

## Analog Electronics : a 2-page study guide by Amanda Falke | December 2015

A simple model for the bipolar transistor using a 0.6 volt ideal diode, controlled current source, and  $r_e$ .

In the CE BJT, small base current controls large collector current. In the simple model, a 0.6 volt drop across the diode is **used for low current applications, and a 0.7 volt drop across the diode is used for medium to high current applications.** The ideal diode is located between the base and emitter. Small signal input on the base is equal to the small signal output at the emitter,  $V_e$ . Output from  $V_e$  is non-inverting with unity gain minus DC offset from diode drop. Output from  $V_c$  is inverting. Current in the collector is  $I_c = \beta I_b$ . Current in the base is essentially zero. Current in the left “tuning” branch of the 4-resistor bias circuit is approximately 10 times collector current. Recall Shockley’s equation:  $I_e = I_{es} * e^{V_{be} / V_t}$  where  $V_t = 26 \text{ mV}$  and where  $I_{es} = \text{“saturation current”} = 10^{-12} \rightarrow 10^{-17} \text{ A}$  (Hambley, p. 213).

The **gain** of a simple model CE BJT inverting amplifier ( $V_c = V_{out}$ ) is  $A_v = -R_c / R_e$ . **Gain when  $r_e$  is the only emitter resistor:** Our gain is limited in a simple CE BJT circuit because we cannot make  $R_e$  too small, as  $R_e$  controls the **DC feedback, as such:  $V_{be} \uparrow \rightarrow V_e \uparrow \rightarrow I_e \uparrow \rightarrow$  ideal diode reverse biased/conducts less current  $\rightarrow I_e$  back down.** To take advantage of the BJT’s high gain capabilities and still keep the DC bias of the circuit stable, we **separate the AC and DC emitter resistors** by adding an RC branch “ **$R_{ac}$** ” parallel to the emitter resistor. When we add this branch, the gain is  $A_v = R_c / R_{ac} + R_{dc}$ .  $R_{dc} \gg R_{ac}$ . This means that so little current will go down the “dc” branch that **we need not consider  $R_{dc}$** . Since  $R_{ac}$  is separated completely from the DC operations and DC bias of the circuit,  $R_{ac}$  can be relatively large, and hence we can exploit the BJT’s full high-gain capabilities. **Once the separate “ $R_{ac}$  RC branch” is added parallel to (common) emitter, gain is simplified to  $gain = g_m R_L$ , or,  $gain = [1/r_e] R_L$ .**

**Transconductance ( $g_m$ ):** Transconductance in a bipolar transistor is programmable by altering  $I_c$ , the collector current.

Transconductance is often referred to as the “sensitivity” of a circuit: “for a small change in gate current, what is the change in output voltage?” Transconductance multiplied by resistance = “dimensionless gain.” Hence, the units of  $g_m$  are the reciprocal of resistance, or  $g_m = 1/r_e$  and  $r_e = 1/g_m$ . Transconductance  **$g_m$  for BJT’s** is a known industry-quantity of  $g_m = 38 * I_c$ . **How to set  $g_m$  and  $1/g_m$  for specific values:** Current-controlled variable gain is a feature of the bipolar transistor. Both  $g_m$  and little  $r_e$  are controlled by the collector current. Set  $g_m$  for a specific value using  $g_m = 38 * I_c$ .

“**Little  $r_e$** ” is a small internal resistance inside of the emitter, and in series with  $R_e$ . Using Ohm’s law:  $r_e = V_t / I_c$  where  $V_t = kT / q$ ; so **little  $r_e = 26 \text{ mV} / I_c$** . **Little  $r_e$  keeps the gain from going to infinity.** **Gain when  $R_e$  and  $r_e$  are the emitter resistors:** Recall the inverting amplifier gain equation  $A_v = -R_c / R_e$ . If  $R_e$  approaches zero, we have **infinite gain**. This problem is resolved by the existence of **little  $r_e$** , or the internal resistance of the emitter. Hence,  $A_v = -R_c / R_e + r_e$  (inverting  $V_c$  out).

