B^M**Tree**

A mechanism to drive existing B⁺Trees to do Join Internally.

RDBMS challenges

Performance has been always a challenge for relational databases. A major problem with relational database that a good schema requires many tables in relation between them, and in consequence the calculation of many joins to satisfy the queries.

DBA spends lots of time to tune the database. Some database schemas are not in BCNF just to avoid some joins. Also some materialized views are just to avoid it. Star Schema born from the fact that joining is complex and to simplify joins.

Standard indexes

The standard indexes used in relational databases are B+tree, hashed keys and bitmap indexes but the problem all suffers from some restrictions.

B+tree have among others the fact that it work just on one table.

Hashed keys are very fast but they require a full key lookup, a perfect match, and a unique identifying value.

Bitmap is also good but it has a limit on the number of different values a column can have.

Bitmap Join Index & Materialized Views

Bitmap join index is efficient but is not general; it is based on Star Schema. Has a lots of bitmap arrays depending on the size of the dimensions tables.

Materialized Views are redundant. No one use Materialized View to order a table, because index is the more natural way. Also B™Tree index is the more natural way to get the join.

BMTREE Overview

B™tree is a new index technology that is based on B⁺tree that prejoin the tables inside it.

B¤tree uses "Virtual Tables" and "Join Path Lists" to make pre-join internally, so it doesn't use the multidimensional index technique with the benefit of more easier and more concise algorithm, no limit for the number of tables in join and easy use: the same way as a native B+tree.

Given n Tables in join, scanning the B™tree return a set of pointers for the rows in join for any possible combination of tables in join.

BMTREE Index

To understand how B™TREE Index works let see what happens when we insert a new Row R_m from Table T_i into the database.

Suppose that table T_i is in Direct Join with a table T_k , we have to look for all the Rows $R_n ... R_z$ in T_k that satisfy the join condition with R_m and insert Rows references to $R_m R_{n...} R_m R_z$ in the virtual table T_{ik} .

The process should be repeated for $R_m R_{n...} R_m R_z$ with a table in join at least with one of the base tables constituting the Virtual Join Table T_{ij} and so on until we scan a path in the sequence of tables in join.

Transformation of Existing B⁺Tree

- •The internal definition for the creation of a B+Tree take in consideration the following:
 - Name of B⁺Tree index follow by an index
 - Number of base tables constituting the virtual table indexed by the B+Tree
 - Length and type of Keys
 - Length and type of Inherited Keys (They are supplementary fields inserted in the B⁺Tree but they are not part of the key and they are not used for comparison)
- Declare the page of B⁺Tree as a buffer of bytes and divide it as needed. Many existing B⁺Tree follow this technique to support different type of multiple columns Key.
- The Leaf Page structure consists of:
 - Pointer to the previous sibling page
 - number of elements in which everyone consists of:
 - Space for the columns forming the keys
 - Space for the Data Pointers (Row Ids) to reference the Row in every table
 - Space for the columns forming the Inherited Keys
 - Pointer to the next sibling Page

Transformation of Existing B⁺**Tree (continue)**

- •The Non Leaf Page structure consists of:
 - Pointer to a child page which key values are smaller than all the keys in the page
 - number of elements in which everyone consists of:
 - Space for the columns forming the keys
 - Pointer to a child page which key values are bigger than the keys in the Element
- Due to the fact that many join keys are duplicates, change has been made for the duplicates in the sense when 2 keys are equals, we consider the data references for them. The B+Tree keeps these possibly duplicated keys separate internally by combining the unique sequence of data references with each key. The process of combination is done logically, and requires no additional space for key storage.

Many advanced B⁺Tree in the market use (Key, Data Reference) combination to refer to unique Row eliminating duplicates internally and use additional fields others than the one forming the key to avoid access to the table.

So for those B⁺Trees, the only modification is instead of space of one Data Reference is a space for multiple Data Reference Space.

Definitions

Base Table:

Base tables are database objects whose structure and the data they contain are both on disk.

Virtual Table:

Virtual tables are tables whose contents are derived from base tables. Only its definition (base tables Names constituting it) is stored on disk.

Definitions

Direct Join:

Two tables are in Direct Join if there is a link between them (in other sense if there is common columns between them).

Join Graph:

A graph representing direct join between tables.

Adjacency List:

List for every table T_i in the database all those tables in direct Join with it.

Generating Join Graph

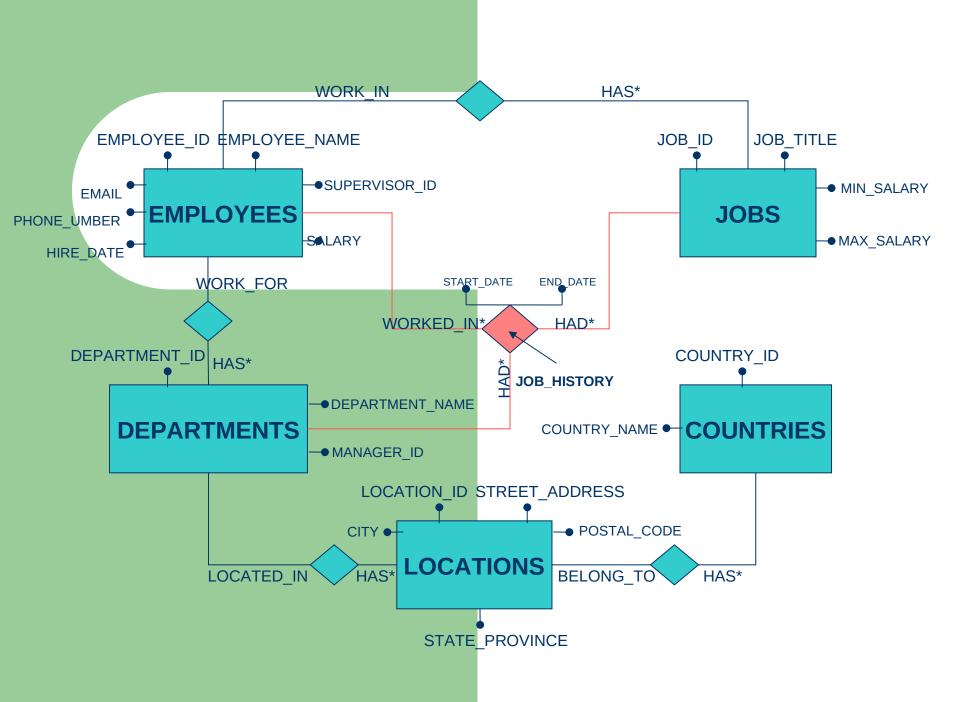
- Base Tables represent the vertexes of the Join Graph.
- Due to the fact that join is commutative, for every pair of tables in direct join between them as defined by DBA create an undirected edge to link them.
- It is very easy to knows which tables are in direct join with others tables from the definition of common columns between them.

The algorithm for generating the Linked List representation of the join Graph is the following:

generateJoinGraph (in BaseTables; out JoinGraph) insert the base tables as vertexes of the graph for every direct join between 2 tables T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

AdjacentList $[T_i]$ += T_k follow by the common key

AdjacentList $[T_k]$ += T_i follow by the common key



Transforming the entity relationship schema into the relational model, we get the following tables:

```
CREATE TABLE EMPLOYEES
  EMPLOYEE_ID INT NOT NULL,
  EMPLOYEE_NAME VARCHAR(35),
  EMAIL VARCHAR(25),
  PHONE_NUMBER VARCHAR(20),
  HIRE_DATE DATE,
  SUPERVISOR_ID INT NOT NULL,
  JOB ID VARCHAR(10),
  SALARY NUMERIC(8,2),
  DEPARTMENT ID VARCHAR(3)
);
CREATE TABLE JOB HISTORY
   EMPLOYEE_ID INT,
   START_DATE DATE,
   END_DATE DATE,
   DEPARTMENT_ID VARCHAR(3),
   JOB_ID VARCHAR(10)
);
CREATE TABLE JOBS
  JOB_ID VARCHAR(10),
  JOB_TITLE VARCHAR(35),
  MIN SALARY DOUBLE,
   MAX SALARY DOUBLE
);
```

```
CREATE TABLE DEPARTMENTS
  DEPARTMENT_ID VARCHAR(3),
  DEPARTMENT_NAME VARCHAR(30),
  MANAGER_ID INT,
  LOCATION_ID INT
 );
CREATE TABLE LOCATIONS
  LOCATION_ID INT,
  STREET_ADDRESS VARCHAR(40),
  POSTAL_CODE VARCHAR(12),
  CITY VARCHAR(30),
  STATE_PROVINCE VARCHAR(25),
  COUNTRY_ID CHAR(2)
);
CREATE TABLE COUNTRIES
  COUNTRY_ID CHAR(2),
  COUNTRY_NAME VARCHAR(40)
);
```

The join for the example is the following:

AND LOCATIONS.COUNTRY ID = COUNTRIES.COUNTRY ID;

```
List where every employee have been worked before along with the department that he is working now:
CREATE JOIN INDEX RECENT IDX
          EMPLOYEES(LAST NAME), DEPARTMENTS, JOBS, JOB HISTORY, LOCATIONS, COUNTRIES
 ON
WHERE EMPLOYEES.EMPLOYEE ID = JOB HISTORY.EMPLOYEE ID
 AND JOBS.JOB ID = JOB HISTORY.JOB ID
 AND EMPLOYEES.DEPARTMENT_ID = DEPARTMENTS.DEPARTMENT_ID
 AND DEPARTMENTS.LOCATION_ID = LOCATIONS.LOCATION_ID
 AND LOCATIONS.COUNTRY_ID = COUNTRIES.COUNTRY_ID;
SELECT EMPLOYEES.EMPLOYEE NAME,
   JOBS.JOB TITLE AS JOB TITLE,
   DEPARTMENTS.DEPARTMENT NAME AS DEPARTMENT NAME,
   COUNTRIES.COUNTRY NAME AS COUNTRY NAME
 FROM EMPLOYEES, JOB_HISTORY, DEPARTMENTS,
    LOCATIONS, JOBS, COUNTRIES
WHERE EMPLOYEES.EMPLOYEE ID = JOB HISTORY.EMPLOYEE ID
 AND JOBS.JOB ID = JOB HISTORY.JOB ID
 AND EMPLOYEES.DEPARTMENT ID = DEPARTMENTS.DEPARTMENT ID
 AND DEPARTMENTS.LOCATION ID = LOCATIONS.LOCATION ID
```

This is another join on the same tables:

```
List where every employee have been worked before along with the department that he is working before:
CREATE JOIN INDEX HISTORY IDX
          EMPLOYEES(LAST NAME), DEPARTMENTS, JOBS, JOB HISTORY, LOCATIONS, COUNTRIES
 ON
WHERE EMPLOYEES.EMPLOYEE ID = JOB HISTORY.EMPLOYEE ID
 AND JOBS.JOB ID = JOB HISTORY.JOB ID
 AND JOB_HISTORY.DEPARTMENT_ID = DEPARTMENTS.DEPARTMENT_ID
 AND DEPARTMENTS.LOCATION_ID = LOCATIONS.LOCATION_ID
 AND LOCATIONS.COUNTRY ID = COUNTRIES.COUNTRY ID;
SELECT EMPLOYEES.FIRST NAME +
   EMPLOYEES.LAST NAME AS NAME,
   JOBS.JOB TITLE AS JOB TITLE,
   DEPARTMENTS.DEPARTMENT_NAME AS DEPARTMENT_NAME,
   COUNTRIES.COUNTRY NAME AS COUNTRY NAME
 FROM JOB_HISTORY, DEPARTMENTS,
    LOCATIONS, JOBS, COUNTRIES, EMPLOYEES
WHERE EMPLOYEES.EMPLOYEE ID = JOB HISTORY.EMPLOYEE ID
 AND JOBS.JOB ID = JOB HISTORY.JOB ID
 AND JOB HISTORY.DEPARTMENT ID = DEPARTMENTS.DEPARTMENT ID
 AND DEPARTMENTS.LOCATION ID = LOCATIONS.LOCATION ID
 AND LOCATIONS.COUNTRY_ID = COUNTRIES.COUNTRY ID;
```

insert the base tables as vertexes of the graph

for every direct join between 2 tables of the form T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

AdjacentList $[T_i]$ += T_k follow by the common key

AdjacentList[T_k] += T_i follow by the common key

Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
0	1	2	3	4	5

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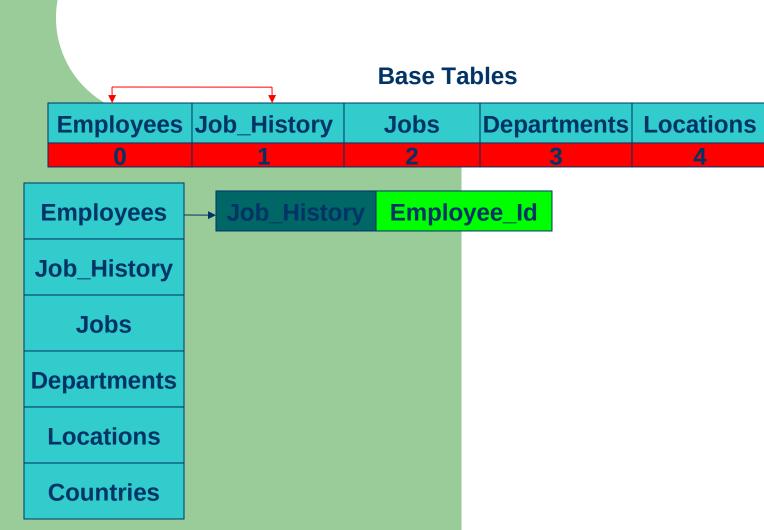
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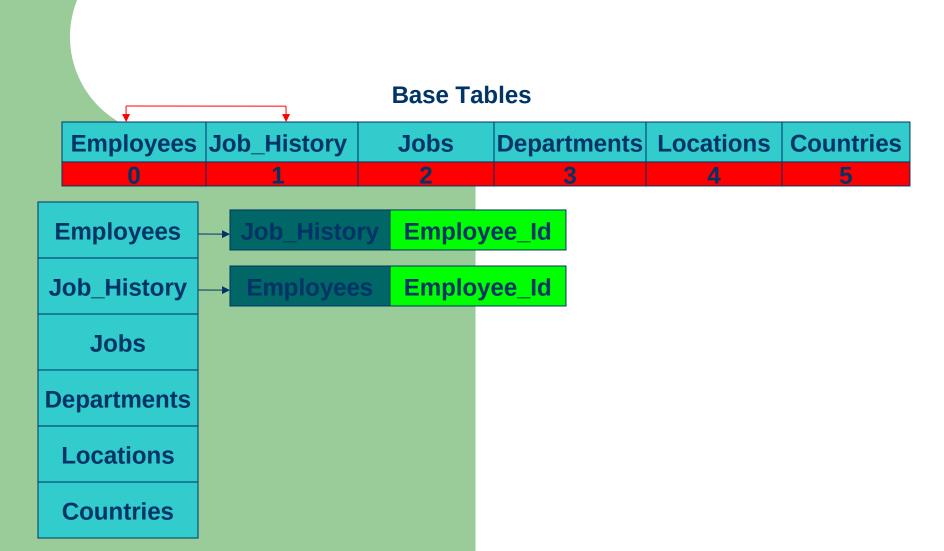


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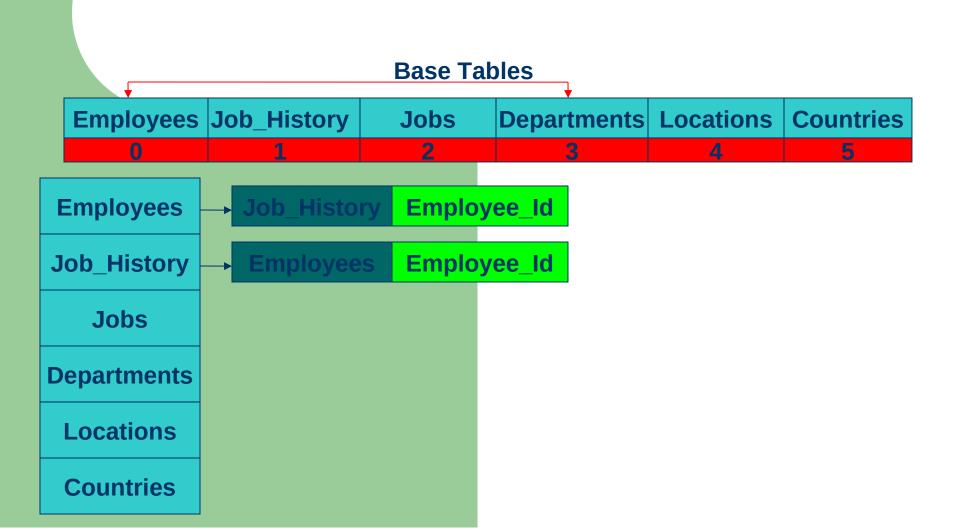
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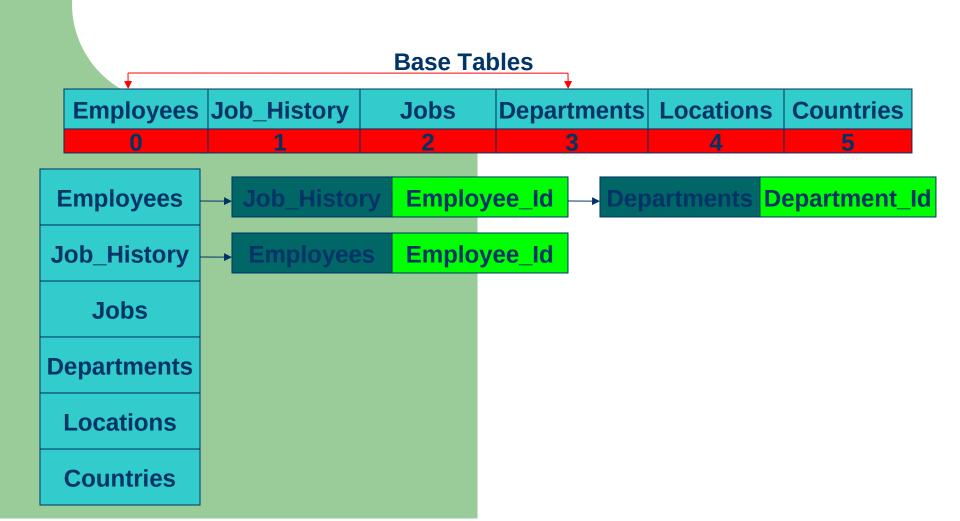
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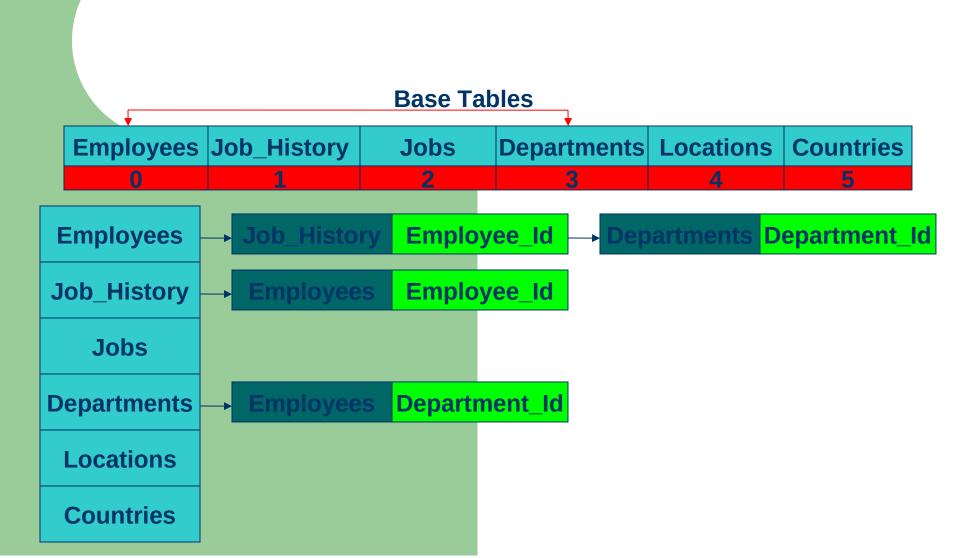


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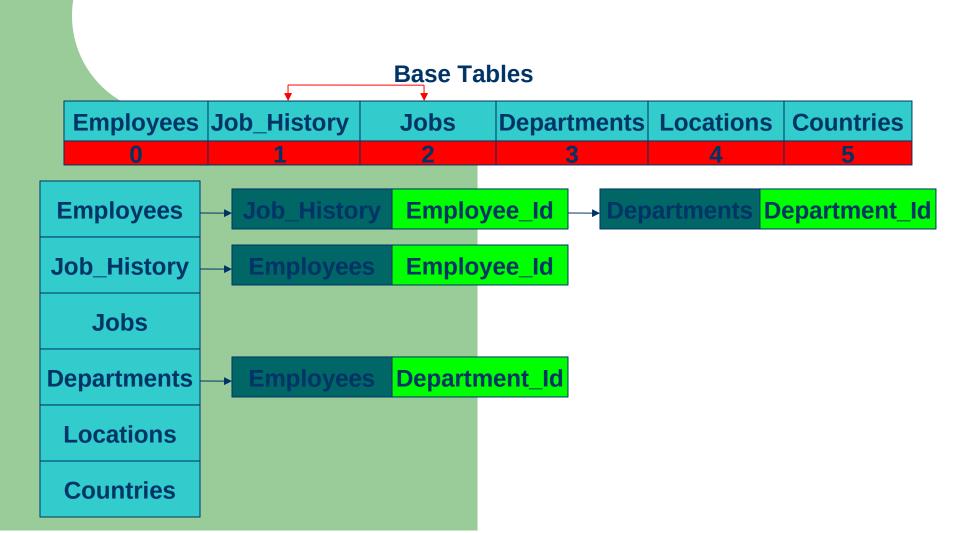
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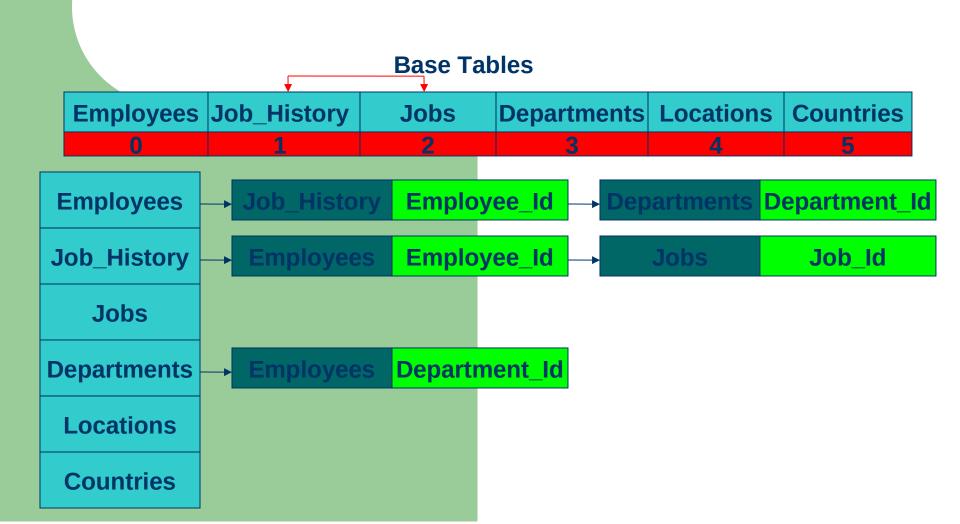
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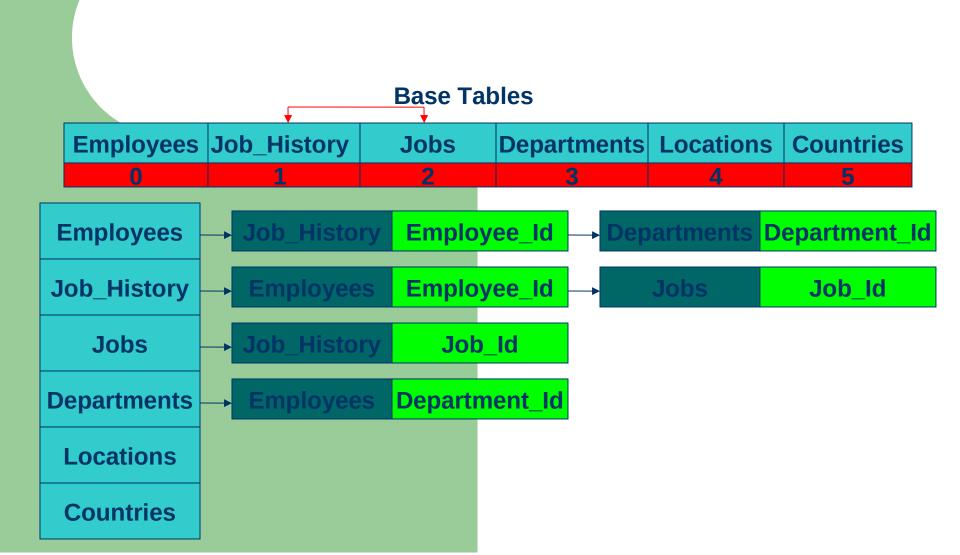


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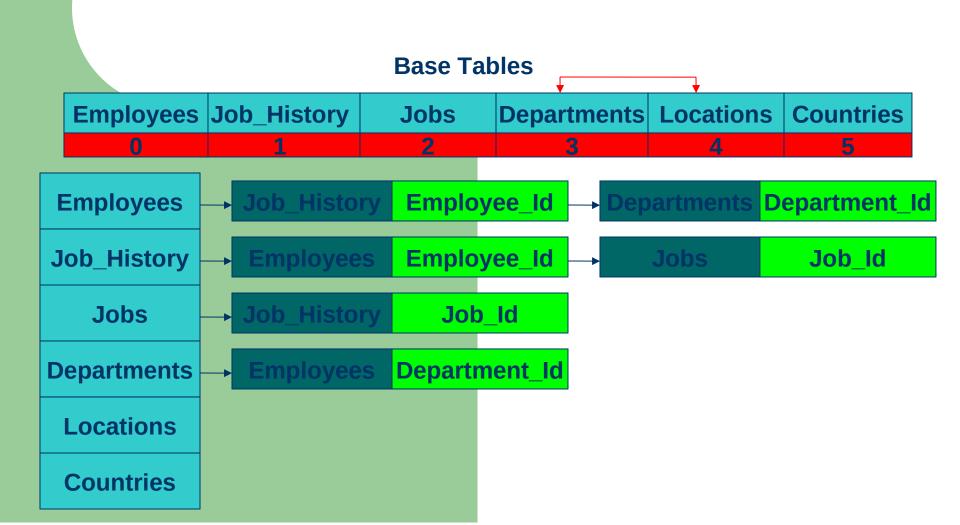
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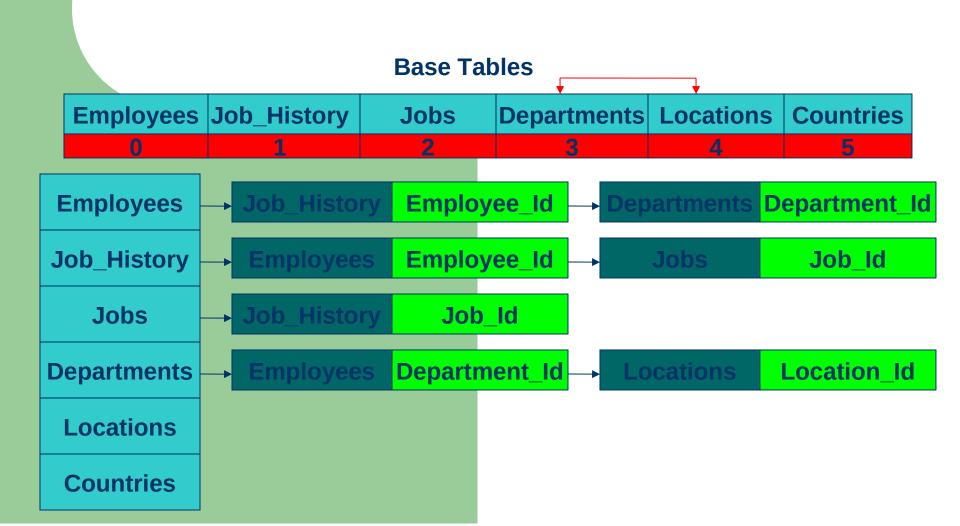
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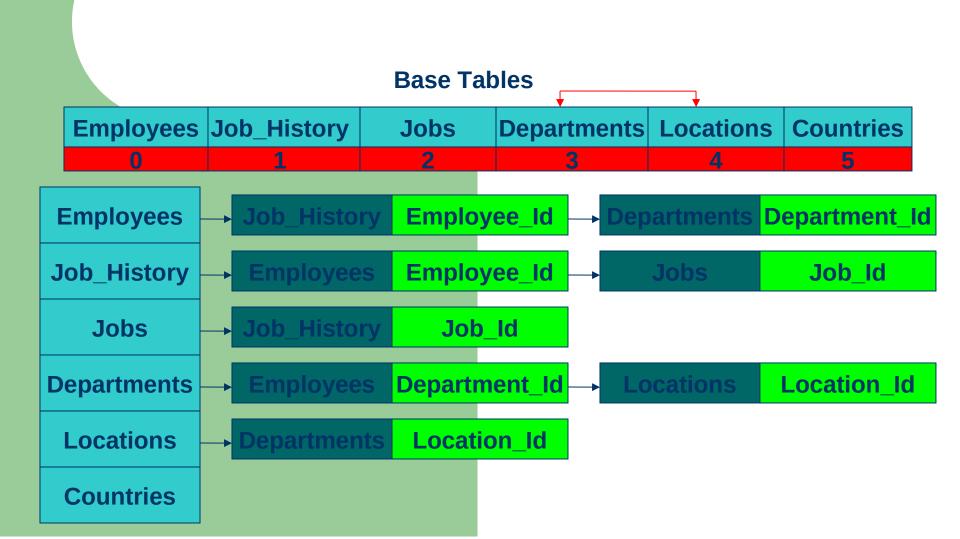


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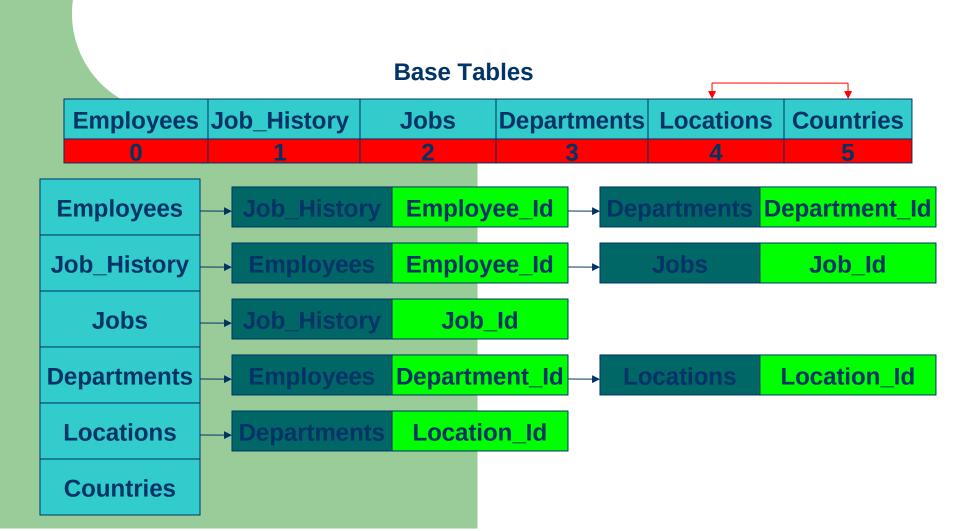
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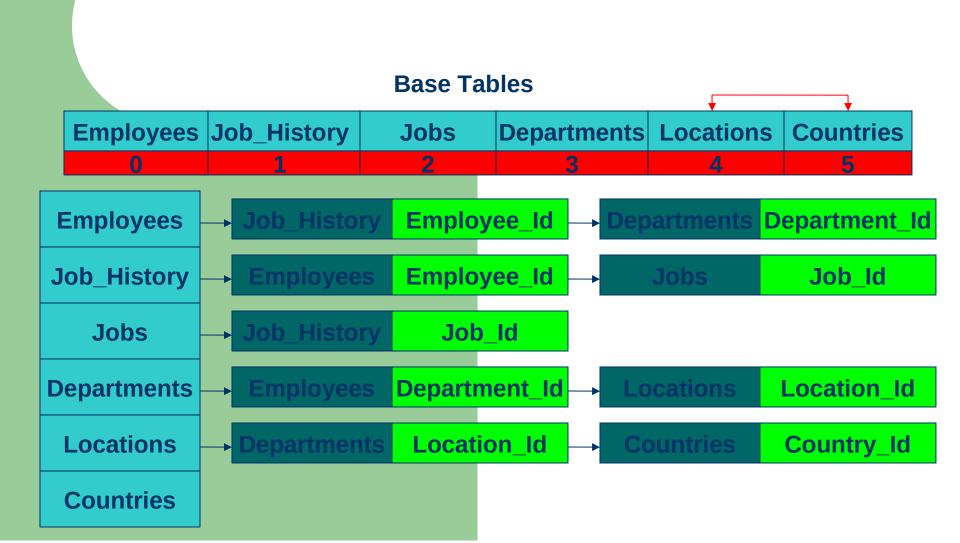
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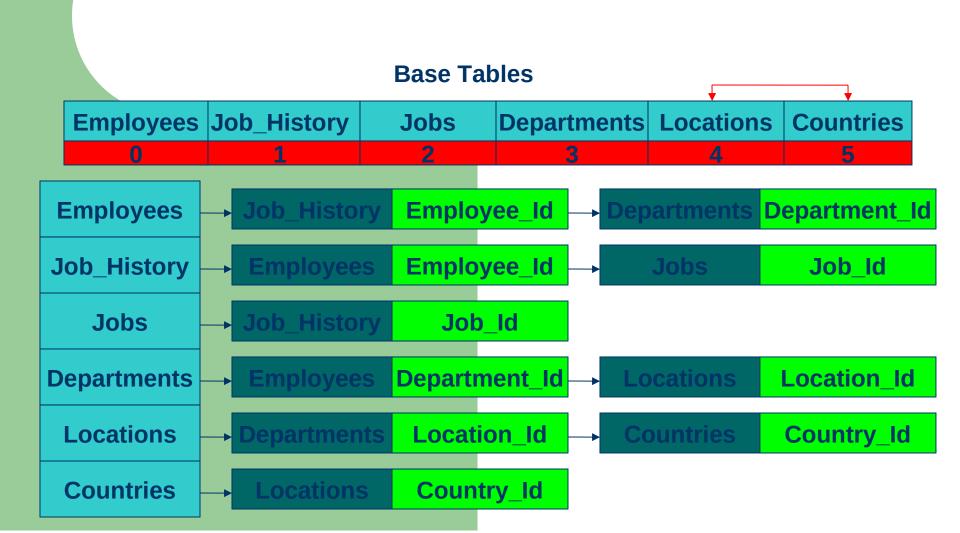


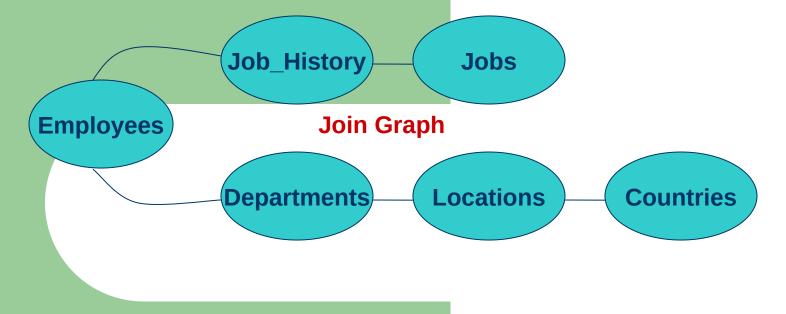
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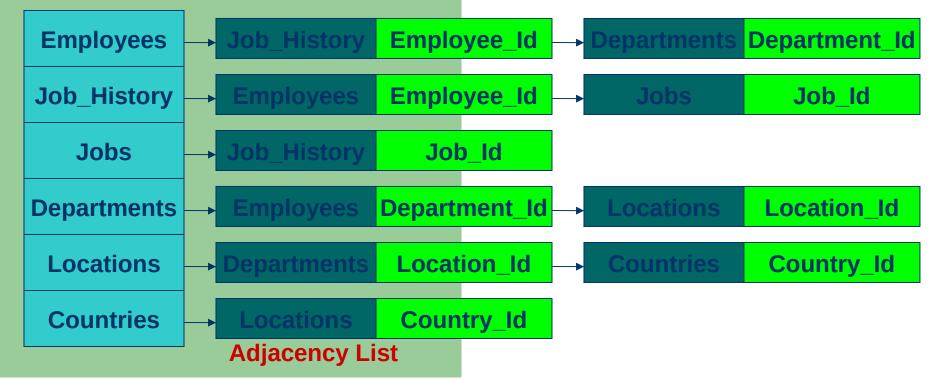
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Linked List representation of the Join Graph



Definitions

Join Path List:

A sequence of tables $T_0...T_{n-1}$ is in the Join Path List if every T_i of them is at least in direct join with another table in the sequence.

Notation

- When index i is not between brackets like in T_i , it represent a base table T_i .
- When index i is between brackets like in T_[i], it represent a base table T_i or a virtual table in which index i represent a set of indexes for the base tables forming the virtual table.

Steps to generate function: Key($T_{[j]}$) getFirstAdjacentListKey($T_{[j]}$, $T_{[k]}$)

for every Base Table T₁ in T₁₁₁ do

```
Take one at a time for every T_{Link(I)} do Take one at a time if T_{Link(I)} in T_{[k]} then return(key(T_I,T_{Link(I)}))
```

Normally one of the 2 tables $T_{[j]}$ or $T_{[k]}$ is a base table this is why we stop after founding the key.

Key could be a one column key or multicolumn key that satisfy the join condition.

Steps to generate Join Path List for the join sequence $T_0...T_m$

```
let T_0...T_m be the base tables
create 2 dynamic arrays queue and path
insert T₀ into path
insert T<sub>0</sub> into queue
repeat
    T<sub>Element</sub> = First Table in queue
    for every Link Item in Adjacent Link of T<sub>Element</sub> from the Join Graph do
         if the Link Item is in the join sequence then
              if path doesn't contain the Link Item then
                   insert Link Item into path
                   insert Link Item into queue
    remove T<sub>Element</sub> from queue
until queue is empty
```

Steps to generate Join Path List for the join sequence $T_0...T_{m \text{ (continue)}}$

```
insert all the names of base tables from path as vertexes in
   the JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do
    take one T<sub>i</sub> at a time
    PathJoinAdjacentList(T<sub>i</sub>) = T<sub>[buf]</sub>
    Key(T_i) = getFirstAdjacentListKey(T_i,T_{fbuff})
    PathJoinAdjacentList(T<sub>[buf]</sub>) = T<sub>i</sub>
    Key(T_{Ibufl}) = getFirstAdjacentListKey(T_{Ibufl}, T_i)
    T_{[buf]} + = T_i
    Insert NodesList[T_{fbufl}] = T_{fbufl}
```

Steps to generate Join Path List for the join sequence $T_0...T_{m \text{ (continue)}}$

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
    take one T<sub>iil</sub> at a time
    for all Base Tables in T<sub>111</sub> do
         take one T<sub>k</sub> at a time
         for every buf. Table = T<sub>k</sub> do
              if (buf.key != Key(T_{ii}) ) and (buf.Key not in InheritedKey(T_{ii})) then
                InheritedKey(T<sub>[ii]</sub>) += buf.key
    if T_1 is the table from which comes Key(T_{111}) then
         buf.Table = T_i
         buf.key = Key(T_{iii})
```



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

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Join Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
T 0	T ₁	T 2	T 3	T4	T 5

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let T₀...T_m be the base tables - create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Element} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Element} from queue until queue is empty path aueue

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Employees

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until queue is empty
                                         Join Graph
                                                                                    Department_Id
 Employees
                       Job History
                                          Employee_Id
                                                                   Departments
                                          Employee Id
 Job_History
                                                                                          Job Id
                       Job History
     Jobs
                                               Job Id
                                         Department_Id
                                                                   Locations
                                                                                      Location Id
Departments
                                                                                       Country_Id
  Locations
                       Departments
                                           Location Id
                                                                   Countries
  Countries
                       Locations
                                            Country_Id
```





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 $\label{eq:tempt} \mbox{remove $T_{\tt Element}$ from queue} \\ \mbox{until queue is empty}$

queue

Job_History

Departments

path

Employees

Job_History

Departments

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Element} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue **Employees** Job_History **Departments** Job_History **Departments**

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
create 2 dynamic arrays queue and path
insert T<sub>0</sub> into path
insert To into queue
repeat
     T<sub>Flement</sub> = First Table in queue
     for every Link Item in Adjacent Link of T<sub>Flement</sub> from the Join Graph do
           if the Link Item is in the join sequence then
                if path doesn't contain the Link Item then
                      insert Link Item into path
                      insert Link Item into queue
     remove T<sub>Flement</sub> from queue
until queue is empty
                                         Join Graph
 Employees
                       Job History
                                          Employee Id
                                                                   Departments
                                                                                    Department_Id
                                          Employee Id
                                                                       Jobs
 Job_History
                                                                                          Job Id
                       Job History
     Jobs
                                              Job Id
                                         Department_Id
                                                                   Locations
                                                                                      Location Id
Departments
                                                                                       Country_Id
  Locations
                       Departments
                                           Location Id
                                                                   Countries
  Countries
                       Locations
                                            Country_Id
```





generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Flement} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue Job_History **Employees** Job_History **Departments Departments** Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Flement} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue Job_History **Employees** Job_History **Departments** Jobs **Departments** Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert T_0 into path insert T_0 into queue repeat $T_{Element} = First \ Table \ in \ queue$ for every Link Item in Adjacent Link of $T_{Element}$ from the Join Graph do if the Link Item is in the join sequence then

if path doesn't contain the Link Item then

insert Link Item into path

insert Link Item into queue remove T_{Element} from queue

until queue is empty

queue

Departments

Jobs

path

Employees

Job_History

Departments

Jobs

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Element} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue **Employees Departments** Jobs Job_History **Departments** Jobs

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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                      insert Link Item into path
                      insert Link Item into queue
     remove T<sub>Flement</sub> from queue
until queue is empty
                                         Join Graph
 Employees
                       Job History
                                          Employee Id
                                                                   Departments
                                                                                    Department_Id
                                          Employee_Id
                                                                       Jobs
 Job_History
                                                                                          Job Id
                       Job History
     Jobs
                                              Job Id
                                         Department_Id
                                                                   Locations
                                                                                      Location Id
Departments
                                                                                       Country_Id
  Locations
                       Departments
                                           Location Id
                                                                   Countries
  Countries
                       Locations
                                            Country_Id
```





generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Flement} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue **Departments Employees** Jobs Job_History **Departments** Jobs Locations

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
create 2 dynamic arrays queue and path
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                  if path doesn't contain the Link Item then
                        insert Link Item into path
                        insert Link Item into queue
      remove T<sub>Flement</sub> from queue
until queue is empty
                                                                                 path
                                         queue
                                                                            Employees
                                     Departments
                                                                            Job_History
                                          Jobs
                                       Locations
                                                                           Departments
                                                                                 Jobs
                                                                             Locations
```

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let T_0...T_m be the base tables create 2 dynamic arrays queue and path insert T_0 into path insert T_0 into queue repeat

T_{Element} = First Table in queue
for every Link Item in Adjacent Link of T_{Element} from the Join Graph do if the Link Item is in the join sequence then
```

for every Link Item in Adjacent Link of T_{Element} from the Join Graph of if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue

remove T_{Element} from queue until queue is empty

queue

Jobs

Locations

path

Employees

Job_History

Departments

Jobs

Locations

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Flement} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue **Employees** Jobs Locations Job_History **Departments** Jobs Locations

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
create 2 dynamic arrays queue and path
insert T<sub>0</sub> into path
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           if the Link Item is in the join sequence then
                if path doesn't contain the Link Item then
                      insert Link Item into path
                      insert Link Item into queue
     remove T<sub>Flement</sub> from queue
until queue is empty
                                         Join Graph
 Employees
                       Job History
                                          Employee Id
                                                                    epartments
                                                                                    Department_Id
                                          Employee Id
                                                                       Jobs
 Job_History
                                                                                          Job Id
                       Job History
     Jobs
                                               Job Id
                                         Department_Id
                                                                   Locations
                                                                                      Location Id
Departments
                                                                                       Country_Id
  Locations
                       Departments
                                           Location Id
                                                                   Countries
  Countries
                       Locations
                                            Country_Id
```





remove T_{Element} from queue until queue is empty

queue

Locations

path

Employees

Job_History

Departments

Jobs

Locations

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
create 2 dynamic arrays queue and path
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            if the Link Item is in the join sequence then
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                         insert Link Item into path
                         insert Link Item into queue
      remove T<sub>Flement</sub> from queue
until queue is empty
                                                                                   path
                                          queue
                                                                              Employees
                                        Locations
                                                                             Job_History
                                                                             Departments
                                                                                   Jobs
                                                                               Locations
```

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
create 2 dynamic arrays queue and path
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                      insert Link Item into path
                      insert Link Item into queue
     remove T<sub>Flement</sub> from queue
until queue is empty
                                         Join Graph
 Employees
                       Job History
                                          Employee Id
                                                                   Departments
                                                                                    Department_Id
                                          Employee_Id
                                                                       Jobs
 Job_History
                                                                                          Job Id
                       Job History
     Jobs
                                              Job Id
                                         Department_Id
                                                                   Locations
                                                                                      Location Id
Departments
                                                                                       Country_Id
  Locations
                       Departments
                                           Location Id
                                                                   Countries
  Countries
                        Locations
                                            Country_Id
```





```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
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      T<sub>Flement</sub> = First Table in queue
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                   if path doesn't contain the Link Item then
                         insert Link Item into path
                         insert Link Item into queue
      remove T<sub>Element</sub> from queue
until queue is empty
                                                                                  path
                                         queue
                                                                             Employees
                                       Locations
                                                                             Job_History
                                                                            Departments
                                                                                  Jobs
                                                                              Locations
                                                                              Countries
```

generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList) let $T_0...T_m$ be the base tables create 2 dynamic arrays queue and path insert To into path insert To into queue repeat **T**_{Flement} = First Table in queue for every Link Item in Adjacent Link of T_{Element} from the Join Graph do if the Link Item is in the join sequence then if path doesn't contain the Link Item then insert Link Item into path insert Link Item into queue remove T_{Flement} from queue until queue is empty path queue Locations **Employees** Job_History Countries **Departments** Jobs Locations **Countries**

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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                         insert Link Item into path
                         insert Link Item into queue
      remove T<sub>Flement</sub> from queue
until queue is empty
                                          queue
                                                                               Employees
                                         Countries
                                                                               Job_History
                                                                              Departments
```

path

Jobs

Locations

Countries

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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                         insert Link Item into queue
      remove T<sub>Flement</sub> from queue
until queue is empty
                                                                                  path
                                         queue
                                                                             Employees
                                       Countries
                                                                             Job_History
                                                                            Departments
                                                                                  Jobs
                                                                              Locations
                                                                              Countries
```

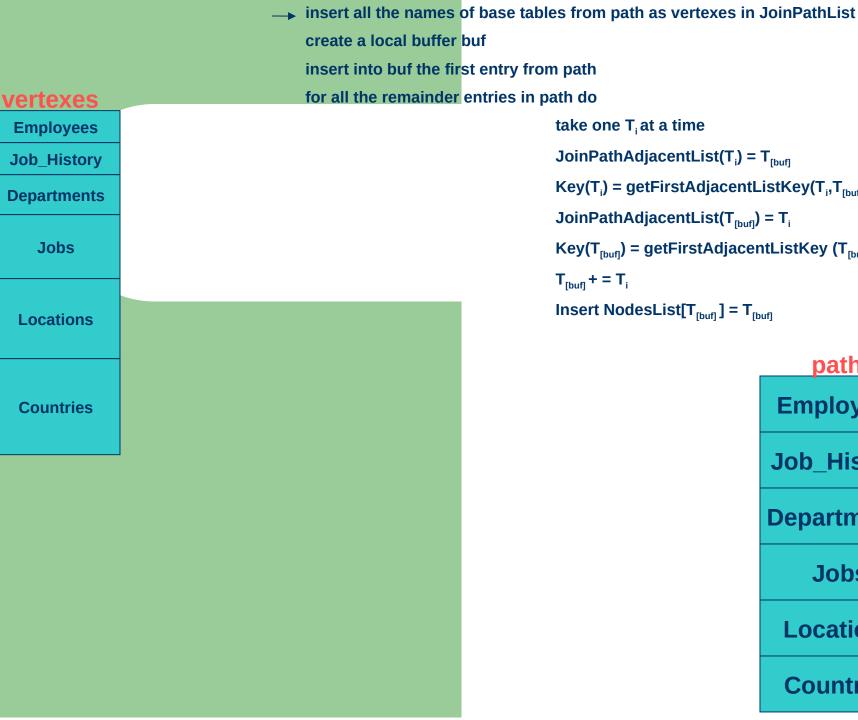
```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T_0...T_m be the base tables
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     remove T<sub>Flement</sub> from queue
until queue is empty
                                         Join Graph
 Employees
                       Job History
                                          Employee_Id
                                                                   Departments
                                                                                    Department_Id
                                          Employee_Id
                                                                       Jobs
 Job_History
                                                                                          Job Id
                       Job History
     Jobs
                                              Job Id
                                         Department_Id
                                                                   Locations
                                                                                      Location Id
Departments
                                                                                       Country_Id
  Locations
                       Departments
                                           Location Id
                                                                   Countries
  Countries
                        Locations
                                            Country_Id
```





