# Carlingford High School



# TRIAL HIGHER SCHOOL CERTIFICATE EXAMINATION

2019

| Student | Number: |  |
|---------|---------|--|
|         |         |  |

# **Mathematics Standard 2**

#### General Instructions

- Reading time 5 minutes
- Working time 2 hours and 30 minutes
- Write using black/blue pen
- Approved calculators may be used
- A reference sheet is provided at the back of this paper
- In Questions in Section II, show relevant mathematical reasoning and/or calculations

# Total marks: 100

Section I – 15 marks (pages 3 – 8)

- Attempt Questions 1 15
- Use the Multiple Choice Answer sheet on page 29
- Allow about 25 minutes for this section

#### **Section II – 85 marks** (pages 9 - 26)

- Attempt Questions 16 46
- Allow about 2 hours and 5 minutes for this section

|       | Linear and<br>Non-Linear<br>Relationships | Applications of Measurement  | Financial<br>Mathematics | Statistical<br>Analysis | Network<br>Concepts   |   |
|-------|---|--|--------------------------|-------------------------|---|---|
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| 34    | /1  |  |                          |                         |   |   |
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| 36    | /2  |  |                          |                         |   |   |
| 37    | /3  |  |                          |                         |   |   |
| 38    | /2  |  |                          |                         |   |   |
| 39    |   | /2   |                          |                         |   |   |
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| 42    |   |  |                          | /1                      |   |   |
| 43    |   |  |                          | /4                      |   |   |
| 44    |   |  |                          |                         | /3  |   |
| 45    |   |  | /4                       |                         |   |   |
| 46    |   | /4   |                          |                         |   |   |
| Total | /20                                       | /29  | /23                      | /24                     | /4  | /100  |

#### Section I: 15 marks

#### Attempt Questions 1-15.

#### Allow 25 minutes for this section

#### Use the multiple-choice answer sheet for Questions 1-15

1. Simplify: 2x(7-x) - 3x

- (A)  $11x x^2$
- (B)  $11x 2x^2$
- (C)  $14x 2x^2 3x$
- (D) 17x 2

2. Cameron earns \$14.50 per hour normal rate. How much does he earn if he works 38 hours at normal rate and 5 hours at time-and-a- half?

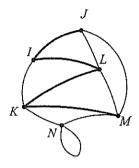
- (A) \$587.25
- (B) \$630.75
- (C) \$659.75
- (D) \$935.25

3. A type of car number plate has two letters, followed by two numerals, followed by two more letters. For example:

Which calculation would give the total number of number plates of this type?

- (A)  $26 \times 26 \times 10 \times 10 \times 26 \times 26$
- (B)  $26 \times 10 \times 10 \times 26 \times 26$
- (C)  $26 \times 25 \times 10 \times 9 \times 26 \times 25$
- (D)  $25 \times 10 \times 9 \times 24 \times 23$

- 4. John measured his height to be 182cm, correct to the nearest centimetre. What is the percentage error in his measurement?
  - (A)  $\pm 0.0027 \%$
  - (B)  $\pm 0.0055 \%$
  - (C)  $\pm 0.27 \%$
  - (D)  $\pm 27\%$
- 5. An undirected network with vertices *I*, *J*, *KL*, *M* and *N* is shown below.



Which term could  $\underline{not}$  be used to describe the highlighted section J I L K M?

- (A) a cycle
- (B) a path
- (C) a tree
- (D) a walk
- 6. An estimate of a person's maximum heart rate, R (in beats per minute) is given by the formula:

R = 220 - A where A is the person's age in years.

It is estimated that a healthy person should have a target heart rate of 55% of their maximum rate when beginning to exercise.

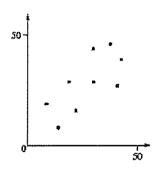
Hanna is a healthy 17 years, 6 months old girl.

What is an estimate of her target heart rate, in beats per minute, when she begins exercising?

