

Carlingford High School



Mathematics

Modified

Year 9 Term 4 Examination

2018

Name: _____

Class: 9MA_1_1

Teacher: Ms Strilakos

- Time allowed: 50 minutes
- Calculators allowed
- Show all necessary working
- Use blue or black pen to write your answers

Topic	INDICES	RATIO AND RATES	TOTAL
TOTAL	/57	/46	/103

INDICES

Q.1

(i) How many times is the pronumeral

k multiplied by itself in the following statement?

$$k \times k \times k \times k$$

4

(ii) Hence complete the following statement by writing the correct number in the box for the index:

$$k \times k \times k \times k = k^{\boxed{4}}$$

(Expanded form)

(Index form)

[2]

(2)

Q.2 Express each of the following in index form:

(i) $a \times a \times a \times a$

$$a^4$$

(ii) $r \times r \times r \times s \times s$

$$r^3 s^2$$

(iii) $2 \times 4 \times y \times y \times y \times y$

$$8y^4$$

(iv) $3 \times m \times m \times 5 \times m$

$$15m^3$$

(4)

[4]

Q.3 Simplify:

(i) $3^4 \times 3^2 = 3^{\boxed{6}}$

(ii) $n^3 \times n^5 = n^8$

(iii) $p^4 \times p = p^5$

(iv) $3a^2 \times a^5 = 3a^7$

(v) $3m^3 \times 4m^6 = \underline{3} \times \underline{4} m^{\boxed{9}}$

$$= \underline{12} m^{\boxed{9}}$$

(vi) $4w^3 \times 2w^4 = 8w^7$

(vii) $-5m^2n^3 \times 4m^4n^3 = -20m^6n^6$

[4+2+2+2]

(10)

Q.4 Simplify:

(i) $y^5 \div y^2 = y^3$

(ii) $\frac{c^8}{c^3} = c^5$

(iii) $\frac{y^7}{y^{-2}} = y^9$

(iv) $15c^4 \div 5c^2 = 3c^2$

(v) $12m^8 \div 3m^4 = 4m^4$

(vi) $18a^{12} \div (-2a^5) = -9a^7$

(vii) $\frac{20b^7}{4b^2} = 5b^5$

(11)

[1+1+1+2+2+2+2]

Q.5 Simplify:

(i) $(m^3)^4 = m^{12}$ |

(ii) $(2a^2)^3 = 8a^6$ | 2

[1+2]

(3)

Q.6 Simplify:

(i) $\left(\frac{3}{m^2}\right)^4 = \frac{81}{m^8}$ |

(ii) $\left(\frac{w^8}{4}\right)^2 = \frac{w^{16}}{16}$ | (2)

[2]

Q.7 Write with a positive index:

(i) $3^{-4} = \frac{1}{3^4}$ |

(ii) $4^{-2} = \frac{1}{4^2}$ |

(iii) $(2m)^{-7} = \frac{1}{(2m)^7} = \frac{1}{2^7 m^7}$ |

(iv) $5w^{-4} = \frac{5}{w^4}$ |

[4]

(4)

Q.8 Find the value of:

(i) $3^0 = 1$ |

(ii) $y^0 = 1$ |

(iii) $6m^0 = 6$ |

(iv) $(3a)^0 = 1$ |

(4)

[4]

Q.9 Simplify:

(i) $4^6 \times 4^{-2} = 4^4$ |

(ii) $x^{-2} \times x^{-5} = x^{-7}$ |

(iii) $w^3 \times w^0 = w^3$ |

[3]

(3)

Q.10 Simplify:

(i) $(2^4)^3 = 2^{12}$ |

(ii) $(4^5)^2 = 4^{10}$ |

(iii) $(7^{-2})^0 = 1$ |

(iv) $(x^{-4})^{-2} = \frac{1}{(x^{-4})^2} = x^8$ |

[4]

(4)

Q.11 Round each number to three significant figures:

(i) $48\,231 = 48\,200$

(ii) $68\,473 = 68\,500$

(iii) $2\,087\,342 = 2\,090\,000$

(iv) $0.00264853 = 0.00265$

[4]

Q.12 Write each number using scientific notation:

(i) $14\,000 = 1.4 \times 10^4$

(ii) $624\,000 = 6.24 \times 10^5$

(iii) $0.000425 = 4.25 \times 10^{-4}$

[3]

Q.13 Write each number as a basic numeral:

(i) $4 \times 10^2 = 400$

(ii) $3.8 \times 10^3 = 3\,800$

(iii) $6 \times 10^{-4} = 0.0006$

[3]

RATIOS

Q.1 Write each ratio in simplest form:

(i) $10 : 30 = 1 : 3$

(ii) $6 : 12 = 1 : 2$

(iii) $24 : 4 = 6 : 1$

(iv) $0.2 : 0.5 = 2 : 5$

(v) $0.04 : 6 = 4 : 600 = 1 : 150$

[1+1+1+2+2]

7

Q.2 Simplify each ratio, remembering to make the units **within** the ratio the same first:

(i) $6\text{mm} : 1\text{cm}$ (Write the cm as mm first)

$= 6 : 10$

$= 3 : 5$

(ii) $480\text{m} : 1\text{km}$ (Change the km to m first)

$= 480 : 1000$

$= 48 : 100$

$= 12 : 25$

(iii) $\$2.40 : \3.00

$= 24 : 30$

$= 4 : 5$

(iv) $36\text{sec} : 2\text{min}$

$= 36 : 120$

$= 3 : 10$

- (v) 9 months : 3 years

$$= 9 : 36$$

$$= 1 : 4$$

[5 X 2]

- Q.3 Jennifer and Maurice share the rent of a business office in the ratio 4 : 5.

The rent is \$3 600 each month.

- (i) How many parts are there in total in the ratio 4 : 5?

9

- (ii) What is the value in dollars (\$) of one part?

$$3600 \div 9 = 400$$

- (iii) How much of the total rent does Jennifer pay?

$$4 \times 400 = \$1600$$

[3]

- Q.4 Complete each of the following sentences:

- (i) \$2 for 2 oranges is a rate of

\$ 1 for 1 orange

- (ii) \$4 for 8 apples is a rate of

50 cents for 1 apple

- (iii) 666km in 6 hours is a rate of

111 km/hr

- (iv) \$20 for 10 kg of flour is a rate of

\$ 2/kg

- (v) \$48 for 4 hours work is a rate of

\$ 12/hr

- (vi) \$784 for 4 days at a hotel is

\$ 196/day

[6]

- Q.5 A plumber took six hours to complete a job.

If he charged \$576 for the job, what was the rate he charged per hour?

$$576 \div 6 = \$96/\text{hr.}$$

[2]

- Q.6 Cordial is mixed with water in the ratio 1 : 4.

If 30 ml of cordial is used to make a glass of cordial, how many ml of water must be used?

C:W

$$= 1 : 4$$

$$= 30 : 4 \times 30$$

∴ 120ml of water must be used

[1]

- Q.7 Ken and Peter share profits from a garage sale in the ratio 4 : 7.

If Ken receives \$248, how much does Peter receive?

$$4:7 = 248:P$$

$$\frac{248}{4} = 62 \quad \therefore P = 7 \times 62 = 434$$

[2]

- Q.8 A tree is drawn to a scale of 1 : 50.

If its height is drawn as a scaled height of 10cm

- (i) how many cm tall is the tree in real life?

$$1:50 = 10 \text{ cm} : x$$

$$x = 500 \text{ cm} = 5 \text{ m}$$

$$500 \text{ cm}$$

- (ii) What is this height in metres?

$$5 \text{ m}$$

[2]

- Q.9 \$8400 is to be divided between Sam and Jed in the ratio 7 : 5.

- (i) How many parts in this ratio?

$$12$$

- (ii) What is the value of one part?

$$8400 \div 12 = 700$$

- (iii) How much does each boy get?

$$\text{Sam: } 7 \times 700 = 4900$$

$$\text{Jed: } 5 \times 700 = 3500$$

[4]

- Q.10 If \$2800 is to be shared between three people in the ratio 2 : 5 : 7

- (i) How many parts in the ratio?

$$14$$

- (ii) What is the value of one part?

$$2800 \div 14 = 200$$

- (iii) How much is the largest share?

$$7 \times 200 = 1400$$

- (iv) How much is the smallest share?

$$2 \times 200 = 400$$

[4]

- Q.11 A car travels a distance of 240 km in 2 hours.

- (i) How far is it travelling in one hour?

$$120 \text{ km}$$

- (ii) How far does it travel in one minute?

$$120 \div 60 = 2 \text{ km/min.}$$

[2]

Q.12 Lilli takes one hour to walk 4 km and another one hour to cycle 8 km.

(i) What is the total distance travelled?

12 km

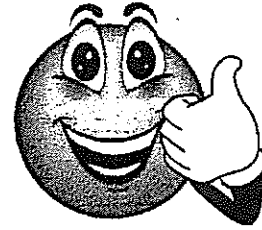
(ii) What was the total time taken to travel this total distance?

2 hrs.

(iii) What was her average speed across the total distance?

$$\frac{12}{2} = 6 \text{ km/hr.}$$

[3]



End of Test

