

# Carlingford High School



## Mathematics Year 10 5.2 Term 2 Test 2019

Student Name: \_\_\_\_\_

*Chen* *Scott*

Circle your Teacher below.

Ms. Aung

Mr Cheng

Mrs Lego

Mr Wilson

*Time allowed: 50 minutes*

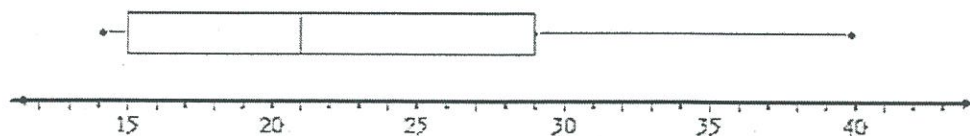
- Complete the examination in blue or black pen.
- Show all necessary working.
- Attempt all questions.

	Data Analysis	Consumer Arithmetic	Total	
Questions	/31	/28		
Total	/31	/28	/59	%

## Data Analysis

1.

(7)



The boxplot represents the ages of 16 people waiting at the bus stop.

Find the following:

- Range =  $40 - 14 = 26$
- Median (Q2) =  $21$
- Upper Quartile (Q3) =  $29$
- Lower Quartile (Q1) =  $15$
- Interquartile Range =  $29 - 15 = 14$
- What percentage of the people were over the age of 29?  $25\%$
- How many people were between 15 and 29?  $\frac{1}{2} \times 16 = 8$

2. A back-to-back stem- and- leaf plot shows the amount of cash (in dollars) carried by a sample of year 11 students at Carlingford High School.

(6)

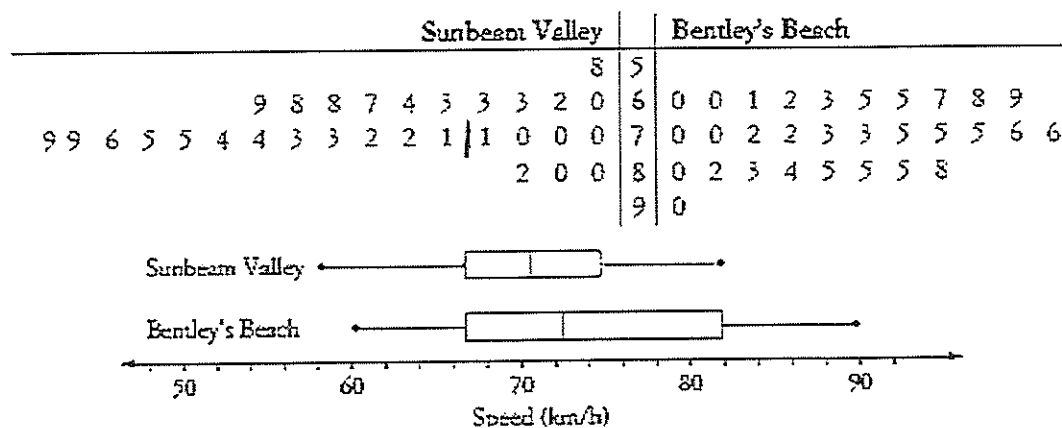
Boys					Girls										
			5	5	3	0	5	5	6	8	9				
		8	5	5	2	0	1	0	2	2	5	5	8	8	9
	9	6	5	5	5	0	0	2	0	5	6	8	8	8	
	8	5	5	4	3	2	0	0	3	0	1	4	5	6	
		5	4	4	2	2	0	4	0	0	5	6			
		6	6	5	4	3	5	0	3	5					
			4	2	2	6	5	5	8						
				5	7	0	4								

- Find the mean amount of cash carried by the girls.  $\$ 31.78$
- Find the median amount of cash carried by the boys.  $\$ 33.50$
- Describe the shape of the distribution for the girls. *positively skewed*
- Find the lower quartile of the boys.  $20$
- Find the upper quartile of the boys.  $45$
- What is the inter quartile range of the boys  $25$

*71  
75 & 85  
Boys*

3. The speeds of cars were monitored along a main road in two different suburbs. The results are shown in the back-to-back stem and leaf plot and parallel boxplots.

