

B⁺Tree

A mechanism to drive existing B⁺Trees to do Join Internally.

B[×]TREE Index

To understand how B[×]TREE Index works let see what happens when we insert a new Row R_m from Table T_i into the database.

Suppose that table T_i is in Direct Join with a table T_k , we have to look for all the Rows $R_n \dots R_z$ in T_k that satisfy the join condition with R_m and insert Rows references to $R_m R_n \dots R_m R_z$ in the virtual table T_{ik} .

The process should be repeated for $R_m R_n \dots R_m R_z$ with a table in join at least with one of the base tables constituting the Virtual Join Table T_{ij} and so on until we scan a path in the sequence of tables in join.

Transformation of Existing B⁺Tree

- The internal definition for the creation of a B⁺Tree take in consideration the following:
 - Name of B⁺Tree index follow by an index
 - Number of base tables constituting the virtual table indexed by the B⁺Tree
 - Length and type of Keys
 - Length and type of Inherited Keys (They are supplementary fields inserted in the B⁺Tree but they are not part of the key and they are not used for comparison)
- Declare the page of B⁺Tree as a buffer of bytes and divide it as needed. Many existing B⁺Tree follow this technique to support different type of multiple columns Key.
- The Leaf Page structure consists of:
 - Pointer to the previous sibling page
 - number of elements in which everyone consists of:
 - Space for the columns forming the keys
 - Space for the Data Pointers (Row Ids) to reference the Row in every table
 - Space for the columns forming the Inherited Keys
 - Pointer to the next sibling Page

Transformation of Existing B⁺Tree (continue)

- The Non Leaf Page structure consists of:
 - Pointer to a child page which key values are smaller than all the keys in the page
 - number of elements in which everyone consists of:
 - Space for the columns forming the keys
 - Pointer to a child page which key values are bigger than the keys in the Element
- Due to the fact that many join keys are duplicates, change has been made for the duplicates in the sense when 2 keys are equals, we consider the data references for them. The B⁺Tree keeps these possibly duplicated keys separate internally by combining the unique sequence of data references with each key. The process of combination is done logically, and requires no additional space for key storage.

Many advanced B⁺Tree in the market use (Key, Data Reference) combination to refer to unique Row eliminating duplicates internally and use additional fields others than the one forming the key to avoid access to the table.

So for those B⁺Trees, the only modification is instead of space of one Data Reference is a space for multiple Data Reference Space.

Definitions

- **Base Table:**

Base tables are database objects whose structure and the data they contain are both on disk.

- **Virtual Table:**

Virtual tables are tables whose contents are derived from base tables. Only its definition (base tables Names constituting it) is stored on disk.

Definitions

Direct Join:

Two tables are in Direct Join if there is a link between them (in other sense if there is common columns between them).

Join Graph:

A graph representing direct join between tables.

Adjacency List:

List for every table T_i in the database all those tables in direct Join with it.

Generating Join Graph

- Base Tables represent the vertexes of the Join Graph.
- Due to the fact that join is commutative, for every pair of tables in direct join between them as defined by DBA create an undirected edge to link them.
- It is very easy to know which tables are in direct join with other tables from the definition of common columns between them.

The algorithm for generating the Linked List representation of the join Graph is the following:

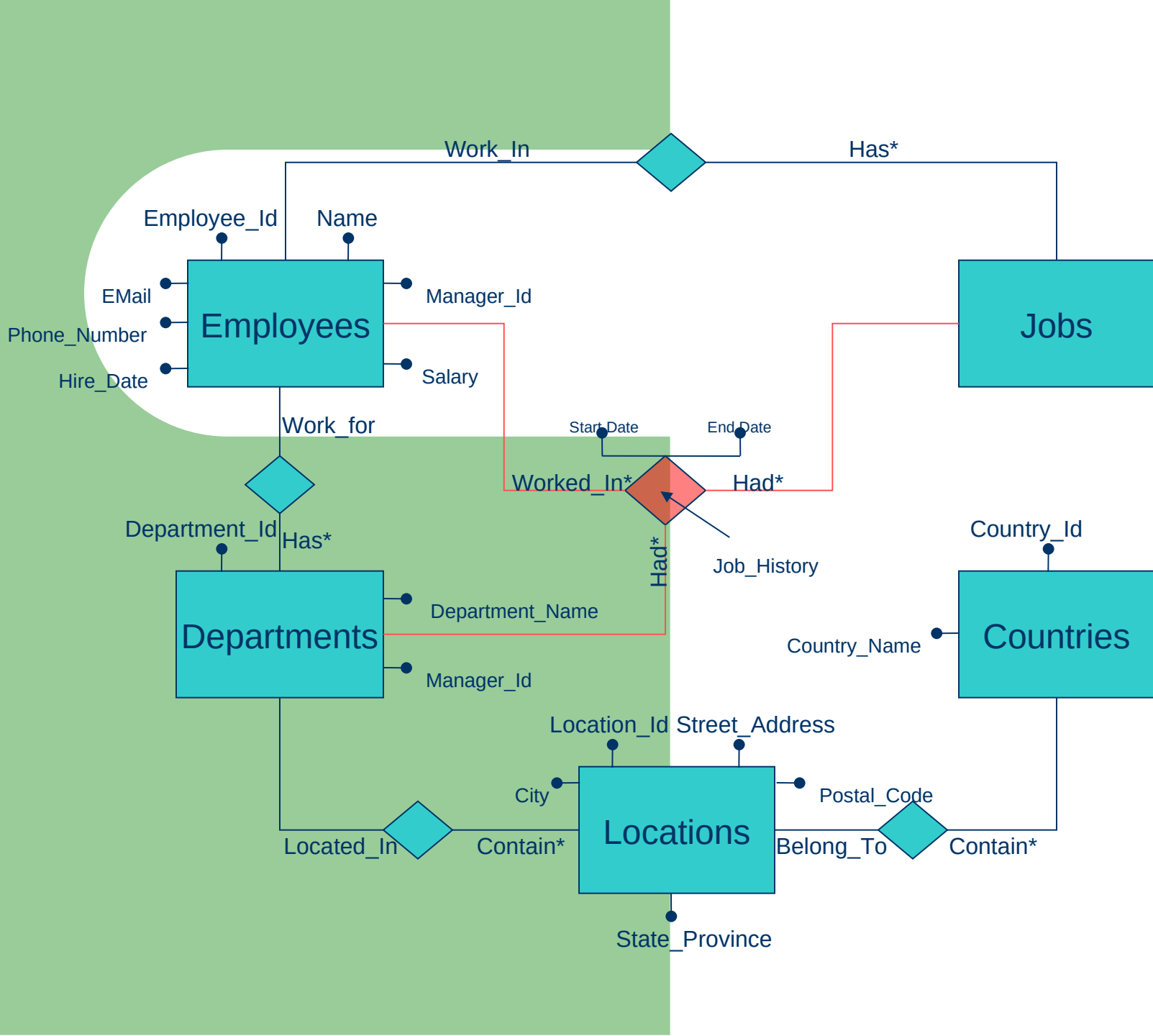
generateJoinGraph (in BaseTables; out JoinGraph)

insert the base tables as vertexes of the graph

for every direct join between 2 tables T_i and T_k where T_i is the table of order i and T_k is the table of order k as defined by the DBA do