```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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      remove T<sub>Element</sub> from queue
until queue is empty
                                                                                   path
                                          queue
                                                                              Employees
                                                                             Job_History
                                                                             Departments
                                                                                   Jobs
                                                                               Locations
                                                                               Countries
```

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
    let T_0...T_m be the base tables
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                       if path doesn't contain the Link Item then
                             insert Link Item into path
                             insert Link Item into queue
          remove T<sub>Element</sub> from queue
→ until queue is empty
                                                                                       path
                                              queue
                                                                                  Employees
                                                                                 Job_History
                                                                                 Departments
                                                                                       Jobs
                                                                                   Locations
                                                                                   Countries
```



take one T_i at a time $JoinPathAdjacentList(T_i) = T_{[buf]}$ $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fbuff})$ JoinPathAdjacentList(T_[huf]) = T_i $Key(T_{[buf]}) = getFirstAdjacentListKey(T_{[buf]},T_i)$ $T_{\text{[buf]}} + = T_{\text{i}}$ Insert NodesList[T_{fbufl}] = T_{fbufl}

path

Employees

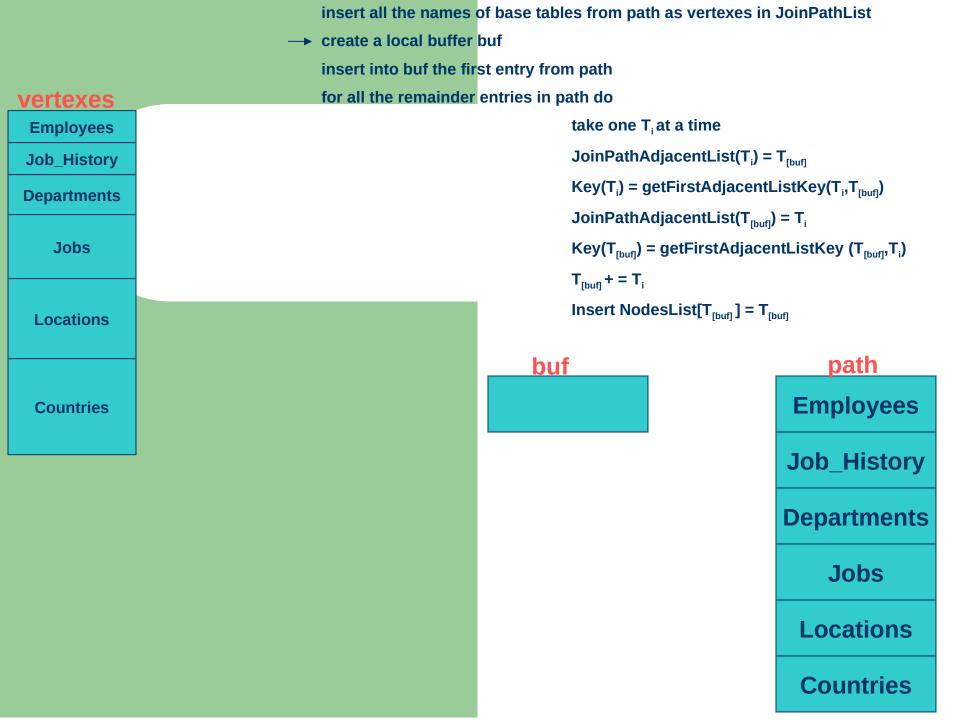
Job_History

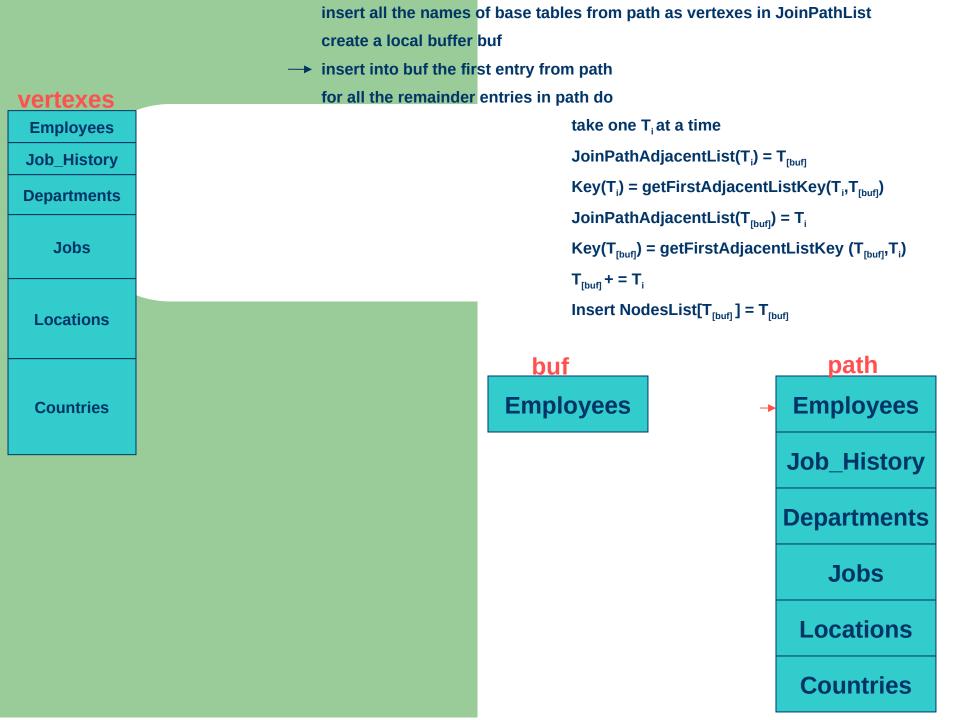
Departments

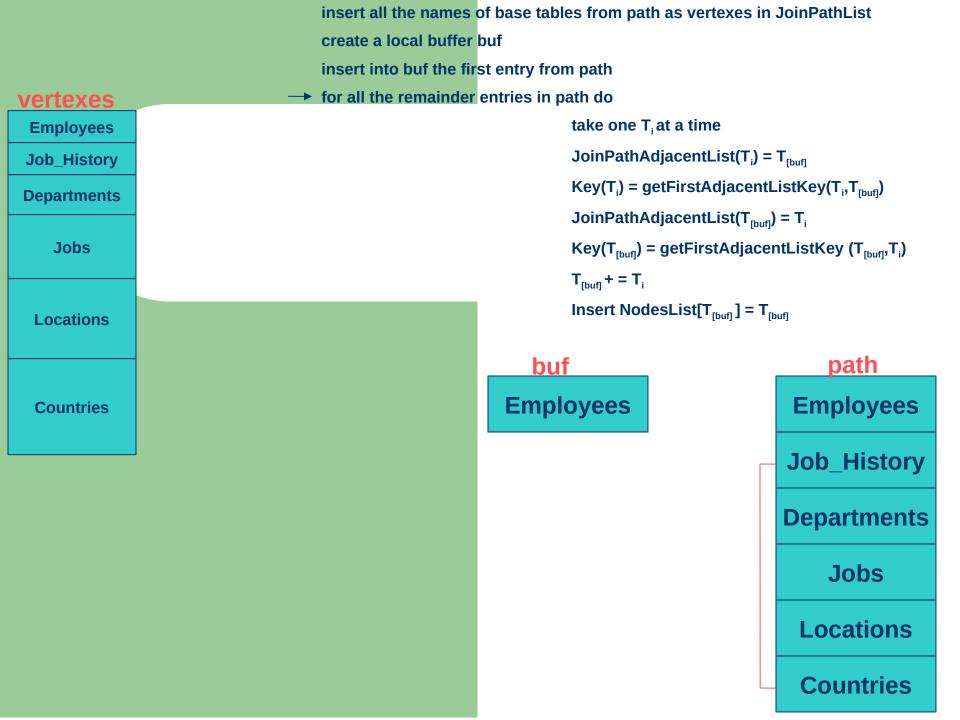
Jobs

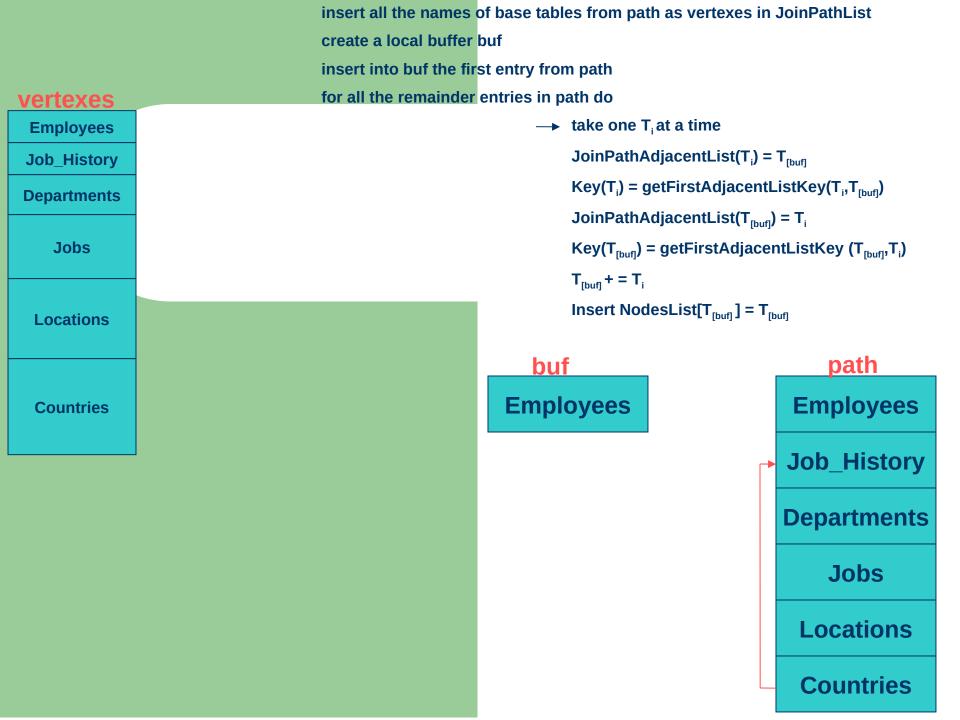
Locations

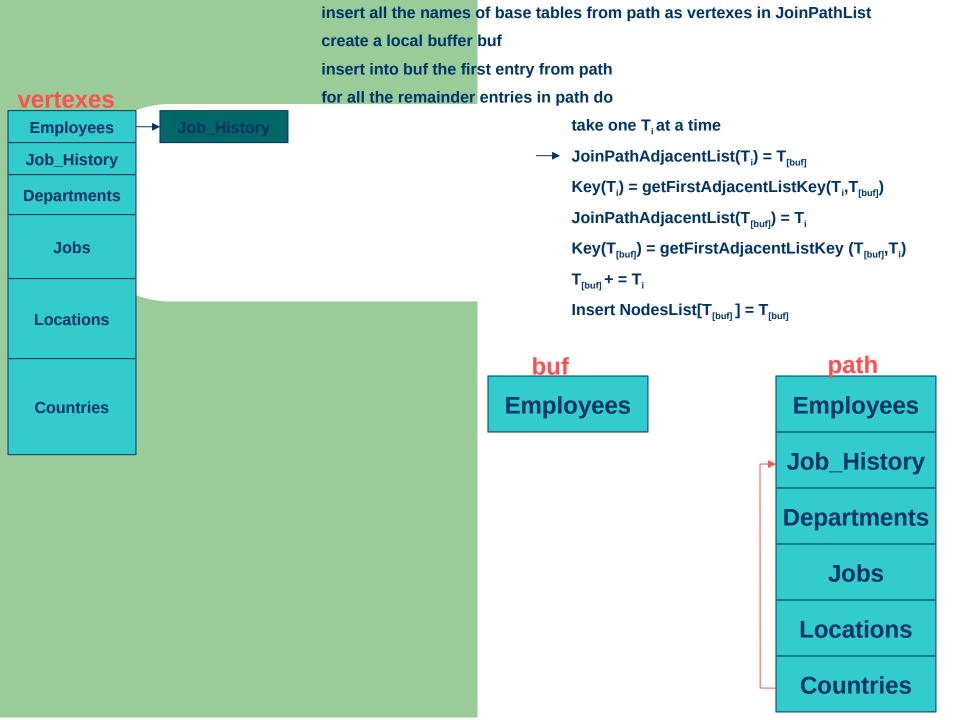
Countries

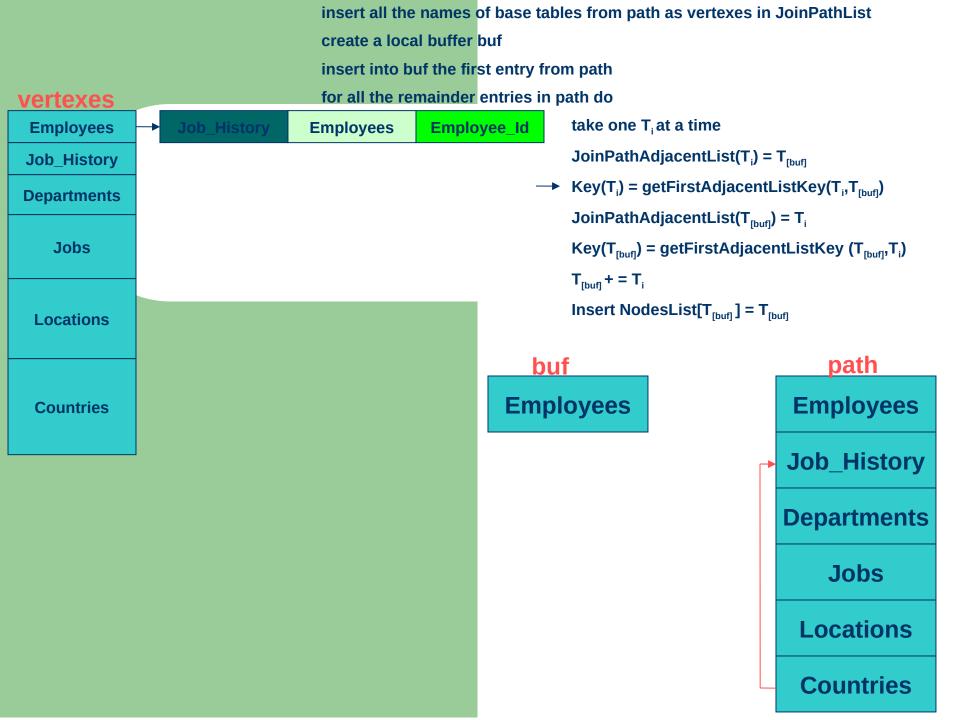


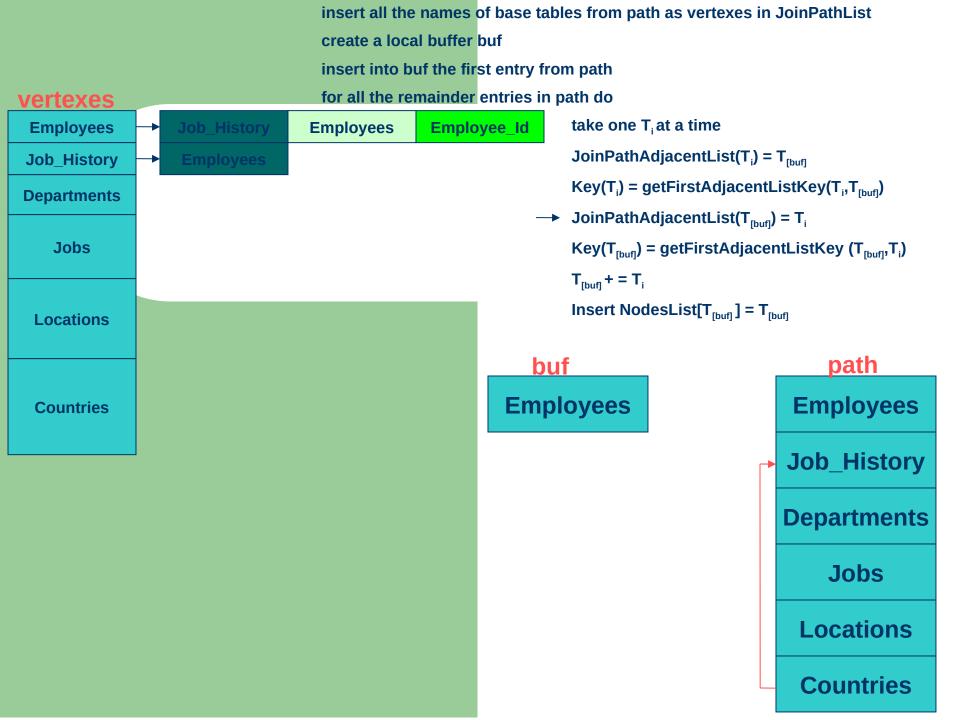


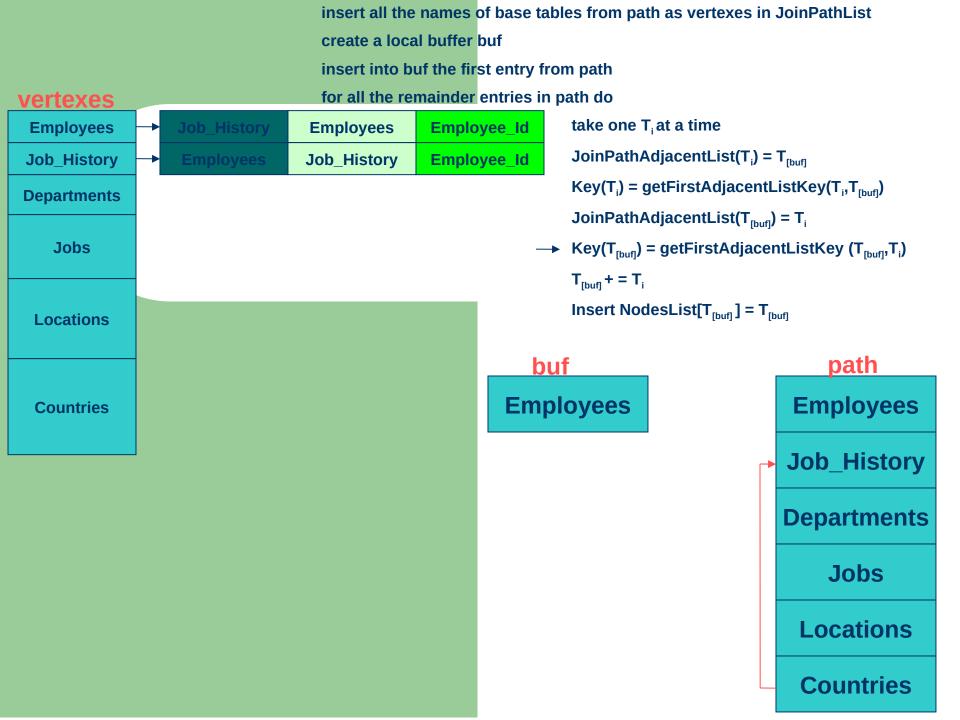


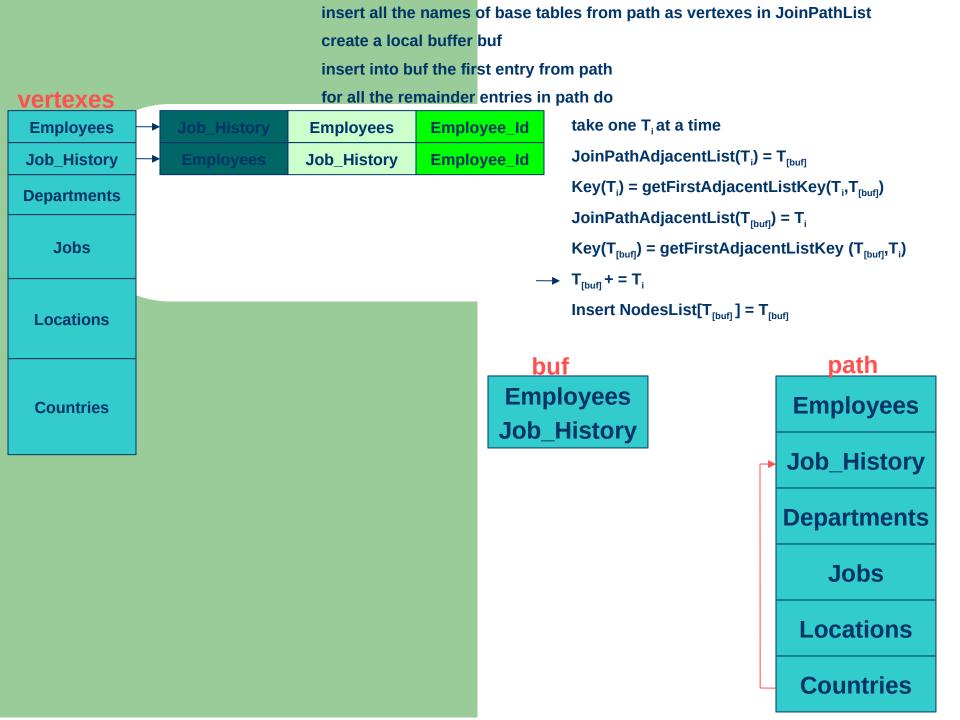


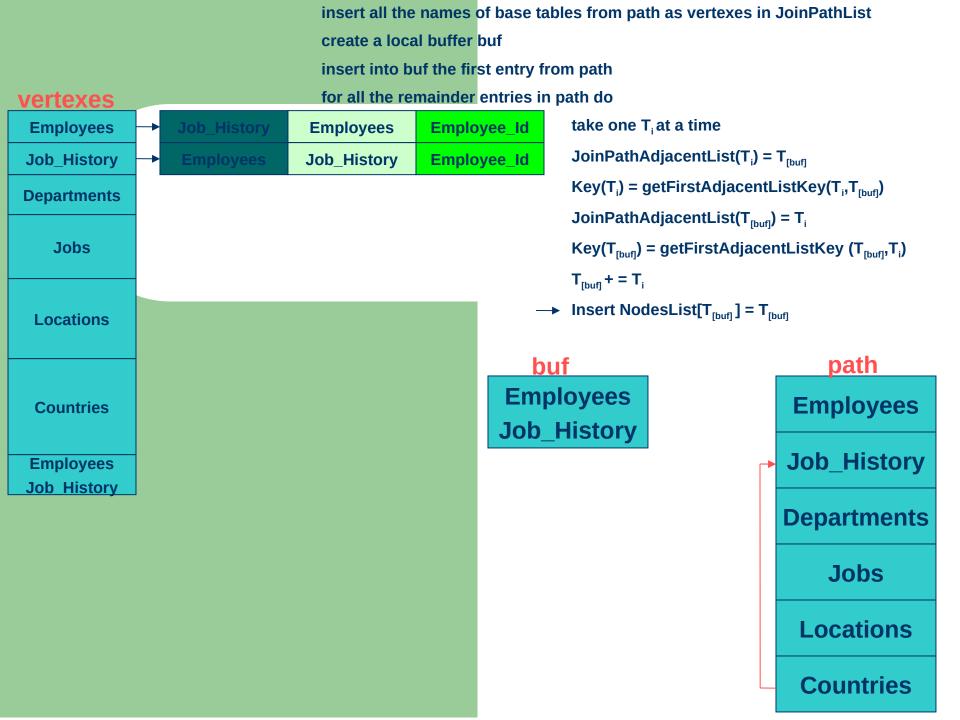


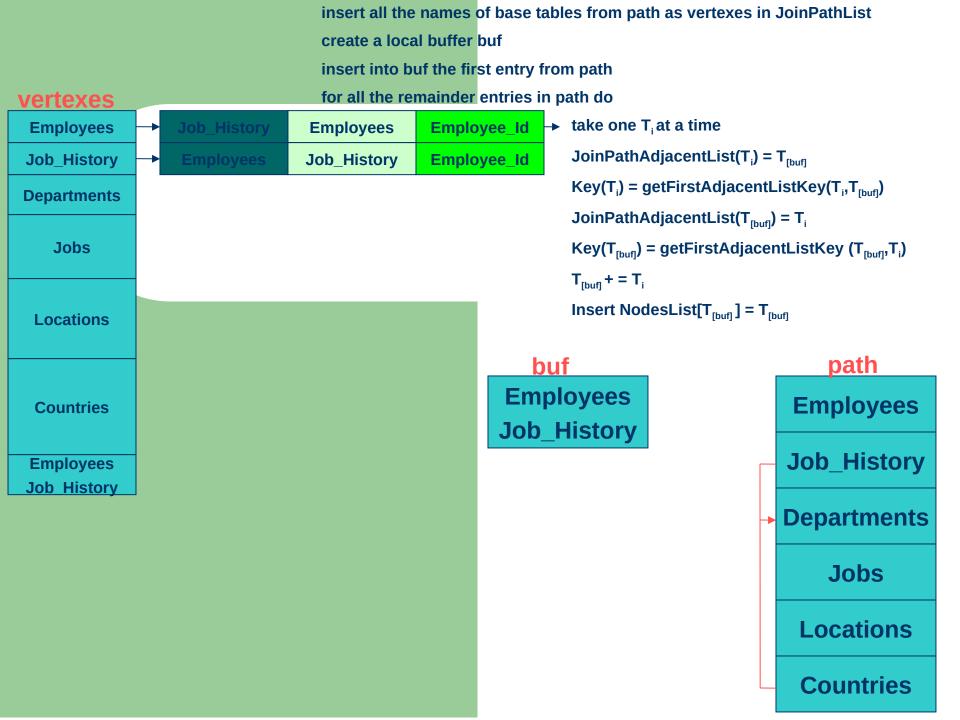


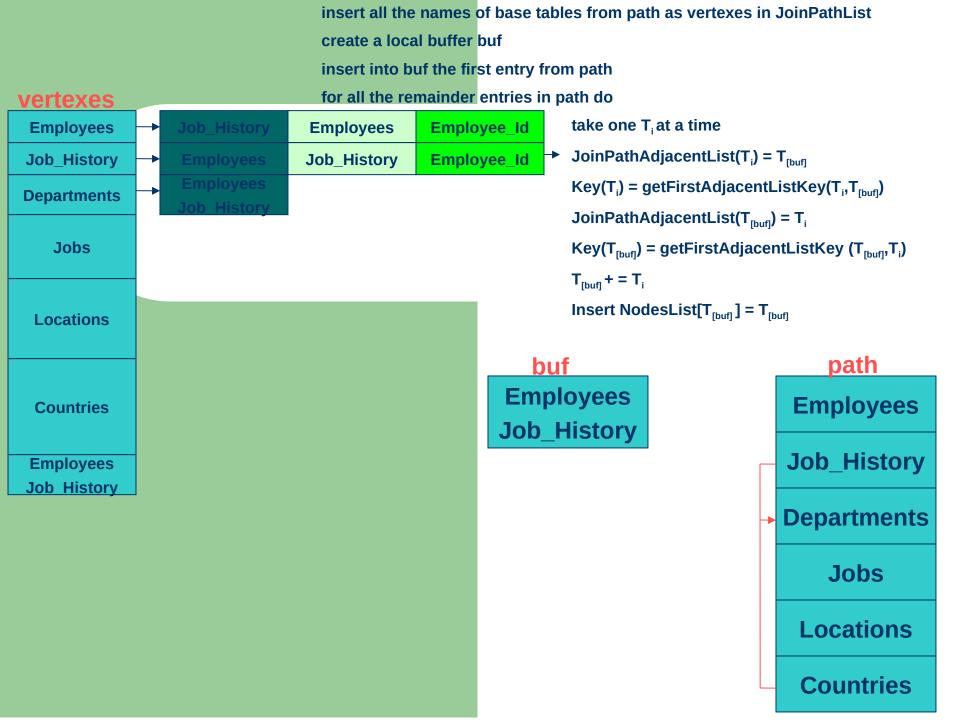


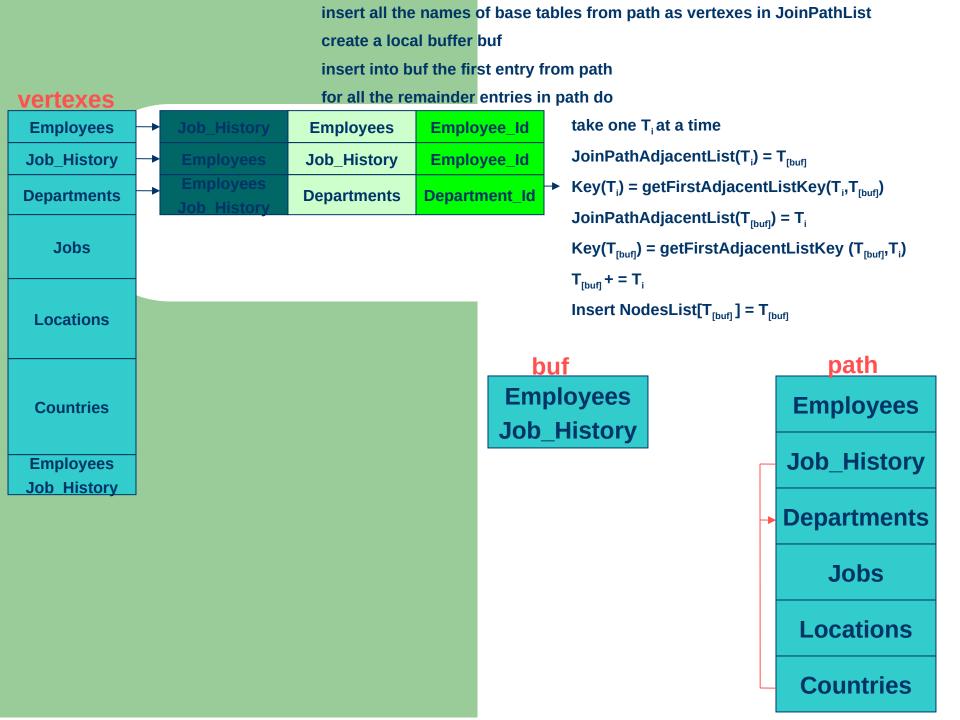


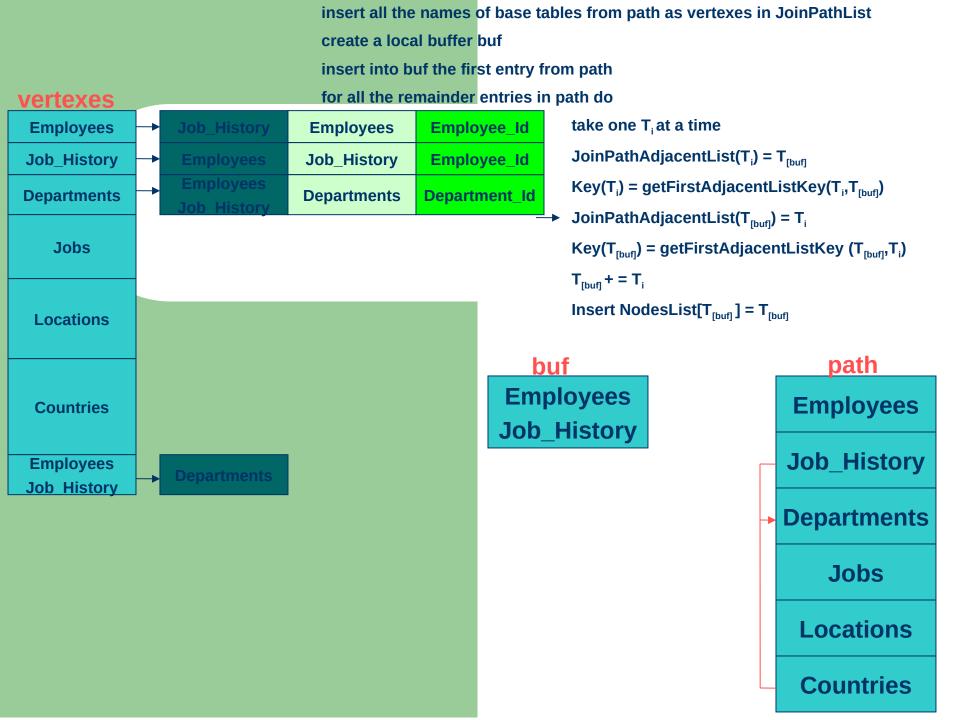


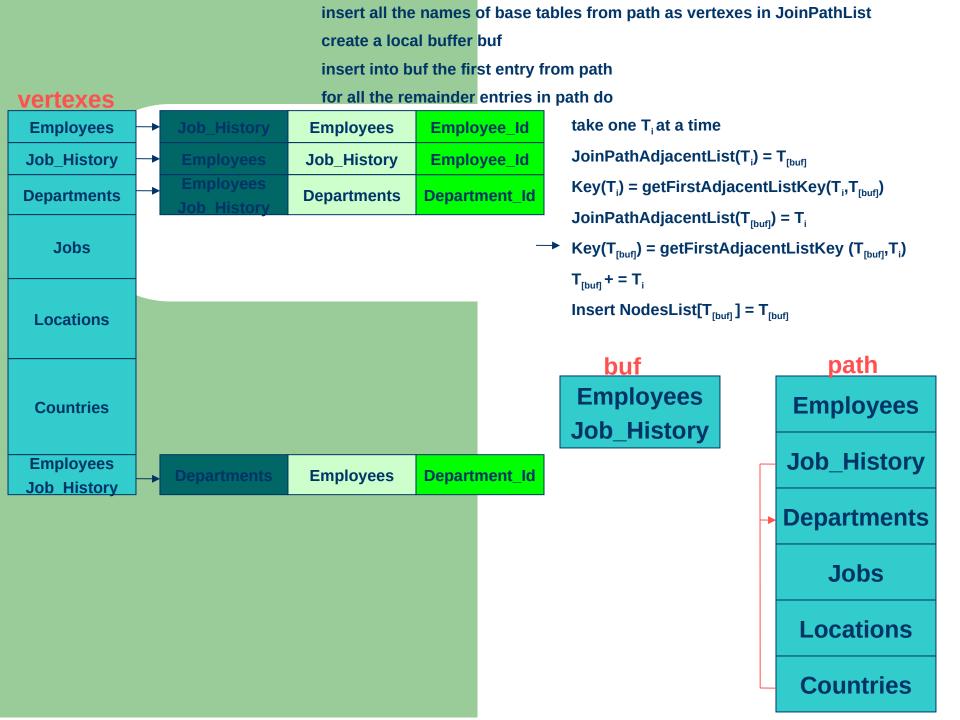


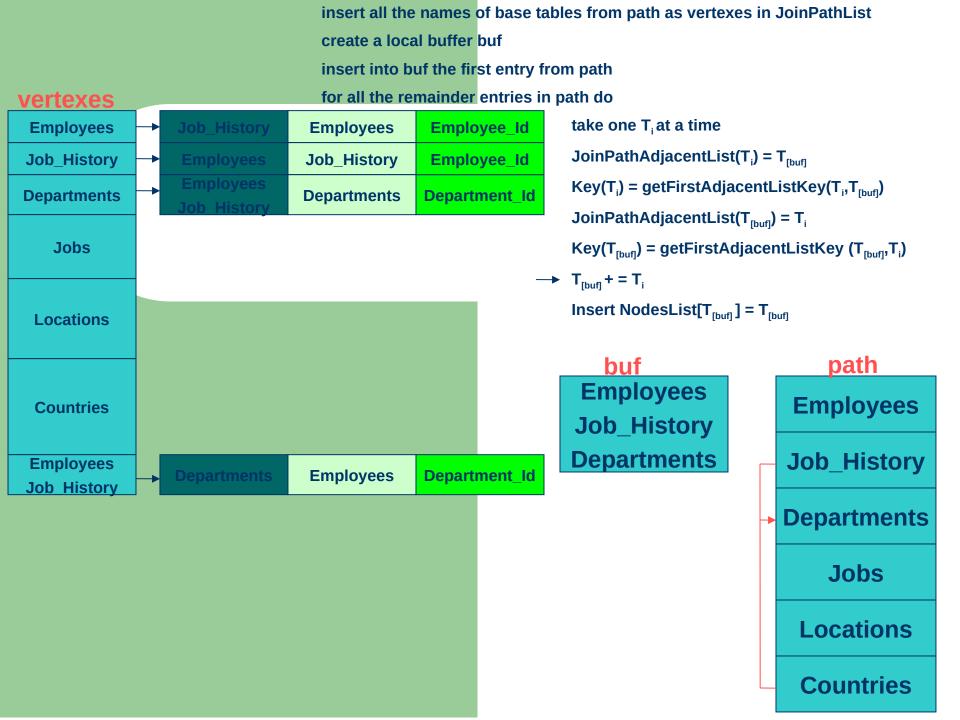


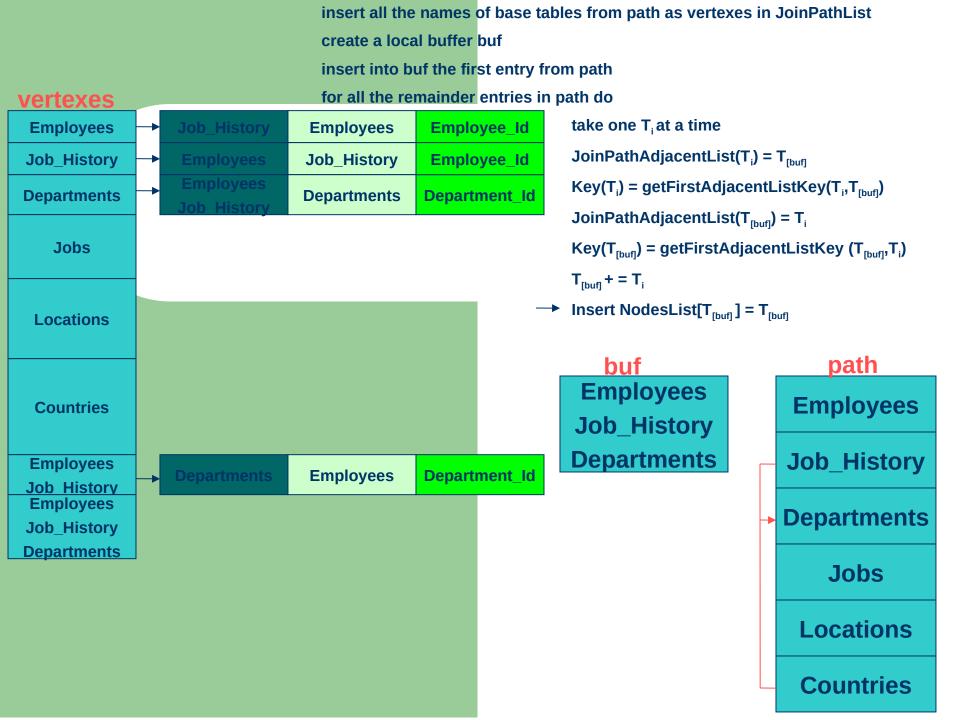


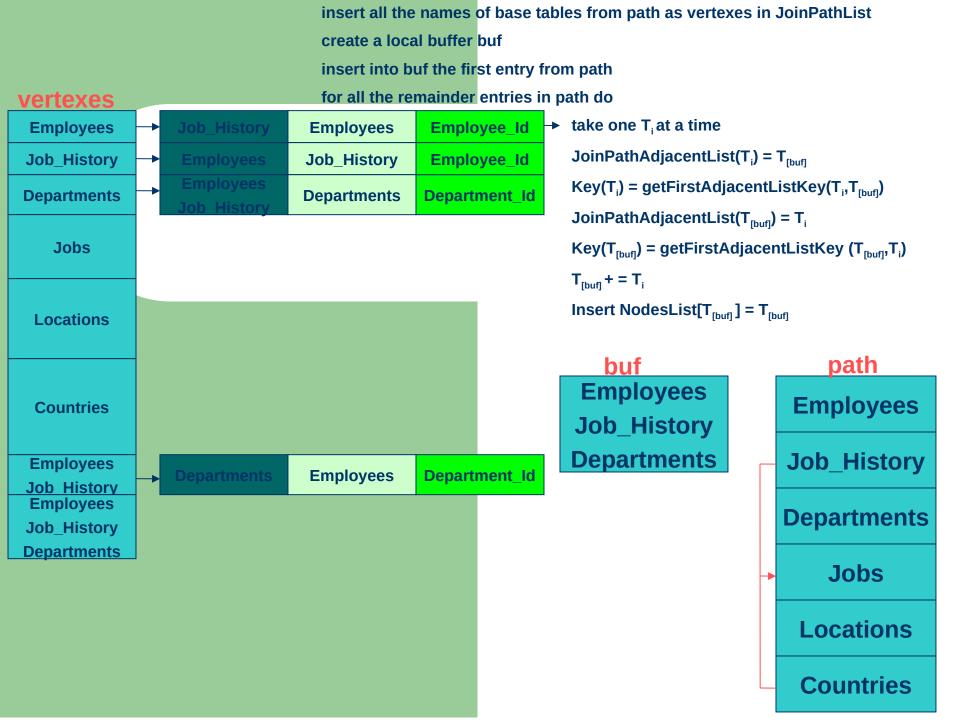


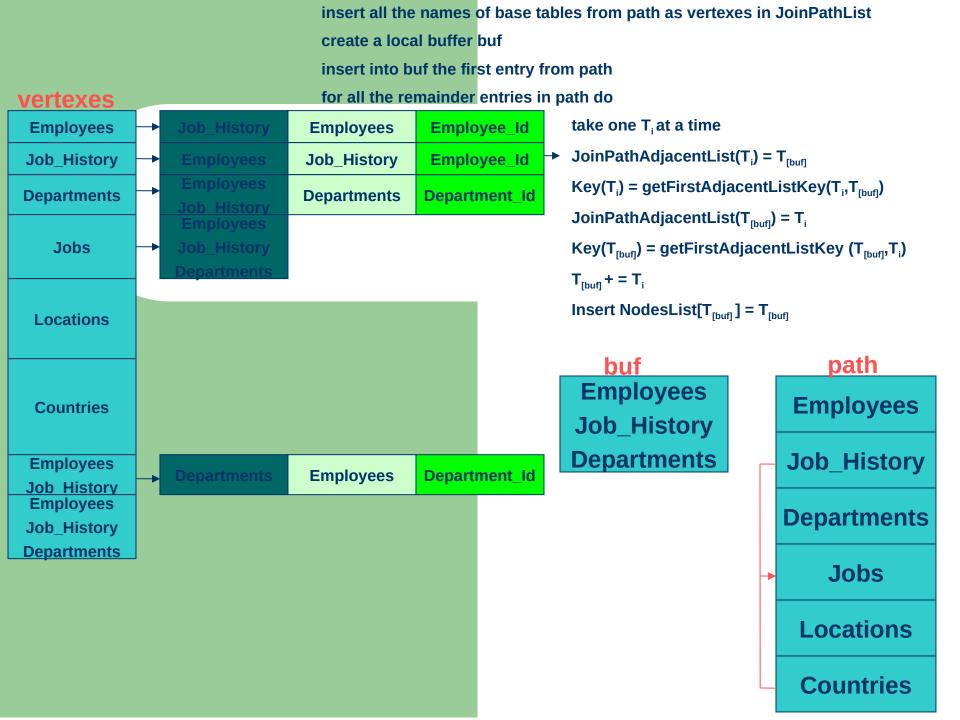


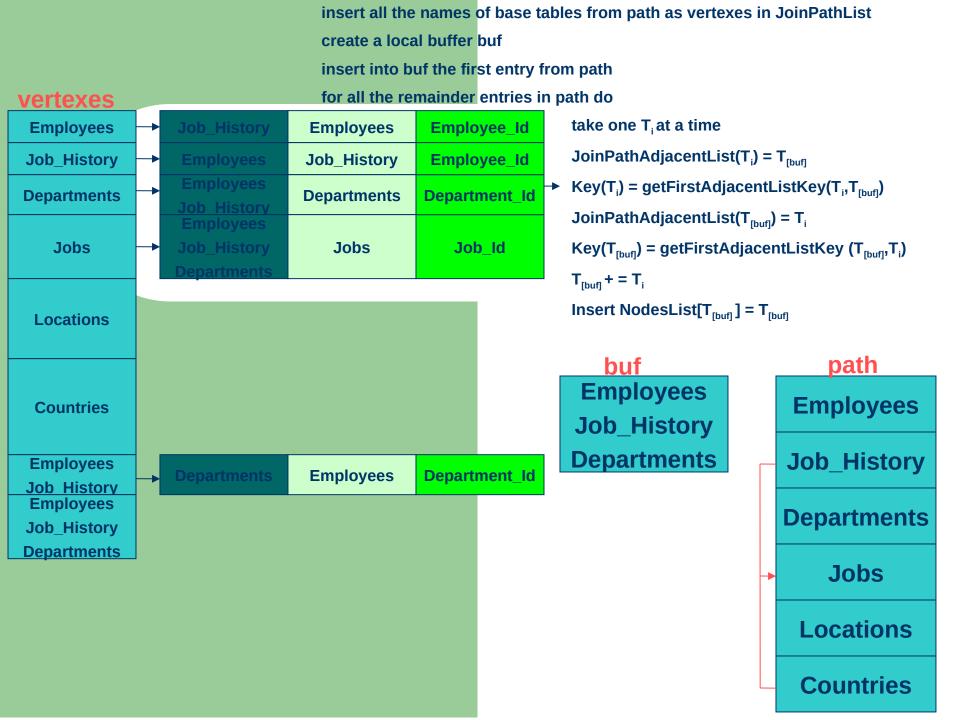


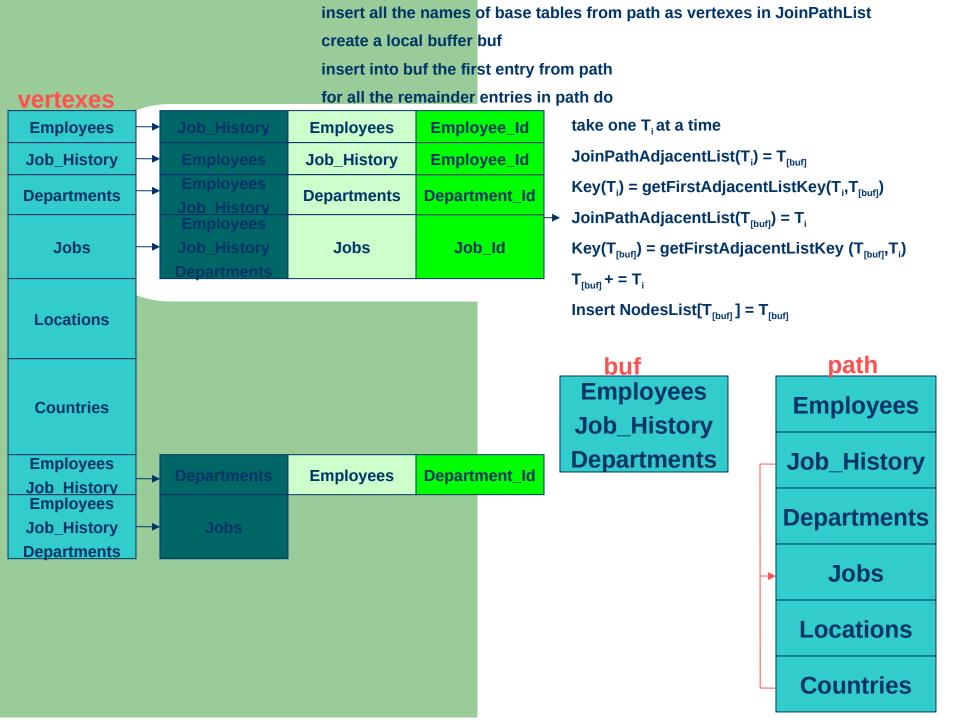


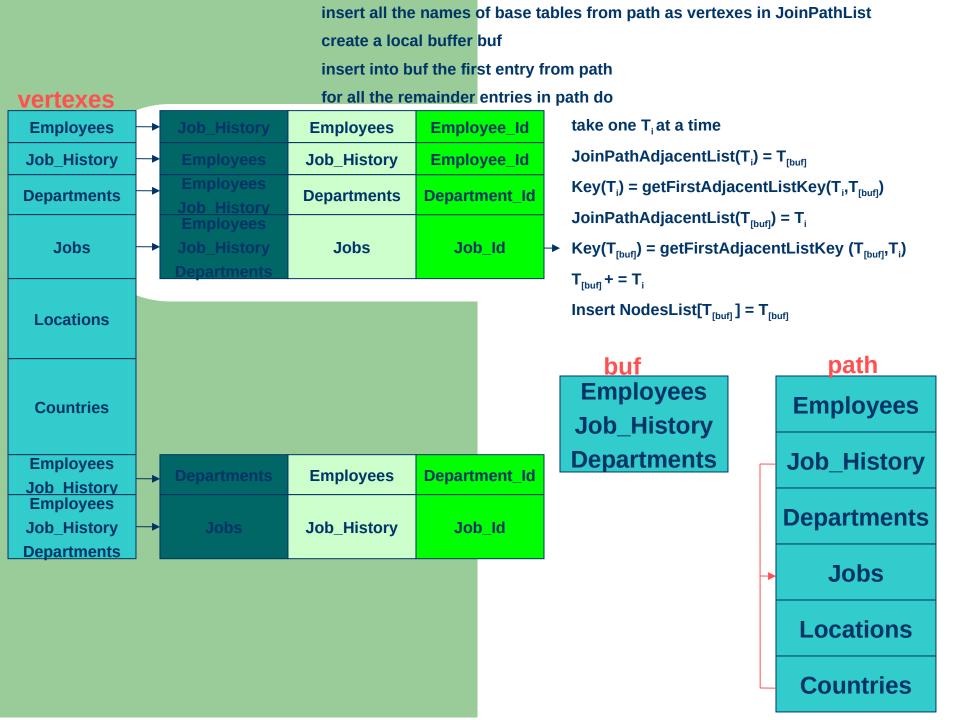


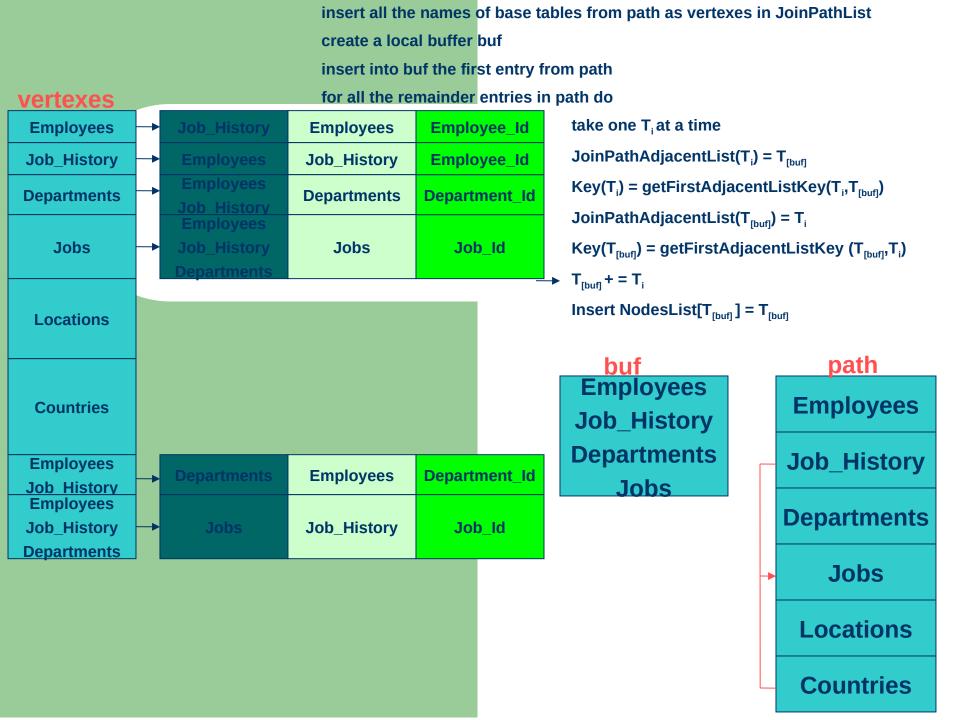


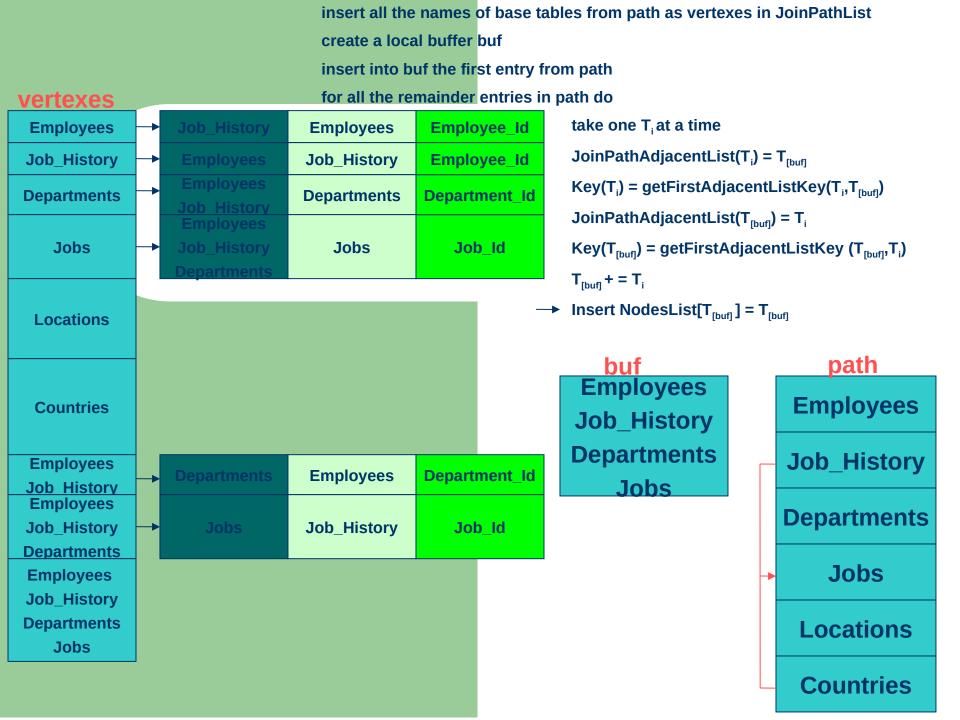


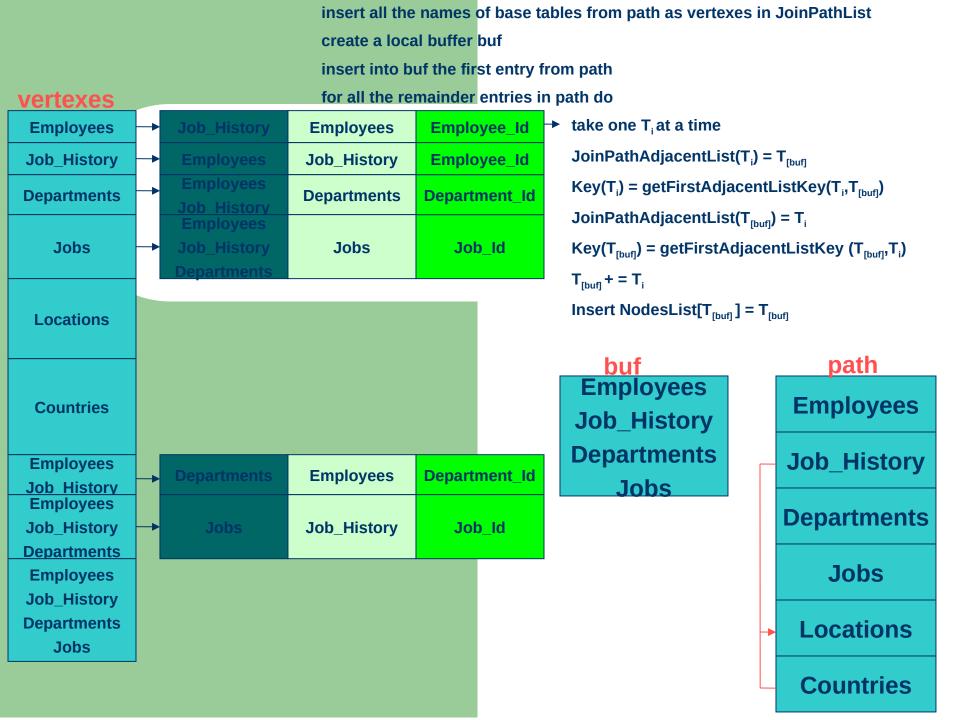


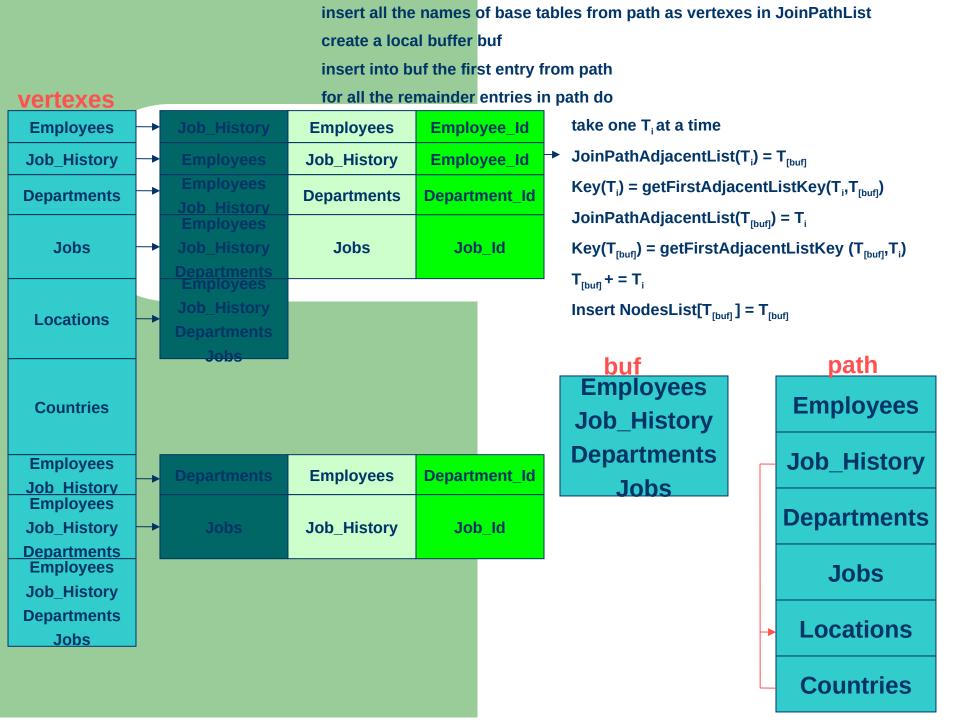


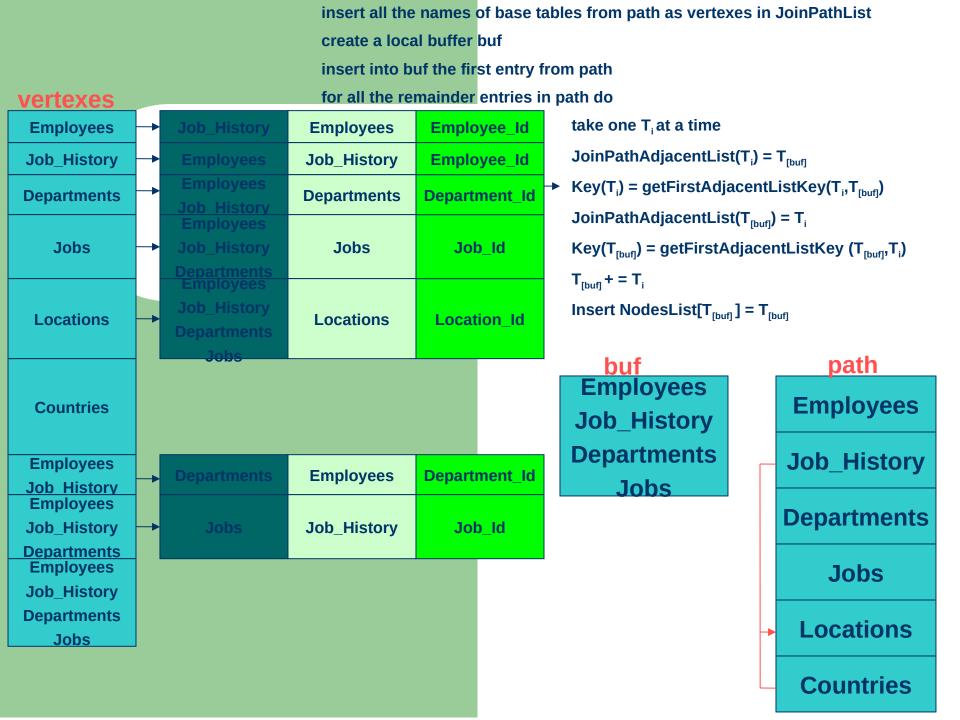


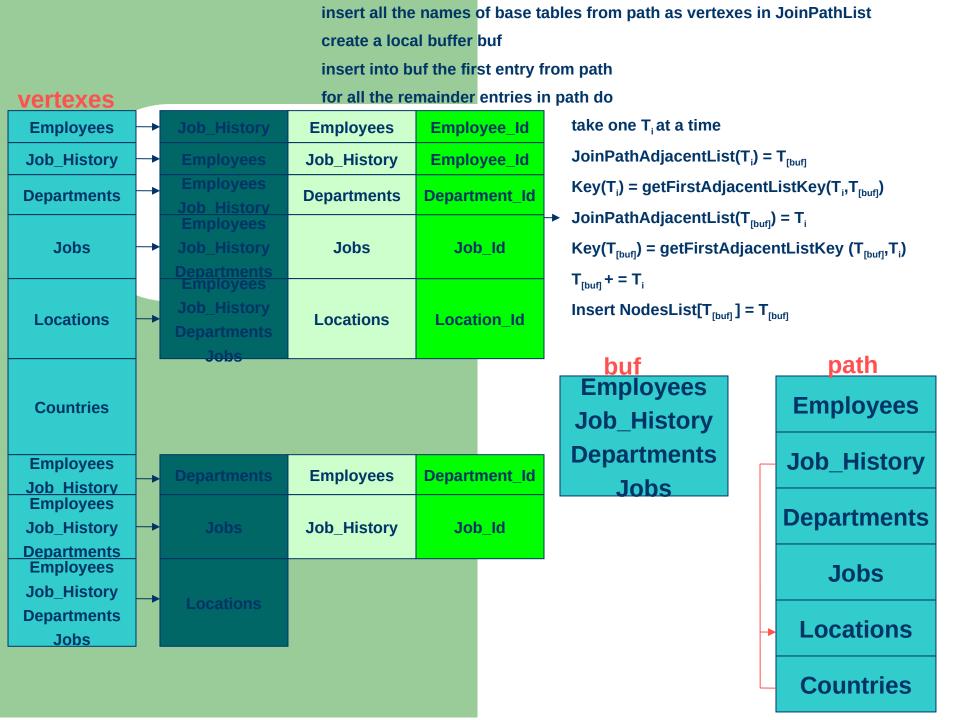


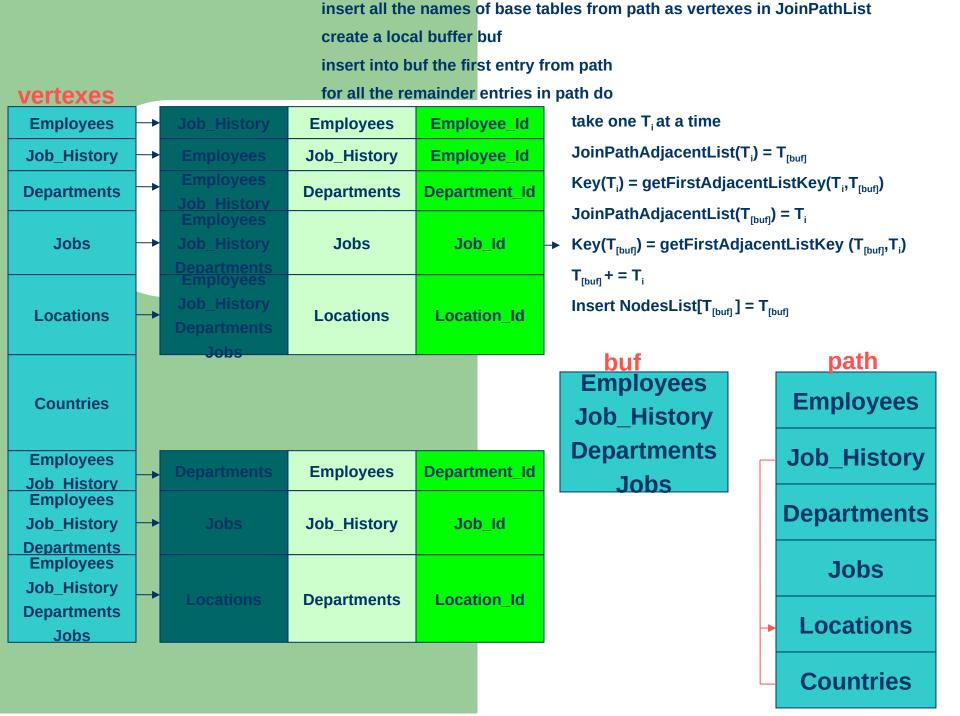


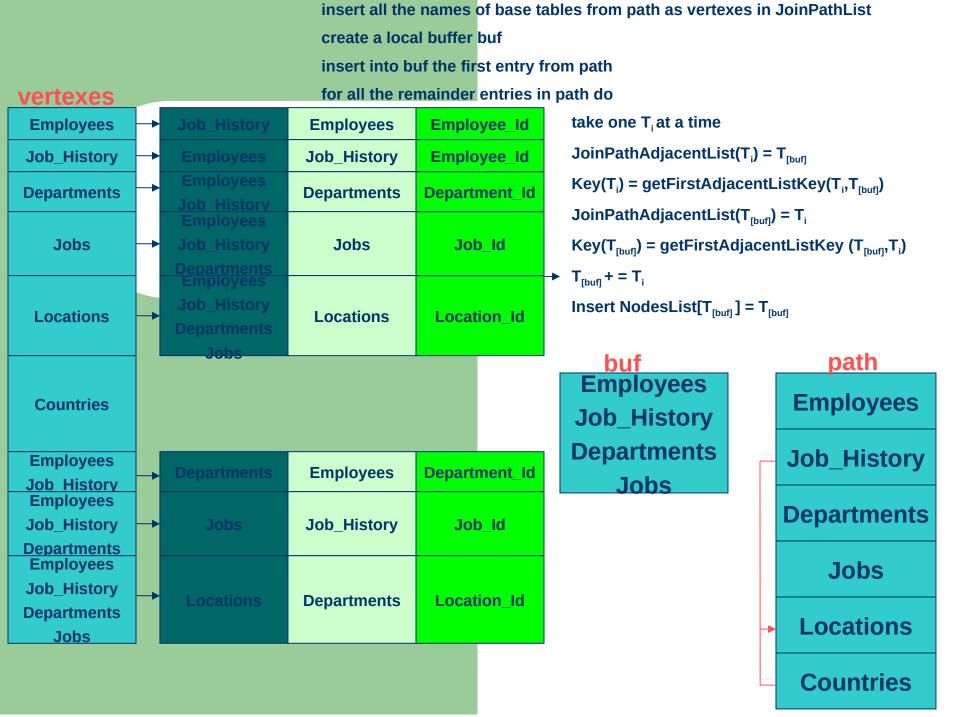




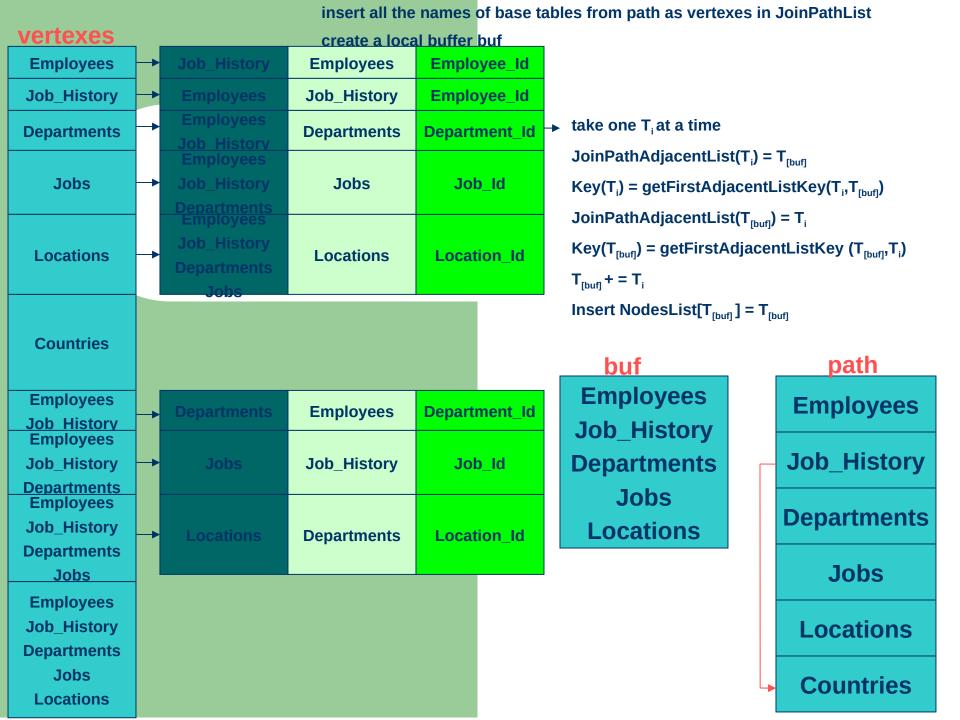








insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History Job History Employee Id** take one Ti at a time **Departments Departments** Department Id $JoinPathAdjacentList(T_i) = T_{Ibufl}$ Jobs **Jobs** Job Id $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fourf})$ JoinPathAdjacentList(T_[buf]) = T_i $Key(T_{fourt}) = getFirstAdjacentListKey(T_{fourt},T_i)$ **Location Id** Locations Locations $T_{\text{fbufl}} + = T_{\text{i}}$ Insert NodesList[T_{fbuff}] = T_{fbuff} Countries path buf **Employees Employees Employees** Department Id **Employees Job History** Job_History **Employees** Job History **Departments Job History** Job Id **Job History Departments** Jobs **Employees Departments** Job History Locations **Departments Location Id Departments** Jobs Jobs **Employees Job History** Locations **Departments Jobs Countries** Locations



insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History** Job History **Employee Id** take one Ti at a time **Departments Departments** Department Id JoinPathAdjacentList(T_i) = T_{Ibufl} **Jobs Jobs** Job Id $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fourf})$ JoinPathAdjacentList(T_[buf]) = T_i $Key(T_{fourt}) = getFirstAdjacentListKey(T_{fourt},T_i)$ **Location Id** Locations Locations $T_{\text{fbufl}} + = T_{\text{i}}$ Insert NodesList[T_{fbuff}] = T_{fbuff} **Countries** path buf **Employees Employees Employees Employees** Department Id **Job History** Job_History **Employees Job History Departments Job History** Job Id **Job History Departments** Jobs **Employees Departments** Job_History Locations **Departments Location Id Departments** Jobs Jobs **Employees Job History** Locations **Departments Jobs Countries** Locations

insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History Job History Employee Id** take one Ti at a time **Departments Departments** Department Id $JoinPathAdjacentList(T_i) = T_{Ibufl}$ **Jobs Jobs** Job Id → Key(T_i) = getFirstAdjacentListKey(T_i,T_[buf]) $JoinPathAdjacentList(T_{Ibufl}) = T_i$ $Key(T_{fourt}) = getFirstAdjacentListKey(T_{fourt},T_i)$ **Location Id** Locations Locations $T_{\text{fbufl}} + = T_{\text{i}}$ Insert NodesList[T_{fbuff}] = T_{fbuff} **Countries Countries** Country Id path buf **Employees Employees Employees** Department Id **Employees Job History** Job_History **Employees** Job History **Departments Job History** Job Id **Job History Departments** Jobs **Employees Departments** Job_History Locations **Departments Location Id Departments** Jobs Jobs **Employees Job History** Locations **Departments Jobs Countries** Locations

insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History Job History Employee Id** take one Ti at a time **Departments Departments** Department Id $JoinPathAdjacentList(T_i) = T_{Ibufl}$ **Jobs Jobs** Job Id $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fourf})$ JoinPathAdjacentList(T_[huf]) = T_i $Key(T_{fourt}) = getFirstAdjacentListKey(T_{fourt},T_i)$ **Location Id** Locations Locations $T_{\text{fbufl}} + = T_{\text{i}}$ Insert NodesList[T_{fbuff}] = T_{fbuff} **Countries Countries** Country Id path buf **Employees Employees Employees** Department Id **Employees Job History** Job_History **Employees Job History Departments Job History** Job Id **Job History Departments** Jobs **Employees Departments** Job_History Locations **Departments Location Id Departments** Jobs Jobs **Employees Job History** Locations **Departments Jobs Countries** Locations

insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History** Job History **Employee Id** take one Ti at a time **Departments Departments** Department Id $JoinPathAdjacentList(T_i) = T_{Ibufl}$ **Jobs Jobs** Job Id $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fourf})$ $JoinPathAdjacentList(T_{Ibufl}) = T_i$ Key(T_[buf]) = getFirstAdjacentListKey (T_[buf],T_i) **Location Id** Locations Locations $T_{\text{fbufl}} + = T_{\text{i}}$ Insert NodesList[T_{fbuff}] = T_{fbuff} **Countries Countries** Country Id path buf **Employees Employees Employees** Department Id **Employees Job History** Job_History **Employees Job History Departments Job History** Job Id **Job History Departments** Jobs **Employees Departments** Job_History Locations **Departments Location Id Departments** Jobs Jobs **Employees Job History** Locations **Locations** Country Id **Departments Jobs**

Locations

Countries

insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History Job History Employee Id** take one Ti at a time **Departments Departments** Department Id $JoinPathAdjacentList(T_i) = T_{Ibufl}$ **Jobs Jobs** Job Id $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fourf})$ $JoinPathAdjacentList(T_{Ibufl}) = T_i$ $Key(T_{fourt}) = getFirstAdjacentListKey(T_{fourt},T_i)$ **Location Id** Locations Locations $T_{\text{[buf]}} + = T_{\text{i}}$ Insert NodesList[T_{fbuff}] = T_{fbuff} **Countries Countries** Country Id path buf **Employees Employees Employees** Department Id **Employees Job History** Job_History **Employees Job History Job History** Job Id **Job History Departments Departments Jobs Employees Departments** Job_History Locations **Departments Location Id Departments** Countries Jobs Jobs **Employees**

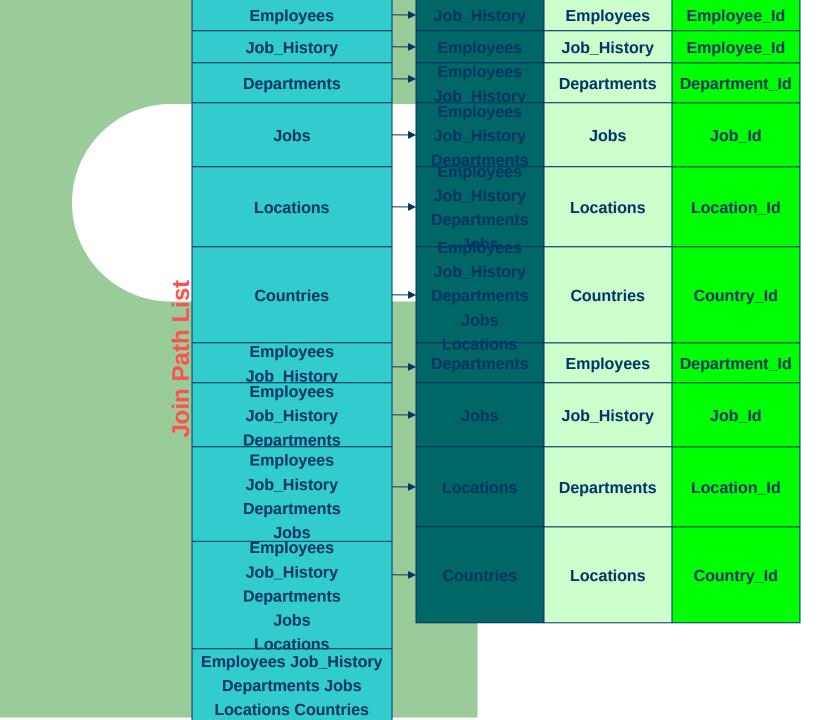
Job History Locations **Locations** Country Id **Departments Jobs Countries** Locations

insert all the names of base tables from path as vertexes in JoinPathList vertexes create a local buffer buf **Employees Employees Employee Id Job History Job History Employee Id** take one Ti at a time **Departments Departments** Department Id $JoinPathAdjacentList(T_i) = T_{Ibufl}$ **Jobs Jobs** Job Id $Key(T_i) = getFirstAdjacentListKey(T_i, T_{fourf})$ $JoinPathAdjacentList(T_{fbuff}) = T_i$ $Key(T_{fourt}) = getFirstAdjacentListKey(T_{fourt},T_i)$ **Location Id** Locations Locations $T_{\text{fbufl}} + = T_{\text{i}}$ Insert NodesList[T_[buf]] = T_[buf] **Countries Countries** Country Id path Vertexes **Employees Employees Employees** Department Id **Employees** Job History Job_History **Employees Job History Job History** Job Id **Job History Departments Departments Jobs Employees Departments** Job_History Locations **Departments Location Id Departments** Countries Jobs Jobs **Employees Job History** Locations Country Id Locations

Countries

Departments Jobs

Locations



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_[i] at a time for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != $Key(T_{[i]})$) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{iii}) then $buf.Table = T_1$ buf.key = $Key(T_{ii})$ buf **Table** Key

create a structure buf with 2 fields: Table and Key

for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_{iil} do

take one T_k at a time

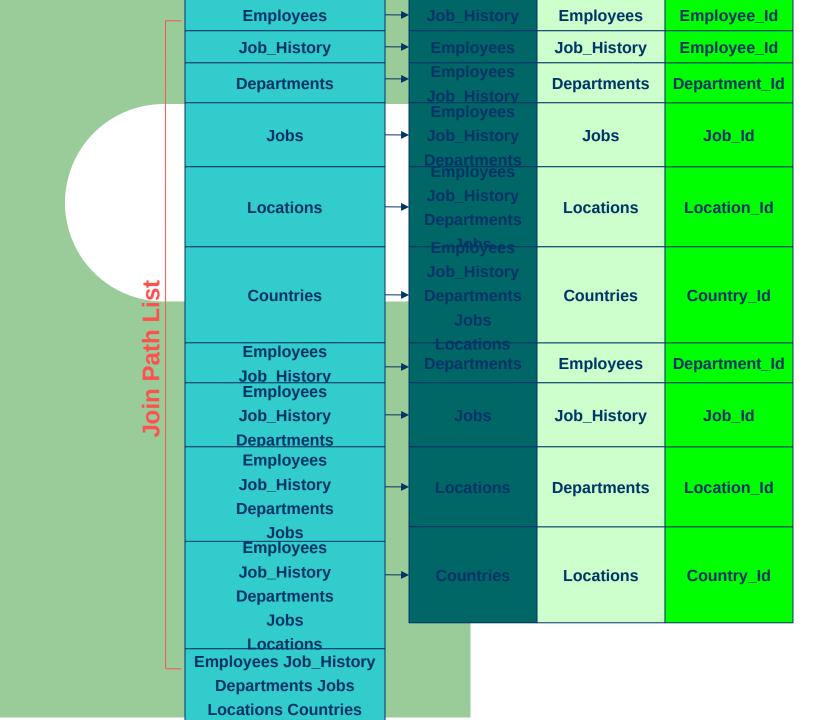
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

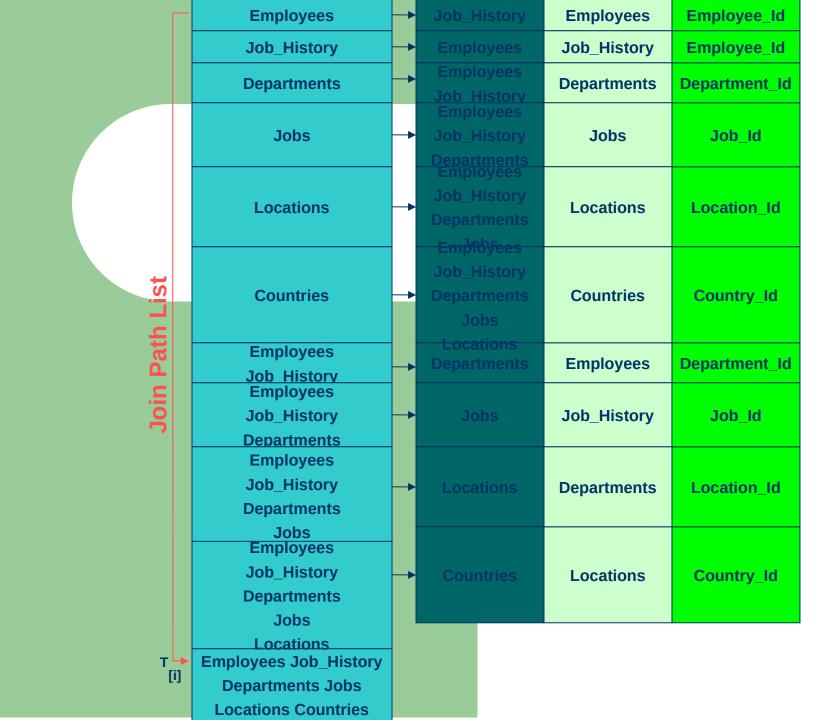
if T_i is the table from which comes Key(T_{ii}) then

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$



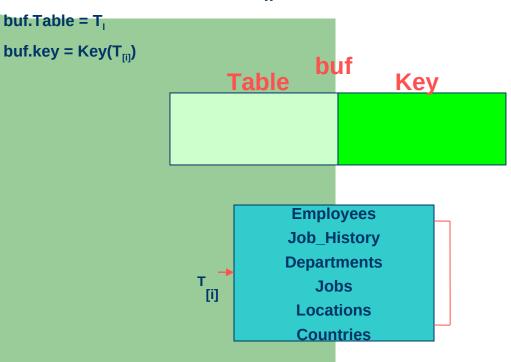
```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
               take one T<sub>k</sub> at a time
               for every buf. Table = T_k do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{\rm fil}$ at a time

for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf. Key not in Inherited Key($T_{[i]}$)) then I Inherited Key($T_{[i]}$) += buf. key

if T_i is the table from which comes Key(T_{ii}) then



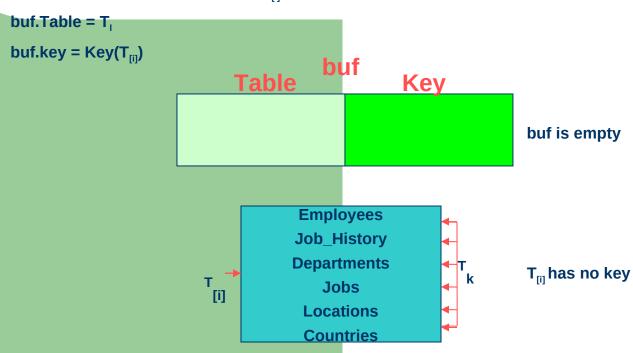
create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{ij} at a time

for all Base Tables inT_[i] do take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{iii}) then



create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>iii</sub> at a time
```

for all Base Tables $inT_{[i]}$ do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf.Table = T₁

 $buf.key = Key(T_{[i]})$

Employees

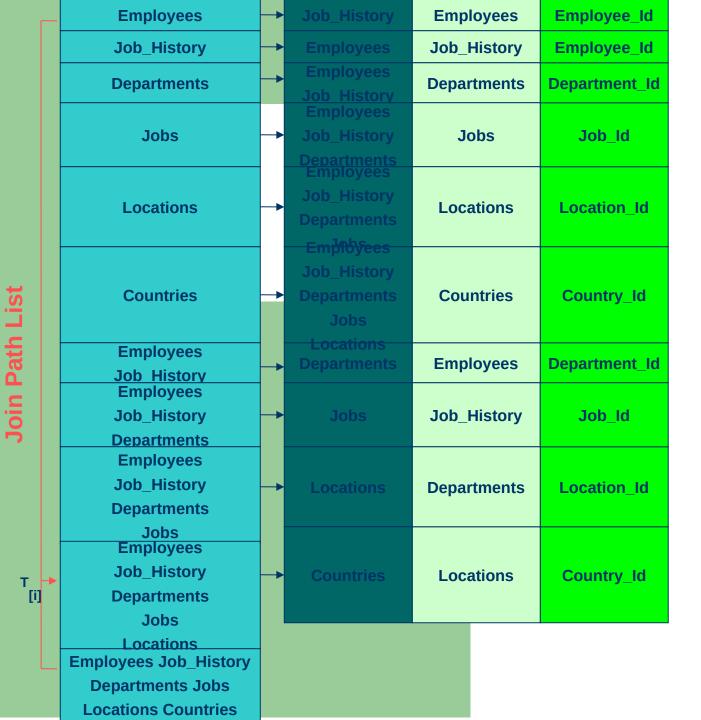
Employee Id Job History Departments Department Id Job Id **Jobs** Locations **Location Id** Country_Id **Countries Employees** Department Id **Job History** Job Id **Departments Location Id** Country Id **Locations**

Employees

Employee Id

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables in $T_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key if T_i is the table from which comes Key($T_{[i]}$) then buf. Table = T_i

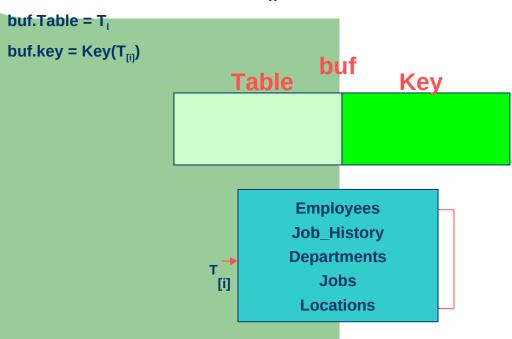
buf.key = $Key(T_{ii})$



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{\rm fit}$ at a time

for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iil} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{iii}) then $buf.Table = T_1$ buf.key = $Key(T_{ii})$ buf **Table** Key **Employees**

[i]

Job_History
Departments
Jobs

Locations

buf is empty

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>iii</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
              take one T<sub>k</sub> at a time
              for every buf. Table = T_k do
                      if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I
                           InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{iii}) then
              buf.Table = T_1
              buf.key = Key(T_{ii})
                                                              buf
                                                 Table
                                                                           Key
```

[i]

Employees
Job_History
Departments
Jobs

Locations

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>iii</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
              take one T<sub>k</sub> at a time
              for every buf. Table = T<sub>k</sub> do
                     if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I
                           InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{iii}) then
              buf.Table = T_1
              buf.key = Key(T_{ii})
                                                             buf
                                                Table
                                                                          Key
                                           Locations
                                                          Employees
                                                         Job_History
                                                         Departments
                                            T
[i]
                                                             Jobs
                                                           Locations
```

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>iii</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
              take one T<sub>k</sub> at a time
              for every buf. Table = T_k do
                     if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I
                          InheritedKey(T<sub>[ii]</sub>) += buf.key
      if T_i is the table from which comes Key(T_{iii}) then
              buf.Table = T_1
              buf.key = Key(T_{[i]})
                                                           buf
                                              Table
                                                                       Key
                                          Locations
                                                                  Country_Id
                                                        Employees
                                                       Job_History
                                                       Departments
                                           T
[i]
                                                           Jobs
                                                         Locations
```

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_[i] do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

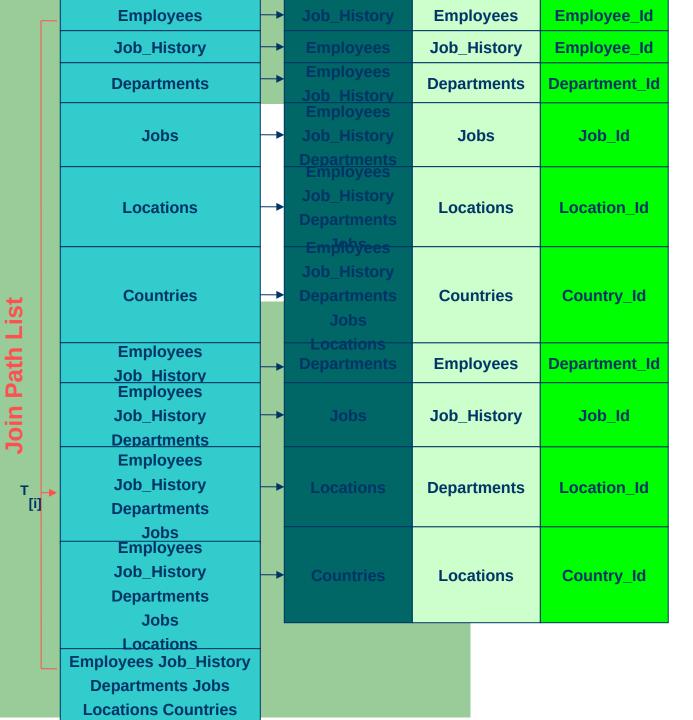
buf.Table = T₁

buf.key = $Key(T_{ii})$

_	Employees	-	Job_History	Employees	Employee_Id
	Job_History	-	Employees	Job_History	Employee_Id
	Departments	-	Employees Job History	Departments	Department_Id
	Jobs	-	Employees Job_History Departments	Jobs	Job_ld
	Locations	-	Departments Employees Job_History Departments Employees	Locations	Location_ld
	Countries	-	Job_History Departments Jobs	Countries	Country_ld
	Employees	_	Locations Departments	Employees	Department_Id
	Job History Employees		•		•
	Job_History		Jobs	Job_History	Job_ld
	Departments		0053	oob_instory	oob_la
	Employees				
	Job_History		Locations	Departments	Location_Id
	Departments		Locations	Departments	Location_iu
	Jobs				
	Employees				
	Job_History	-	Countries	Locations	Country_Id
	Departments				
	Jobs				
	Locations				
	Employees Job_History				
	Departments Jobs				
	Locations Countries				

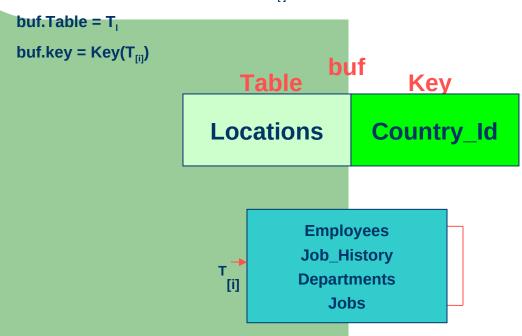
create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables in $T_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key if T_i is the table from which comes Key($T_{[i]}$) then buf. Table = T_i

buf.key = $Key(T_{ii})$



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables in $T_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



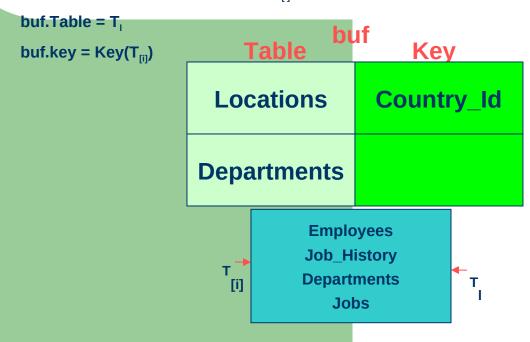
create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iil} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{iii}) then $buf.Table = T_1$ buf.key = $Key(T_{[i]})$ buf **Table** Key **Locations** Country_Id **Employees** Job_History **Departments** [i] **Jobs**

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>iii</sub> at a time
       for all Base Tables inT_{[i]} do
              take one T<sub>k</sub> at a time
              for every buf. Table = T<sub>k</sub> do
                     if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I
                           InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{iii}) then
              buf.Table = T_1
              buf.key = Key(T_{ii})
                                                             buf
                                                Table
                                                                         Key
                                           Locations
                                                                    Country_Id
                                                                                            Locations is not in T<sub>III</sub>
                                                         Employees
                                                         Job_History
                                                         Departments
                                             [i]
                                                             Jobs
```

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>iii</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
              take one T<sub>k</sub> at a time
              for every buf. Table = T<sub>k</sub> do
                     if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I
                           InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{iii}) then
              buf.Table = T_1
              buf.key = Key(T_{[i]})
                                                            buf
                                               Table
                                                                         Key
                                           Locations
                                                                   Country_Id
                                                         Employees
                                                         Job_History
                                                        Departments
                                             [i]
                                                             Jobs
```

for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

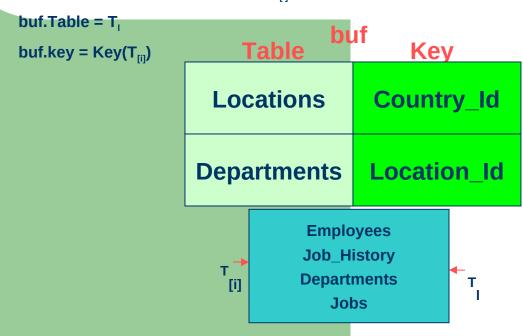
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



```
create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{[i]} at a time for all Base Tables inT_{[i]} do take one T_k at a time
```

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

Employees

Employee Id Job History Departments Department Id Job Id **Location Id** Country_Id **Employees** Department Id **Job History** Job Id **Departments Location Id** Country Id

Employees

Employee Id

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do

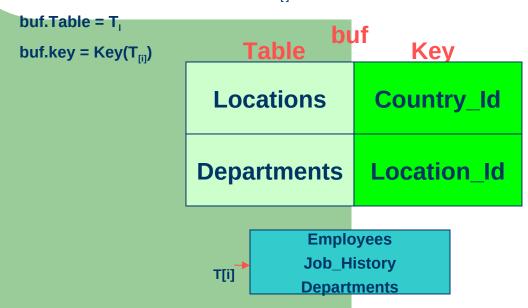
take one T_{iii} at a time

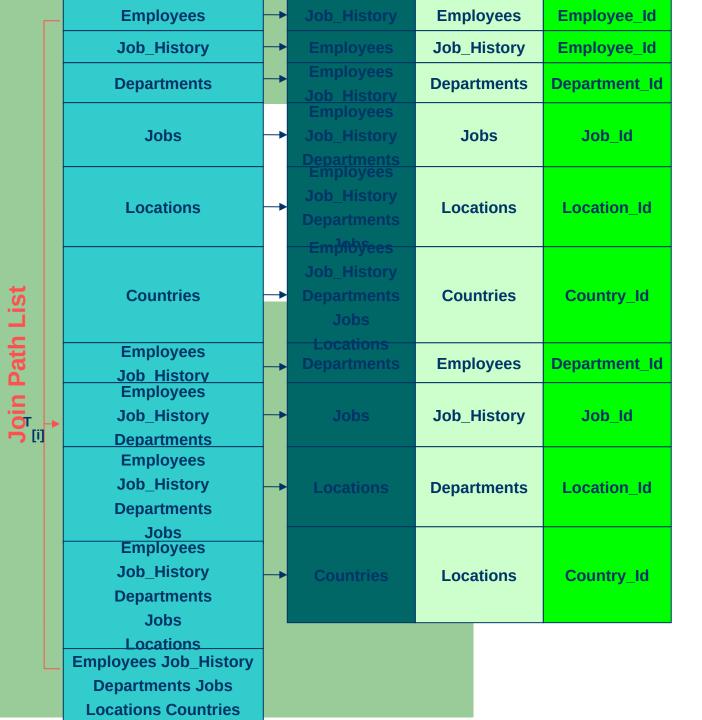
for all Base Tables inT_{iii}do

take one T_k at a time

for every buf. Table = T_k do

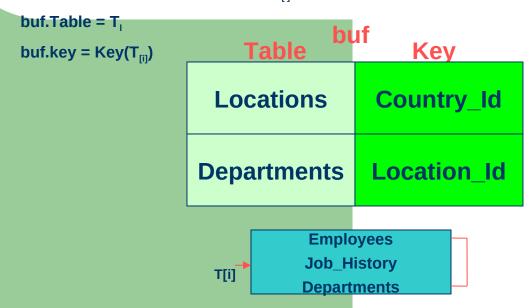
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key





for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I

InheritedKey(T_[ii]) += buf.key

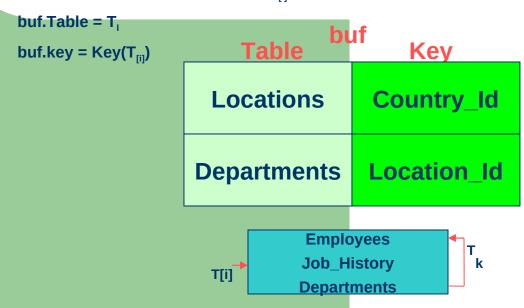


for all Base Tables $inT_{[i]}$ do

take one T_k at a time

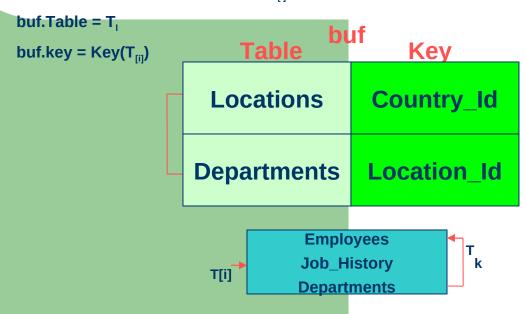
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{(i)}$)) and (buf.Key not in InheritedKey($T_{(i)}$)) then I InheritedKey($T_{(i)}$) += buf.key

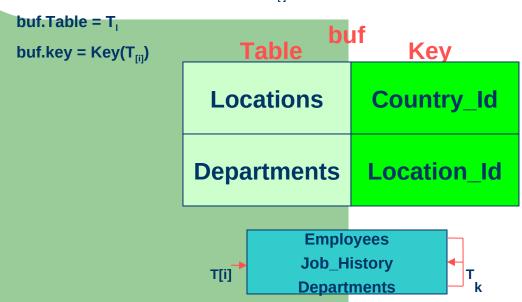


for all Base Tables inT_[i]do

take one T_k at a time

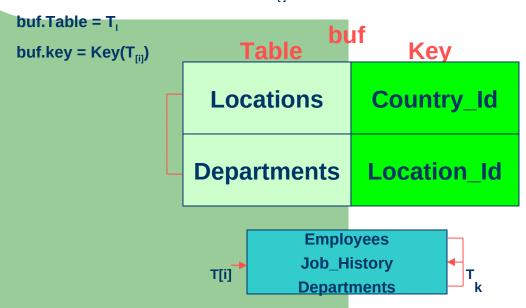
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

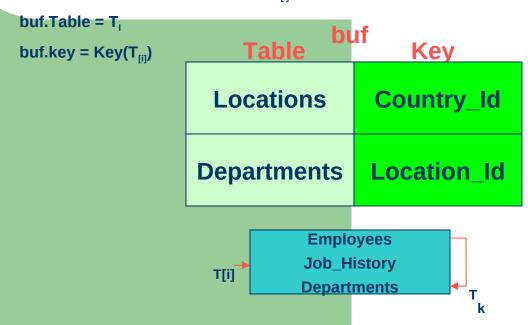


for all Base Tables $inT_{[i]}$ do

take one T_k at a time

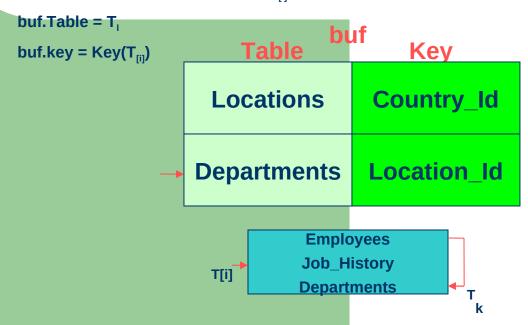
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



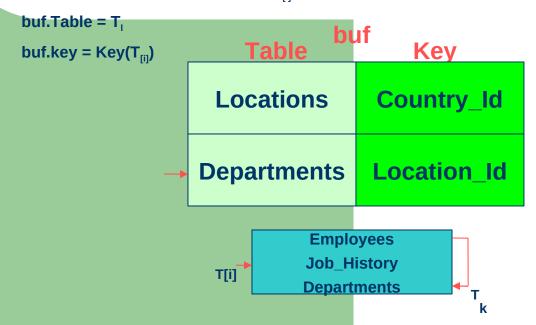
for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



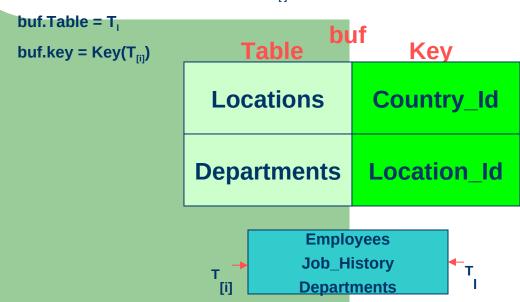
```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



for all Base Tables inT_[i] do take one T_k at a time

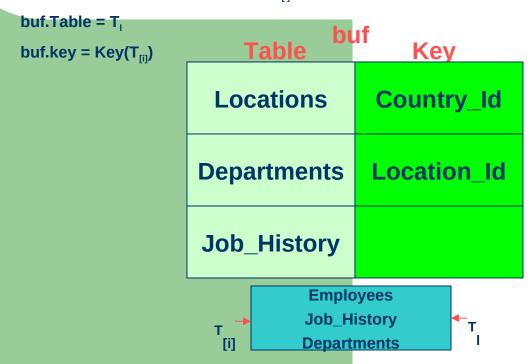
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all the tables in JoinPathList going downward do

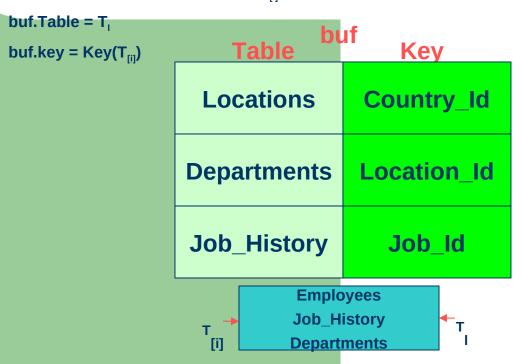
take one T_[i] at a time

for all Base Tables inT_[i] do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

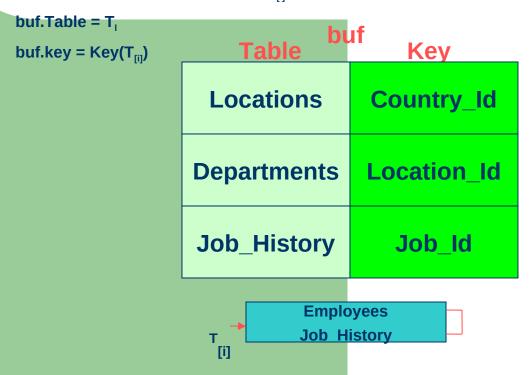
Employees		Job_History	Emplo	oyees	Employee_Id		
Job_History	-	Employees	Job_H	istory	Employee_ld		
Departments	-	Employees Job History	Depart	ments	Department_Id		
Jobs	-	Employees Job_History Departments	Jol	bs	Job_ld		
Locations		Departments Employees Job_History Departments Employees	Locations Countries		Location_ld		
Countries	-	Job_History Departments Jobs			Country_ld		
Employees		Locations Departments	Emplo	ovees	Department_Id		
Job History Employees				,	• –		
Job_History	→	Jobs	Job_History Departments Locations		Job_ld	Departments	Location_ld
Departments Employees Job_History Departments	-	Locations			Location_ld		
Jobs Employees Job_History Departments Jobs	-	Countries			Country_ld		
Locations Employees Job_History Departments Jobs Locations Countries							

for all Base Tables inT_{iii} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



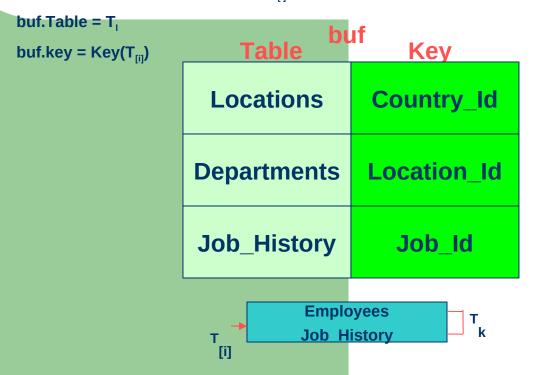


for all Base Tables inT_[i] do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

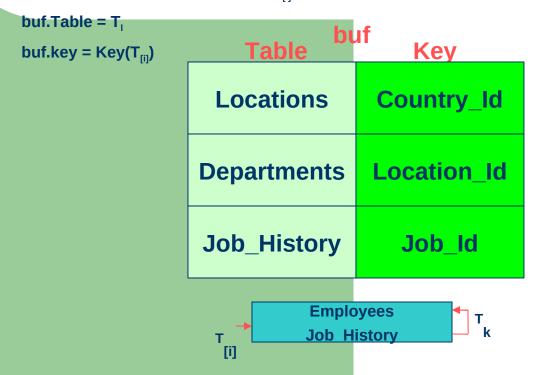


for all Base Tables $inT_{[i]}$ do

take one T_k at a time

for every buf. Table = T_k do

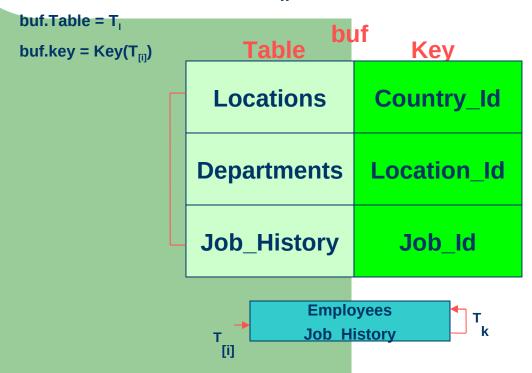
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all Base Tables inT_[i] do take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

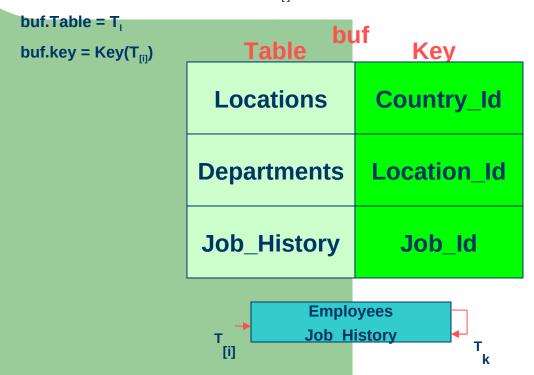


for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

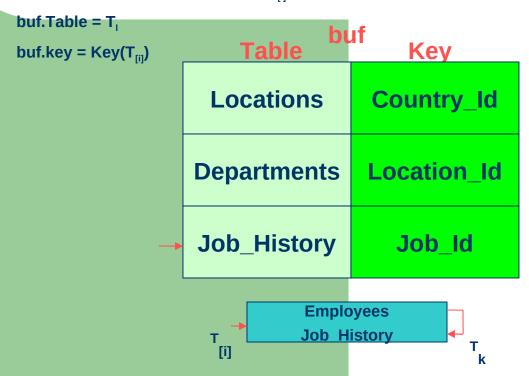


for all Base Tables inT_[i]do

take one T_k at a time

for every buf. Table = T_k do

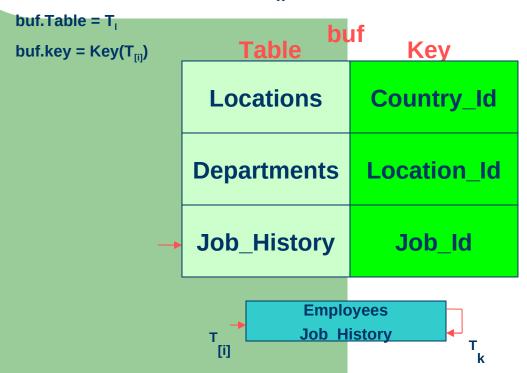
if (buf.key != Key($T_{(i)}$)) and (buf.Key not in InheritedKey($T_{(i)}$)) then I InheritedKey($T_{(i)}$) += buf.key



for all Base Tables $inT_{[i]}$ do take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]})) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```

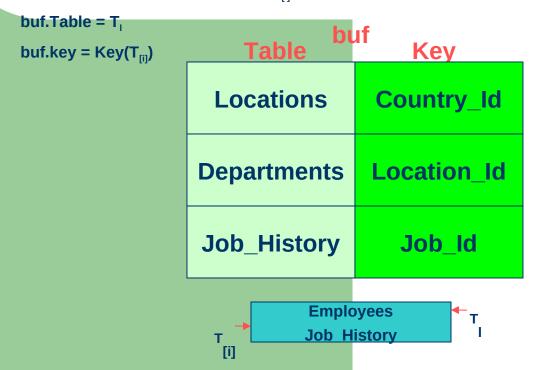


for all Base Tables inT_[i] do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{(i)}$)) and (buf.Key not in InheritedKey($T_{(i)}$)) then I InheritedKey($T_{(i)}$) += buf.key



for all Base Tables inT_{III} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf. Table = T_1 buf **Table** Key buf.key = $Key(T_{iii})$ Locations Country_Id Location_Id **Departments** Job_History Job Id **Employees Employees Job History** [0]

for all Base Tables inT_{iil} do

buf. Table = T_1

buf.key = $Key(T_{iii})$

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf **Table** Key Locations Country_Id Location_Id **Departments** Job_History Job Id **Employees** Department_Id **Employees Job History** [0]

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>iii</sub> at a time
```

for all Base Tables inT_[i] do

take one T_k at a time

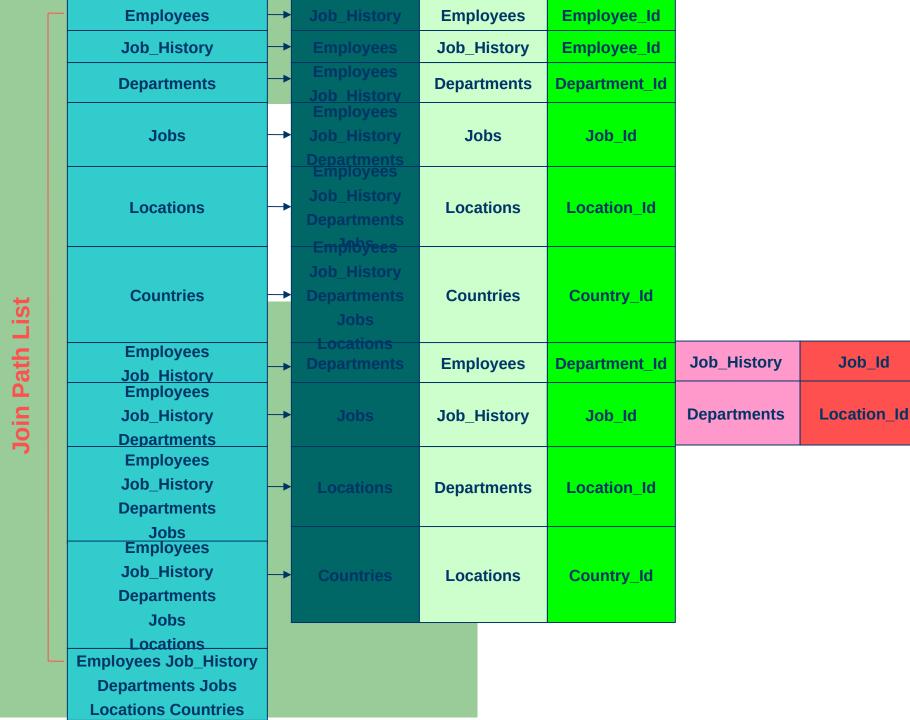
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

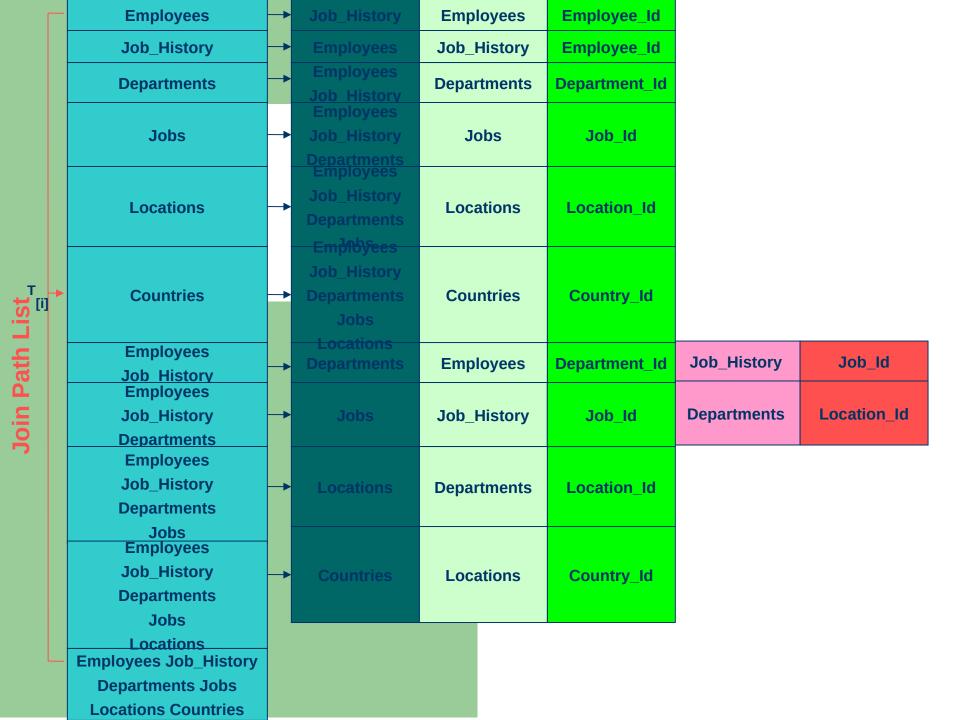
if T_i is the table from which comes Key(T_{ii}) then

buf.Table = T₁

buf.key = $Key(T_{ii})$



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_[i] at a time for all Base Tables inT_{iil} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{ii}) then $buf.Table = T_1$ buf.key = $Key(T_{ii})$



for all Base Tables inT_{iii}do

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

buf Table Key		
Locations	Country_Id	
Departments	Location_ld	
Job_History	Job_ld	
Employees	Department_Id	
Countries		

for all Base Tables inT_{iil} do

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

take one T_k at a time

for every buf. Table = T_k do

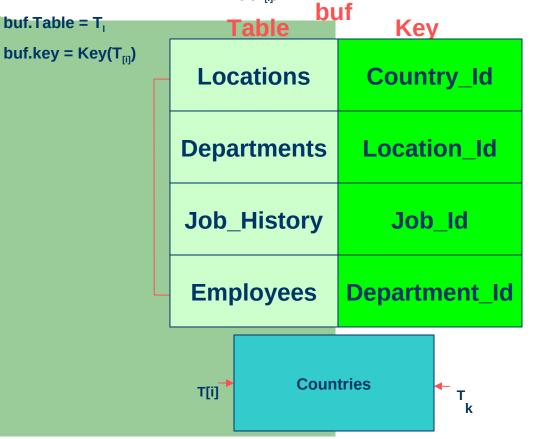
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

Table Key		
Locations	Country_ld	
Departments	Location_ld	
Job_History	Job_ld	
Employees	Department_Id	
T[i] Countries T k		

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables $inT_{[i]}$ do take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iii} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{ii}) then buf buf. Table = T_1 Key Table buf.key = $Key(T_{ii})$ Locations Country_Id **Location Id Departments** Job_History Job Id **Employees** Department_Id **Countries** T[i]

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_{iil} do

take one T_k at a time

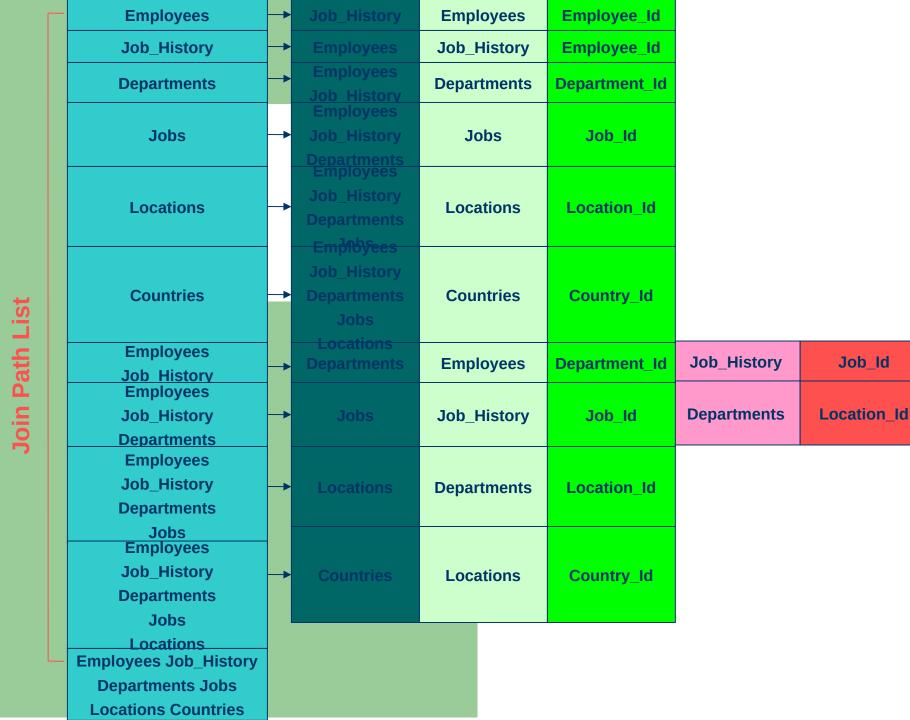
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

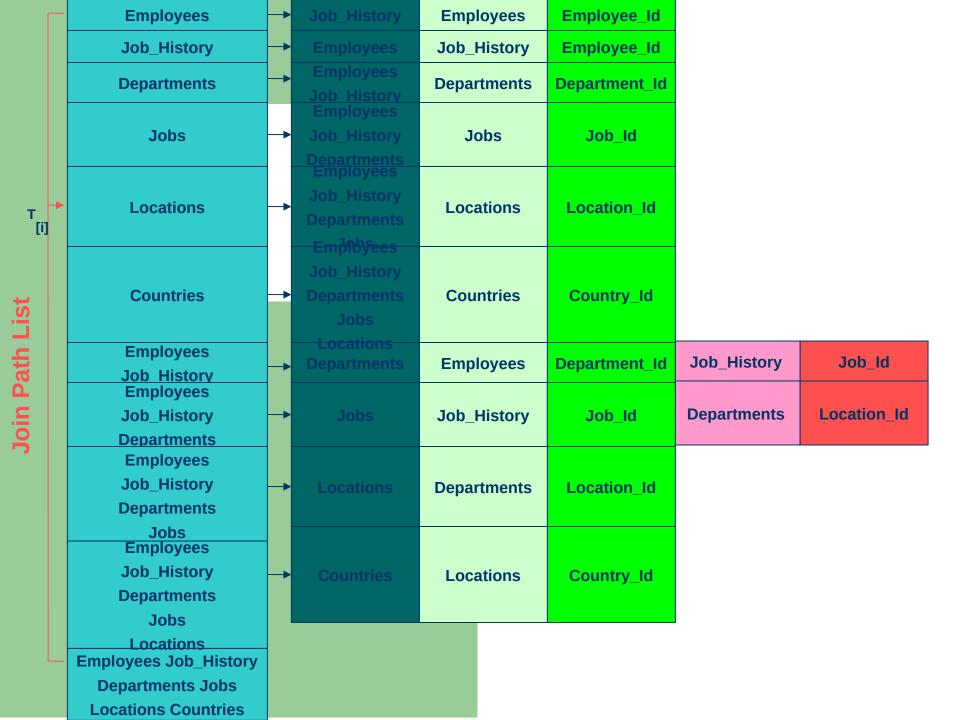
if T_i is the table from which comes Key(T_{ii}) then

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$



