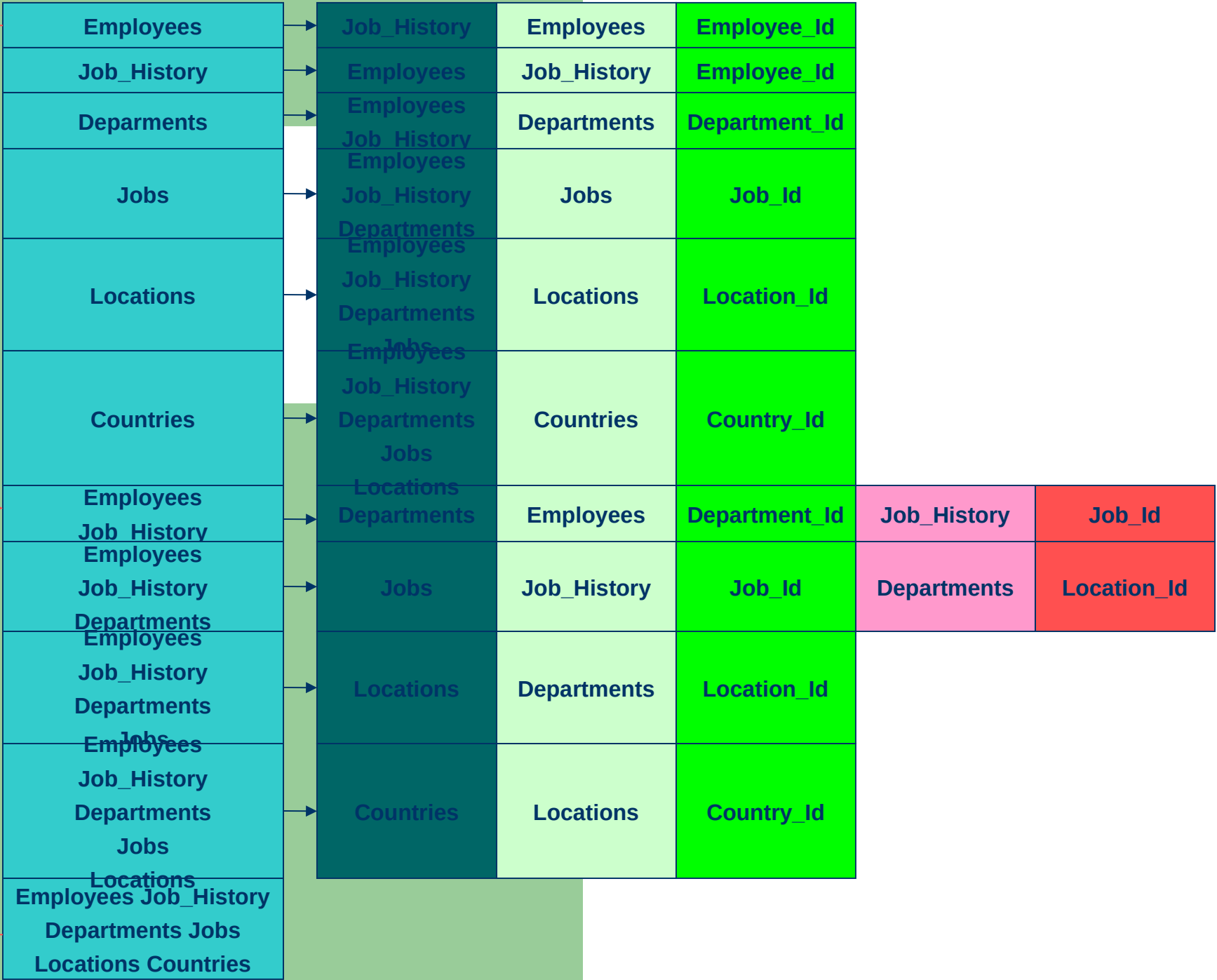
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Join Path List

T
[i]



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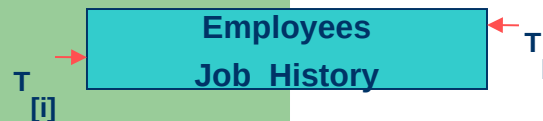
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	



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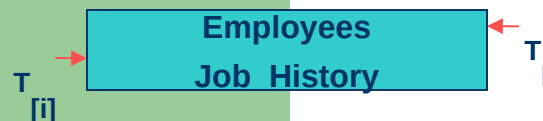
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Join Path List

T[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees	Departments	Department_Id		
		Job_History				
Jobs	→	Employees	Jobs	Job_Id		
		Job_History				
		Departments				
Locations	→	Employees	Locations	Location_Id		
		Job_History				
		Departments				
Countries	→	Employees	Countries	Country_Id		
		Job_History				
		Departments				
		Jobs				
Employees	→	Locations	Employees	Department_Id	Job_History	Job_Id
Job_History	→	Departments				
Employees	→		Jobs	Job_Id	Departments	Location_Id
Job_History	→		Job_History			
Departments	→					
Employees	→	Locations	Departments	Location_Id		
Job_History	→					
Departments	→					
Jobs	→					
Employees	→	Countries	Locations	Country_Id		
Job_History	→					
Departments	→					
Jobs	→					
Locations	→					
Employees Job_History	→					
Departments Jobs	→					
Locations Countries	→					

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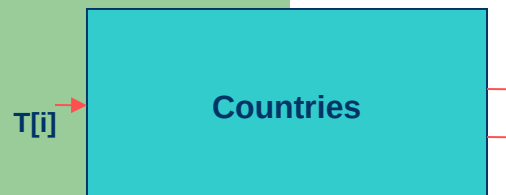
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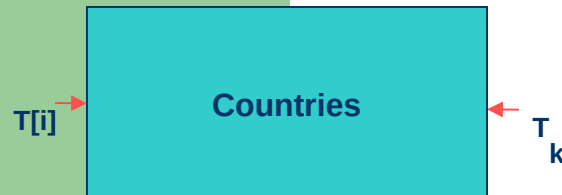
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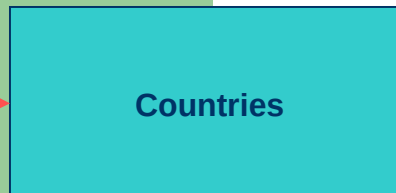
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buf.key = Key($T_{[i]}$)

buf	
Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id

$T_{[i]}$



Countries

T_k

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Table	Key
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$T[i]$ →

Countries

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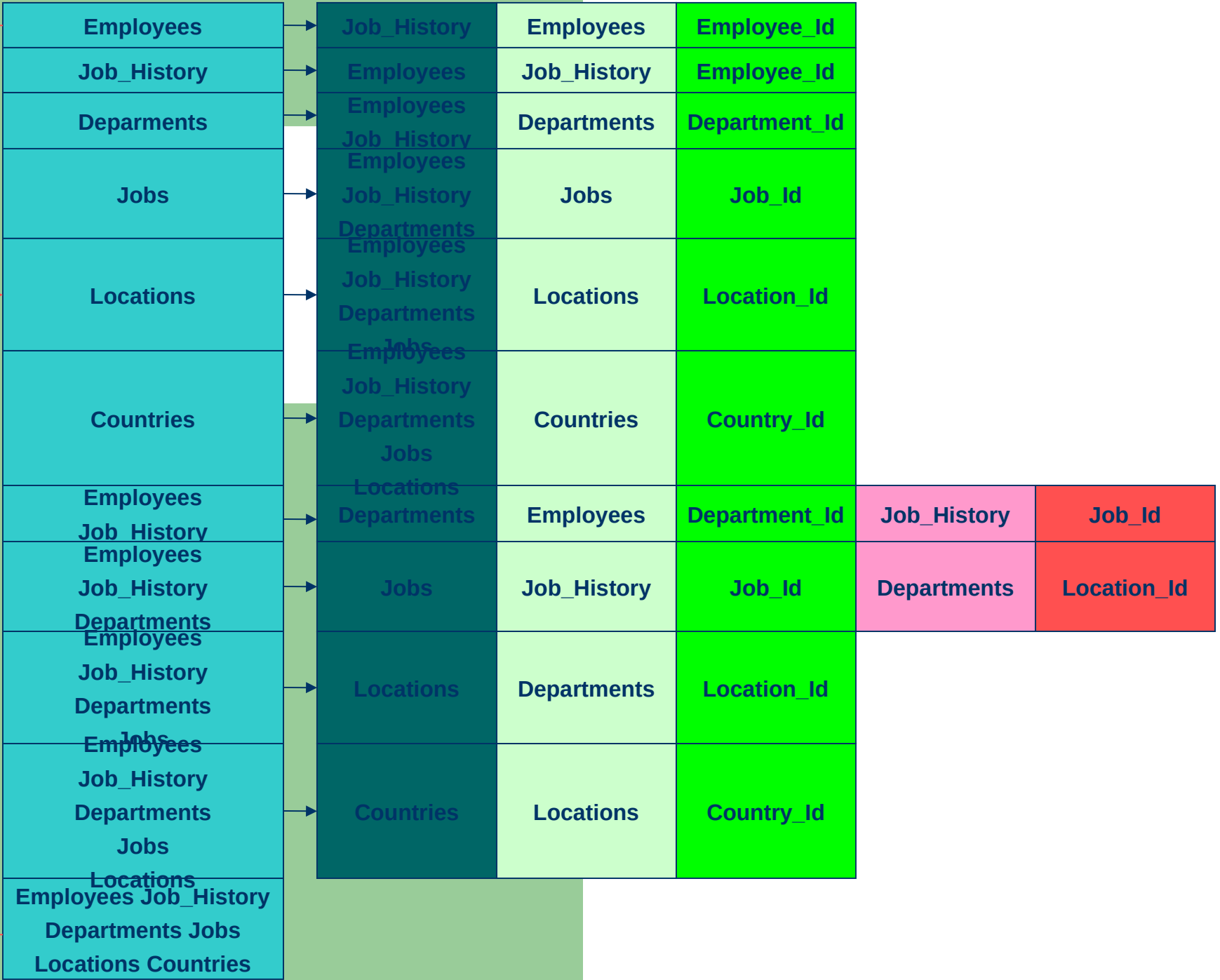
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Join Path List

T
[i]



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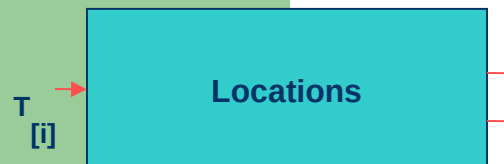
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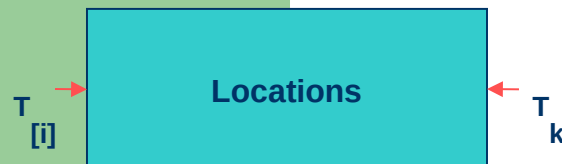
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buf	
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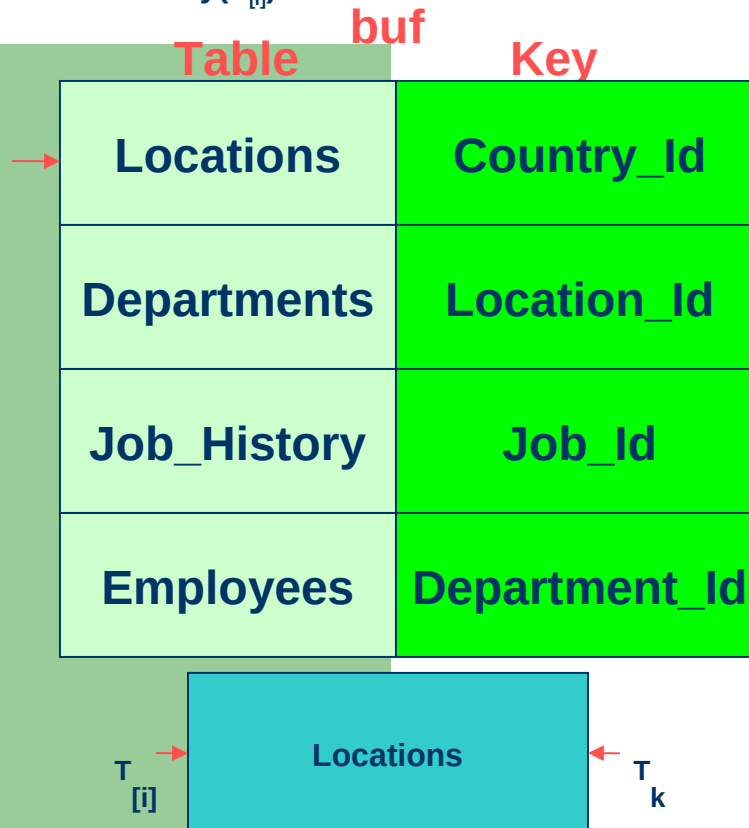
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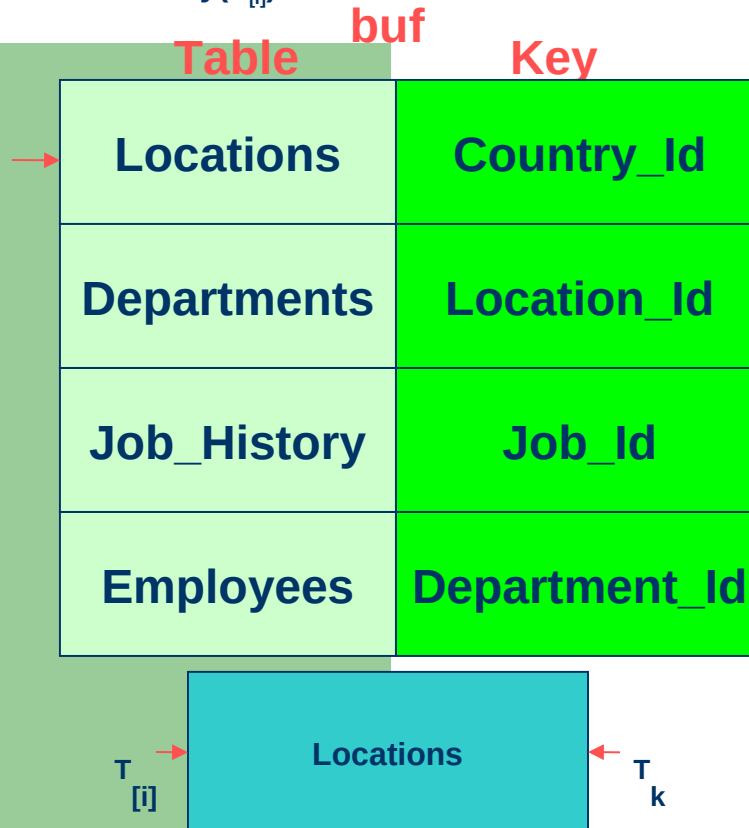
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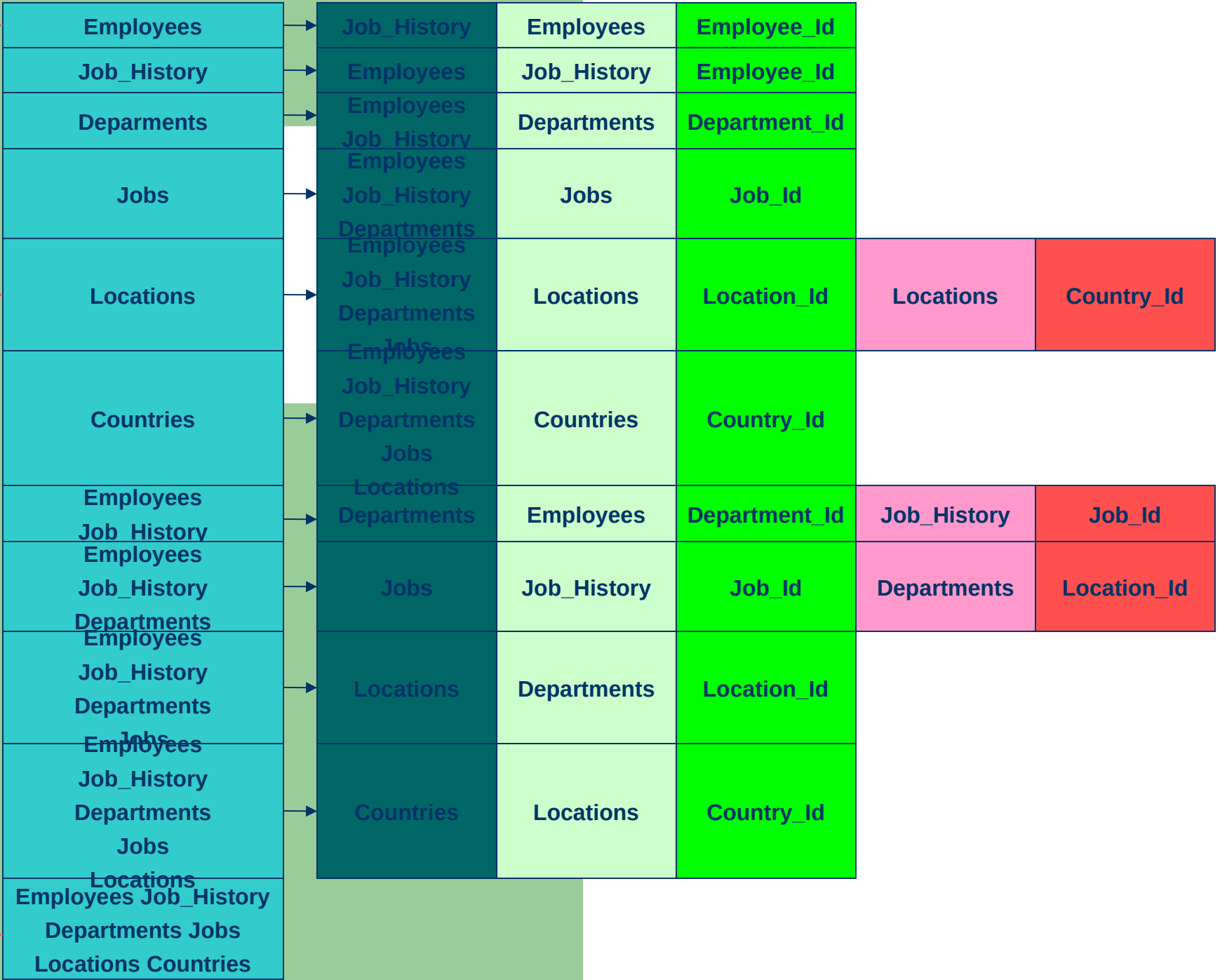
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Path Join List

T
[i]



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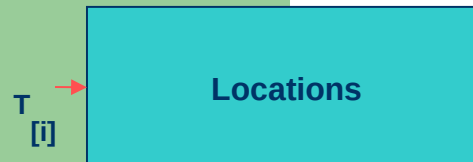
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Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



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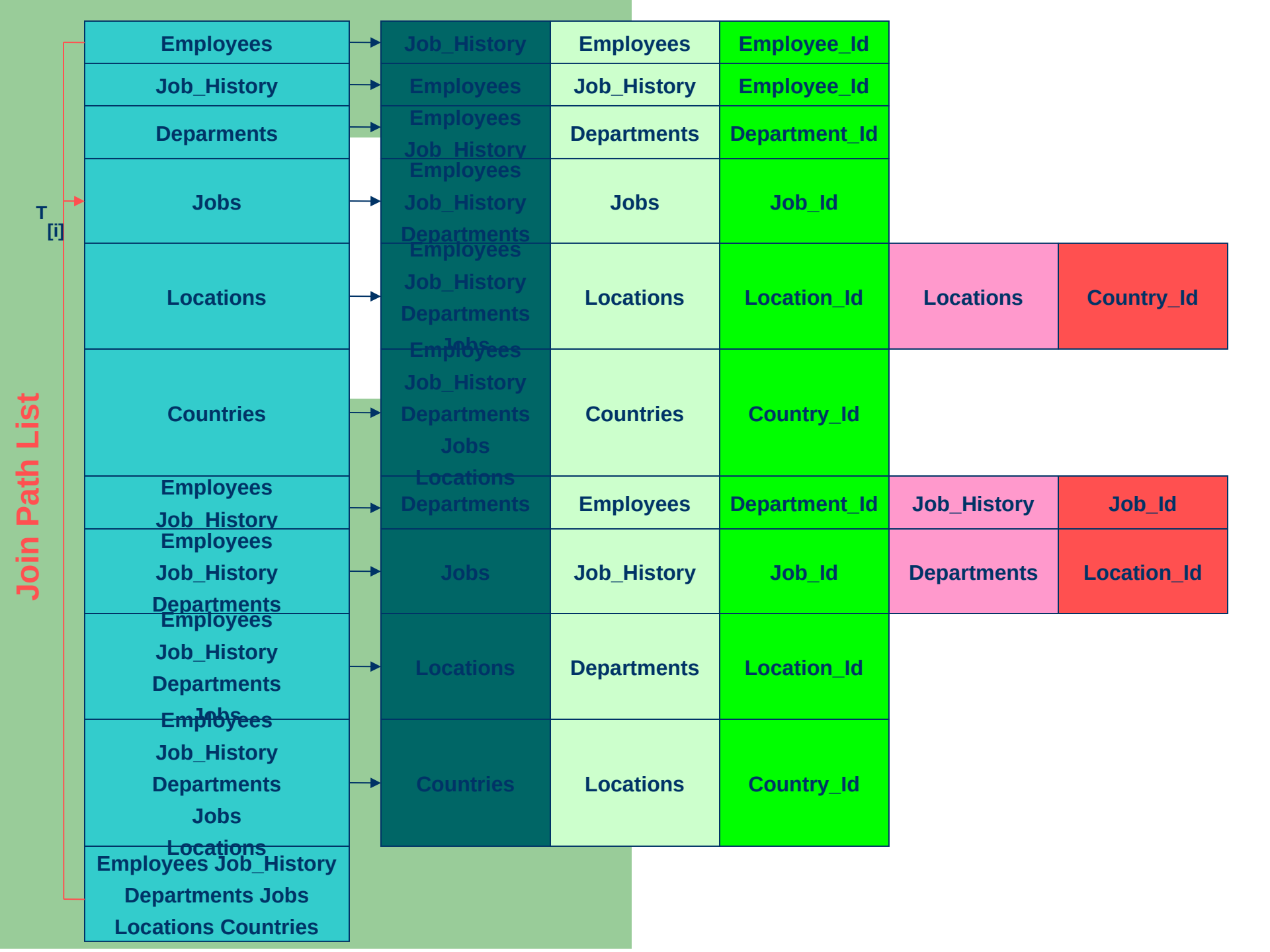
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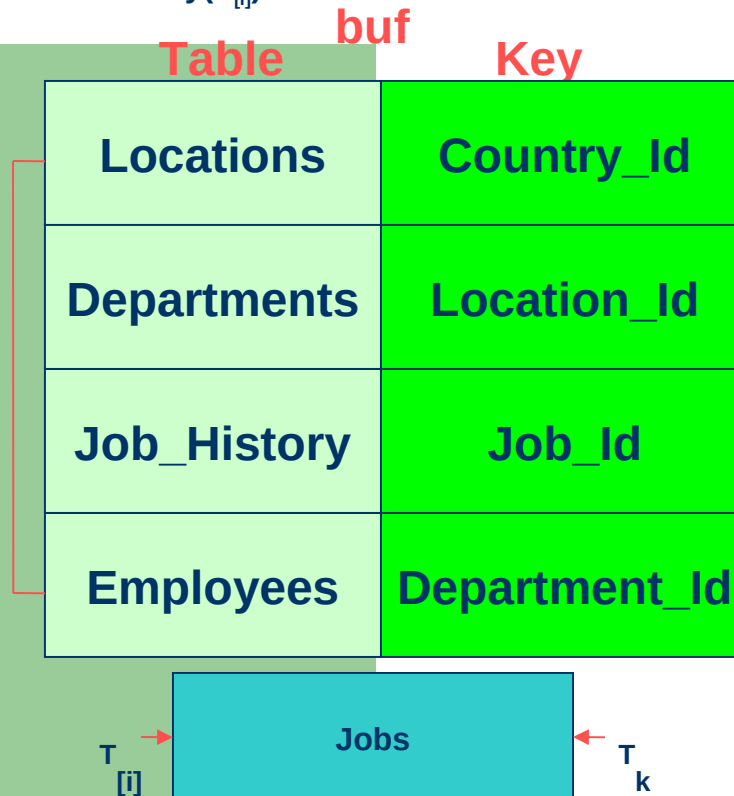
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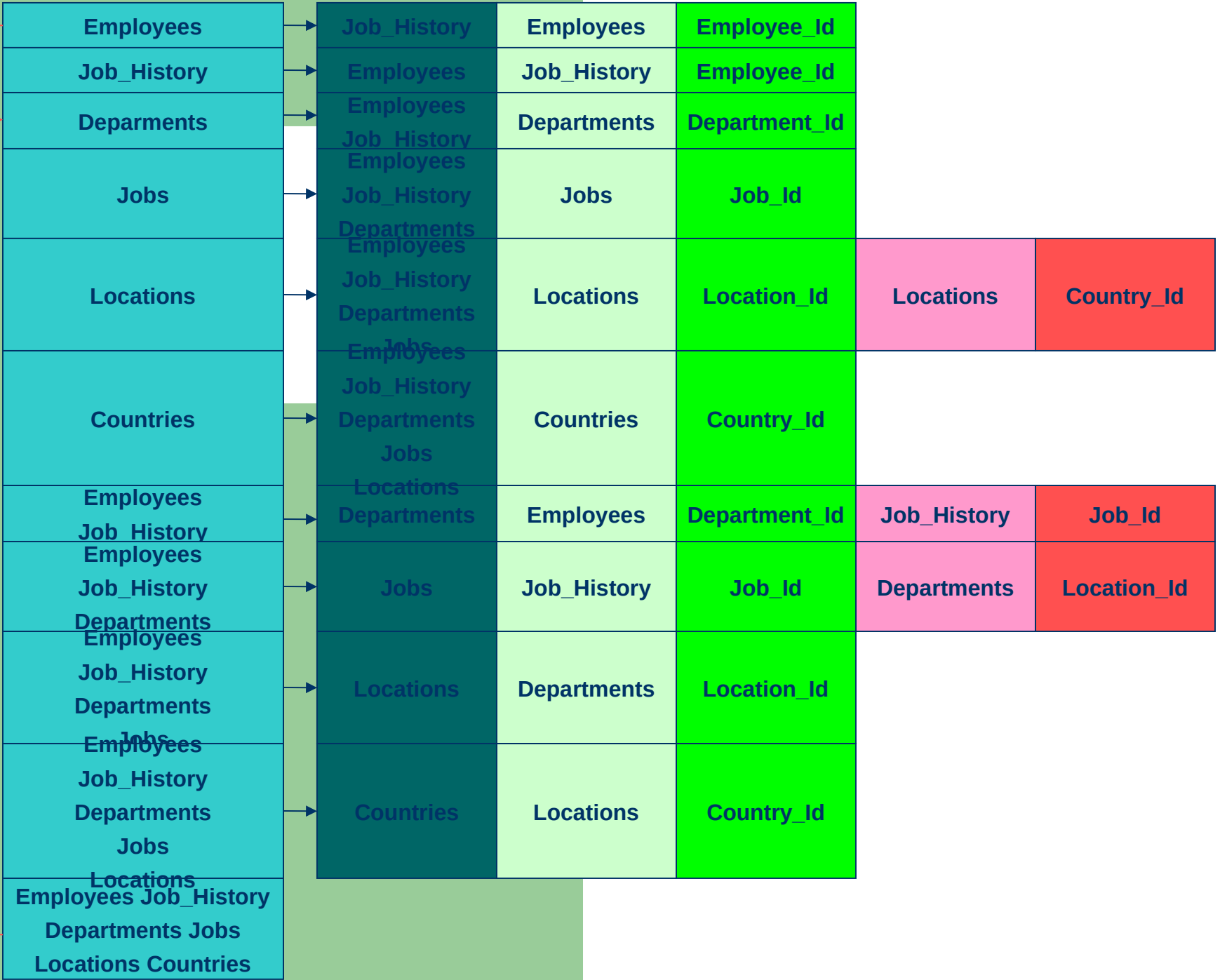
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Join Path List

