

## 6. Honghui

**Program Name:** Honghui.java

**Input File:** honghui.dat

Honghui walked into an old mathematics classroom where he discovered a sequence of colored symbols on the chalkboard. The symbols were faded, but each was either an opening or closing parenthesis ( '(' or ')' ) respectively).

Honghui wants to erase some symbols on the board to form a valid colored parenthesis sequence. Valid colored parenthesis sequences are described by the following grammar:

- An empty sequence is a valid colored parenthesis sequence.
- If  $X$  is a valid colored parenthesis sequence, then  $(X)$  is a valid colored parenthesis sequence if and only if the outer parentheses have the same color.
- If  $X$  and  $Y$  are valid colored parenthesis sequences, then their concatenation  $XY$  is a valid colored parenthesis sequence.

Each symbol takes a different amount of effort to erase. What is the minimum amount of effort Honghui has to put in such that the remaining sequence is a valid colored parentheses sequence?

**Input:** The first line of input is  $T$  ( $1 \leq T \leq 25$ ), the number of test cases. Each test case starts with an integer  $N$  ( $1 \leq N \leq 400$ ), the number of symbols on the chalkboard. The next line is a string of length  $N$  where every character is either '(' or ')', describing the symbols on the chalkboard. Then follows a line with  $N$  integers, the color of each symbol. The color is given as a positive integer in the range  $[1, N]$ . The next line of each test case has  $N$  integers, the effort required to erase each symbol in order. Each effort value is a positive integer at most 1,000,000.

**Output:** For each test case, output the minimum amount of effort required to make a valid parenthesis sequence by erasing some symbols. Format each answer with the case numbers as in the sample.

**Sample input:**

```
2
7
( ( ) ) ( )
1 2 4 2 3 3 1
3 1 4 1 5 9 2
3
)))
3 3 3
1 2 3
```

**Sample output:**

```
Case #1: 4
Case #2: 6
```

**Sample Explanation:** In the first test case, erase the only symbol with color 4 to get the sequence  $( ( ) )$ , which is balanced and has all matching colors. In the second case, all parentheses must be erased.