```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                             InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



for all Base Tables $inT_{[i]}$ do

buf. Table = T_1

buf.key = $Key(T_{ii})$

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

Table Key	
Locations	Country_Id
Departments	Location_ld
Job_History	Job_ld
Employees	Department_Id
Locations	

for all Base Tables inT_{iil} do

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

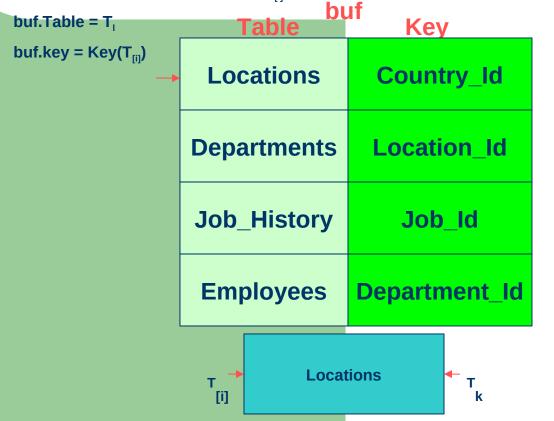
take one T_k at a time

for every buf. Table = T_k do

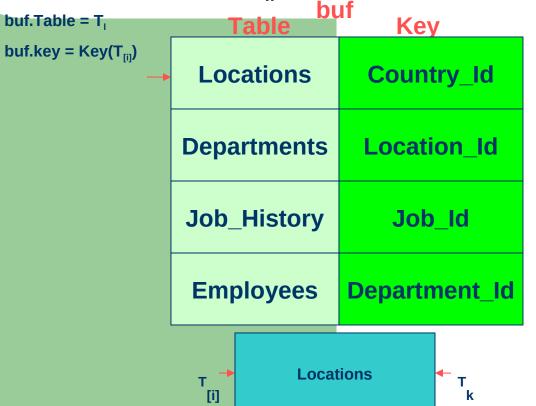
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

Table Key	
Locations	Country_ld
Departments	Location_Id
Job_History	Job_ld
Employees Department_I	
T Locations T k	

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables in $T_{[i]}$ do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key if T_i is the table from which comes Key($T_{[i]}$) then buf. Table | Key



```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]})) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_[i] do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf.Table = T₁

buf.key = $Key(T_{ii})$

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT<sub>iil</sub> do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                             InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



for all Base Tables inT_{iii} do

buf.Table = T₁

 $buf.key = Key(T_{ii})$

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

	Table	Key
_{ij})	Locations	Country_ld
	Departments	Location_Id
	Job_History	Job_ld
	Employees	Department_Id
	Jobs [i]	

for all Base Tables inT_{iii} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

buf

Jobs

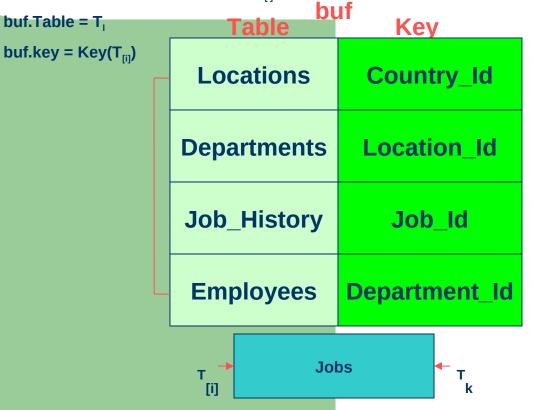
buf. Table = T ₁	Table	Key
buf.key = Key(T _[i])	Locations	Country_Id
	Departments	Location_ld
	Job_History	Job_ld
	Employees	Department_Id

for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key



for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes $Key(T_{ii})$ then

buf.Table = T_i buf.key = Key(T_{ii})

Table	Key	
Locations	Country_Id	
Departments	Location_Id	
Job_History	Job_ld	
Employees	Department_Id	
Jobs [i]		

buf

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>iii</sub> at a time
```

for all Base Tables inT_{iii}do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf.Table = T₁

buf.key = $Key(T_{ii})$

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_[i] at a time for all Base Tables inT_{iil} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{ii}) then $buf.Table = T_1$ buf.key = $Key(T_{ii})$



for all Base Tables inT_{iii}do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf buf. Table = T_1 Key Table buf.key = $Key(T_{iii})$ Locations Country_Id Location_Id **Departments** Job_History Job Id **Employees** Department_Id **Deparments** т [i]

for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

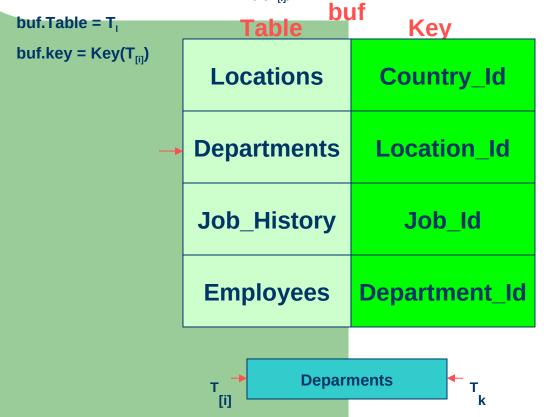
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey(T_[ii]) += buf.key

buf.Table = T ₁	Table	Key
buf.key = Key(T _[i])	Locations	Country_Id
	Departments	Location_Id
	Job_History	Job_ld
	Employees	Department_Id
	T Depart	ments T k

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{[i]}$ at a time for all Base Tables $inT_{[i]}$ do take one T_k at a time for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iii} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{ii}) then buf buf. Table = T_1 Key Table buf.key = $Key(T_{iii})$ Locations Country_Id **Departments** Location_Id Job_History Job Id **Employees** Department_Id **Deparments** Т

[i]

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables $inT_{[i]}$ do take one T_k at a time

for every buf. Table = T_k do

if (buf.key != $Key(T_{[i]})$) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey(T_[ii]) += buf.key

if T_i is the table from which comes $Key(T_{ii})$ then

 $buf.Table = T_1$ buf.key = $Key(T_{ii})$

I abic	ixey
Locations	Country_Id
Departments	Location_ld
Job_History	Job_ld
Employees	Department_Id

Deparments [i]

create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

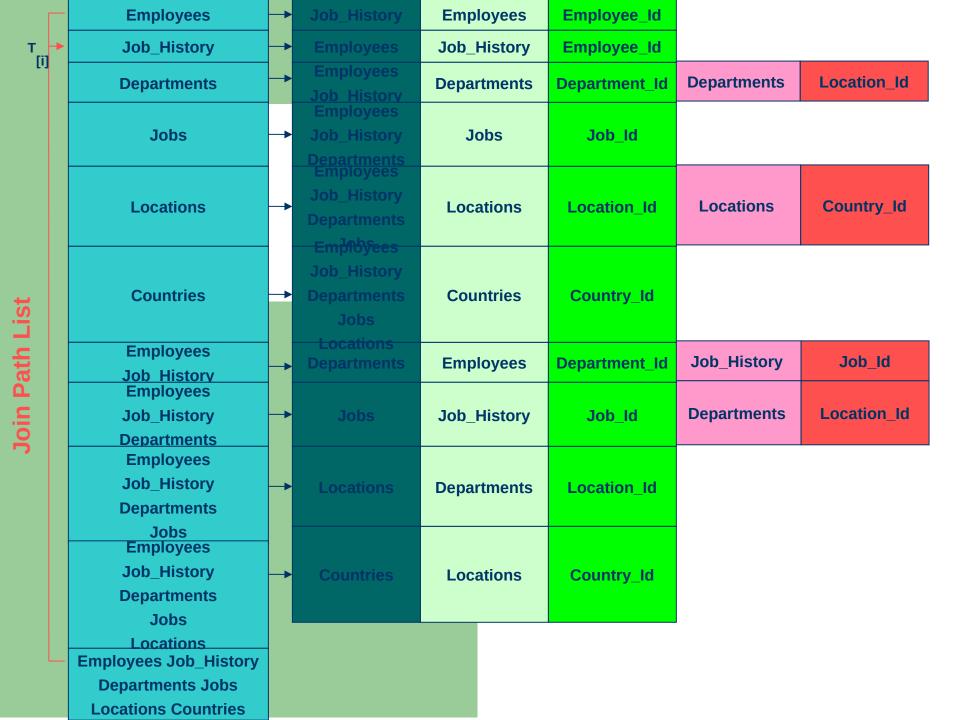
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT<sub>iii</sub> do
               take one T<sub>k</sub> at a time
               for every buf. Table = T_k do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time

for all Base Tables inT_{iii} do

buf. Table = T_1

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_[ii]) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf Key Table buf.key = $Key(T_{iii})$ Locations Country_Id Location_Id **Departments** Job_History Job Id **Employees** Department_Id Job_History т [i]

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create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{\rm fil}$ at a time

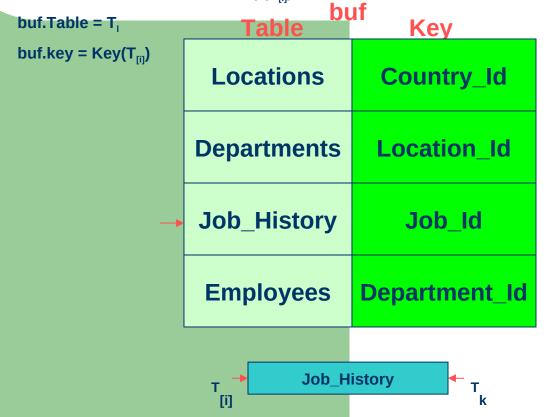
for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one $T_{\rm [i]}$ at a time

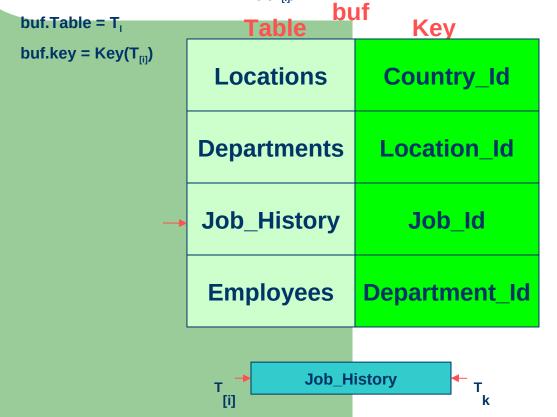
for all Base Tables inT_[i] do

take one T_k at a time

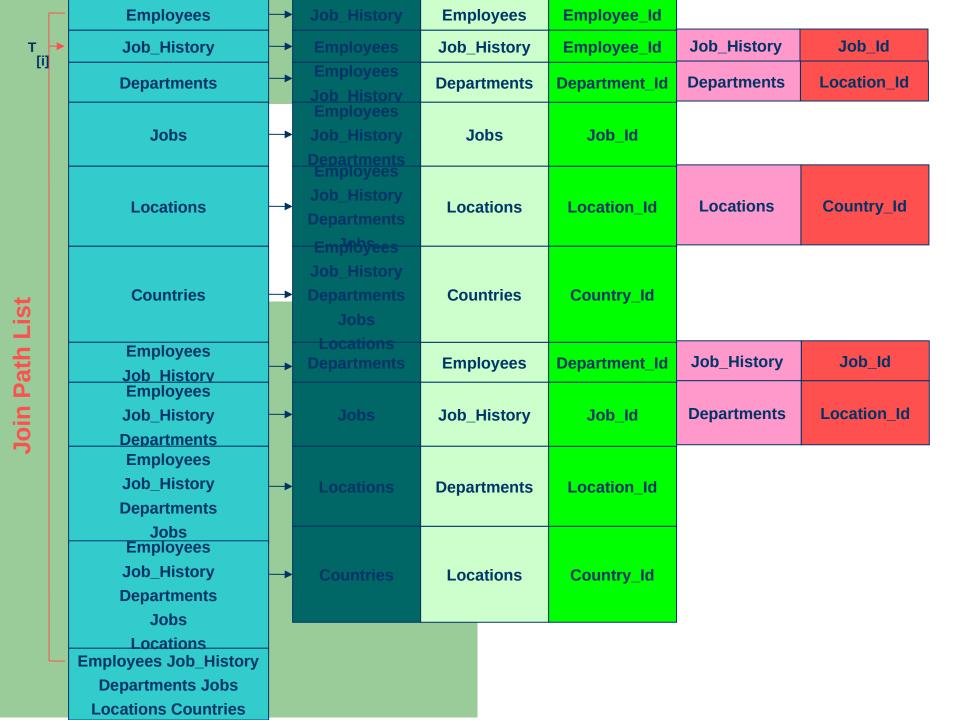
for every buf. Table = T_k do

if (buf.key != Key($T_{[i]}$) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then



```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]})) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



create a structure buf with 2 fields: Table and Key

→ for all the tables in JoinPathList going downward do

```
take one T<sub>[i]</sub> at a time
```

for all Base Tables inT_{iil} do

take one T_k at a time

for every buf. Table = T_k do

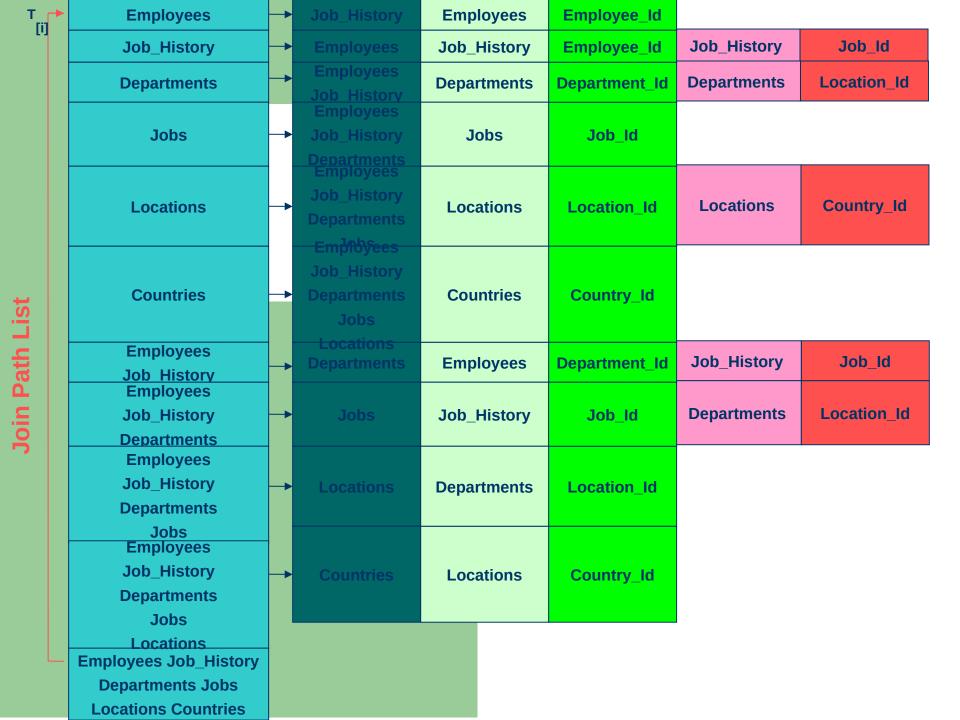
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

 $buf.Table = T_1$

buf.key = $Key(T_{ii})$

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_[i] at a time for all Base Tables inT_{iii} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then I InheritedKey(T_[ii]) += buf.key if T_i is the table from which comes Key(T_{ii}) then $buf.Table = T_1$ buf.key = $Key(T_{ii})$



create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time

for all Base Tables inT_{iii} do

buf. Table = T_1

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_m) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

buf Key Table buf.key = $Key(T_{iii})$ Locations Country_Id Location_Id **Departments** Job_History Job Id **Employees** Department_Id **Employees** т [i]

create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iii} do

buf. Table = T_1

take one T_k at a time

for every buf. Table = T_k do

if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_[ii]) += buf.key

if T_i is the table from which comes Key(T_{ii}) then

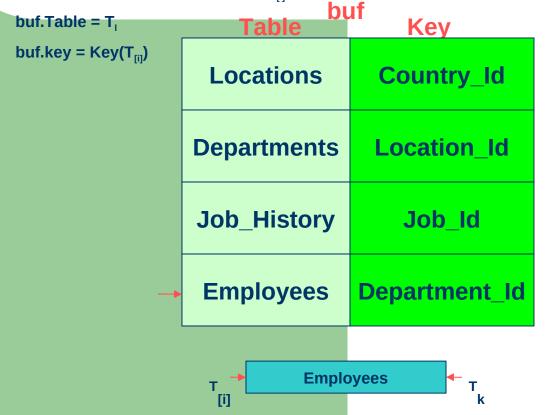
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create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iii} do take one T_k at a time

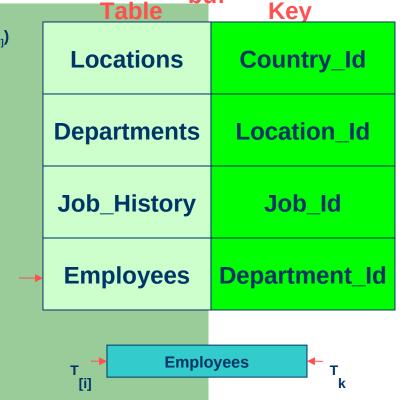
for every buf. Table = T_k do

if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_m) += buf.key

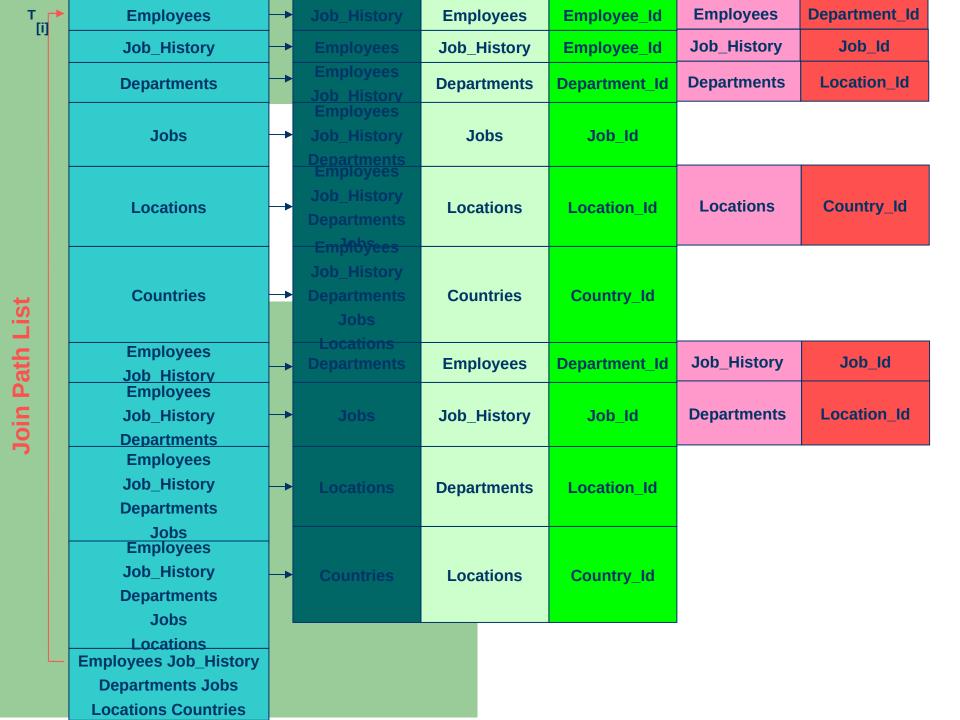
if T_i is the table from which comes Key(T_{ii}) then



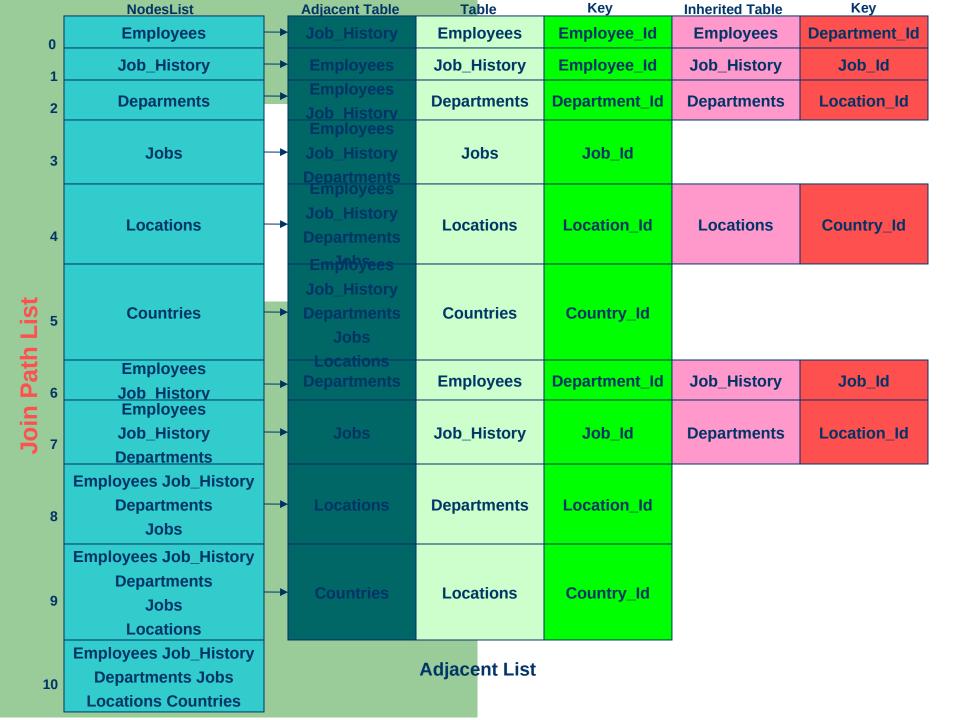
create a structure buf with 2 fields: Table and Key for all the tables in JoinPathList going downward do take one T_{iii} at a time for all Base Tables inT_{iii} do take one T_k at a time for every buf. Table = T_k do if (buf.key != Key(T_{ii})) and (buf.Key not in InheritedKey(T_{ii})) then I InheritedKey(T_m) += buf.key if T_i is the table from which comes Key(T_{ii}) then buf $buf.Table = T_1$ Table buf.key = $Key(T_{iii})$ Locations



```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T<sub>k</sub> do
                       if (buf.key != Key(T_{[i]})) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[ii]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T_1
               buf.key = Key(T_{ii})
```



```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
       take one T<sub>[i]</sub> at a time
       for all Base Tables inT_{[i]} do
               take one T<sub>k</sub> at a time
               for every buf. Table = T_k do
                       if (buf.key != Key(T_{[i]}) ) and (buf.Key not in InheritedKey(T_{[i]})) then I
                            InheritedKey(T<sub>[i]</sub>) += buf.key
       if T_i is the table from which comes Key(T_{ii}) then
               buf.Table = T<sub>1</sub>
               buf.key = Key(T_{ii})
```



Give a general name for the B™Tree.

Give for every entry in the JoinPathList a B⁺Tree index with name as the B™Tree + the PathJoinList entry number.

About the last virtual table, it index has no keys, it works because we consider pairs of < keys, Data Pointers > so they are ordered by their data pointers. Scanning the index we get all the sequences of joined data pointers.

Non Terminal has repeated empty keys they point to different pages. When comes a key it would be inserted in the last page.

Duplicate keys are inserted and when a page is full, the key is repeated in the non terminal.

In any case we can incorporate any key of our choice from the tables forming the virtual table.

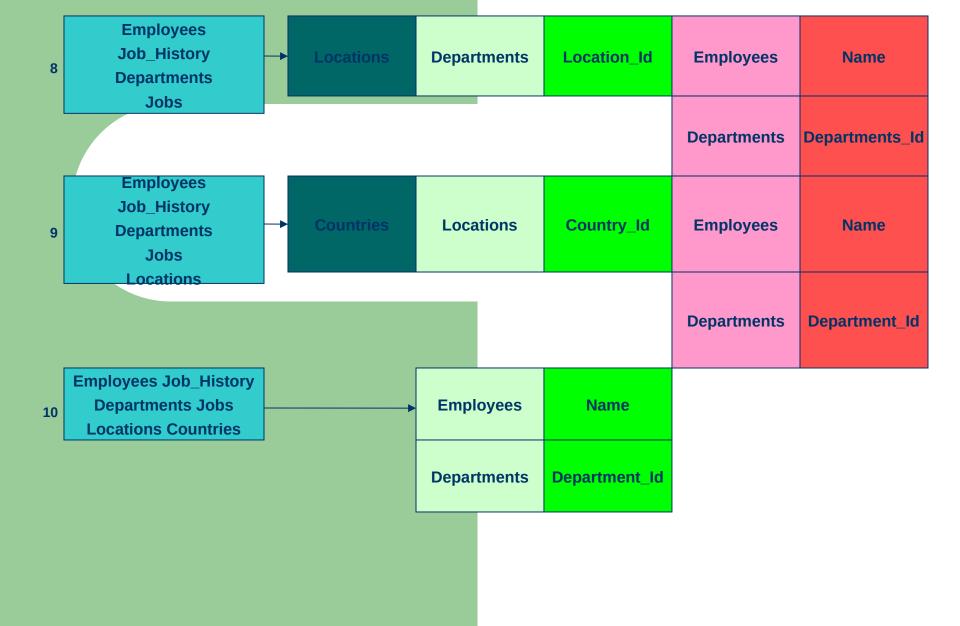
If the table is in join with itself, consider the table twice as aliases.

Define a Create Join Index (IndexName, Eventual columns for the last virtual table representing tables in join)

Implementation:

Use a big buffer and from the Data Dictionary divide it by the keys length, inherited keys length and space for the number of Data Pointers.

Suppose we wants the join sequence of the tables ordered by Employees. Name and Departments. Department Id, applying the algorithm, the JoinPathList becomes: **NodesList Adjacent Table Table** Key **Inherited Table** Key **Employees Employees Employee Id Employees Name Employees** Department_Id Job_History Job_History Employee_Id Job_History Job_Id 1 **Deparments Departments** Department Id **Departments Location Id** 2 **Jobs Jobs** Job Id Join Path List Locations Locations **Location Id** Country_Id Locations **Countries** Country Id **Countries Employees Employees** Department_Id **Employees Name** Job History 6 **Job History** Job Id **Employees** Job_History Job Id **Employees Name** Job_History 7 **Departments Departments** Department_Id **Departments Location Id**



Create B⁺**Trees**

- The Nodes (Vertexes) in the JoinPathList represents all the base tables + virtual tables constituting from the base tables by adding one at a time in mode that the one added is at least in direct join with its precedents.
- Defining a B⁺Tree for every node, the ones for the virtual tables have for every key a set of data pointers equal to the number of base tables constituting it and from definition of the virtual tables, combining the rows pointed by those data pointers we obtain a joined row.

The algorithm for creating B⁺Trees is the following:

```
create B+Trees(in PathJoinList; out B+Trees);
give a general name for the BJoinTree
for all entries in JoinPathList do
       take one node at a time
       create a B+Tree for the node defined as
              name of the B+Tree equal to the name of BJoinTree follow by the
                index number of the node entry
              Number of data pointers equal to the number of base tables
                constituting the virtual table of the node
              Key is defined by the pair <Table, Key> in the adjacent list of the
                node
              Inherited Keys are defined by the pairs <Table, Inheritred Key> in
                the adjacent list of the node
```

NOTE

The data pointers to the tables in join are in order of the last virtual table and not as declared in the create constructor, this is due to the fact that Path is not always in the same order as the tables declared in the constructor.

So to know the order of data pointers in respect to the tables in join, the property "BaseTables" in "BjoinTreeU.pas" should be called to get it.

The function GetDataRefByTableName(BaseTable: string; DataRef: array of DataPointerType): DataPointerType; give the data reference to the row in base table. See Test Index (Button5) in SQLProject.

Insert routine

When a new row R_m from table T_i get inserted do the following:

- Locate the entry of T_i in the JoinPathList
- From its adjacent List, locate the definition of the keys and inherited keys
- From Row $R_{\rm m}$ get the columns constituting the keys and the inherited keys
- Call AddJoinKey (T_i, Keys, InheritedKeys, DP_i) where DP_i is the row id of row R_m.

Notice that Keys_i, InheritedKeys_i and DP_i are relative to the row R_m from table T_i

AddJoinKey (T_[i], [DP_i])

- Call AddKey (B⁺Tree(T_[i]), keys_[i], InheritedKeys_[i], [DP_i]) for the index of table T_[i]
- Locate the entry of T_{ii} in the JoinPathList
- From its adjacent List, locate the Table $T_{[k]}$ adjacent to it and do the following:
 - Locate the entry of $T_{[k]}$ in the JoinPathList
 - FindKey(B⁺Tree(T_[k]), Keys_[i])
 - While found(keys[i]) do

ReturnKeys(B+Tree(T_[k]), keys_[k], InheritedKeys_[k], [DP_k])

Locate the entry of T_{lik} in the JoinPathList

From its adjacent List, locate the definition of the keys and inherited keys

From $\text{keys}_{[i]}$, $\text{inheritedkeys}_{[i]}$, $\text{keys}_{[k]}$, $\text{inheritedkeys}_{[k]}$ get the keys and inherited keys of $T_{[ik]}$

AddJoinKey $(T_{[ik]}, Keys_{[ik]}, InheritedKeys_{[ik]}, [DP_{ik}])$

 $NextKey(B^{+}Tree(T_{[k]}), Keys_{[i]})$

AddJoinKey (T_[i], [DP_i])

In the same fashion when using an ordinary B⁺Tree and one row get inserted, so we check the definition of the B⁺Tree to get the necessary keys from the row to insert them, with B^{Join}Tree we check the definition to get the keys and the inherited keys.

Call AddjoinKey(T_i,[keys],[DP_i])

Employees table

	EMPLO	NAME	EMAIL	PHONE_	HIRE_	JOB ID	SALARY	DEPART
	YEE_ID			NUMBER			SALART	MENT_ID
0	101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN
1	102	Jorge Perez	jperez	448-5268	05/14/1999	AC_MGR	60000	ACC
2	103	Edward Cartier	ecartier	742-8429	03/01/2003	SA_MGR	60000	SAL
3	104	Teresa Gonzalez	tgonzalez	134-8329	12/20/2002	AC_AUD	55000	ACC
4	105	Michelle Blanche	mblanche	745-7496	01/02/2001	SA_REP	35000	SAL

Job_History table

	EMPLOYEE_ID	START_DATE	END_DATE	JOB_ID	DEPARTMENT_ID
0	101	12/16/1998	12/15/1999	AC_AUD	ACC
1	102	05/16/1999	05/15/2001	AC_AUD	ACC
2	101	12/16/1999	12/15/2001	SA_REP	SAL
3	103	03/16/2003	03/15/2004	AC_AUD	ACC

Departments table

	Deparment_Id	Department_Name	Manager_Id	Location_ld
0	FIN	FINANCE	101	1000
1	ACC	ACCOUNTING	102	1010
2	SAL	SALES	103	1020

Jobs Table

	JOB_ID	JOB_TITLE	MIN_SALARY	MAX_SALARY
0	AC_AUD	Accounting Auditor	30000	60000
1	AC_MGR	Accounting Manager	60000	70000
2	FI_MGR	Finance Manager	50000	70000
3	SA_MGR	Sales Manager	les Manager 50000	
4	SA_REP	Sales Representative	30000	40000

Locations table

	LOCATION_ ID	STREET_ADDRESS	POSTAL_ CODE	CITY	STATE PROVINCE	COUNTRY_ ID
0	1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca
1	1010	Calle Sermiento numero 300	62547	Guadalajara	Baja	me
2	1020	Rue des fleurs n. 345	78921	Toulouse	Moyenne	fr

Countries table

	Country_Id	Country_Name
0	ca	Canada
1	fr	France
2	me	Mexico

Inserting first row from table Employees

Base Table

Employees 0

EMPLO	2000	FAAAU	PHONE_	HIRE	100 10	SALARY	DEPART
YEE_ID	NAME	EMAIL.	NUMBER			SALART	MENT_ID
101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN

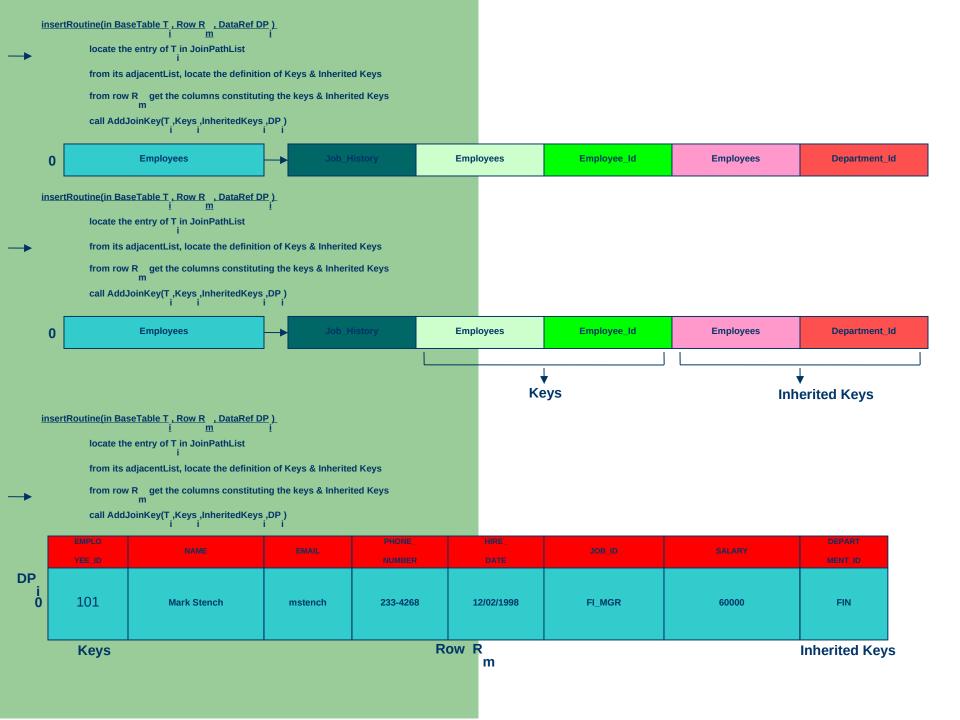


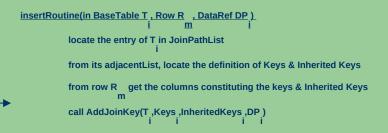
DataRef

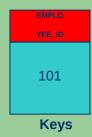
	EMPLO YEE_ID	NAME	EMAIL	PHONE_ NUMBER	HIRE_ DATE		SALARY	DEPART MENT ID
DP i 0	101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	FIN

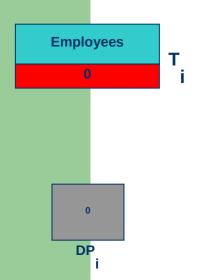
Row R

m

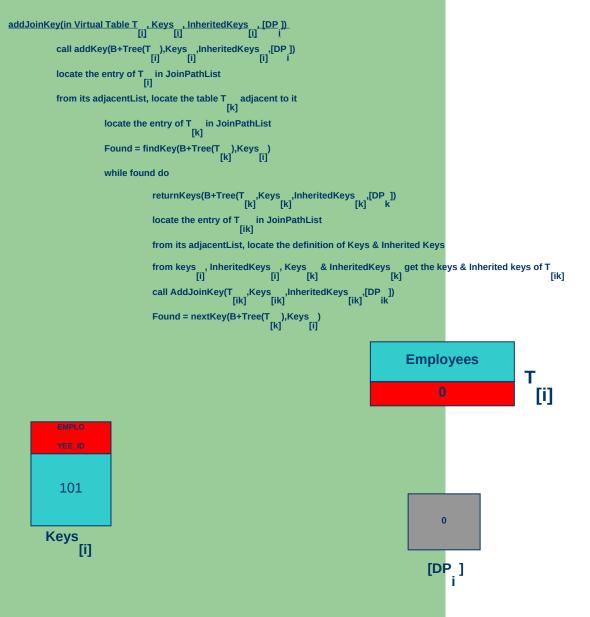


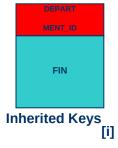


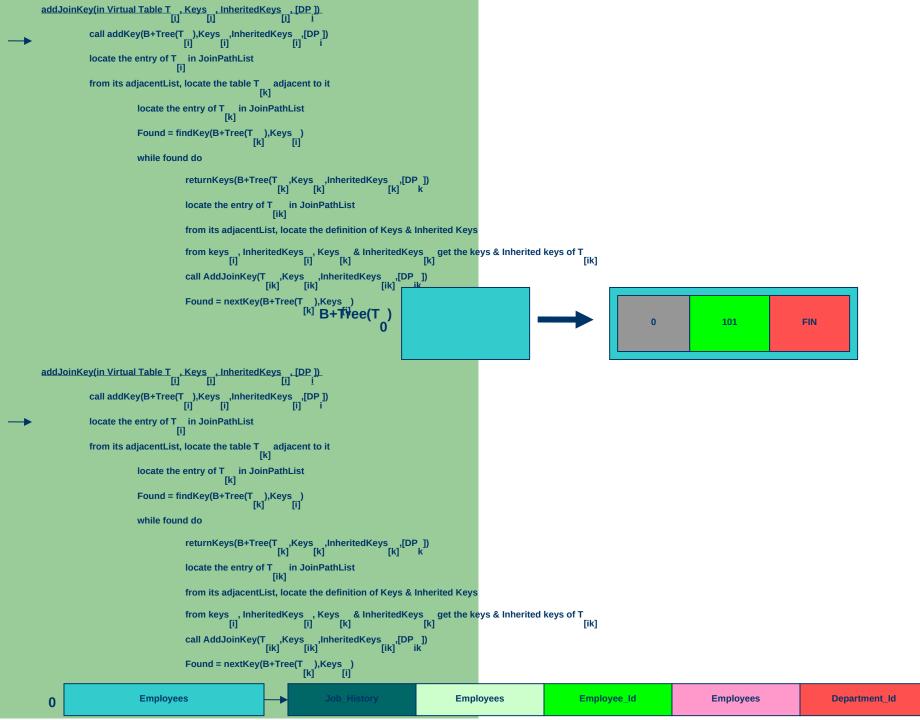












```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ])
                                          call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                                           locate the entry of T__ in JoinPathList
                                          from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                                                     locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                                                     Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                      while found do
                                                                                                                                \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                                                                \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                                                                from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                                                                from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k]
                                                                                                                                call AddJoinKey(T ,Keys ,InheritedKeys ,[ik] ,[DP ]) ik
                                                                                                                                Found = nextKey(B+Tree(T_),Keys_)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Employees
                                                                                       Employees
                                                                                                                                                                                                                                                                                                                                                                                Employees
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Employee_Id
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Department_Id
                                                                                                                                                                                                                                      Adjacent Table
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i]
                                          call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                                           locate the entry of T__ in JoinPathList
                                          from its adjacentList, locate the table T___adjacent to it
                                                                                     \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                                                    Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                      while found do
                                                                                                                                \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                                                                locate the entry of T in JoinPathList [ik]
                                                                                                                                from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                                                                from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] get the keys & Inherited keys of T [k]
                                                                                                                                call AddJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                                                                Found = nextKey(B+Tree(T ),Keys )
                                                                                      Job_History
                                                                                                                                                                                                                                                                                                                                                                              Job_History
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Employee_Id
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Job_History
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Job Id
```

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
                            locate the entry of T_{\underline{\underline{\phantom{A}}}} in JoinPathList
                            from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                         locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                         Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                      \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                      locate the entry of T in JoinPathList [ik]
                                                                                       from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T
                                                                                       call AddJoinKey(T ,,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                       Found = nextKey(B+Tree(T___),Keys__)
                                                           B+Tree(T)
                                                                                                                                                                                                                       Found: FALSE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]).

[i] [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
                            locate the entry of T _{\mbox{\scriptsize [i]}} in JoinPathList
                            from its adjacentList, locate the table T \quad \text{adjacent to it} \quad [k]
                                                         \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                         Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                       returnKeys(B+Tree(T ,Keys ,InheritedKeys ,[DP ])  
[k] [k] [k] k
                                                                                      locate the entry of T___ in JoinPathList
                                                                                       from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                       from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                      {\it call AddJoinKey(T_{[ik]}, Keys, InheritedKeys_{[ik]}, [DP_{ik}])}
                                                                                                                                                                                                                              Found: FALS`E
                                                                                       Found = nextKey(B+Tree(T_),Keys_)
```

```
addJoinKey(in Virtual Table T ___, Keys ___, InheritedKeys ___, [DP_]).

call addKey(B+Tree(T __), Keys ___, InheritedKeys ___, [DP_])

locate the entry of T ___ in JoinPathList

from its adjacentList, locate the table T ___ adjacent to it

locate the entry of T ___ in JoinPathList

Found = findKey(B+Tree(T __), Keys ___, InheritedKeys ___, [DP_])

while found do

returnKeys(B+Tree(T __, Keys __, InheritedKeys ___, [DP_])

locate the entry of T ___ in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

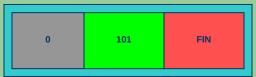
from keys ___, InheritedKeys ___, Keys ___ & InheritedKeys ___, get the keys & Inherited keys of T _____, Keys ___, InheritedKeys _____, [IDP_])

call AddJoinKey(T ___, Keys ____, InheritedKeys _____, [IDP_])

Found = nextKey(B+Tree(T ___, Keys ____, InheritedKeys _____, [IDP_])

[ik]
```





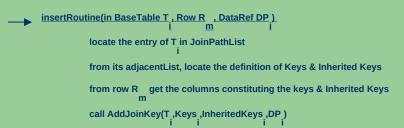
Inserting first row from table Job_History

Base Table

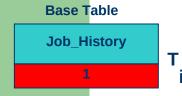
Job_History

-1

EMPLOYEE_ID	START_DATE	END_DATE	JOB_ID	DEPARTMENT_ID
101	12/16/1998	12/15/1999	AC_AUD	ACC

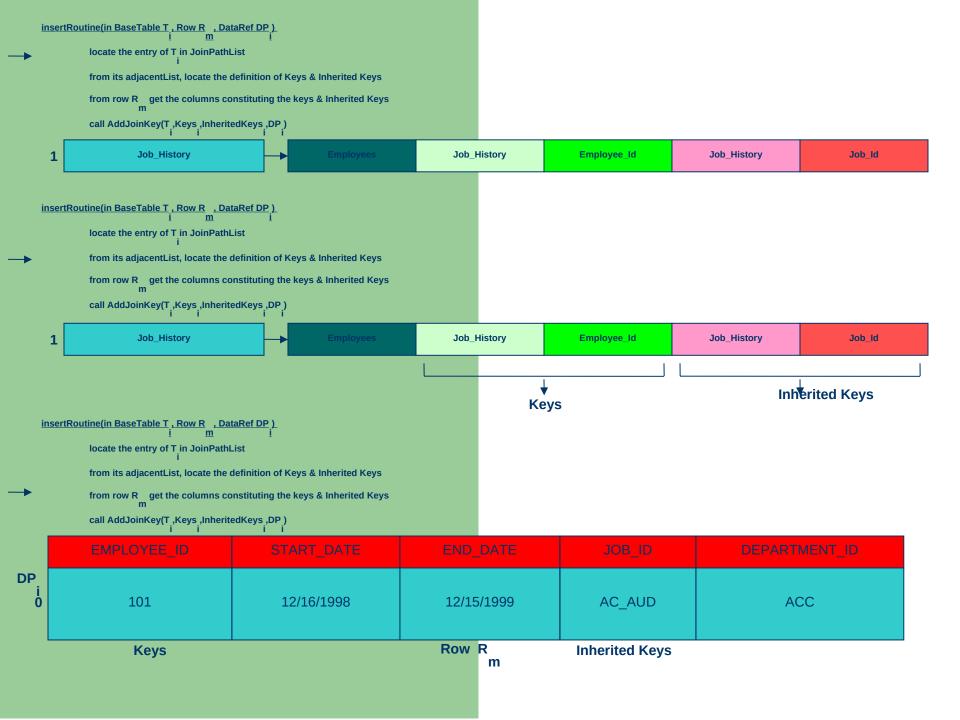


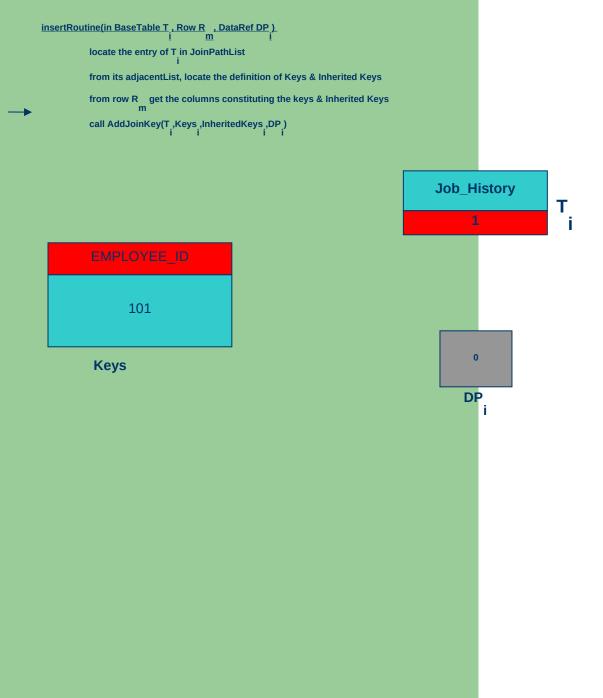
DataRef



	EMPLOYEE_ID	START_DATE	END_DATE	JOB_ID	DEPARTMENT_ID
DP i 0	101	12/16/1998	12/15/1999	AC_AUD	ACC

Row R m

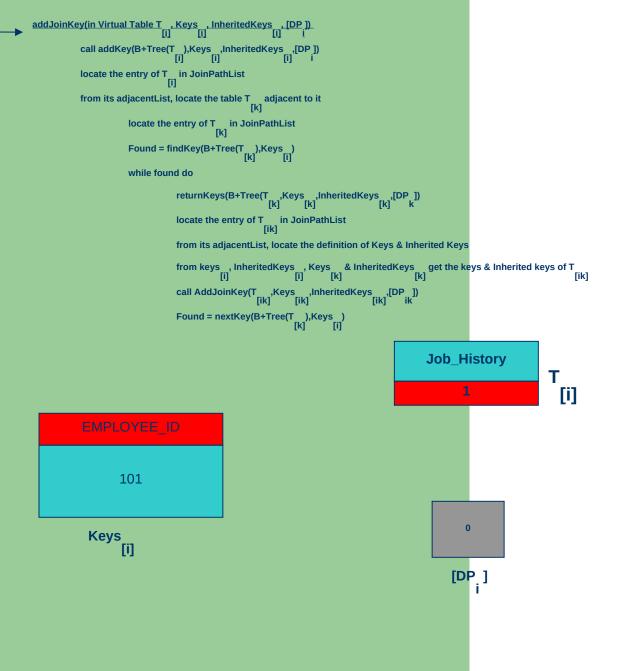




JOB_ID

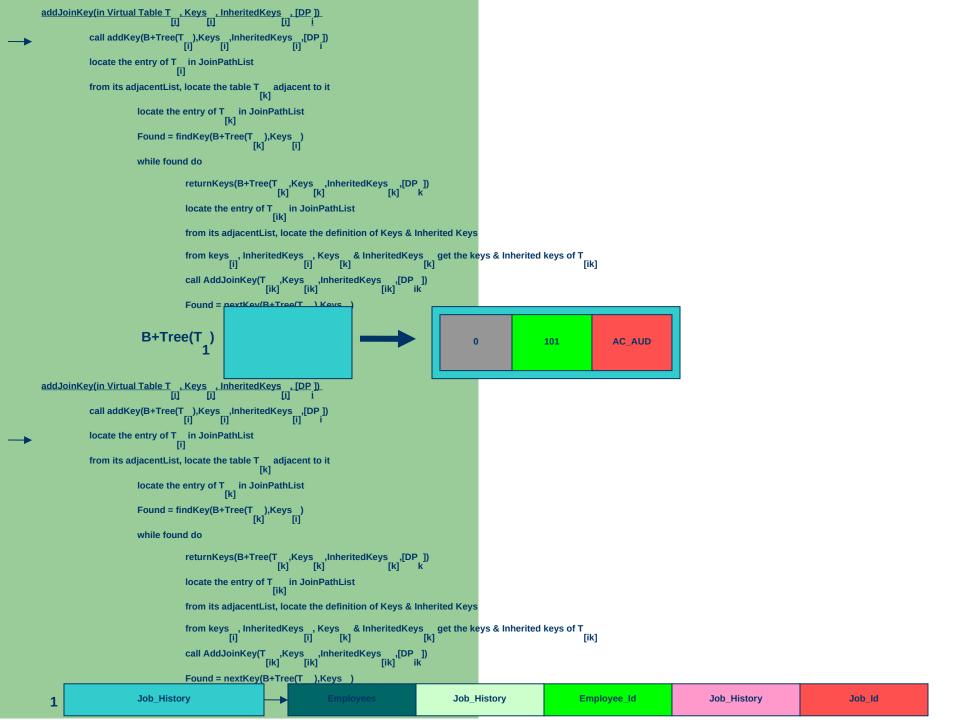
AC_AUD

Inherited Keys



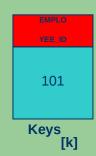
AC_AUD

Inherited Keys



```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                         call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP])
                         locate the entry of T__ in JoinPathList
                         from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                   locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                   Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                   while found do
                                                                             \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                             \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                              from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                             from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k]
                                                                             call AddJoinKey(T ,Keys ,InheritedKeys ,[ik] ,[DP ]) ik
                                                                             Found = nextKey(B+Tree(T__),Keys__)
                                                    Job_History
                                                                                                                                                                                                                               Job_History
                                                                                                                                                                                                                                                                                                   Employee_Id
                                                                                                                                                                                                                                                                                                                                                                          Job_History
                                                                                                                                                                                                                                                                                                                                                                                                                                                     Job Id
                                                                                                                                             Adjacent Table
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP])
                         locate the entry of T_{r:1} in JoinPathList
                         from its adjacentList, locate the table T \quad \text{adjacent to it} \quad [k]
                                                   Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                    while found do
                                                                             locate the entry of T in JoinPathList
                                                                              from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                             from keys , inherited
Keys , Keys & Inherited
Keys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] \\ \hline \end{tabular}
                                                                              call AddJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                              Found = nextKey(B+Tree(T ),Keys )
                                                     Employees
                                                                                                                                                                                                                                Employees
                                                                                                                                                                                                                                                                                                   Employee Id
                                                                                                                                                                                                                                                                                                                                                                          Employees
                                                                                                                                                                                                                                                                                                                                                                                                                                            Department_Id
```