T
[i]



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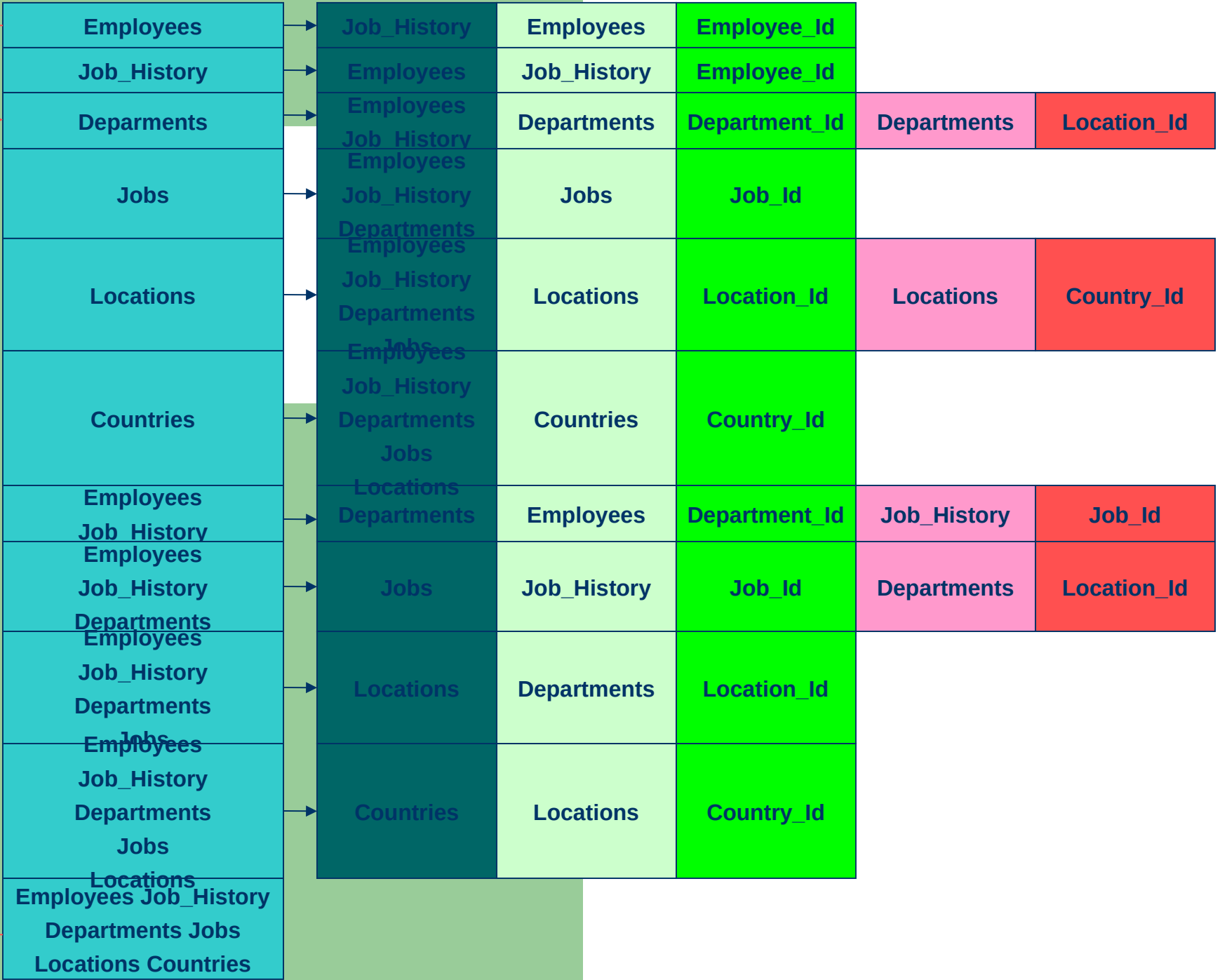
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Join Path List

T
[i]



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Departments	Location_Id
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Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees	Departments	Department_Id	Departments	Location_Id
		Job_History				
Jobs	→	Employees	Jobs	Job_Id		
		Job_History				
		Departments				
Locations	→	Employees	Locations	Location_Id	Locations	Country_Id
		Job_History				
		Departments				
Countries	→	Employees	Countries	Country_Id		
		Job_History				
		Departments				
		Jobs				
Employees	→	Locations	Employees	Department_Id	Job_History	Job_Id
Job_History	→	Departments				
Employees	→		Jobs	Job_Id	Departments	Location_Id
Job_History	→					
Departments	→		Locations	Location_Id		
Employees	→					
Job_History	→		Countries	Country_Id		
Departments	→					
Jobs	→					
Locations	→					
Employees Job_History	→					
Departments Jobs	→					
Locations Countries	→					

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do

→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

buf
Table Key

Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

buf
Table Key

Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

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if (buf.key \neq Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id	Job_History	Job_Id
Deparments	→	Employees	Departments	Department_Id	Departments	Location_Id
		Job_History				
Jobs	→	Employees	Jobs	Job_Id		
		Job_History				
		Departments				
Locations	→	Employees	Locations	Location_Id	Locations	Country_Id
		Job_History				
		Departments				
		Jobs				
Countries	→	Employees	Countries	Country_Id		
		Job_History				
		Departments				
		Jobs				
		Locations				
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Departments Employees	→	Locations	Departments	Location_Id		
Job_History Departments	→	Countries	Locations	Country_Id		
Jobs Employees	→					
Locations Job_History	→					
Departments Jobs	→					
Locations Countries	→					

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

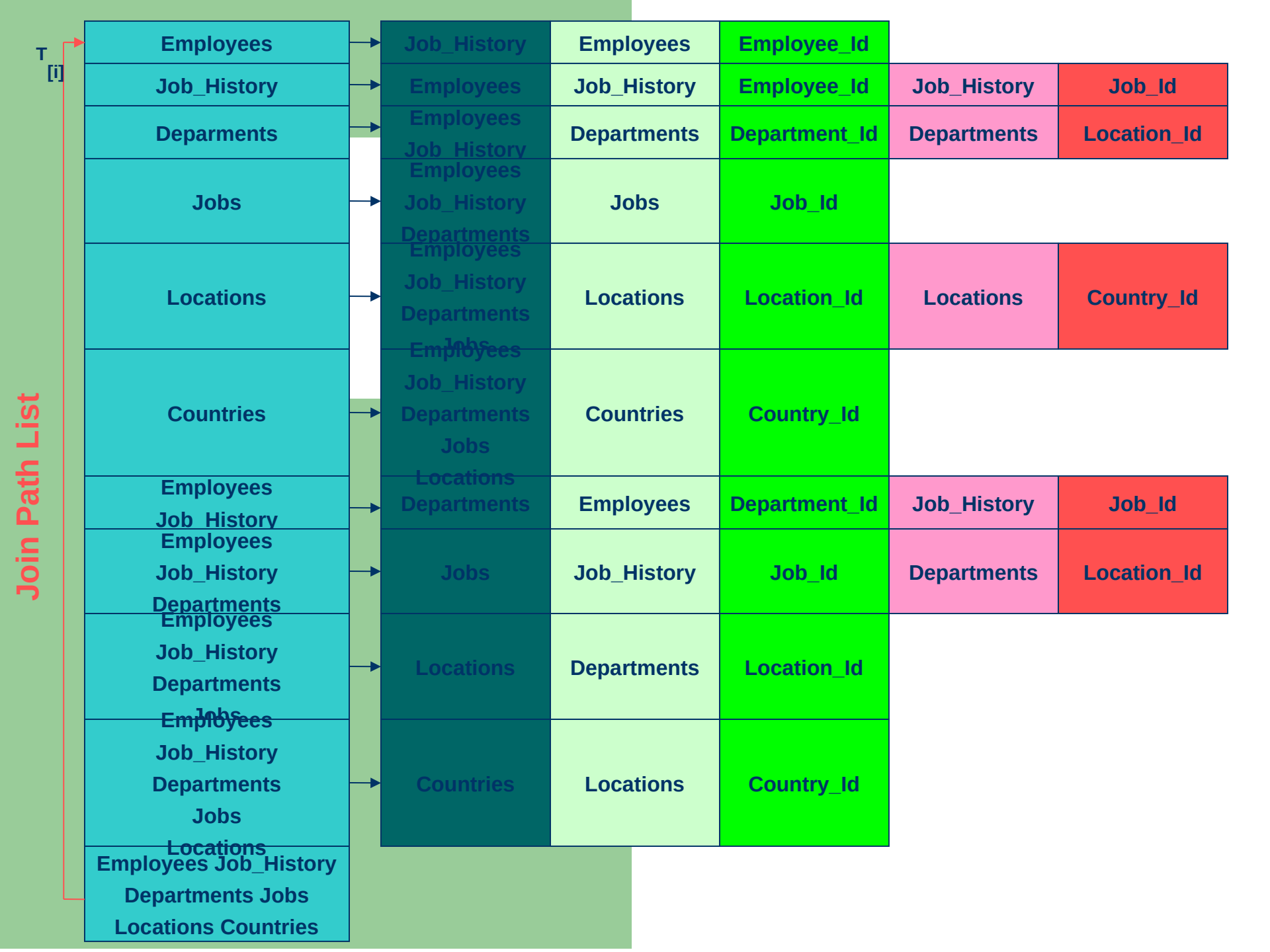
for every buf.Table = T_k do

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→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

→ for all Base Tables in $T_{[i]}$ do

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buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

buf
Table Key

Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

buf
Table Key

Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	Job_History	Employees	Employee_Id	Employees	Department_Id
Job_History	Employees	Job_History	Employee_Id	Job_History	Job_Id
Deparments	Employees	Departments	Department_Id	Departments	Location_Id
Jobs	Job_History	Jobs	Job_Id		
Locations	Job_History	Locations	Location_Id	Locations	Country_Id
Countries	Departments	Countries	Country_Id		
Employees Job_History	Departments	Employees	Department_Id	Job_History	Job_Id
Job_History Employees	Jobs	Job_History	Job_Id	Departments	Location_Id
Departments Employees	Locations	Departments	Location_Id		
Job_History Departments	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs					
Locations Employees Job_History Departments Jobs Locations Countries					

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

NodesList		Adjacent Table		Table		Key		Inherited Table		Key	
0	Employees	→	Job_History	Employees	Employee_Id	Employees	Department_Id				
1	Job_History	→	Employees	Job_History	Employee_Id	Job_History	Job_Id				
2	Deparments	→	Employees Job_History	Departments	Department_Id	Departments	Location_Id				
3	Jobs	→	Employees Job_History Departments	Jobs	Job_Id						
4	Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id				
5	Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id						
6	Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id				
7	Job_History Employees Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id				
8	Job_History Departments Jobs	→	Locations	Departments	Location_Id						
9	Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id						
10	Employees Job_History Departments Jobs Locations Countries		Adjacent List								

Give a general name for the B⁺Tree.

Give for every entry in the JoinPathList a B⁺Tree index with name as the B⁺Tree + the PathJoinList entry number.

About the last virtual table, it index has no keys, it works because we consider pairs of < keys, Data Pointers > so they are ordered by their data pointers. Scanning the index we get all the sequences of joined data pointers.

Non Terminal has repeated empty keys they point to different pages. When comes a key it would be inserted in the last page.

Duplicate keys are inserted and when a page is full , the key is repeated in the non terminal.

In any case we can incorporate any key of our choice from the tables forming the virtual table.

If the table is in join with itself, consider the table twice as aliases.

Define a Create Join Index (IndexName, Eventual columns for the last virtual table representing tables in join)

Implementation:

Use a big buffer and from the Data Dictionary divide it by the keys length, inherited keys length and space for the number of Data Pointers.

Suppose we wants the join sequence of the tables ordered by Employees.Name and Departments.Department_Id, applying the algorithm, the JoinPathList becomes:

NodesList		Adjacent Table	Table	Key	Inherited Table	Key
0	Employees	Job_History	Employees	Employee_Id	Employees	Name
					Employees	Department_Id
1	Job_History	Employees	Job_History	Employee_Id	Job_History	Job_Id
2	Deparments	Employees Job_History	Departments	Department_Id	Departments	Location_Id
3	Jobs	Employees Job_History Departments	Jobs	Job_Id		
		Employees Job_History Departments				
4	Locations	Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
5	Countries	Employees Job_History Departments Jobs	Countries	Country_Id		
		Employees Job_History Departments Jobs				
6	Employees Job_History	Departments	Employees	Department_Id	Employees	Name
					Job_History	Job_Id
7	Employees Job_History Departments	Jobs	Job_History	Job_Id	Employees	Name
					Departments	Department_Id
					Departments	Location_Id

8

Employees
Job_History
Departments
Jobs



Locations

Departments

Location_Id

Employees

Name

9

Employees
Job_History
Departments
Jobs
Locations



Countries

Locations

Country_Id

Employees

Name

10

Employees Job_History
Departments Jobs
Locations Countries



Employees

Name

Departments

Department_Id

Departments

Departments_Id

Departments

Department_Id

Create B⁺Trees

- The Nodes (Vertexes) in the JoinPathList represents all the base tables + virtual tables constituting from the base tables by adding one at a time in mode that the one added is at least in direct join with its precedents.
- Defining a B⁺Tree for every node, the ones for the virtual tables have for every key a set of data pointers equal to the number of base tables constituting it and from definition of the virtual tables, combining the rows pointed by those data pointers we obtain a joined row.

The algorithm for creating B⁺Trees is the following:

create B+Trees(in PathJoinList; out B+Trees);

give a general name for the BJoinTree

for all entries in JoinPathList do

 take one node at a time

 create a B+Tree for the node defined as

 name of the B+Tree equal to the name of BJoinTree follow by the
 index number of the node entry

 Number of data pointers equal to the number of base tables
 constituting the virtual table of the node

 Key is defined by the pair <Table, Key> in the adjacent list of the
 node

 Inherited Keys are defined by the pairs <Table, Inherited Key> in
 the adjacent list of the node

Insert routine

When a new row R_m from table T_i get inserted do the following:

- Locate the entry of T_i in the JoinPathList
- From its adjacent List, locate the definition of the keys and inherited keys
- From Row R_m get the columns constituting the keys and the inherited keys
- Call AddJoinKey (T_i , Keys, InheritedKeys, DP_i) where DP_i is the row id of row R_m .

Notice that $Keys_i$, $InheritedKeys_i$ and DP_i are relative to the row R_m from table T_i

AddJoinKey ($T_{[i]}$, $[DP_i]$)

- Call AddKey ($B^+Tree(T_{[i]}), keys_{[i]}, InheritedKeys_{[i]}, [DP_i]$) for the index of table $T_{[i]}$
- Locate the entry of $T_{[i]}$ in the JoinPathList
- From its adjacent List, locate the Table $T_{[k]}$ adjacent to it and do the following:
 - Locate the entry of $T_{[k]}$ in the JoinPathList
 - FindKey($B^+Tree(T_{[k]}), Keys_{[i]}$)
 - While found($keys_{[i]}$) do
 - ReturnKeys($B^+Tree(T_{[k]}), keys_{[k]}, InheritedKeys_{[k]}, [DP_k]$)
 - Locate the entry of $T_{[ik]}$ in the JoinPathList
 - From its adjacent List, locate the definition of the keys and inherited keys
 - From $keys_{[i]}, inheritedkeys_{[i]}, keys_{[k]}, inheritedkeys_{[k]}$ get the keys and inherited keys of $T_{[ik]}$
 - AddJoinKey ($T_{[ik]}, Keys_{[ik]}, InheritedKeys_{[ik]}, [DP_{ik}]$)
 - NextKey($B^+Tree(T_{[k]}), Keys_{[i]}$)

AddJoinKey ($T_{[i]}$, $[DP_i]$)

In the same fashion when using an ordinary B⁺Tree and one row get inserted, so we check the definition of the B⁺Tree to get the necessary keys from the row to insert them, with B^{Join}Tree we check the definition to get the keys and the inherited keys.

Call AddJoinKey(T_i , [keys], $[DP_i]$)

Employees table

	EMPLOYEE_ID	NAME	EMAIL	PHONE_NUMBER	HIRE_DATE	JOB_ID	SALARY	DEPARTMENT_ID
0	101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN
1	102	Jorge Perez	jperez	448-5268	05/14/1999	AC_MGR	60000	ACC
2	103	Edward Cartier	ecartier	742-8429	03/01/2003	SA_MGR	60000	SAL
3	104	Teresa Gonzalez	tgonzalez	134-8329	12/20/2002	AC_AUD	55000	ACC
4	105	Michelle Blanche	mblanche	745-7496	01/02/2001	SA_REP	35000	SAL

Job_History table

	EMPLOYEE_ID	START_DATE	END_DATE	JOB_ID	DEPARTMENT_ID
0	101	12/16/1998	12/15/1999	AC_AUD	ACC
1	102	05/16/1999	05/15/2001	AC_AUD	ACC
2	101	12/16/1999	12/15/2001	SA_REP	SAL
3	103	03/16/2003	03/15/2004	AC_AUD	ACC

Departments table

	Deparment_Id	Department_Name	Manager_Id	Location_Id
0	FIN	FINANCE	101	1000
1	ACC	ACCOUNTING	102	1010
2	SAL	SALES	103	1020

Jobs Table

	JOB_ID	JOB_TITLE	MIN_SALARY	MAX_SALARY
0	AC_AUD	Accounting Auditor	30000	60000
1	AC_MGR	Accounting Manager	60000	70000
2	FI_MGR	Finance Manager	50000	70000
3	SA_MGR	Sales Manager	50000	60000
4	SA_REP	Sales Representative	30000	40000

Locations table

	LOCATION_ ID	STREET_ADDRESS	POSTAL_ CODE	CITY	STATE PROVINCE	COUNTRY_ ID
0	1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca
1	1010	Calle Sermiento numero 300	62547	Guadalajara	Baja	me
2	1020	Rue des fleurs n. 345	78921	Toulouse	Moyenne	fr

Countries table

	Country_Id	Country_Name
0	ca	Canada
1	fr	France
2	me	Mexico

Inserting first row from table Employees

Base Table

Employees
0

EMPLOYEE_ID	NAME	EMAIL	PHONE_NUMBER	HIRE_DATE	JOB_ID	SALARY	DEPARTMENT_ID
101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN

→ insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

Base Table

Employees
0

T_i

DP_i
0



DataRef

EMPLOYEE_ID	NAME	EMAIL	PHONE_NUMBER	HIRE_DATE	JOB_ID	SALARY	DEPARTMENT_ID
101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN

Row R_m

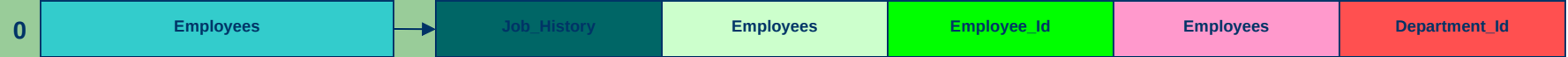
insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T in JoinPathList_i

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T in JoinPathList_i

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T in JoinPathList_i

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

DP _i	EMPLOYEE_ID	NAME	EMAIL	PHONE_NUMBER	HIRE_DATE	JOB_ID	SALARY	DEPARTMENT_ID
	YEE_ID			NUMBER	DATE			MENT_ID
0	101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN

Keys

Row R_m

Inherited Keys

```
insertRoutine(in BaseTable Ti, Row Rm, DataRef DPi)
```

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

```
call AddJoinKey(Ti, Keysi, InheritedKeysi, DPi)
```



EMPLO YEE_ID
101

Keys

Employees
0

T_i

0

DP_i

DEPART MENT_ID
FIN

Inherited Keys



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

EMPLO YEE_ID
101

Keys_[i]

Employees
0

T_[i]

0

[DP]_i

DEPART MENT_ID
FIN

Inherited Keys_[i]

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP $_{[k]}$])

locate the entry of $T_{[ik]}$ in JoinPathList

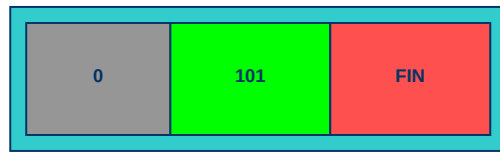
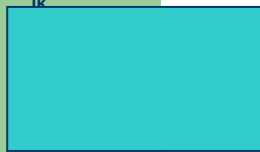
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call AddJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP $_{[ik]}$])

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_0)



addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP $_{[k]}$])

locate the entry of $T_{[ik]}$ in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call AddJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP $_{[ik]}$])

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

0



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

→ from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

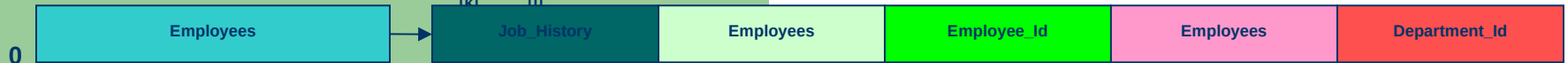
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])



Adjacent Table

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

→ from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

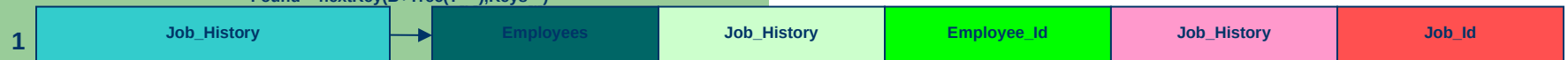
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

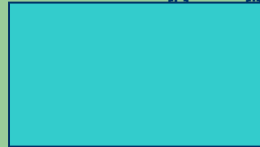
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₁)



Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_i$])

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_i$])

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP $_k$])

locate the entry of $T_{[ik]}$ in JoinPathList

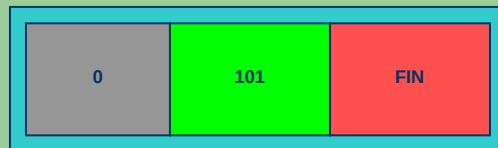
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call AddJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP $_{ik}$])

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_0)



Inserting first row from table Job_History

Base Table

Job_History
1

EMPLOYEE_ID	START_DATE	END_DATE	JOB_ID	DEPARTMENT_ID
101	12/16/1998	12/15/1999	AC_AUD	ACC

→ insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T in JoinPathList
i

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

Base Table

Job_History
1

T_i

	EMPLOYEE_ID	START_DATE	END_DATE	JOB_ID	DEPARTMENT_ID
DP _{i0} ↑ DataRef	101	12/16/1998	12/15/1999	AC_AUD	ACC
	Row R _m				

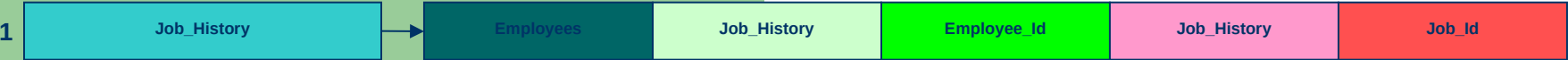
insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



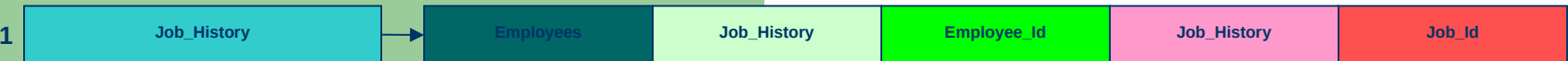
insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



Keys

Inherited Keys

insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

DP _i	Keys		Inherited Keys	
	EMPLOYEE_ID	START_DATE	JOB_ID	DEPARTMENT_ID
0	101	12/16/1998	AC_AUD	ACC