(4)



- a) What is the median speed of Sunbeam valley?  $\frac{71+71}{2} = 71$  (1)
- b) What is the mode speed for Bentley's Beach?  $75 \text{ and } 85$  (1)
- (c) In which suburbs do drivers generally drive faster? Give a possible reasons for your answer.

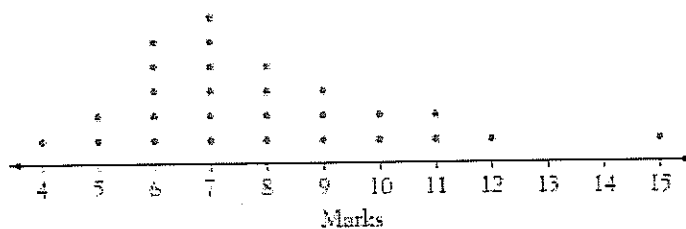
\* Bentley's beach (1)

\* higher median, (1)

\* 25% of drivers drive faster than all drivers in Sunbeam Valley. (1)

4. The results of a maths quiz taken by Year 10 students are displayed below

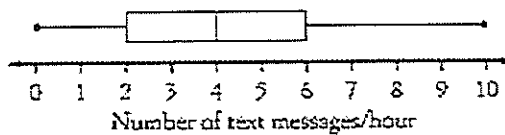
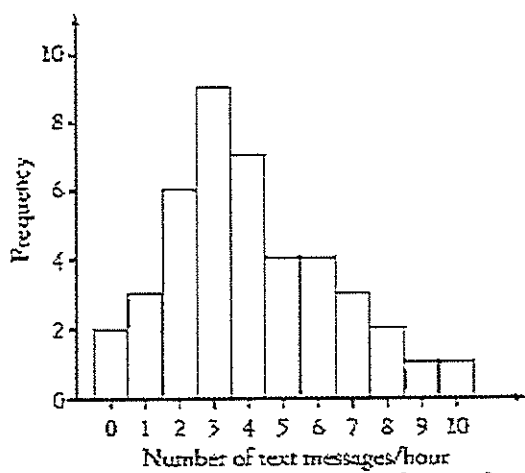
(5)



- a) Find the five point summary for the dot plot {  $4, 6, 7, 9, 15$  } (2)
- b) What is the outlier, if any?  $15$  (1)
- c) Describe the shape of the dot plot.  $\text{skewed right}$  (1)
- d) Find the inter-quartile range.  $9 - 6 = 3$  (1)

5. The number of text messages received per hour by a group of teenagers are displayed below in a frequency histogram and boxplot.

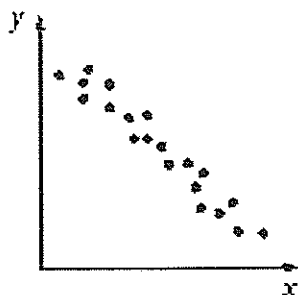
(5)



- a) How many teenagers received less than three messages?  $6 + 3 + 2 = 11$
- b) Find the mode. 3
- c) Find the range.  $10 - 0 = 10$
- d) Find the median. 4
- e) Find the IQR.  $6 - 2 = 4$

6. The results of a Maths test given to four Year 10 classes are shown below;

(2)



Describe the strength and direction of the scatter plot.

strong, negative relation  
✓ (1) ✓ (1)

7.

(2)

a) Describe the meaning of *dependent variable*.

A dependent variable depends on the value of another variable. (1)

b) Which axis is the independent variable?

x-axis (1)

1

- a) i) Calculate the simple interest earned when \$660 is invested for 8 months at 12% p.a.

(2)

$$I = P \times R \times W$$

$$= 660 \times 0.12 \times \frac{8}{12}$$

$$= \$52.80$$

- ii) Find the final amount of the investment at the end of the 8 months.

(1)

$$\text{Final Amount} = \$52.80 + 660$$

$$= \$712.80$$

- b) The interest charged on a loan of \$25 000 over 5 years is \$4375. Calculate the flat rate of interest.