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
             call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
             locate the entry of T_{\underline{\underline{\phantom{A}}}} in JoinPathList
             from its adjacentList, locate the table T {}_{\left[k\right]} adjacent to it
                           locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                           Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                           while found do
                                        {\it returnKeys} (B+Tree (T\_,Keys\_,InheritedKeys\_,[DP\_]) \\ [k]
                                         locate the entry of T _{\mbox{\scriptsize [ik]}} in JoinPathList
                                         from its adjacentList, locate the definition of Keys & Inherited Keys
                                         from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k]
                                         call AddJoinKey(T ,Keys ,InheritedKeys ,[IR],[DP]) _{ik}
                                         Found = nextKey(B+Tree(T<sub>[L]</sub>),Keys<sub>[i]</sub>)
                       B+Tree(T
                                                                                101
                                                                                                      FIN
                                                                                                                                    Found: TRUE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
             call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
             locate the entry of T _{\mbox{\scriptsize [i]}} in JoinPathList
             from its adjacentList, locate the table T % \left[ k\right] adjacent to it \left[ k\right]
                           \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                           Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                           while found do
                                         returnKeys(B+Tree(T ,Keys ,InheritedKeys ,[DP ])  
[k] [k] [k] k
                                         locate the entry of T___ in JoinPathList
                                         from its adjacentList, locate the definition of Keys & Inherited Keys
                                         from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                         call AddJoinKey(T _{[ik]},Keys _{[ik]},InheritedKeys _{[ik]},_{ik}
                                                                                                                                  Found: TRUE
                                         Found = nextKey(B+Tree(T_),Keys_)
```

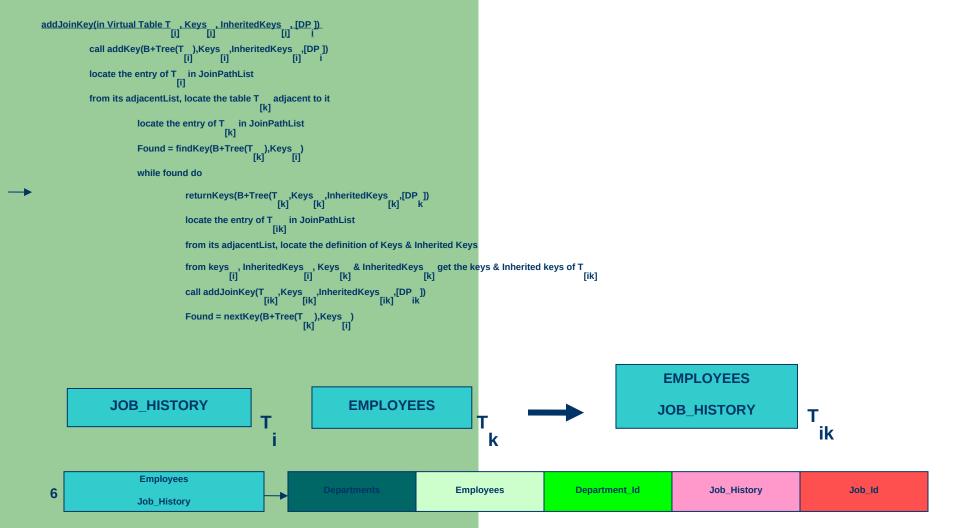


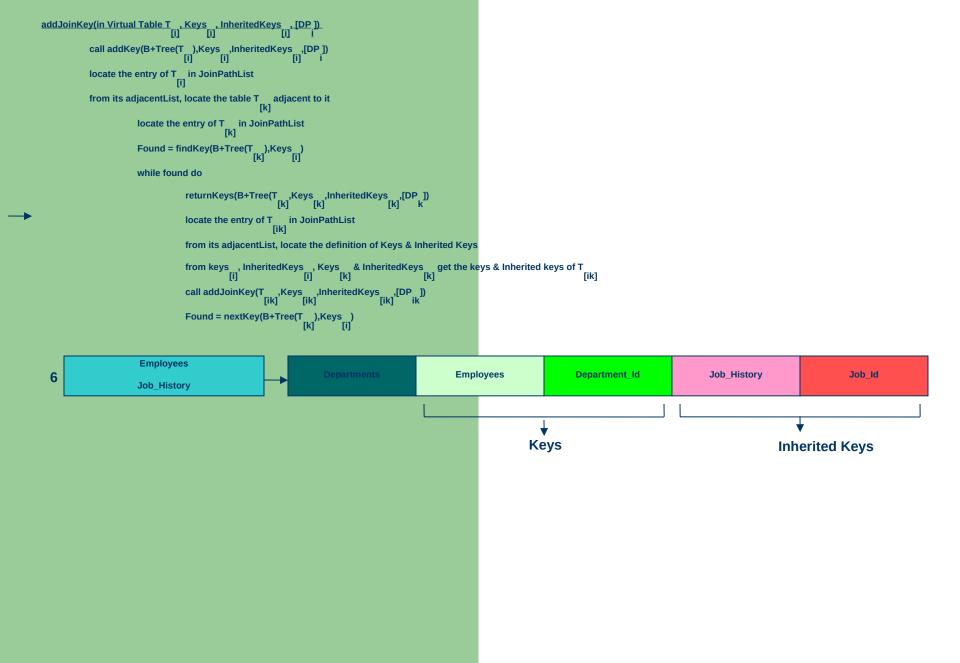
0 [DP]

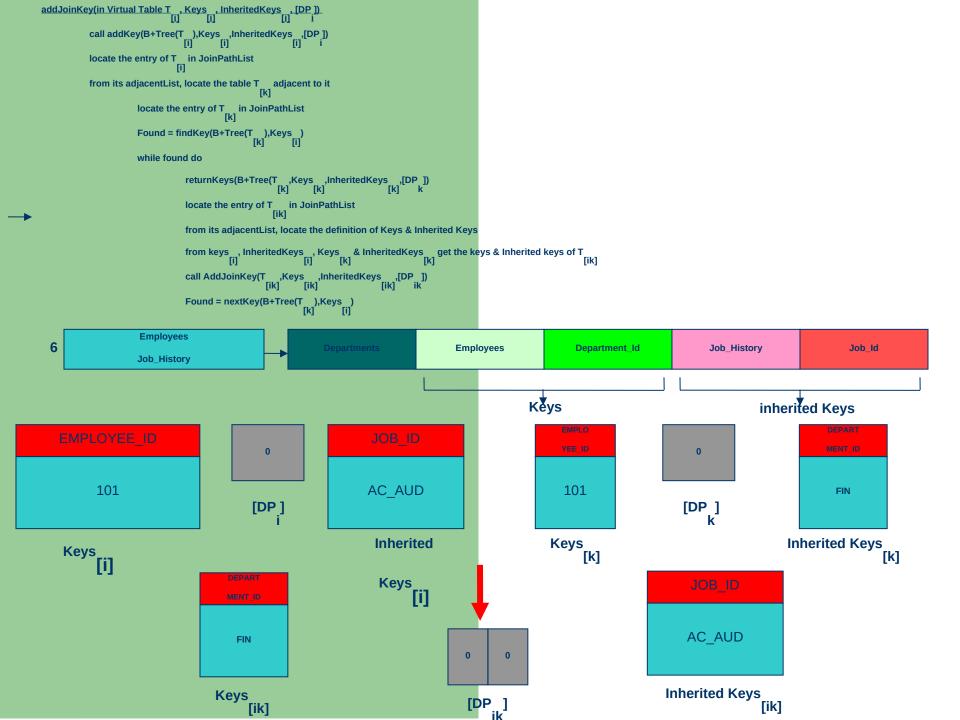


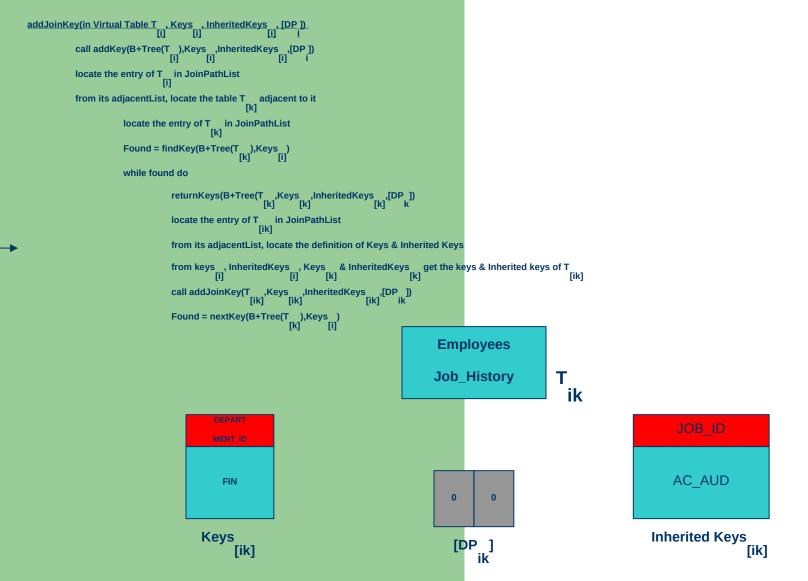
Inherited

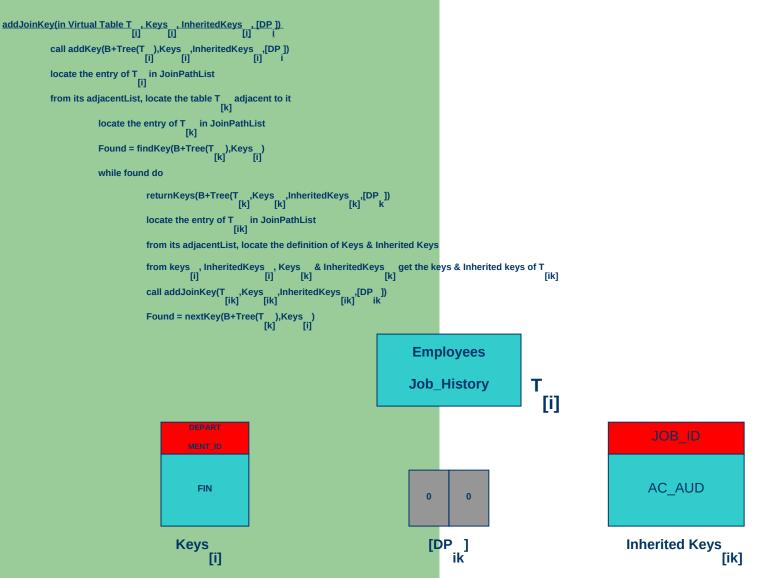
Keys [i

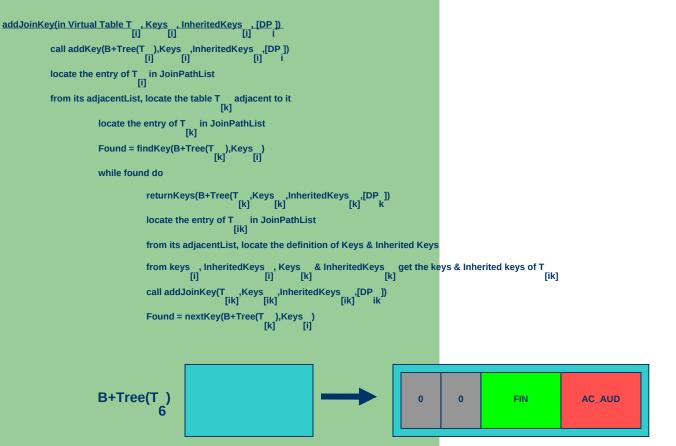


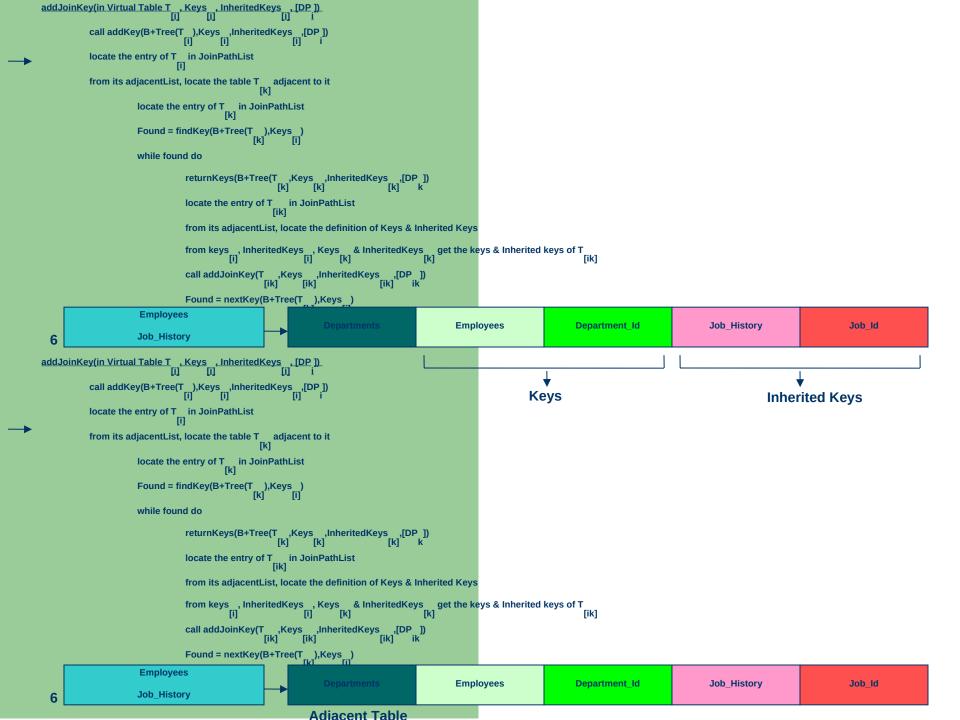












```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]).

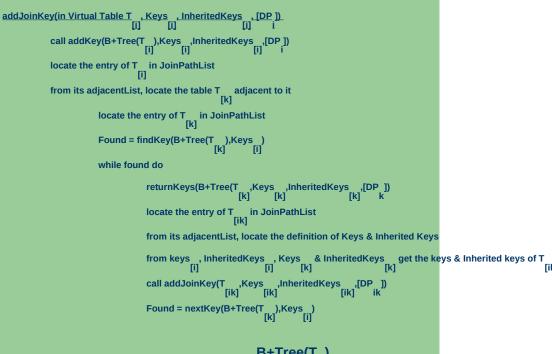
[i] [i] [i]
                           call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP_]) i [i] _{i}
                            locate the entry of T in JoinPathList [i]
                           from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                       \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                       Found = findKey(B+Tree(T ),Keys )
[k] [i]
                                                        while found do
                                                                                   locate the entry of T in JoinPathList
                                                                                    from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                    from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [k] [k]
                                                                                    call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                  Found = nextKey(B+Tree(T_),Keys_)

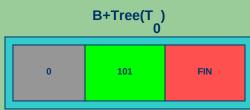
[k]

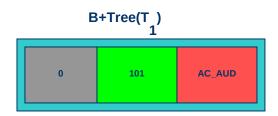
Employee
                                                                                                                                                                                                                                                                                                                       Department_Id
                                                        Deparments
                                                                                                                                                                                                                                               Departments
                                                                                                                                                                                                                                                                                                                                                                                                    Departments
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Location_Id
     2
     addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ])
[i] [i] [i]
                                  call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP]) [i] [i] i
                                  locate the entry of T in JoinPathList
                                  from its adjacentList, locate the table T {}^{\phantom{\dagger}} adjacent to it {}^{\phantom{\dagger}}
                                                              locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                              Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                              while found do
                                                                                          \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                          \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                          from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                          from keys , inherited
Keys , Keys & Inherited
Keys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                          call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik]
                                                                                          Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                      B+Tree(T)
                                                                                                                                                                                                                                                                                                                                                                     Found: FALSE
```

```
locate the entry of T__ in JoinPathList
                            from its adjacentList, locate the table T \, adjacent to it \, [k] \,
                                                        \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                        Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                        while found do
                                                                                     \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                     from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                     from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                     call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
[ik] [ik] [ik]
                                                                                     Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                        Found: FALSE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP])
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                            locate the entry of T in JoinPathList
                            from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                        locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                        Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                        while found do
                                                                                     \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                     locate the entry of T in JoinPathList [ik]
                                                                                     from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                     from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                     {\it call\ addJoinKey(T_{[ik]},Keys_{[ik]},InheritedKeys_{[ik]},[DP_{ik}])}
                                                                                     Found = nextKey(B+Tree(T__),Keys__)
[k] [i]
```

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                            locate the entry of T in JoinPathList [i]
                            from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                         \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                         Found = findKey(B+Tree(T_{[k]}),Keys_{[i]})
                                                         while found do
                                                                                      \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                       from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                       call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
[ik] [ik]
                                                                                    Found = nextKey(B+Tree(T_),Keys_)
B+Tree(T_)
                                                                                                                                                                                                                                                                                101
                                                                                                                                                                                                                                                                                                                                FIN
                                                                                                                                                                                                                                                                                                                                                                                         Found: FALSE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                            locate the entry of T in JoinPathList
                            from its adjacentList, locate the table T _{\mbox{\scriptsize [k]}} adjacent to it
                                                         \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                         Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                      \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                       locate the entry of T in JoinPathList [ik]
                                                                                       from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] get the keys & Inherited keys of T [k]
                                                                                       call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
[ik] [ik] [ik]
                                                                                                                                                                                                                                                                                                                                                                                     Found: FALSE
                                                                                       Found = nextKey(B+Tree(T ),Keys )
[k] [i]
```









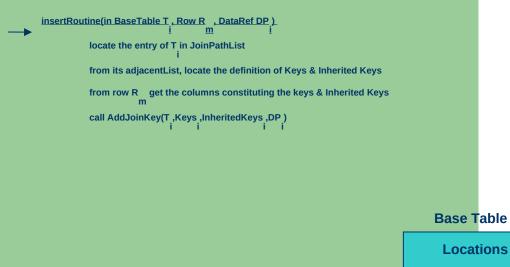
Inserting first row from table Locations

Base Table

Locations

4

LOCATION_ ID	STREET_ADDRESS	POSTAL_ CODE	CITY	STATE PROVINCE	COUNTRY_ ID
1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca

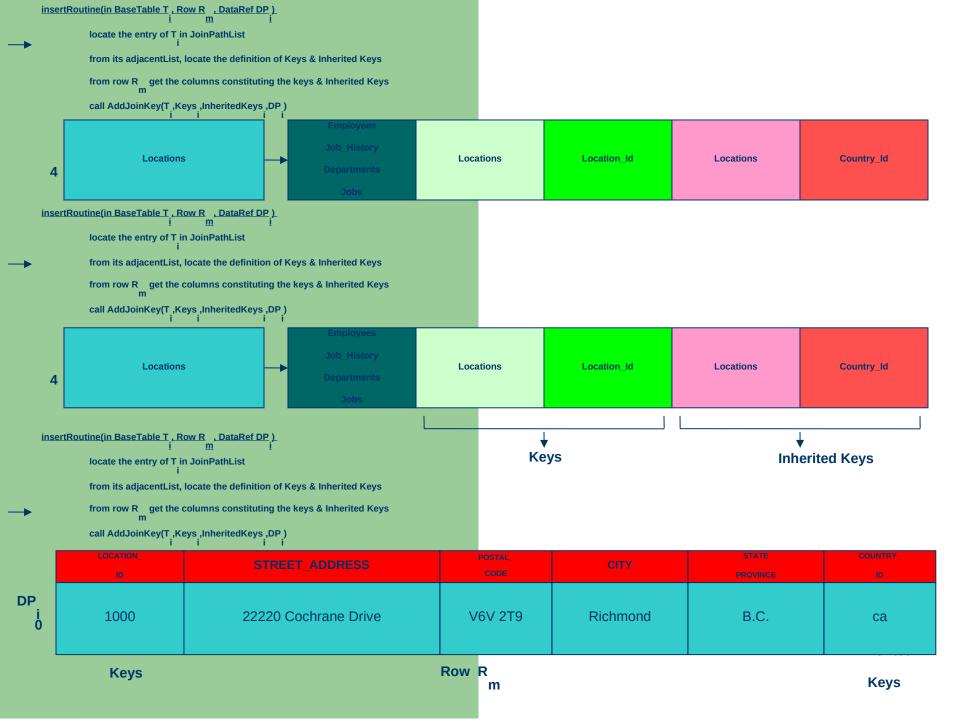


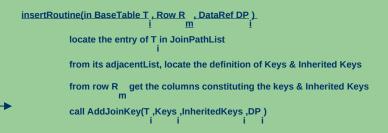
DataRef

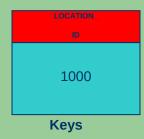
	LOCATION_ ID	STREET_ADDRESS POSTAL CODE		СІТҮ	STATE PROVINCE	COUNTRY_ ID
DP i 0	1000	22220 Cochrane Drive	V6V 2T9	Richmond	B.C.	ca

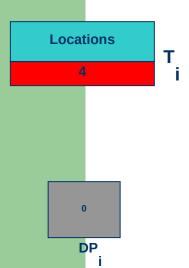
4

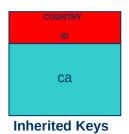
Row R m

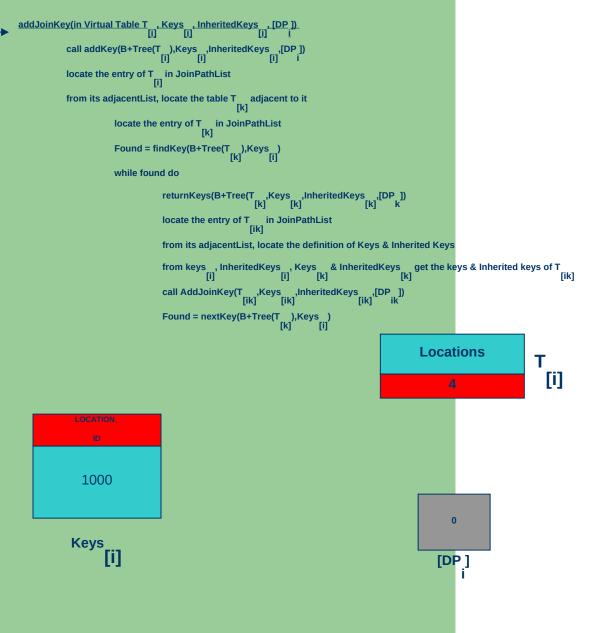




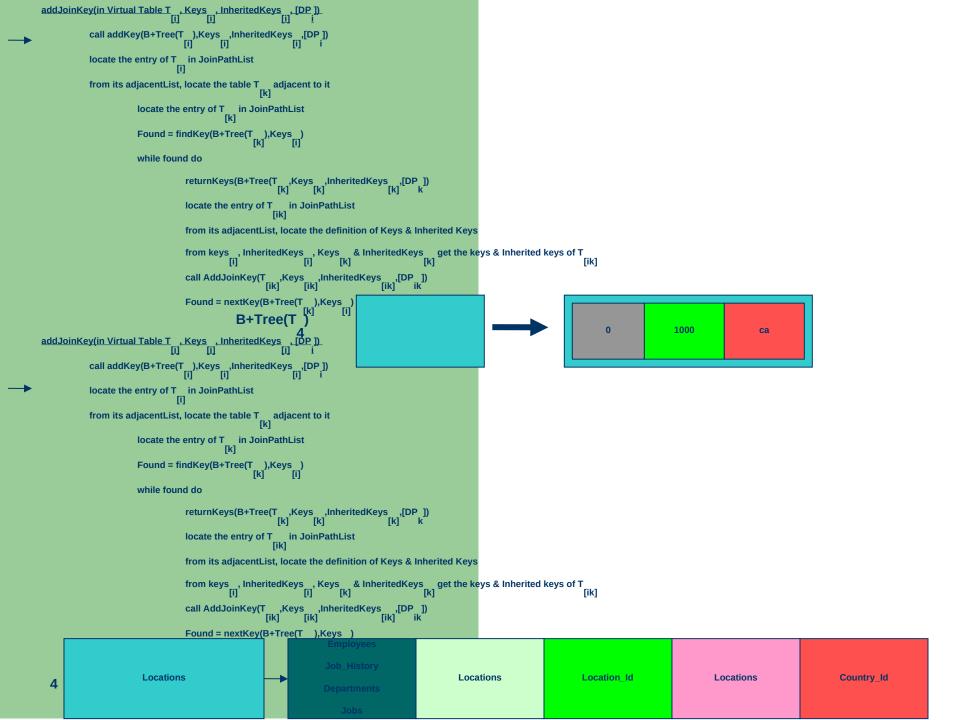


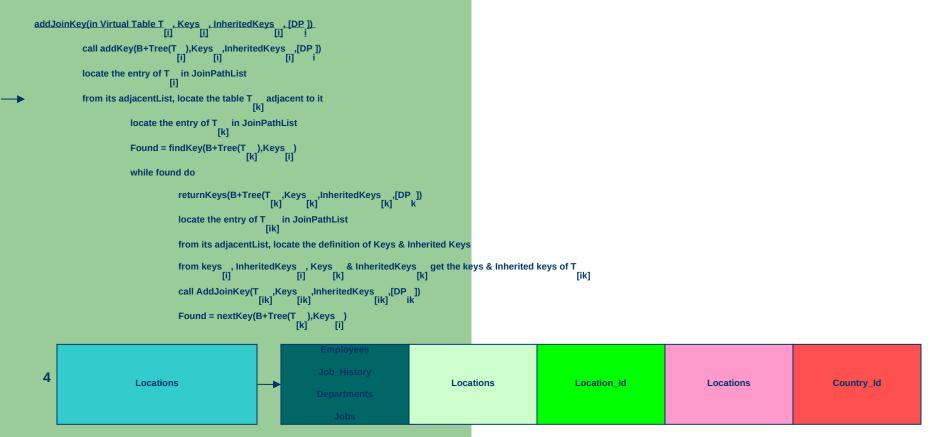








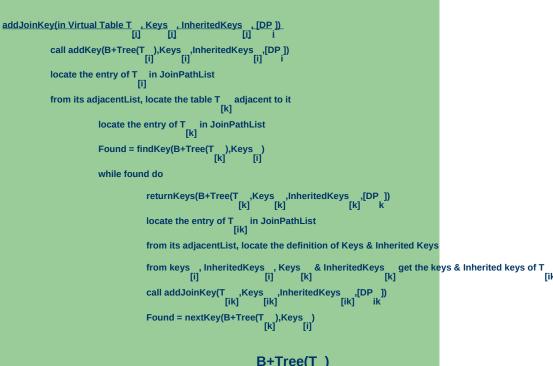


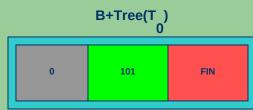


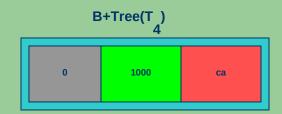
Adjacent Table



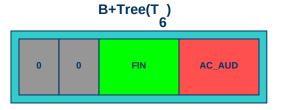
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,I[DP ]) i [i]
                            locate the entry of T in JoinPathList
                            from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                        locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                        Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                        while found do
                                                                                    \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                    locate the entry of T {\color{red}\text{in JoinPathList}} {\color{red}\text{[ik]}}
                                                                                     from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                    from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T
                                                                                    call AddJoinKey(T ,Keys ,InheritedKeys ,[IR],[DP]) _{ik}
                                                                                     Found = nextKey(B+Tree(T___),Keys___)
                                                                                                                                                                                                                         Found: FALSE
                                                         B+Tree(T)
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP]) [i] [i] i
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ]) i
                            \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \text{[i]} \end{array}
                            from its adjacentList, locate the table T adjacent to it
                                                        \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \quad [k] \end{array}
                                                        Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                         while found do
                                                                                    locate the entry of T in JoinPathList
                                                                                     from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                     from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T
[i] [k] [k] [k]
                                                                                    call AddJoinKey(T ,Keys ,InheritedKeys ,[DP ])
                                                                                                                                                                                                                        Found: FALSE
                                                                                     Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
```











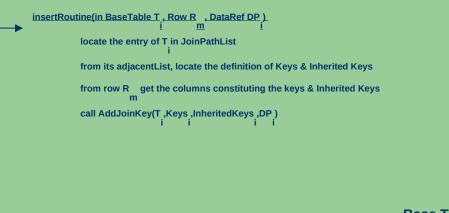
Inserting first row from table Departments

Base Table

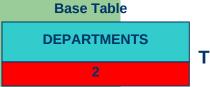
DEPARTMENTS

2

Deparment_Id	Department_Name	Manager_Id	Location_ld
FIN	FINANCE	101	1000

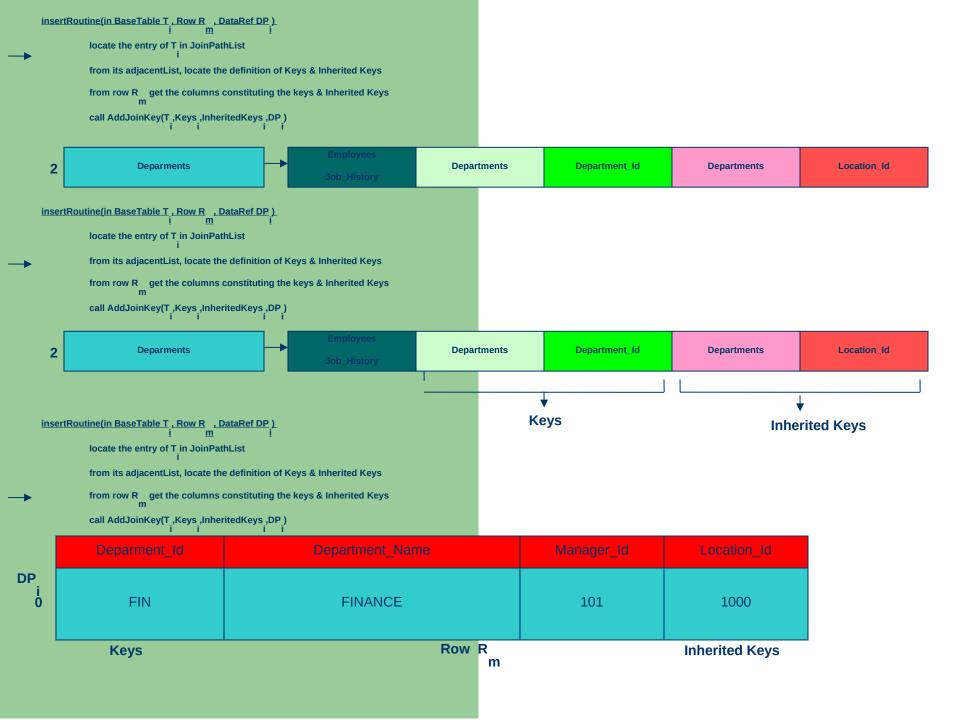


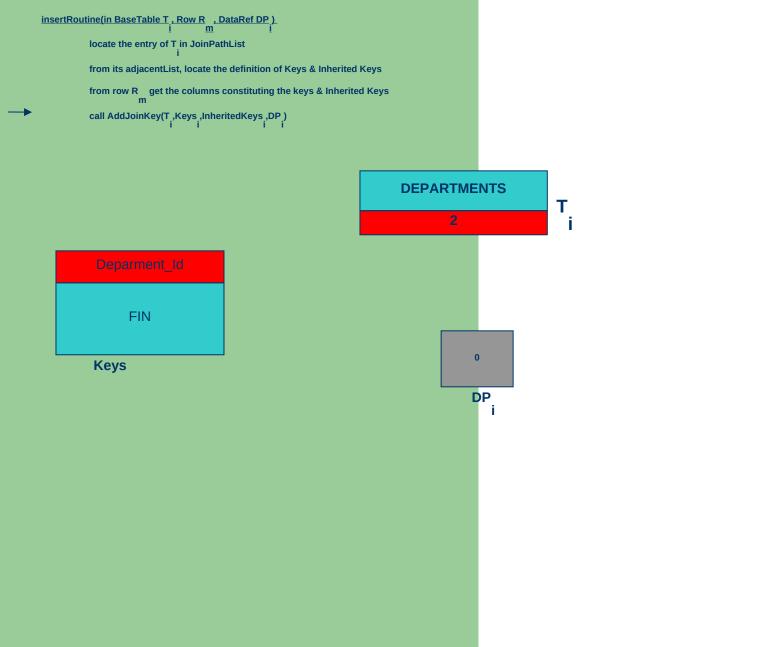
DataRef



	Deparment_Id	Department_Name	Manager_ld	Location_Id
DP i 0	FIN	FINANCE	101	1000

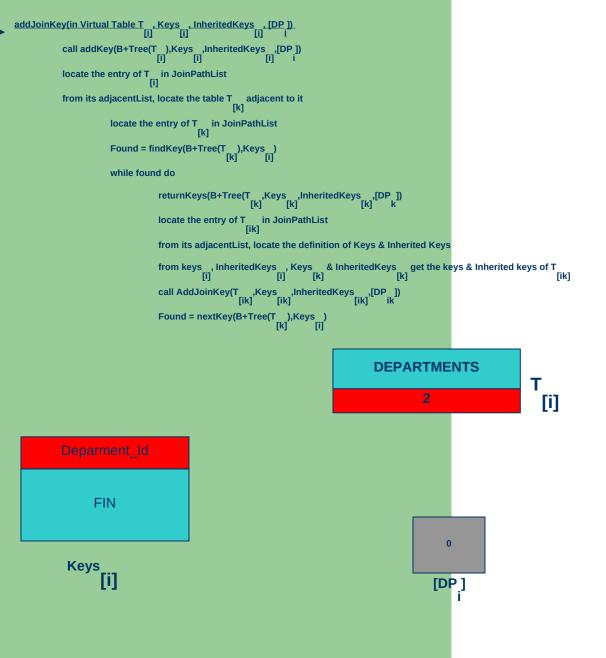
Row R m

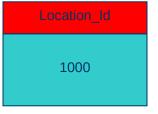




1000

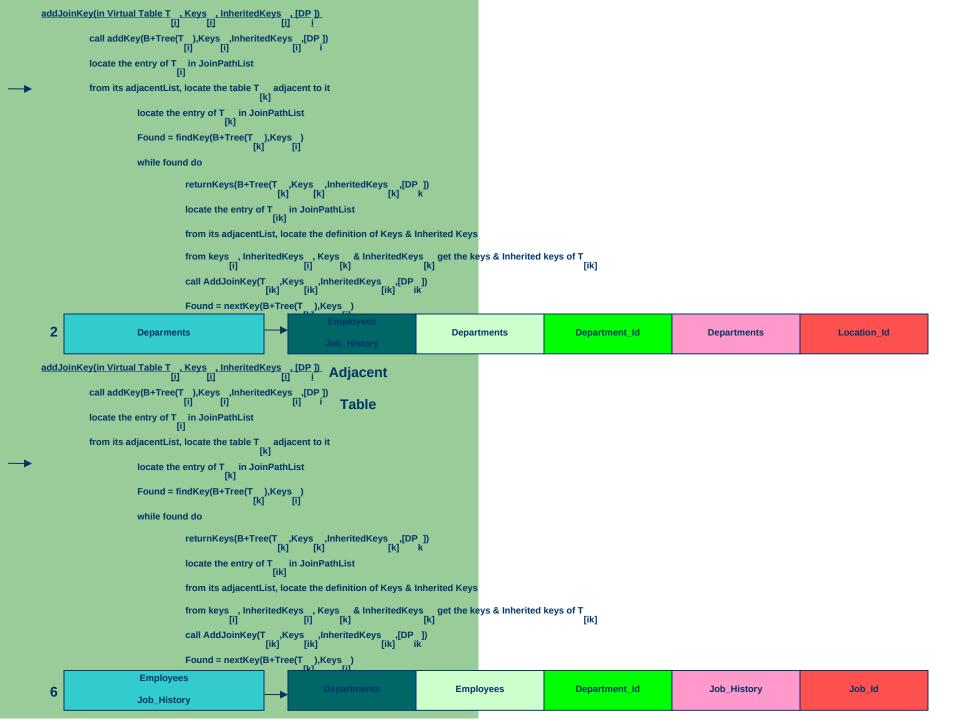
Keys



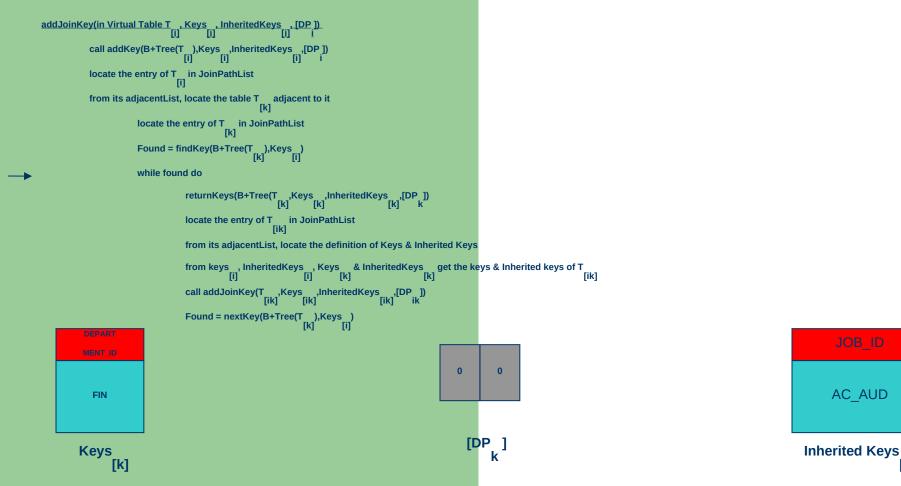


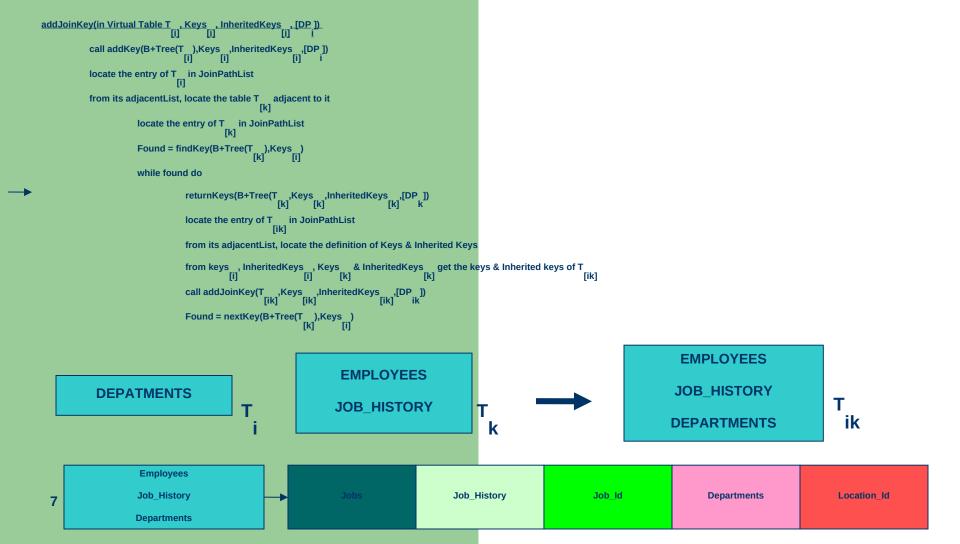
Inherited Keys
[i]

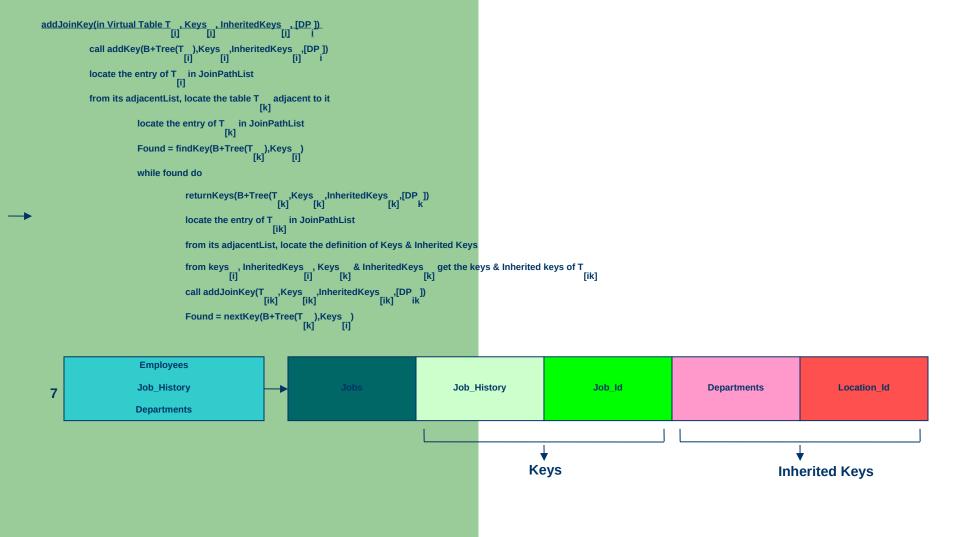
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
             call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
             locate the entry of T_{r:1} in JoinPathList
             from its adjacentList, locate the table T \, adjacent to it \, [k] \,
                           \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                           Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                           while found do
                                         returnKeys(B+Tree(T ,Keys ,InheritedKeys ,[DP ])
                                         locate the entry of T _{\rm [ik]} in JoinPathList
                                         from its adjacentList, locate the definition of Keys & Inherited Keys
                                         from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                                                                                            [ik]
                                         call AddJoinKey(T_ik],Keys_,InheritedKeys_,[ik],[DP_ik]
                                        Found = nextKey(B+Tree(T<sub>[k]</sub>),Keys<sub>[i]</sub>
B+Tree(T<sub>)</sub>
                                                                                                                                                                                                               FIN
                                                                                                                                                                                                                                     1000
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
             call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad [i]
             \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \text{[i]} \end{array}
             from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                           \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                           Found = findKey(B+Tree(T_),Keys_)
[k]
[i]
                           while found do
                                         locate the entry of T in JoinPathList [ik]
                                         from its adjacentList, locate the definition of Keys & Inherited Keys
                                         from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                         call AddJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                         Found = nextKey(B+Tree(T_),Keys_)
                           Deparments
                                                                                                                                                          Department_Id
  2
                                                                                                                      Departments
                                                                                                                                                                                                Departments
                                                                                                                                                                                                                                     Location_Id
```

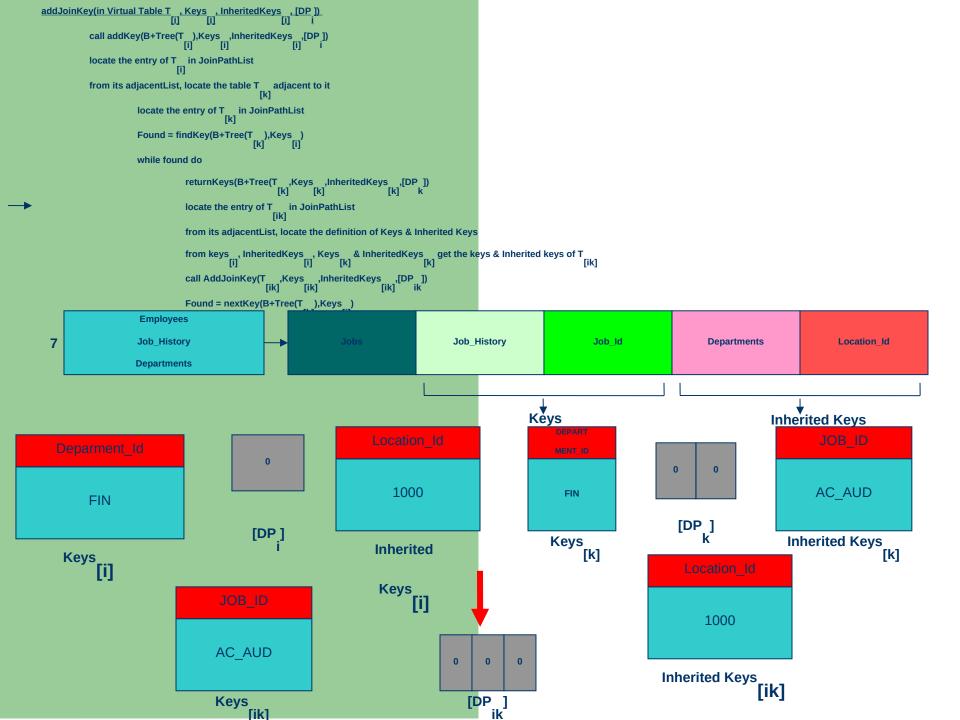


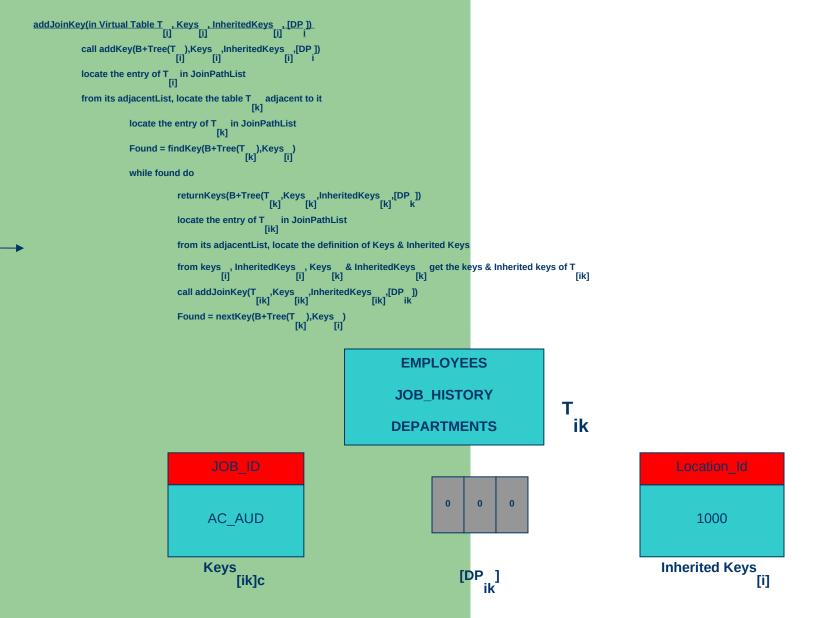
```
call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP_]) i
                           locate the entry of T in JoinPathList [i]
                           from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                      \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ \text{[k]} \end{array}
                                                      Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                       while found do
                                                                                  \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                  locate the entry of T_{r:1,2} in JoinPathList
                                                                                  from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                  from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                   call AddJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                   Found = nextKey(B+Tree(T___),Keys__)
                                        B+Tree(T)
                                                                                                                                                                FIN
                                                                                                                                                                                                                                                                            Found: TRUE
                                                                                                                                                                                                        AC_AUD
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i]
                           call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
                           locate the entry of T _{\mbox{\scriptsize [i]}} in JoinPathList
                           from its adjacentList, locate the table T \quad adjacent to it \quad [k]
                                                       locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                       Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                       while found do
                                                                                  locate the entry of T___ in JoinPathList
                                                                                   from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                  from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                  {\it call AddJoinKey(T_{[ik]}, Keys, InheritedKeys, [ik], [DP_{ik}])}
                                                                                                                                                                                                                                                                Found: TRUE
                                                                                   Found = nextKey(B+Tree(T_),Keys_)
```

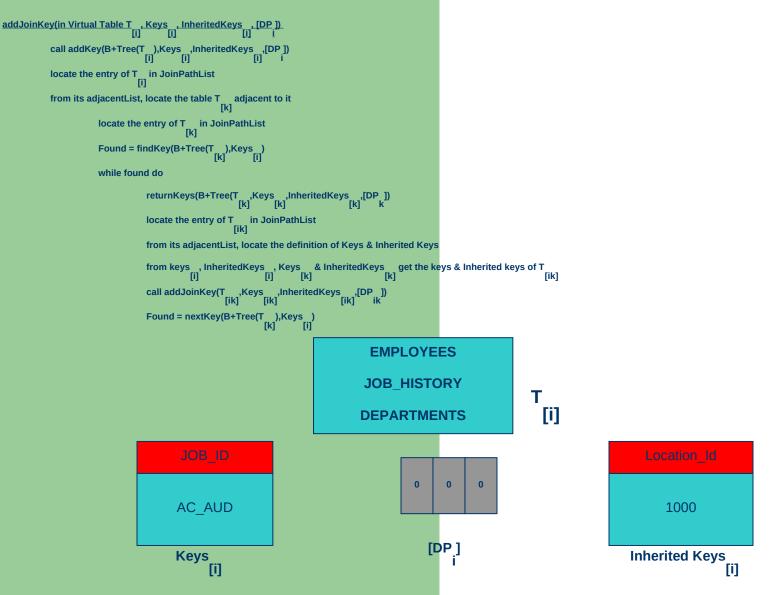


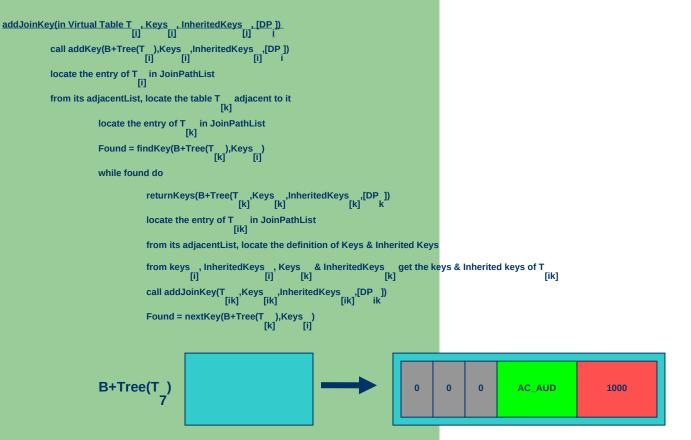


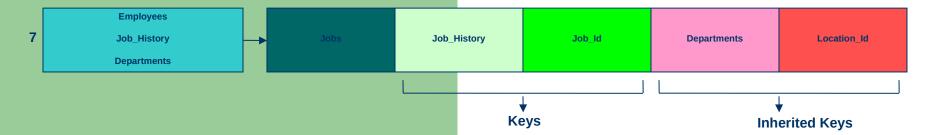














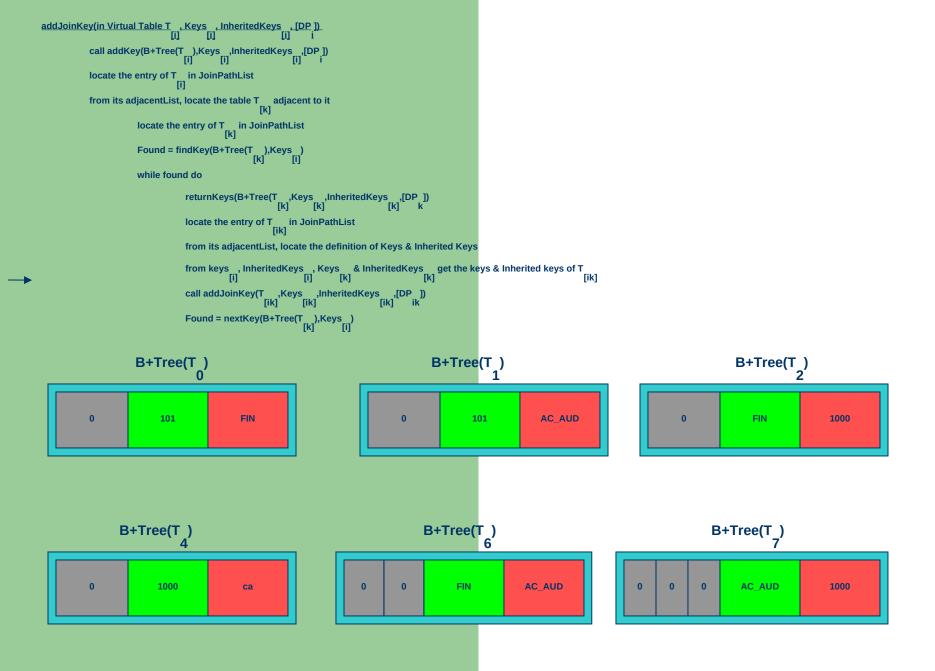
Adjacent Table

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                            call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP_]) i [i] _{i}
                            \begin{array}{ccc} \text{locate the entry of T} & \text{in JoinPathList} \\ & & [i] \end{array}
                            from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                         \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \text{[k]} \end{array}
                                                         Found = findKey(B+Tree(T ),Keys )
[k] [i]
                                                          while found do
                                                                                      locate the entry of T___ in JoinPathList
                                                                                       from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                       call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] [ik] ik
                                                                                      Found = nextKey(B+Tree(T<sub>r1-1</sub>),Keys<sub>r1</sub>)
                                                                   Jobs
                                                                                                                                                                                                                                                                 Jobs
                                                                                                                                                                                                                                                                                                                                            Job Id
     3
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                             locate the entry of T in JoinPathList [i]
                            from its adjacentList, locate the table T _{\mbox{\scriptsize [k]}} adjacent to it
                                                         Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                      \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                      locate the entry of T in JoinPathList [ik]
                                                                                      from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T
[i] [k] [k]
                                                                                       call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
                                                                                                                                                                                                                                         B+Tree(T)
                                                                                       Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
```

Found: FALSE

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                             locate the entry of T__ in JoinPathList
                             from its adjacentList, locate the table T \, adjacent to it \, [k] \,
                                                         \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \text{[k]} \end{array}
                                                          Found = findKey(B+Tree(T_{[k]}),Keys_{[i]})
                                                          while found do
                                                                                        return Keys (B+Tree (T\_, Keys\_, Inherited Keys\_, [DP\_]) \\ [k] [k] [k] 
                                                                                       \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                        from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                       from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                       call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
                                                                                                                                                                                                       Found: FALSE
                                                                                       Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                             call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                             locate the entry of T in JoinPathList
                             from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                          locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                          Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                       \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                        locate the entry of T in JoinPathList [ik]
                                                                                        from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                        from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                       {\it call\ addJoinKey(T_{[ik]},Keys_{[ik]},InheritedKeys_{[ik]},[DP_{ik}])}
                                                                                        Found = nextKey(B+Tree(T__),Keys__)
[k] [i]
```