**Separating the AC signal and DC circuits using DC blocking capacitors:** A capacitor in series with a source behaves like a high pass filter. DC has a frequency of zero; the **DC blocking capacitor** blocks (filters out) all DC voltage **components**.  $V_{CC}$  is a DC Bias voltage to tune the circuit to its quiescent point and DC operating ideal characteristics. **DC blocking capacitors set frequency response:** Capacitance is set using a corner (cutoff) frequency  $\omega = 2 \pi f$ . In a high pass filter, corner frequency is set lower than the desired frequency response; vice versa for low pass filters. A good **corner frequency** to use for high pass filter is 15.7Hz. Before capacitance is set, the **equivalent ac resistance** looking into the input, for  $C_{in}$ , and the equivalent ac resistance looking into the output, for  $C_{out}$ , must be calculated. Generally the **equivalent resistance** looking into the input is  $R_1 \parallel R_2 \parallel \beta R_e$ , and this  $R_{eq} \ll$  lowest R in this equation. Equivalent resistance looking into the output is just  $R_c$ . Recall that  $\beta = 100$ . **Calculating capacitance** is  $\omega = 1 / RC$ ; to calculate  $C_{in}$ , R is equivalent ac resistance looking in; to calculate  $C_{out}$ , R is just  $R_c$ .

**Common Emitter :  $V_{ce}$  Design Constraint**

**The circuit design must meet this minimum threshold voltage drop across transistor of 0.2V in order to be a current controlled current source operating in the active region (s).**

“**Collector current** is independent of collector-to-emitter voltage, so long as  $V_{ce} > 0.2 \text{ V}$ .” (Hambley, p. 214). Therefore the voltage between the collector and the emitter, aka the voltage drop across the transistor, does not affect the collector current so long as that voltage drop across the transistor is at least 2/10 of a volt. This is a “threshold voltage” of sorts. The bipolar junction’s base current  $I_b$  is very responsive to small changes in base-emitter voltage  $V_{be}$ . **That small change in base current  $I_b$  results in a relatively large change in collector current  $I_c$** , due to dependency  $I_c = \beta I_b$ . **The BJT functions as a switch**, with the base as the controlling entity. **The base current is the current-controlling region**, but the base current’s variation will

rely on the base voltage, aka the small signal input voltage. **The threshold voltage  $V_{ce} > 0.2V$**  is in regards to the minimum current (voltage) required through (over) the base (base-emitter ideal diode) in order to forward bias the transistor's emitter (diode) junction. **A more common sense way to say that is that the voltage drop across the transistor must be at least 0.2V, or transistor won't be DC-biased or "turned on."**

**There are three stages of operation for the BJT: Note  $V_{ce}$  minimum design requirements for drop across BJT:**

**CUTOFF REGION:**  $V_{ce} < 0.2V$  threshold voltage. Transistor = open circuit.

• no current •  $V_{be} < 0.6V$  (emitter-base junction is reverse biased) • Recall shaded area on BJT plot

If  $V_{ce}$  is greater than  $V_{be}$ , the collector junction is reverse biased.

**SATURATION REGION:** Due to increase in  $V_{be}$ :  $V_{ce} \sim 0.2V$  threshold voltage. Transistor appears as short circuit.  $V_{ce}$  has JUST reached threshold voltage. • Recall shaded area on BJT plot

•  $V_{ce} \sim 0.2V$ . This is called " $V_{ce}$  is at the saturation voltage."  $V_{ce}$  has just reached it.

$V_{be} > 0.6V$  (emitter-base junction is forward biased)

**FORWARD ACTIVE REGION:** Linear Amplification.  $V_{ce} > 0.2V$  and  $V_{cc} < V_{ce}$ .

The supply voltage must be above the voltage drop across the transistor  $V_{ce}$ , and comfortably so for **centering** design purposes.

• Recall active area on BJT plot

**Load line calculations for the BJT: Quiescent point bias design :**  $V_{gs}$  is to a MOSFET plot as  $I_b$  is to a BJT plot.