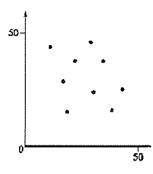
- (A) 202.5
- (B) 91.1
- (C) 210.4
- (D) 111.4

7. Which graph below best shows data with a correlation closest to -0.3?

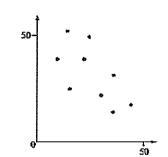
(A)



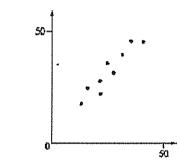
(B)



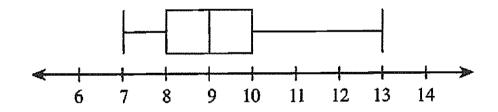
(c)



(a)



8. The box-and-whisker plot below represents the number of calls made to find a casual person for the day.



Which of the following must be correct?

- (A) The median is 9
- (B) The mode is 9
- (C) The mean is 9
- (D) The interquartile range is 9

9. A house was purchased in 1984 for \$65 000. Assume that the rate of inflation in Australia has averaged at 3% per annum..

Which expression gives the value of the house in 2009?

- (A)  $65000(1+0.03)^{25}$
- (B)  $65000(1+3)^{25}$
- (C)  $65000 \times 25 \times 0.03$
- (D)  $65000 \times 25 \times 3$
- Darren borrowed \$18 000 from the Credit Union for 3 years, at 8% per annum monthly reducible interest, to buy a car. His monthly repayments are \$564.

The table below shows the calculations for the first two months of his loan.

| -            | Principal (P) | Interest (I) | P+I         | P+I-R       |
|--------------|---------------|--------------|-------------|-------------|
| First month  | \$18 000      | \$120        | \$18 120    | \$17 556    |
| Second month | \$17 556      | \$117.04     | \$17 673.04 | \$17 109.04 |
| Third month  |               |              |             |             |

How much will Darren owe the Credit Union at the end of the three months?

- (A) \$16 545.04
- (B) \$16 659.10
- (C) \$17 787.10
- (D) \$17 913.73
- 11. Which of the following correctly expresses n as the subject of  $v = \frac{3mn^2}{r}$ ?
  - (A)  $n = \pm \frac{\sqrt{rv}}{3m}$
  - (B)  $n = \pm r \sqrt{\frac{v}{3m}}$
  - (C)  $n = \pm \frac{r\sqrt{v}}{3m}$
  - (D)  $n = \pm \sqrt{\frac{rv}{3m}}$

12. Ridges High decide to survey their students using a stratified random sample which will be based on year level and gender. The following table shows the number of students in each level and their gender.

| Year level | Males | Females |
|------------|-------|---------|
| 7          | 110   | 105     |
| 8          | 110   | 110     |
| 9          | 105   | 100     |
| 10         | 100   | 102     |
| 11         | 98    | 101     |
| 12         | 84    | 75      |

Based on this table, how many Year 12 girls should be surveyed in a sample of 80 students?

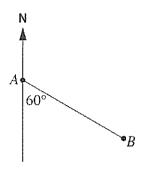
- (A) 4
- (B) 5
- (C) 6
- (D) 7
- 13. Jihwan lists the costs of running his car:
  - Registration \$378.00 annually
  - CTP insurance \$546.00 annually
  - Comprehensive insurance \$460.00 annually
  - Mechanical service and repairs \$450.00 every three months
  - Petrol and consumables \$40.00 per week

He wants to put money into an account each week to cover these costs and allow an extra 10% contingency in case of unforeseen expenses.

How much (to the nearest dollar) should he deposit each week?

- (A) \$89.00
- (B) \$101.00
- (C) \$102.00
- (D) \$111.00

14. What is the bearing of A from B?



- (A) 060°
- (B) 120°
- (C) 300°
- (D) 150°
- 15. The table below is used to calculate monthly loan repayments.

Monthly loan repayments (in dollars) per \$1000 borrowed

| Înteresi<br>rate % pa | 5 years | 10 years | 15 years | 20 years |
|-----------------------|---------|----------|----------|----------|
| 5%                    | 18.87   | 10.61    | 7.91     | 6.60     |
| 6%                    | 19.33   | 11.10    | 8.44     | 7.16     |
| 7%                    | 19.80   | 11.61    | 8.99     | 7.75     |
| 8%                    | 20.28   | 12.13    | 9.56     | 8.36     |
| 9%                    | 20.76   | 12.67    | 10.14    | 9.00     |

Daniel has borrowed \$70 000 at 8% per annum for 15 years.