 AdjacentList[T_i] += T_k follow by the common key

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Base Tables

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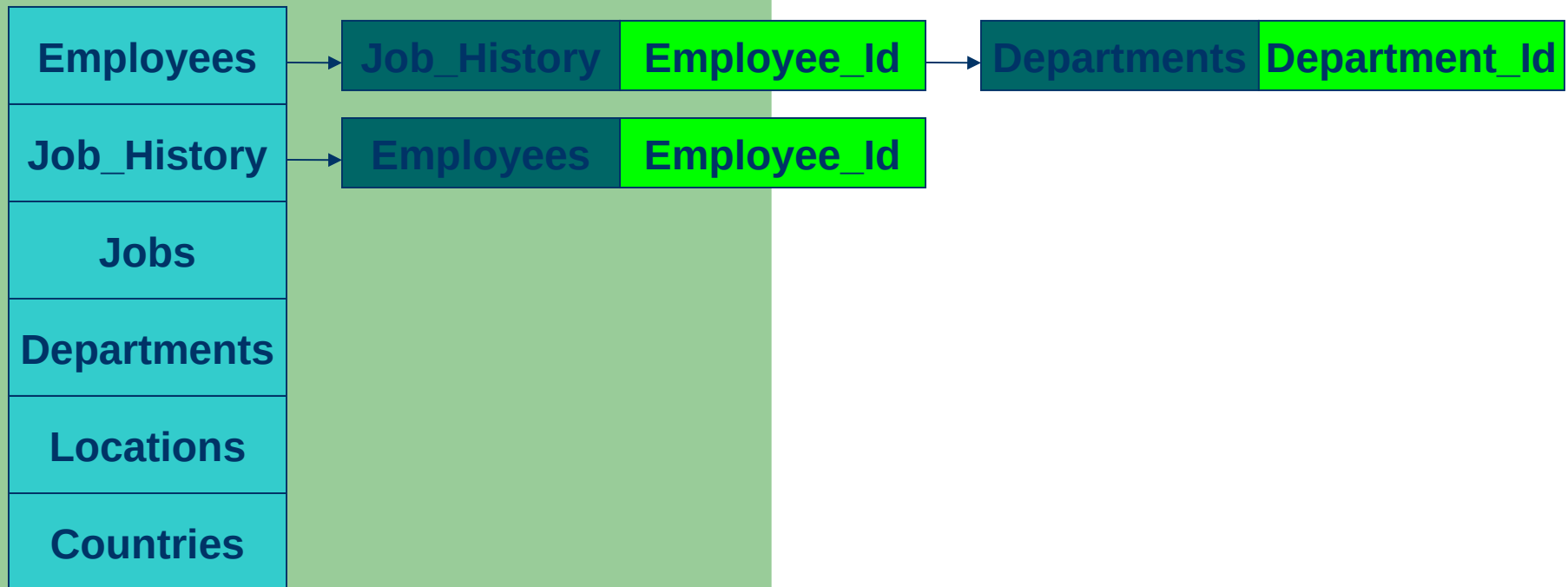
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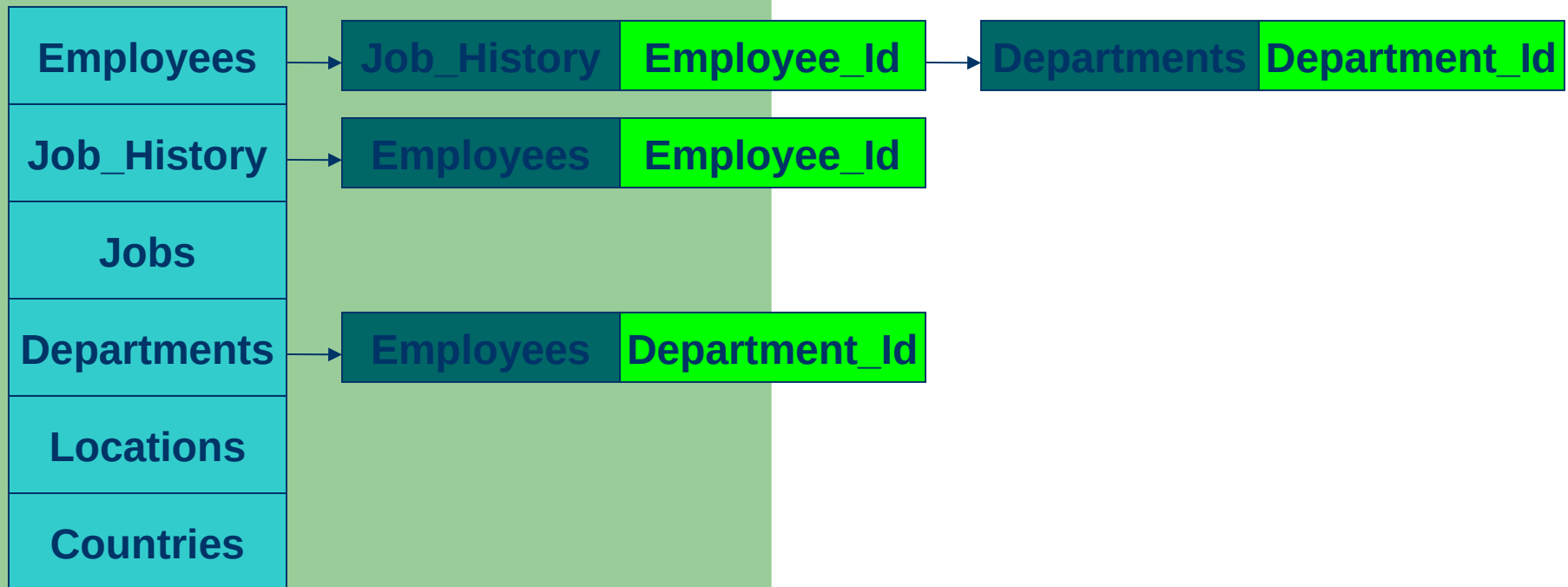
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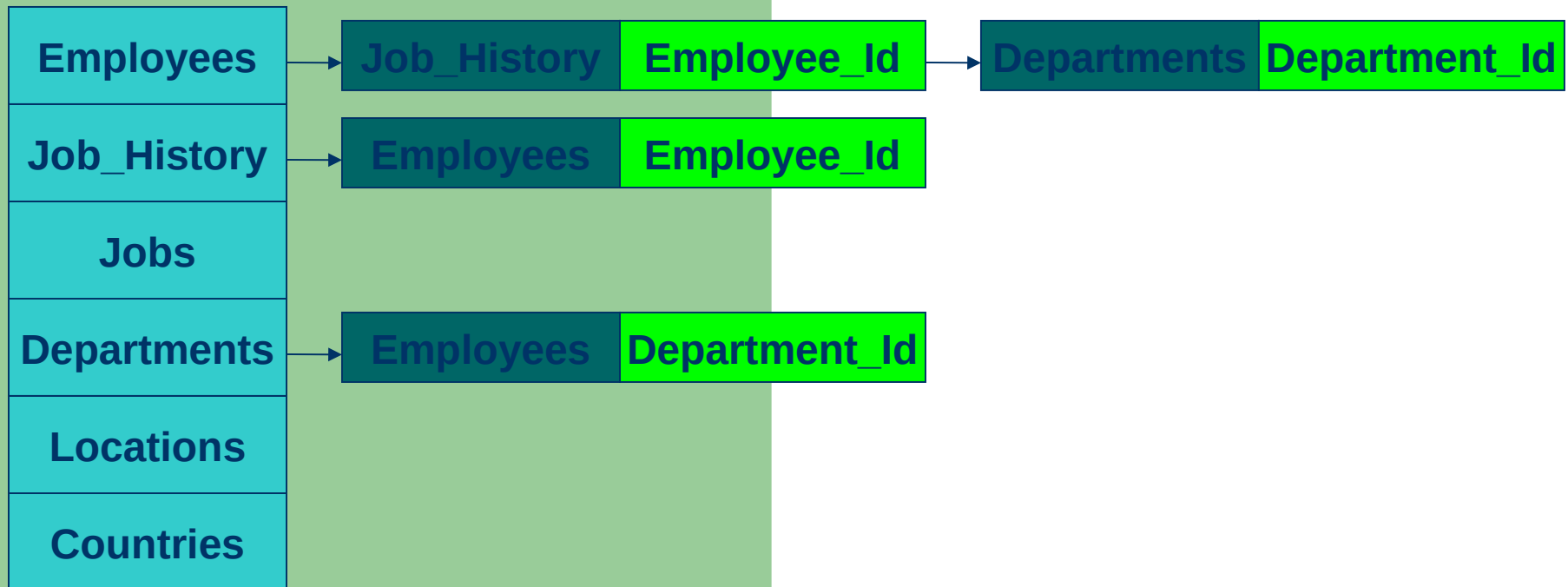
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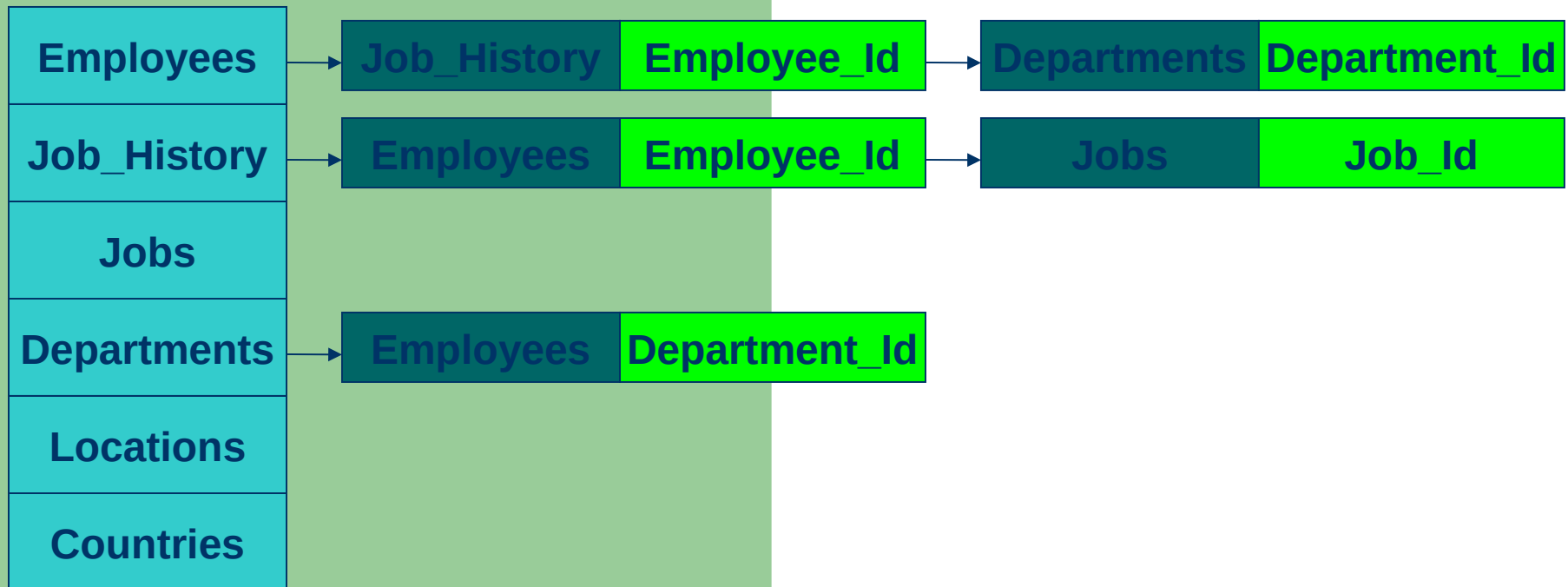
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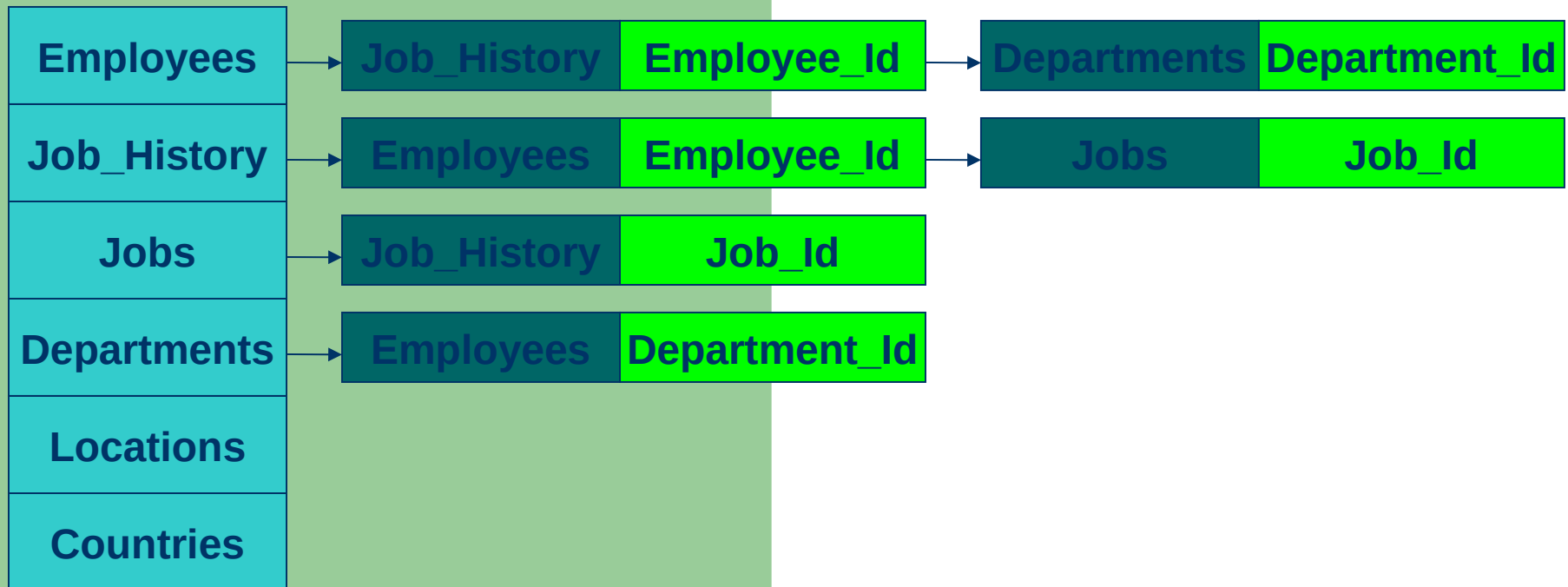
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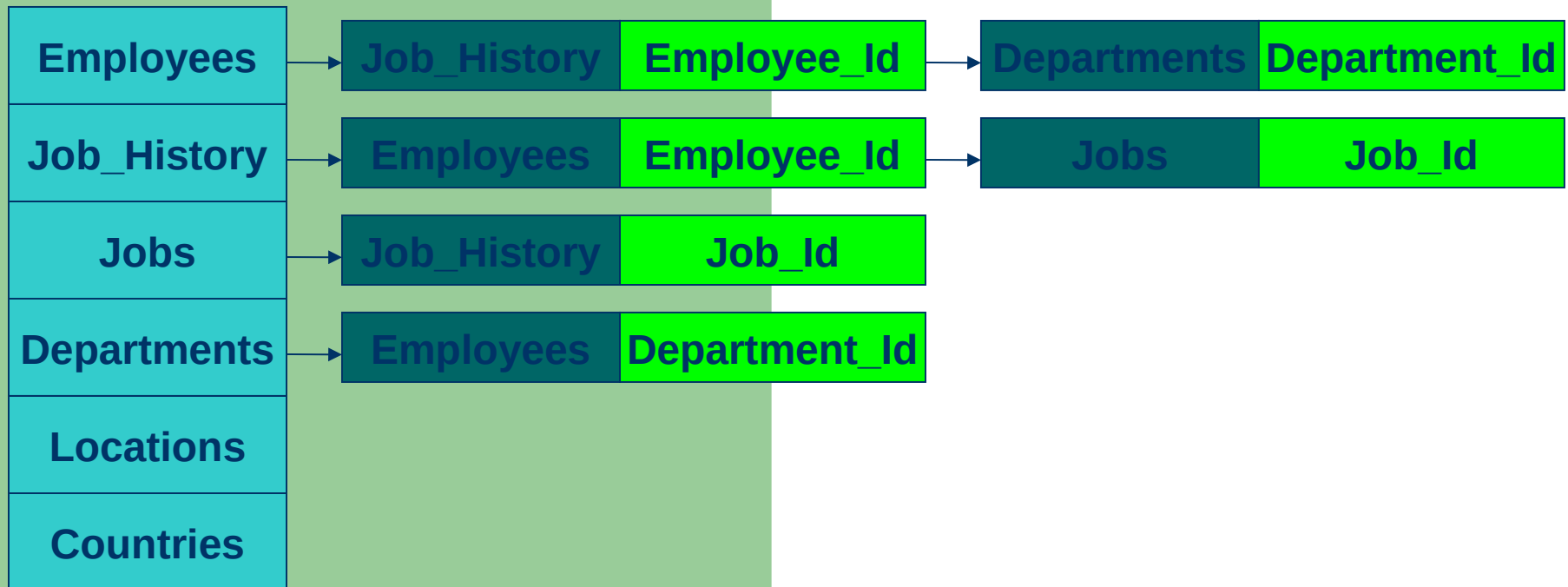
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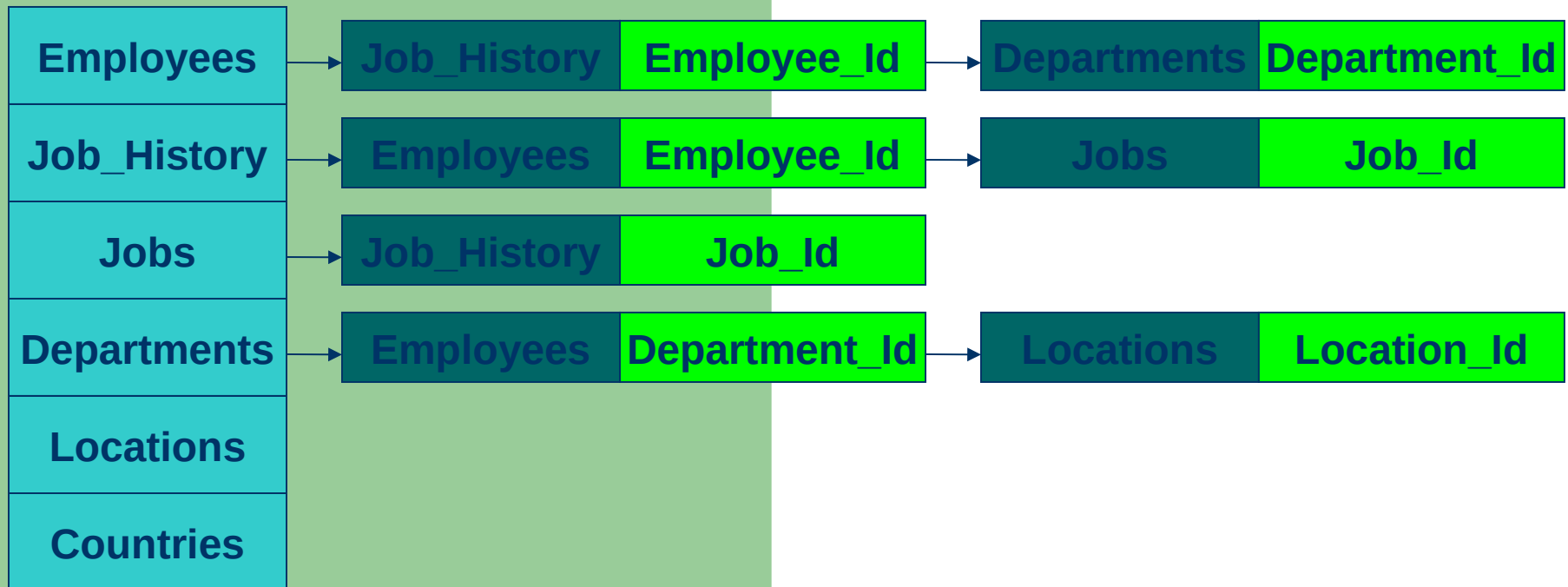
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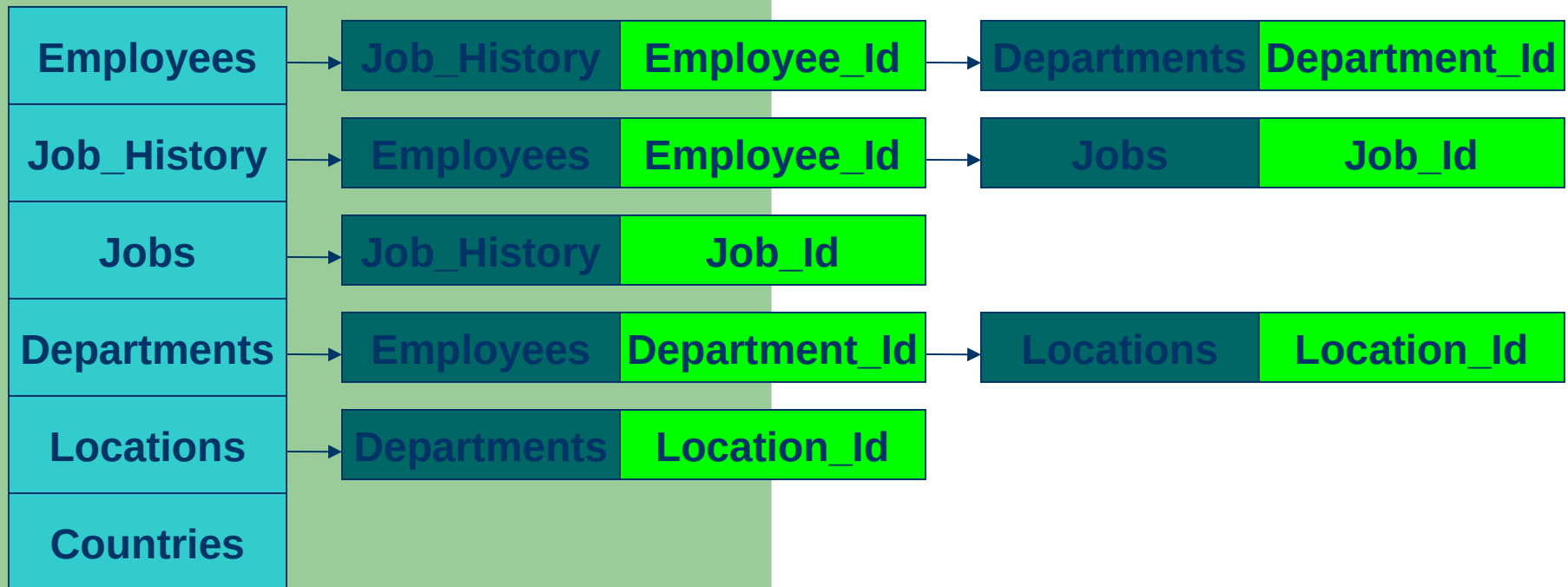
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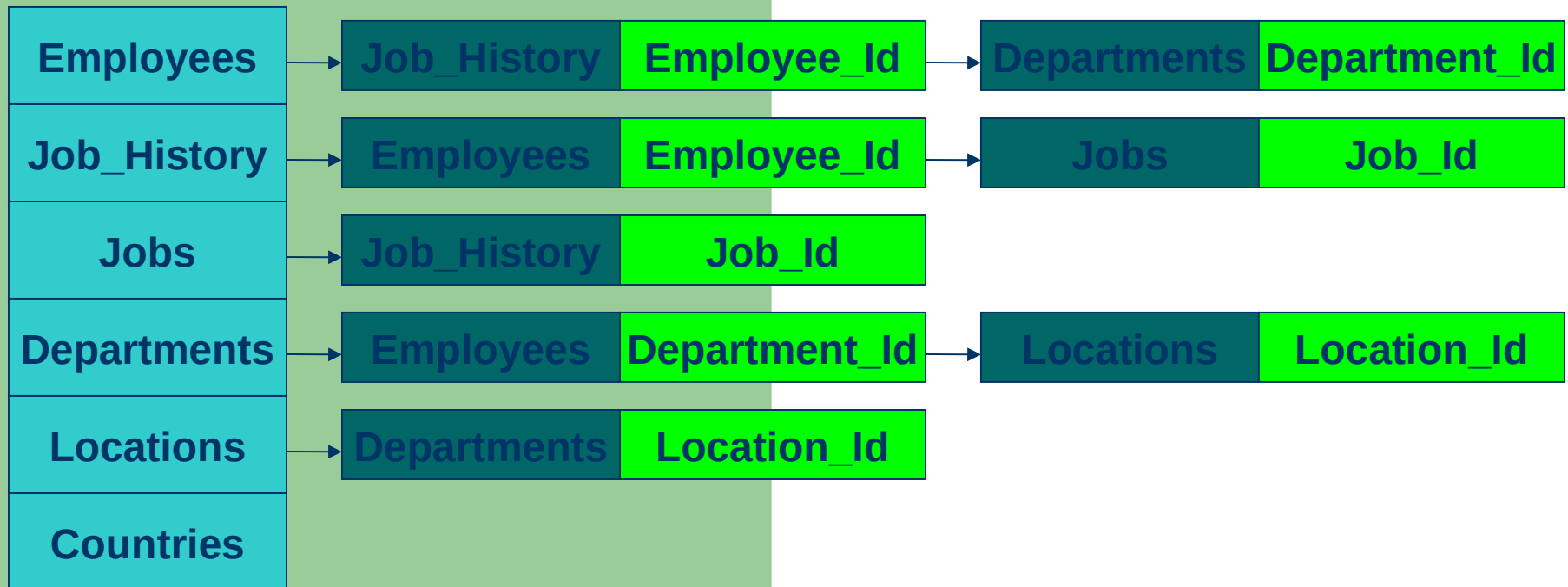
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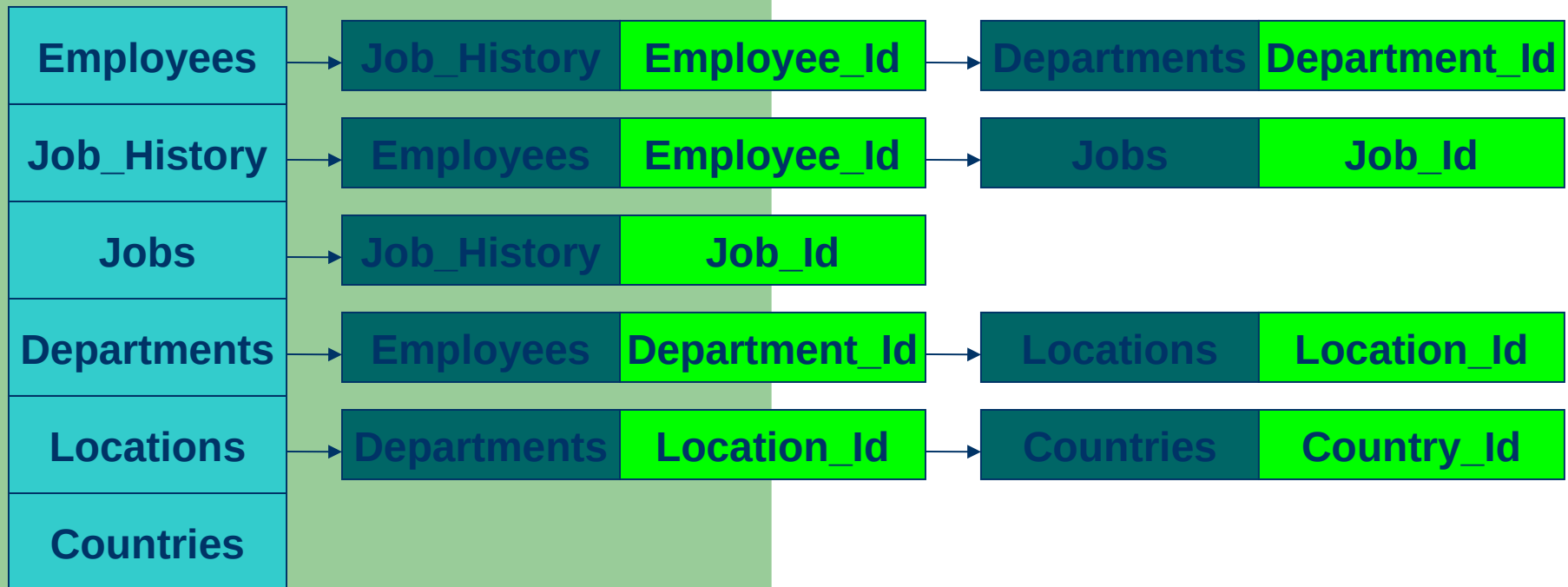
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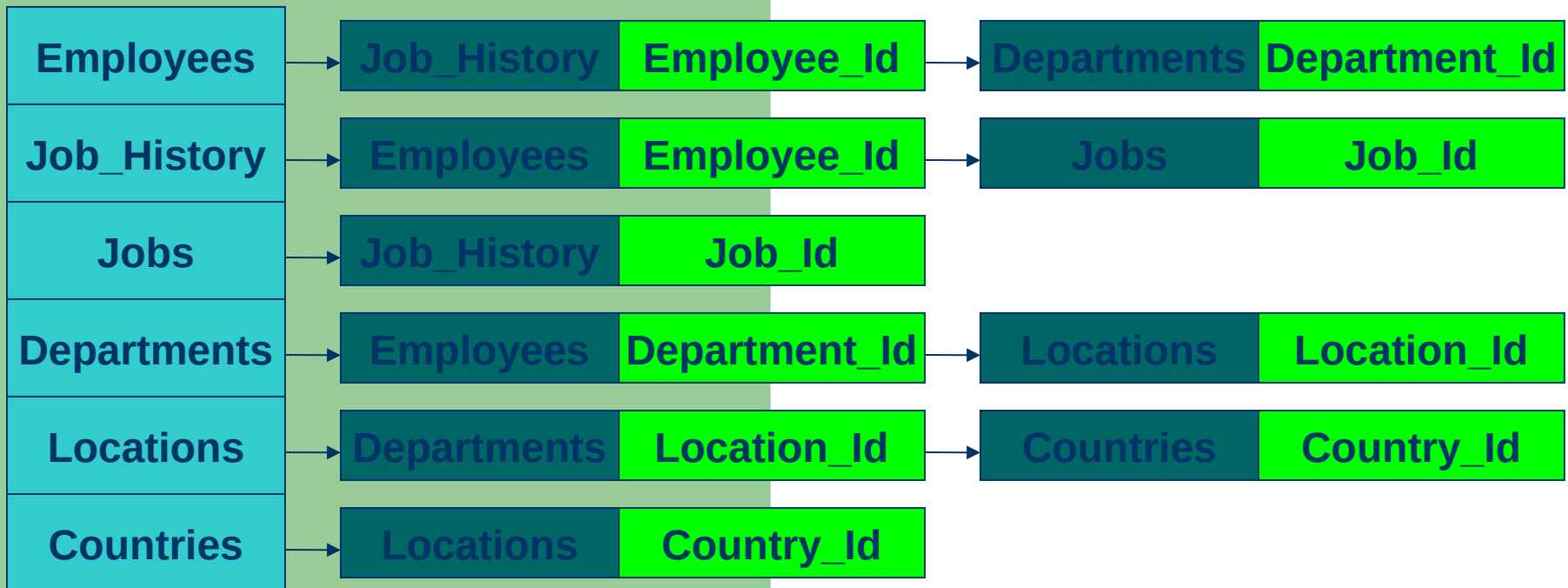
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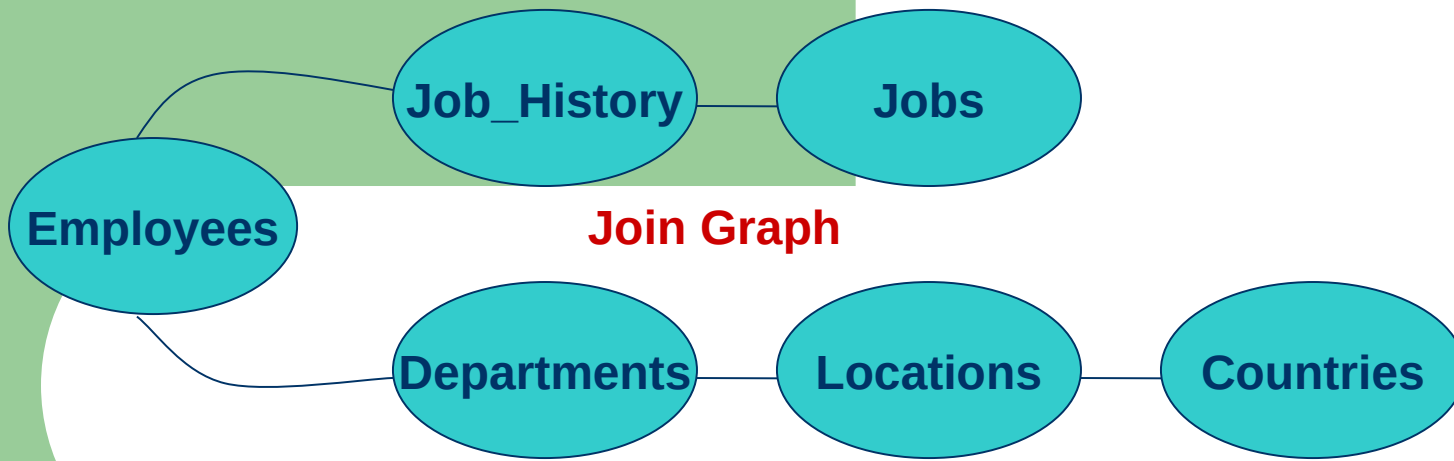
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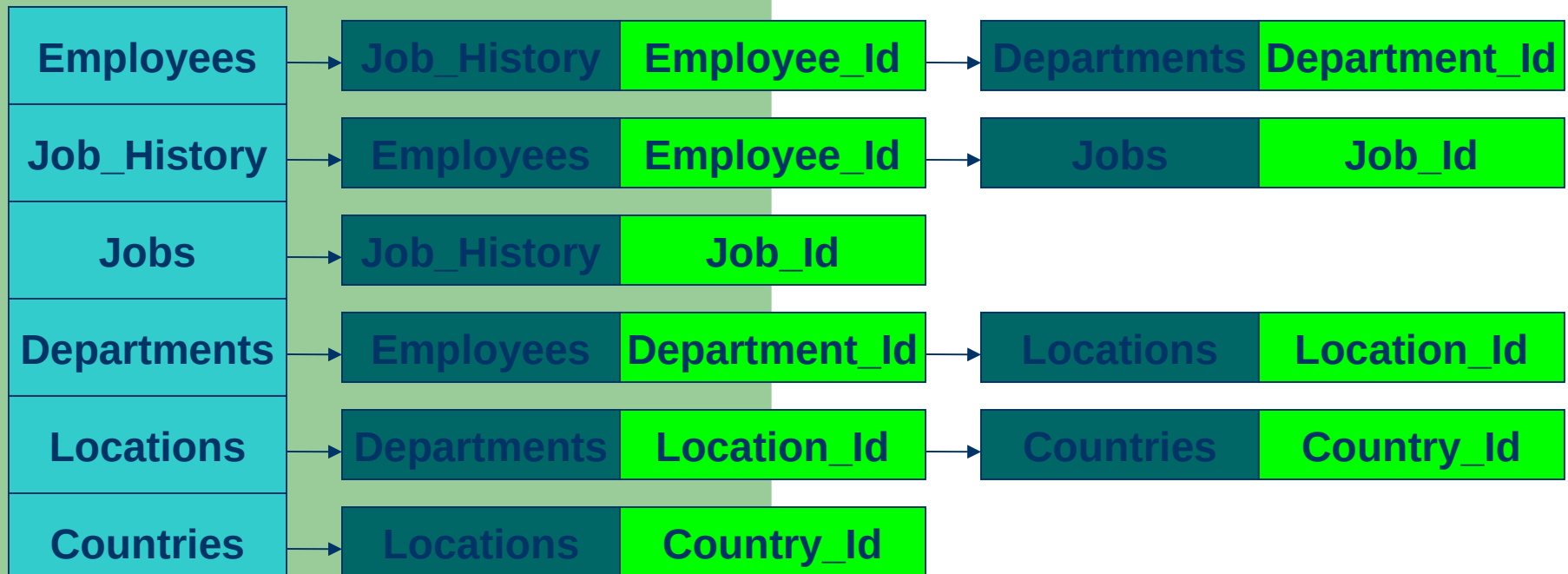
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Linked List representation of the Join Graph



Definitions

Join Path List:

A sequence of tables $T_0 \dots T_{n-1}$ is in the Join Path List if every T_i of them is at least in direct join with another table in the sequence.

Notation

- When index i is not between brackets like in T_i , it represent a base table T_i .

When index i is between brackets like in $T_{[i]}$, it represent a base table T_i or a virtual table in which index i represent a set of indexes for the base tables forming the virtual table.

Steps to generate function: $\text{Key}(T_{[j]})$ $\text{getFirstAdjacentListKey}(T_{[j]}, T_{[k]})$

for every Base Table T_l in $T_{[j]}$ do

Take one at a time

for every $T_{\text{Link}(l)}$ do

Take one at a time

if $T_{\text{Link}(l)}$ in $T_{[k]}$ then

return($\text{key}(T_l, T_{\text{Link}(l)})$)

Normally one of the 2 tables $T_{[j]}$ or $T_{[k]}$ is a base table this is why we stop after founding the key.