Keys

Row R_m

Inherited Keys

```
insertRoutine(in BaseTable Ti, Row Rm, DataRef DPi)
```

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



EMPLOYEE_ID
101

Keys

Job_History
1

T_i

0

DP_i

JOB_ID
AC_AUD

Inherited Keys



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

EMPLOYEE_ID
101

Keys_[i]

Job_History
1

T_[i]

0

[DP]_i

JOB_ID
AC_AUD

Inherited Keys_[i]

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₁)

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

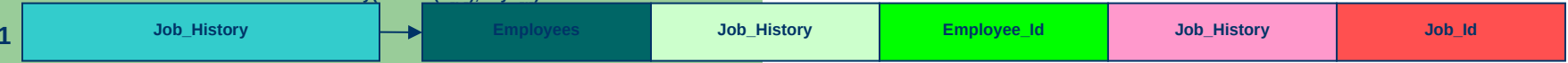
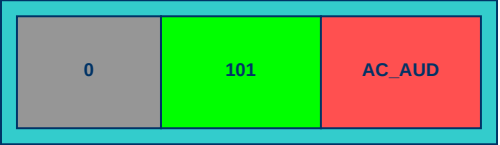
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

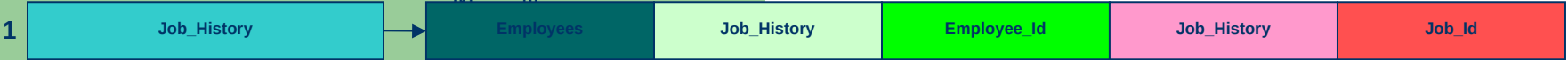
from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

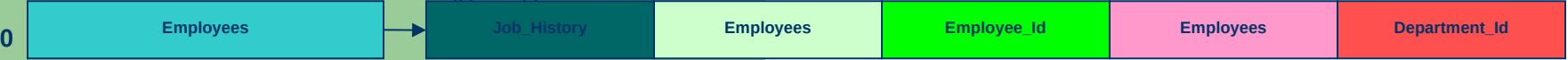


```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call AddJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])
```



Adjacent Table

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call AddJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])
```



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

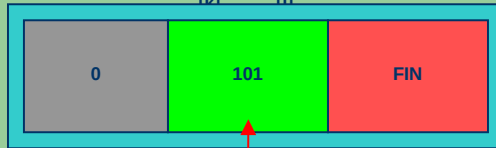
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[ik]), Keys_[i])

B+Tree(T₀)



Found: TRUE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[ik]), Keys_[i])

Found: TRUE

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```

EMPLO
YEE_ID
101

Keys_[k]

0

[DP]_k

DEPART
MENT_ID
FIN

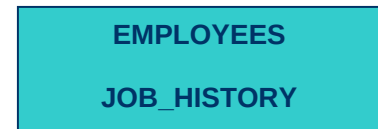
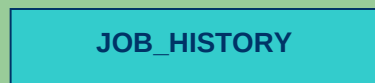
Inherited

Keys_[i]

```

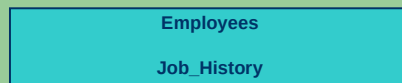
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```



T_{ik}

6



```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList

```

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

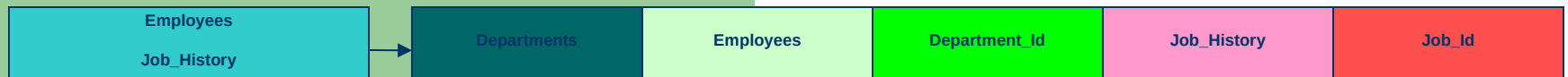
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

6



Keys

Inherited Keys

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do

```

```

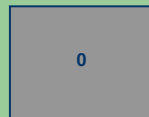
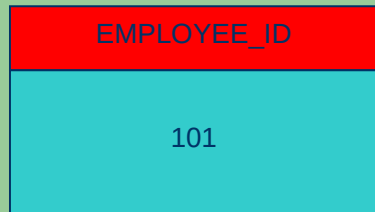
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call AddJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

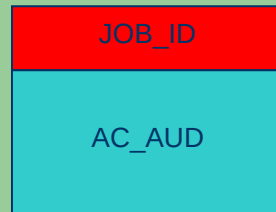


Keys

inherited Keys

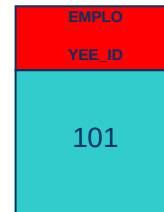


[DP]_i

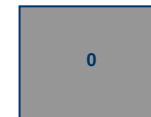


Inherited

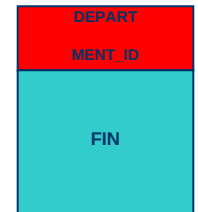
Keys_[i]



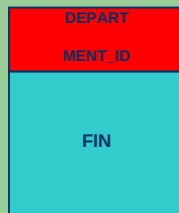
Keys_[k]



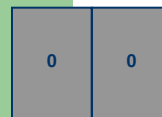
[DP]_k



Inherited Keys_[k]



Keys_[ik]

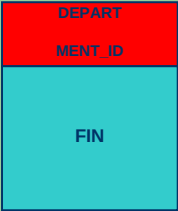


[DP]_{ik}

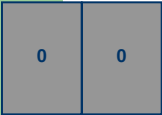


Inherited Keys_[ik]


```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```



Keys_[ik]



[DP]_{ik}



Inherited Keys_[ik]



addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP_i]$)

call addKey($B+Tree(T_{[i]})$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP_i]$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey($B+Tree(T_{[k]})$, Keys $_{[i]}$)

while found do

returnKeys($B+Tree(T_{[k]})$, Keys $_{[k]}$, InheritedKeys $_{[k]}$, $[DP_k]$)

locate the entry of $T_{[ik]}$ in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, $[DP_{ik}]$)

Found = nextKey($B+Tree(T_{[k]})$, Keys $_{[i]}$)

DEPART
MENT_ID
FIN

Keys $_{[i]}$

Employees
Job_History

$T_{[i]}$

0	0
---	---

$[DP_{ik}]$

JOB_ID
AC_AUD

Inherited Keys $_{[ik]}$

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP] $_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

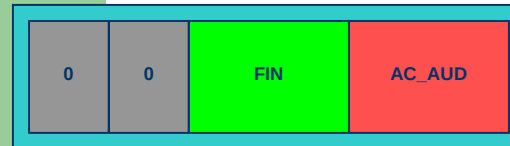
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP] $_{ik}$)

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_6)



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_k])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_k])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[i]), Keys_[i])



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_k])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_k])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[i]), Keys_[i])



Keys

Inherited Keys

Adjacent Table

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₂)



Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

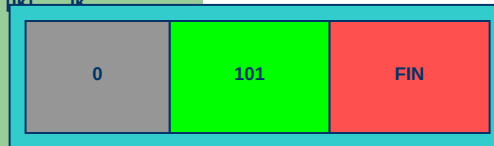
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₀)



Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP $_{[k]}$])

locate the entry of $T_{[ik]}$ in JoinPathList

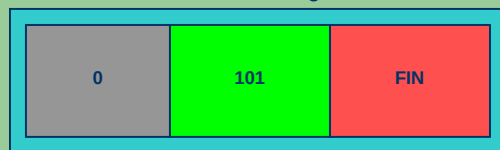
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

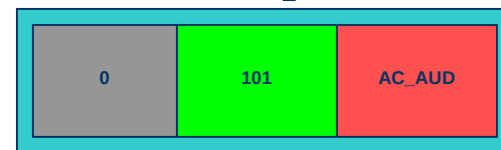
call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP $_{[ik]}$])

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

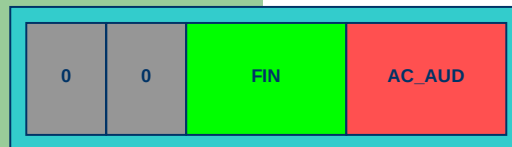
B+Tree(T_0)



B+Tree(T_1)



B+Tree(T_6)



Inserting first row from table Locations

Base Table

Locations
4

LOCATION_ ID	STREET_ADDRESS	POSTAL_ CODE	CITY	STATE PROVINCE	COUNTRY_ ID
1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca

→ insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

Base Table

Locations
4

T_i

LOCATION_ ID	STREET_ADDRESS	POSTAL_ CODE	CITY	STATE PROVINCE	COUNTRY_ ID
1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca

DP_i
0

↑
DataRef

Row R_m

insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

4

Locations

Employees
Job_History
Departments
Jobs

Locations

Location_Id

Locations

Country_Id

insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

4

Locations

Employees
Job_History
Departments
Jobs

Locations

Location_Id

Locations

Country_Id

insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

DP_{i0}

LOCATION_ ID	STREET_ ADDRESS	POSTAL_ CODE	CITY	STATE PROVINCE	COUNTRY_ ID
1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca

Keys

Row R_m

Keys

Keys

Inherited Keys

```
insertRoutine(in BaseTable Ti, Row Rm, DataRef DPi)
```

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i, Keys_i, InheritedKeys_i, DP_i)



LOCATION_ ID
1000

Keys

Locations
4

T_i

0

DP_i

COUNTRY_ ID
ca

Inherited Keys



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

LOCATION_ ID
1000

Keys_[i]

Locations
4

T_[i]

0

[DP]_i

COUNTRY_ ID
ca

Inherited Keys_[i]

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

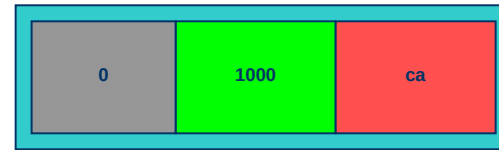
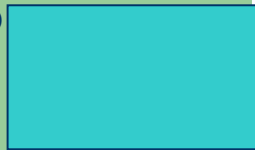
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])



4



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

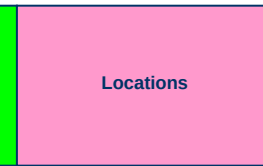
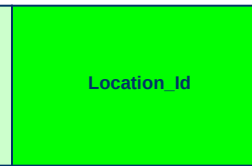
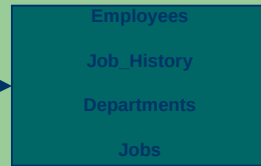
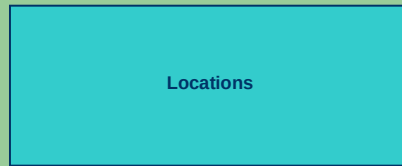
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

4



Adjacent Table

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP $_{[i]}$])

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP $_{[k]}$])

locate the entry of $T_{[ik]}$ in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call AddJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP $_{[ik]}$])

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

8



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₈)

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

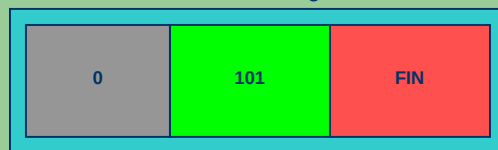
Found: FALSE

```

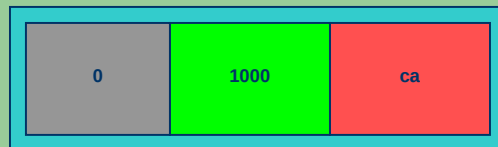
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

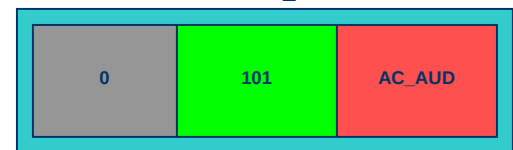
B+Tree(T₀)



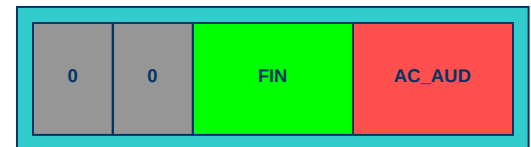
B+Tree(T₄)



B+Tree(T₁)



B+Tree(T₆)



Inserting first row from table Departments

Base Table

DEPARTMENTS
2

Department_Id	Department_Name	Manager_Id	Location_Id
FIN	FINANCE	101	1000

→ insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

Base Table

DEPARTMENTS
2

T_i

DP_i
0

↑
DataRef

Deparment_Id	Department_Name	Manager_Id	Location_Id
FIN	FINANCE	101	1000

Row R_m

insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

2

Departments

Employees

Job_History

Departments

Department_Id

Departments

Location_Id

insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

2

Departments

Employees

Job_History

Departments

Department_Id

Departments

Location_Id

insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

DP_i
0

Department_Id

Department_Name

Manager_Id

Location_Id

FIN

FINANCE

101

1000

Keys

Row R_m

Inherited Keys

Keys

Inherited Keys

```
insertRoutine(in BaseTable Ti, Row Rm, DataRef DPi)
```

locate the entry of T in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i, Keys_i, InheritedKeys_i, DP_i)



Deparment_Id
FIN

Keys

DEPARTMENTS
2

T_i

0

DP_i

Location_Id
1000

Keys



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Deparment_Id
FIN

Keys_[i]

DEPARTMENTS
2

T_[i]

0

[DP]_i

Location_Id
1000

Inherited Keys_[i]

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₂)

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

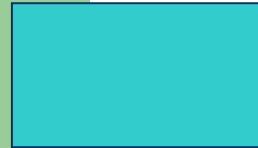
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])



2



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

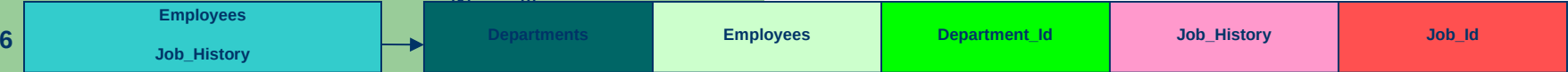
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Adjacent
Table



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

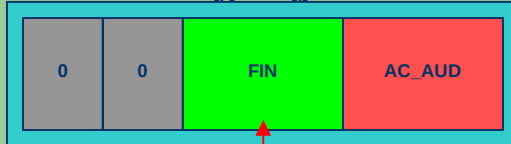
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₆)



Found: TRUE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: TRUE

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
```

```
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```

DEPART
MENT_ID
FIN

Keys_[k]

0	0
---	---

[DP]_k

JOB_ID
AC_AUD

Inherited Keys_[k]

```

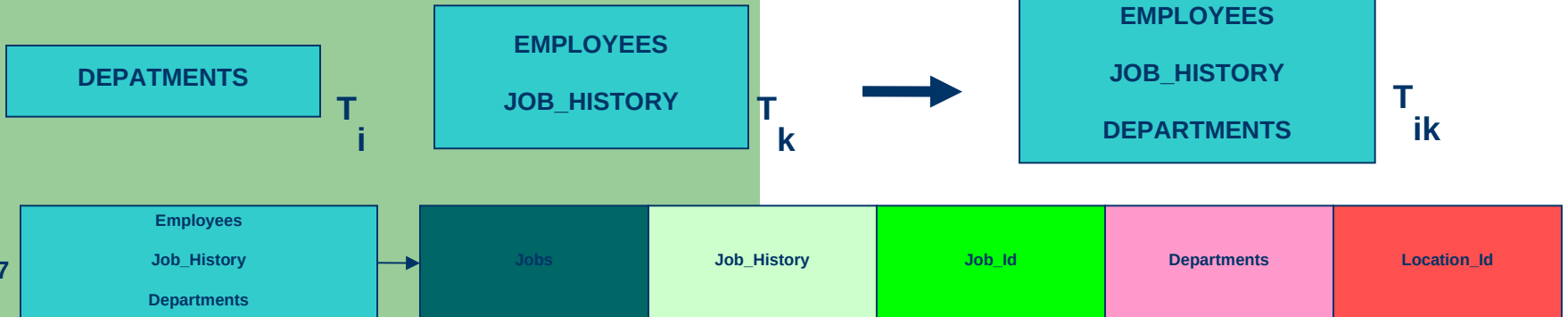
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do

```

```

    returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
    locate the entry of T[ik] in JoinPathList
    from its adjacentList, locate the definition of Keys & Inherited Keys
    from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
    call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
    Found = nextKey(B+Tree(T[k]), Keys[i])

```



addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP])

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP])

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP])

locate the entry of $T_{[ik]}$ in JoinPathList

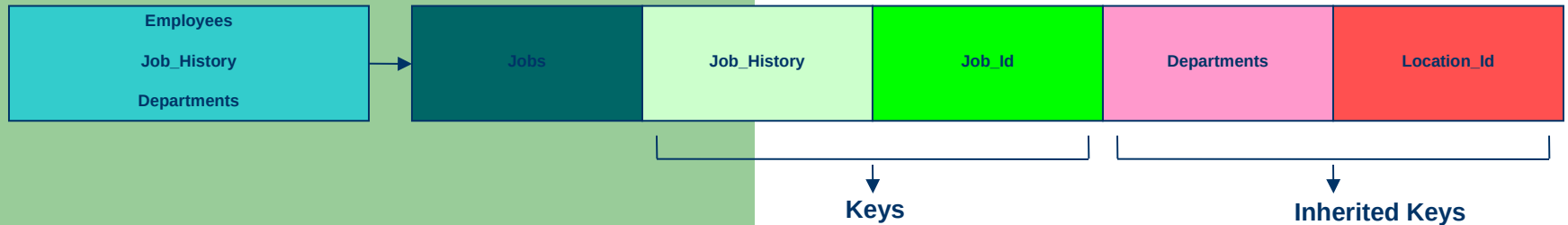
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP])

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

7



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

7

Employees

Job_History

Departments

Jobs

Job_History

Job_Id

Departments

Location_Id

Keys

Inherited Keys

Deparment_Id

FIN

Keys_[i]

[DP]_i

Location_Id

1000

Inherited

Keys_[i]

DEPART
MENT_ID

FIN

Keys_[k]

0

0

[DP]_k

JOB_ID

AC_AUD

Inherited Keys_[k]

JOB_ID

AC_AUD

Keys_[ik]

0 0 0

[DP]_{ik}

Location_Id

1000

Inherited Keys_[ik]

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```

EMPLOYEES		
JOB_HISTORY		
DEPARTMENTS		

T_{ik}

JOB_ID
AC_AUD

Keys_{[ik]c}

0	0	0
---	---	---

[DP]_{ik}

Location_Id
1000

Inherited Keys_[i]



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

JOB_ID
AC_AUD

Keys_[i]

EMPLOYEES
JOB_HISTORY
DEPARTMENTS

T_[i]

0	0	0
---	---	---

[DP]_i

Location_Id
1000

Inherited Keys_[i]

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP] $_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

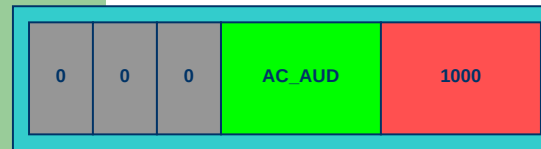
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP] $_{ik}$)

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_7)



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

7



Keys

Inherited Keys

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

7



Adjacent Table

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it

```

```

    locate the entry of T[k] in JoinPathList
    Found = findKey(B+Tree(T[k]), Keys[i])

```

```

    while found do

```

```

        returnKeys(B+Tree(T[k], Keys[k], InheritedKeys[k], [DPk])

```

```

        locate the entry of T[ik] in JoinPathList

```

```

        from its adjacentList, locate the definition of Keys & Inherited Keys

```

```

        from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]

```

```

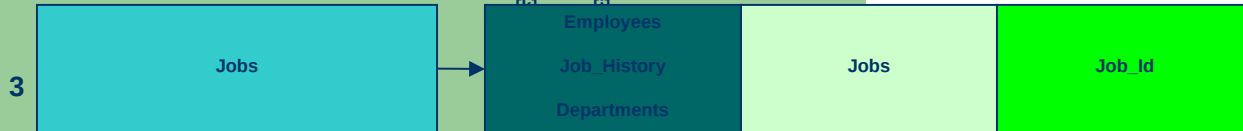
        call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])

```

```

        Found = nextKey(B+Tree(T[k]), Keys[i])

```



```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it

```

```

    locate the entry of T[k] in JoinPathList
    Found = findKey(B+Tree(T[k]), Keys[i])

```

```

    while found do

```

```

        returnKeys(B+Tree(T[k], Keys[k], InheritedKeys[k], [DPk])

```

```

        locate the entry of T[ik] in JoinPathList

```

```

        from its adjacentList, locate the definition of Keys & Inherited Keys

```

```

        from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]

```

```

        call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])

```

```

        Found = nextKey(B+Tree(T[k]), Keys[i])

```

B+Tree(T₃)



Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys

```

```

            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

B+Tree(T₆)



Found: FALSE

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys

```

```

            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

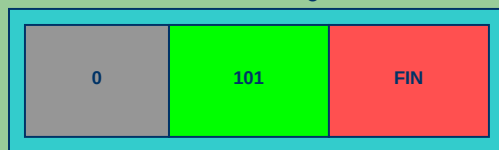
Found: FALSE

```

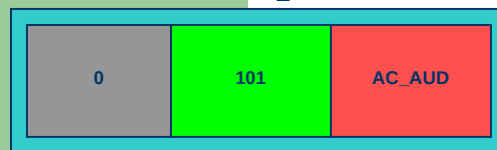
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

B+Tree(T₀)



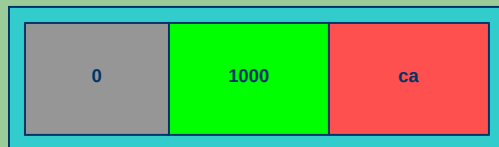
B+Tree(T₁)



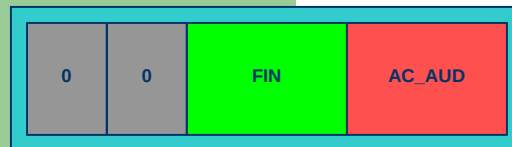
B+Tree(T₂)



B+Tree(T₄)



B+Tree(T₆)



B+Tree(T₇)



Inserting first row from table Jobs

Base Table

JOB_ID
3

JOB_ID	JOB_TITLE	MIN_SALARY	MAX_SALARY
AC_AUD	Accounting Auditor	30000	60000

→ insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

Base Table

JOBS
3

T_i

DP _i	JOBS	JOBS	JOBS	JOBS
0	AC_AUD	Accounting Auditor	30000	60000

DataRef

Row R_m

insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

3

Jobs



Employees
Job_History
Departments

Jobs

Job_Id

insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

3

Jobs



Employees
Job_History
Departments

Jobs

Job_Id

insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

DP_{i0}

JOB_ID	JOB_TITLE	MIN_SALARY	MAX_SALARY
AC_AUD	Accounting Auditor	30000	60000

Keys

Row R_m

Keys

Inherited Keys

```
insertRoutine(in BaseTable Ti, Row Rm, DataRef DPi)
```

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

```
call AddJoinKey(Ti, Keysi, InheritedKeysi, DPi)
```



JOB_ID
AC_AUD

Keys

JOBS
3

T_i

0

DP_i



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

JOB_ID
AC_AUD

Keys_[i]

JOBS
3

T_[i]

0

[DP]_i

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

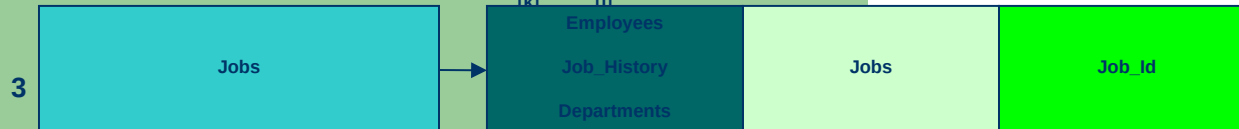
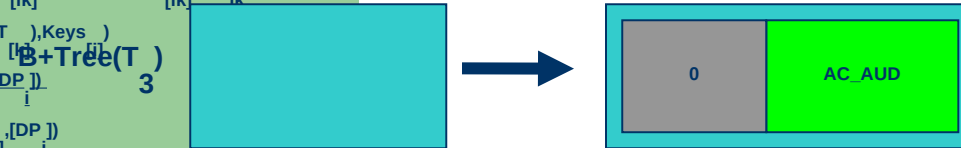
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

3

Jobs



Employees		
Job_History		
Departments		

Adjacent Table

7

Employees
Job_History
Departments



Jobs	Job_History	Job_Id	Departments	Location_Id
------	-------------	--------	-------------	-------------

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

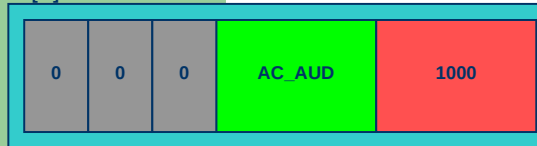
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₇)



Found: TRUE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

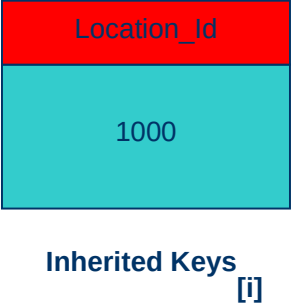
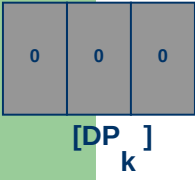
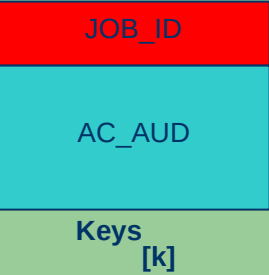
from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: TRUE