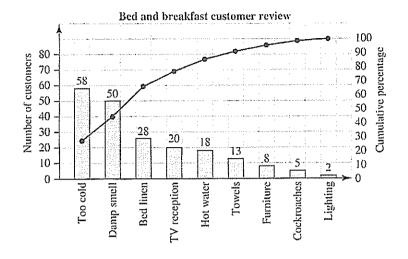
What is his monthly laon repayment?

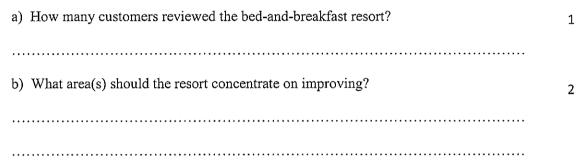
- (A) \$143.40
- (B) \$669.20
- (C) \$8 030.40
- (D) \$10 038.00

# **End of Section 1**

#### Question 16 (3 marks)

The Pareto chart below shows the complaints of customers staying at a particular bed-and-breakfast located in an alpine resort area.





#### Question 17 (3 marks)

The masses of the adult female koalas in a colony are normally distributed with a mean of 9.5 kg and a standard deviation of 0.8 kg.

By calculating the z-scores, what percentage of these females would you expect to have masses between 7.9 kg and 10.3 kg?

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# Question 18 (7 marks)

The ordered back-to-back stem-and-leaf plot below shows the distribution of maximum temperatures in Sydney and Melbourne over the last fortnight of January this year.

| Sydney              |   | Melbourne |
|---------------------|---|-----------|
|                     | 1 | 8 9       |
| 9 9 8 8 7 7 6 5 4 3 | 2 | 3 6 9     |
| 4 2 1               | 3 | 12666     |
| 1                   | 4 | 1 3 4 5   |

| a) What was the highest recorded temperature?   | 1 |
|---|---|
| b) What was Sydney's median temperature in the last fortnight of January?   | 1 |
| c) Sydney has a lower quartile $(Q_L)$ of 26 and an upper quartile $(Q_U)$ of 31. Is the temperature of 41 an outlier? Justify your answer with mathematical working. | 2 |
|   |   |
|   |   |
| d) Compare and contrast the two data sets by examining the shape and skewness of the distributions and the measures of location and spread.                           | 3 |
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# Question 19 (2 marks)

Rosa compared her examination results in Chemistry and Biology.

|           | Mean | Standard Deviation | Mark |
|-----------|------|--------------------|------|
| Chemistry | 80   | 12                 | 92   |
| Biology   | 58   | 10.5               | 89   |

| a) Rosa's z-score for Biology is 2.95. What does this mean?  | 1 |
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| c) If Rosa's z-score for Chemistry is 1, in which subject did she perform better in?<br>Explain your answer.   | 1 |
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| Question 20 (2 marks)  |   |
| The average rate for domestic electricity is \$0.18/kWh.  Calculate the cost of running an 800-watt air conditioner for 6 hours per day for 90 days. |   |
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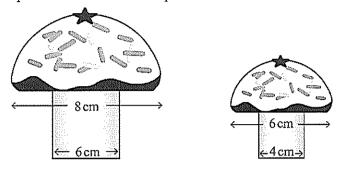
# Question 21 (3 marks)

Margaret lives in Dubbo, NSW, which is in the Eastern Standard Time zone of UTC + 10. Areej lives in Denver, Colorado which has longitude of UTC -7.

| a) What is the time difference between Dubbo and Denver?  | : |
|---|---|
|   |   |
|   |   |
| b) If Margaret makes a call to Areej at 7:30 am on Friday 5 <sup>th</sup> July (Dubbo time), what will be the local time and date in Denver when Areej receives the call? | Ź |
|   |   |
|   |   |
|   |   |
| Question 22 (1 mark)  |   |
| Simplify fully: $\frac{3t^2}{d} \times \frac{5dt}{6}$   |   |
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| Question 23 (2 marks)   |   |
| Solve the equation: $\frac{2x-2}{3} - 4 = 6$  |   |
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#### Question 24 (4 marks)

A café sells two sizes of muffins. The bottom section of the larger size muffin is shaped as a cube with side length 6 cm. When cooked, a hemisphere is formed on the top with a diameter of 8 cm. The bottom section of the smaller size muffin is shaped as a cube with side length 4 cm. When cooked, a hemisphere is formed on the top with a diameter of 6 cm.