Key could be a one column key or multicolumn key that satisfy the join condition.

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$

```
let  $T_0 \dots T_m$  be the base tables
create 2 dynamic arrays queue and path
insert  $T_0$  into path
insert  $T_0$  into queue
repeat
     $T_{\text{Element}}$  = First Table in queue
    for every Link Item in Adjacent Link of  $T_{\text{Element}}$  from the Join Graph do
        if the Link Item is in the join sequence then
            if path doesn't contain the Link Item then
                insert Link Item into path
                insert Link Item into queue
    remove  $T_{\text{Element}}$  from queue
until queue is empty
```

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$ (continue)

insert all the names of base tables from path as vertexes in the JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{PathJoinAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{PathJoinAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]}^+ = T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$ (continue)

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
 take one $T_{[i]}$ at a time
 for all Base Tables in $T_{[i]}$ do
 take one T_k at a time
 for every buf.Table = T_k do
 if (buf.key \neq Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
 InheritedKey($T_{[i]}$) += buf.key
if T_1 is the table from which comes Key($T_{[i]}$) then
 buf.Table = T_1
 buf.key = Key($T_{[i]}$)

→ generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)
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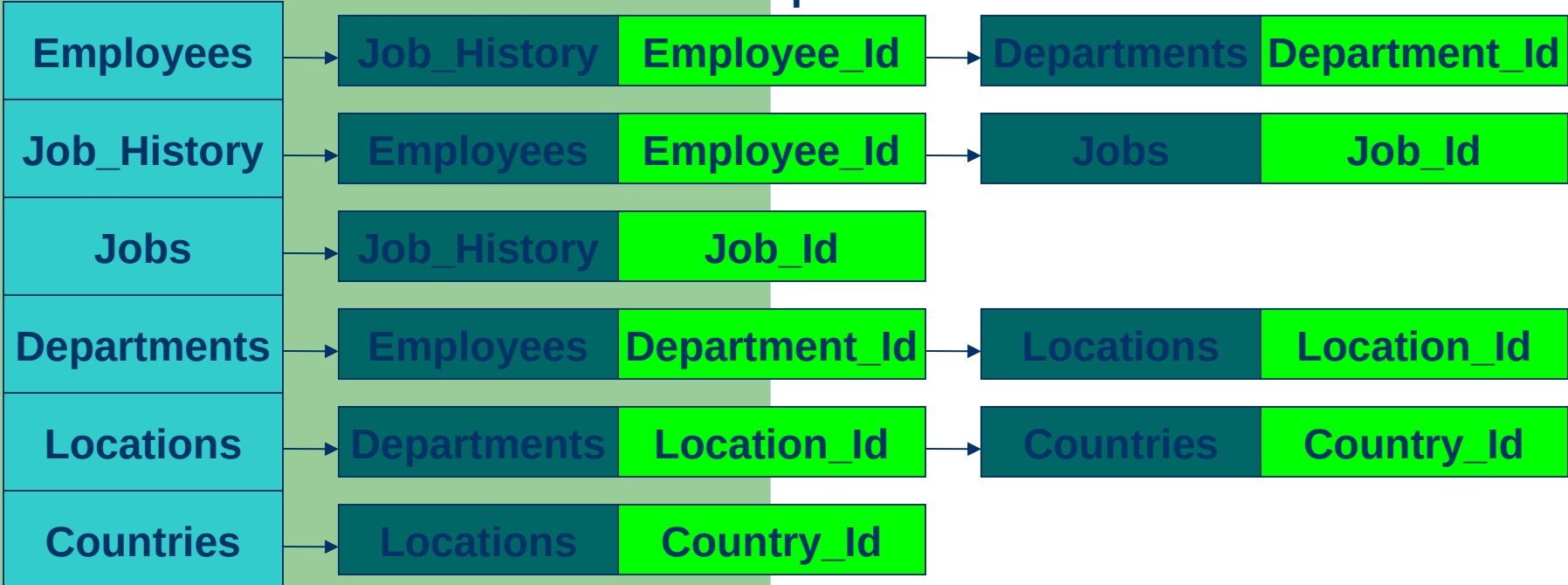
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Join Base Tables

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Join Graph



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T_2

T_3

T_4

T_5

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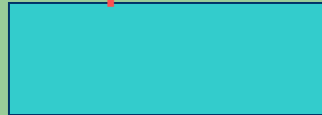
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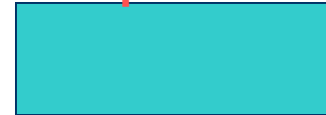
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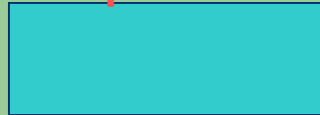
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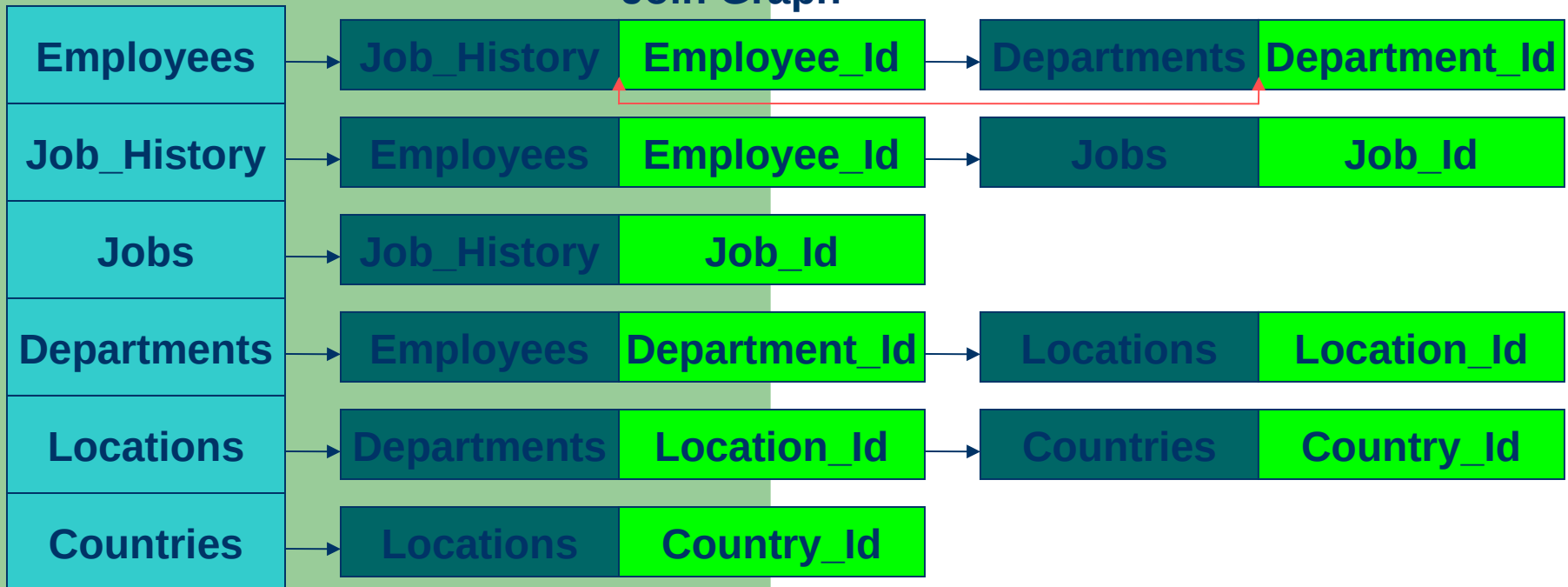
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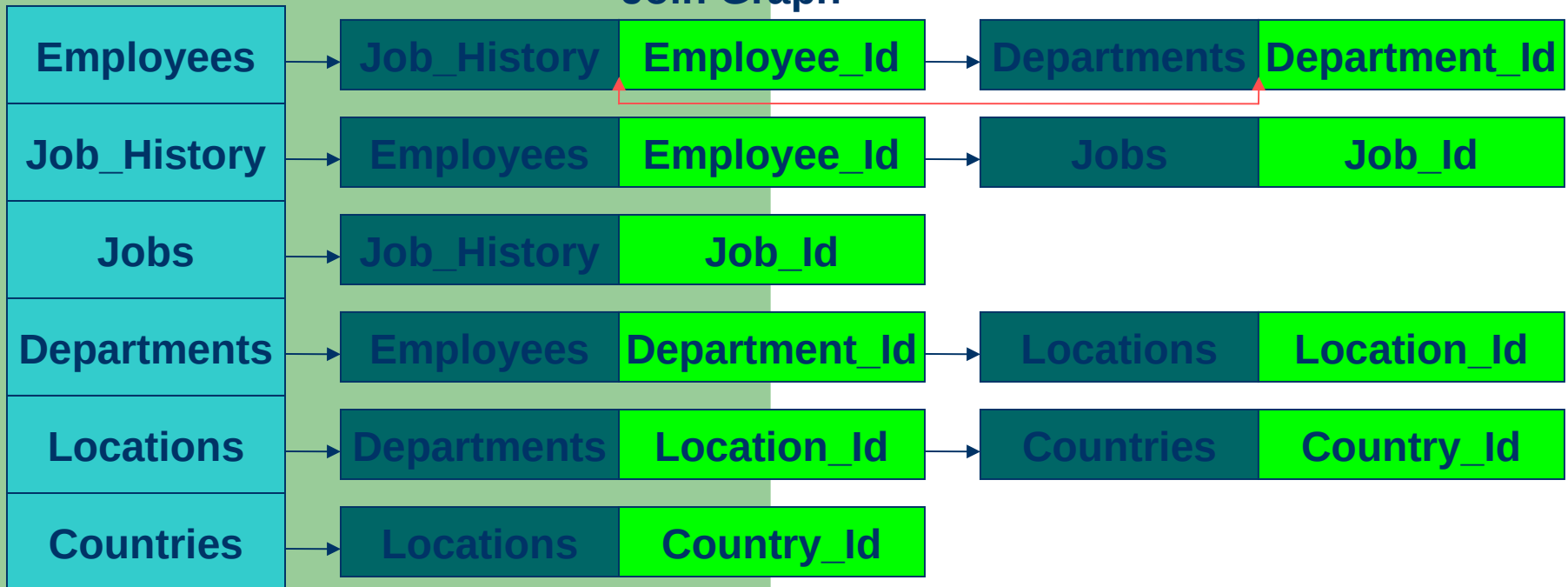
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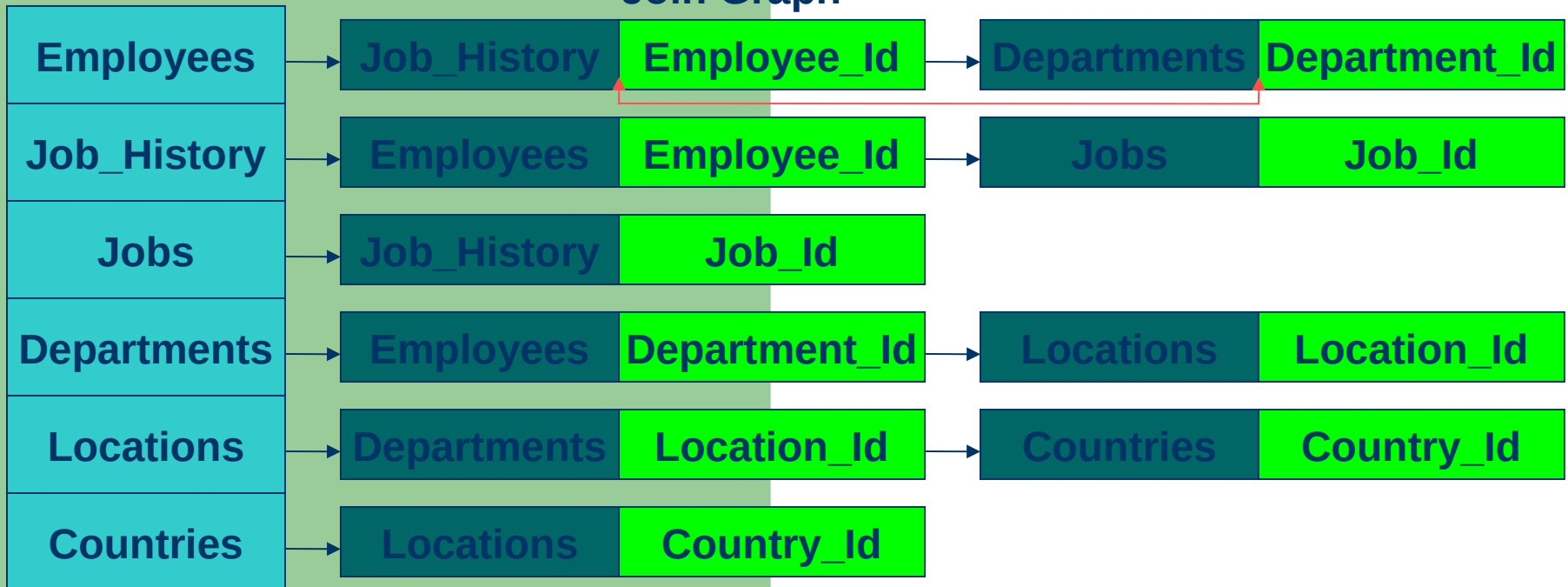
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Employees

Join Base Tables

Employees	Job_History	Jobs	Departments	Locations	Countries
-----------	-------------	------	-------------	-----------	-----------

Join Graph



generateJoinPathList (in Join Base Tables, JoinGraph; out JoinPathList)

let $T_0 \dots T_m$ be the base tables

create 2 dynamic arrays queue and path

insert T_0 into path

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repeat

T_{Element} = First Table in queue

for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

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until queue is empty

queue



Employees

path

Employees

Job_History

Departments

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Job_History
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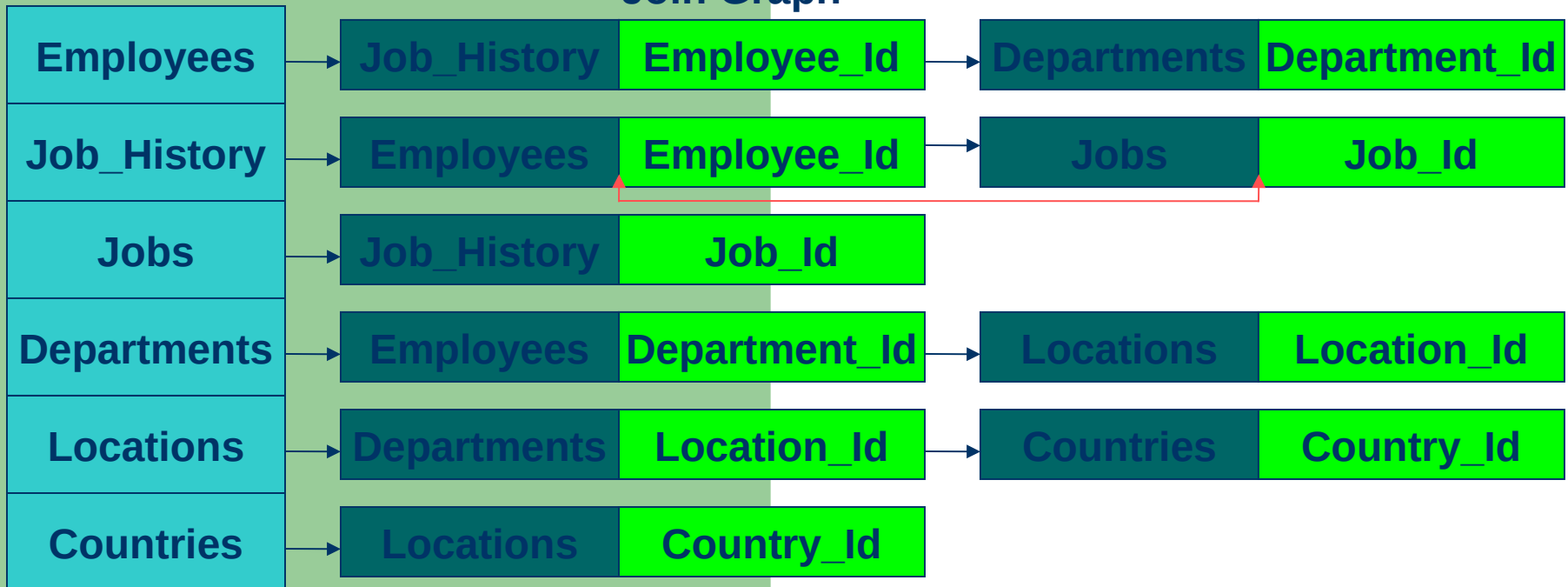
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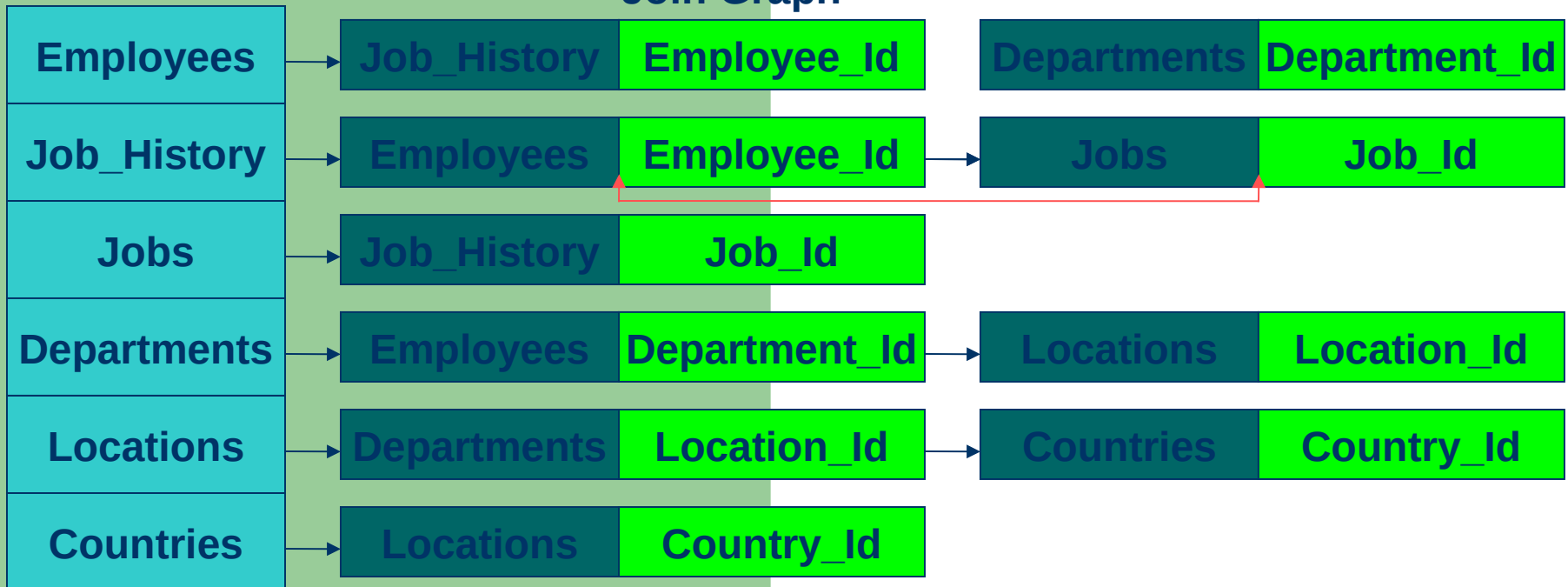
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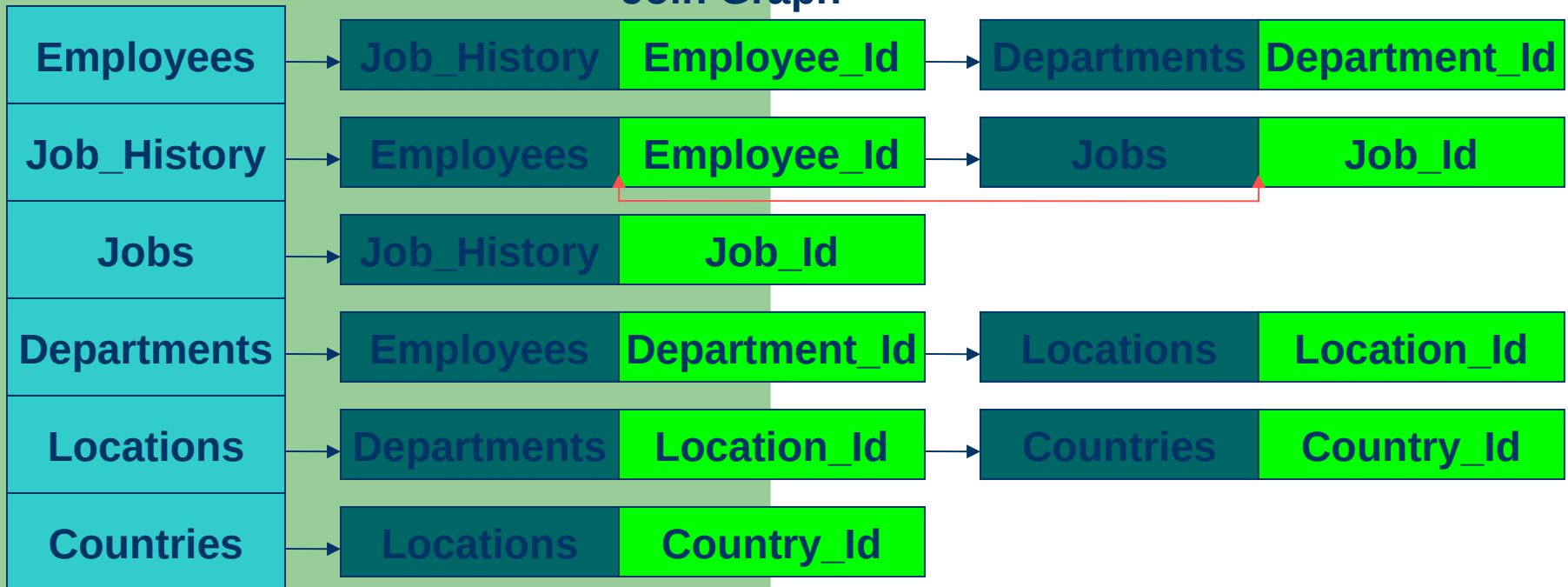
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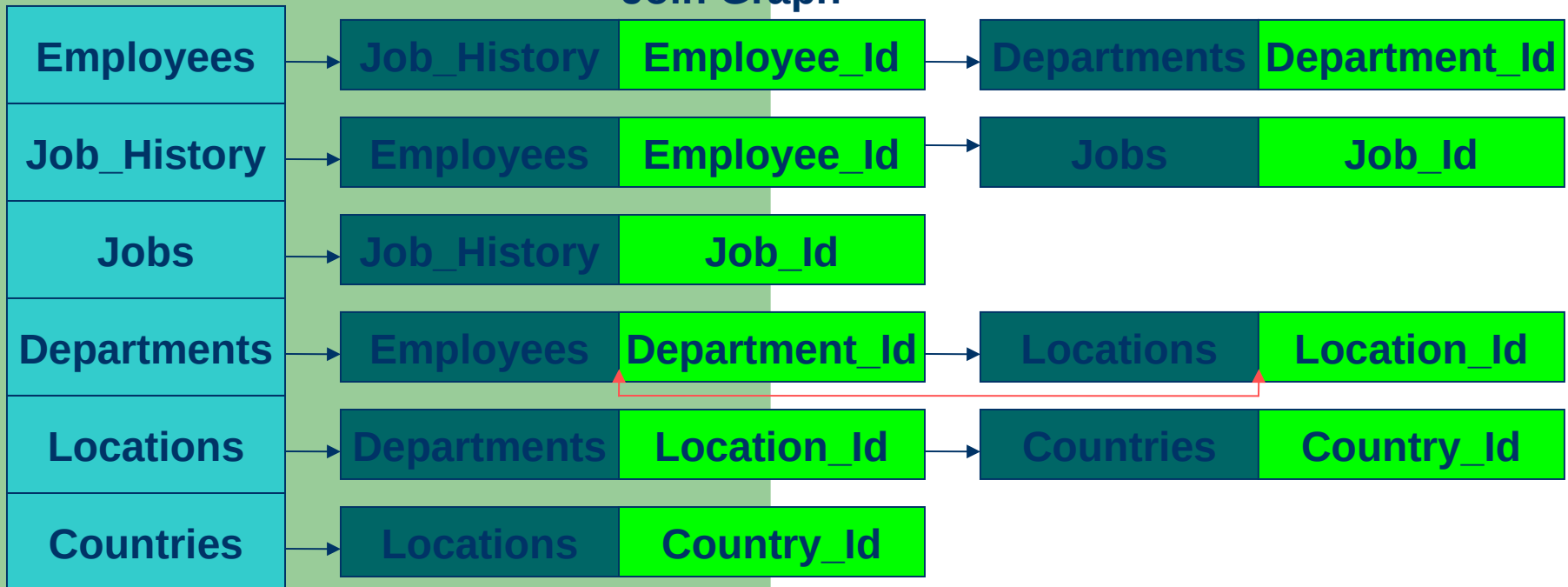
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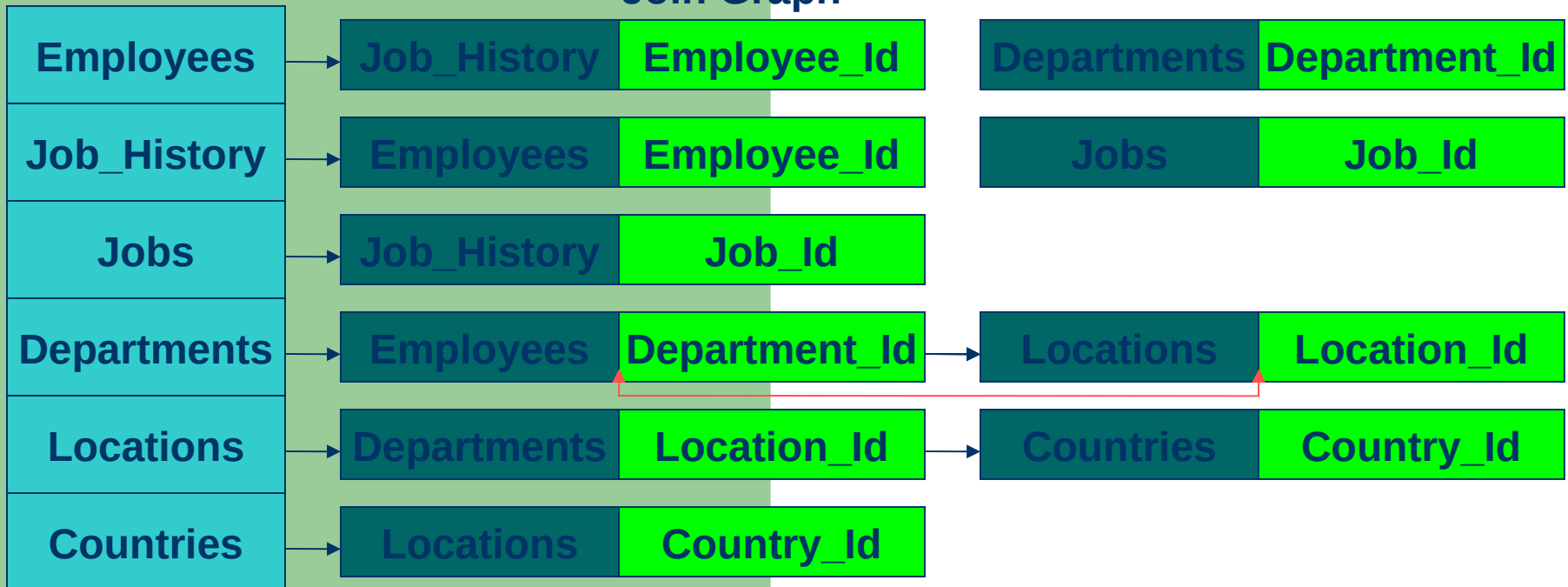
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Job_History