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])
```




```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do

```

```

            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

JOBS

T_i

EMPLOYEES
JOB_HISTORY
DEPARTMENTS

T_k



EMPLOYEES
JOB_HISTORY
DEPARTMENTS
JOBS

T_{ik}

8

Employees
Job_History
Departments
Jobs



Locations

Departments

Location_Id

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

8



Keys

Inherited Keys

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do

```

```

    returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)

```

```

    locate the entry of T[ik] in JoinPathList

```

```

    from its adjacentList, locate the definition of Keys & Inherited Keys

```

```

    from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]

```

```

    call AddJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)

```

```

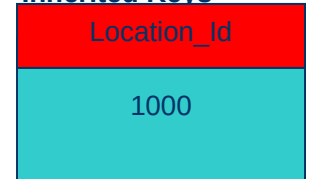
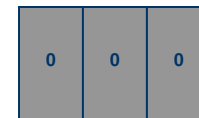
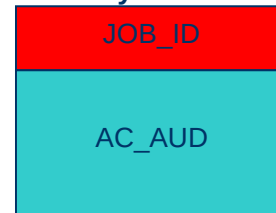
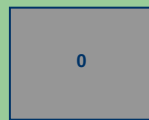
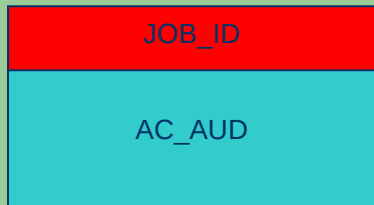
    Found = nextKey(B+Tree(T[k]), Keys[i])

```



Keys

Inherited Keys



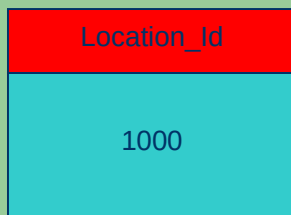
Keys_[i]

[DP]_i

Keys_[k]

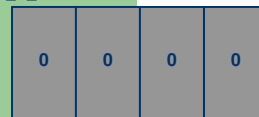
[DP]_k

Inherited Keys_[k]



Keys_[ik]

Inherited
Keys_[i]



[DP]_{ik}

Inherited Keys_[ik]

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])
```

Location_Id
1000

Keys_[ik]

EMPLOYEES
JOB_HISTORY
DEPARTMENTS
JOBS

T_{ik}

0	0	0	0
---	---	---	---

[DP_{ik}]
ik

Inherited Keys_[ik]



addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP]_i$)

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP]_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, $[DP]_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, $[DP]_{ik}$)

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

Location_Id
1000

Keys $_{[i]}$

EMPLOYEES
JOB_HISTORY
DEPARTMENTS
JOBS

$T_{[i]}$

0	0	0	0
---	---	---	---

$[DP]_i$

Inherited Keys $_{[i]}$

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP] $_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

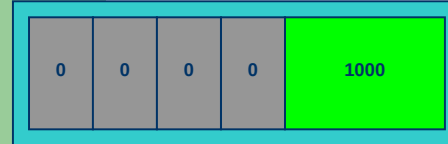
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP] $_{ik}$)

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_8)



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

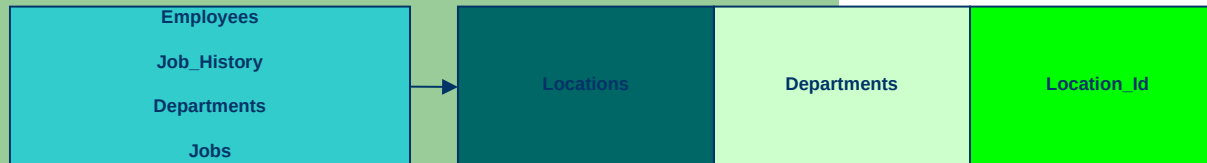
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

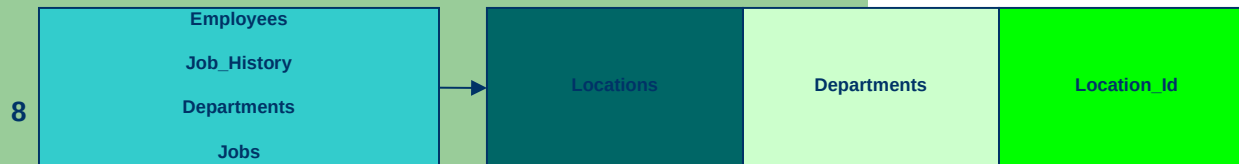
8



```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```



Adjacent
Table

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

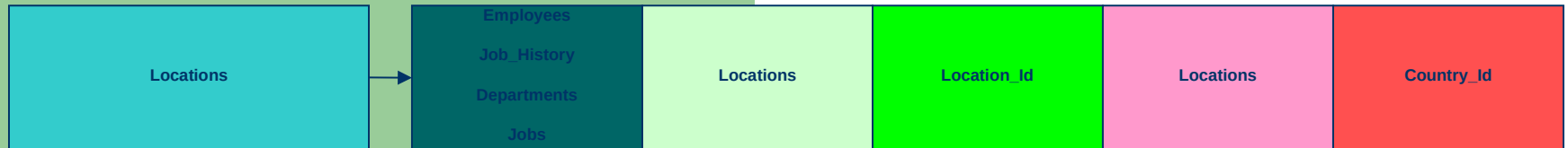
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

4



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

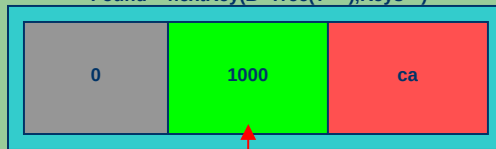
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₄)



Found: TRUE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: TRUE

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
```

```
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```

LOCATION_ ID
1000

Keys_[k]

0

[DP]_k

COUNTRY_ ID
ca

Inherited Keys_[i]

```

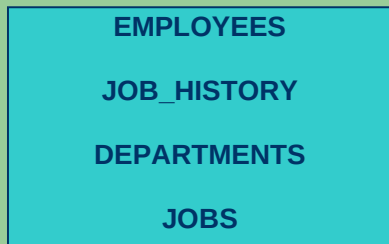
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do

```

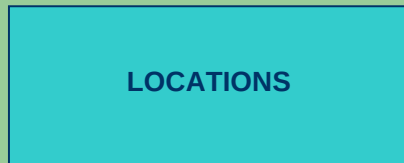
```

    returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
    locate the entry of T[ik] in JoinPathList
    from its adjacentList, locate the definition of Keys & Inherited Keys
    from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
    call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
    Found = nextKey(B+Tree(T[k]), Keys[i])

```



T_i

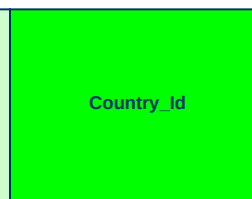
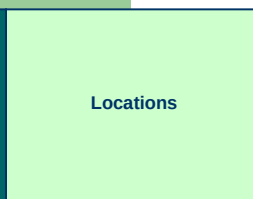


T_k



T_{ik}

9



addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP]_i$)

call addKey($B+Tree(T_{[i]})$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP]_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey($B+Tree(T_{[k]})$, Keys $_{[i]}$)

while found do

returnKeys($B+Tree(T_{[k]})$, Keys $_{[k]}$, InheritedKeys $_{[k]}$, $[DP]_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

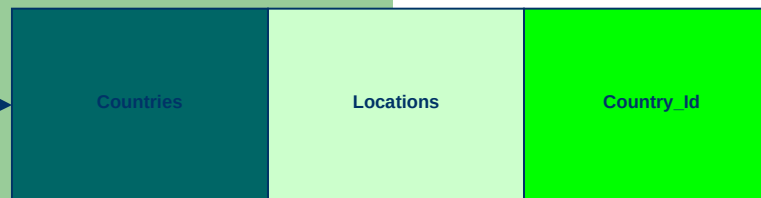
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, $[DP]_{ik}$)

Found = nextKey($B+Tree(T_{[k]})$, Keys $_{[i]}$)

9



Keys

Inherited Keys

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

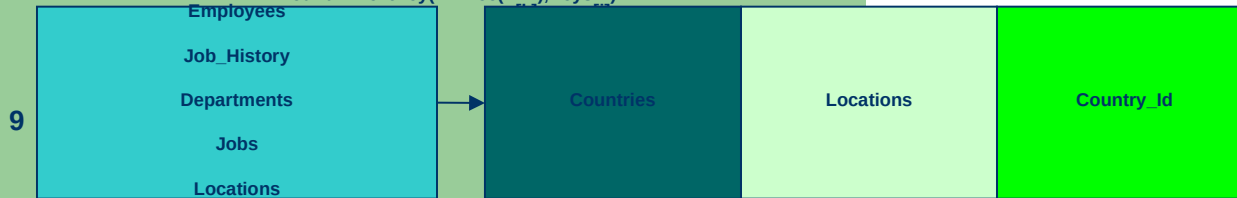
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

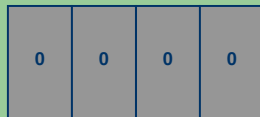
from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

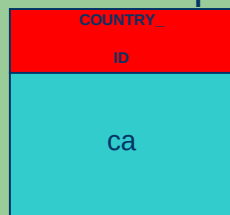
Found = nextKey(B+Tree(T_[k]), Keys_[i])



Keys_[i]

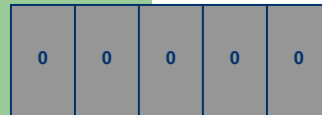


[DP]_i

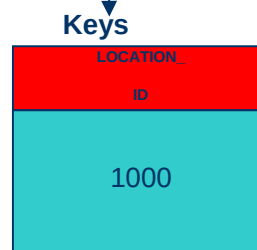


Keys_[ik]

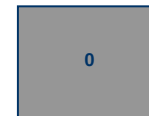
Inherited Keys_[i]



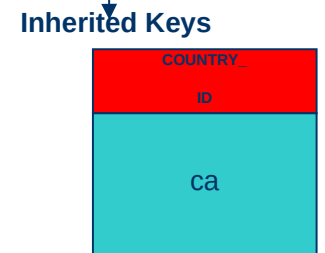
[DP]_{ik}



Keys_[k]



[DP]_k



Inherited Keys_[k]

Inherited Keys_[ik]

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
```

```
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```

COUNTRY_ ID
ca

Keys_[ik]

0	0	0	0	0
---	---	---	---	---

[DP]_{ik}

EMPLOYEES
JOB_HISTORY
DEPARTMENTS
JOBS
LOCATIONS

T_{ik}

Inherited Keys_[ik]

→ addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

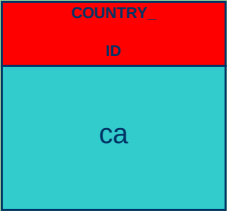
locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

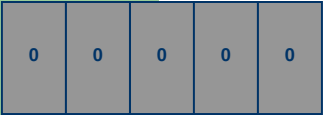
from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])



Keys_[i]



[DP]_i



T_[i]

Inherited Keys_[i]

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP] $_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

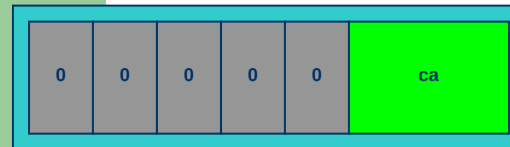
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP] $_{ik}$)

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_9)



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

9

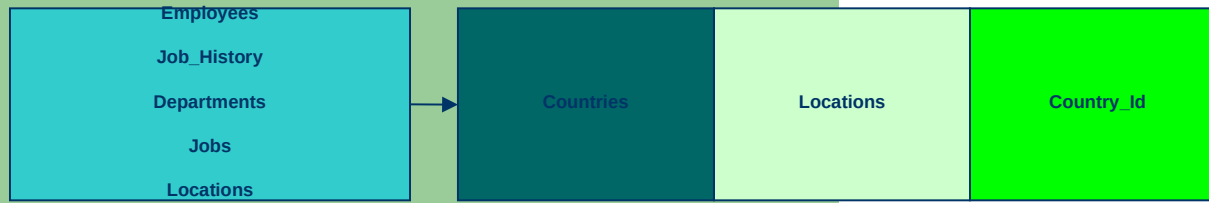


```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

9



Adjacent Table

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[i]), Keys_[i])

5

Countries

Employees

Job_History

Departments

Jobs

Locations

Countries

Country_Id

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[i]), Keys_[i])

B+Tree(T₅)

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

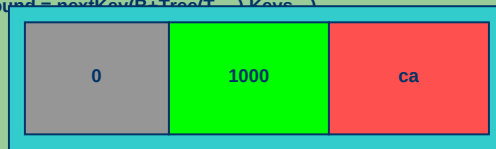
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₄)



Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₇)

0	0	0	AC_AUD	1000
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Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

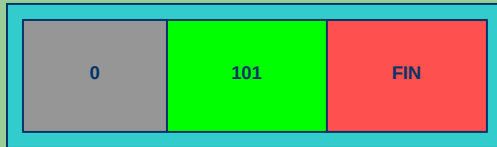
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

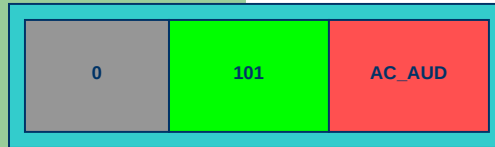
call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₀)



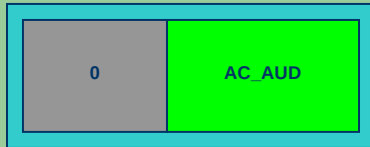
B+Tree(T₁)



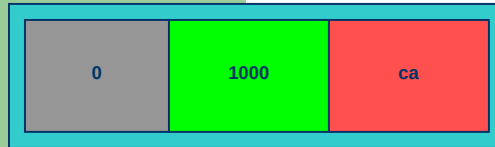
B+Tree(T₂)



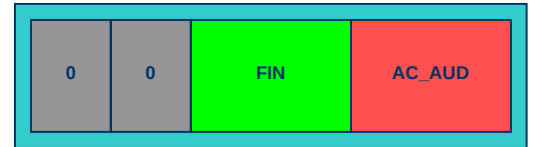
B+Tree(T₃)



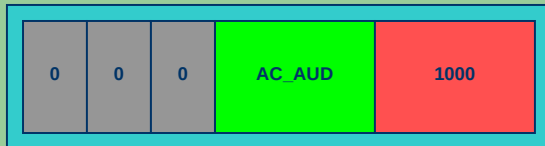
B+Tree(T₄)



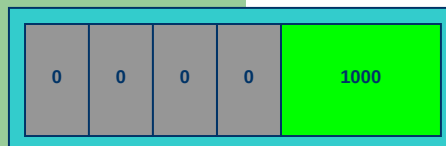
B+Tree(T₆)



B+Tree(T₇)



B+Tree(T₈)



B+Tree(T₉)



Inserting first row from table Countries

Base Table

COUNTRIES
5

Country_Id	Country_Name
ca	Canada

→ insertRoutine(in BaseTable T_i , Row R_m , DataRef DP_i)

locate the entry of T in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i , Keys $_i$, InheritedKeys $_i$, DP_i)

Base Table

COUNTRIES
5

T_i

DP_i
0



DataRef

Country_Id	Country_Name
ca	Canada

Row R_m

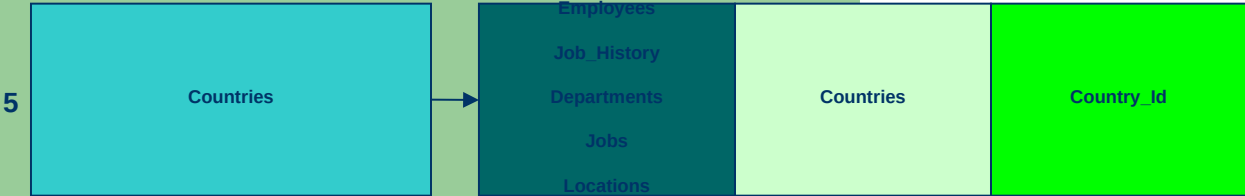
insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



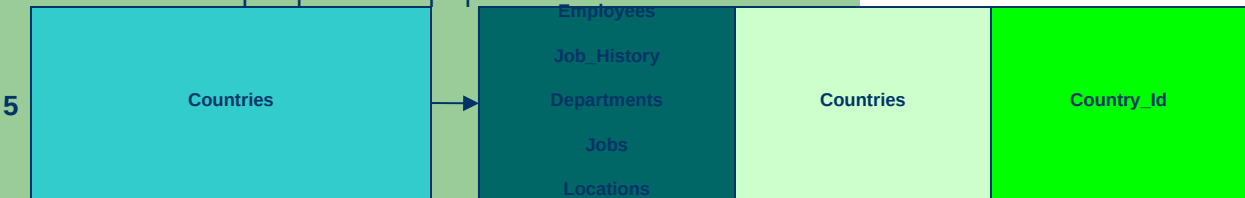
insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)



insertRoutine(in BaseTable T_i, Row R_m, DataRef DP_i)

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i,Keys_i,InheritedKeys_i,DP_i)

Country_Id		Country_Name	
ca		Canada	

Keys

Inherited Keys

Keys

Row R_m

```
insertRoutine(in BaseTable Ti, Row Rm, DataRef DPi)
```

locate the entry of T_i in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from row R_m get the columns constituting the keys & Inherited Keys

call AddJoinKey(T_i, Keys_i, InheritedKeys_i, DP_i)



Country_Id
ca

Keys

COUNTRIES
5

T_i

0

DP_i

Inherited Keys



addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP]_i$)

call addKey($B+Tree(T_{[i]})$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, $[DP]_i$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey($B+Tree(T_{[k]})$, Keys $_{[i]}$)

while found do

returnKeys($B+Tree(T_{[k]})$, Keys $_{[k]}$, InheritedKeys $_{[k]}$, $[DP]_k$)

locate the entry of $T_{[ik]}$ in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call AddJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, $[DP]_{ik}$)

Found = nextKey($B+Tree(T_{[k]})$, Keys $_{[i]}$)

COUNTRIES
5

$T_{[i]}$

Country_Id
ca

Keys $_{[i]}$

0

$[DP]_i$

Inherited Keys $_{[i]}$

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

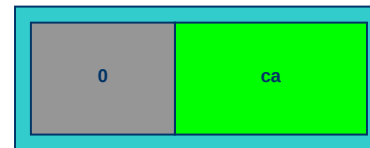
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

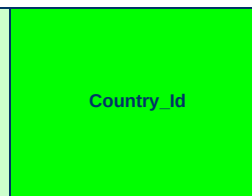
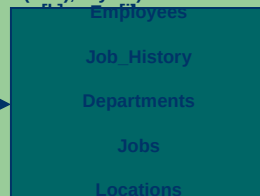
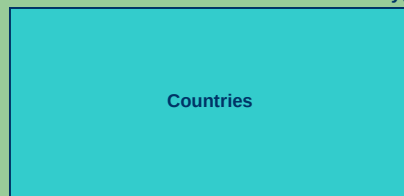
call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

B+Tree(T₅)



5



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

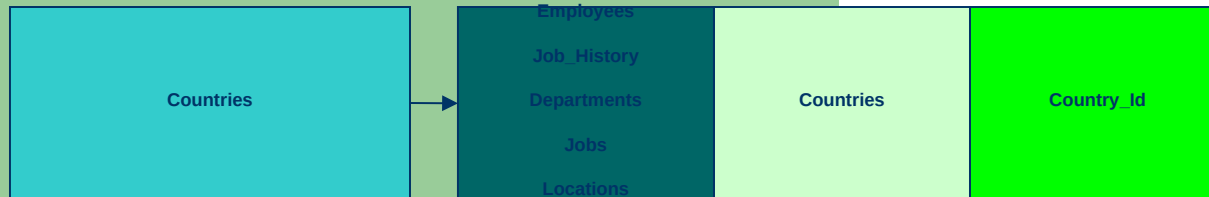
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

5



Adjacent Table

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

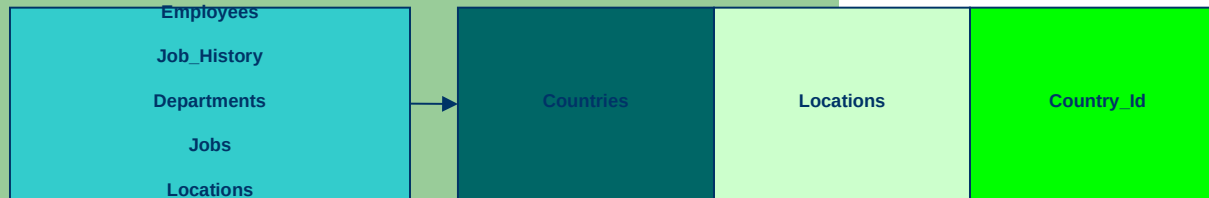
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

9

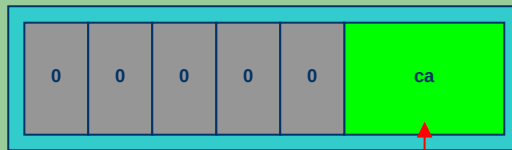


```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call AddJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

B+Tree(T₉)



Found: TRUE

```

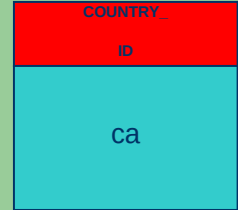
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call AddJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

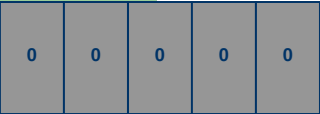
Found: TRUE

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
```

```
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])
```



Keys_[k]



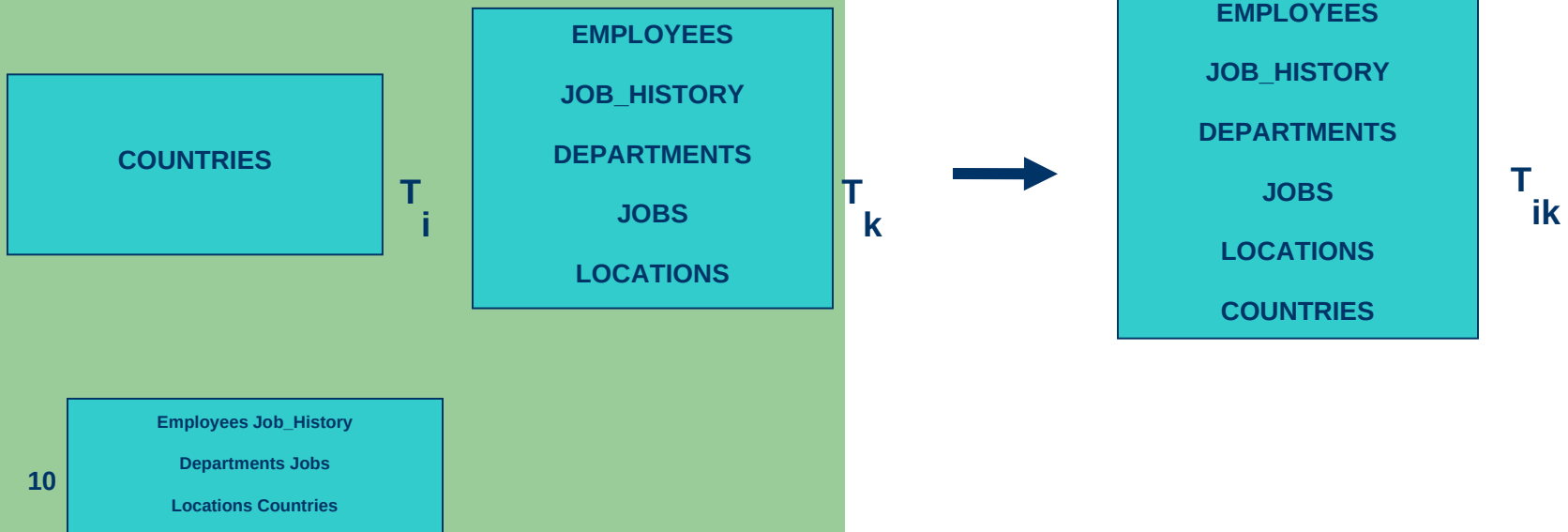
[DP_k]

Inherited Keys_[i]

```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```



```

addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DPi])
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DPi])
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DPk])
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DPik])
            Found = nextKey(B+Tree(T[k]), Keys[i])

```

Employees Job_History

Departments Jobs

Locations Countries

10

Keys

Inherited Keys

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call AddJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

10

Employees Job_History

Departments Jobs

Locations Countries

Keys

Inherited Keys

Country_Id

ca

0

[DP]_i

Inherited

Keys_[i]

COUNTRY_

ID

ca

Keys_[k]

[DP]_k

Inherited Keys_[k]

0	0	0	0	0
---	---	---	---	---

0	0	0	0	0	0
---	---	---	---	---	---

Keys_[ik]

[DP]_{ik}

Inherited Keys_[ik]

```
addJoinKey(in Virtual Table T[i], Keys[i], InheritedKeys[i], [DP]i)
    call addKey(B+Tree(T[i]), Keys[i], InheritedKeys[i], [DP]i)
    locate the entry of T[i] in JoinPathList
    from its adjacentList, locate the table T[k] adjacent to it
        locate the entry of T[k] in JoinPathList
        Found = findKey(B+Tree(T[k]), Keys[i])
        while found do
            returnKeys(B+Tree(T[k]), Keys[k], InheritedKeys[k], [DP]k)
            locate the entry of T[ik] in JoinPathList
            from its adjacentList, locate the definition of Keys & Inherited Keys
            from keys[i], InheritedKeys[i], Keys[k] & InheritedKeys[k] get the keys & Inherited keys of T[ik]
            call addJoinKey(T[ik], Keys[ik], InheritedKeys[ik], [DP]ik)
            Found = nextKey(B+Tree(T[k]), Keys[i])
```



T_{ik}

0	0	0	0	0	0
---	---	---	---	---	---

Keys_[ik]

[DP]_{ik}

Inherited Keys_[ik]

→ addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

EMPLOYEES

JOB_HISTORY

DEPARTMENTS

JOBS

LOCATIONS

COUNTRIES

T_[i]

0	0	0	0	0	0
---	---	---	---	---	---

Keys_[i]