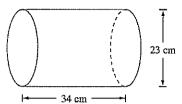


The price is based on the volume of cake mixture used in the muffin. The large muffin costs \$5.40.

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| cm <sup>3</sup> . 1 |
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# Question 25 (2 marks)

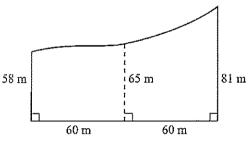
Calculate the surface area of the closed cylinder drawn below, correct to 3 significant figures.



| <br>      | • • • • • | • • • • • | • • • • • |           |      | • • • • | ••••    |         | • • • • | <br>• • • • | • • • • | ••••      | • • • • • | • • • • | • • • • | • • • • | • • • • | • • • • | <br>• • • • | ٠.  |
|-----------|-----------|-----------|-----------|-----------|------|---------|---------|---------|---------|-------------|---------|-----------|-----------|---------|---------|---------|---------|---------|-------------|-----|
| <br>      |           |           |           |           |      |         |         | <i></i> |         | <br>        |         |           |           | ,       |         |         |         |         | <br>        |     |
|           |           |           |           |           |      |         |         |         |         |             |         |           |           |         |         |         |         |         |             |     |
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|           |           |           |           |           |      |         |         |         |         |             |         |           |           |         |         |         |         |         |             |     |

# Question 26 (4 marks)

A lake has a cross-section as shown below.



2

2

| a) | Calculate the area of this cross-section using two applications of the Trapezoidal rule.   |
|----|--|
|    |  |
|    |  |
|    |  |
| b) | The lake is 60 cm deep. Marc thinks he can empty the lake using an eight-litre bucket. How many times would he have to fill the bucket from the lake in order to empty the lake? $(1m^3 = 1000 L)$ |
|    |  |
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#### Question 27 (3 marks)

On 15<sup>th</sup> March, James bought a camera costing \$1600 using a credit card. Compound interest was charged at a rate of 21.3% per annum for purchases. There is no interest-free period. The period for which interest was charged included the date of purchase and the date of payment.

James made no other purchases on his card.

| a) What is the daily percentage interest rate, correct to 3 decimal places?  | 1 |
|--|---|
| b) What amount was paid when the account was paid in full on 31st March?   | 2 |
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| Question 28 (3 marks)  |   |
| Patrick is considering purchasing a television at a price of \$3990. He has a deposit of \$500 but needs to borrow the rest of the money. A finance company offers him the money at a flat rate of 21% p.a. to be repaid monthly over 4 years. |   |
| a) What is the total amount that Patrick must borrow to purchase the television?   | 1 |
| b) Calculate the interest paid on the balance over the four years.   | 1 |
|  |   |
|  |   |
|  |   |
| c) Calculate the monthly repayment on the loan.  | 1 |
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# Question 29 (3 marks)

Bonita buys 500 shares in a company at \$4.50 per share.

| a)         | If there are fixed brokerage fees of \$25.60 and stamp duty of 15 cents per \$100 or part thereof, calculate the total cost for Bonita to buy the shares.                         |
|------------|---|
| •••        |   |
| •••        |   |
| b)         | The company pays a dividend of 90 cents per share. Calculate the dividend yield on the shares, correct to one decimal place.  |
| • •        |   |
| • •        |   |
| • •        |   |
| Quest      | ion 30 (3 marks)  |
|            | wants to take out a home loan to buy a unit. He has saved \$45 000 as a deposit and he ly afford to pay back \$3600 per month. The bank interest rate is 6.8% per annum over ars. |
| Using buy? | the Present Value formula, calculate the most expensive unit that Mark can afford to  |
| ouy:       | $A = a \left\{ \frac{(1+r)^n - 1}{r(1+r)^n} \right\}$   |
| • •        |   |
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# Question 31 (2 marks)

Tabitha purchased a machine for \$60 000. This machine depreciates in value over time. Two methods of depreciation were considered by the company.