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Join Base Tables

Employees

Job_History

Jobs

Departments

Locations

Countries

Join Graph

Employees

Job_History

Employee_Id

Departments

Department_Id

Job_History

Employees

Employee_Id

Jobs

Job_Id

Jobs

Job_History

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Departments

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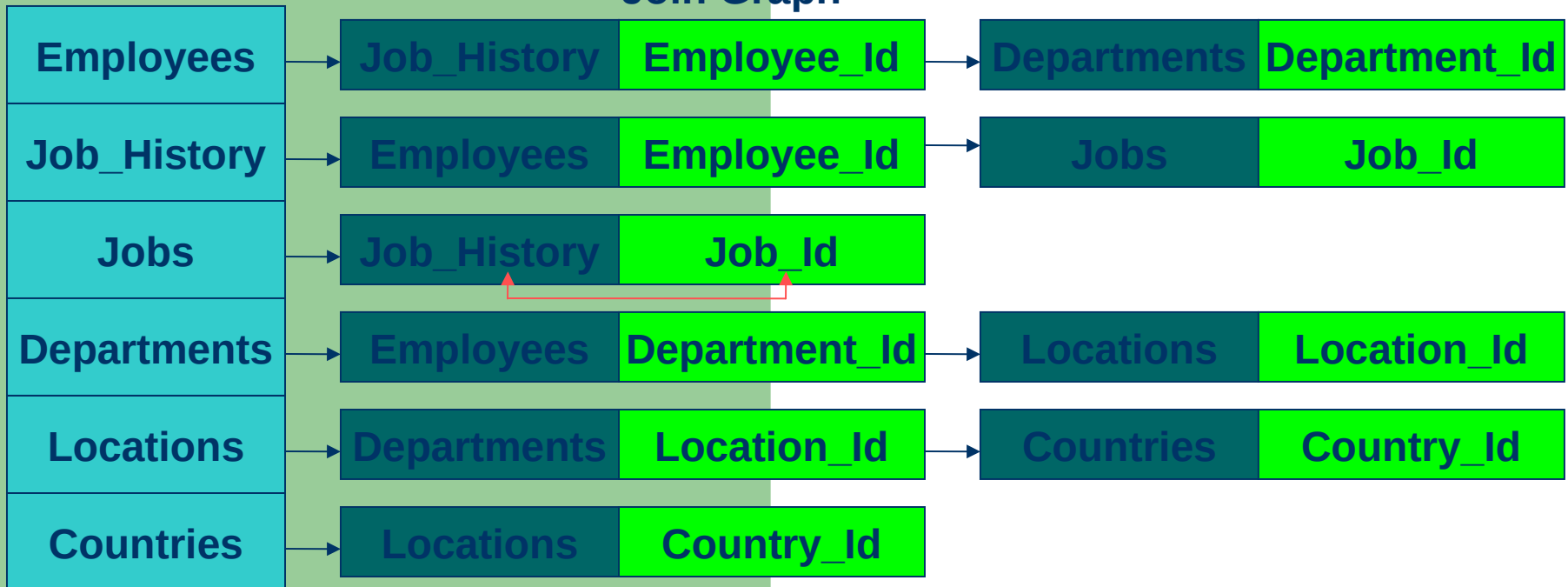
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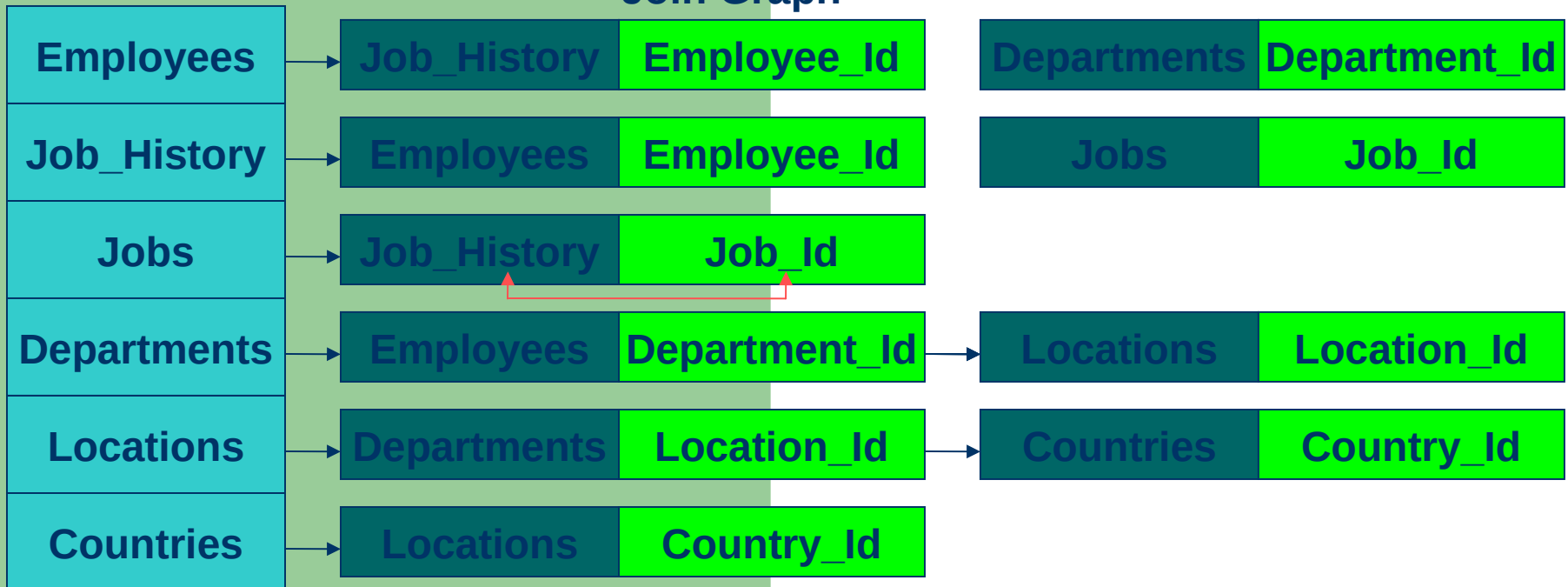
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Employees

Jobs

Job_History

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Join Base Tables

Employees

Job_History

Jobs

Departments

Locations

Countries

Join Graph

Employees

Job_History

Employee_Id

Departments

Department_Id

Job_History

Employees

Employee_Id

Jobs

Job_Id

Jobs

Job_History

Job_Id

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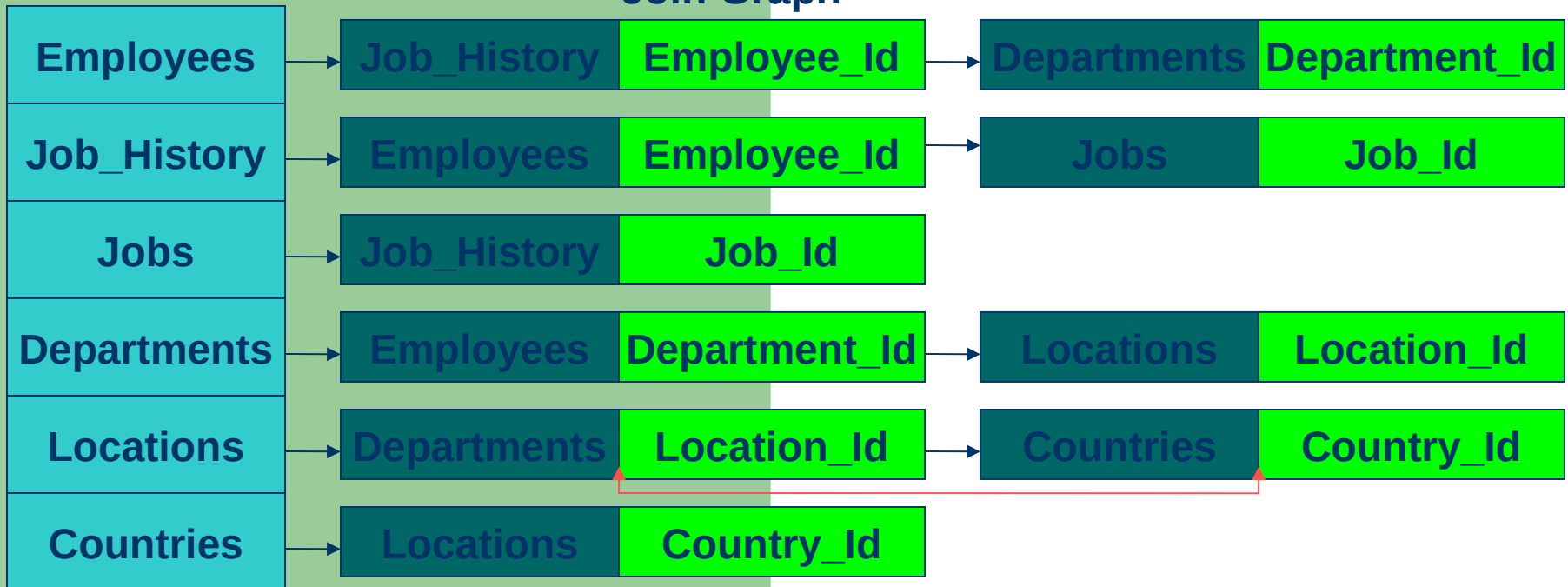
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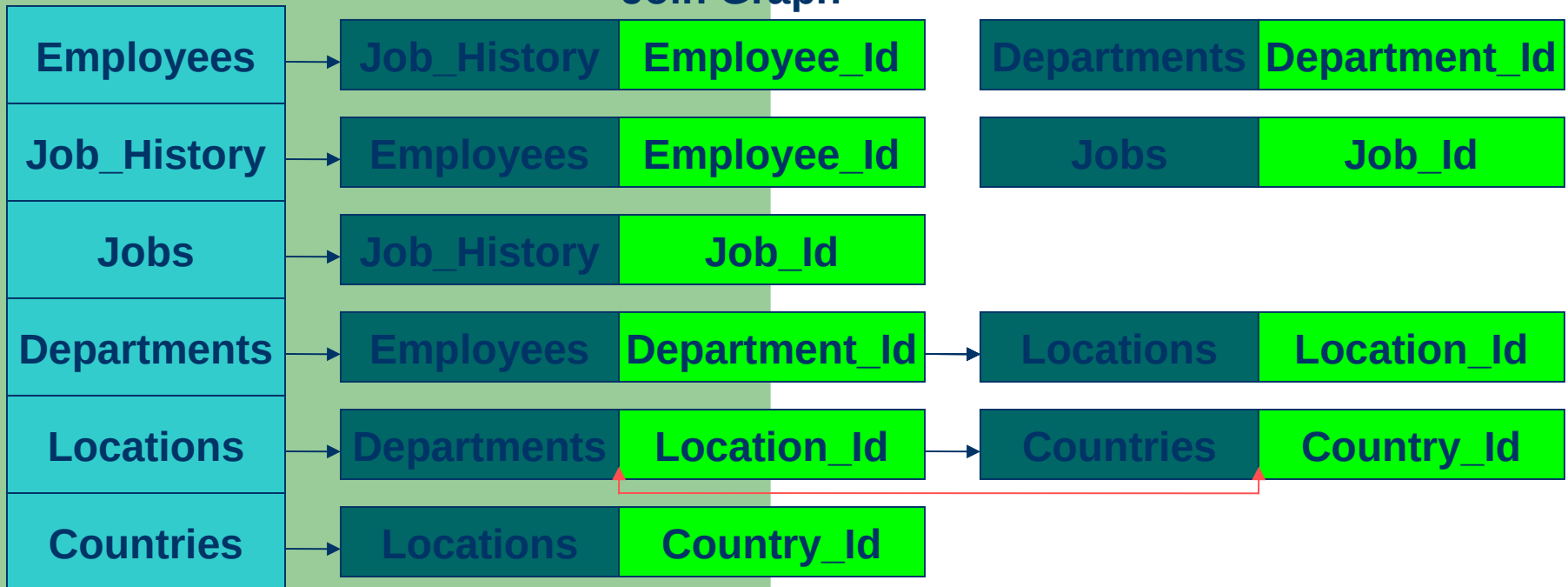
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Join Base Tables

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Job_History

Jobs

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Locations

Countries

Join Graph

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Job_History

Employee_Id

Departments

Department_Id

Job_History

Employees

Employee_Id

Jobs

Job_Id

Jobs

Job_History

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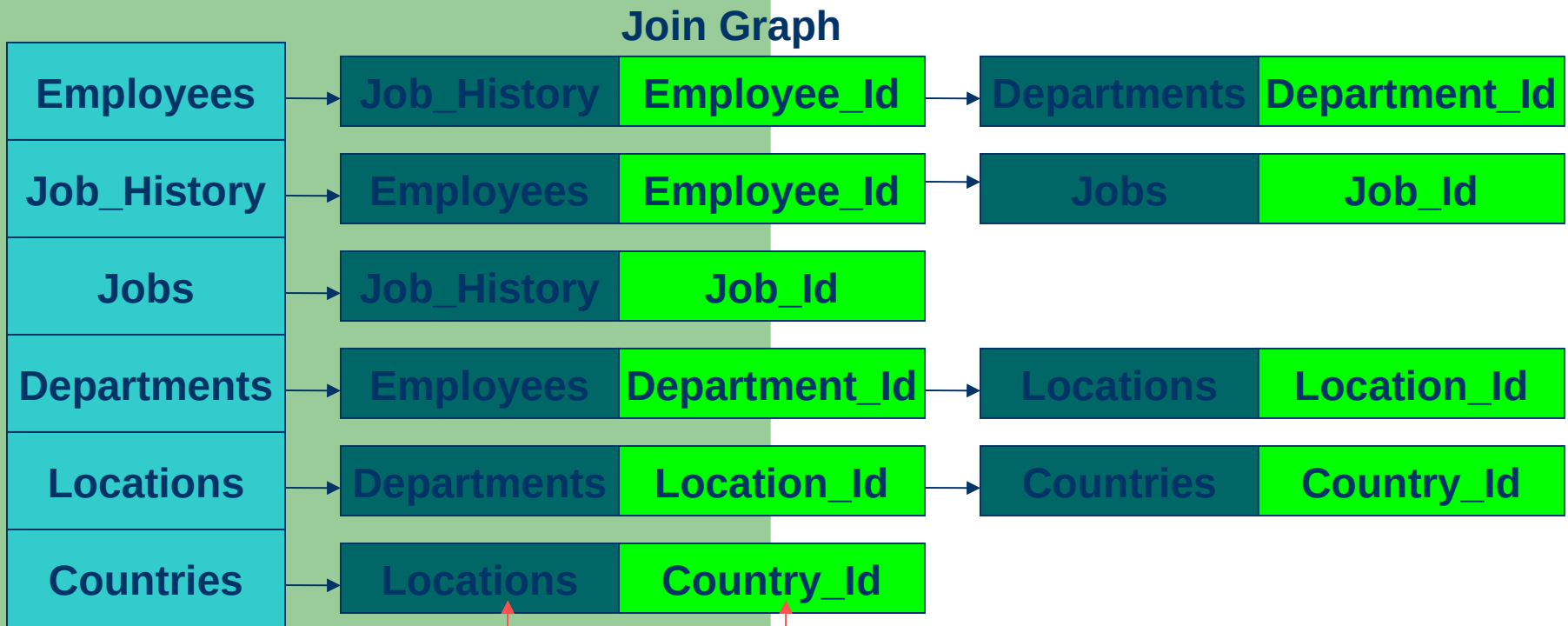
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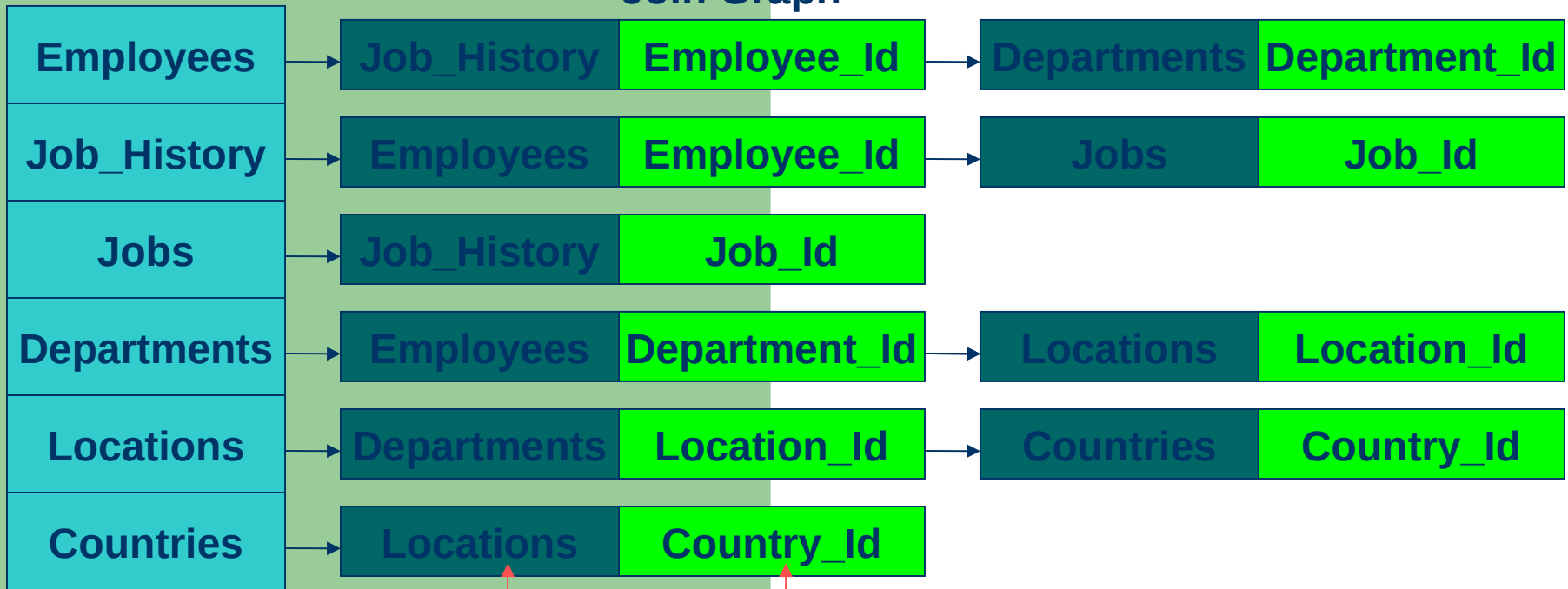
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Join Base Tables