[DP]_i

Inherited Keys_[i]

addJoinKey(in Virtual Table $T_{[i]}$, Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_{[i]}$)

call addKey(B+Tree($T_{[i]}$), Keys $_{[i]}$, InheritedKeys $_{[i]}$, [DP] $_{[i]}$)

locate the entry of $T_{[i]}$ in JoinPathList

from its adjacentList, locate the table $T_{[k]}$ adjacent to it

locate the entry of $T_{[k]}$ in JoinPathList

Found = findKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

while found do

returnKeys(B+Tree($T_{[k]}$), Keys $_{[k]}$, InheritedKeys $_{[k]}$, [DP] $_{[k]}$)

locate the entry of $T_{[ik]}$ in JoinPathList

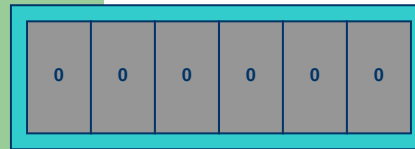
from its adjacentList, locate the definition of Keys & Inherited Keys

from keys $_{[i]}$, InheritedKeys $_{[i]}$, Keys $_{[k]}$ & InheritedKeys $_{[k]}$ get the keys & Inherited keys of $T_{[ik]}$

call addJoinKey($T_{[ik]}$, Keys $_{[ik]}$, InheritedKeys $_{[ik]}$, [DP] $_{[ik]}$)

Found = nextKey(B+Tree($T_{[k]}$), Keys $_{[i]}$)

B+Tree(T_{10})



addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

10

Employees Job_History

Departments Jobs

Locations Countries

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP_i])

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP_k])

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Employees Job_History

Departments Jobs

Locations Countries

Adjacent

Table

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

addJoinKey(in Virtual Table T_[i], Keys_[i], InheritedKeys_[i], [DP]_i)

call addKey(B+Tree(T_[i]), Keys_[i], InheritedKeys_[i], [DP]_i)

locate the entry of T_[i] in JoinPathList

from its adjacentList, locate the table T_[k] adjacent to it

locate the entry of T_[k] in JoinPathList

Found = findKey(B+Tree(T_[k]), Keys_[i])

while found do

returnKeys(B+Tree(T_[k]), Keys_[k], InheritedKeys_[k], [DP]_k)

locate the entry of T_[ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

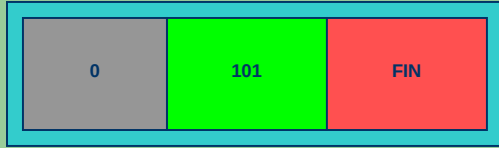
from keys_[i], InheritedKeys_[i], Keys_[k] & InheritedKeys_[k] get the keys & Inherited keys of T_[ik]

call addJoinKey(T_[ik], Keys_[ik], InheritedKeys_[ik], [DP]_{ik})

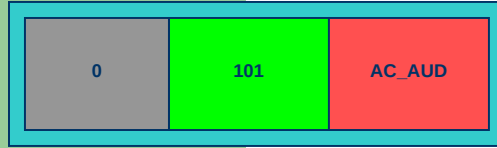
Found = nextKey(B+Tree(T_[k]), Keys_[i])

Found: FALSE

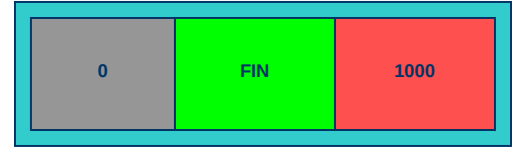
B+Tree(T₀)



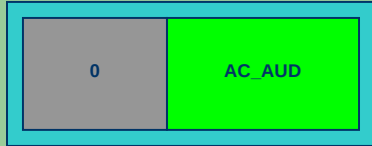
B+Tree(T₁)



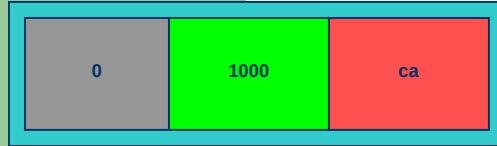
B+Tree(T₂)



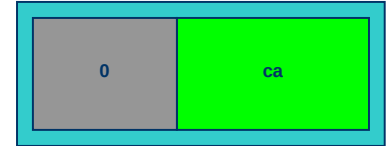
B+Tree(T₃)



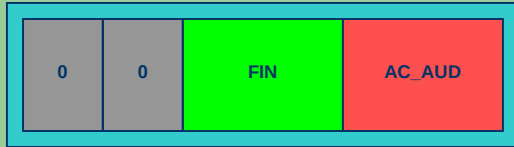
B+Tree(T₄)



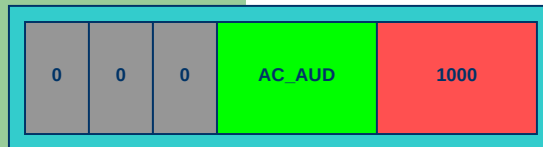
B+Tree(T₅)



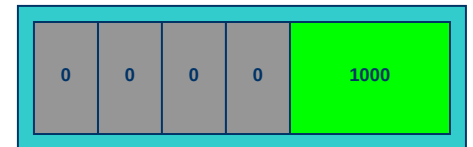
B+Tree(T₆)



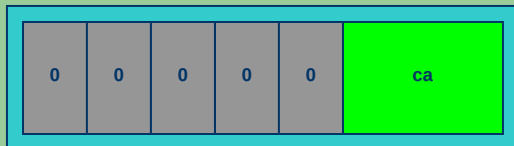
B+Tree(T₇)



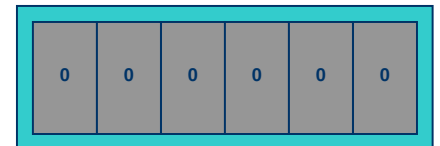
B+Tree(T₈)



B+Tree(T₉)

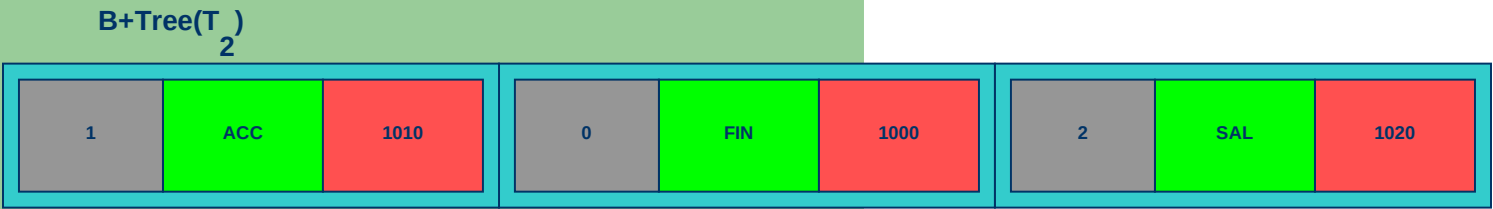
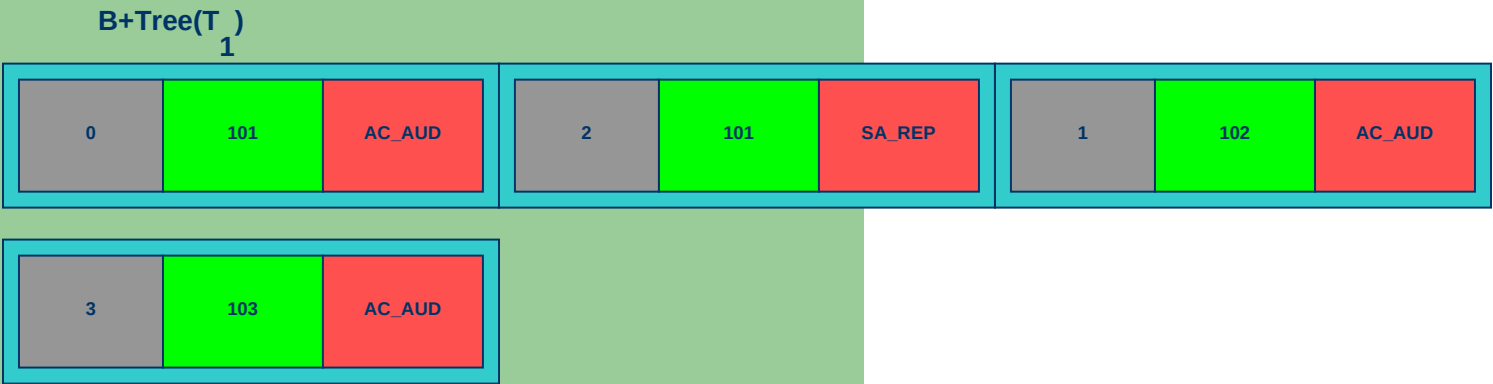
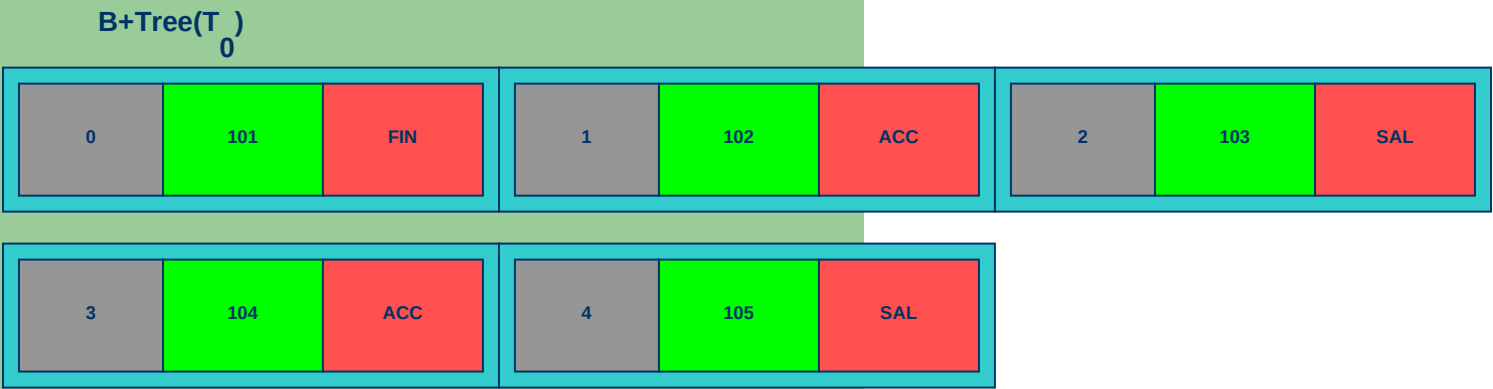


B+Tree(T₁₀)

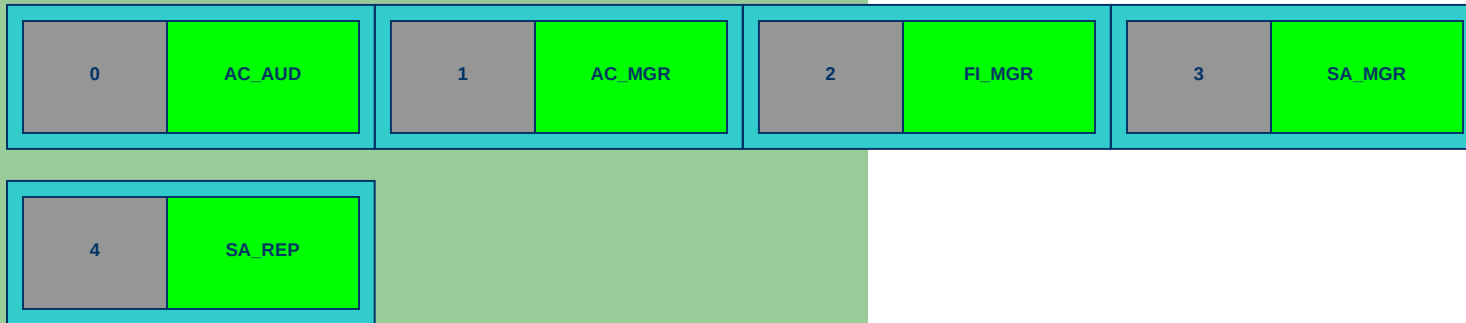


As we can notice from the last index we have an element with 6 data pointers respectively pointing to the 6 base tables forming the virtual table T_{10} , with all values equal to the first row on each table, those rows are in join together.

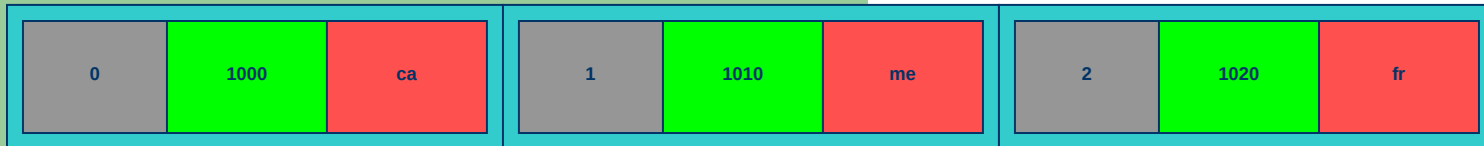
Inserting all the remaining rows from the tables we obtain the following indexes where the last index shows the join between the rows from the tables.



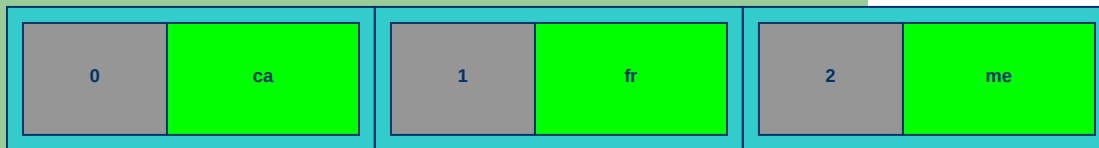
B+Tree(T₃)



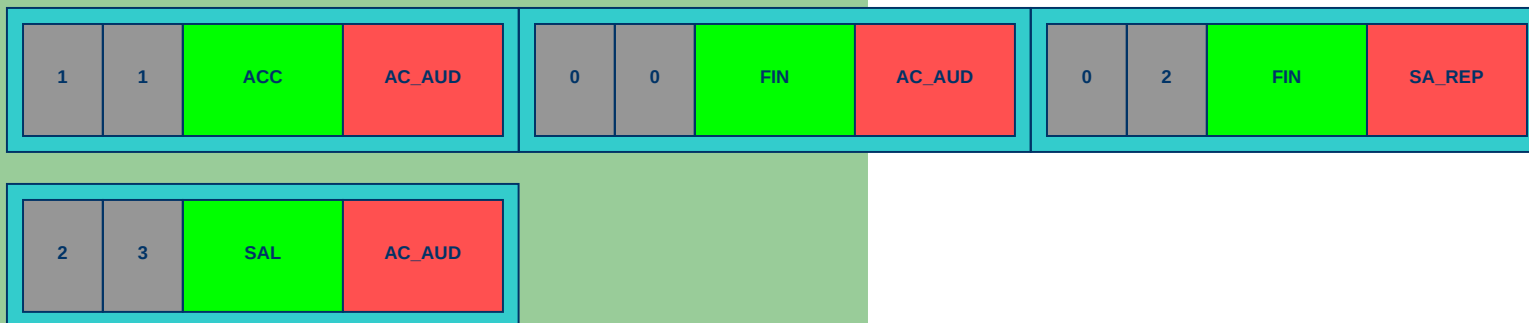
B+Tree(T₄)



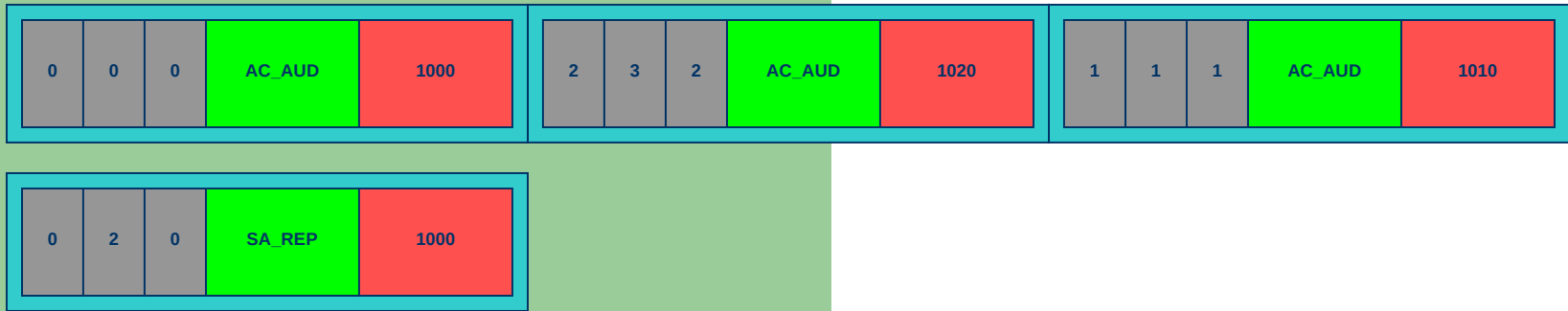
B+Tree(T₅)



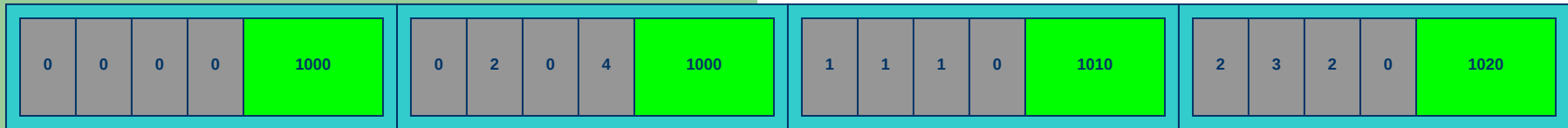
B+Tree(T₆)



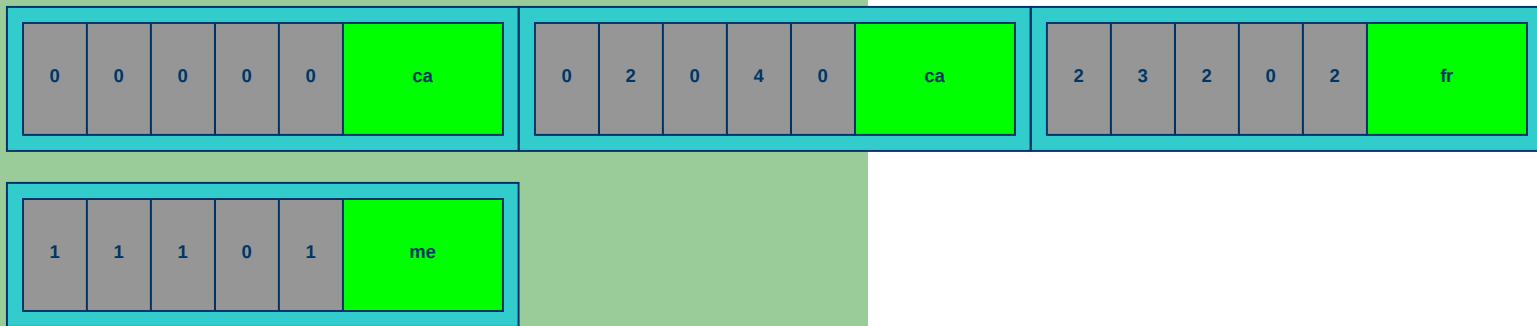
B+Tree(T₇)



B+Tree(T₈)



B+Tree(T₉)



B+Tree(T₁₀)



Delete routine

When a row R_m from table T_i get deleted do the following:

- Locate the entry of T_i in the JoinPathList
- From its adjacent List, locate the definition of the keys and inherited keys
- From Row R_m get the columns constituting the keys and the inherited keys
- Call DelJoinKey (T_i , $Keys_i$, $InheritedKeys_i$, DP_i) where DP_i is the row id of row R_m

Notice that $Keys_i$, $InheritedKeys_i$ and DP_i are relative to the row R_m from table T_i

DelJoinKey ($T_{[i]}$, $Keys_{[i]}$, InheritedKeys $_{[i]}$, $[DP_i]$)

- Call delKey (B+Tree($T_{[i]}$), $keys_{[i]}$, InheritedKeys $_{[i]}$, $[DP_i]$) for the index of table $T_{[i]}$
- Locate the entry of $T_{[i]}$ in the JoinPathList
- From its adjacent List, locate the Table $T_{[k]}$ adjacent to it and do the following:
 - } Locate the entry of $T_{[k]}$ in the JoinPathList
 - } FindKey(B+Tree($T_{[k]}$), $Keys_{[i]}$)
 - } While found($keys_{[i]}$) do
 - ReturnKeys(B+Tree($T_{[k]}$), $keys_{[k]}$, InheritedKeys $_{[k]}$, $[DP_k]$)
 - Locate the entry of $T_{[ik]}$ in the JoinPathList
 - From its adjacent List, locate the definition of the keys and inherited keys
 - From $keys_{[i]}$, inheritedkeys $_{[i]}$, $keys_{[k]}$, inheritedkeys $_{[k]}$ get the keys and inherited keys of $T_{[ik]}$
 - DelJoinKey ($T_{[ik]}$, $Keys_{[ik]}$, InheritedKeys $_{[ik]}$, $[DP_{ik}]$)
 - NextKey(B+Tree($T_{[k]}$), $Keys_{[i]}$)

Complexity of the algorithm for the creation of JoinPathList.

The complexity for the creation of JoinPathList structure is:
 $2*n-1$ where n is the number of tables in join.

Proof:

We can prove it by induction on the number of tables in join.

For $m = 1$:

The complexity should be $2*1-1 = 1$ in fact it is the only table that get inserted in the JoinPathList.

For $m = n-1$:

Suppose that the number of tables in JoinPathList is $2*(n-1)-1$.

For $m = n$:

The n^{th} table get inserted as a Vertex in the JoinPathList at the beginning of the algorithm.
The n^{th} table get inserted in queue and path dynamic arrays because the n tables are in join and at least there is one table in the $(n-1)$ remaining table that is in join with the n^{th} table.

So when the algorithm run at certain point should execute:

$$T_{[\text{buf}]} += T_i$$

$$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$$

where T_i is T_n , so the number of tables in JoinPathList are: $2*(n-1)-1 + 1 + 1 = 2*n-1$

Complexity of the algorithm for the insertion and deletion.

Delete is symmetric to insert in the algorithm in the sense where there is an insert we use a delete, so they have both the same complexity.

When inserting a new row in the database we use the B^{JoinTree} mechanism to drive us in the insert for the join.

Suppose that the order of the B^+ Trees is m and the number of elements for every B^+ Tree with i as index from the $(2^n - 1)$ B^+ Trees is $p_i * l_i$ where in average there is l_i elements satisfying the join between every pair of tables.

In the worst case when get inserted row with the lowest order tables T_0 and T_1 in this case we call recursively the insert procedure for $(2^n - 1) - (n - 1) = n$ times.

The complexity will be:

$$O(n * \log_m(l_i * p_i))$$

Complexity of the algorithm for the other operations.

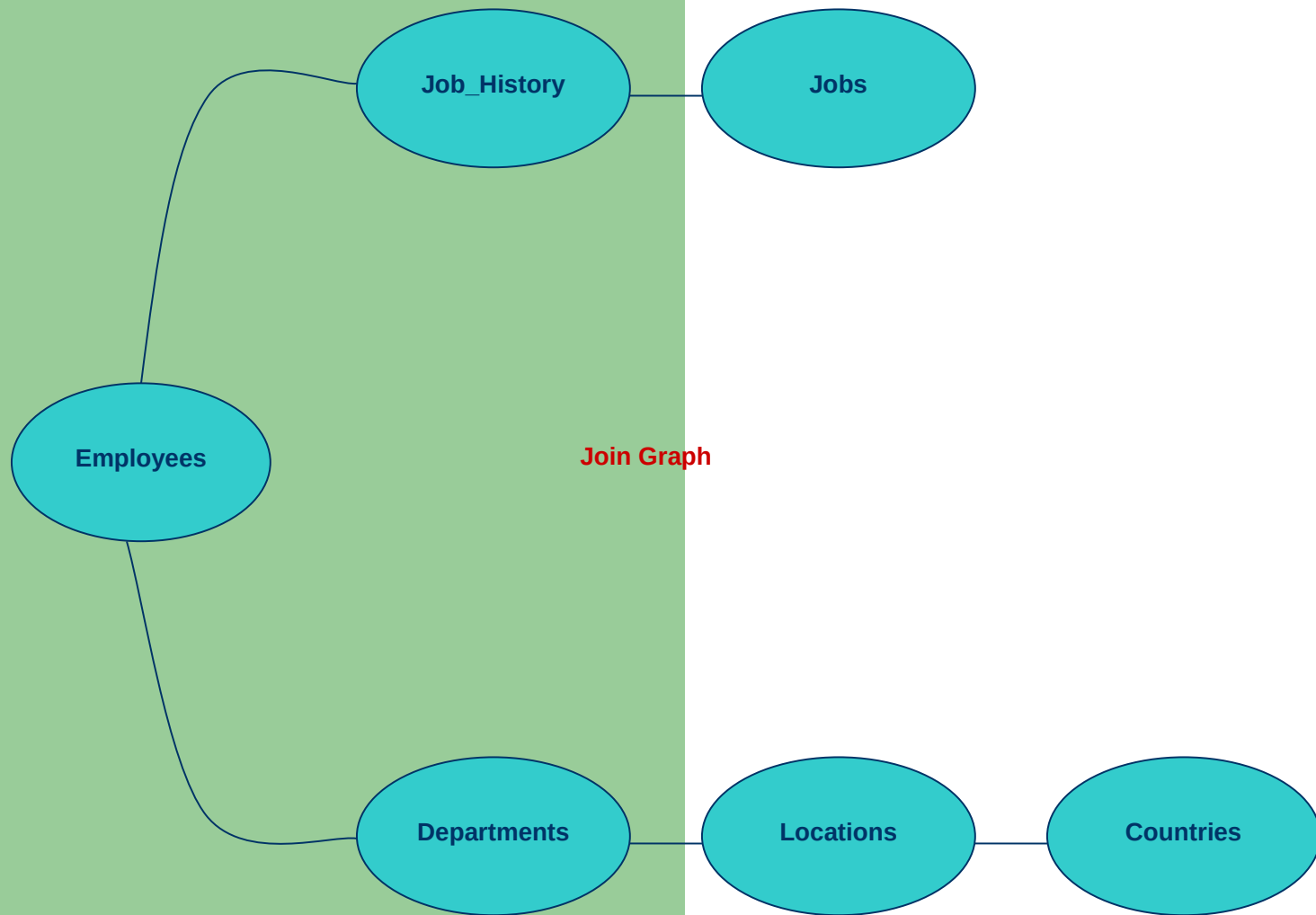
The only B⁺Tree of our interest for the scan is the one with the latest index that have the join of the tables inside it.