| Method 1 — Straight line: The machine is depreciated Method 2 — Declining-balance: The machine is depreciated the machine is depr |   |
|--|---|
| a) Find the value of the machine after 3 years using   | the declining-balance method.             |
|  |   |
|  |   |
| b) Using the straight-line method, how many years value of \$12 000?   | will it take for the machine to reach a 1 |
|  |   |
|  |   |
| 0 4: 22 (0   |   |
| Question 32 (2 marks)  The formula to provide an estimate for blood alcohol co   | ontent for females is:                    |
| $BAC_{Female} = \frac{10N}{5}.$  | −7.5 <i>H</i><br>5 <i>M</i>               |
| where $N$ is the number of standard drinks consumed, $H$ $M$ is the person's weight in kilograms.  | is the number of hours of drinking and    |
| Florence, who weighs 64 kg, has her <i>BAC</i> measured at How many drinks did she have according to the formul  |   |
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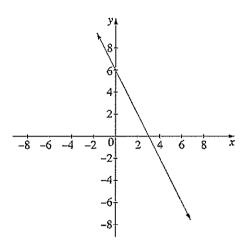
# Question 33 (3 marks)

Joey's car uses 6.3L/100 km.

| a)  | How much petrol does she use to travel 1375 km from Sydney to Adelaide? Answer correct to one decimal place.                        | 1 |
|-----|---|---|
| •   | ,   |   |
|     |   |   |
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|     |   |   |
| b)  | Petrol cost \$1.20/L. How far, to the nearest kilometre, can Joey travel on \$75?   | 2 |
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|     |   |   |
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|     |   |   |
| Que | stion 34 (1 mark)   |   |
|     | k's formula, shown below, is used to calculate the dosage of medication for children aged een 2 and 12, based on the child's build. |   |
|     | $Dosage = \frac{weight in kg \times adult dosage}{70}$  |   |
|     | ug has an adult dosage of 45 ml. Calculate the dosage given for a child who is 11 years of and who weighs 67 kg.                    |   |
|     |   |   |
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#### Question 35 (2 marks)

The graph of a line is shown below.



a) Write the equation of the line in the form y = mx + b.

1

b) When the line with equation y = x + 3 is drawn on the same number plane, these two lines will intersect.

What is the point of intersection of these two lines?

1

.....

#### Question 36 (2 marks)

The table below compares age (in years) and pulse rate (in beats per minute).

|   | а | 5    | 10   | 15   | 20   | 25   | 30   |
|---|---|------|------|------|------|------|------|
| İ | p | 62.6 | 64.1 | 65.9 | 67.6 | 69.0 | 70.4 |

a) Calculate the value of the correlation coefficient, correct to three decimal places.

1

.....

b) Find the equation of the line of best fit, giving your values correct to two decimal places.

.....

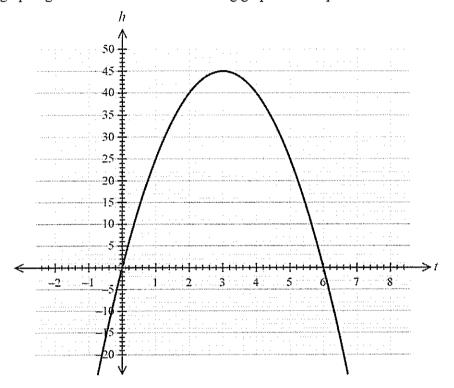
#### Question 37 (3 marks)

Ethan uses the equation below to model the height of a ball tossed into the air from ground level and allowed to fall under gravity (with air resistance ignored).

$$h = 30t - 5t^2$$

where h is the height of the ball in metres and t is the time elapsed in seconds

Ethan uses graphing software to draw the following graph of the equation.



Ethan knows that only part of this curve applies to his model for the height of the ball.

a) Between what values of t does the graph model the height of the ball?

b) What is the maximum height that the ball reaches, AND when did this occur?

1

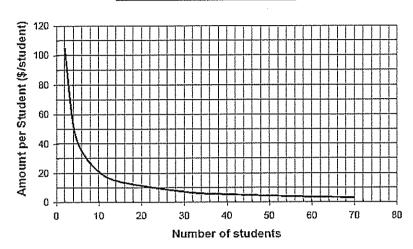
c) For how many seconds is the ball more than 25 metres from the ground?

#### Question 38 (2 marks)

A preschool centre pays \$270 to hire a bus for an excursion. Selina is organising the excursion and has worked out an equation that will determine, depending on the number of students, the amount each student will need to pay to cover the cost of the bus.

The graph below also shows the amount to be paid per student based on the number of students.