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Job_History

Jobs

Departments

Locations

Countries

Join Graph

Employees

Job_History

Employee_Id

Departments

Department_Id

Job_History

Employees

Employee_Id

Jobs

Job_Id

Jobs

Job_History

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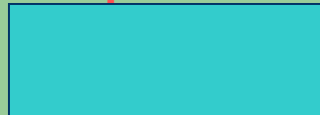
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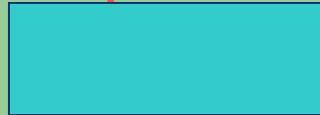
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path



vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

→ insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

path

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries



insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

→ insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path



Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

insert all the names of base tables from path as vertexes in JoinPathList

create a local buffer buf

insert into buf the first entry from path



for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

Employees

Job_History

Departments

Jobs

Locations

Countries

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do



take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path

Employees

Job_History

Departments

Jobs

Locations

Countries



vertexes



insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time



$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

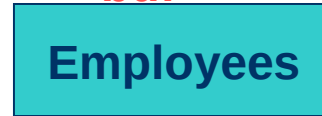
$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

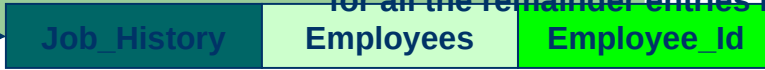
buf



path



vertexes



insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

JoinPathAdjacentList(T_i) = $T_{[buf]}$

Key(T_i) = getFirstAdjacentListKey(T_i , $T_{[buf]}$)

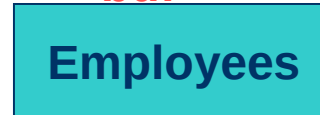
JoinPathAdjacentList($T_{[buf]}$) = T_i

Key($T_{[buf]}$) = getFirstAdjacentListKey($T_{[buf]}$, T_i)

$T_{[buf]} += T_i$

Insert NodeList[$T_{[buf]}$] = $T_{[buf]}$

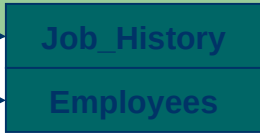
buf



path



vertexes



Employees

Employee_Id

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

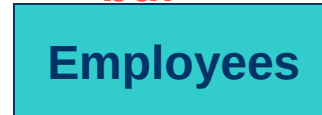
$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

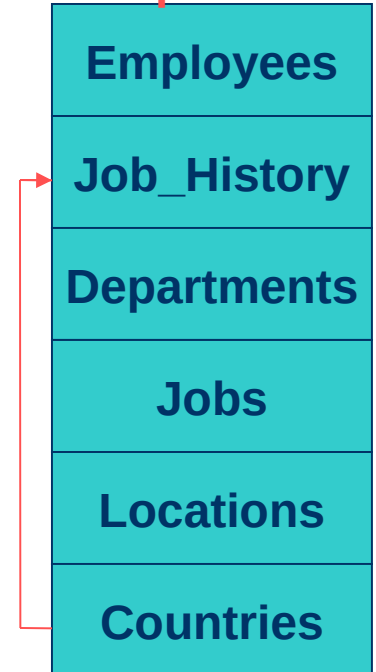
$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$



buf



path



vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

→ $\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

→ $\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

→ $T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id

vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id

for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History

Job_History
Employees
Employees Job_History

Employees
Job_History

Employee_Id
Employee_Id

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees
Job_History
Deparments
Jobs
Locations
Countries
Employees Job_History

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History	Departments	Department_Id

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees

Job_History

Departments

Jobs

Locations

Countries

Employees
Job_History

Job_History

Employees

Employees
Job_History

Employees

Job_History

Departments

Employee_Id

Employee_Id

Department_Id

Departments

Employees
Job_History

Employees

Job_History

Departments

Jobs

Locations

Countries

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
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for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

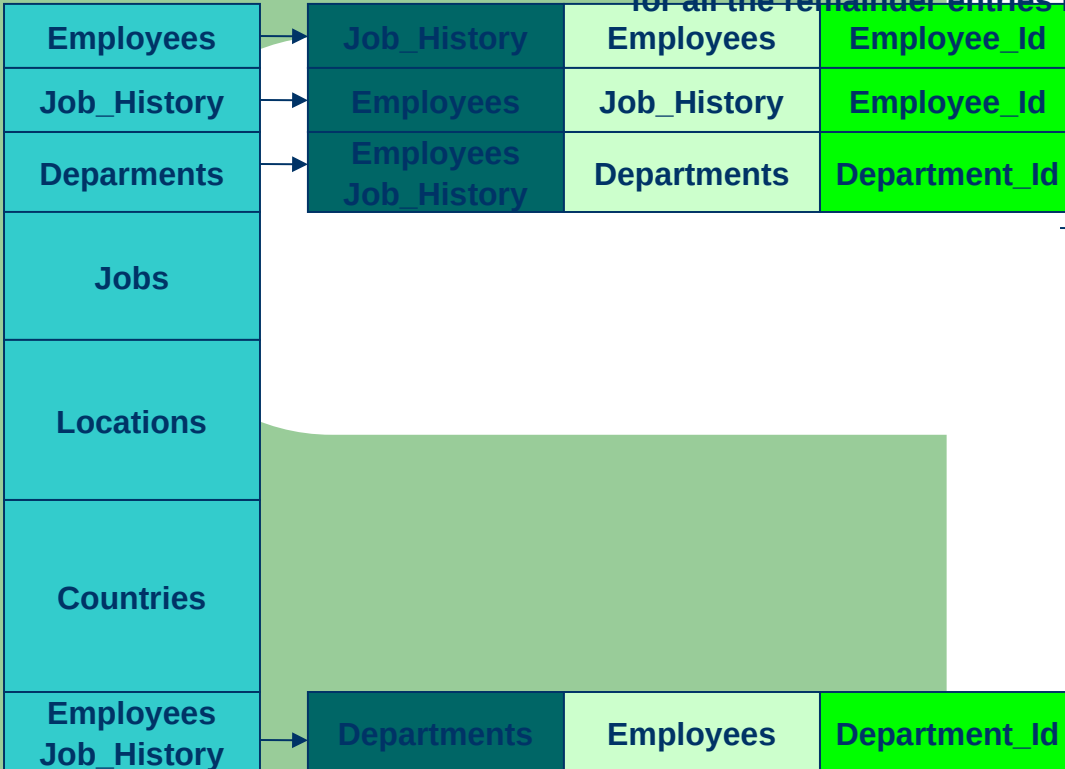
$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History

path

Employees
Job_History
Departments
Jobs
Locations
Countries



vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

→ $\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

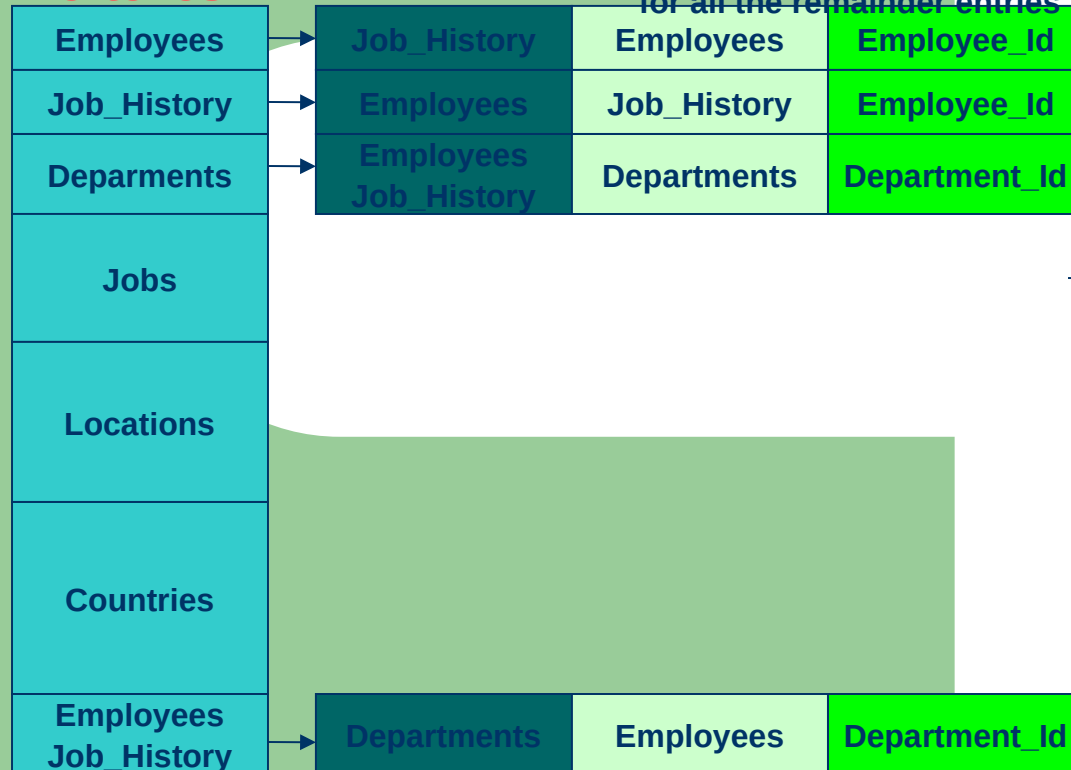
$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries



vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
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for all the remainder entries in path do

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$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

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$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

→ $T_{[\text{buf}]} += T_i$

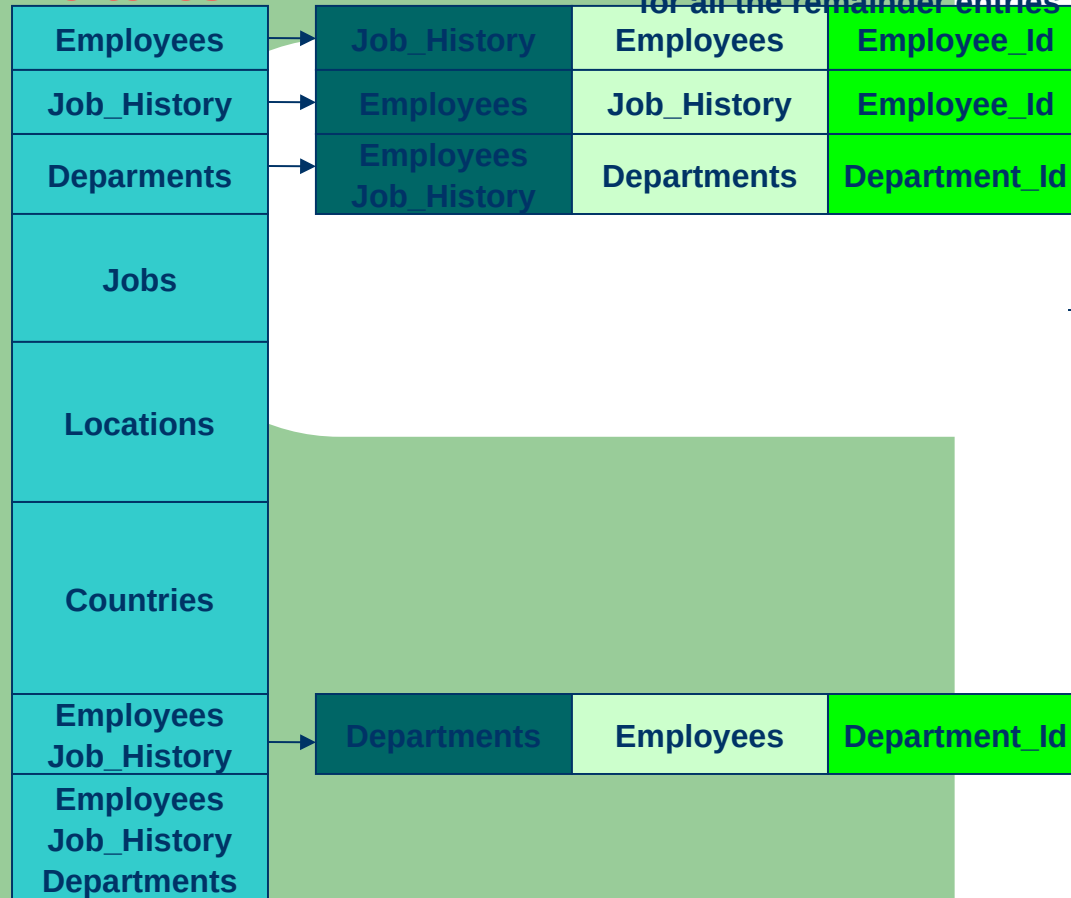
$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History
Departments

path

Employees
Job_History
Departments
Jobs
Locations
Countries



vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
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for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History
Employees Job_History Departments

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History	Departments	Department_Id

Departments	Employees	Department_Id
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Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

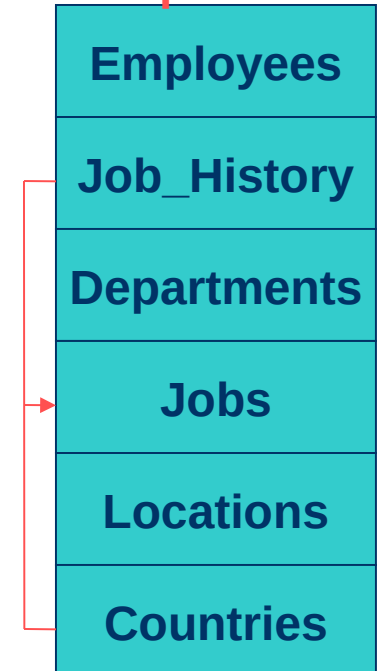
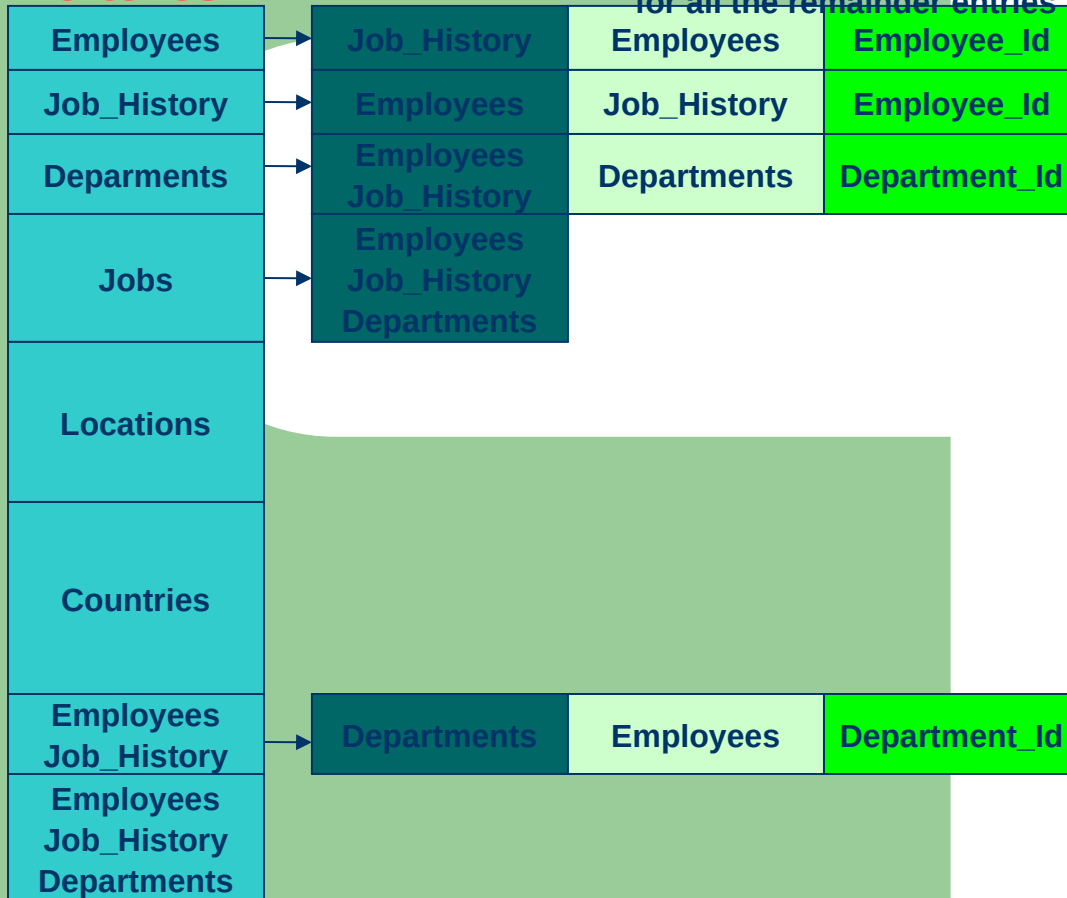
$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path



vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries



Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History	Departments	Department_Id
Employees Job_History Departments	Jobs	Job_Id

Departments	Employees	Department_Id
-------------	-----------	---------------

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History
Employees Job_History Departments

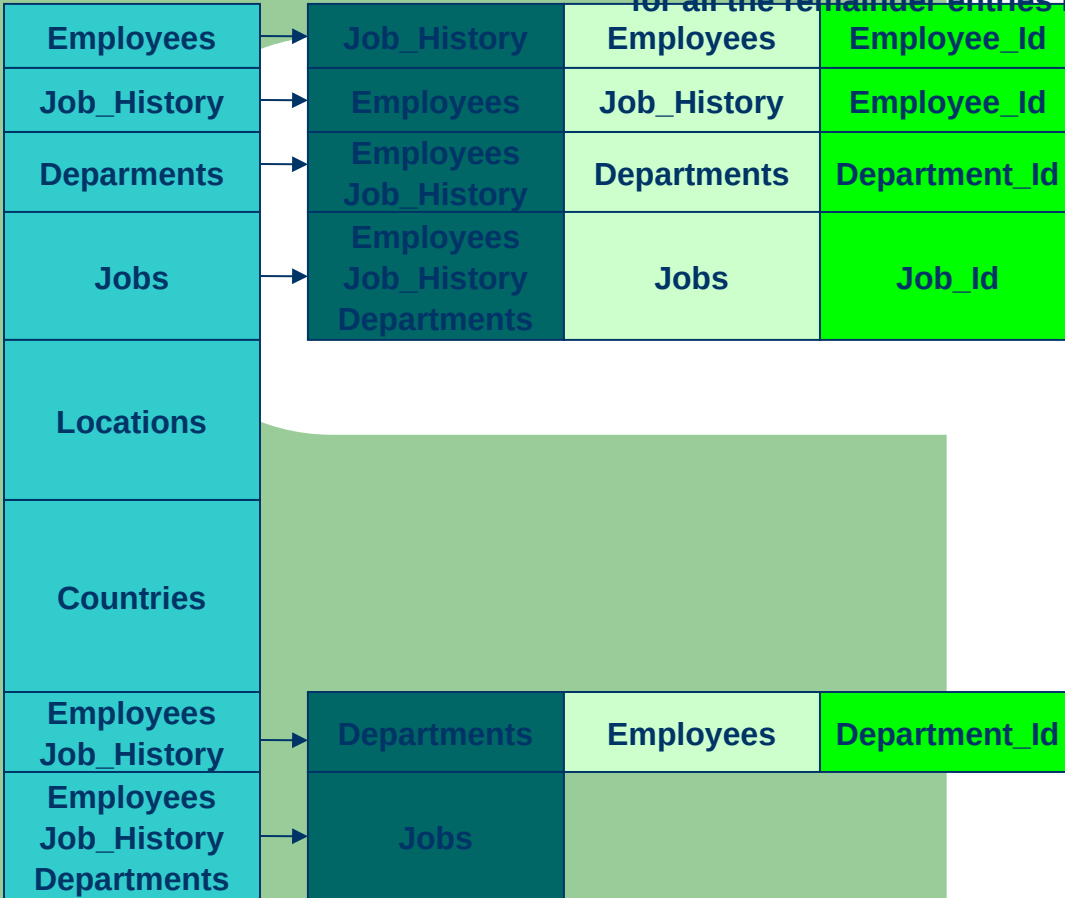
vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time
 $\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$
 $\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$
 $\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$
 $\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$
 $T_{[\text{buf}]} += T_i$
 $\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path



Employees
Job_History
Departments

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History	Departments	Department_Id
Employees Job_History Departments	Jobs	Job_Id