• Plot  $I_c$  versus  $V_{ce}$  • Use load line equation  $V_{cc} = I_c R_c + V_c + V_e$  •  $I_{c \max} = V_{cc} / R_c + R_e$

**Common base:** for when we want electronic impedance match. Reverse isolation is used when we don't want to "see" what is on the output. You are driving the circuit from the output but only "looking" at the input. 50 ohm impedance. Small signals, and an input that's isolated from the output, and we define the input impedance. **Common emitter:** for when we want lots of voltage gain. **Common collector:** for when we want lots of current into the load.

<p><b>COMMON EMITTER 4-R BIAS CIRCUIT DESIGN SEQUENCE:</b></p> <ol style="list-style-type: none"> <li>1. Pick <math>V_{cc}</math></li> <li>2. Pick <math>V_c</math> if <math>R_c</math> not given: <math>0V &lt; V_c &lt; V_{cc}</math> If given <math>R_c</math>, pick the voltage drop over <math>R_c</math>: <math>V_{dropR_c} = I_c R_c</math>, that will give you <math>V_c</math>: <math>V_c = V_{cc} - V_{dropR_c}</math>. <b><u><math>V_c</math> IS Q POINT OUTPUT.</u></b></li> <li>3. <math>V_e</math>: Set <math>0.1V &lt; V_e &lt; 1V</math>. <math>V_e</math> is DC feedback</li> <li>4. <math>V_{be}</math> (or <math>V_{in}</math>): <math>V_{be} - V_{dropdiode} = V_e</math></li> <li>5. <math>R_e</math>: Ohm's law: <math>R_e = V_e / I_c</math></li> <li>6. Find <math>I_{bias} = 1/10 * I_c</math> and <math>I_b = 1/100 I_c</math></li> <li>7. Find <math>R_1</math> and <math>R_2</math>: Ohm's law: <math>V_{cc} = I_{bias}(R_1 + R_2)</math> or voltage divider <math>V_1 = V_{cc} (R_1 / (R_1 + R_2))</math></li> <li>8. Find gm. gm of BJT = <math>38 I_c</math>. Recall that <math>r_e = 1/gm</math>.</li> <li>9. Find gain = <math>-R_c / R_e</math>.</li> <li>10. little <math>r_e</math> and calculate that into actual gain = <math>-R_c / (R_e + r_e)</math>. Is this close to step 7? Find % of variation here.</li> <li>9. Design frequency response: Find equivalent ac resistances, and capacitances.</li> <li>10. Note that with additional "Reac RC branch", gain is just gain = gmRL.</li> </ol>	<p>"COMMON" refers to whatever is grounded and not connected to either input or output.</p> <p><b>Common base:</b></p> <ol style="list-style-type: none"> <li>1. Use same exact CE circuit, but input is now through emitter, base is grounded, and collector is output just as before. <math>V_{in}</math> on emitter has a <math>C_{in}</math> and looks symmetrical with <math>C_{out}</math> on collector ("horizontal branches").</li> <li>2. Voltage divider for <math>R_1</math> and <math>R_2</math>. <math>V_1 \sim V_{cc}/2</math>, for now.</li> <li>3. <math>V_e = V_1</math> - diode drop.</li> <li>4. <math>V_c</math> is still the q point. <math>V_{cc} - V_e = V_c</math>.</li> <li>5. Input impedance is super low like 5-10 ohms, output Z is super high. <math>Z_{out} \sim \text{source} / \text{beta of transistor}</math>.</li> <li>6. <math>1 / 2 \pi R C_{in}</math> = corner frequency</li> <li>7. <math>V_c</math> is still Q point</li> <li>8. Input current is essentially what output current is due to super low impedance of input on "<math>V_e</math>"</li> <li>9. Voltage swings cleanly from <math>V_{cc}</math> to zero</li> <li>10. RF applications</li> </ol> <p><b>Common collector "Emitter follower:"</b></p> <ol style="list-style-type: none"> <li>1. Make a new branch in parallel with <math>R_e</math>. Put another R on.</li> <li>2. Put a C in between the two, up top (in series with both).</li> <li>3. <math>V_{out}</math> is across this second R in the second branch you just added.</li> </ol>
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An important overview of the bipolar junction transistor should always include that the desired mode of operation is always the linear mode, when a large enough voltage drop across the transistor is part of the inherent circuit design, as well as a significant design constraint.