(2)

$$R = \frac{I}{PN}$$

$$= \frac{4375}{25000 \times 5}$$

$$= 0.035$$

$$= 3.5\%$$

- c) i) Find the total amount of the investment if \$2500 is invested at 7.3% p.a. for 3 years with interest compounded annually.

(2)

$$A = P(1+r)^n$$

$$= 2500(1+0.073)^3$$

$$= \$3088.44$$

- ii) Calculate the compound interest earned.

(1)

$$CI = \$3088.44 - \$2500$$

$$= \$588.44$$

- d) Find the amount of **interest earned** if \$3500 is invested for 4 years at 7% p.a. interest, where interest is **compounded quarterly**.

(3)

$$r = 7 \div 4 = 1.75\% \quad n = 4 \times 4 = 16$$

$$= 0.0175$$

$$A = P(1+r)^n$$

$$= 3500(1+0.0175)^{16}$$

$$= 4619.75$$

$$\therefore \text{Interest earned} = 4619.75 - 3500 = \$1119.75$$

- e) Henry has \$5000 in an account earning 14% p.a. interest, compounded yearly. How long will it take for him to double his money (correct to the nearest month)?

(3)

$$10000 = 5000(1+0.14)^n$$

$$2 = 1.14^n$$

$n = \frac{\ln 2}{\ln 1.14}$	$1.14^4 = 1.69$	5 years 3 months
$= 5.29$	$1.14^5 = 1.92$	5 years 4 months
5 years 3 months	$1.14^6 = 2.19$	
	$1.14^{5.1} = 2.00$	

Take

- 2 Angela's car is now worth \$8 670. A year ago it was worth \$10 200.

- (i) Show that the car has depreciated 15% during that year.

(1)

$$A = P(1-r)^n$$

$$8670 = 10200(1-r)$$

$$1-r = \frac{8670}{10200} \quad r = 1 - \frac{8670}{10200}$$

$$= 0.15 = 15\%$$

- (ii) Angela sells her car after a further four years. If the car continues to depreciate at the same rate (15% p.a.), determine its value when she sells it.

(2)

$$A = 10200(1-0.15)^5$$

$$= \$4525.79$$

- (iii) What is the depreciation over the 5 years?

(1)

$$\text{Total depreciation} = \$10,200 - \$4525.79$$

$$= \$5674.21$$

3

Ian purchases a new plasma TV valued at \$4000 by paying a 20% deposit and repaying the balance in equal monthly instalments over 2 years at a flat interest rate of 8.5% p.a.

Calculate:

- a) the amount of deposit paid.

(1)

$$\text{deposit} = \frac{20}{100} \times 4000 = \$800$$

- b) and the amount of balance owing.

(1)

$$\text{Amount owing} = \$4000 - \$800 \\ = \$3200$$

- c) the interest charged on the balance.

(1)

$$I = \frac{8.5}{100} \times 3200 \times 2 \\ = \$544$$

- d) the total to be repaid.

(1)

$$\text{Total to be repaid} = 3200 + 544 \\ = \$3744$$

- e) the amount of each monthly installment.

(1)

$$\text{Monthly instalment} = \$3744 \div 24 \\ = \$156$$

- f) the total amount paid for the TV.

(1)

$$\text{Total Amount} = 4000 + 544 \\ = \$4544$$



4

Peter purchases a new refrigerator for \$1900 on a deferred payment plan. He chooses a deferred payment plan over 2 years. They make no repayments for the first six months, then pay \$135 per month

- a) Calculate the total repayments.

(1)

$$\begin{aligned} \text{Total repayments} &= \$135 \times 18 \\ &= \$2430 \end{aligned}$$

- b) How much interest did he pay?

(1)

$$\begin{aligned} I &= 2430 - 1900 \\ &= 530 \end{aligned}$$

- c) What percentage of the purchase price is paid in interest?

(2)

$$\begin{aligned} \% I &= \frac{530}{1900} \times 100 \\ &= 27.89\% \end{aligned}$$

End of Examination