Departments	Employees	Department_Id
Jobs	Job_History	Job_Id

buf

Employees
Job_History
Departments

path

Employees
Job_History
Departments
Jobs
Locations
Countries



vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

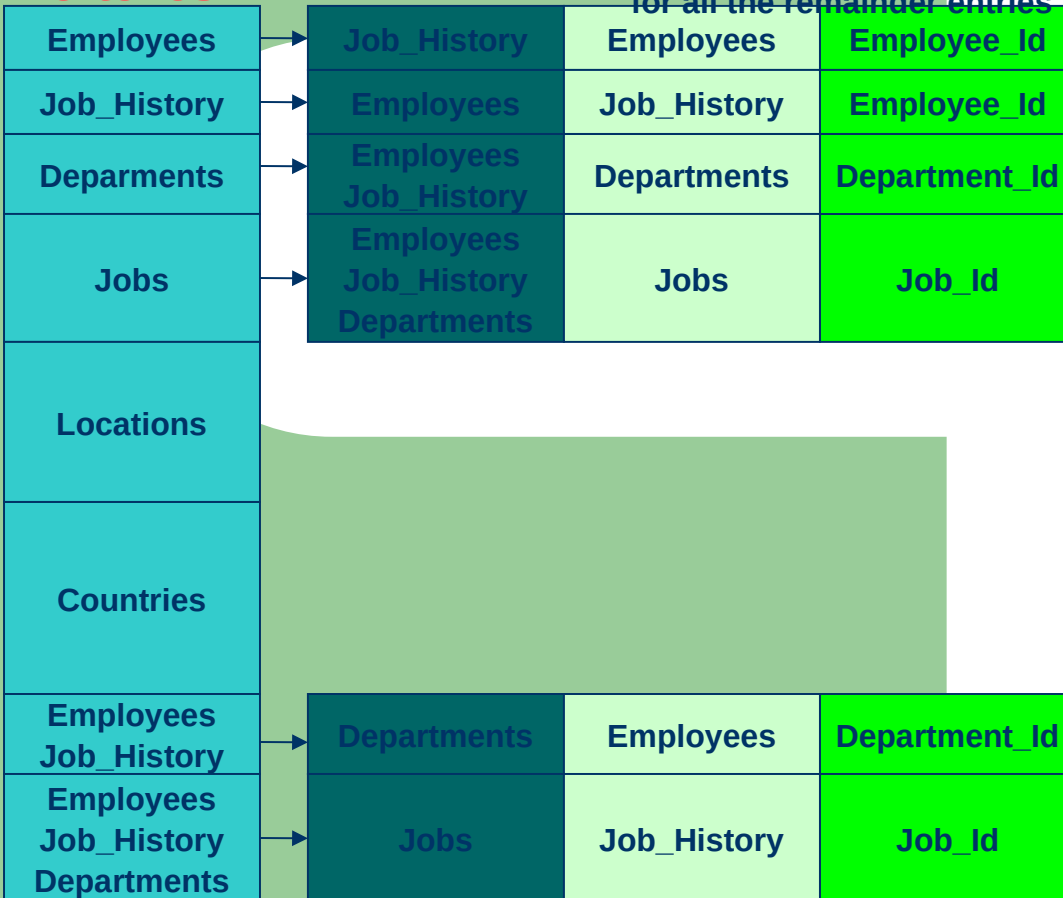
$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs

Employees
Job_History
Departments
Jobs
Locations
Countries



insert all the names of base tables from path as vertexes in JoinPathList
 create a local buffer buf
 insert into buf the first entry from path
 for all the remainder entries in path do

take one T_i at a time
 $\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$
 $\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$
 $\text{JoinPathAdjacentList}(T_{[\text{buf}]}) = T_i$
 $\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$
 $T_{[\text{buf}]} += T_i$
 $\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

vertexes

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id

Locations			
Countries			
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs			

buf

Employees
Job_History
Departments
Jobs

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

insert all the names of base tables from path as vertexes in JoinPathList
create a local buffer buf
insert into buf the first entry from path
for all the remainder entries in path do

take one T_i at a time

$\text{JoinPathAdjacentList}(T_i) = T_{[\text{buf}]}$

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$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

Employees
Job_History
Departments
Jobs

path

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History
Employees Job_History Departments
Employees Job_History Departments Jobs

Job_History	Employees	Employee_Id
Employees	Job_History	Employee_Id
Employees Job_History	Departments	Department_Id
Employees Job_History Departments	Jobs	Job_Id

Departments	Employees	Department_Id
Jobs	Job_History	Job_Id

vertexes

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buf

Employees
Job_History
Departments
Jobs

path

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees
Job_History
Departments
Jobs
Locations
Countries
Employees Job_History
Employees Job_History Departments
Employees Job_History Departments Jobs

Job_History
Employees
Employees Job_History
Employees Job_History Departments
Employees Job_History Departments Jobs

Departments
Jobs
Employees
Job_History

Employees
Job_History
Departments
Jobs

Employee_Id
Employee_Id
Department_Id
Job_Id

Department_Id
Job_Id

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buf

path

Employees
Job_History
Departments
Jobs

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries			
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs			

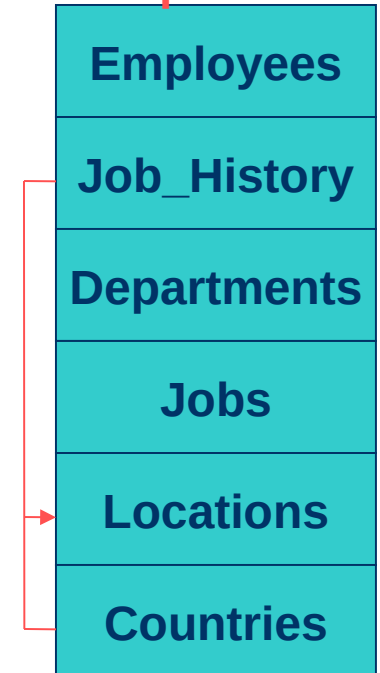
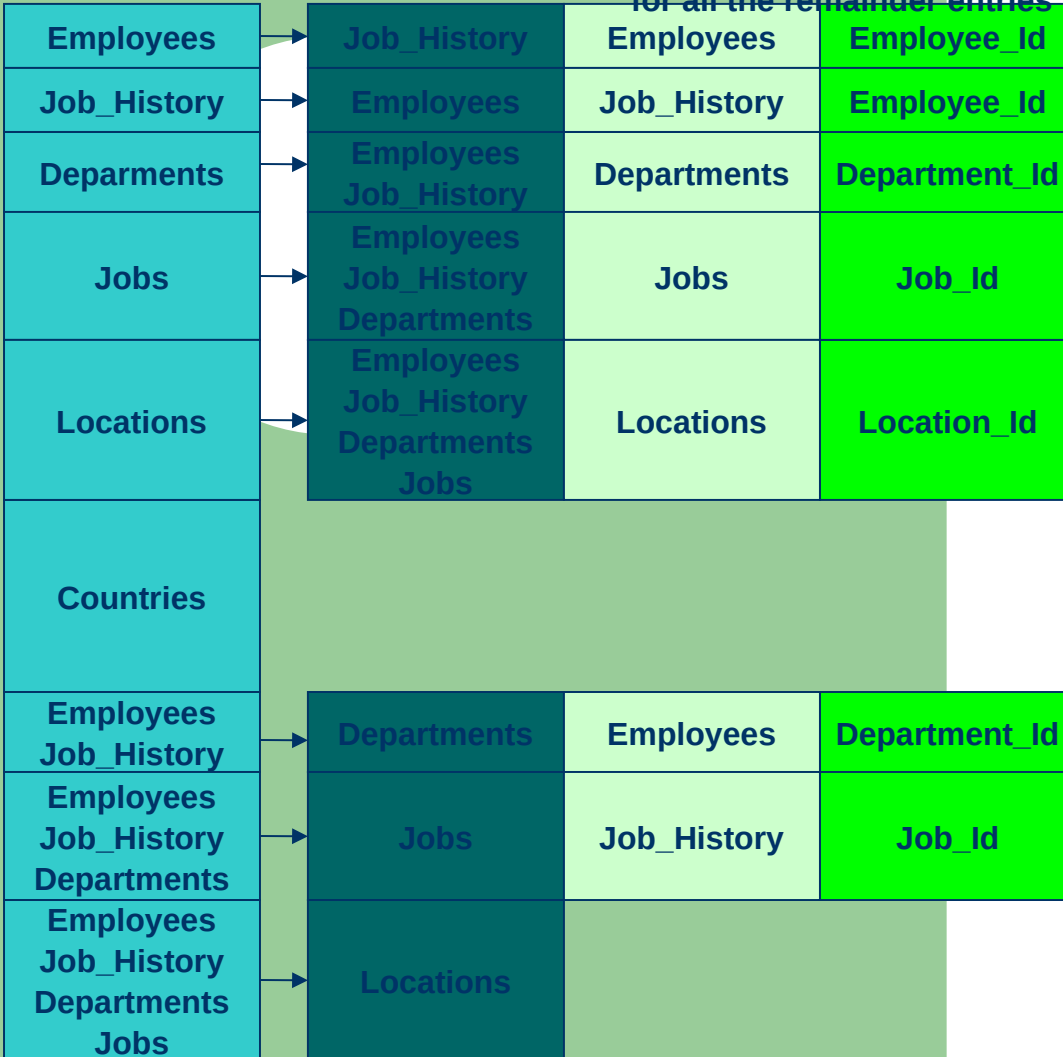
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buf

path



vertexes

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buf

Employees
Job_History
Departments
Jobs

path

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries			
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id

Countries			
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id

buf

Employees
Job_History
Departments
Jobs
Locations

path

Employees
Job_History
Departments
Jobs
Locations
Countries

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buf

path

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id

Countries

Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id

Employees Job_History Departments Jobs Locations
--

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

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buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries			
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations			

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 $T_{[\text{buf}]} += T_i$
 $\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	Employees Job_History Departments Jobs Locations		
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations			

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 $T_{[\text{buf}]} += T_i$
 $\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations			

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 $\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	Countries		

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 $T_{[\text{buf}]} += T_i$
 $\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

buf

path

Employees
Job_History
Departments
Jobs
Locations

Employees
Job_History
Departments
Jobs
Locations
Countries

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	Countries	Locations	Country_Id

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	Countries	Locations	Country_Id

buf

Employees
Job_History
Departments
Jobs
Locations
Countries

path

Employees
Job_History
Departments
Jobs
Locations
Countries

vertexes

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$T_{[\text{buf}]} += T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

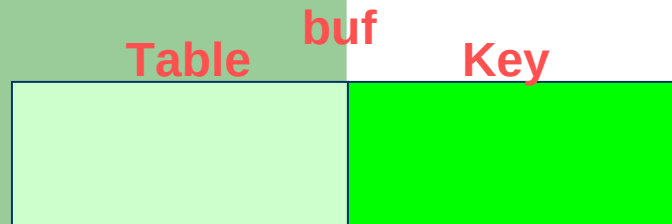


Employees	Job_History	Employees	Employee_Id
Job_History	Employees	Job_History	Employee_Id
Departments	Employees Job_History	Departments	Department_Id
Jobs	Employees Job_History Departments	Jobs	Job_Id
Locations	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	Departments	Employees	Department_Id
Employees Job_History Departments	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	Countries	Locations	Country_Id

Join Path List

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

→ create a structure **buf** with 2 fields: **Table** and **Key**
for all the tables in **JoinPathList** going downward do
 take one $T_{[i]}$ at a time
 for all Base Tables in $T_{[i]}$ do
 take one T_k at a time
 for every **buf.Table** = T_k do
 if (**buf.key** != **Key**($T_{[i]}$)) and (**buf.Key** not in **InheritedKey**($T_{[i]}$)) then
 InheritedKey($T_{[i]}$) += **buf.key**
 if T_i is the table from which comes **Key**($T_{[i]}$) then
 buf.Table = T_i
 buf.key = **Key**($T_{[i]}$)



→ create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

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take one T_k at a time

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buf.key = Key($T_{[i]}$)

Join Path List

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

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Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

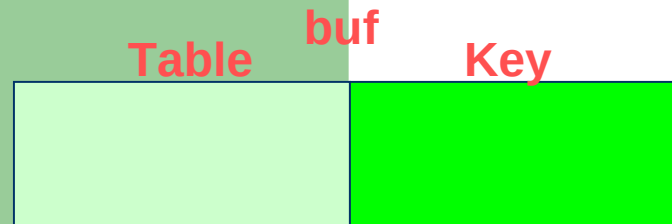
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create a structure buf with 2 fields: Table and Key
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for all Base Tables in $T_{[i]}$ do

take one T_k at a time

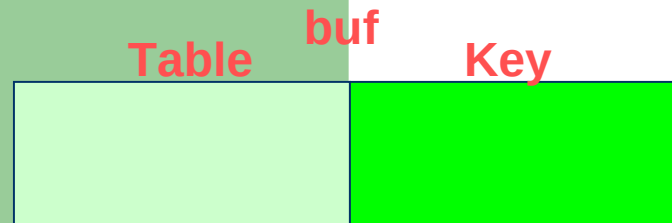
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buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

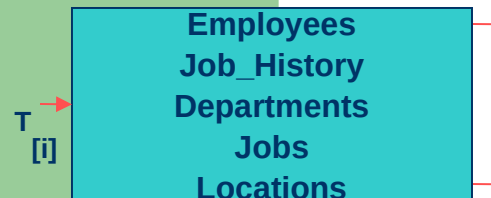
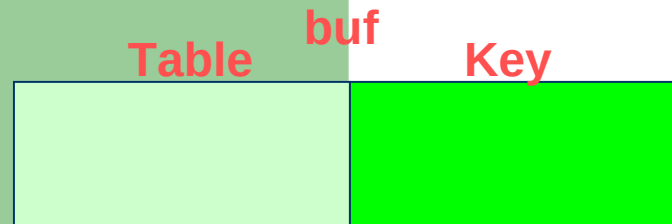
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

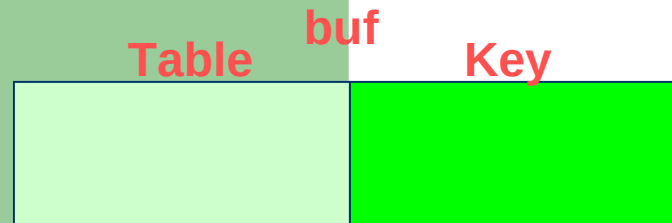
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

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create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

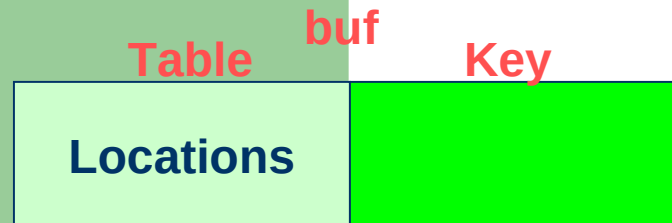
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

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create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

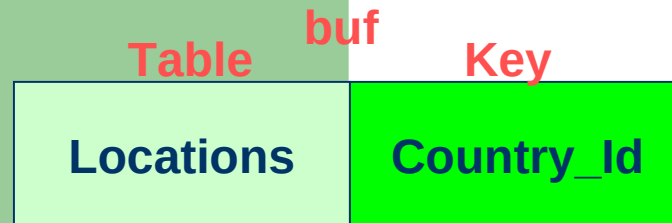
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

→ for all Base Tables in $T_{[i]}$ do

take one T_k at a time

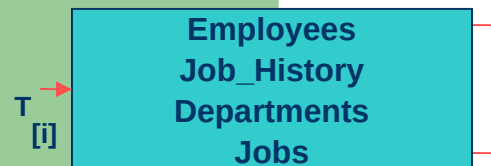
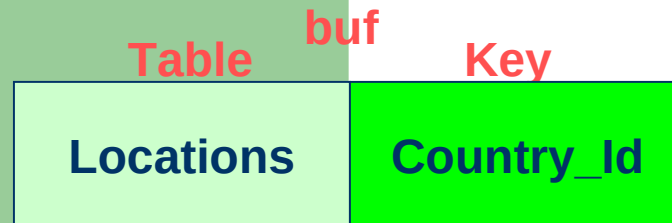
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

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buf.Table = T_i

buf.key = Key($T_{[i]}$)



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

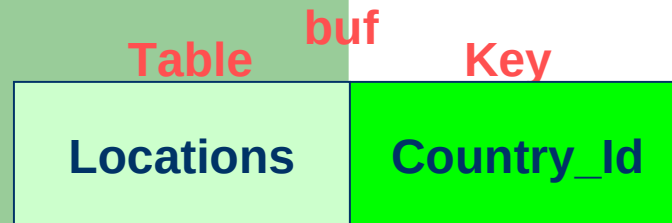
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
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for all Base Tables in $T_{[i]}$ do

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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id
Job_History	→	Employees	Job_History	Employee_Id
Deparments	→	Employees Job_History	Departments	Department_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id
Employees Job_History	→	Departments	Employees	Department_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id
Employees Job_History Departments Jobs Locations Countries				

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

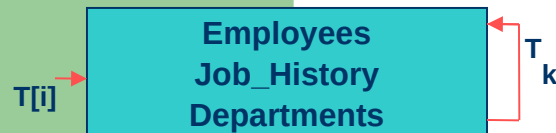
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

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Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

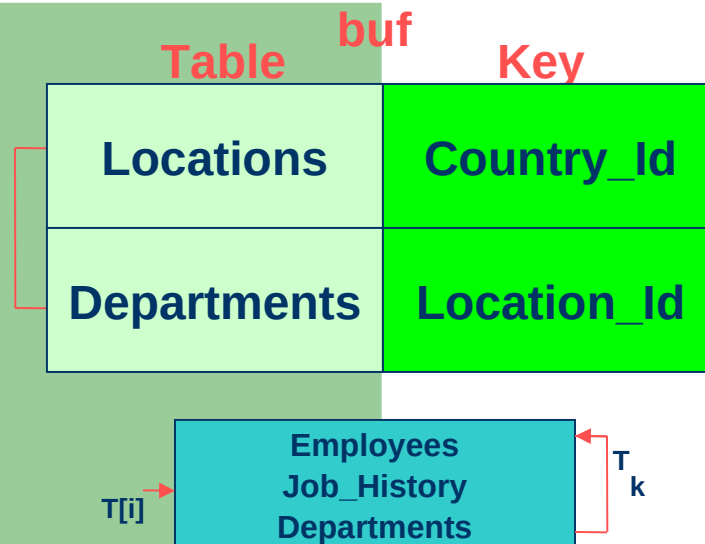
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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for every buf.Table = T_k do

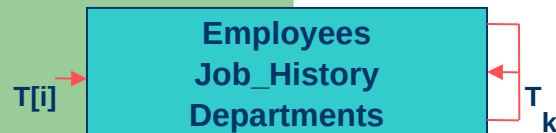
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
 for all the tables in JoinPathList going downward do
 take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

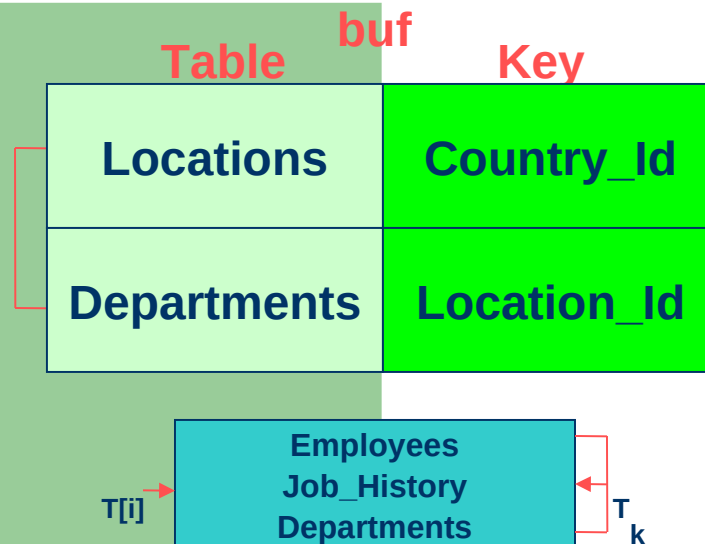
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

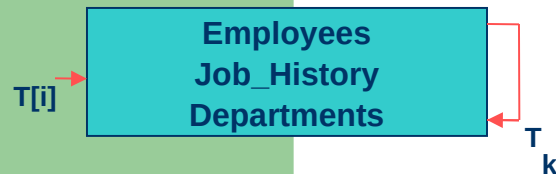
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

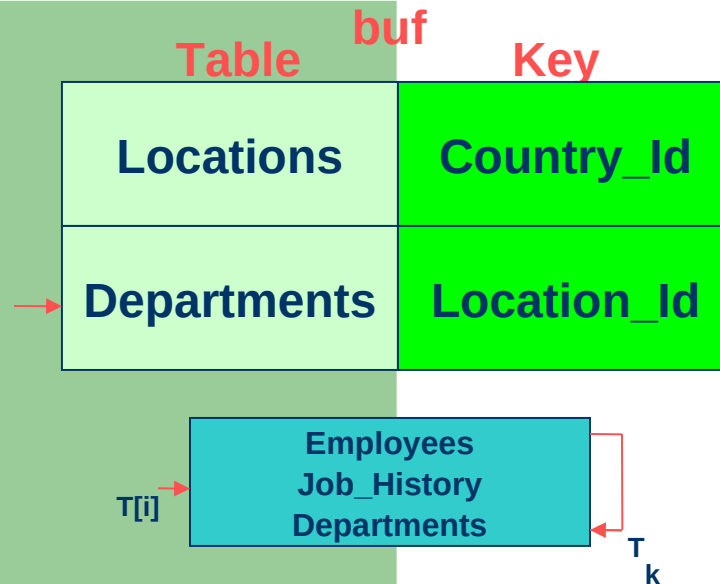
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

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for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

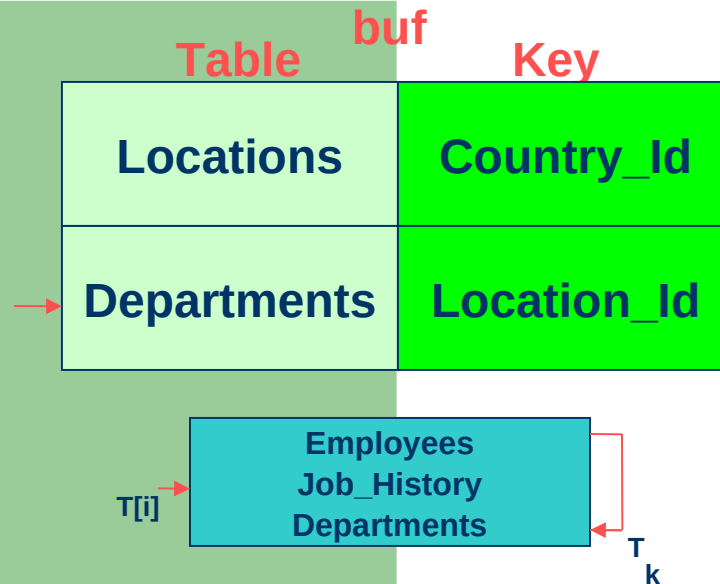
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create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