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                              call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP_]) i [i] _{i}
                              \begin{array}{ccc} \text{locate the entry of T} & \text{in JoinPathList} \\ & & [i] \end{array}
                              from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                           \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                           Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                             while found do
                                                                                           return Keys (B+Tree (T\_, Keys\_, Inherited Keys\_, [DP\_]) \\ [k] [k] [k] 
                                                                                          locate the entry of T in JoinPathList
                                                                                           from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                          from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                           call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] [ik] ik
                                                                                          Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                                                                                                     Found: FALSE
                                                                                                                                                                                                                          AC AUD
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                              call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                              locate the entry of T in JoinPathList [i]
                              from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                           locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                            Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                             while found do
                                                                                          \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                          \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                           from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                          from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] get the keys & Inherited keys of T [k]
                                                                                           call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
[ik] [ik] [ik]
                                                                                                                                                                                                                                                                                                 Found: FALSE
                                                                                          Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
```

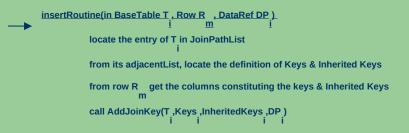


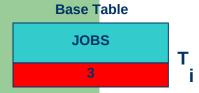
Inserting first row from table Jobs

Base Table

JOBS 3

JOB_ID	JOB_TITLE	MIN_SALARY	MAX_SALARY
AC_AUD	Accounting Auditor	30000	60000

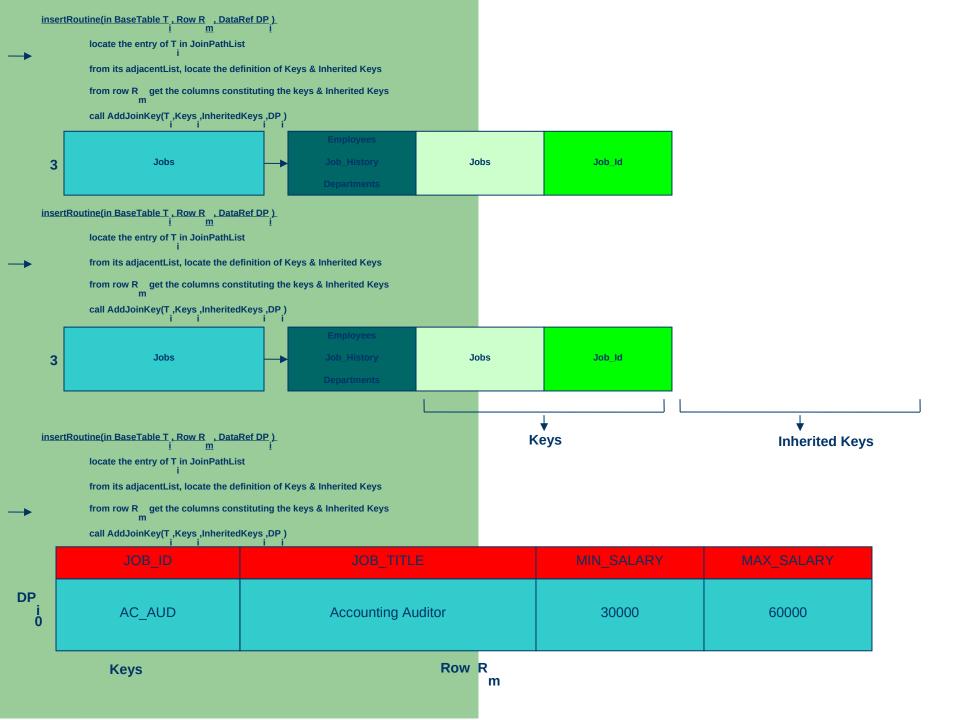


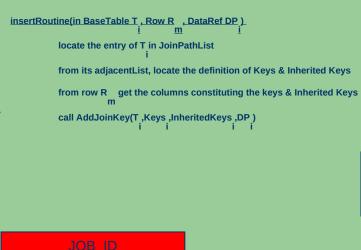


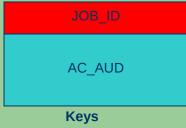
	JOB_ID	JOB_TITLE	MIN_SALARY	MAX_SALARY
DP i 0	AC_AUD	Accounting Auditor	30000	60000
DataRe	ef	Row R		

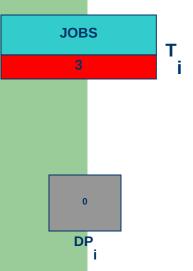
Row R

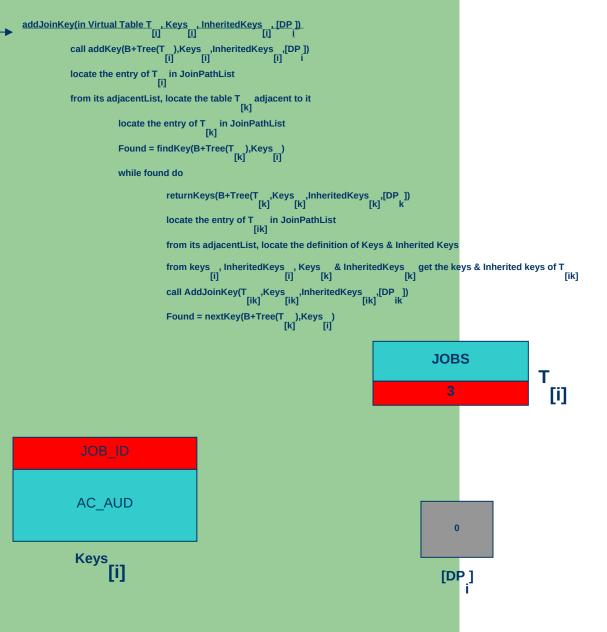
m

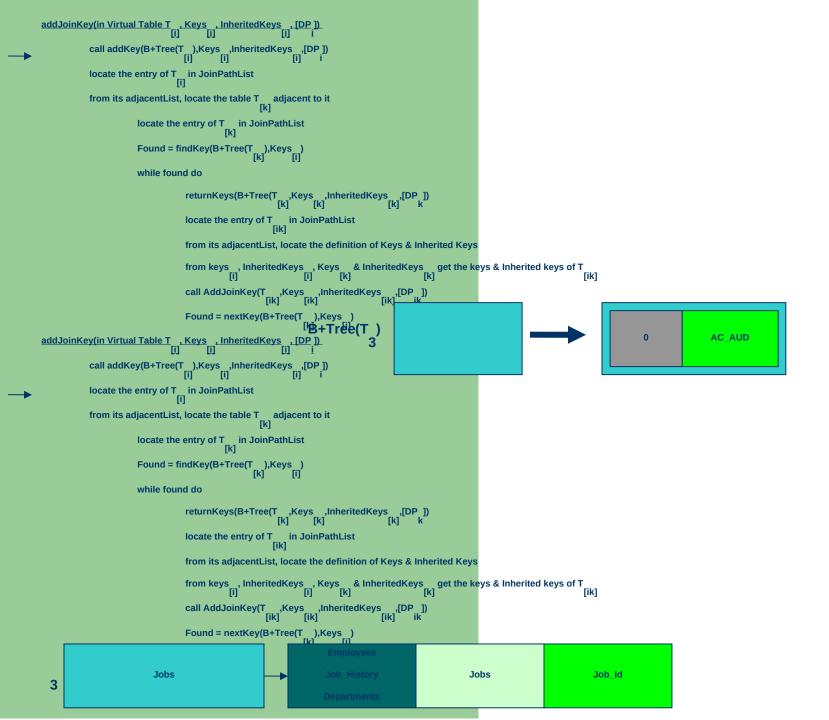


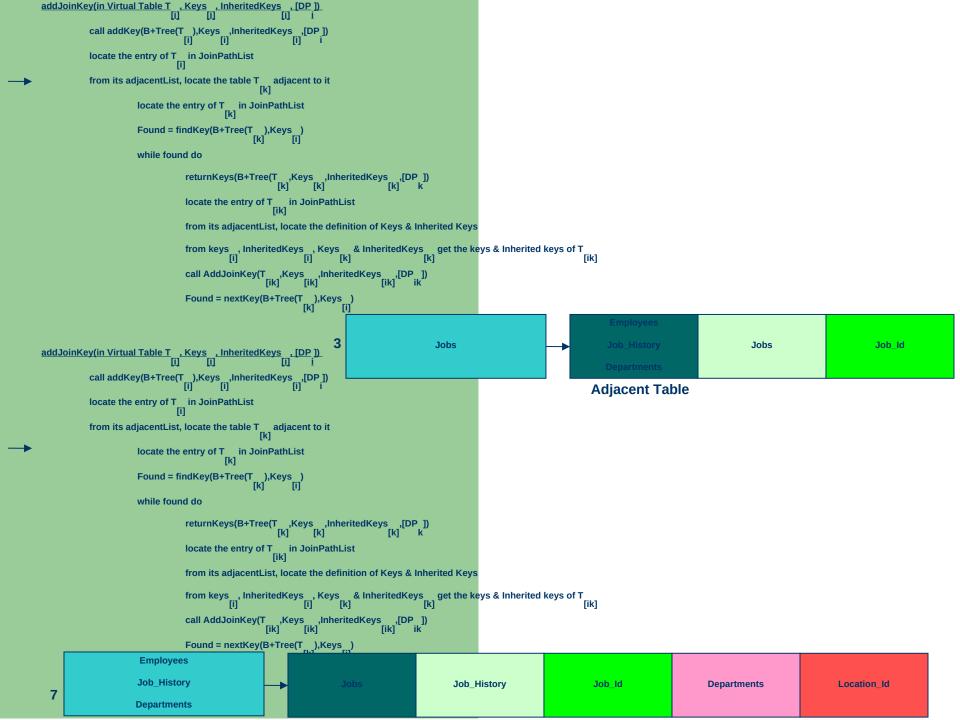




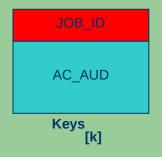


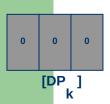






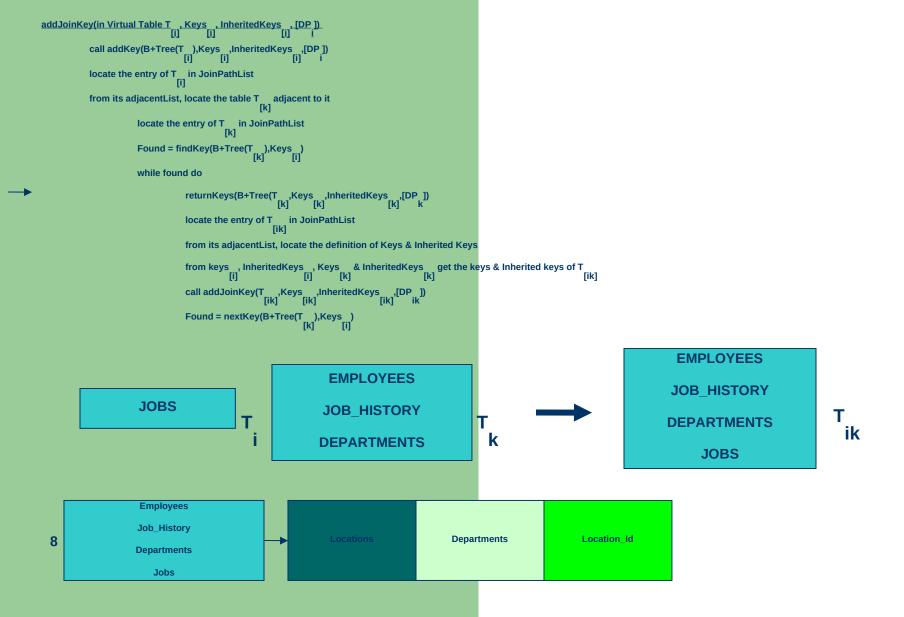
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                           call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
                           locate the entry of T in JoinPathList
                           from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                      locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                       Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                       while found do
                                                                                 \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                 locate the entry of T in JoinPathList [ik]
                                                                                  from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                 from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T
                                                                                                                                                                                                                                                 B+Tree(T)
                                                                                  Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                                                                                                                                                                                                 Found: TRUE
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                                  AC_AUD
                                                                                                                                                                                                                                                                                                                    1000
                                                                                                                                                                                                                        0
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                           call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
                           locate the entry of T in JoinPathList [i]
                           from its adjacentList, locate the table T \quad \text{adjacent to it} \quad [k]
                                                      locate the entry of T in JoinPathList
                                                      Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                       while found do
                                                                                  returnKeys(B+Tree(T ,Keys ,InheritedKeys ,[DP ])  
[k] [k] [k] k
                                                                                 locate the entry of T in JoinPathList
                                                                                  from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                 from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                 call AddJoinKey(T ,Keys ,InheritedKeys ,[DP ])
                                                                                                                                                                                                                                                                                                                                                                                            Found: TRUE
                                                                                  Found = nextKey(B+Tree(T_),Keys_)
```

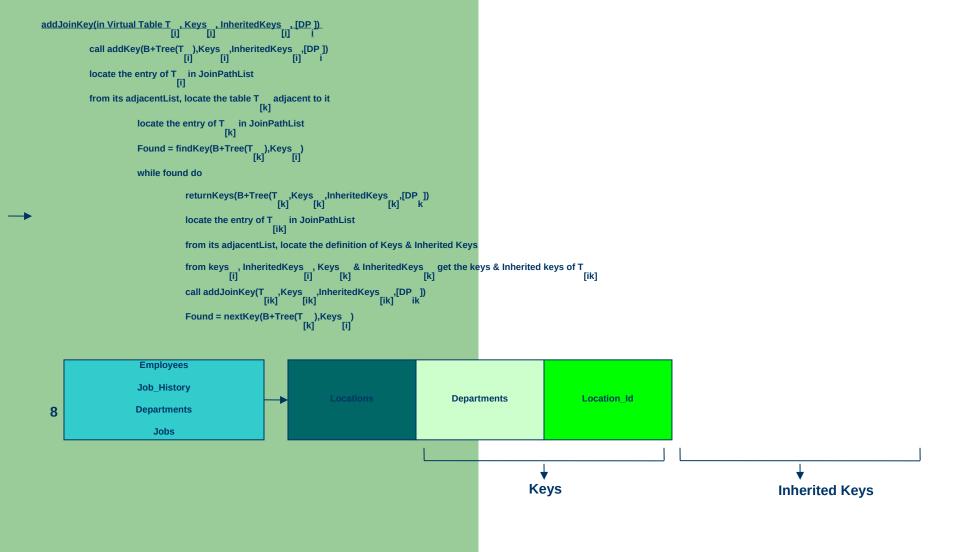


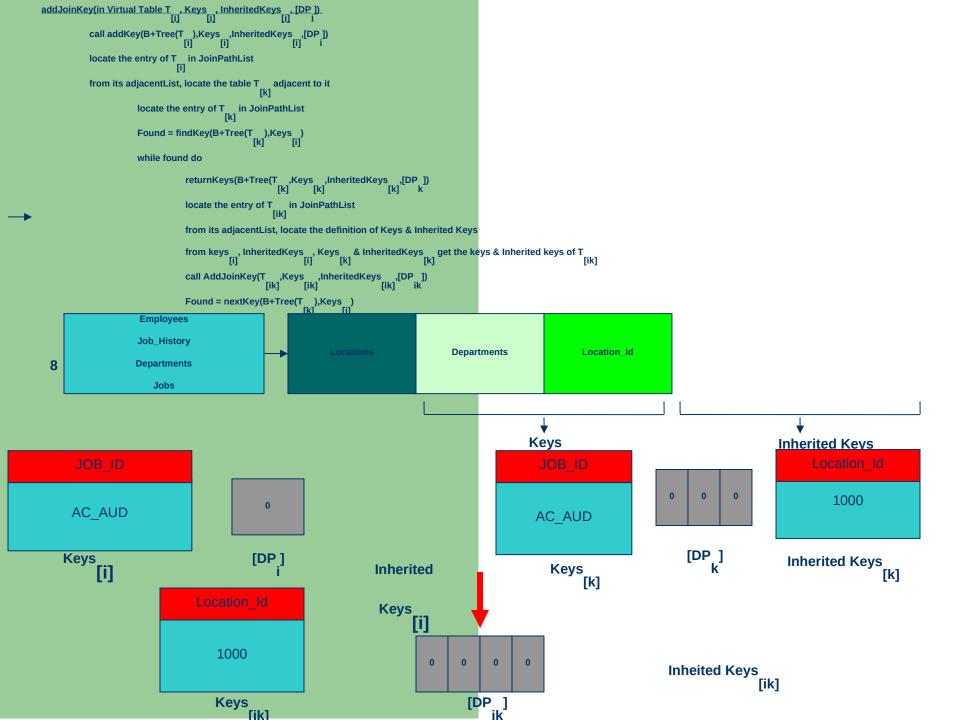


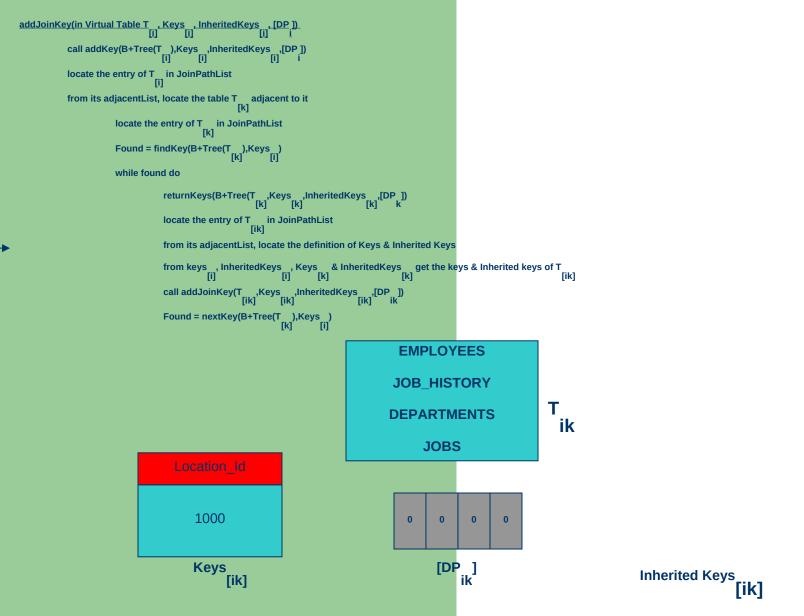
Location_Id
1000

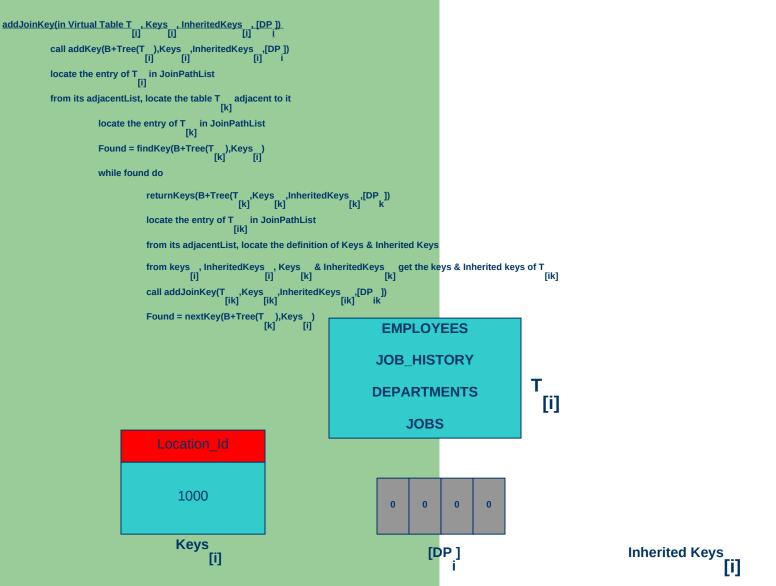
Inherited Keys [i

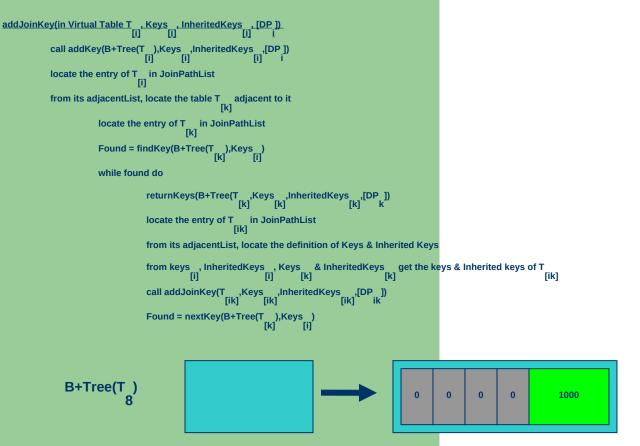












```
addJoinKey(in Virtual Table T___, Keys__, InheritedKeys__, IDP_]).

call addKey(B+Tree(T__),Keys__, InheritedKeys___, IDP_])
locate the entry of T__ in JoinPathList

from its adjacentList, locate the table T__ adjacent to it

locate the entry of T__ in JoinPathList

Found = findKey(B+Tree(T__,),Keys__,)

while found do

returnKeys(B+Tree(T__, Keys__, InheritedKeys__, InheritedK
```





Adjacent

Table

```
addJoinKey(in Virtual Table T __, Keys __, InheritedKeys __, [DP_]).

call addKey(B+Tree(T __), Keys __, InheritedKeys __, [DP_])

locate the entry of T __ in JoinPathList

from its adjacentList, locate the table T __ adjacent to it

locate the entry of T __ in JoinPathList

Found = findKey(B+Tree(T __), Keys __, InheritedKeys __, [DP_])

while found do

returnKeys(B+Tree(T __, Keys __, InheritedKeys __, [DP_])

locate the entry of T __ [ik] in JoinPathList

from its adjacentList, locate the definition of Keys & Inherited Keys

from keys __, InheritedKeys __, Keys __ & InheritedKeys __ [k]

call addJoinKey(T __, Keys __, InheritedKeys __, [DP_])

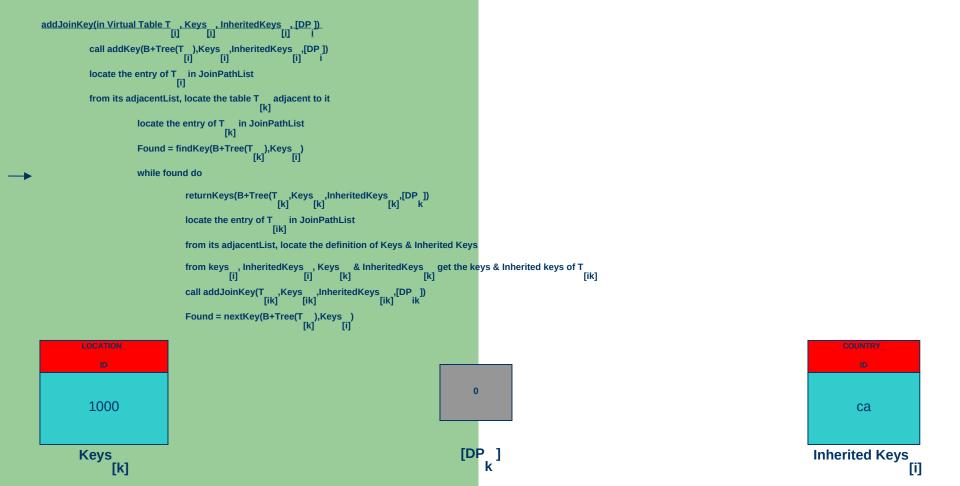
call addJoinKey(T __, Keys __, InheritedKeys __, [DP_])

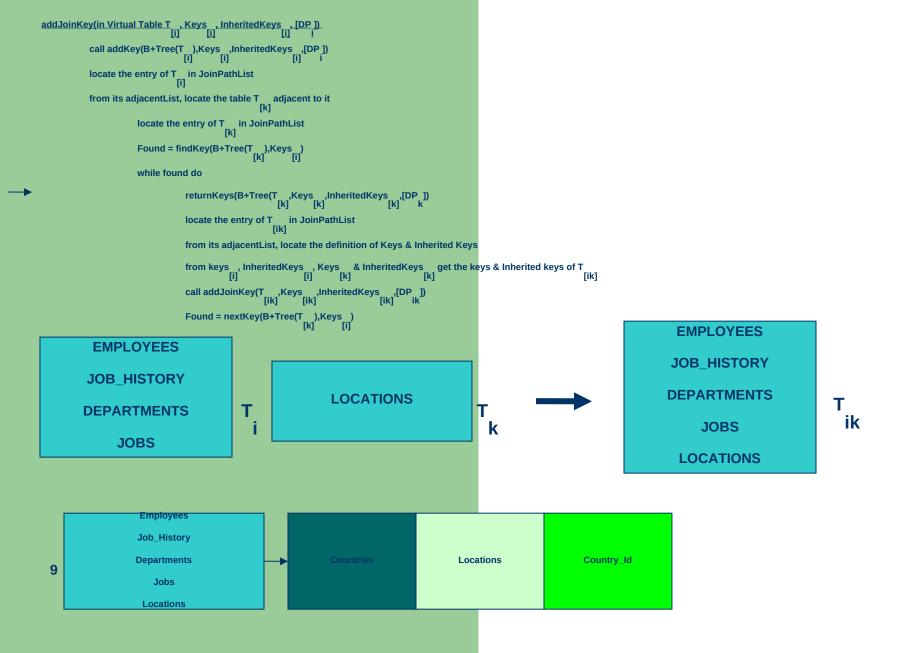
Found = nextKey(B+Tree(T __, Keys __, InheritedKeys __, [DP_])

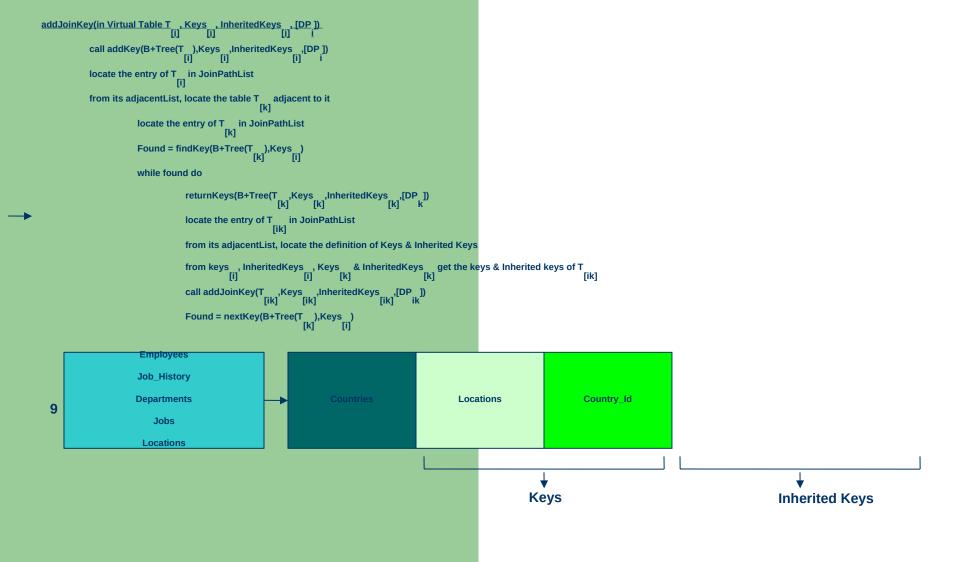
Found = nextKey(B+Tree(T __, Keys __, InheritedKeys __, [DP_])
```

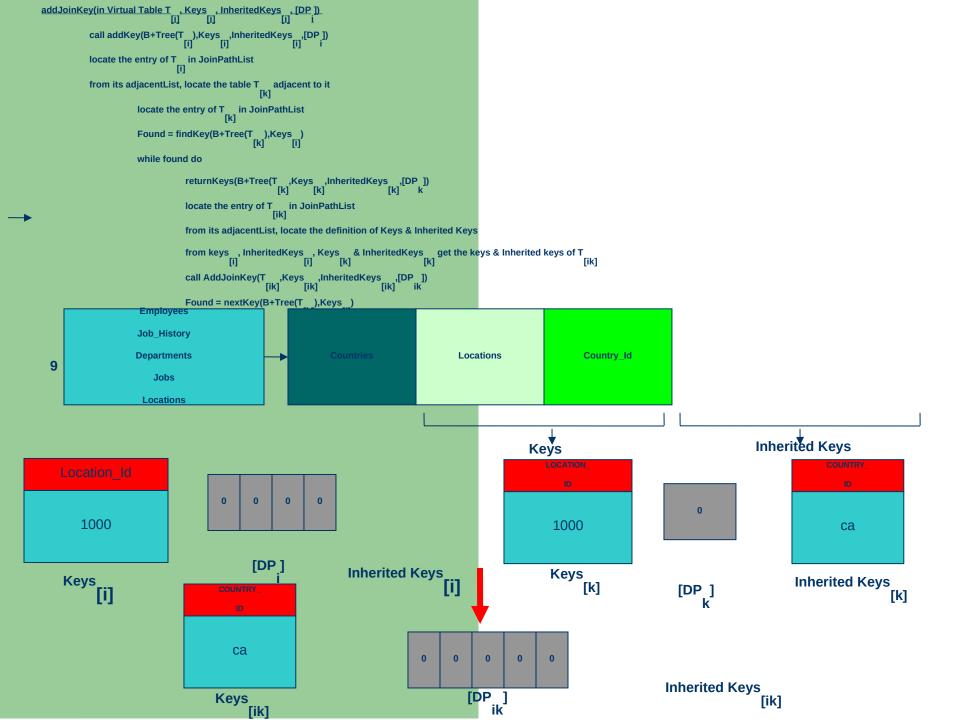


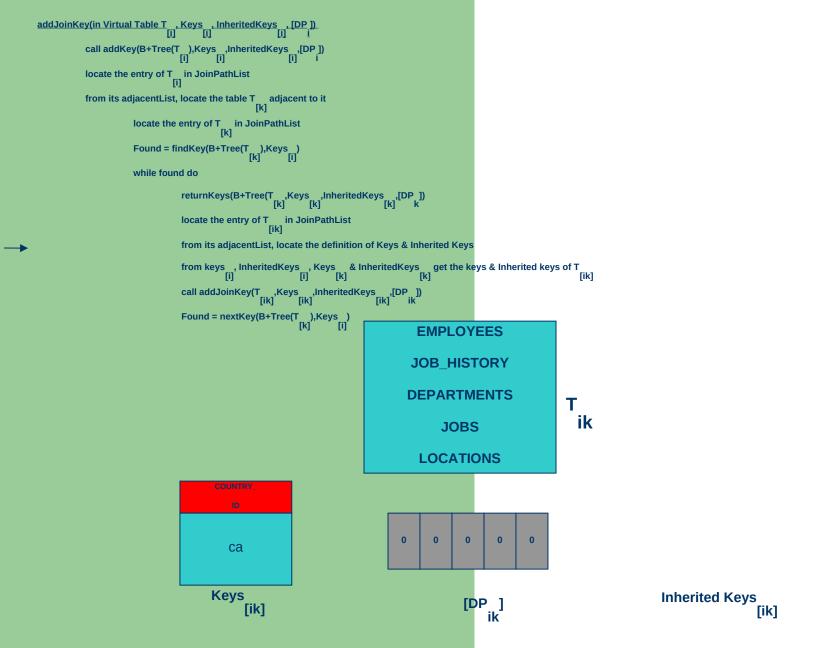
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
            locate the entry of T in JoinPathList
            from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                         locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                         Found = findKey(B+Tree(T_),Keys_)
[k]
[i]
                         while found do
                                       return Keys (B+Tree (T_{[k]}, Keys_{,} Inherited Keys_{[k]}, [DP_{]}) \\
                                      locate the entry of T _{\mbox{\scriptsize [ik]}} in JoinPathList
                                      from its adjacentList, locate the definition of Keys & Inherited Keys
                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                      call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] [ik] ik
                                      Found = nextKey(B+Tree(T ),Keys )
      B+Tree(T
                                                        1000
                                                                                                                                        Found: TRUE
                                                                              ca
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]).
[i] [i] [i]
            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
            locate the entry of T _{\mbox{\scriptsize [i]}} in JoinPathList
            from its adjacentList, locate the table T \quad adjacent to it \quad [k]
                         \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                         Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                         while found do
                                      locate the entry of T___ in JoinPathList
                                      from its adjacentList, locate the definition of Keys & Inherited Keys
                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                      call AddJoinKey(T _{[ik]},Keys _{[ik]},InheritedKeys _{[ik]},_{ik}
                                                                                                                                       Found: TRUE
                                      Found = nextKey(B+Tree(T_),Keys_)
```

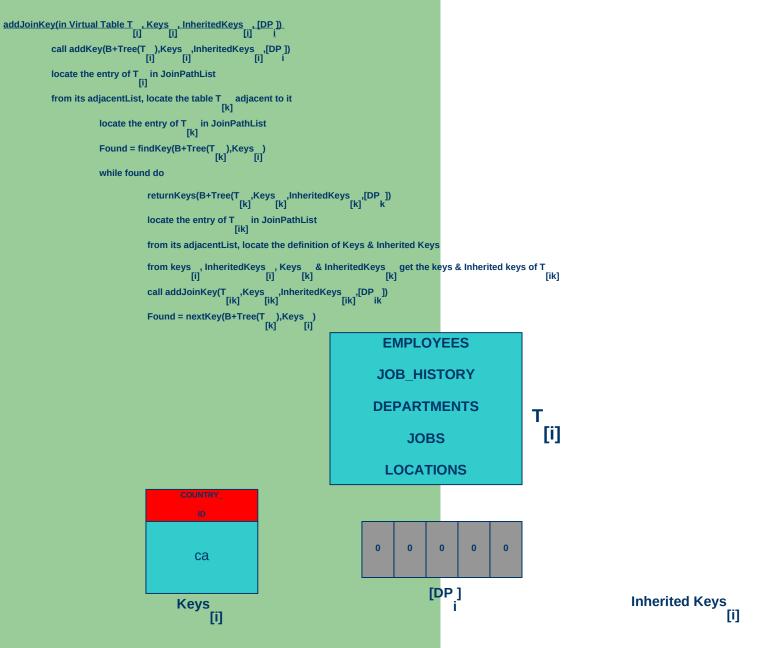


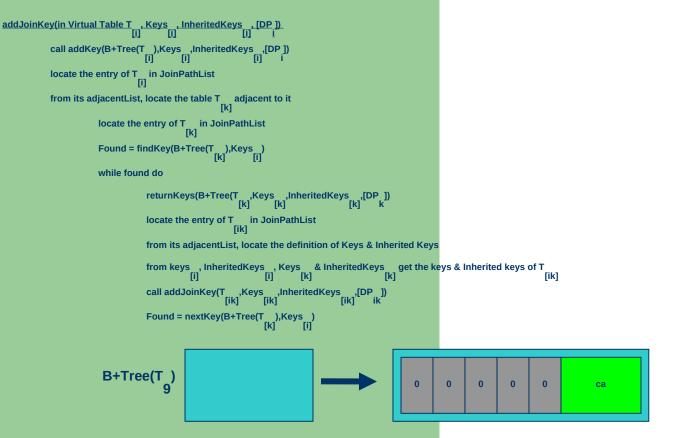


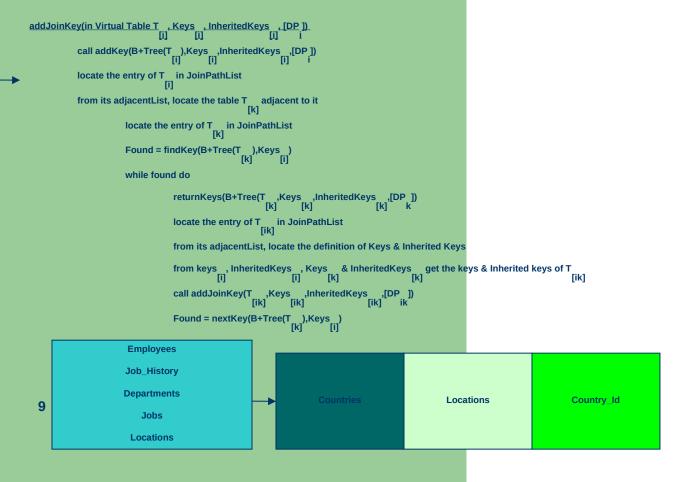


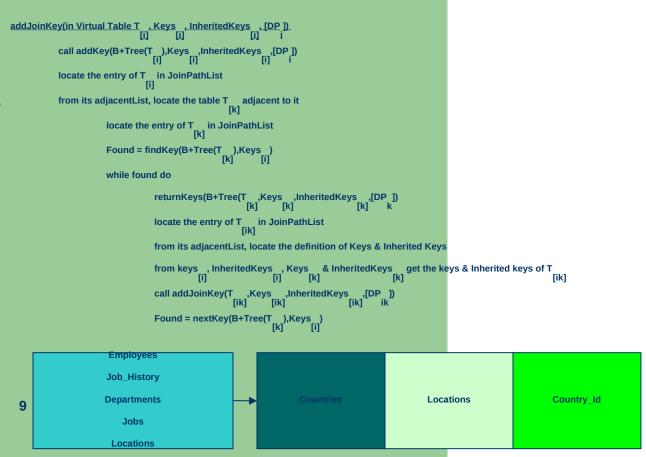




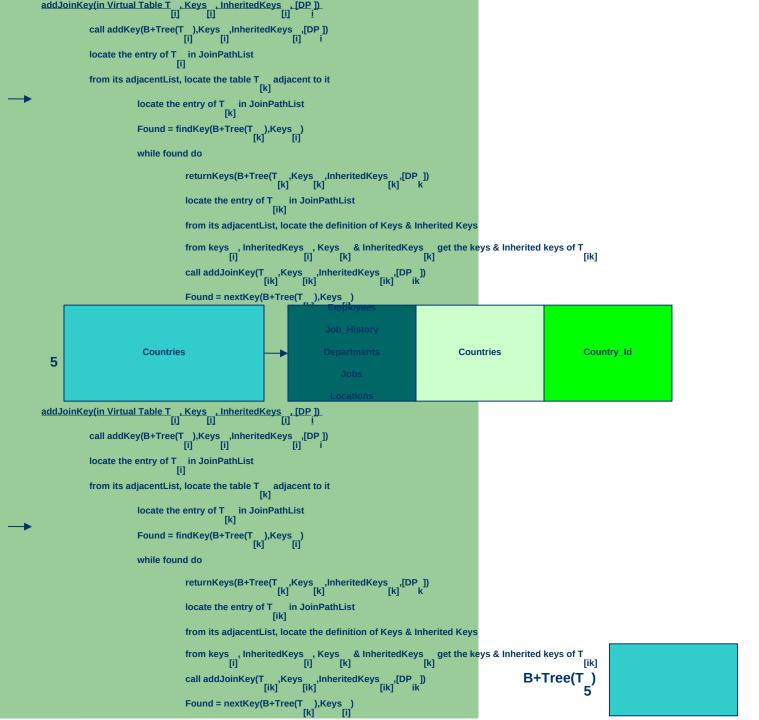








Adjacent Table



Found: FALSE

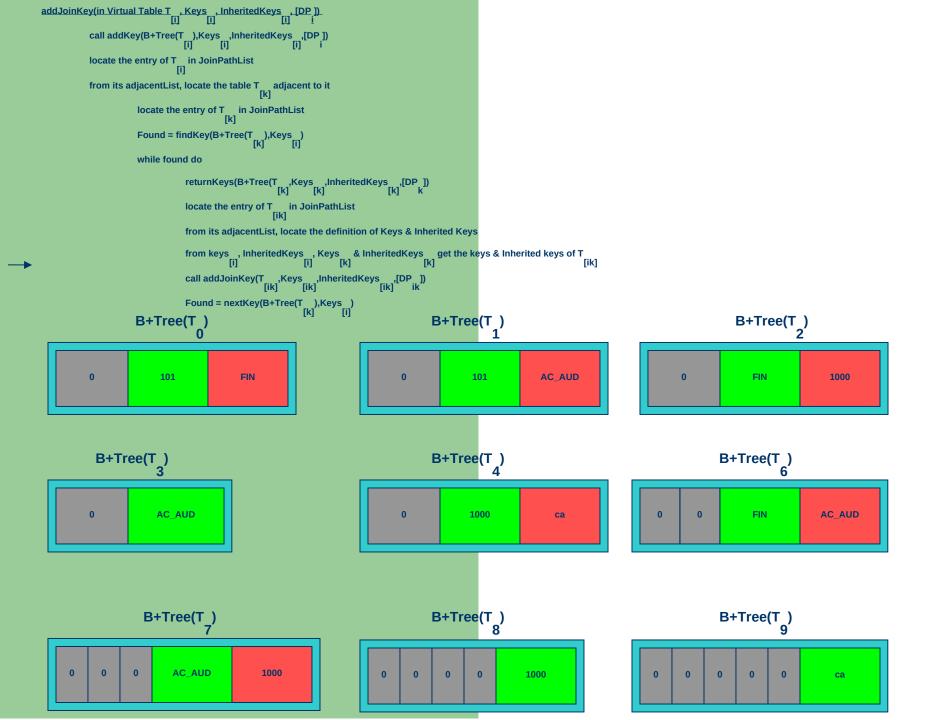
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                            locate the entry of T__ in JoinPathList
                            from its adjacentList, locate the table T \, adjacent to it \, [k] \,
                                                        \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \text{[k]} \end{array}
                                                         Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                         while found do
                                                                                      \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                      from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                      call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
[ik] [ik] [ik]
                                                                                                                                                                                                                                                Found: FALSE
                                                                                      Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \qquad \qquad [i] \qquad \qquad i 
                            locate the entry of T in JoinPathList
                            from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                         locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                        Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                      \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                      locate the entry of T in JoinPathList [ik]
                                                                                      from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                      from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                      call addJoinKey(T__,Keys_,InheritedKeys_,[DP_]) ik]
                                                                                      Found = nextKey(B+Tree(T ),Keys )
[k] [i]
```

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                            call addKey(B+Tree(T_i),Keys_,InheritedKeys_,[DP_i)
                             locate the entry of T in JoinPathList [i]
                             from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                         \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                          Found = findKey(B+Tree(T_),Keys_)
[k]
[i]
                                                          while found do
                                                                                       \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                        from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                       from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                        call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                              B+Tree(T
                                                                                                                                                                   1000
                                                                                                                                                                                                                      ca
                                                                                                                                                                                                                                                                               Found: FALSE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i]
                             call addKey(B+Tree(T ),Keys ,InheritedKeys ,I[DP ]) i
                             locate the entry of T in JoinPathList
                             from its adjacentList, locate the table T _{\mbox{\scriptsize [k]}} adjacent to it
                                                          \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                          Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                       \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                        locate the entry of T in JoinPathList [ik]
                                                                                        from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                       from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] get the keys & Inherited keys of T [k]
                                                                                        call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])
[ik] [ik] [ik]
                                                                                        Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                                                                                Found: FALSE
```

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] [i]
                             call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])  [i] \quad [i] \quad [i] \quad i 
                             locate the entry of T in JoinPathList
                             from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                                                          locate the entry of T in JoinPathList [k]
                                                          Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                        {\it returnKeys} (B+Tree (T\_,Keys\_,InheritedKeys\_,IDP\_)) \\ [k]
                                                                                        locate the entry of T _{\mbox{\scriptsize [ik]}} in JoinPathList
                                                                                        from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                        from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k]
                                                                                        call addJoinKey(T_,Keys_,InheritedKeys_,[DP_])
call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP])
                             \begin{array}{c} \text{locate the entry of T} \quad \text{in JoinPathList} \\ \text{[i]} \end{array}
                             from its adjacentList, locate the table T adjacent to it
                                                          locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                                                          Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                          while found do
                                                                                        \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                        \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                        from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                        from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                        call AddJoinKey(T ,,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                        Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                                                                                       Found: FALSE
                                                                                                                           0
                                                                                                                                                                        AC AUD
                                                                                                                                                                                                                              1000
```

```
call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ])
            locate the entry of T \quad in JoinPathList \quad [i]
            from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                        \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                        Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                         while found do
                                     \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                     from its adjacentList, locate the definition of Keys & Inherited Keys
                                     from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                     call addJoinKey(T ,Keys ,InheritedKeys ,[DP ])  [ik] \begin{tabular}{ll} [ik] & [ik] \\ \hline \end{tabular}
                                     Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
```

Found: FALSE



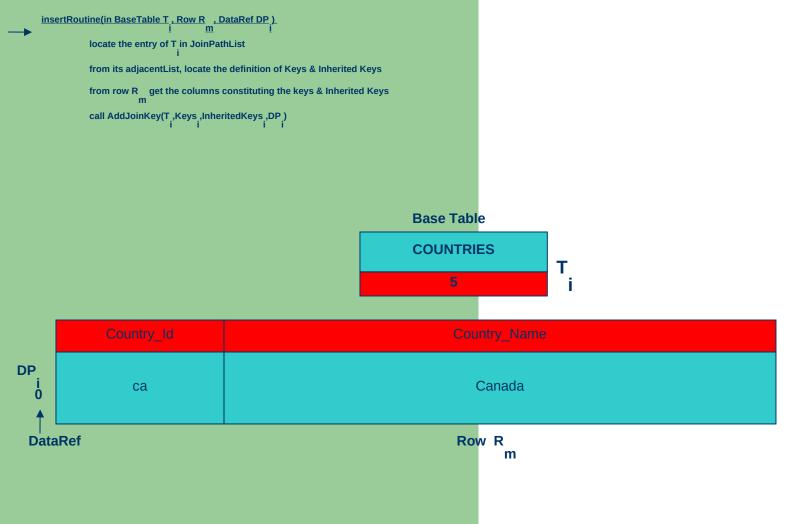
Inserting first row from table Countries

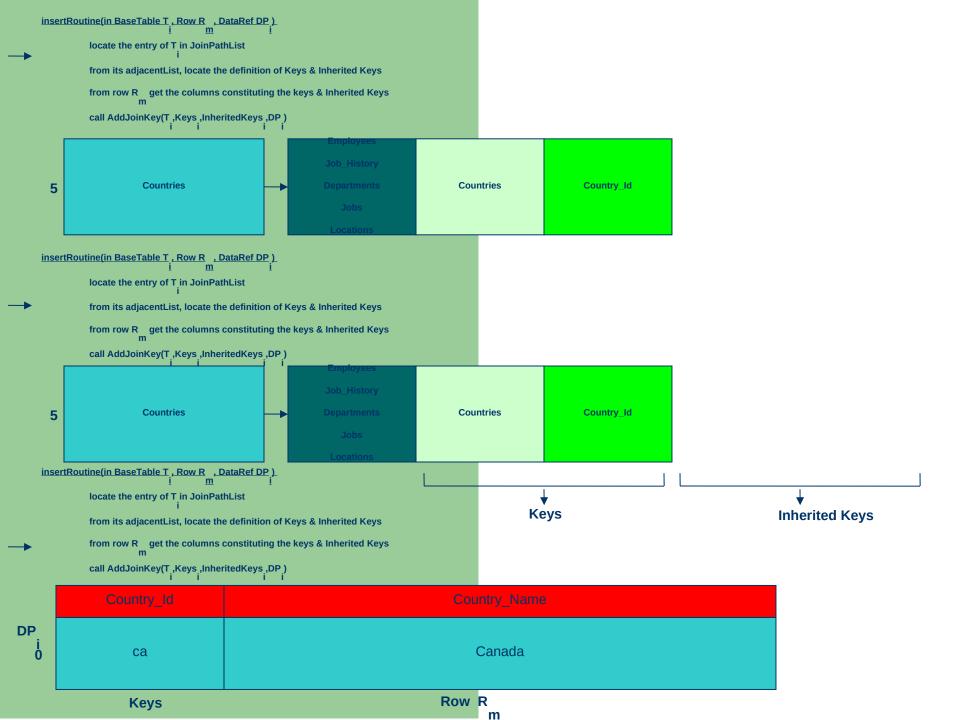
Base Table

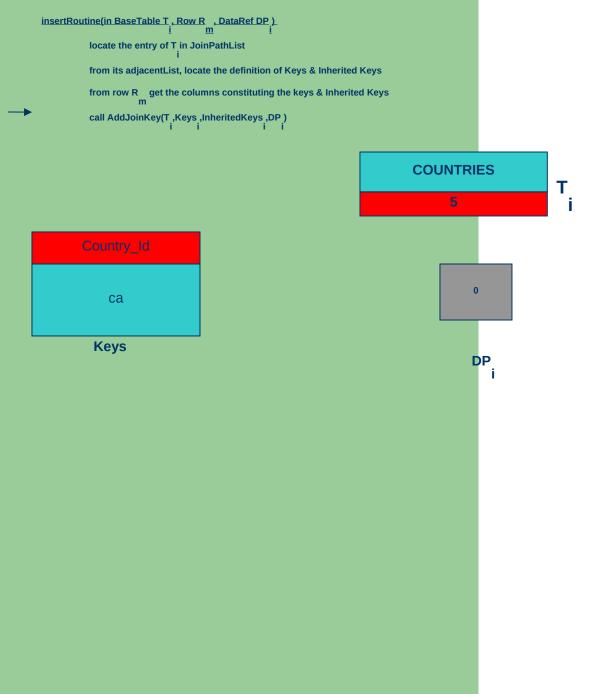
COUNTRIES

5

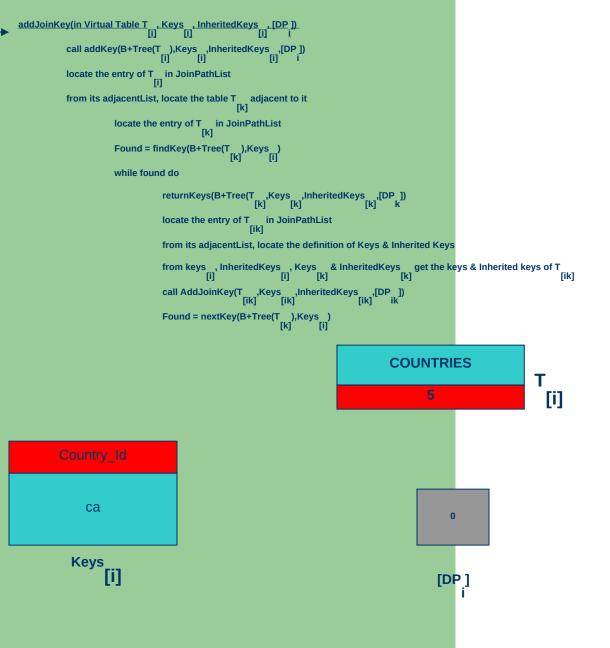
Country_ld	Country_Name
ca	Canada



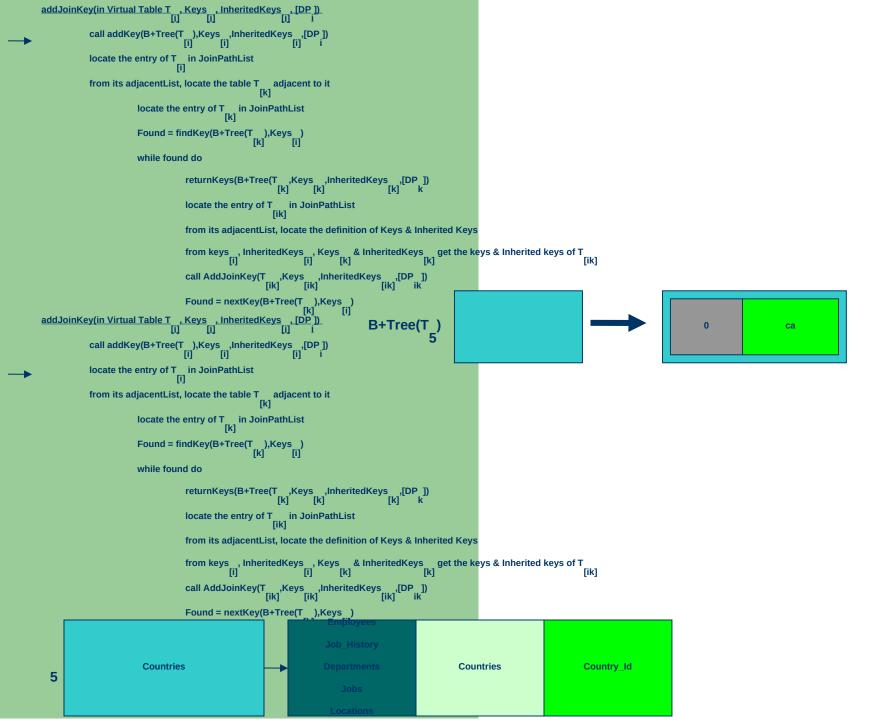


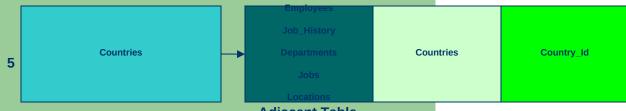


Inherited Keys



Inherited Keys [i]

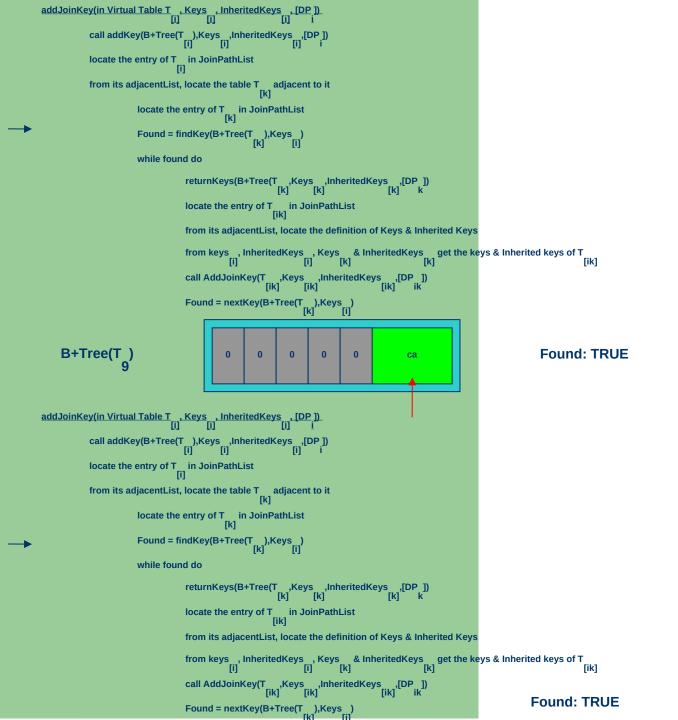


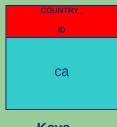


Adjacent Table

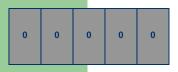
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i]
              call addKey(B+Tree(T_),Keys_,InheritedKeys_,[DP_])  [i] \quad [i] \quad [i] \quad i 
               locate the entry of T_ in JoinPathList
              from its adjacentList, locate the table T {}_{\mbox{\scriptsize [k]}} adjacent to it
                             locate the entry of T \phantom{\Big|} in JoinPathList \phantom{\Big|} [k]
                             Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                             while found do
                                             return Keys (B+Tree (T\_,Keys\_,Inherited Keys\_,IDP\_]) \\ [k] [k] [k] 
                                            \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                            from its adjacentList, locate the definition of Keys & Inherited Keys
                                            from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                            {\it call AddJoinKey(T_{[ik]}, Keys_{[ik]}, InheritedKeys_{[ik]}, [DP_{ik}])}
                                            Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                              Employees
                             Job_History
```





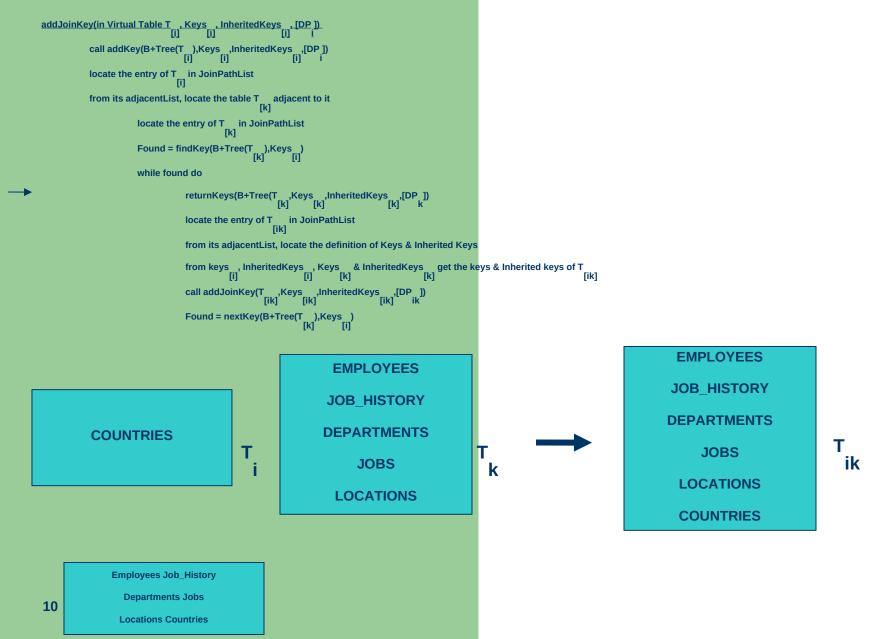


Keys [k]



[DP]

Inherited Keys



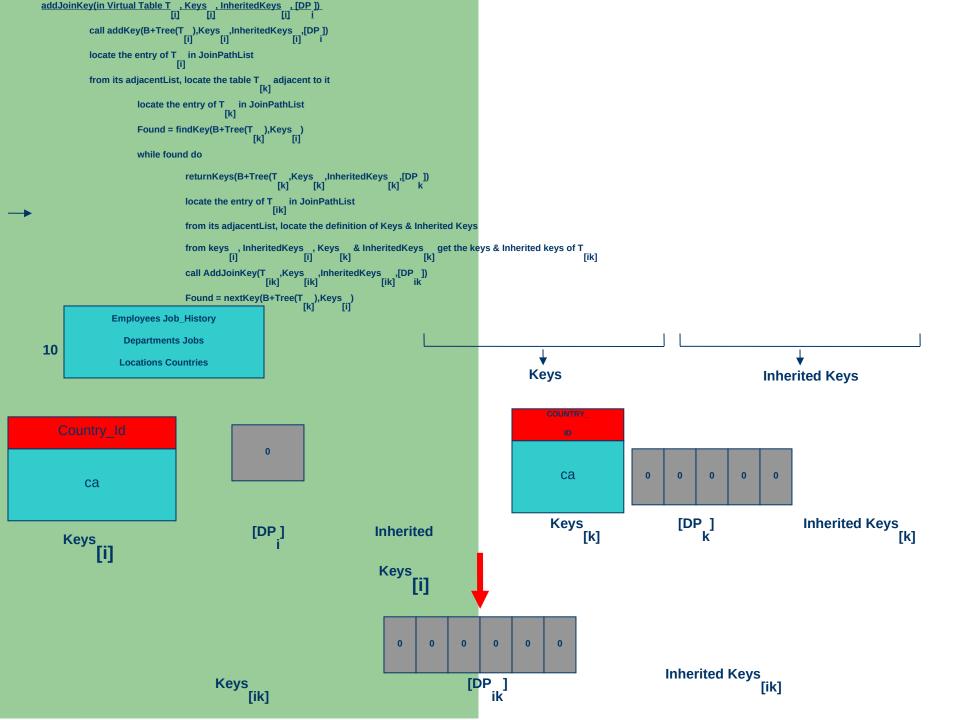
Employees Job_History

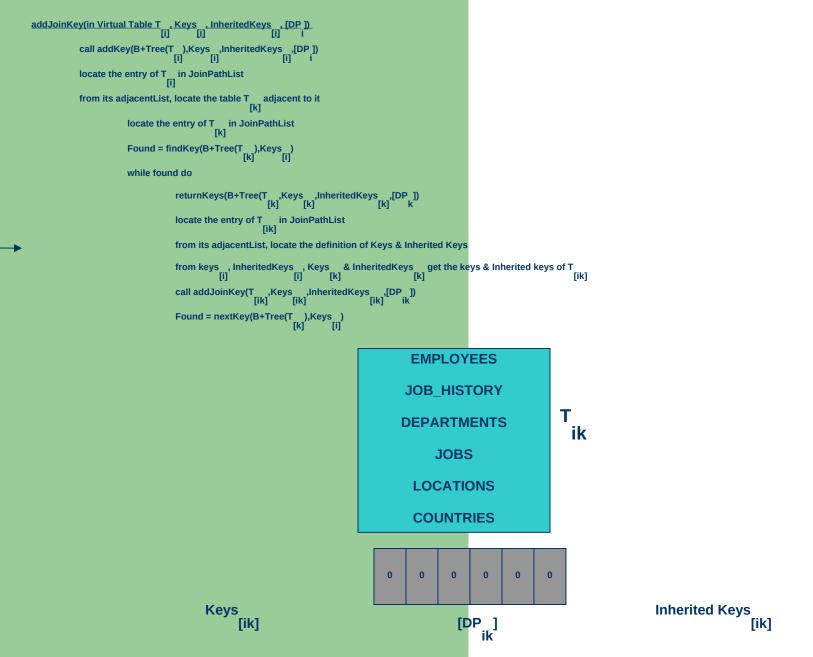
Departments Jobs

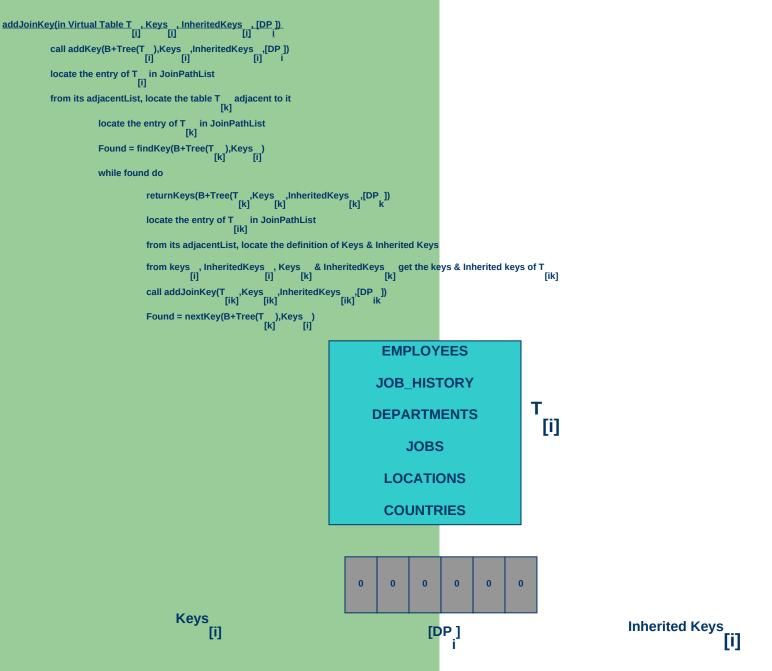
10

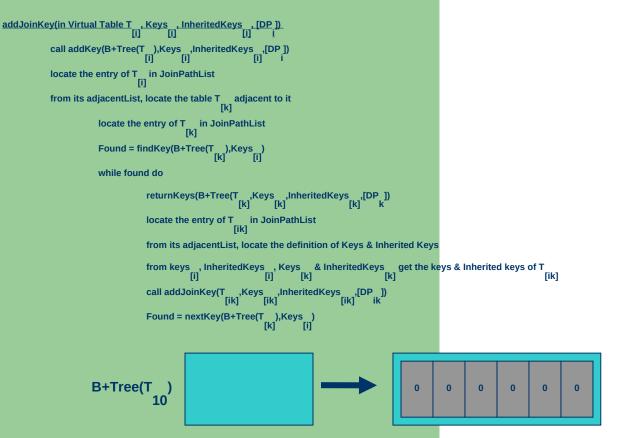
Locations Countries

↓ ↓ ↓ Keys Inherited Keys









10

Employees Job_History

Departments Jobs

Locations Countries

Employees Job_History

Departments Jobs

Locations Countries

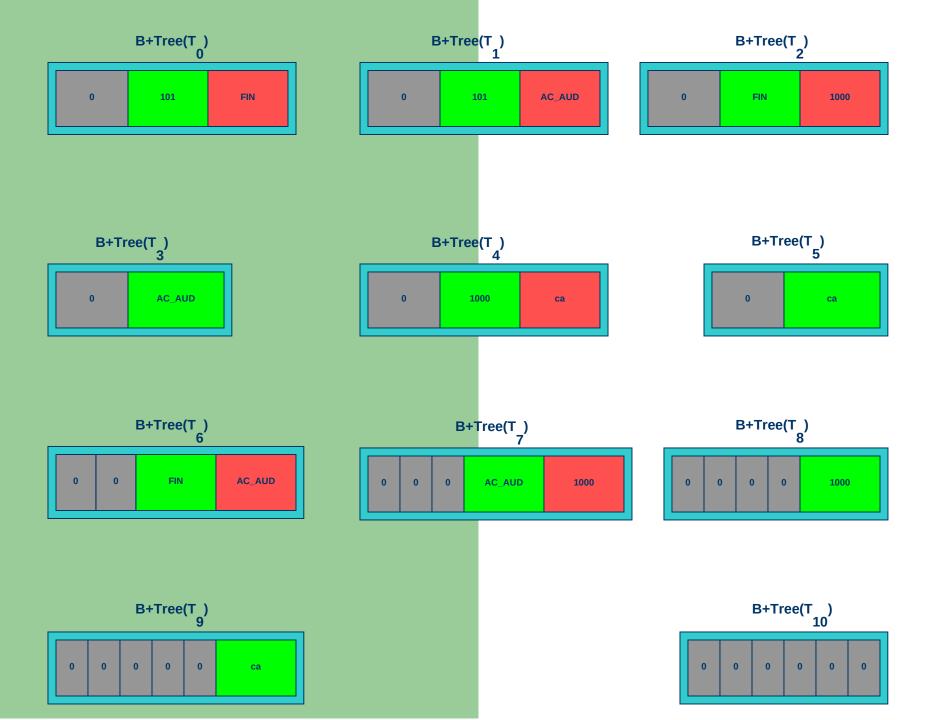
Adjacent

Table

10