#### Cost of the Bus Per Student



The formula used to draw this graph was  $A = \frac{270}{N}$ 

where A = amount per student N = number of students attending the excursion

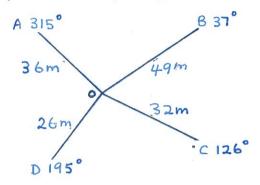
a) Use the graph to find the approximate cost per student if 22 students go on the excursion.
 b) How many students will need to go on the excursion to cover all costs if they each pay \$2.30?

#### Question 39 (2 marks)

The weight of an object on the moon varies directly with its weight on Earth. An astronaut who weighs 84 kg on Earth weighs only 14 kg on the moon. A lunar landing craft weighs 2449 kg when on the moon. Calculate the weight of this landing craft when on Earth.

#### Question 40 (3 marks)

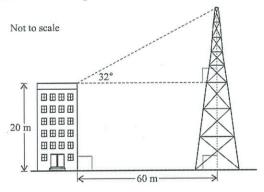
The following notebook entry was made during a compass radial survey of a field.



| a) | Show that the size of angle AOB is 82°.                          | 1 |
|----|--|---|
|    |  |   |
| b) | Find the area of the triangle AOB, correct to one decimal place. | 2 |
|    |  |   |
|    |  |   |

#### Question 41 (2 marks)

The diagram below shows a building and a communications tower. From the top of the building, the angle of elevation of the top of the tower is  $32^{\circ}$ .



| Determine the height of the tower, correct to the nearest metre. |
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# Question 42 (1 mark)

Angela recorded the number of births at a hospital over the period of a week.

| Outcome              | Frequency |
|----------------------|-----------|
| Number of girls born | 144       |
| Number of boys born  | 156       |

| What is the relative f | frequency of a | girl b | eing born? |
|------------------------|----------------|--------|------------|
|------------------------|----------------|--------|------------|

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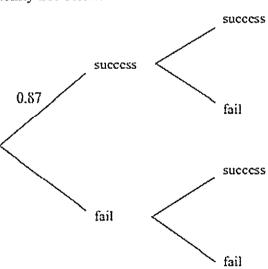
#### Question 43 (4 marks)

A new vaccine has a probability of 0.87 of being successful in preventing the spread of a virus. Two people are selected at random to test the vaccine.

2

2

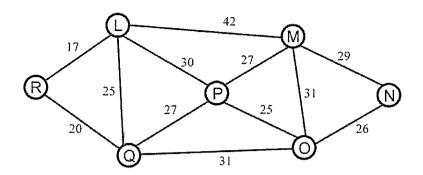
a) Complete the probability tree below.



| b) What is the probability of the vaccine being successful on at least one persons? |  |
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#### Question 44 (3 marks)

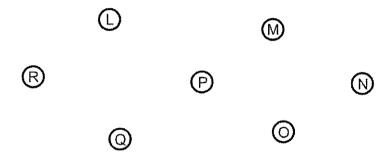
A network of pipes connects nodes labelled L to R. The length of each pipe in kilometres is shown in the diagram below.



The owner of the network wants to reduce the number of pipes but still connect all the nodes.

a) Draw the minimum spanning tree that will achieve the owner's requirement on the set of nodes below.





| b) | What is the minimum length of pipe needed to connect the seven nodes? | ] |
|----|---|---|
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#### Question 45 (4 marks)

The table below shows the tax payable to the Australian Taxation Office for different taxable incomes.

| Taxable income       | Tax on this income                            |
|----------------------|---|
| \$0 - \$18 200       | Nil   |
| \$18 201 - \$37 000  | 19c for each \$1 over \$18 200                |
| \$37 001 - \$80 000  | \$3572 plus 32.5c for each \$1 over \$37 000  |
| \$80 001 - \$180 000 | \$17 547 plus 37c for each \$1 over \$80 000  |
| \$180 001 and over   | \$54 547 plus 45c for each \$1 over \$180 000 |

Santiago has a gross salary of \$65 000. He has tax deductions of \$800 for work related expenses. The Medicare levy that he pays is calculated at 2% of his taxable income.

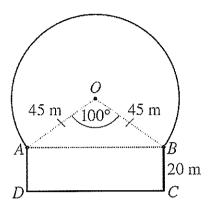
Will Santiago receive a tax refund or will he owe money to the Australian Taxation Office?