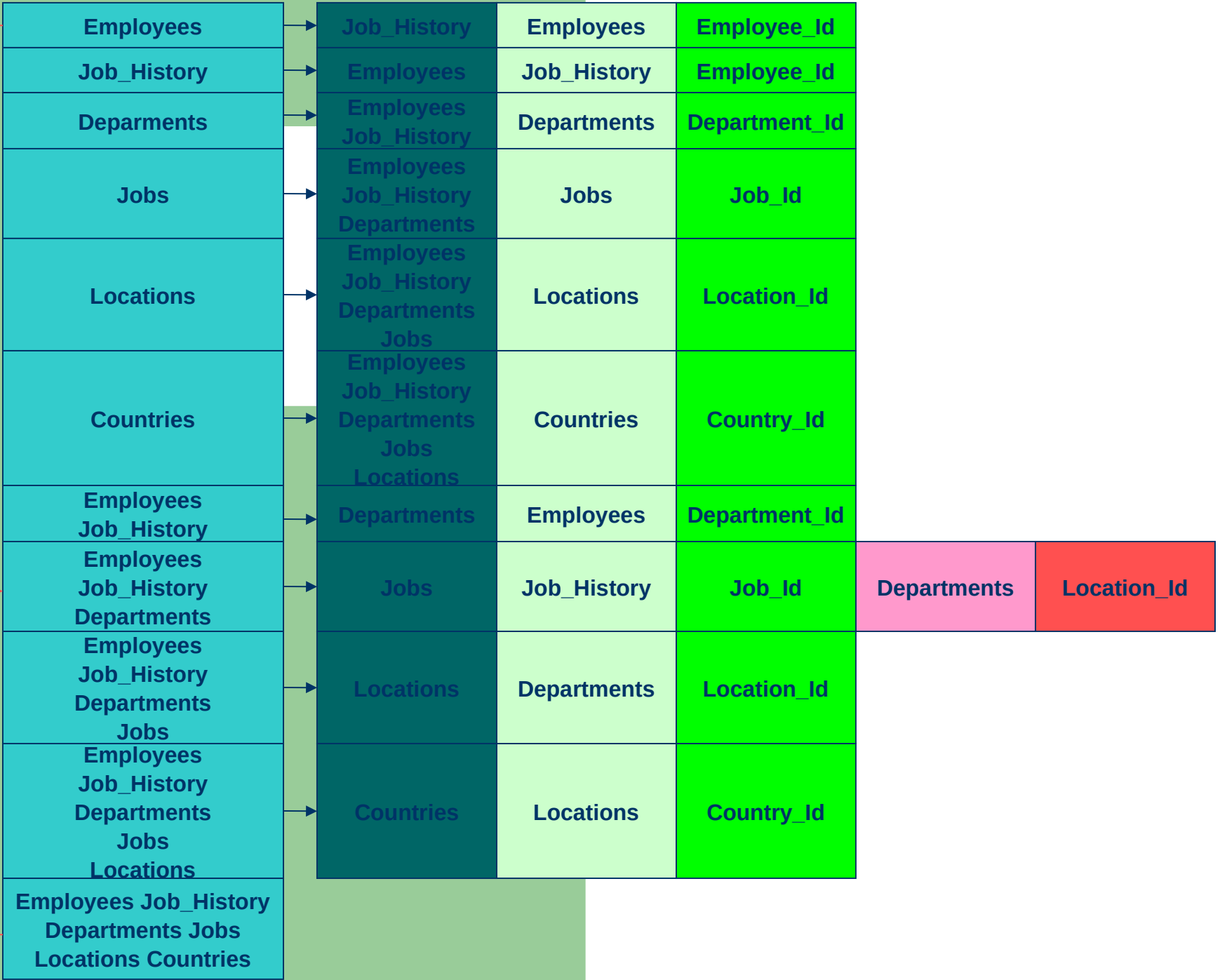
if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

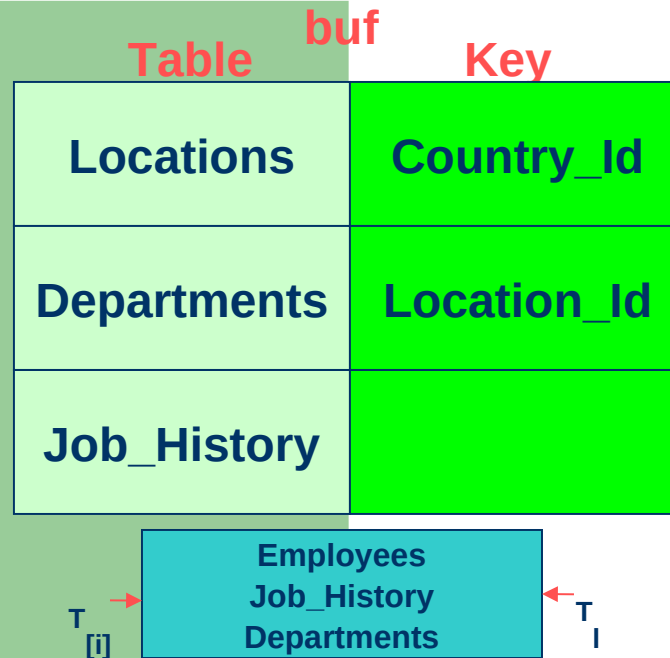
for every buf.Table = T_k do

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for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

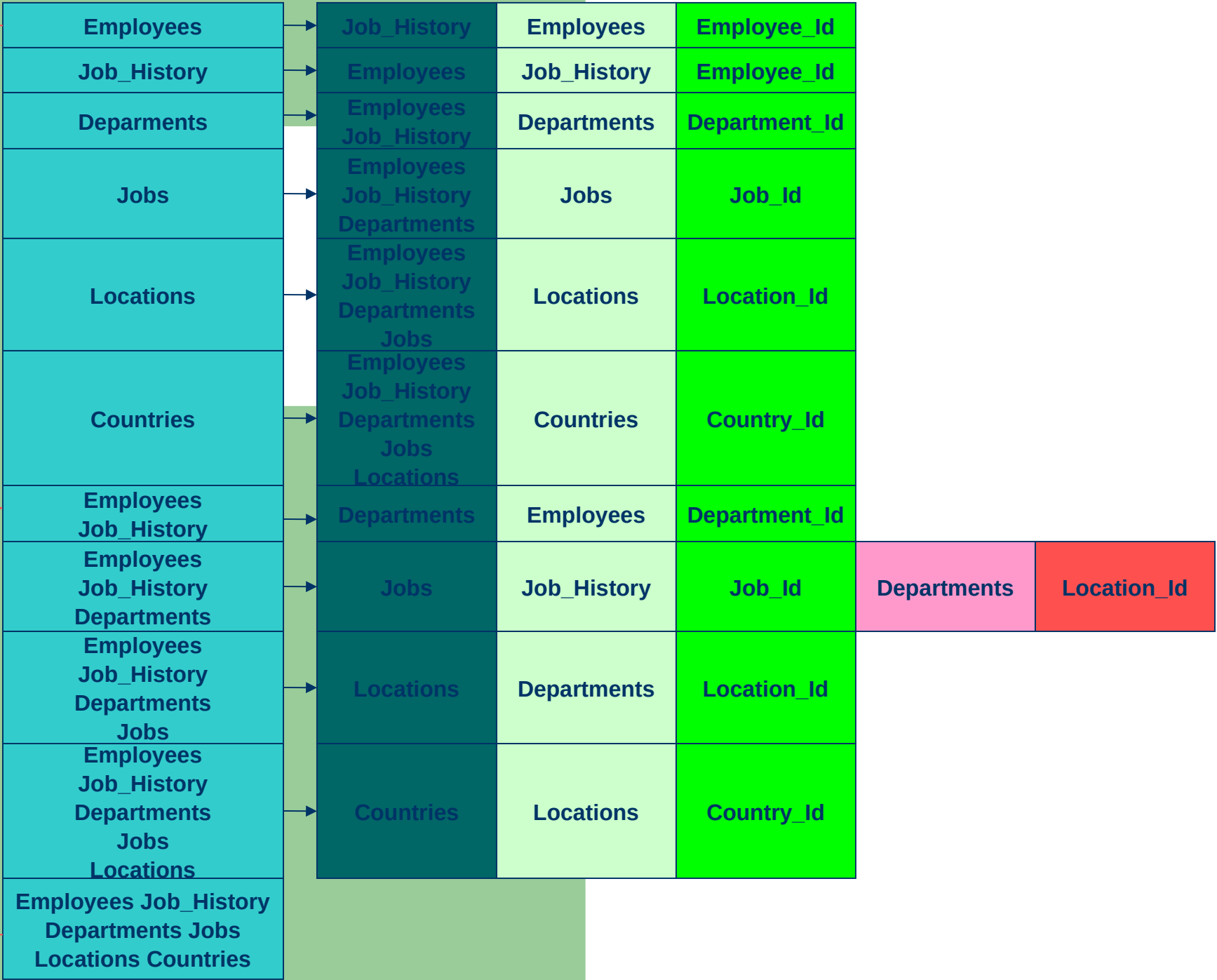
if T_i is the table from which comes Key($T_{[i]}$) then

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buf.key = Key($T_{[i]}$)

Join Path List

[i]



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

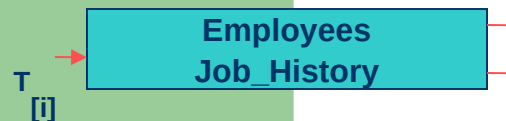
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

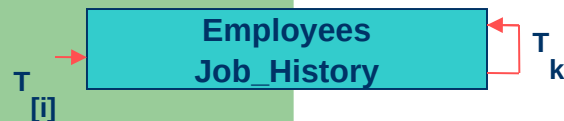
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
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for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



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for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

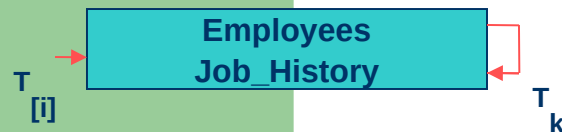
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

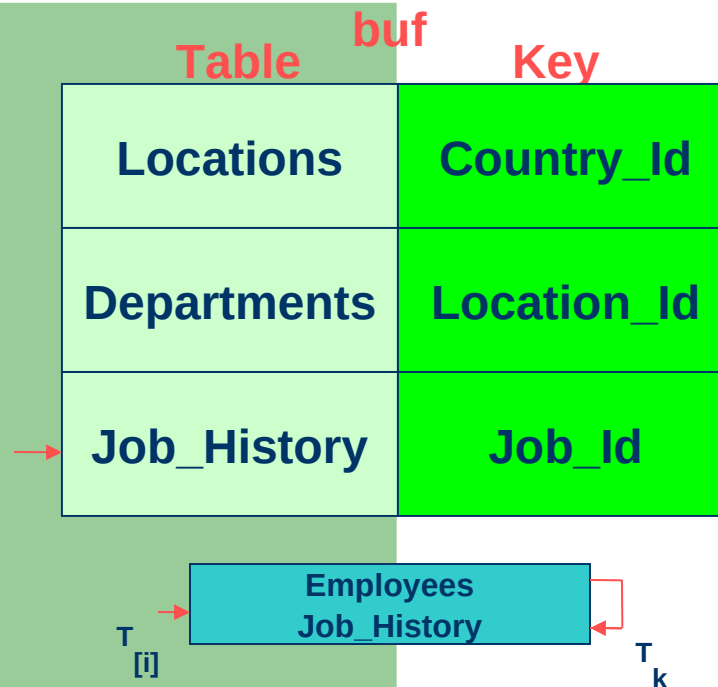
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

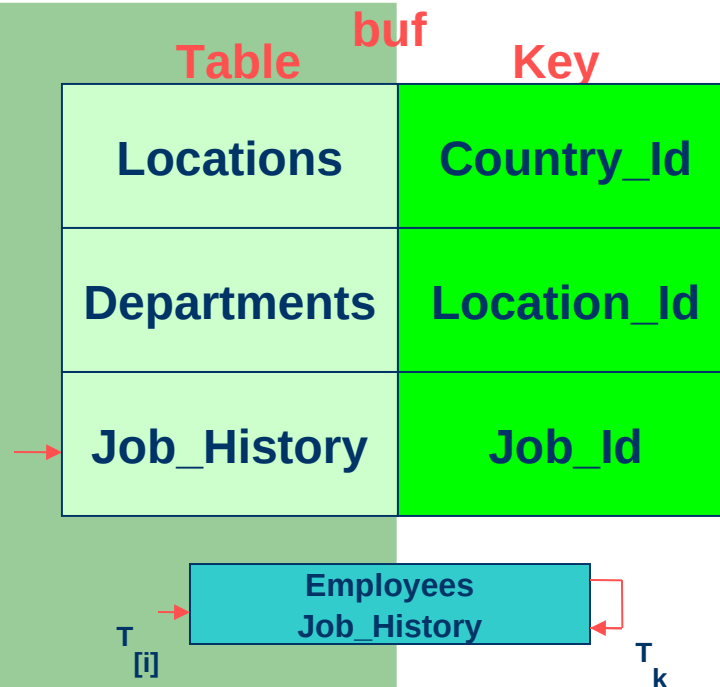
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
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for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

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buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees Job_History	Departments	Department_Id		
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id		
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

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buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do

→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then

InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees Job_History	Departments	Department_Id		
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id		
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id

$T[i]$

Countries

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

→ for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

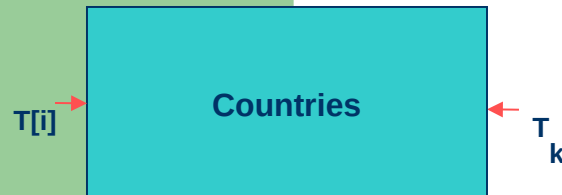
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

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buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id

$T_{[i]}$

Countries

T_k

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id

$T[i]$ →

Countries

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees Job_History	Departments	Department_Id		
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id		
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

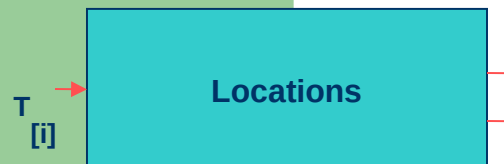
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

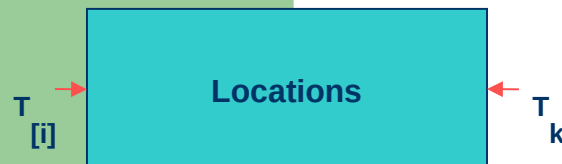
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

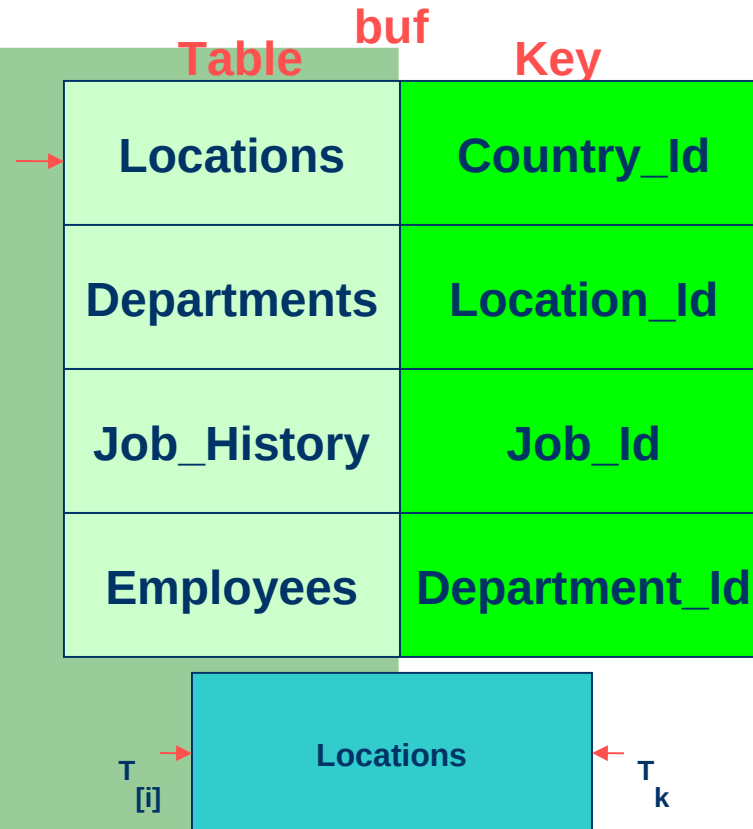
for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

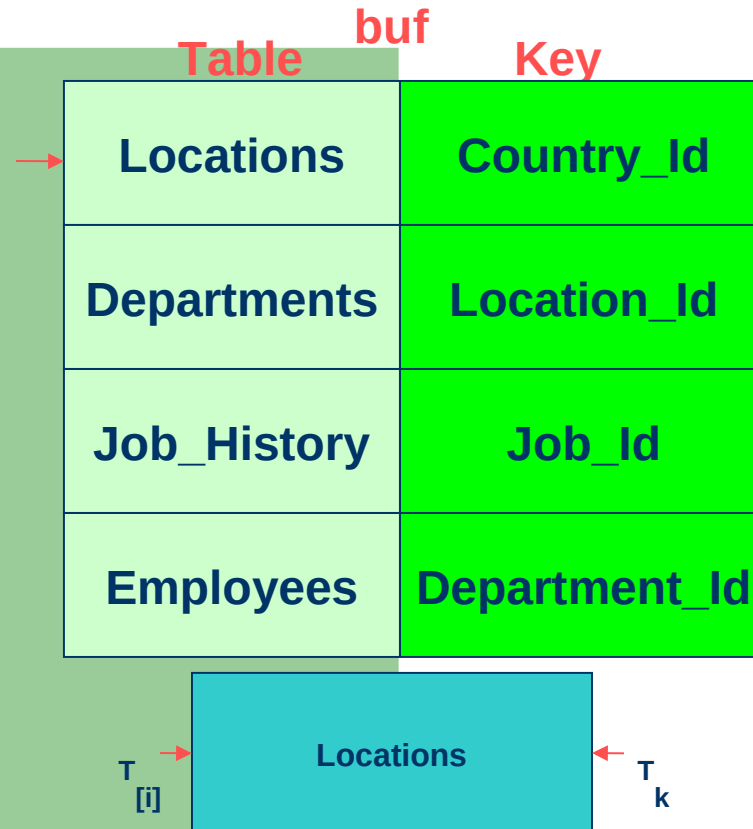
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InheritedKey($T_{[i]}$) += buf.key

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buf.Table = T_i

buf.key = Key($T_{[i]}$)



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

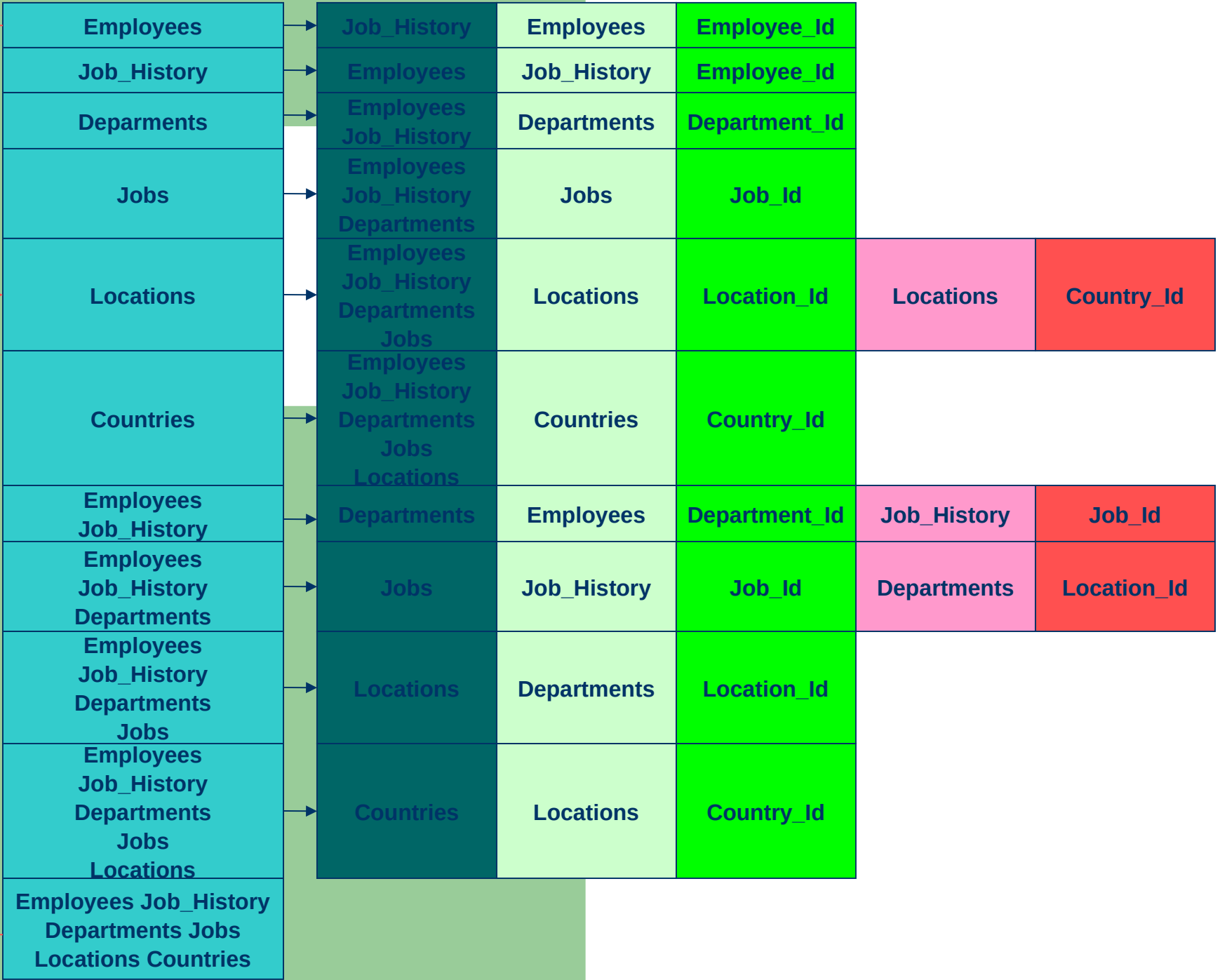
if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Path Join List