Suppose that the number of elements for the latest index is $p_{(2*n-1)}$ so the other operations on this B⁺Tree for find, search, prev, next,... are the same as for normal B⁺Tree.with the same number of elements.

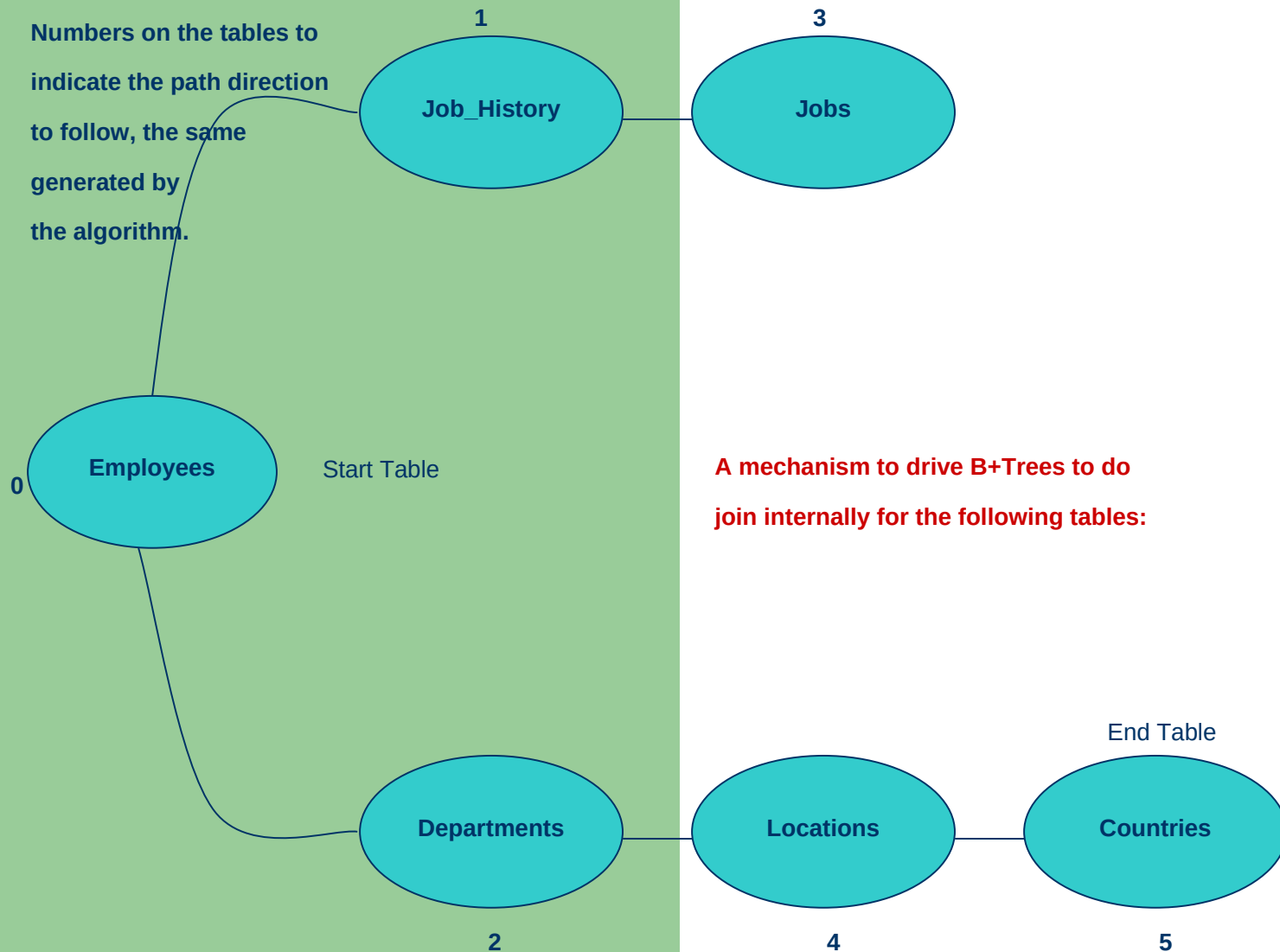
Proof of correctness.

To prove the correctness of the algorithm let see how does the algorithm work for the example above and later generalize it.

The Join Graph could be calculated easily even manually when we know which Tables are in direct join with others.



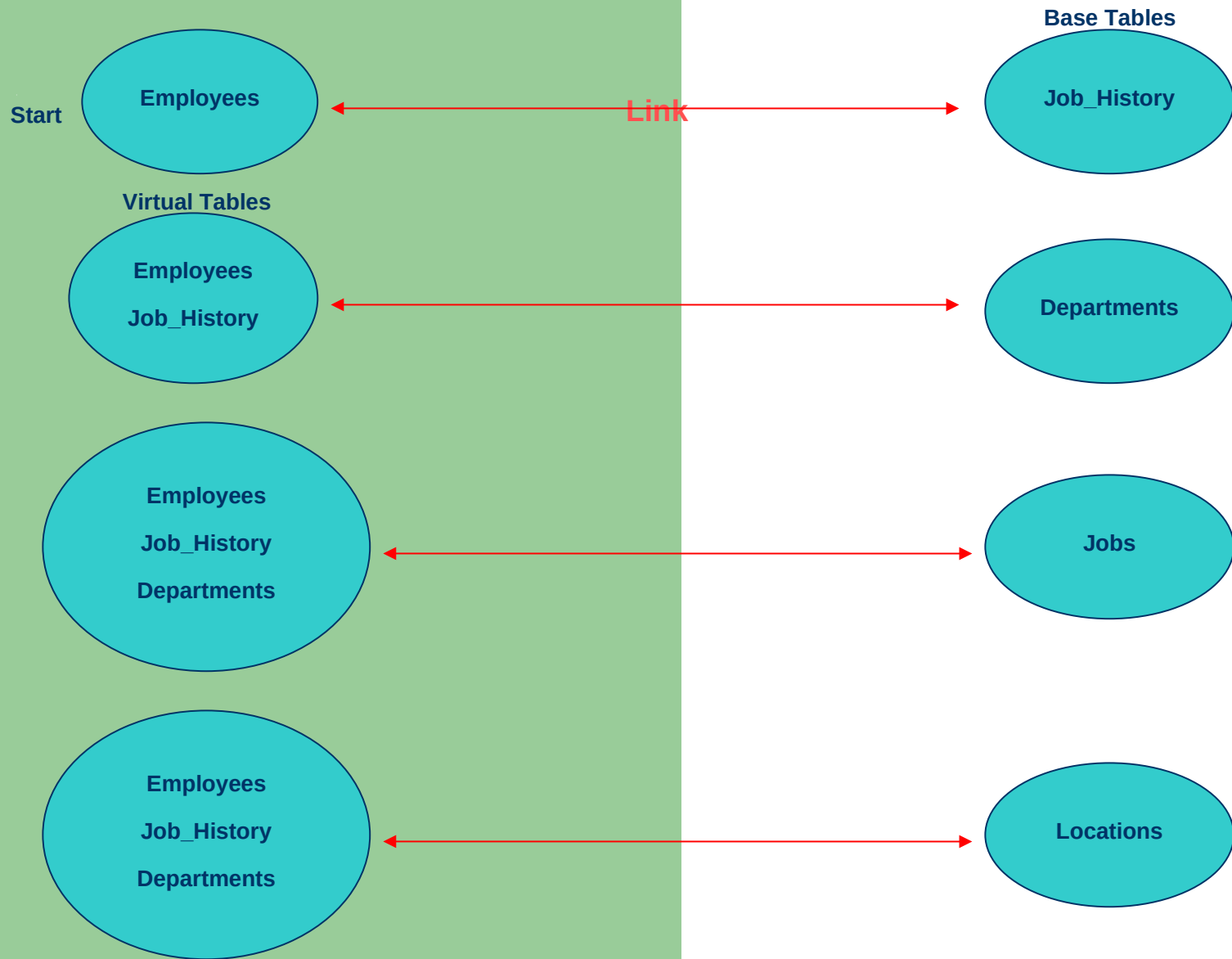
Let define a path in the Join Graph, the same path generated by the algorithm:
generateJoinPathList

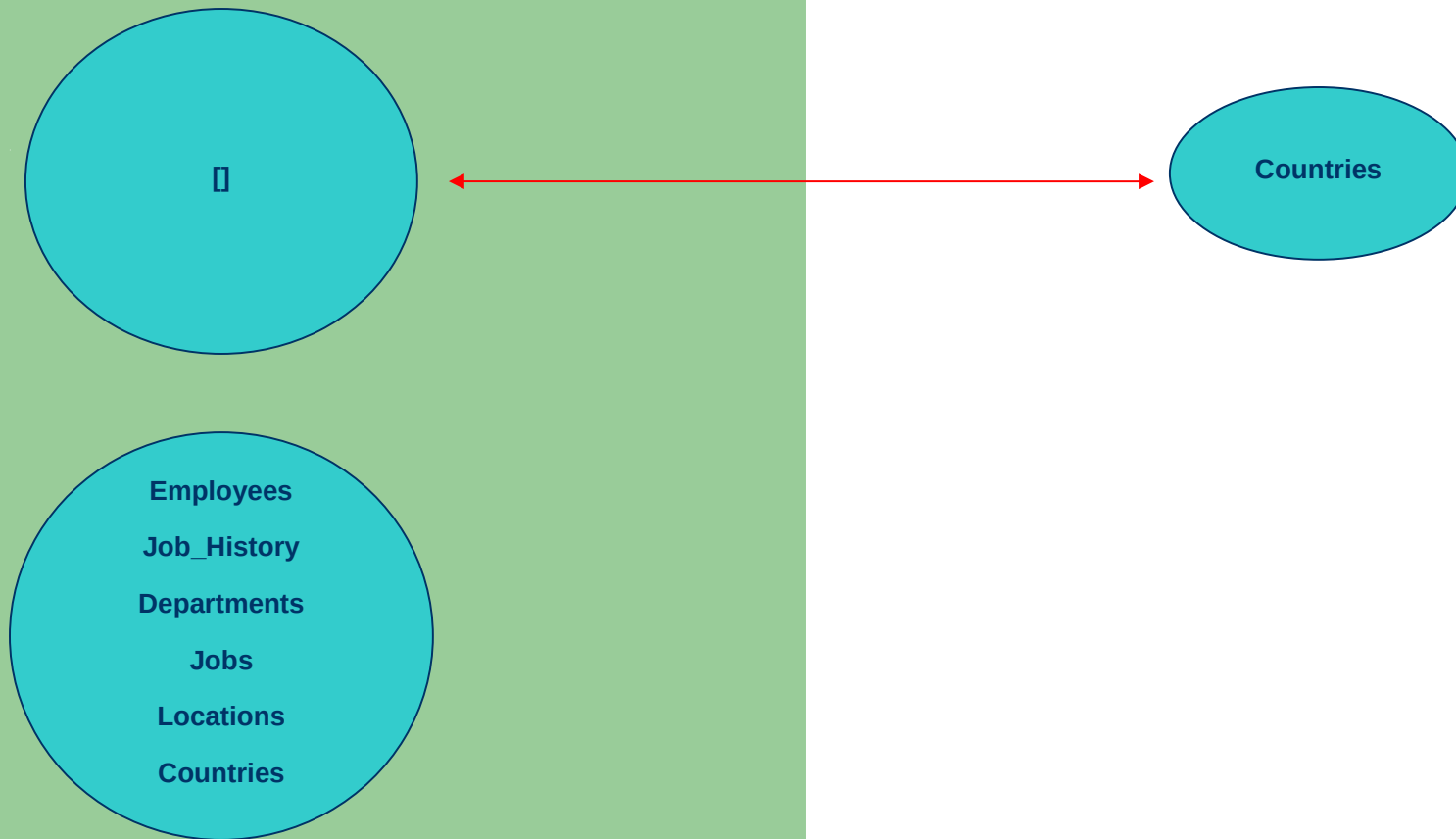


Notice that in the path if we reach one table it is not necessary to continue from it.

This is very important because this makes the tables free from any order,
independent selection of the start and end tables.

By grouping comes out: `





There is no restriction on how the rows from base tables get inserted (Any order with any sequence).

The only restriction is that the Data Pointers are in the same order as the virtual table in Join Path List.

If we insert for example in the B+Tree that belongs to virtual table

T[Employees,Job_History,Departments,Jobs,Locations]

We should insert

DP[Employees,Job_History,Departments,Jobs,Locations]

respectively

As we can see for every Virtual Table there is a Base Table in which there is a direct join between them and vice versa, in fact they belong to the same Path in the Join Graph.

The idea consists in that every Virtual Table is constituted from Base Tables that are joined together. In fact the Base Tables constituting the Virtual Table appear by adding one at a time that is in direct join with the one of the previous tables.

Now the join between tables should be calculated and stored to be found. For this reason B+Tree is declared for every Virtual Table that can hold references for rows from Base Tables constituting the Virtual Table in mode that concatenating them together bring out a joined Row.

Rows are inserted into a database as one row from a base table at a time, the system look for the link table, and check the B+Tree to see if there is any row that satisfy the join with the newly inserted; if this is the case combine each row satisfying with newly inserted by their references, and insert the combined row in the virtual table that has as base tables the base tables of the 2 previously tables.

So at any time when a row get inserted, the link table may eventually have the rows that satisfy the join with it, so they are combined and the process continue to the last virtual table or if they didn't get inserted yet in the virtual table, later when they get inserted they are confronted with the one inserted yet and the process continue on the same way.

The last table will contain all base tables in join together.

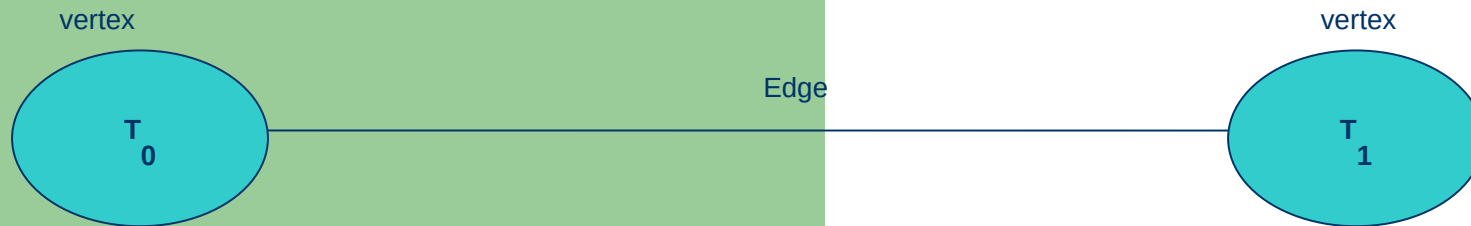
Proof of correctness.

Notice that what we show before is independent from the number of tables, so that the same reasoning apply to any number of tables and the proof of correctness could be easily proved by induction.

Let prove the correctness by induction.

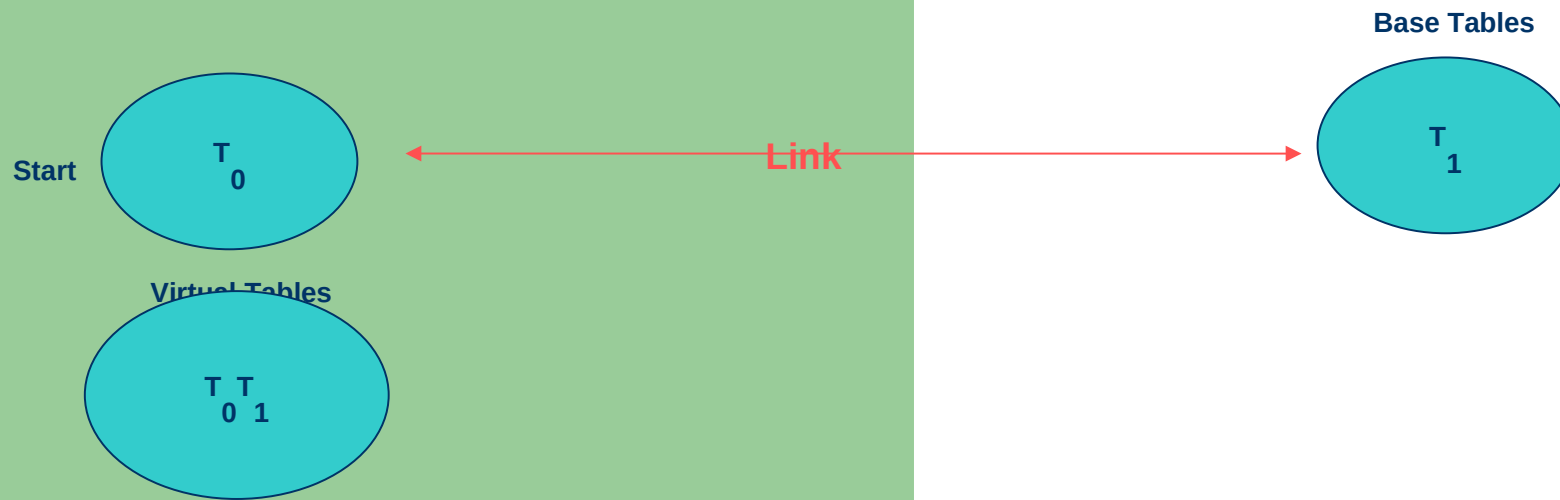
To do it, let see the correctness for 2 tables T_0 and T_1 in join together.

The join graph should be the following:

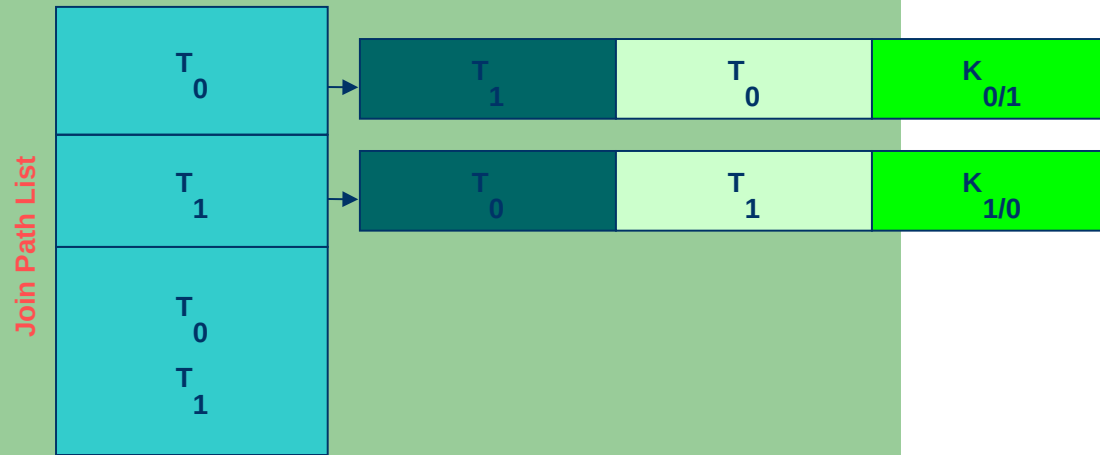


There are just 2 paths between the 2 tables: or from T_0 going toward T_1 or vice versa, let consider the former, the second case is symmetric and after all T_0 and T_1 are of arbitrarily choice.

By grouping comes out:



So, the JoinPathList should be the following:



If any key has been defined on the last virtual table and doesn't exist as a key on the base tables then should be propagated as inherited key in the appropriate base table; but for the prove of correctness in case of 2 tables, it is not important.

To prove the correctness of the algorithm, we have to prove that the last virtual table contain data references to all the rows that combined form the join between the 2 base tables and only those in other sense it is equivalent to the result of the join between the 2 tables.

Let prove that the last virtual table contain data references to all the rows that combined form the join between the 2 base tables:

Suppose by absurd that there is a row $R_{m/0}$ from table T_0 and a row $R_{n/1}$ from table T_1 that are in join together and they don't have references in the last virtual table.

If the 2 rows are in join together so their respective keys satisfy the join condition.

Suppose that $R_{m/0}$ comes first, so $\text{key}(R_{m/0})$ is inserted in the $B+Tree(T_0)$.

When $R_{n/1}$ get inserted later, the insert algorithm look in JoinPathList the adjacent table to T_1 , it finds that T_0 is such table and look in $B+Tree(T_0)$ all the keys that satisfy the join condition with the value of $\text{key}(R_{n/1})$. It will get $\text{key}(R_{m/0})$ because such key satisfy the join condition, it will combine the data references of the 2 Rows and insert in the virtual table such couple of references.

This is in contradiction on what we assume initially.

The case that $R_{n/1}$ comes first is symmetric.

Let prove that the only couples of data references in the last virtual table are those that combined make the join between the 2 base tables:

Suppose by absurd that there is a couple of references DP_0 and DP_1 that are data pointers to rows from table T_0 and table T_1 respectively in the virtual table and that the combined row doesn't belong to a join between the 2 base tables.

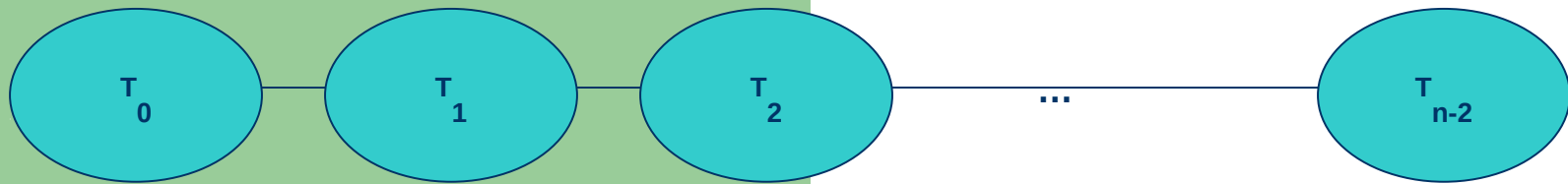
If such a couple of data pointers exist, it comes out because there is 2 keys belonging to the rows pointed by the data pointers and such keys satisfy the join condition, this is in contradiction on what we assume initially.

The initial case when there is only 2 tables in join is proved to be correct. Now let suppose that the correctness is true for $n-1$ tables and let prove it when the number of tables is n tables.

The easiest way to prove it for n tables is to expand the virtual table with $(n-1)$ base tables. This virtual table has a B+Tree that is constituted from set of elements in which every element has a common key value with the n th table and $(n-1)$ data pointers that points to the $(n-1)$ base tables. By expanding in the sense that from every element taking the $(n-1)$ rows from the $(n-1)$ tables and considering them as one row in a virtual table, we can look at the virtual table as a table populated with such rows.

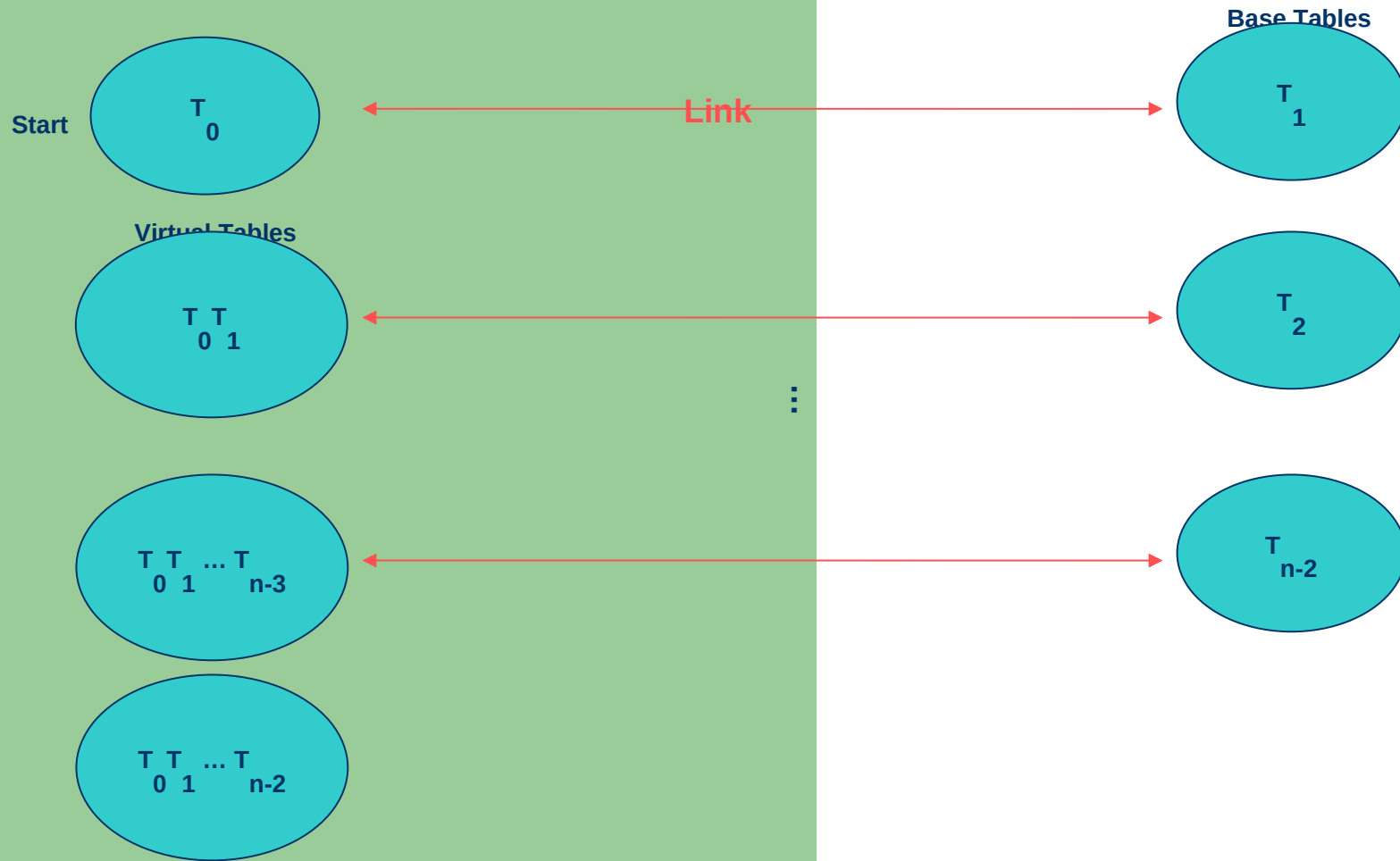
Let see first the Join Graph for the $(n-1)$ tables and how they went in group and later what happens when we consider the n th table.