Santiago has already paid \$14 200 in tax.

| Justify your answer with appropriate calculations. |  |              |       |       |       |       |   |                       |         |
|--|--|--------------|-------|-------|-------|-------|---|-----------------------|---------|
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# Question 46 (4 marks)

A school playground consists of part of a circle, with centre O, and a rectangle as shown in the diagram below. The radius OB of the circle is 45 m, the width BC of the rectangle is 20 m and LAOB is 100°.



| What is the perimeter of the whole playground, correct to one decimal place? |
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| Section II  | Extra writing space |  |  |  |  |  |
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| If you use this space, clearly indicate which question you are answering. |                     |  |  |  |  |  |
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## Mathematics Standard 2

#### REFERENCE SHEET

#### Measurement

#### Limits of accuracy

Absolute error =  $\frac{1}{2}$  × precision

Upper bound = measurement + absolute error

Lower bound = measurement - absolute error

#### Length

$$l = \frac{\theta}{360} \times 2\pi r$$

#### Area

$$A = \frac{\theta}{360} \times \pi r^2$$

$$A = \frac{h}{2} (a + b)$$

$$A \approx \frac{h}{2} \left( d_f + d_l \right)$$

#### Surface area

$$A = 2\pi r^2 + 2\pi rh$$

$$A = 4\pi r^2$$

Volume

$$V = \frac{1}{3}Ah$$

$$V = \frac{4}{3}\pi r^3$$

#### Trigonometry

$$\sin A = \frac{\text{opp}}{\text{hyp}}, \quad \cos A = \frac{\text{adj}}{\text{hyp}}, \quad \tan A = \frac{\text{opp}}{\text{adj}}$$

$$A = \frac{1}{2}ab\sin C$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$c^2 = a^2 + b^2 - 2ab\cos C$$

$$\cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

#### **Financial Mathematics**

$$FV = PV(1+r)^n$$

#### Straight-line method of depreciation

$$S = V_0 - Dn$$

#### Declining-balance method of depreciation

$$S = V_0 (1 - r)^n$$

### Statistical Analysis

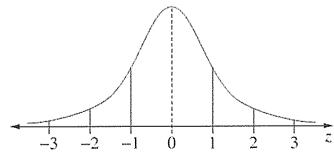
An outlier is a score

less than  $\, Q_1 - 1.5 \times IQR \,$  or

more than  $Q_3$  +  $1.5 \times IQR$ 

$$z = \frac{x - \overline{x}}{s}$$

#### Normal distribution



- approximately 68% of scores have z-scores between -1 and 1
- approximately 95% of scores have z-scores between –2 and 2
- approximately 99.7% of scores have z-scores between –3 and 3



# 2019 Trial Higher School Certificate Examination Mathematics Standard 2

| Stude                        | nt 1              | Vumbe                  | r                      |                |                      |   |                                 |
|------------------------------|-------------------|------------------------|------------------------|----------------|----------------------|---|---------------------------------|
|                              |                   | Se                     | ction I                | – Multip       | le Choice A          | Answer Sheet                                |                                 |
| Allow abou                   |                   |                        |                        |                | vers the quest       | tion. Fill in the resp                      | oonse oval completely.          |
| Sample:                      | Ž                 | 2 + 4 =                | (A)                    | ) <sup>2</sup> | (B) 6<br>B ●         | (C) 8                                       | (D) 9<br>D <b>O</b>             |
| If you think answer.         | you ha            | ve made a              | mistake,               | , put a cro    | ss through th        | e incorrect answer                          | and fill in the new             |
|                              |                   |                        | A                      |                | В                    | c 🔾   | D 🔾                             |
| If you chang<br>indicate the | ge your<br>correc | mind and<br>t answer l | have cro<br>by writing | ssed out v     | d <b>correct</b> and | sider to be the corre<br>I drawing an arrow | ect answer, then<br>as follows. |
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|                              | 3.                | A 🔾                    | В                      | c 🔾            | D 🔘                  |   |                                 |
|                              | 4.                | A 🔾                    | В                      | С              | D 🔾                  |   |                                 |
|                              | 5.                | A 🔾                    | В                      | c 🔾            | D 🔾                  |   |                                 |
|                              | 6.                | $A \bigcirc$           | В                      | С              | D 🔾                  |   |                                 |
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