T
[i]



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

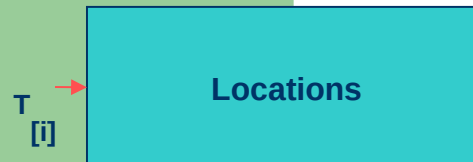
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees Job_History	Departments	Department_Id		
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

→ for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

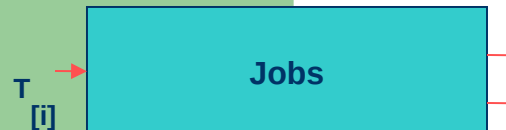
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

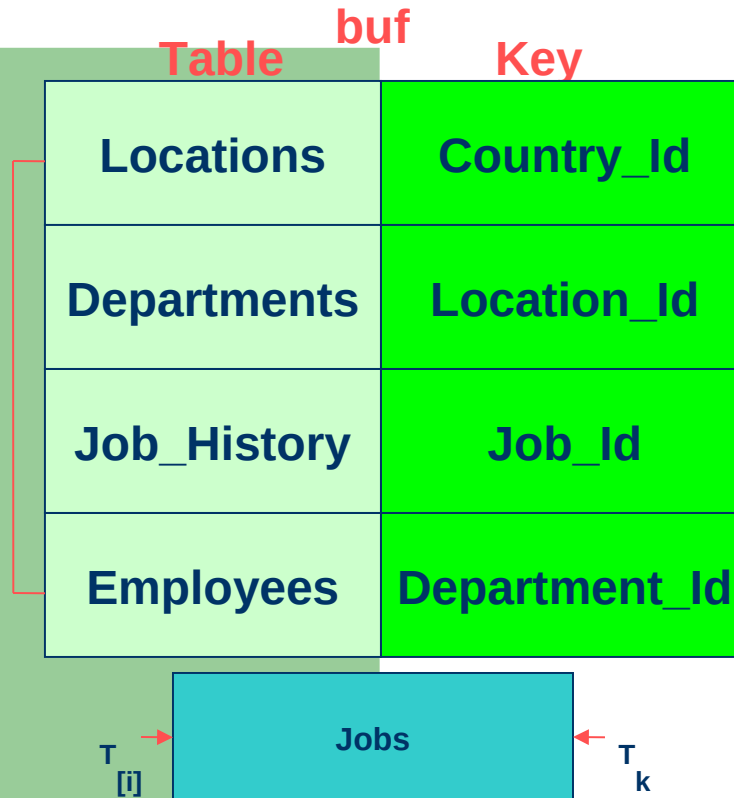
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buf.Table = T_i

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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
→ take one $T_{[i]}$ at a time

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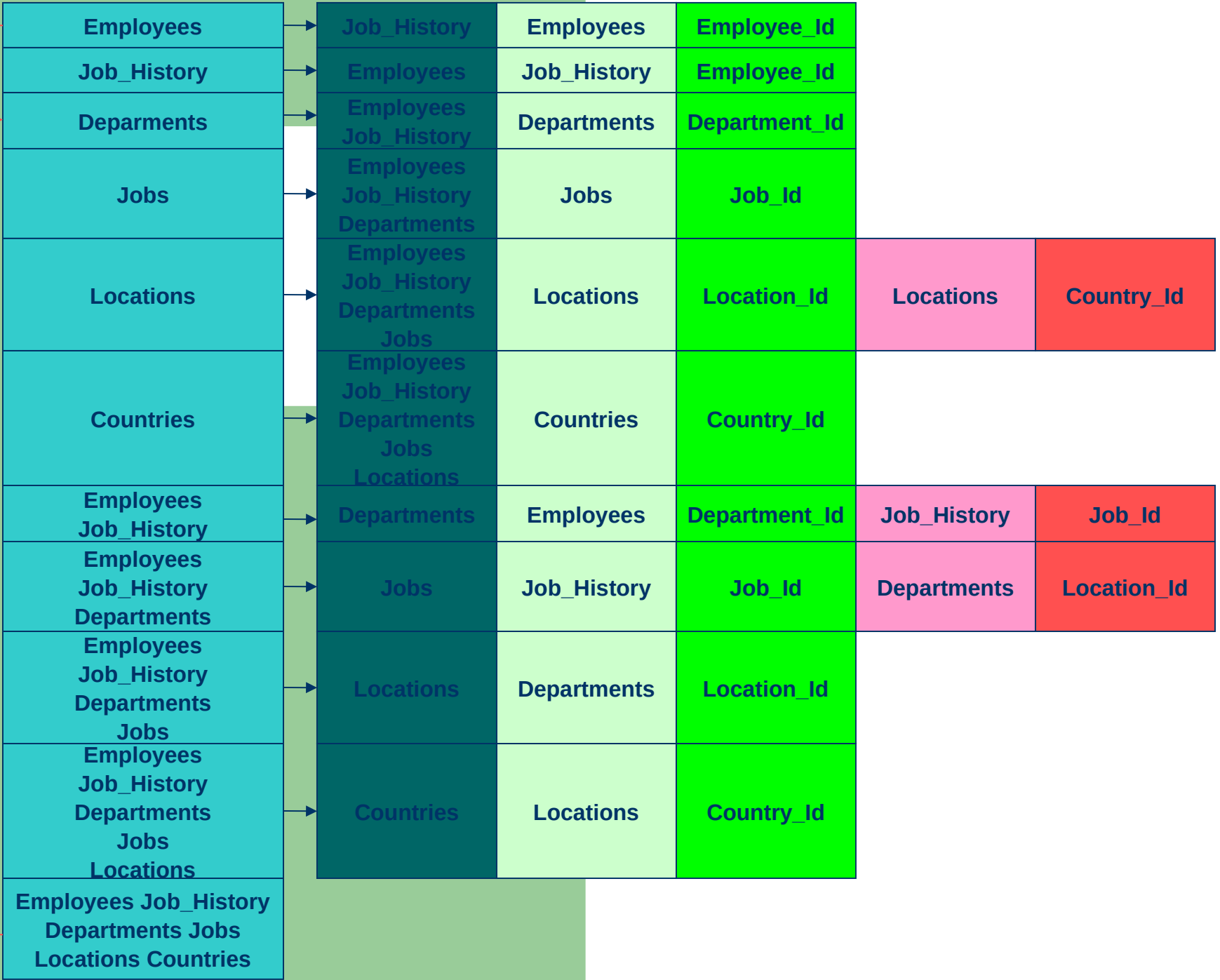
if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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InheritedKey($T_{[i]}$) += buf.key

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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



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take one $T_{[i]}$ at a time

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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



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for all the tables in JoinPathList going downward do
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if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees Job_History	Departments	Department_Id	Departments	Location_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
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take one T_k at a time

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buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
→ take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

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InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id		
Deparments	→	Employees Job_History	Departments	Department_Id	Departments	Location_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

create a structure buf with 2 fields: Table and Key
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buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
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for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

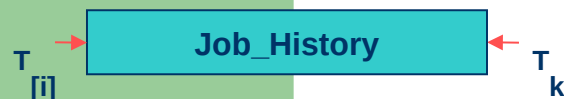
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Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
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take one T_k at a time

for every buf.Table = T_k do

if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

buf.Table = T_i

buf.key = Key($T_{[i]}$)

Table	Key
Locations	Country_Id
Departments	Location_Id
Job_History	Job_Id
Employees	Department_Id



create a structure buf with 2 fields: Table and Key
for all the tables in JoinPathList going downward do
take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

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Join Path List

T
[i]

Employees	→	Job_History	Employees	Employee_Id		
Job_History	→	Employees	Job_History	Employee_Id	Job_History	Job_Id
Deparments	→	Employees Job_History	Departments	Department_Id	Departments	Location_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

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Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries						

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Departments	Location_Id
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Departments	Location_Id
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Join Path List

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[i]

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Job_History	→	Employees	Job_History	Employee_Id	Job_History	Job_Id
Deparments	→	Employees Job_History	Departments	Department_Id	Departments	Location_Id
Jobs	→	Employees Job_History Departments	Jobs	Job_Id		
Locations	→	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
Countries	→	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
Employees Job_History	→	Departments	Employees	Department_Id	Job_History	Job_Id
Employees Job_History Departments	→	Jobs	Job_History	Job_Id	Departments	Location_Id
Employees Job_History Departments Jobs	→	Locations	Departments	Location_Id		
Employees Job_History Departments Jobs Locations	→	Countries	Locations	Country_Id		
Employees Job_History Departments Jobs Locations Countries	→					

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for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

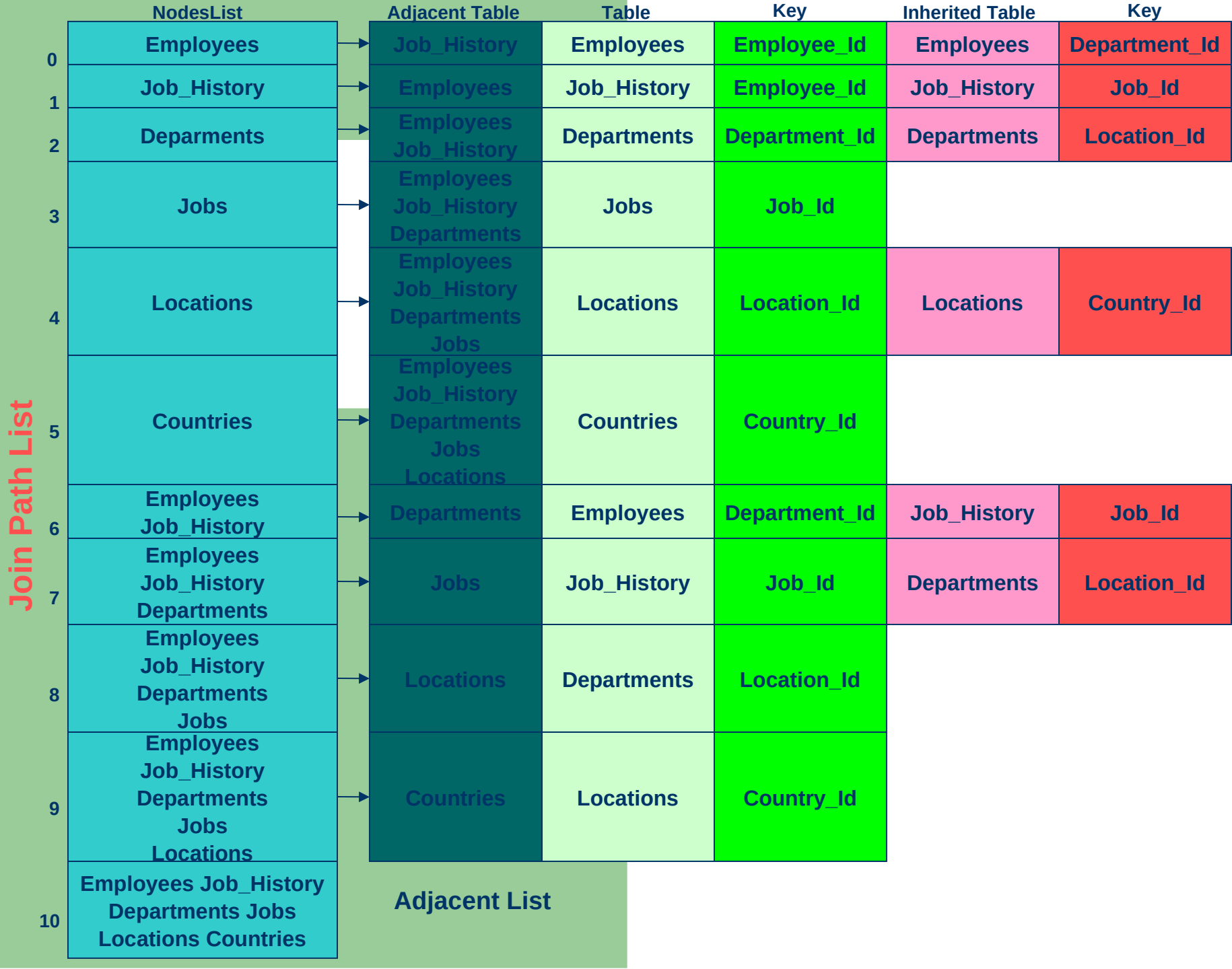
if (buf.key != Key($T_{[i]}$)) and (buf.Key not in InheritedKey($T_{[i]}$)) then
InheritedKey($T_{[i]}$) += buf.key

if T_i is the table from which comes Key($T_{[i]}$) then

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buf.key = Key($T_{[i]}$)





Give a general name for the B⁺Tree.

Give for every entry in the JoinPathList a B⁺Tree index with name as the B⁺Tree + the PathJoinList entry number.

About the last virtual table, it index has no keys, it works because we consider pairs of < keys, Data Pointers > so they are ordered by their data pointers. Scanning the index we get all the sequences of joined data pointers.

Non Terminal has repeated empty keys they point to different pages. When comes a key it would be inserted in the last page.

Duplicate keys are inserted and when a page is full , the key is repeated in the non terminal.

In any case we can incorporate any key of our choice from the tables forming the virtual table.

If the table is in join with itself, consider the table twice as aliases.

Define a Create Join Index (IndexName, Eventual columns for the last virtual table representing tables in join)

Implementation:

Use a big buffer and from the Data Dictionary divide it by the keys length, inherited keys length and space for the number of Data Pointers.

Suppose we wants the join sequence of the tables ordered by Employees.Name and Departments.Department_Id, applying the algorithm, the JoinPathList becomes:

NodesList		Adjacent Table	Table	Key	Inherited Table	Key
0	Employees	Job_History	Employees	Employee_Id	Employees	Name
					Employees	Department_Id
1	Job_History	Employees	Job_History	Employee_Id	Job_History	Job_Id
2	Deparments	Employees Job_History	Departments	Department_Id	Departments	Location_Id
3	Jobs	Employees Job_History Departments	Jobs	Job_Id		
4	Locations	Employees Job_History Departments Jobs	Locations	Location_Id	Locations	Country_Id
5	Countries	Employees Job_History Departments Jobs Locations	Countries	Country_Id		
6	Employees Job_History	Departments	Employees	Department_Id	Employees	Name
7	Employees Job_History Departments	Jobs	Job_History	Job_Id	Job_History	Job_Id
					Employees	Name
					Departments	Department_Id
					Departments	Location_Id

8

Employees
Job_History
Departments
Jobs



Locations

Departments

Location_Id

Employees

Name

9

Employees
Job_History
Departments
Jobs
Locations



Countries

Locations

Country_Id

Employees

Name

10

Employees
Job_History
Departments
Jobs
Locations
Countries



Employees

Name

Departments

Department_Id

Departments

Departments_Id

Employees

Departments

Department_Id

Insert routine

When a new row R_m from table T_i get inserted do the following:

- Locate the entry of T_i in the JoinPathList
- From its adjacent List, locate the definition of the keys and inherited keys
- From Row R_m get the columns constituting the keys and the inherited keys
- Call AddJoinKey (T_i , Keys, InheritedKeys, DP_i) where DP_i is the row id of row R_m .

AddJoinKey ($T_{[i]}$, $[DP_i]$)

- Call AddKey ($B^+Tree(T_{[i]}), keys_{[i]}, InheritedKeys_{[i]}, [DP_i]$) for the index of table $T_{[i]}$
- Locate the entry of $T_{[i]}$ in the JoinPathList
- From its adjacent List, locate the Table $T_{[k]}$ adjacent to it and do the following:
 - Locate the entry of $T_{[k]}$ in the JoinPathList
 - FindKey($B^+Tree(T_{[k]}), Keys_{[i]}$)
 - While found($keys_{[i]}$) do
 - ReturnKeys($B^+Tree(T_{[k]}), keys_{[k]}, InheritedKeys_{[k]}, [DP_k]$)
 - Locate the entry of $T_{[ik]}$ in the JoinPathList
 - From its adjacent List, locate the definition of the keys and inherited keys
 - From $keys_{[i]}, inheritedkeys_{[i]}, keys_{[k]}, inheritedkeys_{[k]}$ get the keys and inherited keys of $T_{[ik]}$
 - AddJoinKey ($T_{[ik]}, Keys_{[ik]}, InheritedKeys_{[ik]}, [DP_{ik}]$)
 - NextKey($B^+Tree(T_{[k]}), Keys_{[i]}$)

AddJoinKey ($T_{[i]}$, $[DP_i]$)

In the same fashion when using an ordinary B⁺Tree and one row get inserted, so we check the definition of the B⁺Tree to get the necessary keys from the row to insert them, with B^{Join}Tree we check the definition to get the keys and the inherited keys.

Call AddjoinKey(T_i , [keys], $[DP_i]$)

Delete routine

Call DelJoinKey (T_i , DP_i) where DP_i is the data pointer of the deleted row from the base table T_i .

DelJoinKey ($T_{[i]}$, $[DP_i]$)

- Call DelKey ($B^+Tree(T_{[i]}), keys_{[i]}, [DP_i]$) for the index of table $T_{[i]}$
- Locate the entry of $T_{[i]}$ in the JoinPathList
- From its adjacent List, locate the Table $T_{[k]}$ adjacent to it and do the following:
 - Locate the entry of $T_{[k]}$ in the JoinPathList
 - FindKey($B^+Tree(T_{[k]}), Keys_{[i]}$)
 - While found($keys_{[i]}$) do
 - ReturnKeys($B^+Tree(T_{[k]}), keys_{[k]}, InheritedKeys_{[k]}, [DP_k]$)
 - Locate the entry of $T_{[ik]}$ in the JoinPathList
 - From its adjacent List, locate the definition of the keys and inherited keys
 - From $keys_{[i]}, inheritedkeys_{[i]}, keys_{[k]}, inheritedkeys_{[k]}$ get the keys and inherited keys of $T_{[ik]}$
 - DelJoinKey ($T_{[ik]}, Keys_{[ik]}, [DP_{ik}]$)
 - NextKey($B^+Tree(T_{[k]}), Keys_{[i]}$)

B \bowtie Tree with incremental Join

Due to the fact that join is commutative and associative and we are working on Virtual Tables and using indexes on them; it is possible instead of calculating all the join combinations to calculate incrementally the join.

This issue works just when the n tables are in direct path join between them but if they are not we are not interested.

Giving a casual order for the tables.

Beginning from Table 0, get a table T_i in direct join with it.

A Join Path List comes out with 2 entries from T_0 to T_i and from T_i to T_0 .

The index number start always with 0.

Repeat, with T_{0i} and get a next table that is in direct join with T_0 or with T_i , the process continue till we scan all the tables.

This algorithm is linear, is $2*n - 1$.

Complexity of the algorithm for the creation of JoinPathList.

The complexity for the creation of JoinPathList structure is: $2*n-1$ where n is the number of tables in join.

Proof:

We can prove it by induction on the number of tables in join.

For $m = 1$:

The complexity should be $2*1-1 = 1$ in fact it is the only table that get inserted in the JoinPathList.

For $m = n-1$:

Suppose that the number of tables in JoinPathList is $2*(n-1)-1$.

For $m = n$:

The n^{th} table get inserted as a Vertex in the JoinPathList at the beginning of the algorithm. The n^{th} table get inserted in queue and path dynamic arrays because the n tables are in join and at least there is one table in the $(n-1)$ remaining table that is in join with the n^{th} table.

So when the algorithm run at certain point should execute:

$$T_{[\text{buf}]} += T_i$$

$$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$$

where T_i is T_n , so the number of tables in JoinPathList are: $2*(n-1)-1 + 1 + 1 = 2*n-1$

Complexity of the algorithm for the insertion and deletion.

Delete is symmetric to insert in the algorithm in the sense where there is an insert we use a delete, so they have both the same complexity. When inserting a new row in the database we use the B^{JoinTree} structure to drive us in the insert for the join.

Suppose that the order of the B^+ Tree is m , the number of elements in the $(2^n - 1)$ B^+ Trees is p_i where i is the index of the B^+ Tree and that in average there is l_i elements satisfying the join between every pair of tables.

In the worst case when get inserted row with the lowest order tables T_0 and T_1 in this case we call recursively the insert procedure for $(2^n - 1) - (n - 1) = n$ times.

The complexity will be: $\text{Ord}(n * l_i * \log_{m/2}(p_i))$

Complexity of the algorithm for the other operation.

The only B⁺Tree of our interest for the scan is the one with the latest index that have the join of the tables inside it.

Suppose that the number of elements for the latest index is $p_{(2*n-1)}$ so the other operations on this B⁺Tree for find, search, prev, next,... are the same as for normal B⁺Tree with the same number of elements.

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$

insert all the Names of Base Tables from the join sequence $T_0 \dots T_m$ as vertexes in the PathJoinList

create 2 dynamic arrays queue and path

insert T_0 into path

insert T_0 into queue

repeat

T_{Element} = First Table in queue

 for every Link Item in Adjacent Link of T_{Element} from the Join Graph do

 if the Link Item is in the join sequence then

 if path doesn't contain the Link Item then

 insert Link Item into path

 insert Link Item into queue

 remove T_{Element} from queue

until queue is empty

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$ (continue)

create a local buffer buf

insert into buf the first entry from path

for all the remainder entries in path do

take one T_i at a time

$\text{PathJoinAdjacentList}(T_i) = T_{[\text{buf}]}$

$\text{Key}(T_i) = \text{getFirstAdjacentListKey}(T_i, T_{[\text{buf}]})$

$\text{PathJoinAdjacentList}(T_{[\text{buf}]}) = T_i$

$\text{Key}(T_{[\text{buf}]}) = \text{getFirstAdjacentListKey}(T_{[\text{buf}]}, T_i)$

$T_{[\text{buf}]}^+ = T_i$

$\text{Insert NodesList}[T_{[\text{buf}]}] = T_{[\text{buf}]}$

Steps to generate Join Path List for the join sequence $T_0 \dots T_m$ (continue)

create a structure buf with 2 fields: Table and Key
for all the tables in PathJoinList going downward do

take one $T_{[i]}$ at a time

for all Base Tables in $T_{[i]}$ do

take one T_k at a time

for every buf.Table = T_k do

**if (buf.key \neq Key($T_{[i]}$)) and (buf.Key not in AuxKey($T_{[i]}$)) then AuxKey($T_{[i]}$)
+= buf.key**

if T_l is the table from which comes Key($T_{[i]}$) then

buf.Table = T_l

buf.key = Key($T_{[i]}$)