The join graph for the (n-1) tables should be the following:

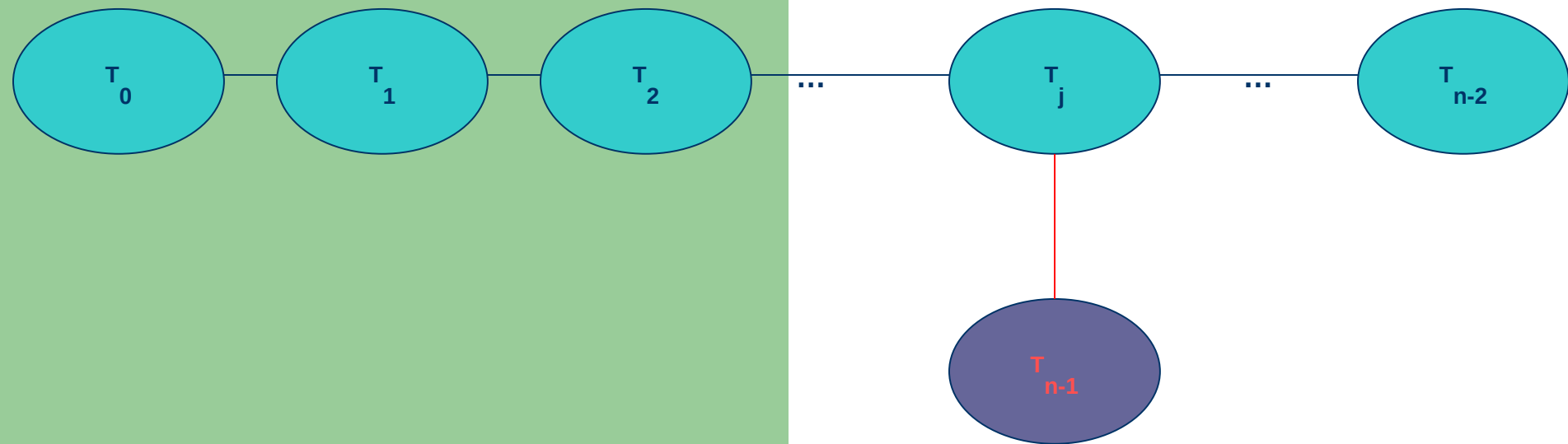


Suppose that the choice of $T_0 \dots T_{n-2}$ are in the way that the path start from T_0 , continue by $T_1 \dots T_{n-3}$ till the end to arrive at T_{n-2} .

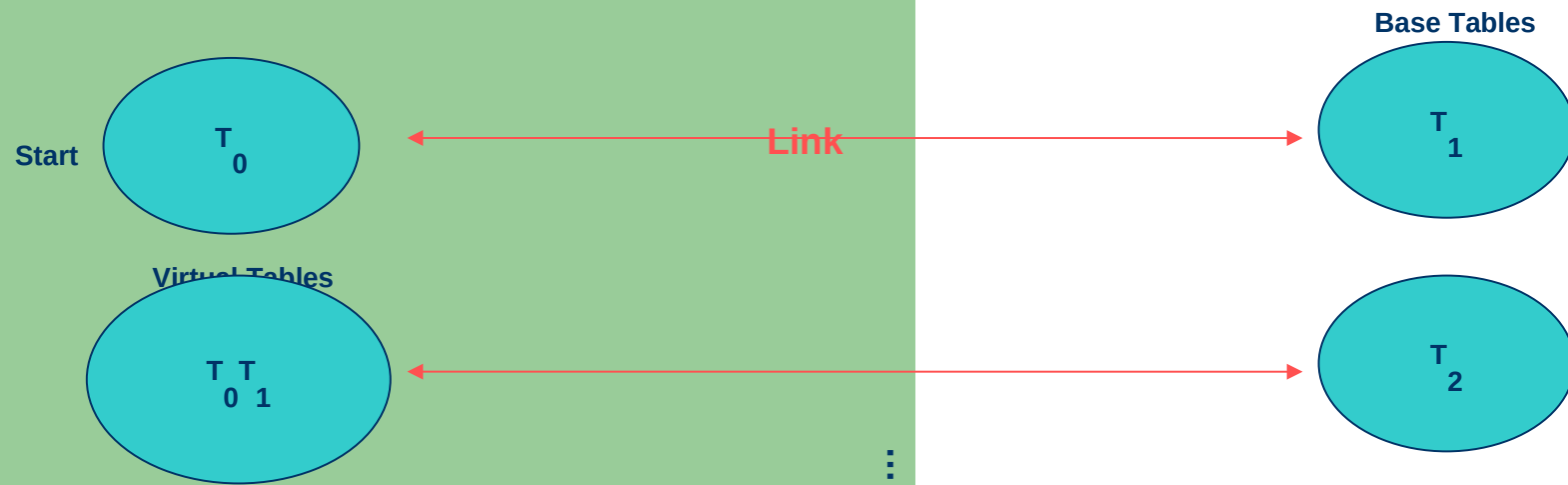
By grouping comes out:

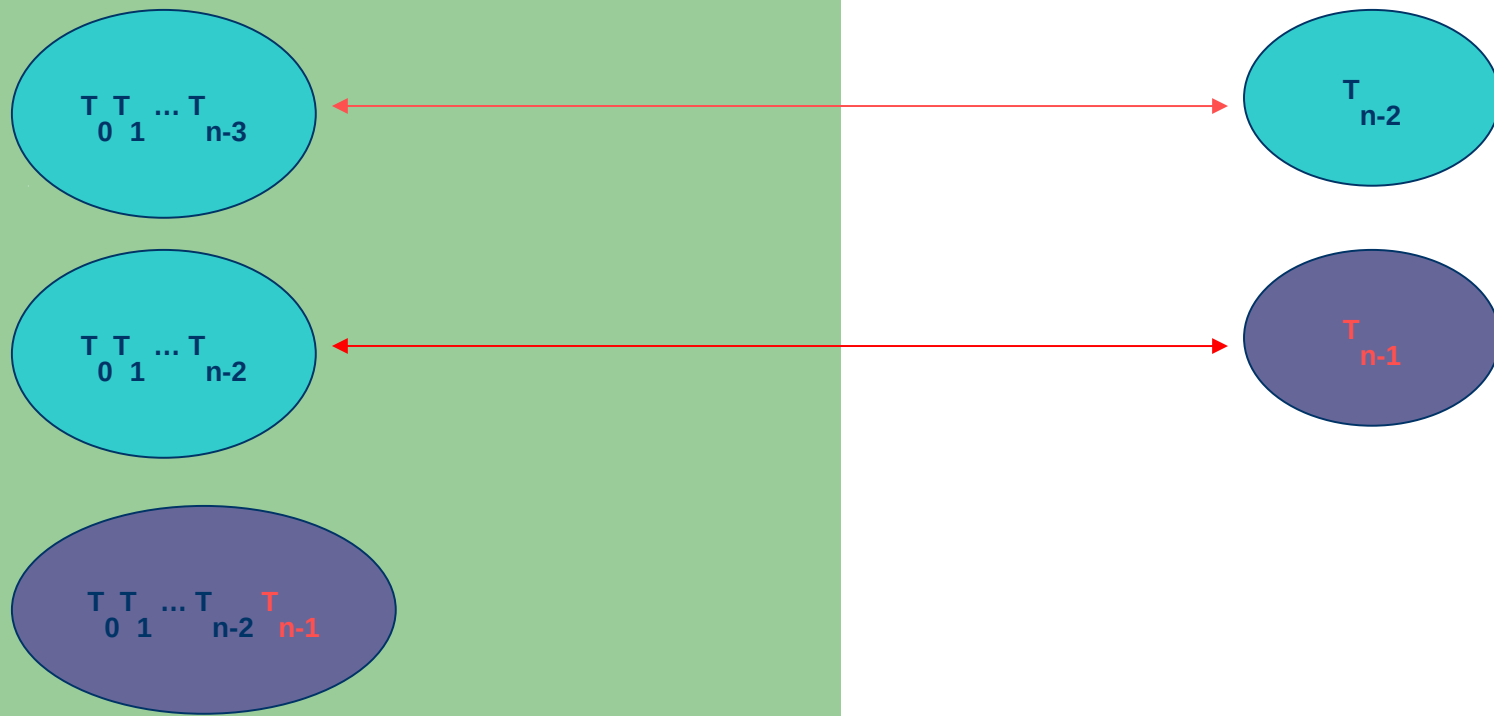


If there is one more table, the join graph would be the following:



The path should look like this:





So if we expand the virtual table $T_0 \dots T_{n-2}$ so the link would be just between it and the table T_{n-1} , where the common key should be from table T_j .

So we have the following situation:

Table $T_0 \dots T_{n-2}$ an expanded table from the virtual table $T_0 \dots T_{n-2}$ and by induction it is the same table obtained by the join of the (n-1) base tables.

Table T_{n-1}

So if we name $T_0 \dots T_{n-2}$ as T_0 and T_{n-1} as T_1 , we return to the case already proved of 2 tables where the common key in $T_0 \dots T_{n-2}$ is calculated from the combined joined row in the place of the row pointed by DP_j .

The only thing remain to prove is the propagation of the key from $T_0 \dots T_{n-2}$ to T_j and the eventual keys from $T_0 \dots T_{n-1}$ to some base tables in the base tables $T_0 \dots T_{n-1}$ but this is guaranteed in the third phase of the algorithm generateJoinPathList because it goes backward and insert eventual inherited keys.

Self Join

If the table is in join with itself, consider the table twice, every one with the necessary index.

Let see an example of self join.

Suppose that we add a column named `SUPERVISOR_ID` in the table `EMPLOYEES`, it has the id of the supervisor for a given employee.

Suppose that we have the following query:

```
SELECT A.EMPLOYEE_NAME, B.EMPLOYEE_NAME  
FROM EMPLOYEES AS A, EMPLOYEES AS B  
WHERE A.EMPLOYEE_ID = B.SUPERVISOR_ID
```

The table `EMPLOYEES` with the new column `SUPERVISOR_ID` is shown in slide 575.



generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

AdjacentList[T_i] += T_k follow by the common key

AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
0	1

generateJoinGraph (in BaseTables; out JoinGraph)

→ insert the base tables as vertexes of the graph

for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

AdjacentList[T_i] += T_k follow by the common key

AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
0	1

Employees/Employee_Id
Employees/Supervisor_Id

generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

→ for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

AdjacentList[T_i] += T_k follow by the common key

AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
0	1

Employees/Employee_Id
Employees/Supervisor_Id

generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

→ AdjacentList[T_i] += T_k follow by the common key

AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
0	1



generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

AdjacentList[T_i] += T_k follow by the common key

AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
0	1

Employees/Employee_Id

Employees/Supervisor_Id

Employee_Id

Employees/Supervisor_Id

Employees/Employee_Id

Supervisor_Id

Vertex
Employees/
Employee_Id

Join Graph

Edge

Employees/
Employee_Id

Linked List representation of the Join Graph

Adjacent List



Node
Tables

Adjacent
Tables

Common keys between
Node & Adjacent Tables
belongs to Node Tables

→ generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

```
let T0 ... Tm be the base tables
create 2 dynamic arrays queue and path

insert T0 into path

insert T0 into queue

repeat
    TElement = First Table in queue
    for every Link Item in Adjacent Link of TElement from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue
    remove TElement from queue
until queue is empty
```

Join Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
-----------------------	-------------------------

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

→ let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

Join Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
-----------------------	-------------------------

T_0

T_1

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

→ create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

 for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

 if the Link Item is in the join sequence then

 if path doesn't contain the Link Item then

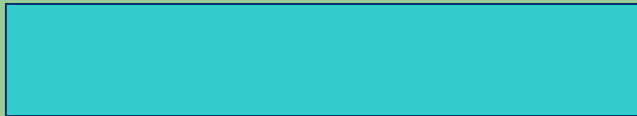
 insert Link Item into path

 insert Link Item into queue

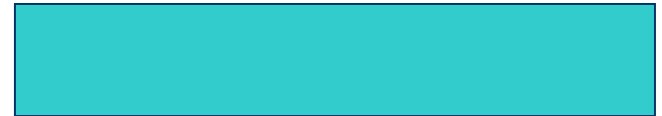
 remove T_{Element} from queue

until queue is empty

queue



path



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path

→ insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

Join Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
-----------------------	-------------------------

T_0

T_1

queue

--

path

Employees/Employee_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path

→ insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

 for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

 if the Link Item is in the join sequence then

 if path doesn't contain the Link Item then

 insert Link Item into path

 insert Link Item into queue

 remove T_{Element} from queue

until queue is empty

Join Base Tables

Employees/Employee_Id	Employees/Supervisor_Id
-----------------------	-------------------------

T_0

T_1

queue

Employees/Employee_Id

path

Employees/Employee_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path

insert T_0 into path

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repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue

Employees/Employee_Id

path

Employees/Employee_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

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repeat

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if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Employees/Employee_Id

path

Employees/Employee_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

→ T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

queue



Employees/Employee_Id

path

Employees/Employee_Id

Join Graph

Employees/Employee_Id



Employees/Supervisor_Id

Employee_Id



Employees/Supervisor_Id



Employees/Employee_Id

Supervisor_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove T_{Element} from queue

until queue is empty

Join Base Tables



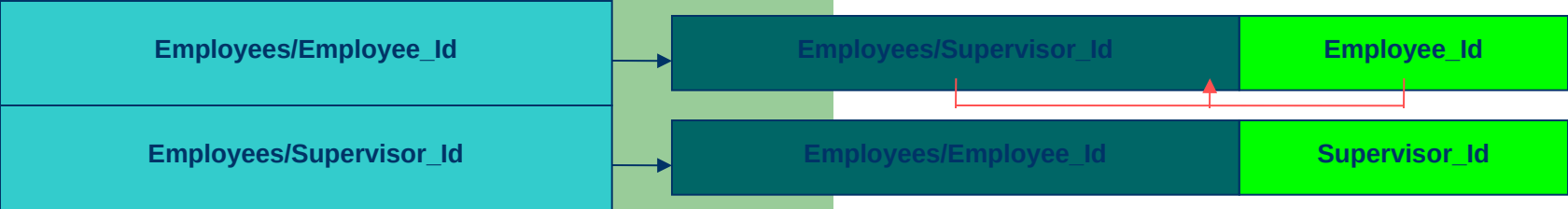
queue



path



Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

$T_{Element}$ = First Table in queue

for every Link Item in Adjacent Link of $T_{Element}$ from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

remove $T_{Element}$ from queue

until queue is empty

Join Base Tables



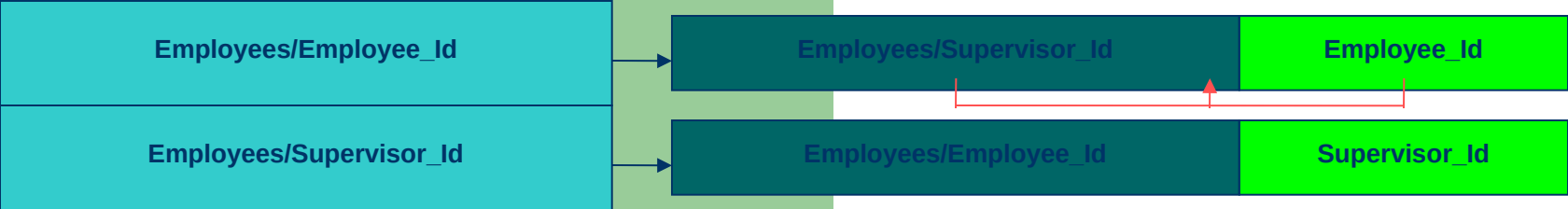
queue



path



Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

```
let T0 ... Tm be the base tables
create 2 dynamic arrays queue and path

insert T0 into path

insert T0 into queue

repeat
    TElement = First Table in queue
    for every Link Item in Adjacent Link of TElement from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue

    remove TElement from queue
until queue is empty
```

queue



Employees/Employee_Id

path

Employees/Employee_Id
Employees/Supervisor_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

```
let T0 ... Tm be the base tables
create 2 dynamic arrays queue and path

insert T0 into path

insert T0 into queue

repeat
    TElement = First Table in queue
    for every Link Item in Adjacent Link of TElement from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue

    remove TElement from queue
until queue is empty
```

queue



Employees/Employee_Id
Employees/Supervisor_Id

path

Employees/Employee_Id
Employees/Supervisor_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

```
let T0 ... Tm be the base tables
create 2 dynamic arrays queue and path

insert T0 into path

insert T0 into queue

repeat
    TElement = First Table in queue
    for every Link Item in Adjacent Link of TElement from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue
    remove TElement from queue
until queue is empty
```

queue

Employees/Supervisor_Id

path

Employees/Employee_Id
Employees/Supervisor_Id

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let T₀...T_m be the base tables
create 2 dynamic arrays queue and path

insert T₀ into path

insert T₀ into queue

repeat

→ T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

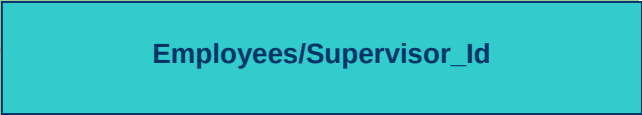
insert Link Item into path

insert Link Item into queue

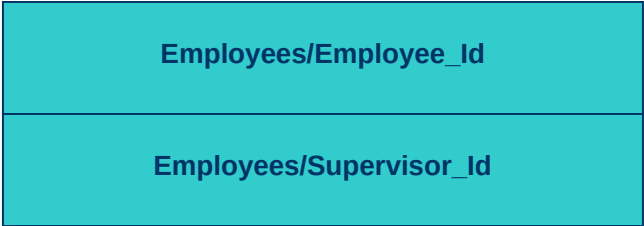
remove T_{Element} from queue

until queue is empty

queue



path



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables
create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

→ T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

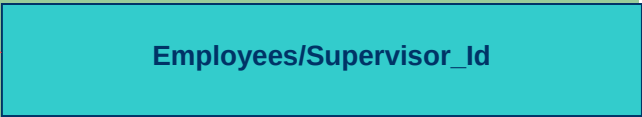
insert Link Item into path

insert Link Item into queue

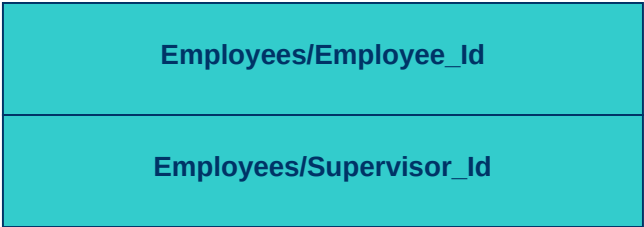
remove T_{Element} from queue

until queue is empty

queue



path



Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

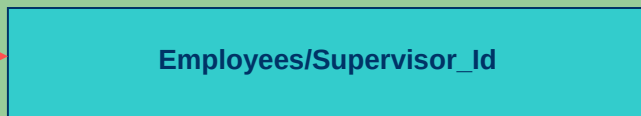
remove T_{Element} from queue

until queue is empty

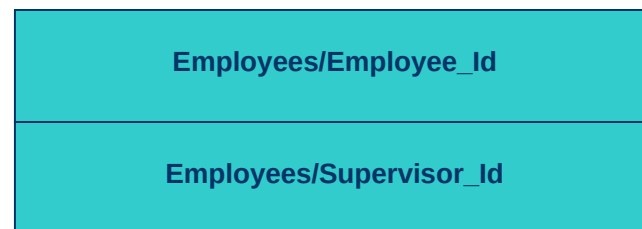
Join Base Tables



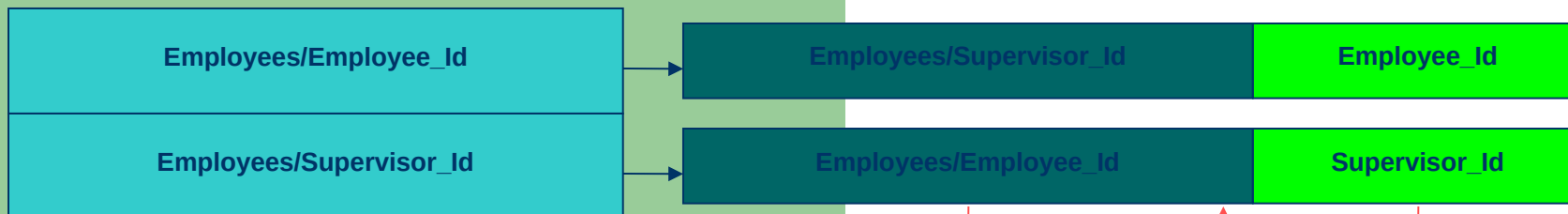
queue



path



Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue

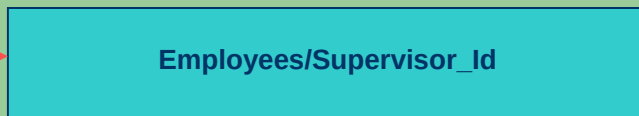
remove T_{Element} from queue

until queue is empty

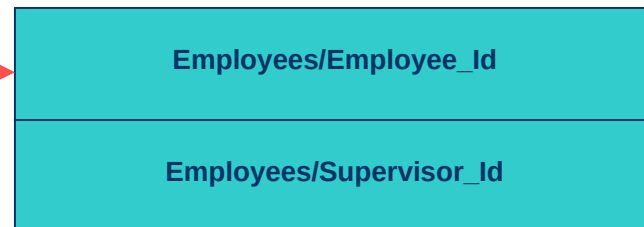
Join Base Tables



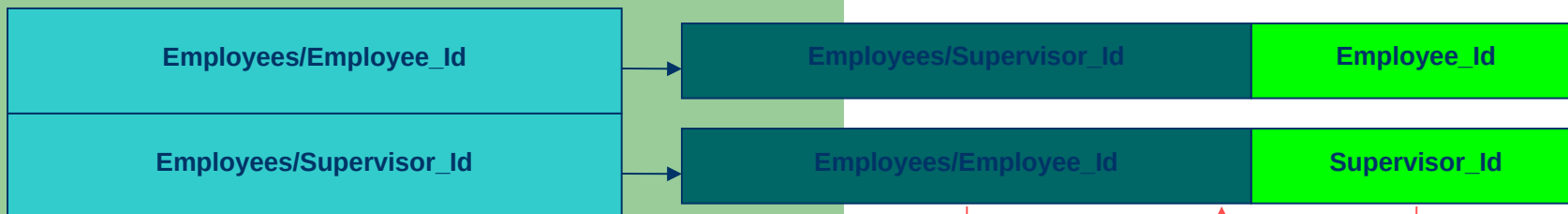
queue



path



Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

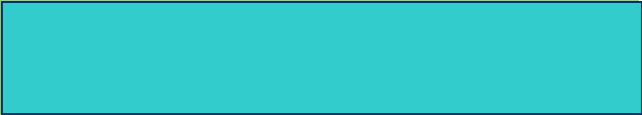
```
let T0 ... Tm be the base tables
create 2 dynamic arrays queue and path

insert T0 into path

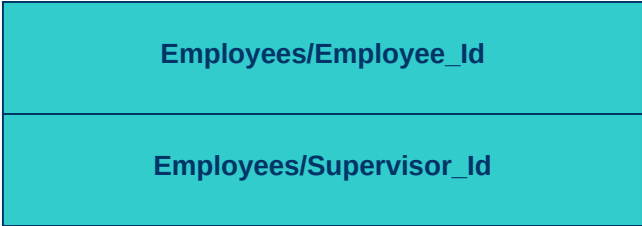
insert T0 into queue

repeat
    TElement = First Table in queue
    for every Link Item in Adjacent Link of TElement from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue
    remove TElement from queue
until queue is empty
```

queue



path



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

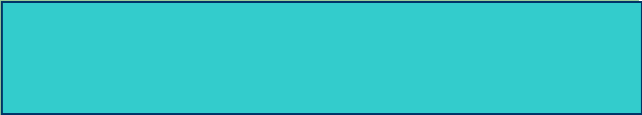
```
let T0 ... Tm be the base tables
create 2 dynamic arrays queue and path

insert T0 into path

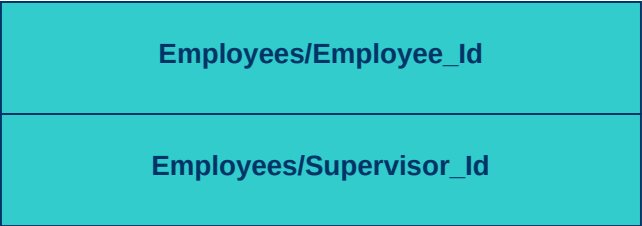
insert T0 into queue

repeat
    TElement = First Table in queue
    for every Link Item in Adjacent Link of TElement from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue
    remove TElement from queue
until queue is empty
```

queue



path



→ insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} + = T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