```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                            locate the entry of T__ in JoinPathList
                            from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                       \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                       Found = findKey(B+Tree(T_),Keys_)
[k]
[i]
                                                       while found do
                                                                                   \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                    from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                   from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                    call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                   Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
                                                                                                                                                                                                                  Found: FALSE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]). [i] [i]
                            call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ]) [i] [i] [i] [i]
                            locate the entry of T in JoinPathList
                            from its adjacentList, locate the table T _{\mbox{\scriptsize [k]}} adjacent to it
                                                       locate the entry of T in JoinPathList
                                                       Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                       while found do
                                                                                   \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                   locate the entry of T in JoinPathList
                                                                                    from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                    from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                   call addJoinKey(T_,Keys_,InheritedKeys_,[DP_])
                                                                                                                                                                                                                    Found: FALSE
                                                                                    Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
```

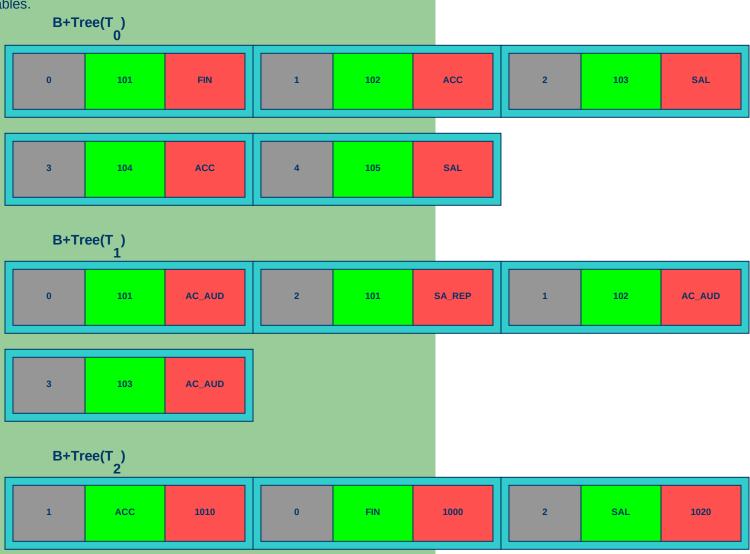
```
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]) [i] [i] i
                           locate the entry of T__ in JoinPathList
                           from its adjacentList, locate the table T \phantom{\Big|} adjacent to it \phantom{\Big|} [k]
                                                       \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [k] \end{array}
                                                       Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                       while found do
                                                                                   \begin{array}{c} \text{locate the entry of T} & \text{in JoinPathList} \\ & [ik] \end{array}
                                                                                    from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                   from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T \begin{tabular}{c|c} [i] & [k] & [k] \end{tabular}
                                                                                    call addJoinKey(T ,Keys ,InheritedKeys ,[DP ]) [ik] ik
                                                                                   Found = nextKey(B+Tree(T<sub>[k]</sub>),Keys<sub>[i]</sub>) Found: FALSE
addJoinKey(in Virtual Table T , Keys , InheritedKeys , [DP ]). [i] [i]
                           call addKey(B+Tree(T ),Keys ,InheritedKeys ,[DP ]) [i] [i] [i] [i]
                           locate the entry of T in JoinPathList
                           from its adjacentList, locate the table T _{\mbox{\scriptsize [k]}} adjacent to it
                                                       locate the entry of T \quad in JoinPathList \quad [k]
                                                       Found = findKey(B+Tree(T_),Keys_)
[k] [i]
                                                        while found do
                                                                                   \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
                                                                                   locate the entry of T in JoinPathList
                                                                                    from its adjacentList, locate the definition of Keys & Inherited Keys
                                                                                    from keys , InheritedKeys , Keys & InheritedKeys get the keys & Inherited keys of T [i] [k] [k]
                                                                                   call addJoinKey(T_,Keys_,InheritedKeys_ik,[DP_])
                                                                                                                                                                                                                      Found: FALSE
                                                                                    Found = nextKey(B+Tree(T_),Keys_)
[k] [i]
```

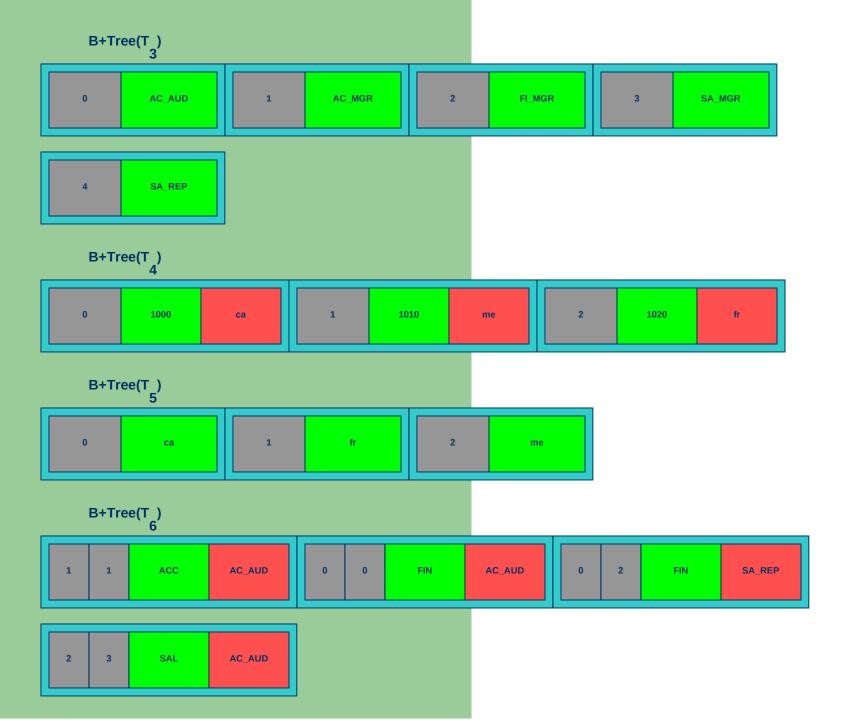


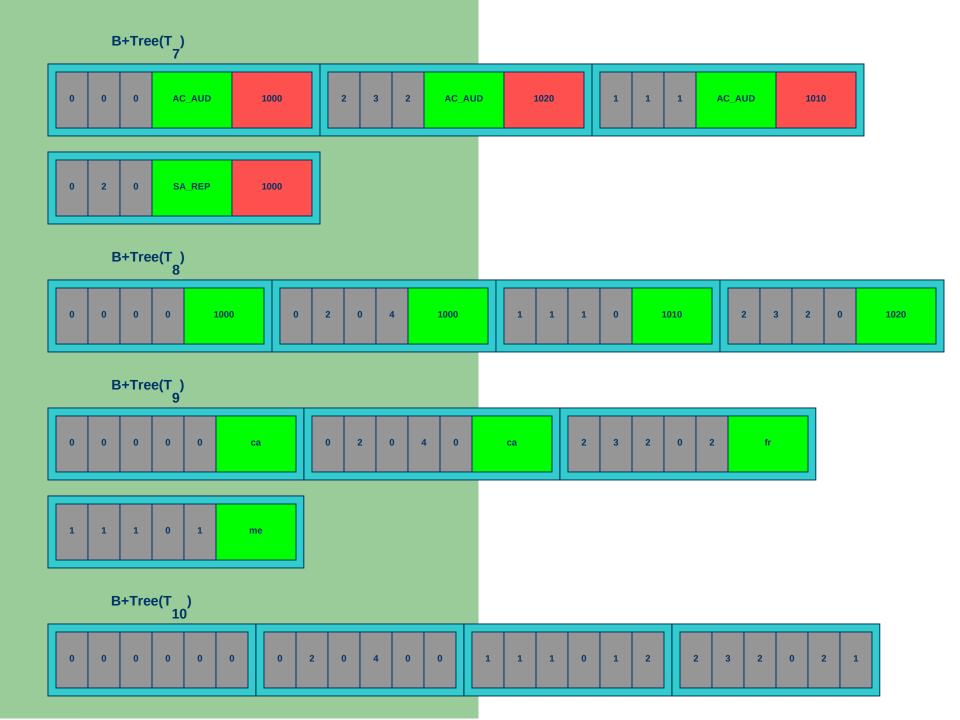
As we can notice from the last index we have an element with 6 data pointers respectively pointing to the 6 base tables forming the virtual table

T, with all values equal to the first row on each table, those rows are in join together.

Inserting all the remaining rows from the tables we obtain the following indexes where the last index shows the join between the rows from the tables.







Delete routine

When a row R_m from table T_i get deleted do the following:

- Locate the entry of T_i in the JoinPathList
- From its adjacent List, locate the definition of the keys and inherited keys
- From Row R_m get the columns constituting the keys and the inherited keys
- Call DelJoinKey (T_i, Keys_i, InheritedKeys_i, DP_i) where DP_i is the row id of row R_m
 - Notice that $Keys_i$, $InheritedKeys_i$ and DP_i are relative to the row R_m from table T_i

DelJoinKey (T_[i], Keys_[i], InheritedKeys_[i], [DP_i])

- Call delKey (B⁺Tree($T_{[i]}$), keys_[i], InheritedKeys_[i], [DP_i]) for the index of table $T_{[i]}$
- Locate the entry of T_{ii} in the JoinPathList
- From its adjacent List, locate the Table $T_{[k]}$ adjacent to it and do the following:
 - Locate the entry of $T_{[k]}$ in the JoinPathList
 - FindKey(B+Tree(T_[k]), Keys_[i])
 - While found(keys[i]) do
 - ReturnKeys(B+Tree(T_[k]), keys_[k], InheritedKeys_[k], [DP_k])
 - Locate the entry of T_{lik} in the JoinPathList
 - From its adjacent List, locate the definition of the keys and inherited keys
 - From $\text{keys}_{[i]}$, $\text{inheritedkeys}_{[i]}$, $\text{keys}_{[k]}$, $\text{inheritedkeys}_{[k]}$ get the keys and inherited keys of $\text{T}[_{ik]}$
 - DelJoinKey (T_[ik], Keys_[ik], InheritedKeys_[ik], [DP_{ik}])
 - $NextKey(B^{+}Tree(T_{[k]}), Keys_{[i]})$

B¤Tree with incremental Join

Due to the fact that join is commutative and associative and we are working on Virtual Tables and using indexes on them; it is possible instead of calculating all the join combinations to calculate incrementally the join.

This issue works just when the n tables are in direct path join between them but if they are not we are not interested.

Giving a casual order for the tables.

Beginning from Table 0, get a table T_i in direct join with it.

A Join Path List comes out with 2 entries from T_o to T_i and from T_i to T_o . The index number start always with 0.

Repeat, with T_0 or T_i and get a next table that is in direct join with T_0 or with T_i , the process continue till we scan all the tables.

This algorithm is linear, is 2*n - 1.

Complexity of the algorithm for the creation of JoinPathList.

The complexity for the creation of JoinPathList structure is: 2*n-1 where n is the number of tables in join.

Proof:

We can prove it by induction on the number of tables in join.

For m = 1:

The complexity should be 2*1-1 = 1 in fact it is the only table that get inserted in the JoinPathList.

For m = n-1:

Suppose that the number of tables in JoinPathList is 2*(n-1)-1.

For m = n:

The nth table get inserted as a Vertex in the JoinPathList at the beginning of the algorithm. The nth table get inserted in queue and path dynamic arays because the n tables are in join and at least there is one table in the (n-1) remaining table that is in join with the nth table.

So when the algorithm run at certain point should execute:

$$T_{[buf]} + = T_i$$

Insert NodesList[$T_{[buf]}$] = $T_{[buf]}$

where T_i is T_n so the number of tables in JoinPathList are: 2*(n-1)-1+1+1=2*n-1

Complexity of the algorithm for the insertion and deletion.

Delete is symmetric to insert in the algorithm in the sense where there is an insert we use a delete, so they have both the same complexity.

When inserting a new row in the database we use the B^{Join}Tree mechanism to drive us in the insert for the join.

Suppose that the order of the B⁺Trees is m and the number of elements for every B⁺Tree with i as index from the (2*n-1) B⁺Trees is p_i * l_i where in average there is l_i elements satisfying the join between every pair of tables.

In the worst case when get inserted row with the lowest order tables T_0 and T_1 in this case we call recursively the insert procedure for (2*n - 1) - (n - 1) = n times.

The complexity will be:

 $Ord(n * log_m(l_i * p_i))$

Complexity of the algorithm for the other operations.

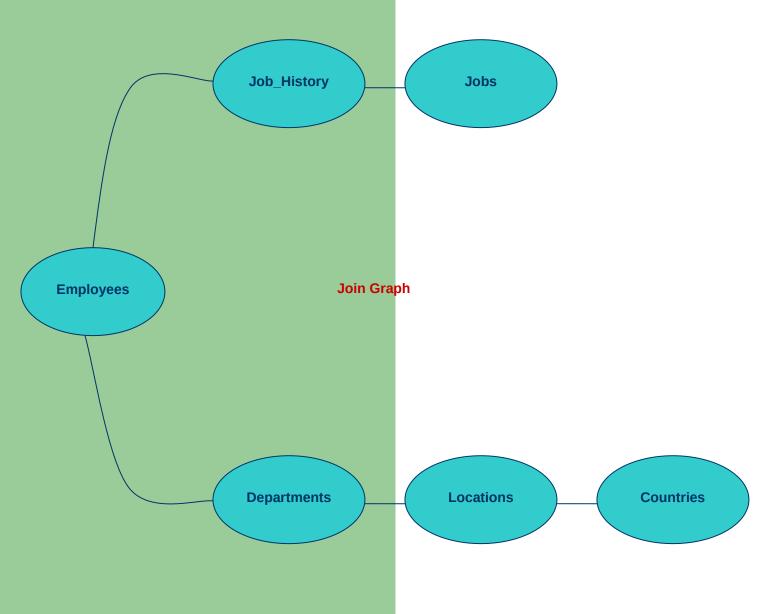
The only B⁺Tree of our interest for the scan is the one with the latest index that have the join of the tables inside it.

Suppose that the number of elements for the latest index is $p_{(2*n-1)}$ so the other operations on this B⁺Tree for find, search, prev, next,... are the same as for normal B⁺Tree.with the same number of elements.

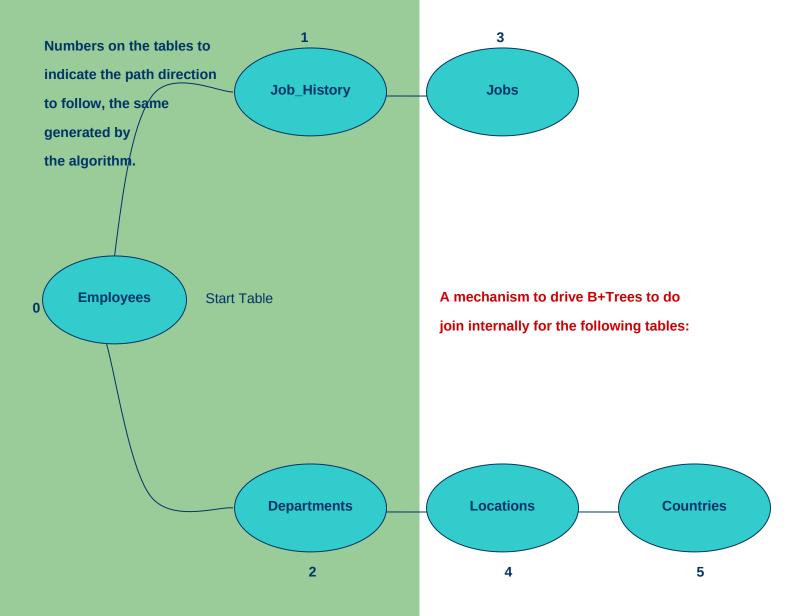
Proof of correctness.

To prove the correctness of the algorithm let see how does the algorithm work for the example above and later generalize it.

The Join Graph could be calculated easily even manually when we know which Tables are in direct join with others.



Let define a path in the Join Graph, the same path generated by the algorithm: generateJoinPathList

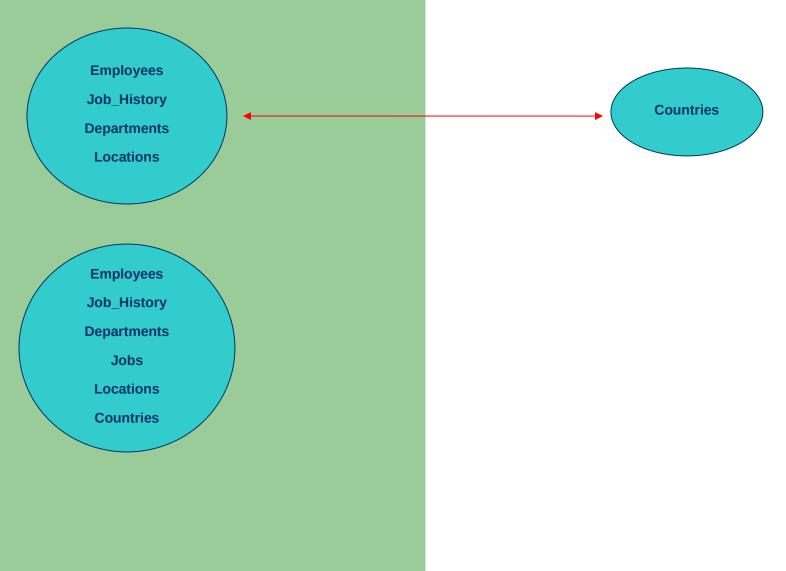


Notice that in the path if we reach one table it is not necessary to continue from it.

This is very important because this makes the tables free from any order,

independent selection of the start table.





There is no restriction on how the rows from base tables get inserted (Any order with any sequence).

As we can see for every Virtual Table there is a Base Table in which there is a direct join between them and vice versa, in fact they belongs to the same Path in the Join Graph.

The idea consists in that every Virtual Table is constituted from Base Tables that are in join together. In fact the Base Tables constituting the Virtual Table appears by adding one at time that is in direct join with the one of the previous tables.

Now the join between tables should be calculated and stored to be found. For this reason B+Tree is declared for every Virtual Table that can hold references for rows from Base Tables constituting the Virtual Table in mode that concatenating them together bring out a joined Row.

Rows are inserted into a database as one row from a base table at a time, the system look for the link table, and check the B+Tree to see if there is any row that satisfy the join with the newly inserted; if this is the case combine each row satisfying with newly inserted by their references, and insert the combined row in the virtual table that has as base tables the base tables of the 2 previously tables.

So at any time when a row get inserted, the link table may eventually have the rows that satisfy the join with it, so they are combined and the process continue to the last virtual table or if they didn't get inserted yet in the virtual table, later when they get inserted they are confronted with the one inserted yet and the process continue on the same way.

The last table will contain all base tables in join together.

Proof of correctness.

Notice that what we show before is independent from the number of tables, so that the same reasoning apply to any number of tables and the proof of correctness could be easily proved by induction.

Let prove the correctness by induction.

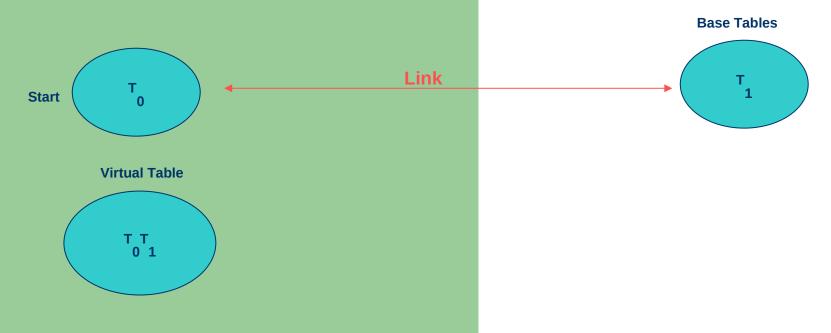
To do it, let see the correctness for 2 tables T and T in join together.

The join graph should be the following:

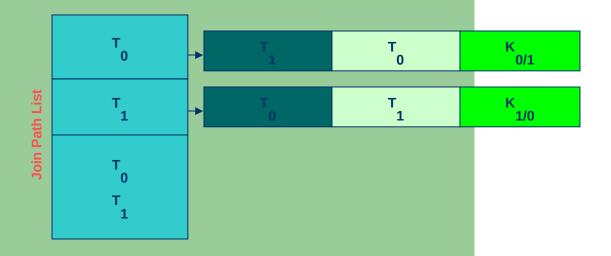


There are just 2 paths between the 2 tables: or from T going toward T or vice versa, let consider the former, the second case is symmetric and after all T and T are of arbitrarily choice.

By grouping comes out:



So, the JoinPathList should be the following:



If any key has been defined on the last virtual table and doesn't exist as a key on the base tables then should be propagated as inherited key in the appropriate base table; but for the prove of correctness in case of 2 tables, it is not important.

To prove the correctness of the algorithm, we have to prove that the last virtual table contain data references to all the rows that combined form the join between the 2 base tables and only those in other sense it is equivalent to the result of the join between the 2 tables.

Let prove that the last virtual table contain data references to all the rows that combined form the join between the 2 base tables:

Suppose by absurd that there is a row R from table T and a row R from table T that are in join together and they don't have references m/0 n/1 1 in the last virtual table.

If the 2 rows are in join together so their respective keys satisfy the join condition.

Suppose that R comes first, so key(R) is inserted in the B+Tree(T). m/0

When R get inserted later, the insert algorithm look in JoinPathList the adjacent table to T , it finds that T is such table and look in 1 - 0 = 0 B+Tree(T) all the keys that satisfy the join condition with the value of key(R). It will get key(R) because such key satisfy the join 1 - 0 = 0 condition, it will combine the data references of the 2 Rows and insert in the virtual table such couple of references.

This is in contradiction on what we assume initially.

The case that R comes first is symmetric. n/1

Let prove that the only couples of data references in the last virtual table are those that combined make the join between the 2 base tables:

Suppose by absurd that there is a couple of references DP and DP that are data pointers to rows from table T and table T respectively in the virtual table and that the combined row doesn't belong to a join between the 2 base tables.

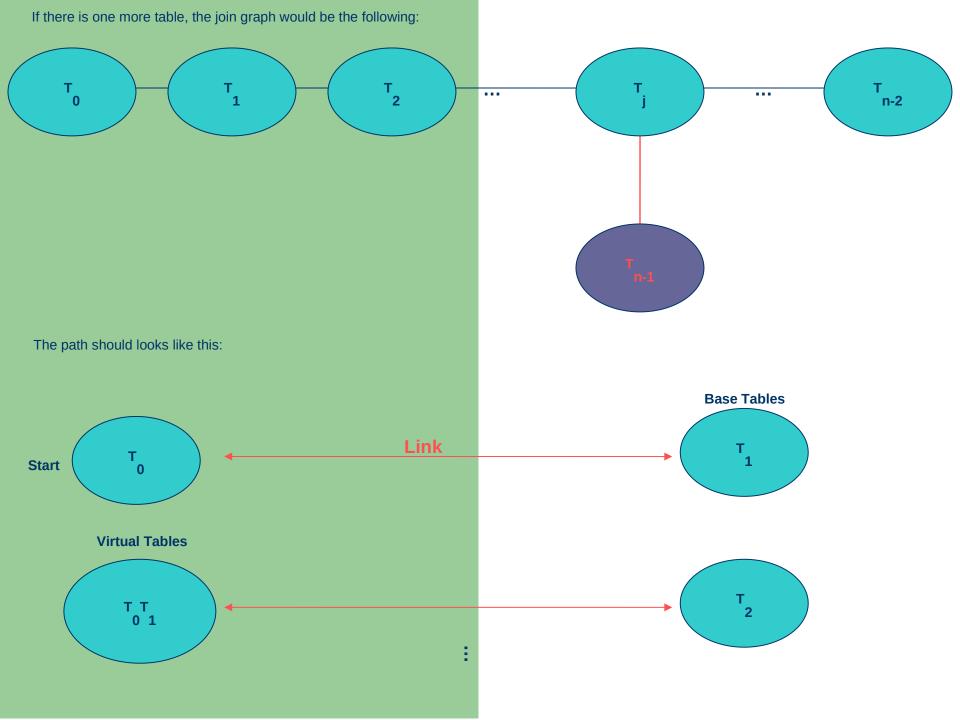
If such a couple of data pointers exist, it comes out because there is 2 keys belonging to the rows pointed by the data pointers and such keys satisfy the join condition, this is in contradiction on what we assume initially.

The initial case when there is only 2 tables in join is proved to be correct. Now let suppose that the correctness is true for n-1 tables and let prove it when the number of tables is n tables.

The easiest way to prove it for n tables is to expand the virtual table with (n-1) base tables. This virtual table has a B+Tree that is constituted from set of elements in which every element has a common key value with the nth table and (n-1) data pointers that points to the (n-1) base tables. By expanding in the sense that from every element taking the (n-1) rows from the (n-1) tables and considering them as one row in a virtual table, we can look at the virtual table as a table populated with such rows.

Let see first the Join Graph for the (n-1) tables and how they went in group and later what happens when we consider the nth table.

The join graph for the (n-1) tables should be the following: T₀ T 2 T 1 T n-2 Suppose that the choice of T ... T are in the way that the path start from T , continue by T ... T till the end to arrive at T . n-2 n-2By grouping comes out: **Base Tables** T₁ Link **Start Virtual Tables** T 2 T T 0 1 T n-2 T T ... T n-3



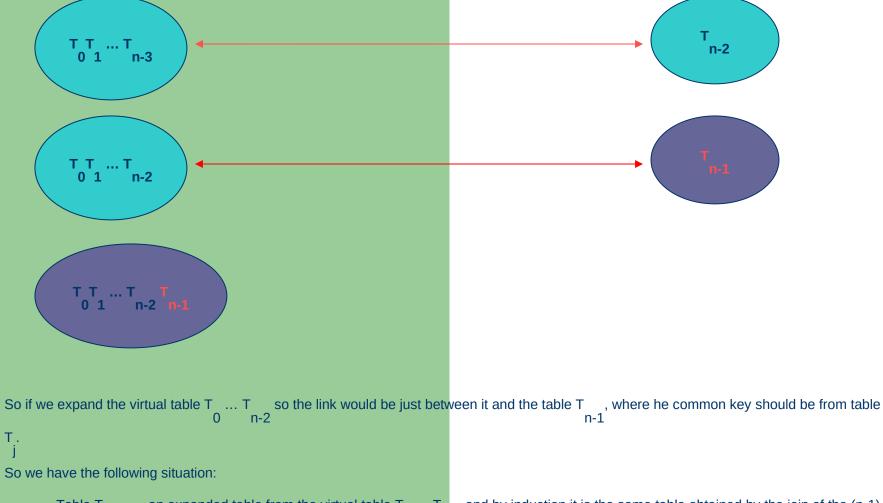


Table T ... an expanded table from the virtual table T ... T and by induction it is the same table obtained by the join of the (n-1) 0 n-2 base tables.

Table T n-1

So if we name T ... as T and T as T , we return to the case already proved of 2 tables where the common key in T ... is calculated 0 n-2 0 n-1 1

from the combined joined row in the place of the row pointed by DP.

The only thing remain to prove is the propagation of the key from T ...T to T and the eventual keys from T ...T to some base tables in n-2 j to T and the eventual keys from T ...T to some base tables in n-2 j to T and the eventual keys from T ...T to some base tables in n-2 j the base tables T ... T but this is guaranteed in the third phase of the algorithm generateJoinPathList because it goes backward and insert eventual inherited keys.

Self Join

If the table is in join with itself, consider the table twice, every one with the necessary index.

Let see an example of self join.

Suppose that we add a column named SUPERVISOR_ID in the table EMPLOYEES, it has the id of the supervisor for a given employee.

Suppose that we have the following query:

SELECT A.EMPLOYEE_NAME, B.EMPLOYEE_NAME

FROM EMPLOYEES AS A, EMPLOYEES AS B

WHERE A.EMPLOYEE_ID = B.SUPERVISOR_ID

The table EMPLOYEES with the new column SUPERVISOR_ID is shown in slide 575.

generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

for every direct join between 2 tables of the form T and T where T is the table of order i and T is the table of order k as defined by the DBA do i

 $\begin{array}{c} AdjacentList[T] \ += \ T \\ i & k \end{array}$ follow by the common key

 $\begin{array}{lll} & \text{AdjacentList[T]} & \text{+= T} & \text{follow by the common key} \\ & \text{i} & \\ \end{array}$

Base Tables

Employees/Employee_Id	Employees/Supervisor_Id		
0	1		

```
generateJoinGraph (in BaseTables; out JoinGraph)
insert the base tables as vertexes of the graph
for every direct join between 2 tables of the form T and T where T is the table of order i and T is the table of order k as defined by the DBA do
```

$$\begin{array}{c} \text{AdjacentList[T]} \text{ $+$=$ T$} \text{ follow by the common key} \\ i \\ k \end{array}$$

AdjacentList[T]
$$+=$$
 T follow by the common key

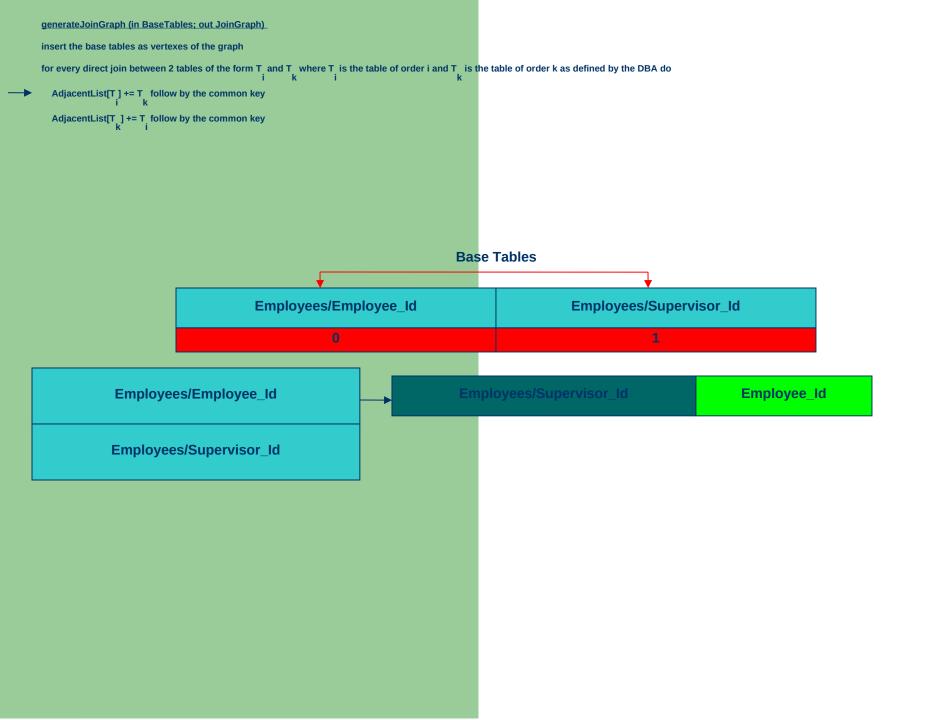
Base Tables

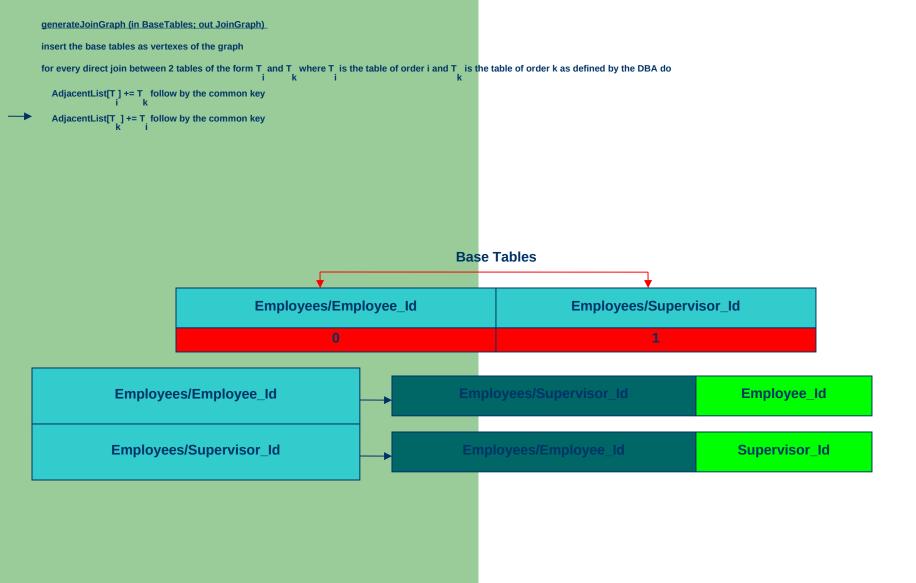
Employees/Employee_Id Employees/Supervisor_Id

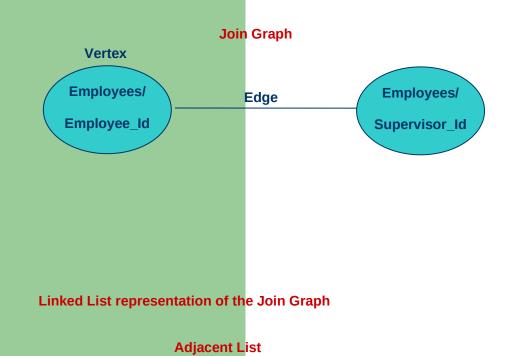
0 1

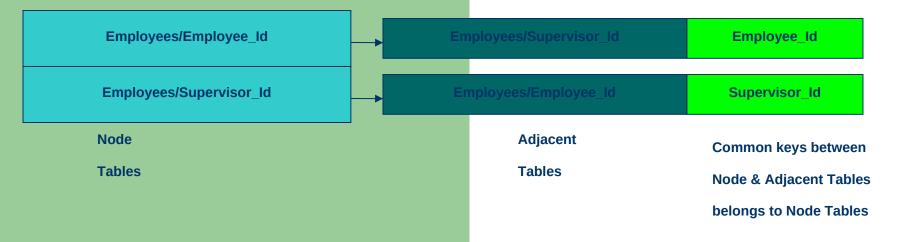
Employees/Employee_Id

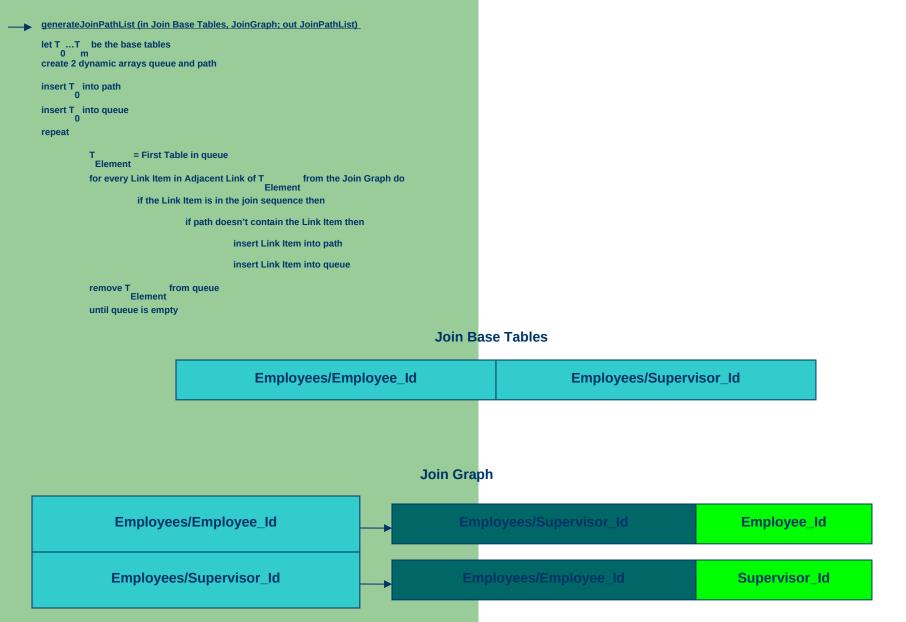
generateJoinGraph (in BaseTables; out JoinGraph) insert the base tables as vertexes of the graph for every direct join between 2 tables of the form T and T where T is the table of order i and T is the table of order k as defined by the DBA do AdjacentList[T] $\stackrel{}{\underset{i}{=}} T$ follow by the common key AdjacentList[T] += T follow by the common key **Base Tables** Employees/Employee_Id Employees/Supervisor_Id Employees/Employee_Id Employees/Supervisor_Id











generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let T ...T be the base tables
0 m
create 2 dynamic arrays queue and path

insert T into path
insert T into queue
repeat

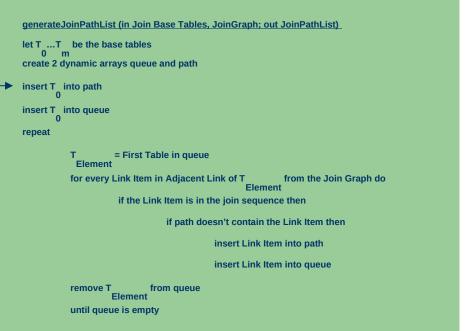
T = First Table in queue
Element
for every Link Item in Adjacent Link of T from the Join Graph do
Element
if the Link Item is in the join sequence then
if path doesn't contain the Link Item then
insert Link Item into queue
remove T from queue
Element
until queue is empty

Join Base Tables

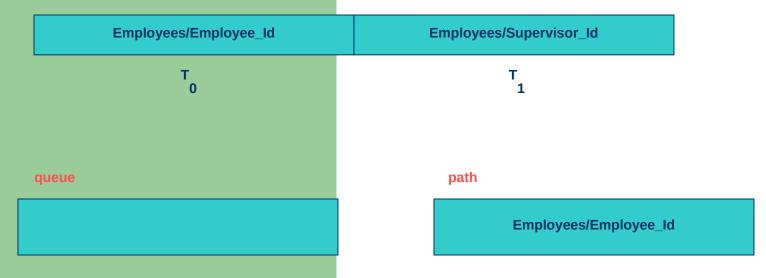
Join Base Tables					
Employees/Employee_Id	Employees/Supervisor_Id				
T 0	T 1				

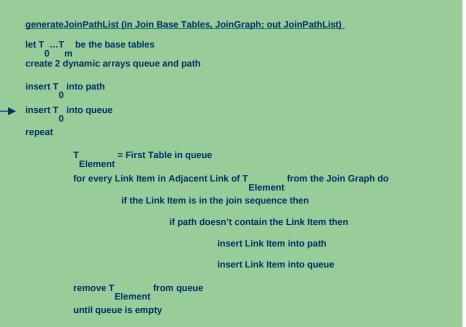
```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
       let T ...T be the base tables 0 m
---- create 2 dynamic arrays queue and path
       insert T into path
       insert T into queue
       repeat
                 T = First Table in queue Element
                 for every Link Item in Adjacent Link of T
                                                                from the Join Graph do
                            if the Link Item is in the join sequence then
                                      if path doesn't contain the Link Item then
                                                 insert Link Item into path
                                                 insert Link Item into queue
                 remove T Element
                                  from queue
                  until queue is empty
                                    queue
```

path			

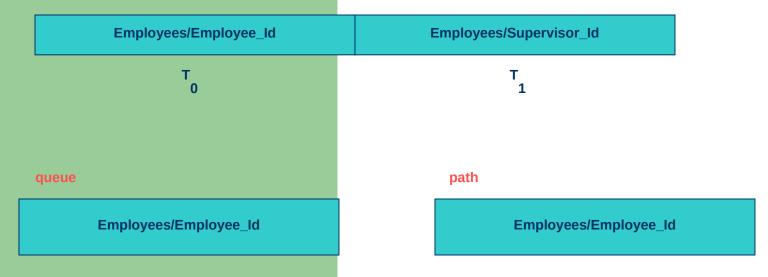


Join Base Tables





Join Base Tables



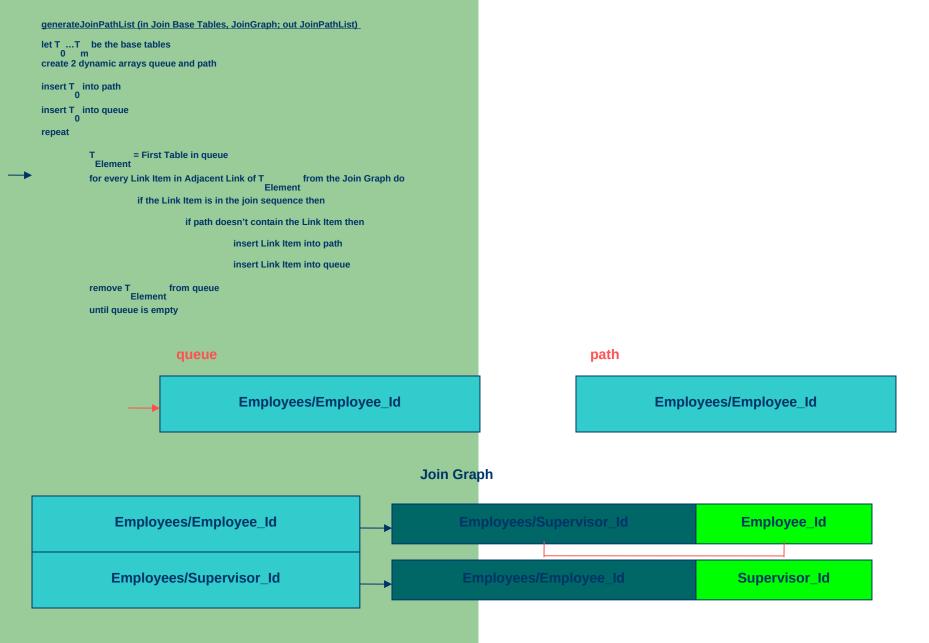
```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
create 2 dynamic arrays queue and path
insert T into path
insert T into queue
repeat
          T = First Table in queue Element
          for every Link Item in Adjacent Link of T

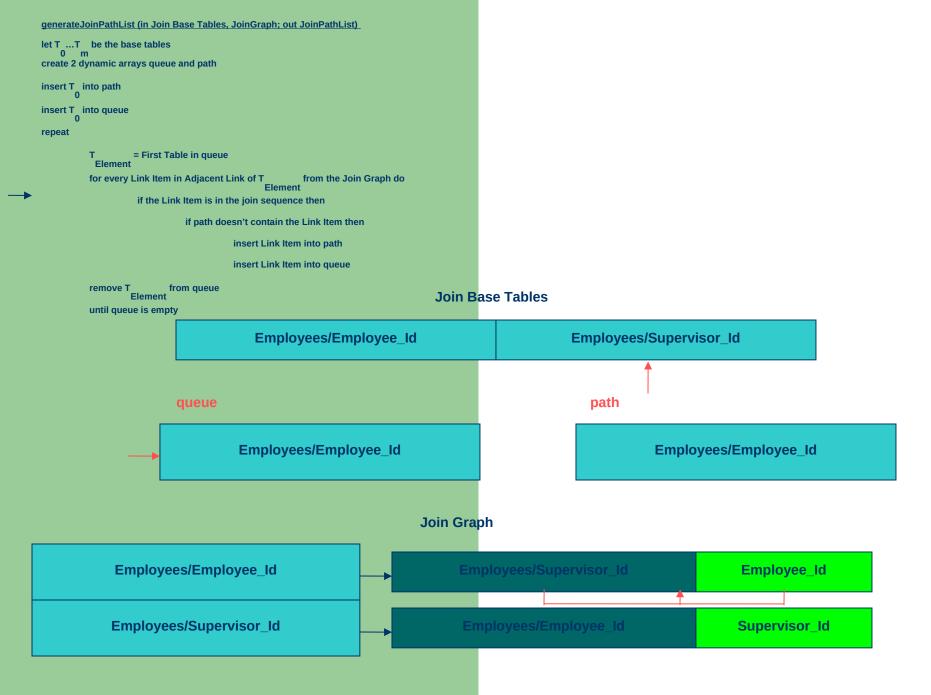
Element
                                                 from the Join Graph do
                   if the Link Item is in the join sequence then
                             if path doesn't contain the Link Item then
                                       insert Link Item into path
                                       insert Link Item into queue
          remove T
                         from queue
                  Element
          until queue is empty
                           queue
                                        Employees/Employee_Id
```

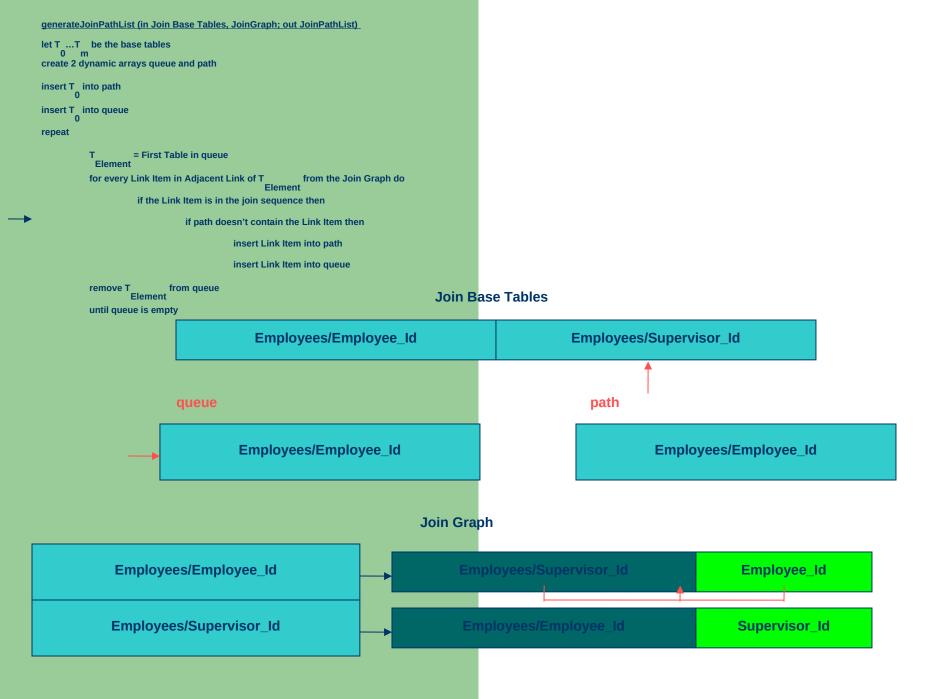
Employees/Employee_Id

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
create 2 dynamic arrays queue and path
insert T into path
insert T into queue
repeat
         T = First Table in queue Element
         for every Link Item in Adjacent Link of T_
                                                    from the Join Graph do
                   if the Link Item is in the join sequence then
                             if path doesn't contain the Link Item then
                                      insert Link Item into path
                                      insert Link Item into queue
         remove T
                         from queue
                  Element
         until queue is empty
                           queue
                                       Employees/Employee_Id
```

Employees/Employee_Id







```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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         T = First Table in queue Element
         for every Link Item in Adjacent Link of T

Element
                                                    from the Join Graph do
                   if the Link Item is in the join sequence then
                             if path doesn't contain the Link Item then
                                       insert Link Item into path
                                      insert Link Item into queue
          remove T
                         from queue
                  Element
         until queue is empty
                           queue
                                       Employees/Employee_Id
```

Employees/Employee_Id

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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insert T into path
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repeat
         T = First Table in queue Element
         for every Link Item in Adjacent Link of T

Element
                                                   from the Join Graph do
                   if the Link Item is in the join sequence then
                            if path doesn't contain the Link Item then
                                      insert Link Item into path
                                      insert Link Item into queue
         remove T
                         from queue
                 Element
         until queue is empty
                          queue
                                       Employees/Employee_Id
                                      Employees/Supervisor_Id
```

Employees/Employee_Id

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
create 2 dynamic arrays queue and path
insert T into path
insert T into queue
repeat
          T = First Table in queue Element
          for every Link Item in Adjacent Link of T

Element
                                                      from the Join Graph do
                    if the Link Item is in the join sequence then
                              if path doesn't contain the Link Item then
                                        insert Link Item into path
                                        insert Link Item into queue
                          from queue
                  Element
          until queue is empty
```

queue

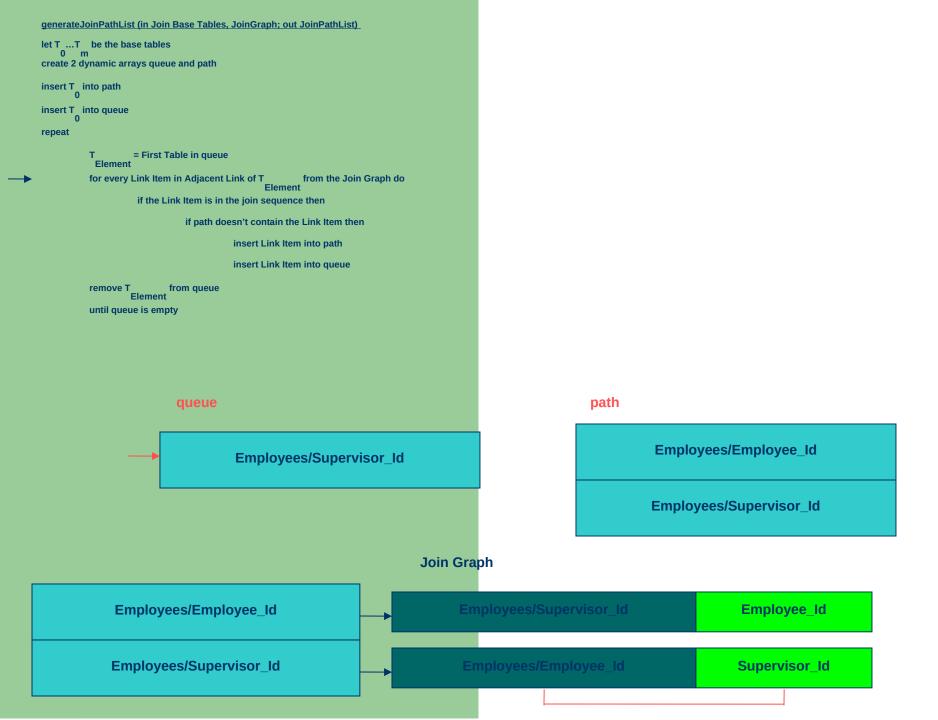
Employees/Supervisor_Id

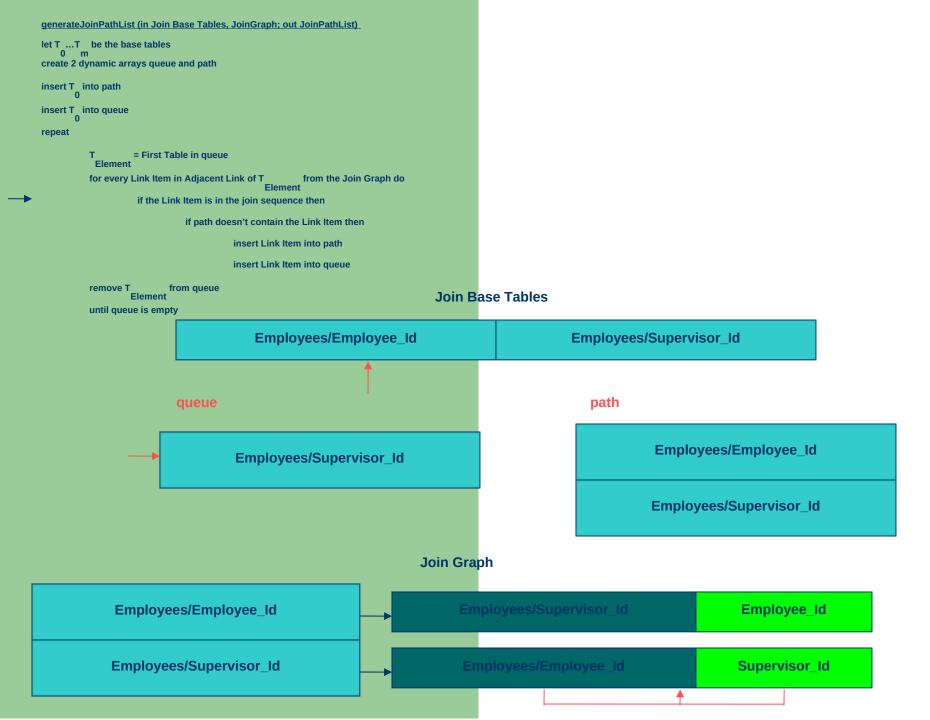
path

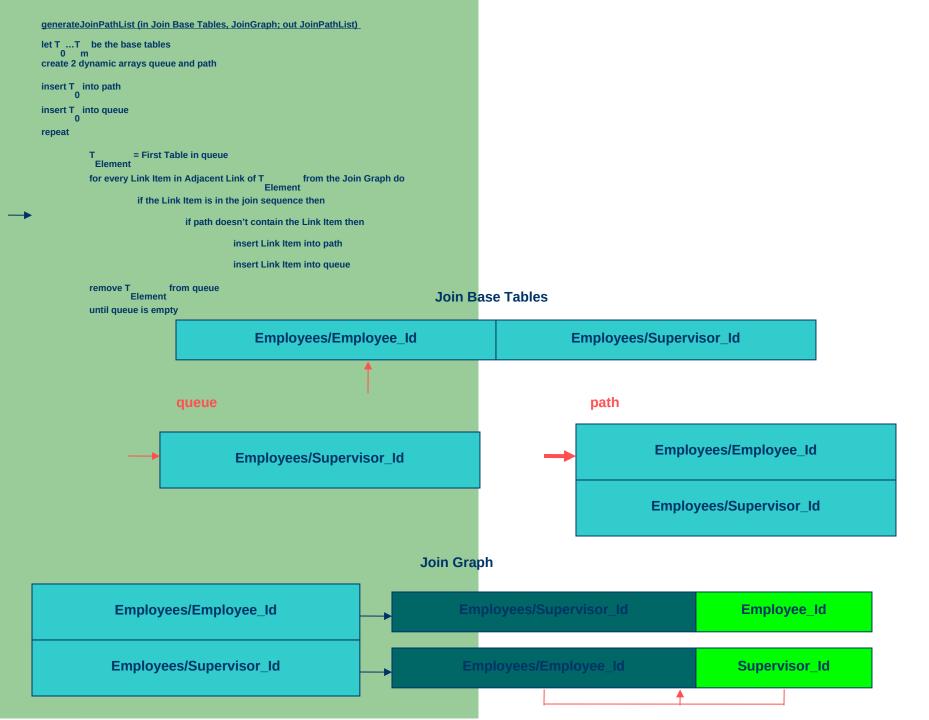
Employees/Employee_Id

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
create 2 dynamic arrays queue and path
insert T into path
insert T into queue
repeat
         T = First Table in queue Element
         for every Link Item in Adjacent Link of T_
                                                    from the Join Graph do
                   if the Link Item is in the join sequence then
                             if path doesn't contain the Link Item then
                                       insert Link Item into path
                                      insert Link Item into queue
          remove T
                         from queue
                  Element
          until queue is empty
                           queue
                                       Employees/Supervisor_Id
```

Employees/Employee_Id







```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
let T ...T be the base tables 0 m
create 2 dynamic arrays queue and path
insert T into path
insert T into queue
repeat
          T = First Table in queue Element
          for every Link Item in Adjacent Link of T

Element
                                                      from the Join Graph do
                     if the Link Item is in the join sequence then
                                if path doesn't contain the Link Item then
                                          insert Link Item into path
                                          insert Link Item into queue
           remove T
                            from queue
                    Element
           until queue is empty
                              queue
```

Employees/Employee_Id

```
generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
create 2 dynamic arrays queue and path
insert T into path
insert T into queue
repeat
          T = First Table in queue Element
          for every Link Item in Adjacent Link of T

Element
                                                  from the Join Graph do
                   if the Link Item is in the join sequence then
                              if path doesn't contain the Link Item then
                                       insert Link Item into path
                                       insert Link Item into queue
          remove T
                          from queue
                  Element
          until queue is empty
                            queue
```

Employees/Employee_Id

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

$$\label{eq:continuous} \begin{split} \mbox{JoinPathAdjacentList(T)} = \mbox{T} \\ \mbox{[buf]} & \mbox{i} \end{split}$$

Nodes

Employees/Employee_Id

Employees/Supervisor_Id

Employees/Employee_Id

path

Nodes

insert all the names of base tables from path as vertexes in JoinPathList create a local buffer buf insert into buf the first entry from path for all the remainder entries in path do take one T at a time $\label{eq:continuous} \textbf{JoinPathAdjacentList}(\textbf{T}) = \textbf{T} \\ \textbf{i} \quad [\textbf{buf}]$
$$\label{eq:continuous} \begin{split} \mbox{JoinPathAdjacentList(T)} = \mbox{T} \\ \mbox{[buf]} & \mbox{i} \end{split}$$
+ = T [buf] Insert NodesList[T] = T [buf] Employees/Employee_Id path Employees/Supervisor_Id Employees/Employee_Id buf

Nodes

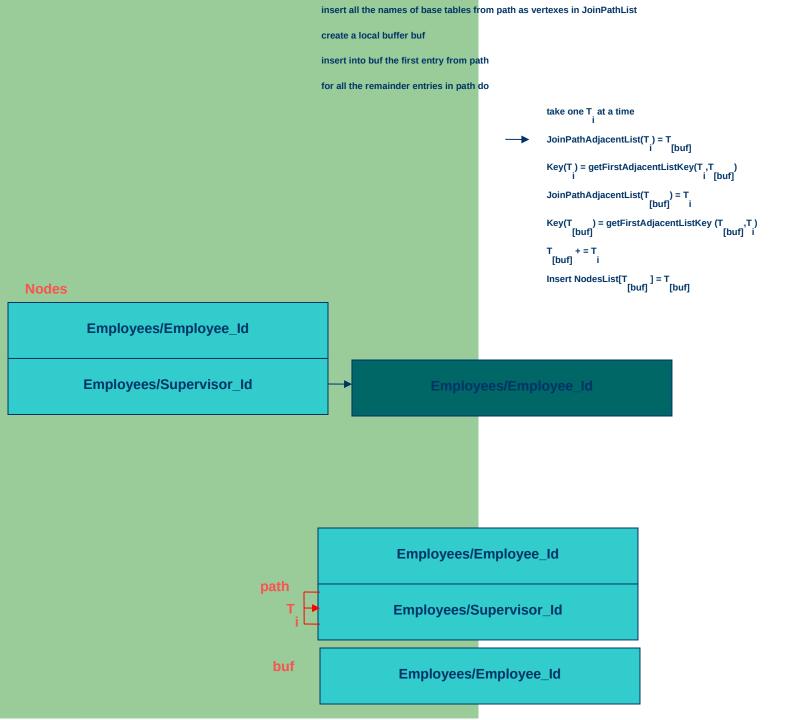
Employees/Employee_Id

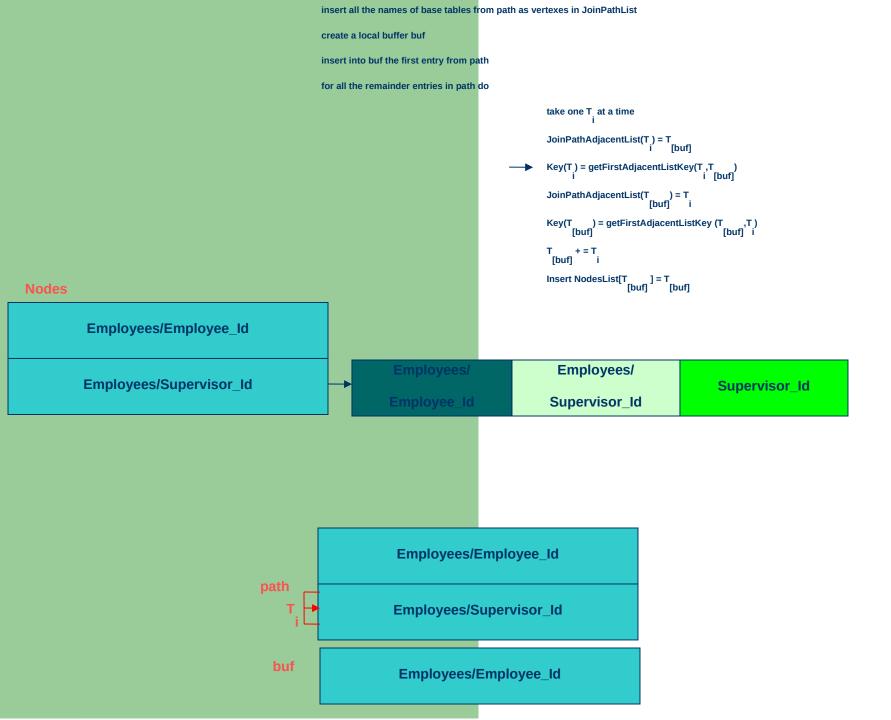
insert all the names of base tables from path as vertexes in JoinPathList create a local buffer buf insert into buf the first entry from path for all the remainder entries in path do take one T at a time JoinPathAdjacentList(T) = T
i [buf]
$$\label{eq:continuous} \begin{split} \mbox{JoinPathAdjacentList(T)} &= \mbox{T} \\ \mbox{[buf]} & \mbox{i} \end{split}$$
 $(T_{[buf]}) = getFirstAdjacentListKey (T_{[buf]},T_{i})$ + = T [buf] Insert NodesList[T] = T [buf] **Nodes** Employees/Employee_Id Employees/Supervisor_Id Employees/Employee_Id path Employees/Supervisor_Id Employees/Employee_Id buf

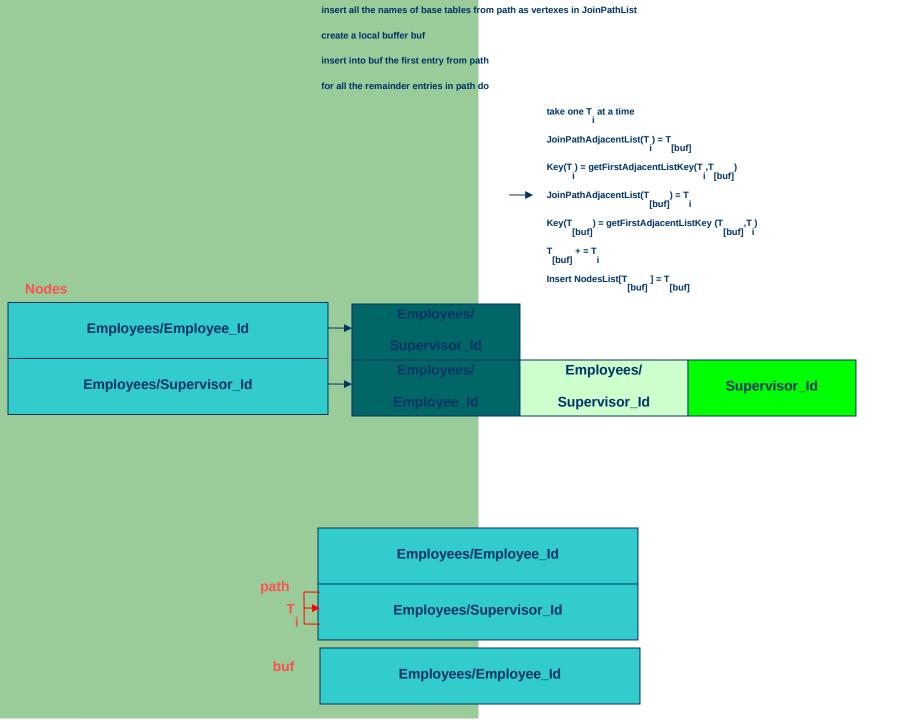
insert all the names of base tables from path as vertexes in JoinPathList create a local buffer buf insert into buf the first entry from path for all the remainder entries in path do take one T at a time JoinPathAdjacentList(T) = T
i [buf]
$$\label{eq:continuous} \begin{split} \mbox{JoinPathAdjacentList(T)} &= \mbox{T} \\ \mbox{[buf]} & \mbox{i} \end{split}$$
 $(T_{[buf]}) = getFirstAdjacentListKey (T_{[buf]},T_{i})$ + = T [buf] Insert NodesList[T] = T [buf] Employees/Employee_Id path Employees/Supervisor_Id buf Employees/Employee_Id

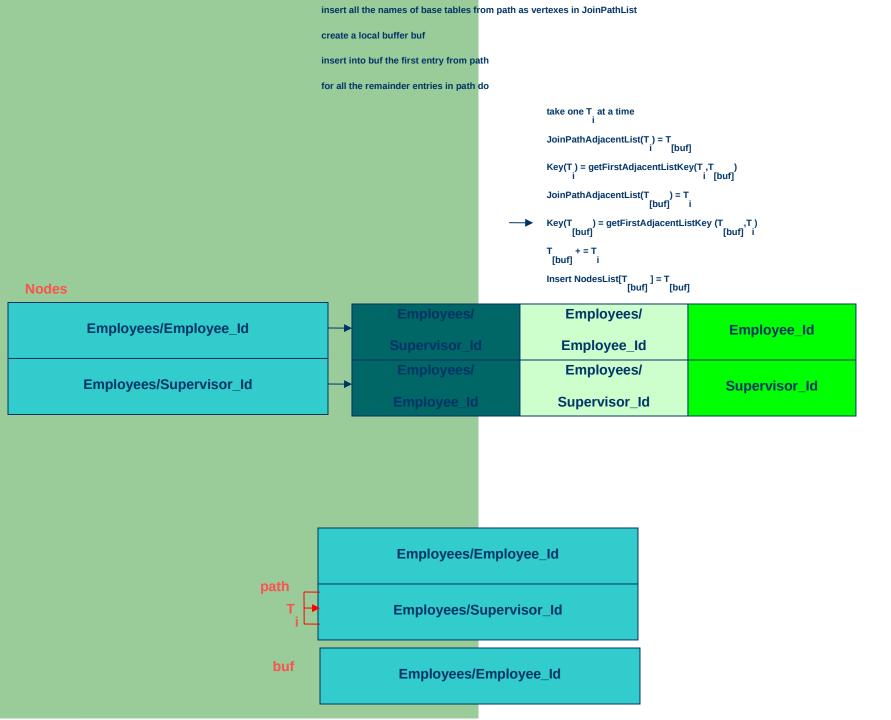
Nodes

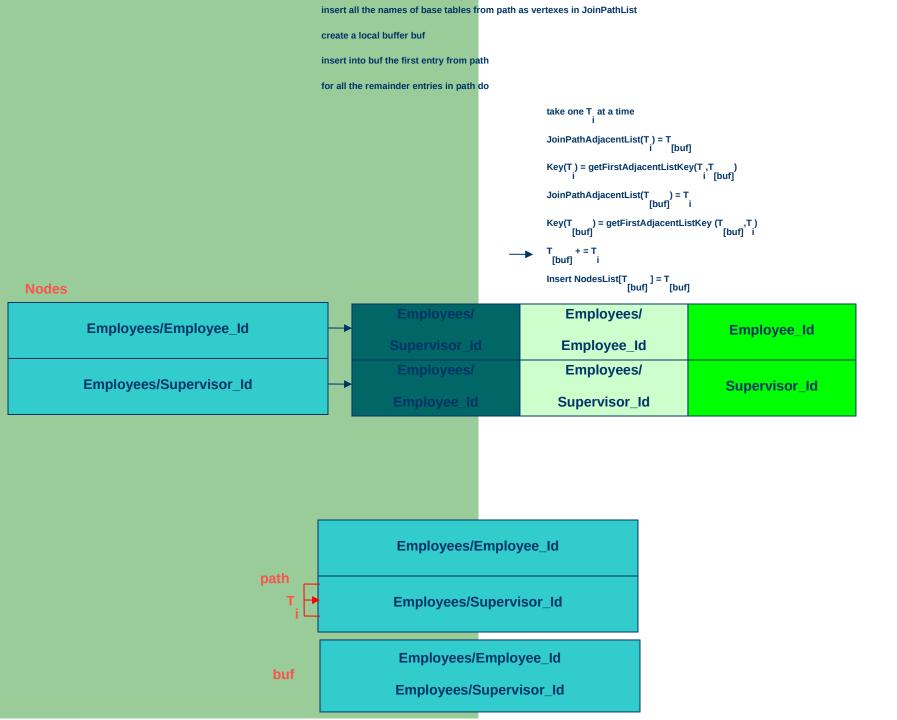
Employees/Employee_Id

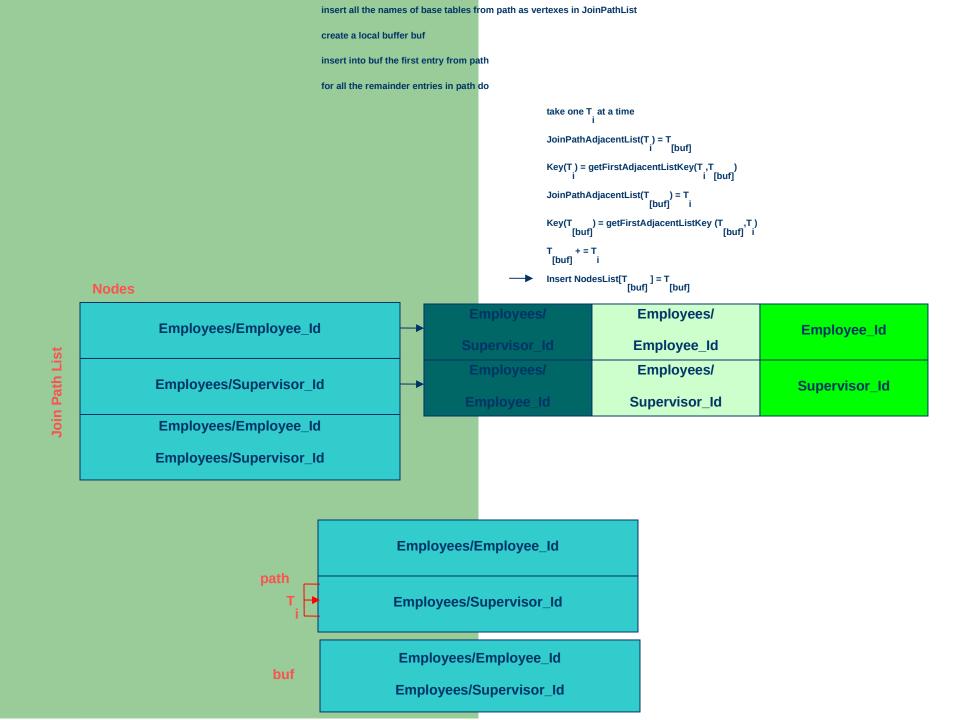




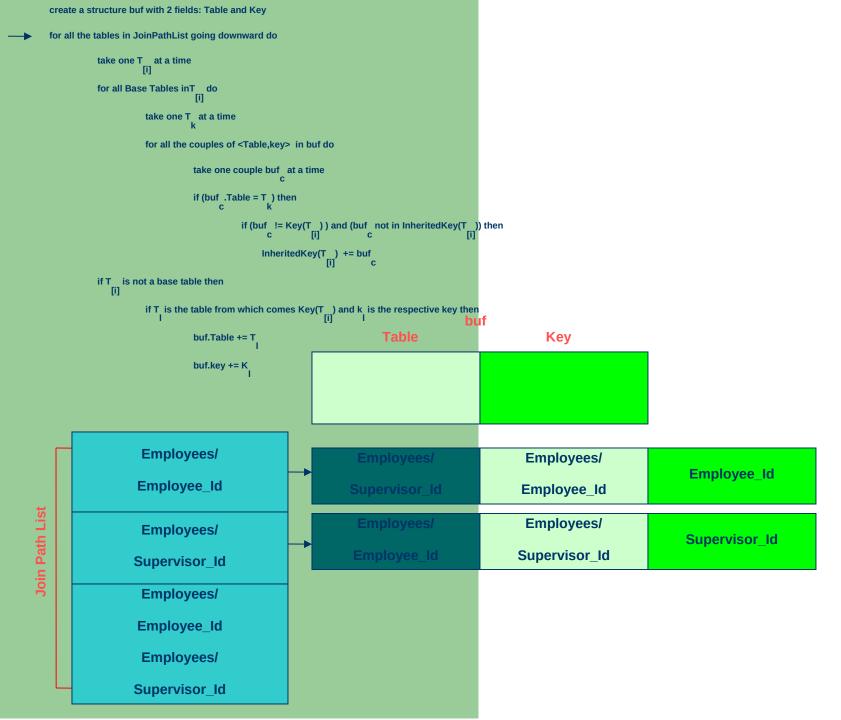


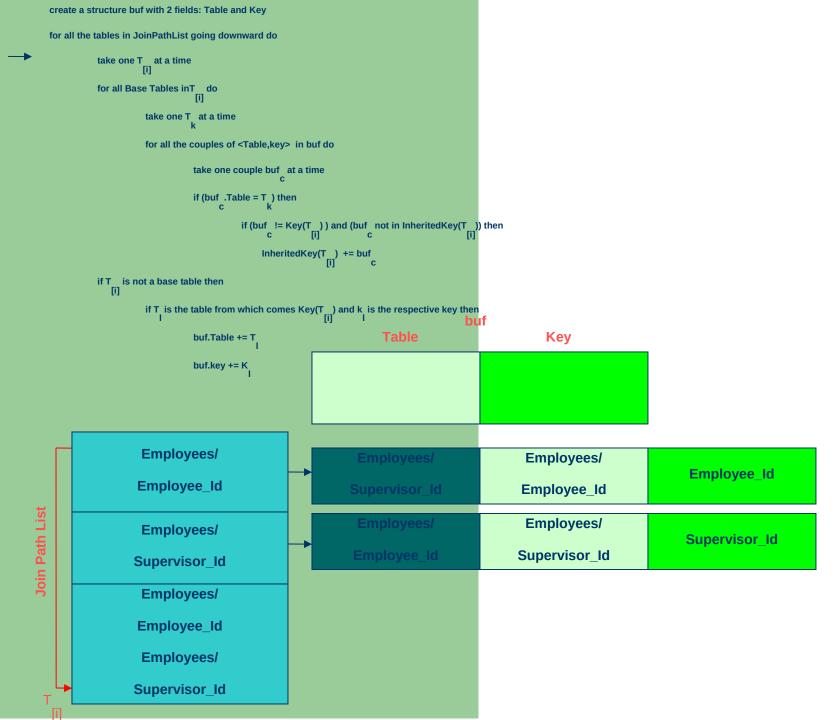


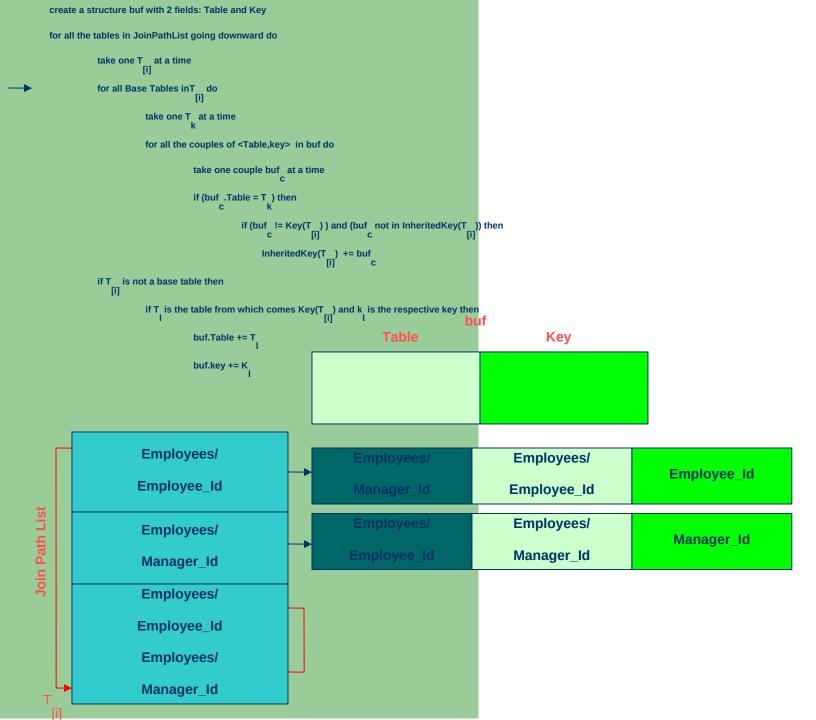


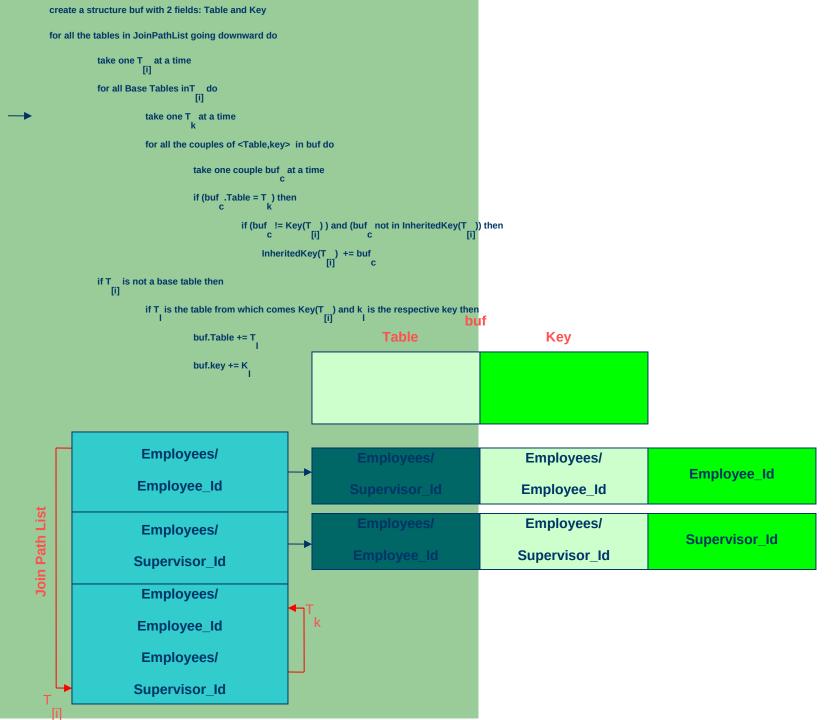


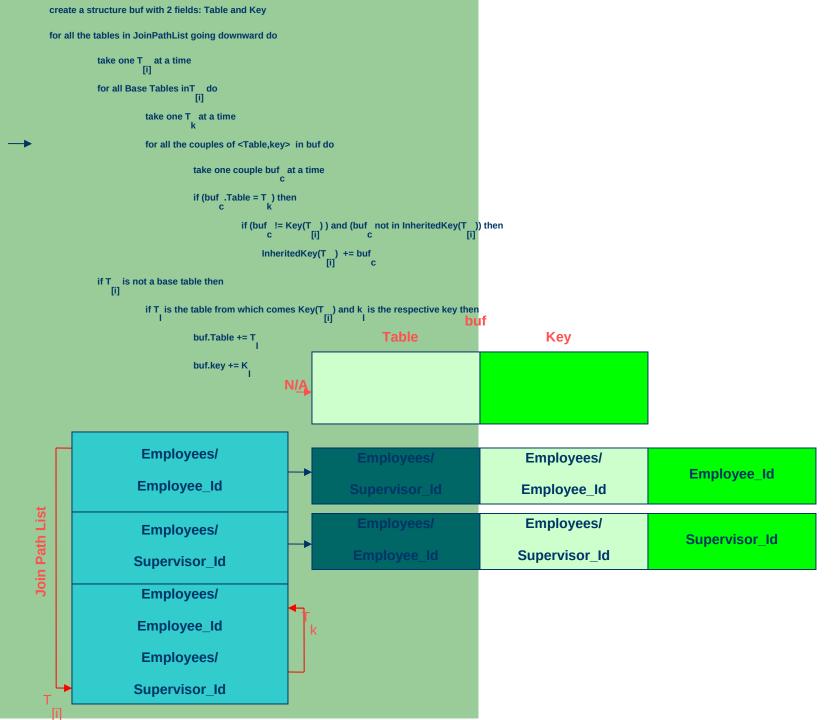
```
create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
           take one T at a time [i]
           for all Base Tables inT do
                      take one T at a time
                       for all the couples of <Table,key> in buf do
                                  take one couple buf at a time
                                  if (buf .Table = T ) then
                                             if (buf _{\rm C} != Key(T _{\rm [i]}) ) and (buf _{\rm C} not in InheritedKey(T _{\rm [i]})) then
                                                  InheritedKey(T ) += buf c
           if T is not a base table then
              [0]
                      if T is the table from which comes Key(T ) and k is the respective key then [i] I
                                                                                                   buf
                                                                                Table
                                                                                                                       Key
                                  buf.key += K
```

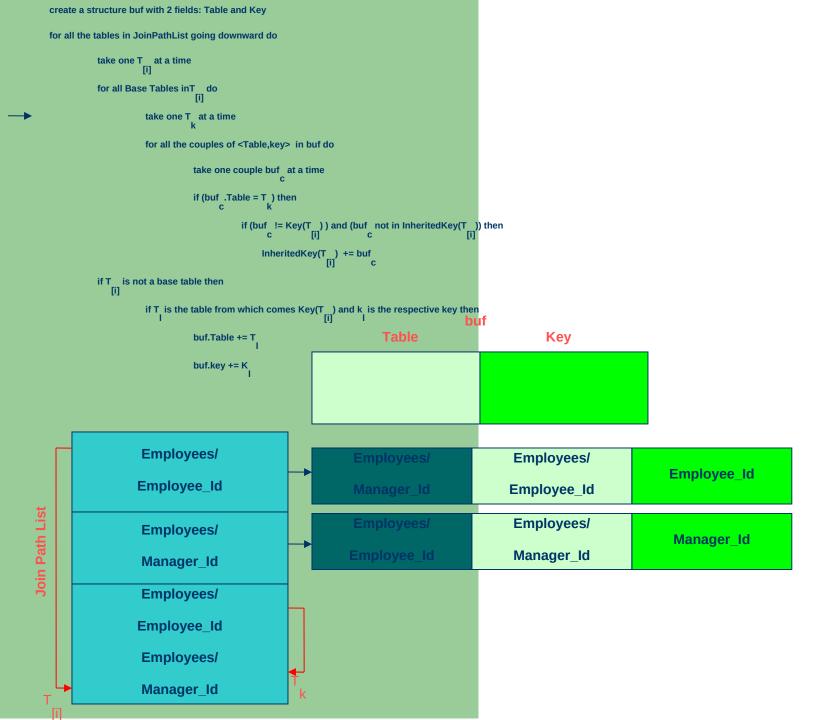


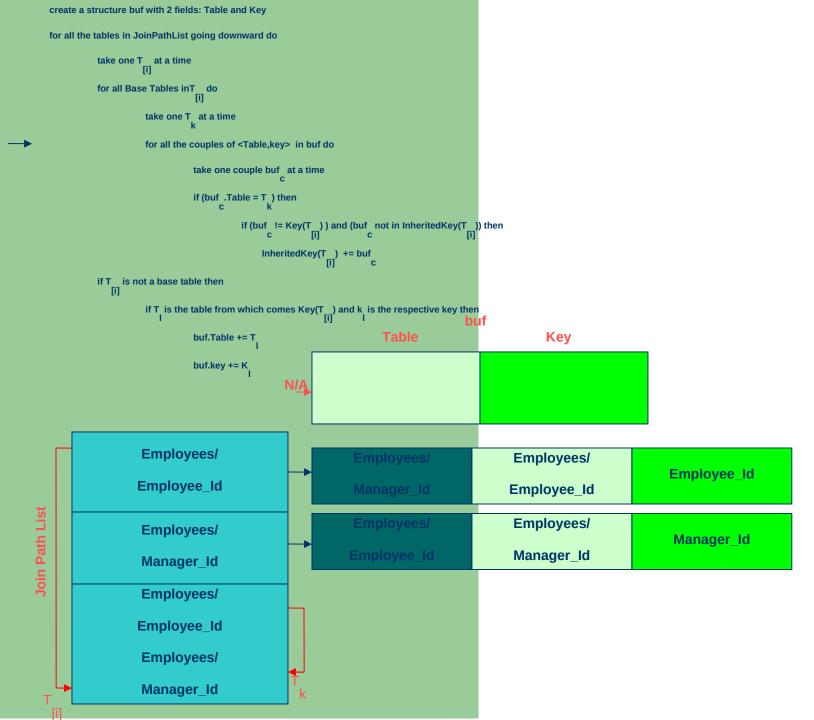


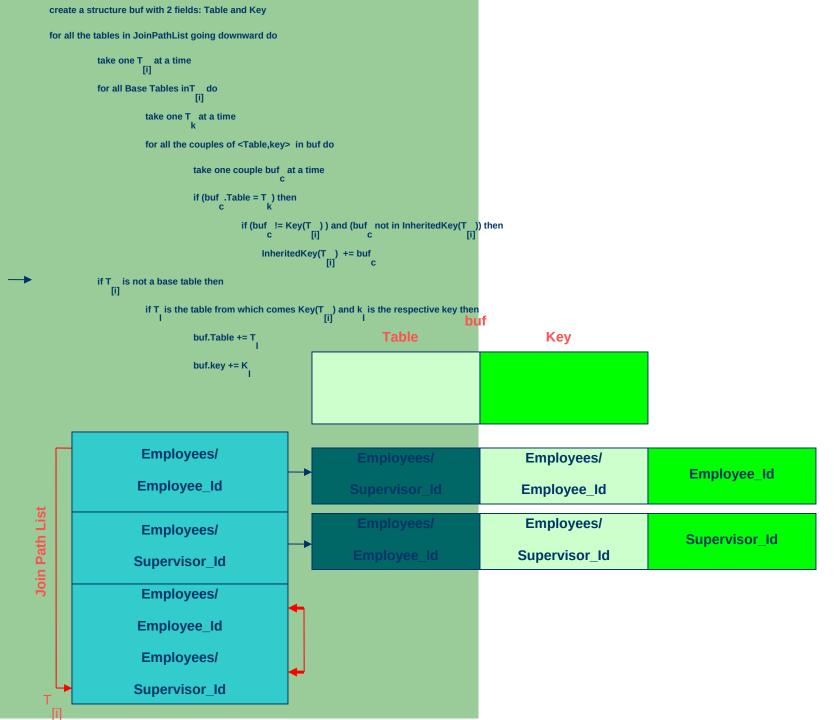


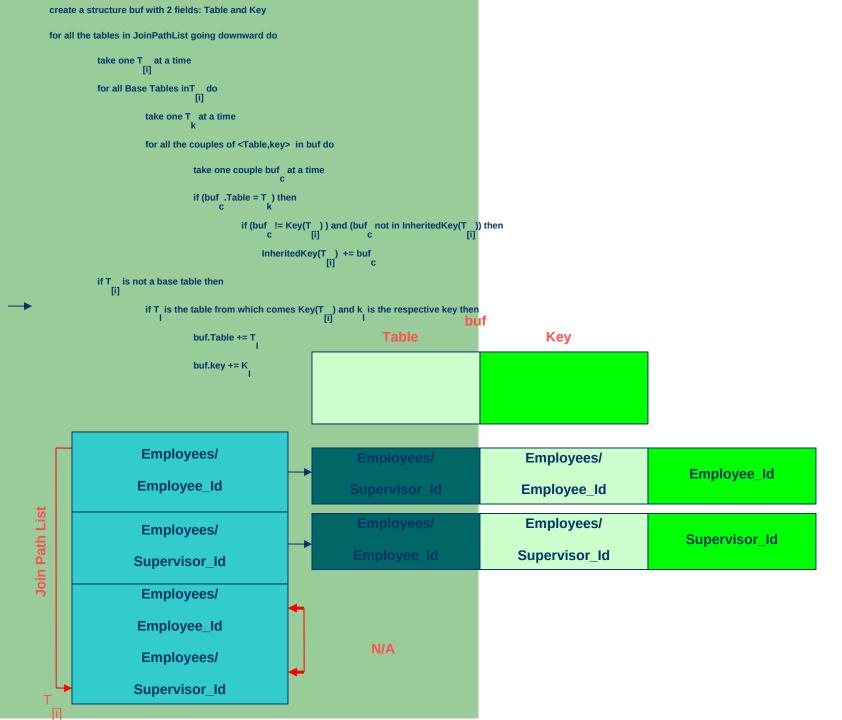


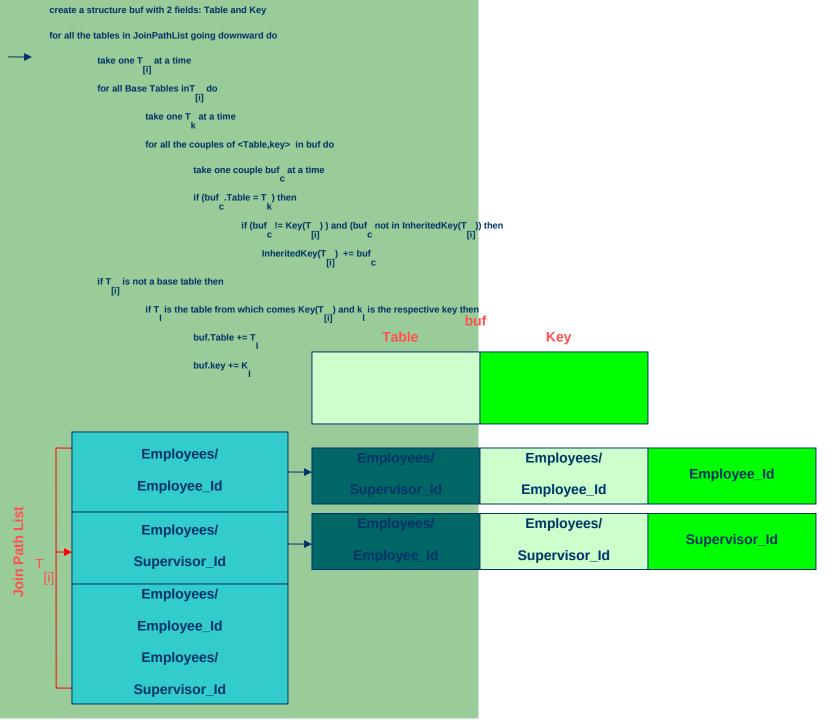


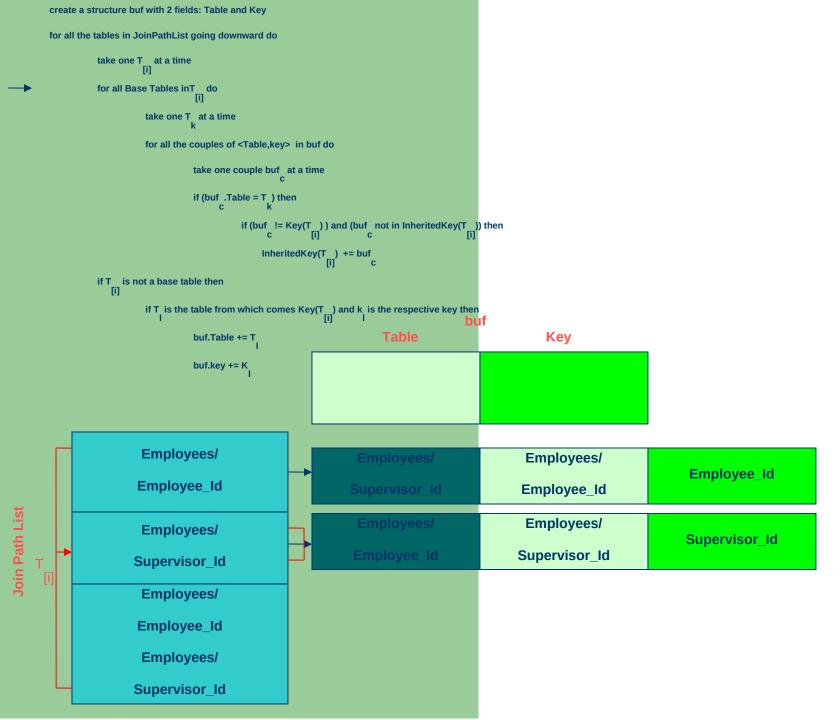


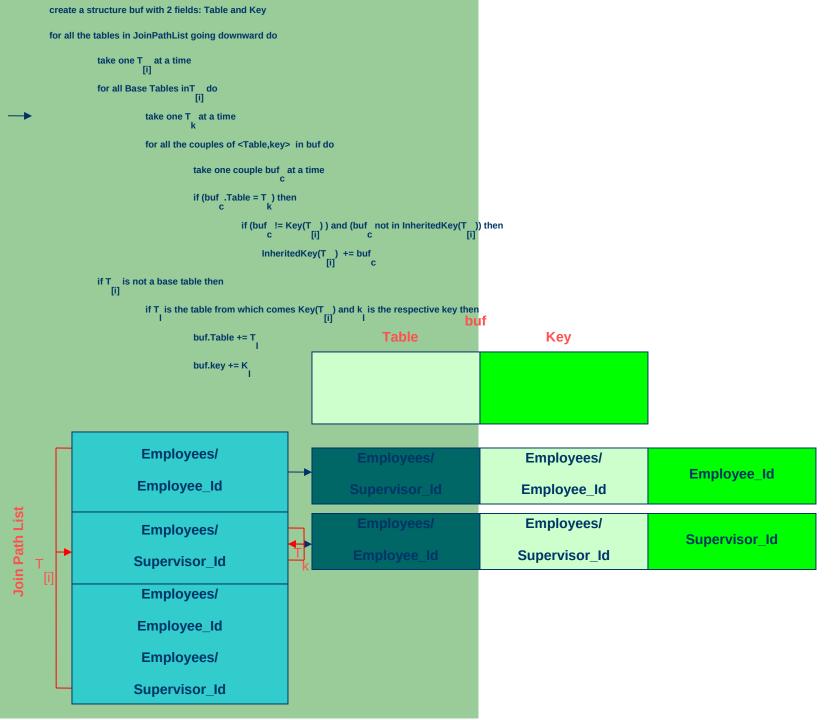


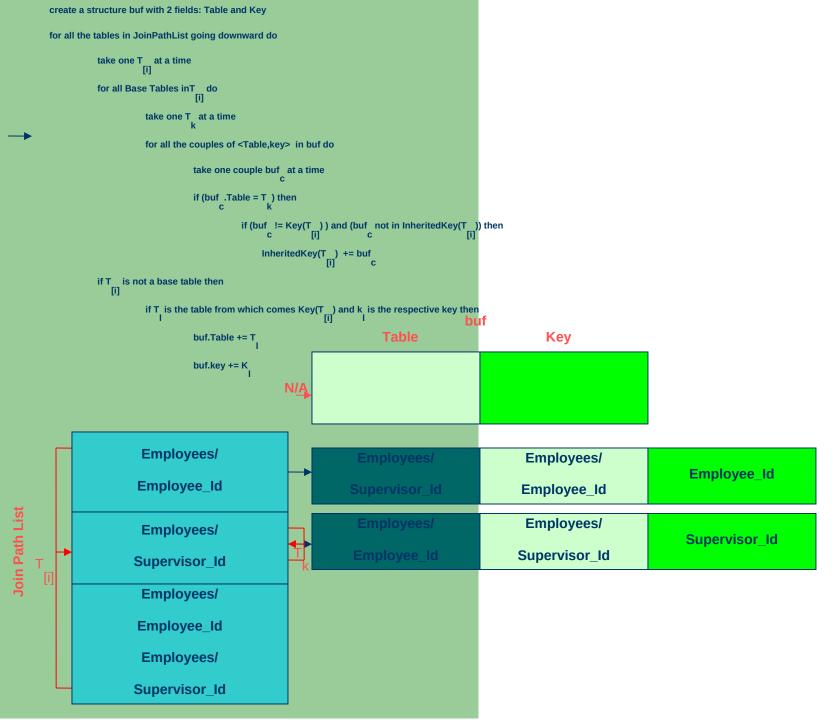


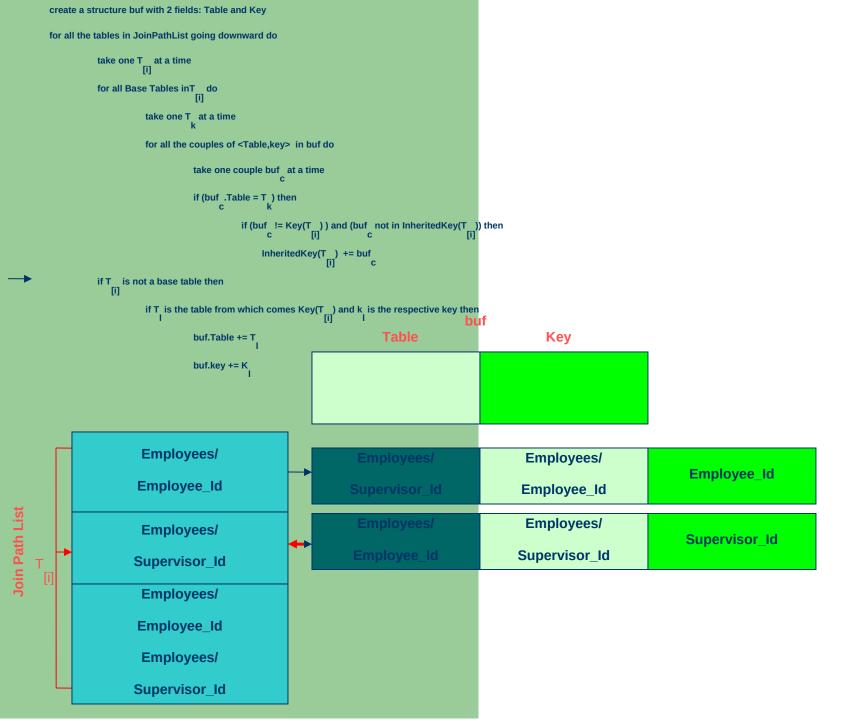


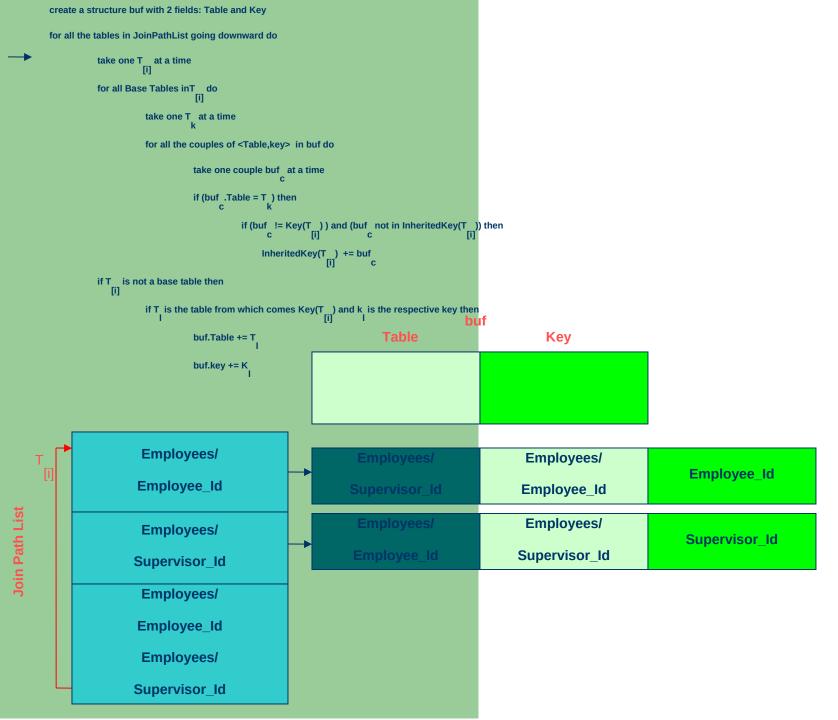


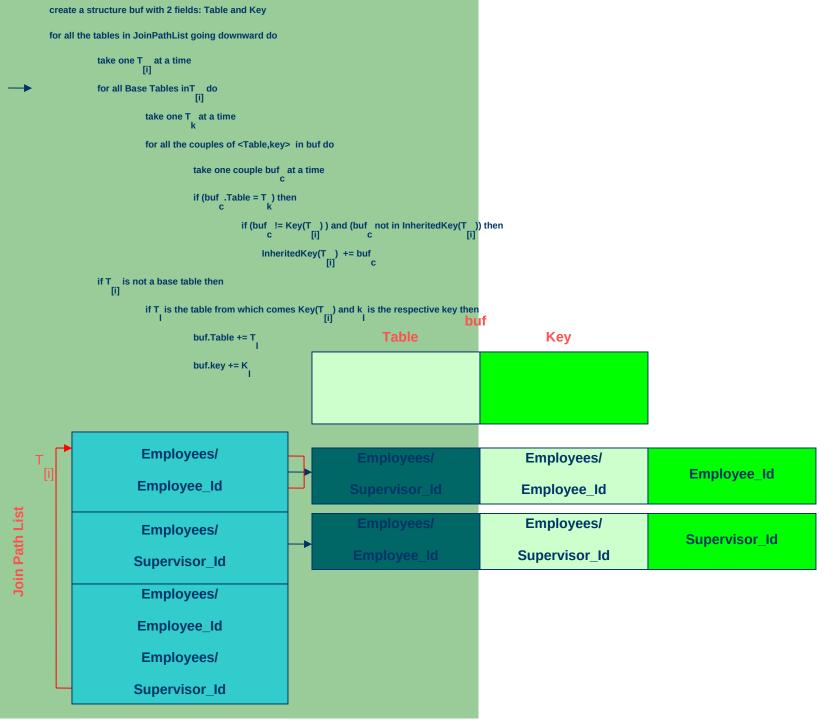


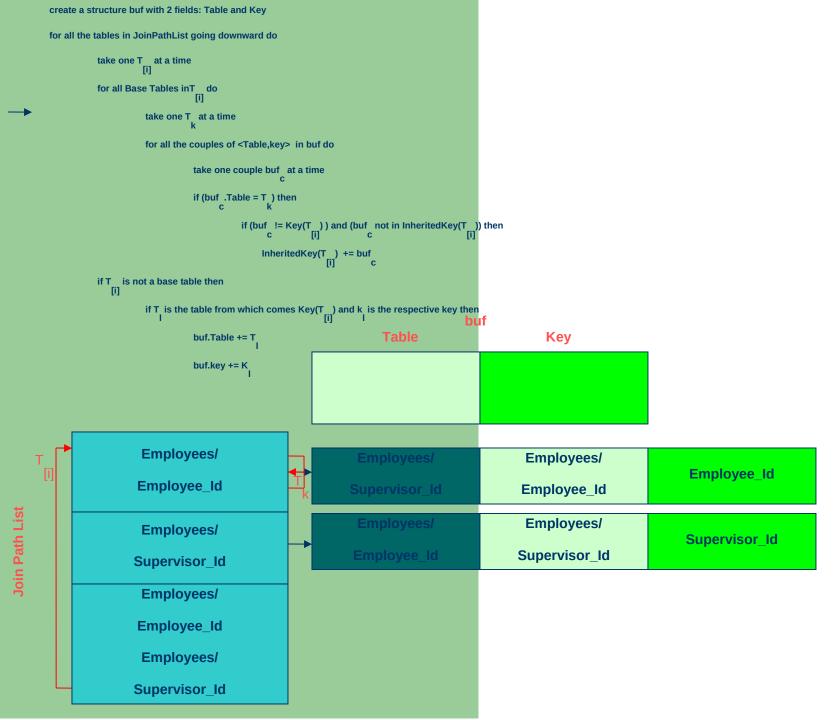


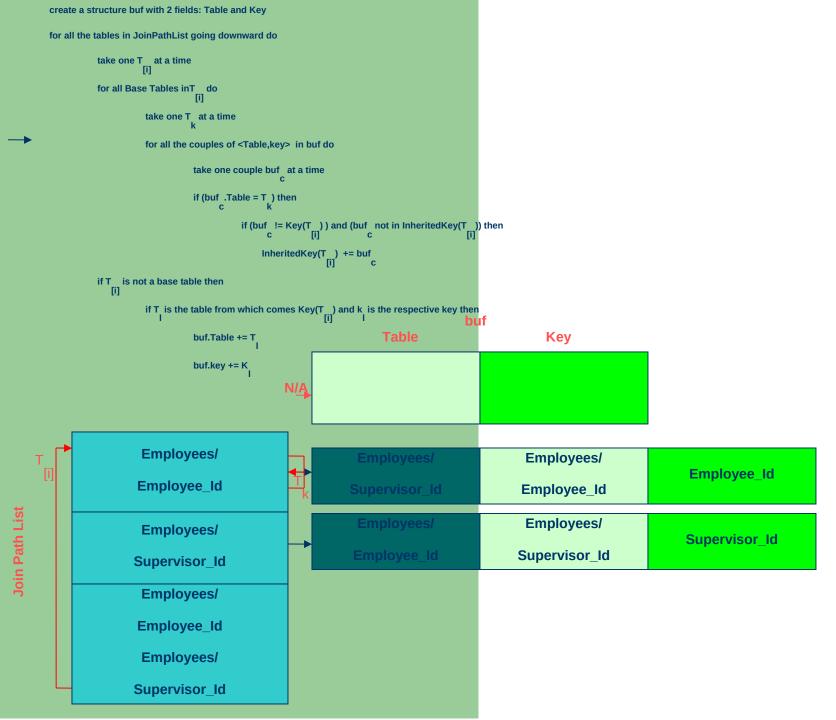


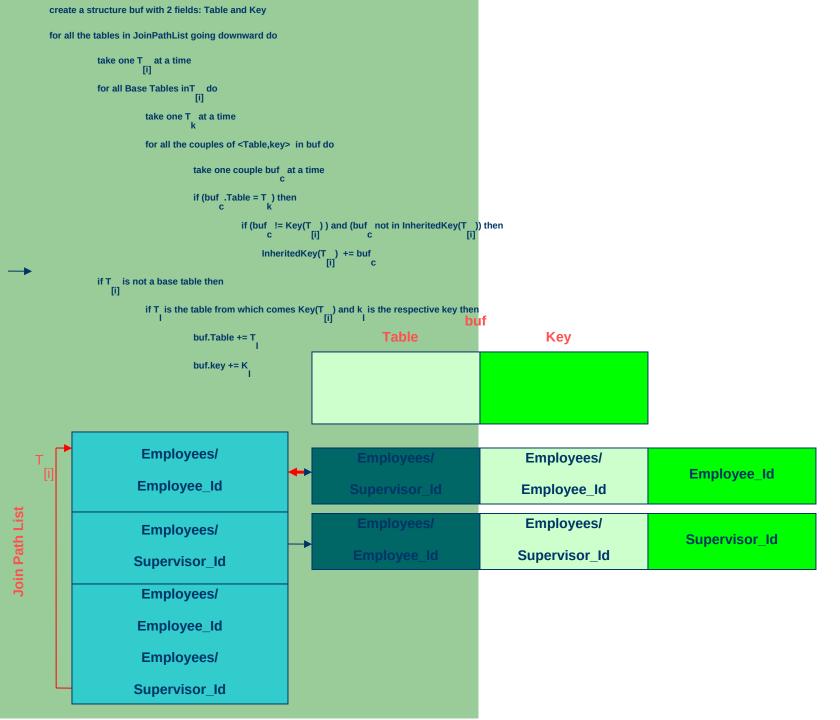












```
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 for all the tables in JoinPathList going downward do
           take one T at a time [i]
           for all Base Tables inT do [i]
                     take one T at a time
                     for all the couples of <Table,key> in buf do
                               take one couple buf at a time
                               if (buf .Table = T ) then
                                          if (buf _{\rm C} != Key(T _{\rm C} ) ) and (buf _{\rm C} not in InheritedKey(T _{\rm C} )) then
                                              InheritedKey(T ) += buf
[i] c
           if T is not a base table then [i]
                     if T is the table from which comes Key(T) and k is the respective key then
                               buf.key += K
                     Employees/
                                                                                                      Employees/
                                                                                                                                         Employee_Id
                    Employee_Id
                                                                                                      Employee_Id
Join Path List
                                                                                                       Employees/
                     Employees/
                                                                                                                                         Supervisor_Id
                                                                                                     Supervisor_Id
                   Supervisor_Id
                     Employees/
                    Employee_Id
                     Employees/
```

Supervisor_Id

Employees table

	EMPLO	NAME	EMAIL	PHONE_	HIRE_	JOB ID	SALARY	SUPER	DEPART
	YEE_ID			NUMBER	DATE			VISOR_ID	MENT_ID
0	101	Mark Stench	mstench	233-4268	12/02/1998	FI_MGR	60000	106	FIN
1	102	Jorge Perez	jperez	448-5268	05/14/1999	AC_MGR	60000	106	ACC
2	103	Edward Cartier	ecartier	742-8429	03/01/2003	SA_MGR	60000	106	SAL
3	104	Teresa Gonzalez	tgonzalez	134-8329	12/20/2002	AC_AUD	55000	102	ACC
4	105	Michelle Blanche	mblanche	745-7496	01/02/2001	SA_REP	35000	103	SAL
5	106	Peter Spencer	pspencer	111-2222	01/01/1996	GE_MGR	120000	NULL	GEN