Nodes

Employees/Employee_Id

Employees/Supervisor_Id

path

Employees/Employee_Id

Employees/Supervisor_Id

insert all the names of base tables from path as vertexes in JoinPathList



create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} + = T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

Nodes

Employees/Employee_Id

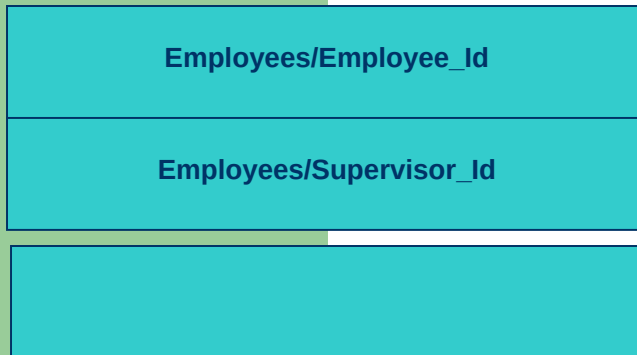
Employees/Supervisor_Id

path

Employees/Employee_Id

Employees/Supervisor_Id

buf



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

→ insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} + = T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

Nodes

Employees/Employee_Id

Employees/Supervisor_Id

path

Employees/Employee_Id

Employees/Supervisor_Id

buf

Employees/Employee_Id

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

→ for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} + T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

Nodes

Employees/Employee_Id

Employees/Supervisor_Id

path

Employees/Employee_Id

Employees/Supervisor_Id

buf

Employees/Employee_Id

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

→ Make one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

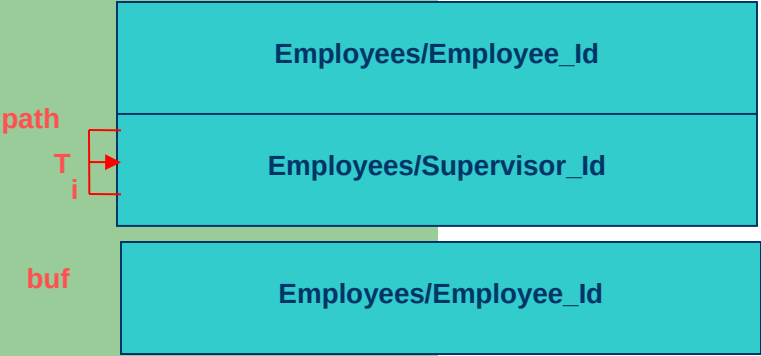
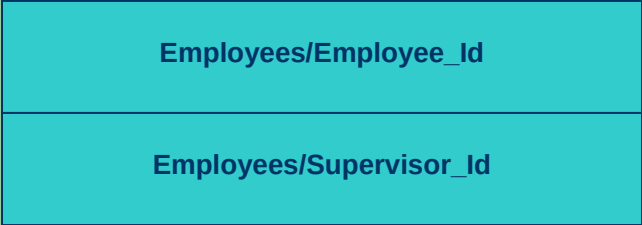
$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} + = T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

Nodes



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

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for all the remainder entries in path do

take one T_i at a time

→ $\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} + T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

Nodes

Employees/Employee_Id

Employees/Supervisor_Id

Employees/Employee_Id

Employees/Employee_Id

Employees/Supervisor_Id

Employees/Employee_Id

path

T_i

buf

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

→ $JoinPathAdjacentList(T_i) = T_{[buf]}$

$Key(T_i) = getFirstAdjacentListKey(T_i, T_{[buf]})$

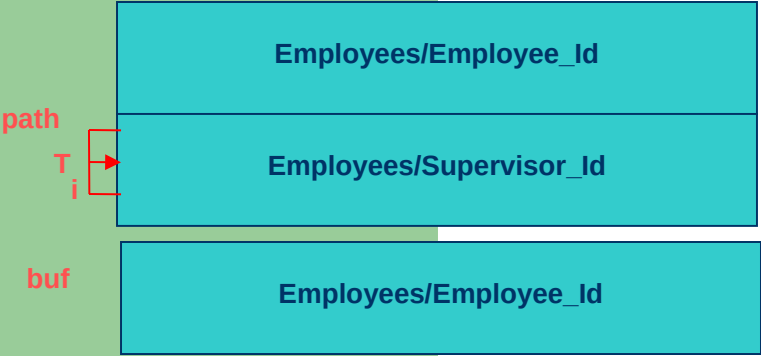
$JoinPathAdjacentList(T_{[buf]}) = T_i$

$Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

Insert NodesList[$T_{[buf]}$] = $T_{[buf]}$

Nodes



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

→ $\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

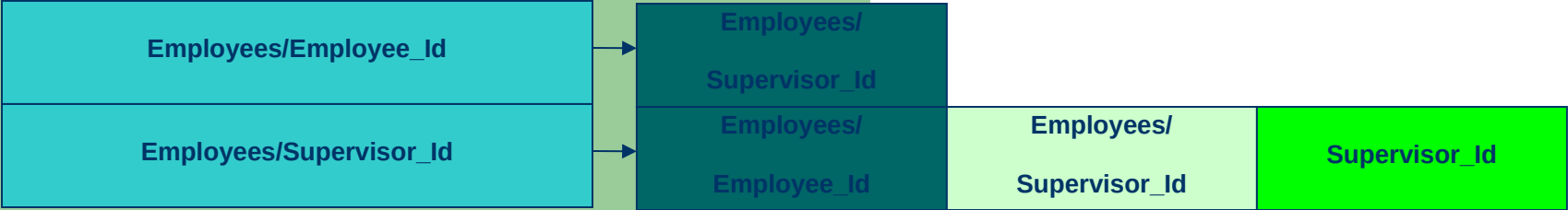
$\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

$\text{Insert NodesList}[T_{[buf]}] = T_{[buf]}$

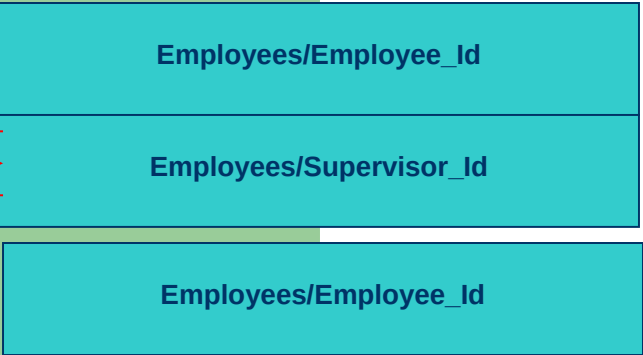
Nodes



path

T_i

buf



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[buf]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[buf]})$

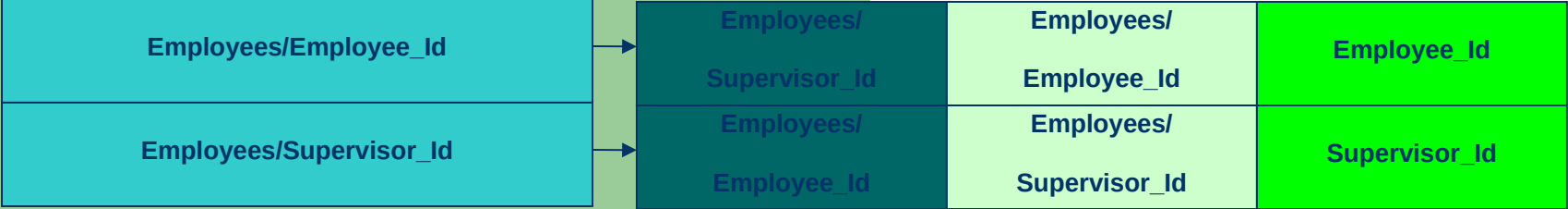
→ $\text{JoinPathAdjacentList}(T_{[buf]}) = T_i$

$\text{Key}(T_{[buf]}) = \text{getFirstAdjacentListKey}(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

Insert $\text{NodesList}[T_{[buf]}] = T_{[buf]}$

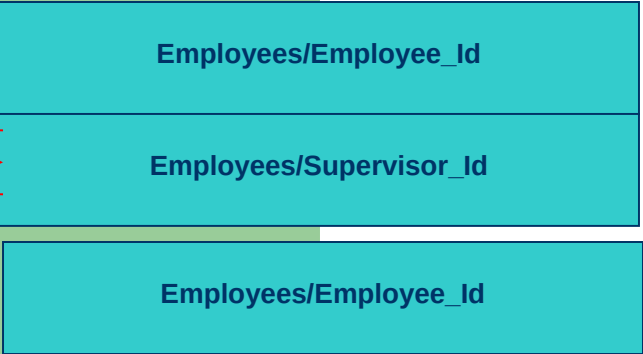
Nodes



path

T_i

buf



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$JoinPathAdjacentList(T_i) = T_{[buf]}$

$Key(T_i) = getFirstAdjacentListKey(T_i, T_{[buf]})$

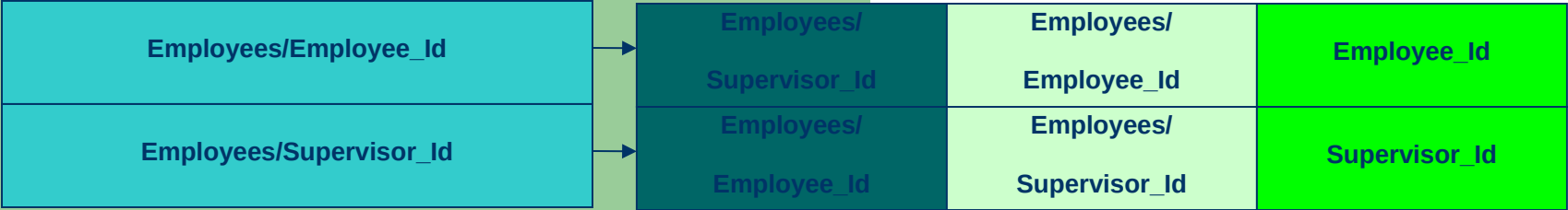
$JoinPathAdjacentList(T_{[buf]}) = T_i$

→ $Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]}, T_i)$

$T_{[buf]} += T_i$

Insert NodesList[$T_{[buf]}$] = $T_{[buf]}$

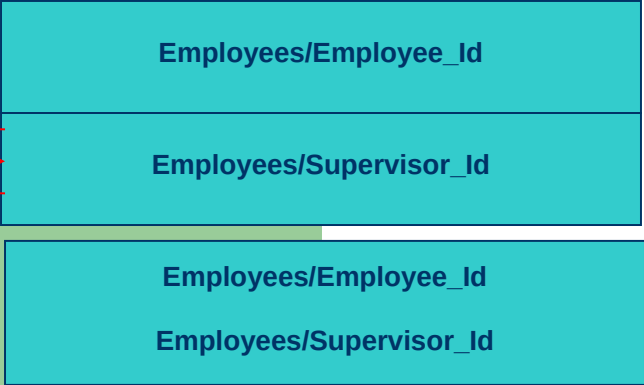
Nodes



path

T_i

buf



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$JoinPathAdjacentList(T_i) = T_{[buf]}$

$Key(T_i) = getFirstAdjacentListKey(T_i, T_{[buf]})$

$JoinPathAdjacentList(T_{[buf]}) = T_i$

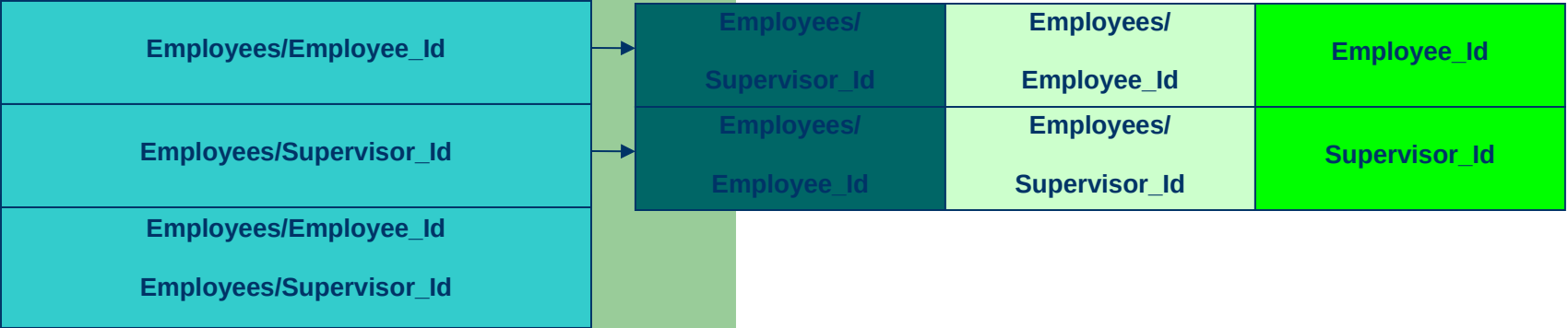
$Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]}, T_i)$

→ $T_{[buf]} += T_i$

Insert NodesList[$T_{[buf]}$] = $T_{[buf]}$

Nodes

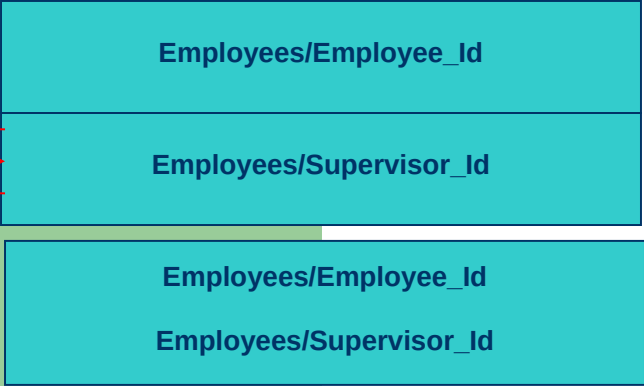
Join Path List



path

T_i

buf



create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in } \text{InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

buf

Key



create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Join Path List

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if (buf_c.Table = T_k) then

if (buf_c != Key($T_{[i]}$)) and (buf_c not in InheritedKey($T_{[i]}$)) then

InheritedKey($T_{[i]}$) += buf_c

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes Key($T_{[i]}$) and k_l is the respective key then

buf.Table += T_l

buf.key += K_{k_l}

Table

Key

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in } \text{InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Manager_Id
Employees/ Employee_Id Employees/ Manager_Id

Employees/ Manager_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Manager_Id	Manager_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

T_k

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if $T_{[i]}$ is the table from which comes $\text{Key}(T_{[i]})$ and k_i is the respective key then

$\text{buf}.\text{Table} += T_{[i]}$

$\text{buf}.\text{key} += K_{[i]}$

Table

Key

N/A

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

T_k

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in } \text{InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Manager_Id
Employees/ Employee_Id Employees/ Manager_Id



k

Employees/ Manager_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Manager_Id	Manager_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

N/A

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Manager_Id
Employees/ Employee_Id Employees/ Manager_Id

T_k

Employees/ Manager_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Manager_Id	Manager_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in } \text{InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

N/A

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

N/A

--	--

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{Key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

Join Path List

$T_{[i]}$

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

$T_{[i]}$

Employees/
Employee_Id

Employees/
Supervisor_Id

Employees/
Employee_Id

Employees/
Supervisor_Id

Join Path List

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]}))$ then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

$T_{[i]}$

Join Path List

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

--	--

$T_{[i]}$

Employees/
Employee_Id

Employees/
Supervisor_Id

Employees/
Employee_Id

Employees/
Supervisor_Id

Employees/
Supervisor_Id

Employees/
Employee_Id

Employee_Id

Employees/
Supervisor_Id

Supervisor_Id

Join Path List

$T_{[i]}$
 K_{k_l}

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c$ not in $\text{InheritedKey}(T_{[i]})$) then

$\text{InheritedKey}(T_{[i]}) += \text{buf}_c$

if $T_{[i]}$ is not a base table then

if T_l is the table from which comes $\text{Key}(T_{[i]})$ and k_l is the respective key then

$\text{buf}.\text{Table} += T_l$

$\text{buf}.\text{key} += K_{k_l}$

Table

Key

N/A

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

$T_{[i]}$

Employees/
Employee_Id

Employees/
Supervisor_Id

Employees/
Employee_Id

Employees/
Supervisor_Id

Employees/
Supervisor_Id

Employees/
Employee_Id

Employee_Id

Supervisor_Id

Join Path List

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if $(\text{buf}_c.\text{Table} = T_k)$ then

if $(\text{buf}_c.\text{key} \neq \text{Key}(T_{[i]}))$ and $(\text{buf}_c \text{ not in InheritedKey}(T_{[i]}))$ then

InheritedKey($T_{[i]}$) += buf_c

if $T_{[i]}$ is not a base table then

if $T_{[i]}$ is the table from which comes $\text{Key}(T_{[i]})$ and k_i is the respective key then

$\text{buf}.\text{Table} += T_{[i]}$

$\text{buf}.\text{key} += K_{k_i}$

Table

Key

--	--

Employees/ Supervisor_Id	Employees/ Employee_Id	Employee_Id
Employees/ Employee_Id	Employees/ Supervisor_Id	Supervisor_Id

$T_{[i]}$

Join Path List

Employees/ Employee_Id
Employees/ Supervisor_Id
Employees/ Employee_Id Employees/ Supervisor_Id

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for all the couples of $\langle \text{Table}, \text{key} \rangle$ in buf do

take one couple buf_c at a time

if (buf_c.Table = T_k) then

if (buf_c.key != Key($T_{[i]}$)) and (buf_c not in InheritedKey($T_{[i]}$)) then

InheritedKey($T_{[i]}$) += buf_c

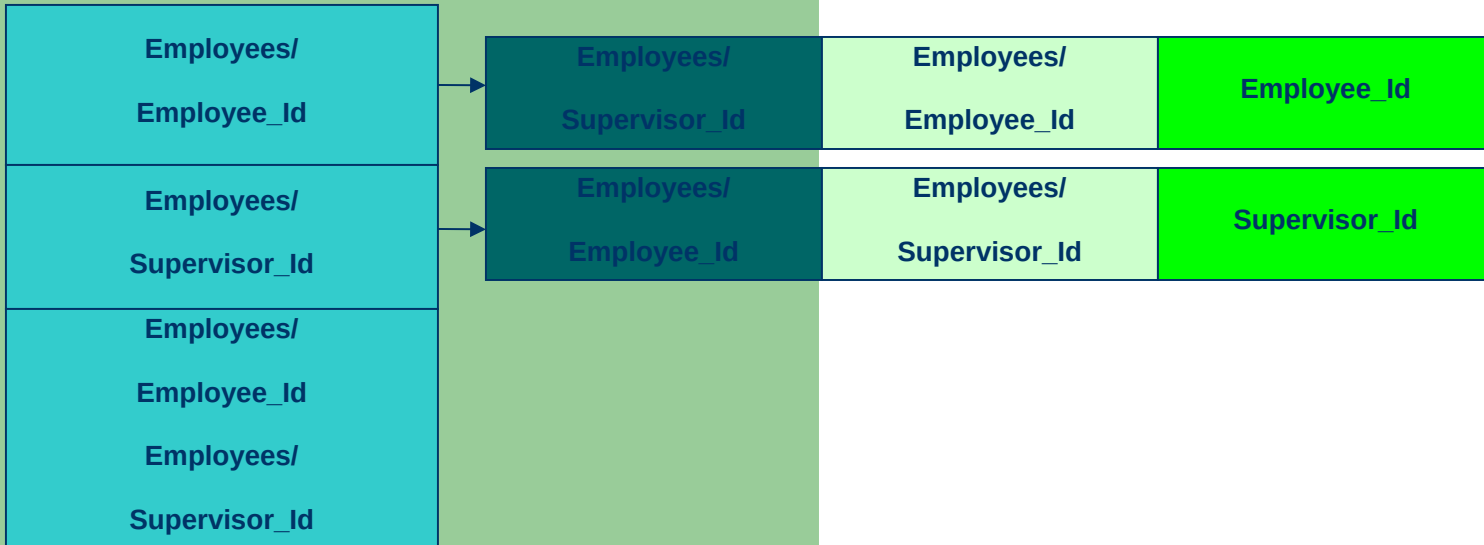
if $T_{[i]}$ is not a base table then

if T_l is the table from which comes Key($T_{[i]}$) and k_l is the respective key then

buf.Table += T_l

buf.key += K_{k_l}

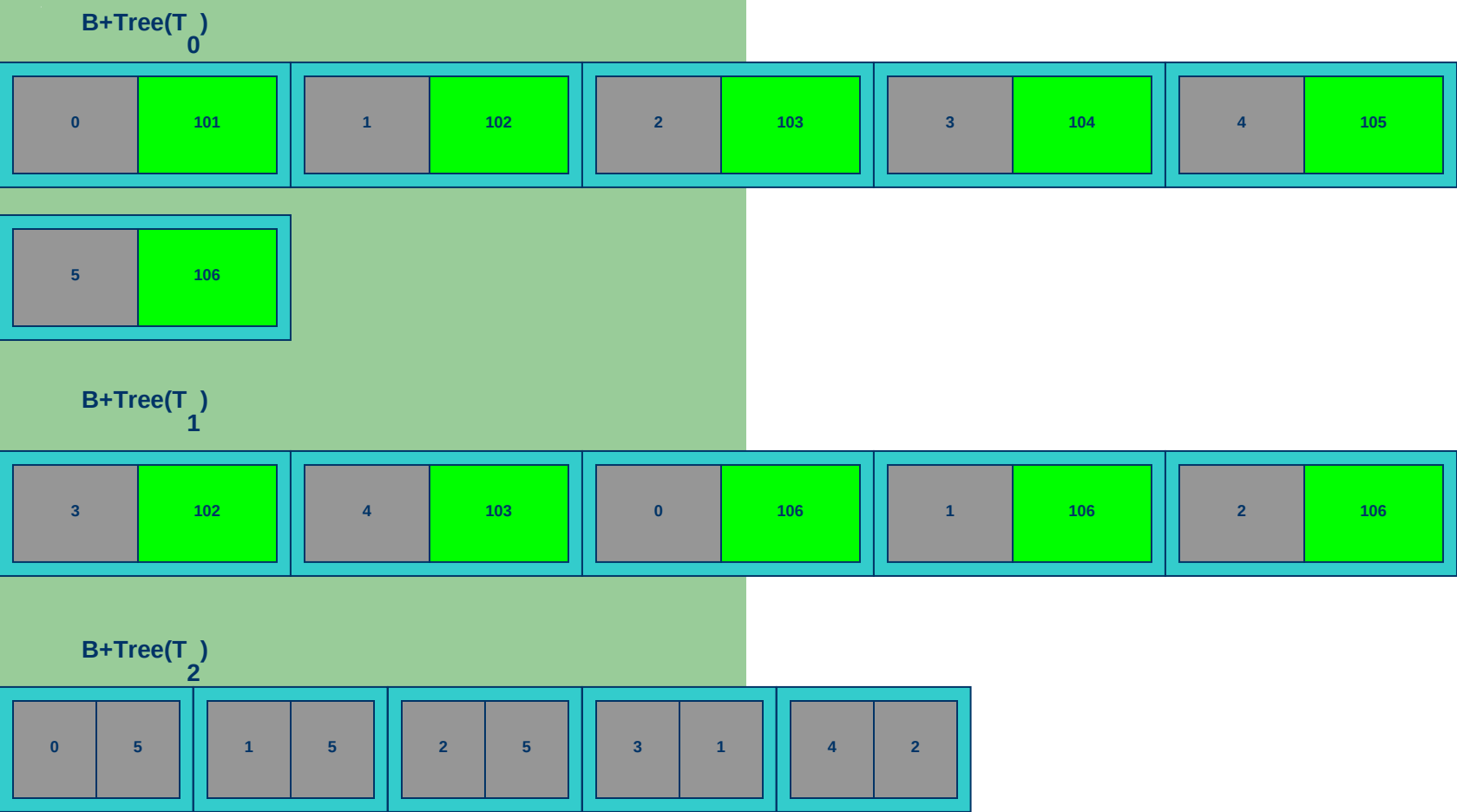
Join Path List



Employees table

	EMPLOYEE_ID	NAME	EMAIL	PHONE_NUMBER	HIRE_DATE	JOB_ID	SALARY	SUPERVISOR_ID	DEPARTMENT_ID
0	101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	106	FIN
1	102	Jorge Perez	jperez	448-5268	05/14/1999	AC_MGR	60000	106	ACC
2	103	Edward Cartier	ecartier	742-8429	03/01/2003	SA_MGR	60000	106	SAL
3	104	Teresa Gonzalez	tgonzalez	134-8329	12/20/2002	AC_AUD	55000	102	ACC
4	105	Michelle Blanche	mblanche	745-7496	01/02/2001	SA_REP	35000	103	SAL
5	106	Peter Spencer	pspencer	111-2222	01/01/1996	GE_MGR	120000	NULL	GEN

Applying the insert routine for all the rows in the table EMPLOYEES, we obtain the following indexes:



B \bowtie Tree with incremental Join

Due to the fact that join is commutative and associative and we are working on Virtual Tables and using indexes on them; it is possible instead of calculating all the join combinations to calculate incrementally the join.

This issue works just when the n tables are in direct path join between them but if they are not we are not interested.

Giving a casual order for the tables.

Beginning from Table 0, get a table T_i in direct join with it.

A Join Path List comes out with 2 entries from T_0 to T_i and from T_i to T_0 .

The index number start always with 0.

Repeat, with T_{0i} and get a next table that is in direct join with T_0 or with T_i , the process continue till we scan all the tables.

This algorithm is linear, is $2*n - 1$.