## M ath D iagnostic T est

20	Q	uestions
35	М	inutes

For questions in the Q uantitative C om parison form at ("Q uantity A" and "Q uantity B " given), the answ er choices are alw ays as follow s: (A) Q uantity A is greater. (B) Q uantity B is greater. (C) The two quantities are equal. (D) The relationship cannot be determined from the information given. For questions follow ed by a num eric entry box you are to enter your ow n answ er in the box. For questions follow ed by fraction-style num eric entry boxes enter your answ er in the form of a fraction. You are not required to reduce fractions. For exam ple, if the answ er is 1/4, you may enter 25/100 or any equivalent fraction. A II num bers used are real num bers. A II figures are assum ed to lie in a plane unless otherw ise indicated.G eom etric figures are not necessarily draw n to scale.Y ou should assum e,how ever,that lines that appear to be straight are actually straight, points on a line are in the order show n, and all geom etric objects are in the relative positions show n.C oordinate system s, such as xy-planes and num ber lines, as well as graphical data presentations such as bar charts, circle

1.

<u>Q uantity A</u>

0.01410

<u>Q uantity B</u>

0.0141

2.A certain bookstore sells only paperbacks and hardbacks. Each of the 200 paperbacks in stock sells for a price betw een \$8 and \$12, and each of the 100 hardbacks in stock sells for a price betw een \$14 and \$18.

graphs, and line graphs, are drawn to scale. A symbol that appears more than once in a

question has the sam e m eaning throughout the question.

Q uantity A Q uantity B

The average price of the books in stock at the bookstore

\$9.99

3.

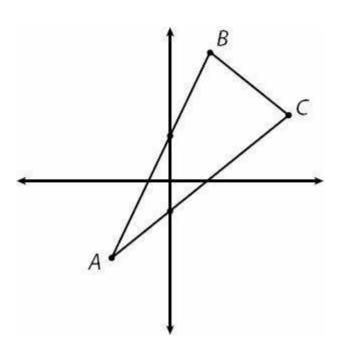
## Q uantity A

#### Q uantity B

$$\frac{x-3}{-x}$$

$$\frac{3-x}{-x}$$

4.



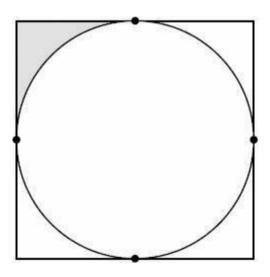
Q uantity A

Q uantity B

The slope of line segm ent AB

The slope of line segm ent AC

5.



In the figure above, the circle is inscribed a square that has area 16.

### Q uantity A

**Q** uantity B

The area of the shaded region

1

6.

8.

In Triangle ABC, AB = 12, AC = 10, and BC = 5.

### Q uantity A Q uantity B

The m easure of angle A

The m easure of angle C

52

- 9.If X is a positive integer, how m any integer values are possible for x?
  - (A)5
  - (B)6
  - (C) 7
  - (D)8
  - (E) 10
- 10.If 3x + 6y = 69 and 2x y = 11, w hat is the value of y?



11.If 
$$7^9 + 7^9 + 7^9 + 7^9 + 7^9 + 7^9 + 7^9 = 7^X$$
, then  $x = 7^X$ 

- (A)9
- (B) 10
- (C) 12
- (D) 63
- $(E) 9^{7}$
- 12.In a certain election race, all of the 8,400 votes were cast for either C andidate A or C andidate B. If votes for C andidate A and votes for C andidate B were cast in a 4 to 3 ratio, how m any votes were cast for C andidate A?





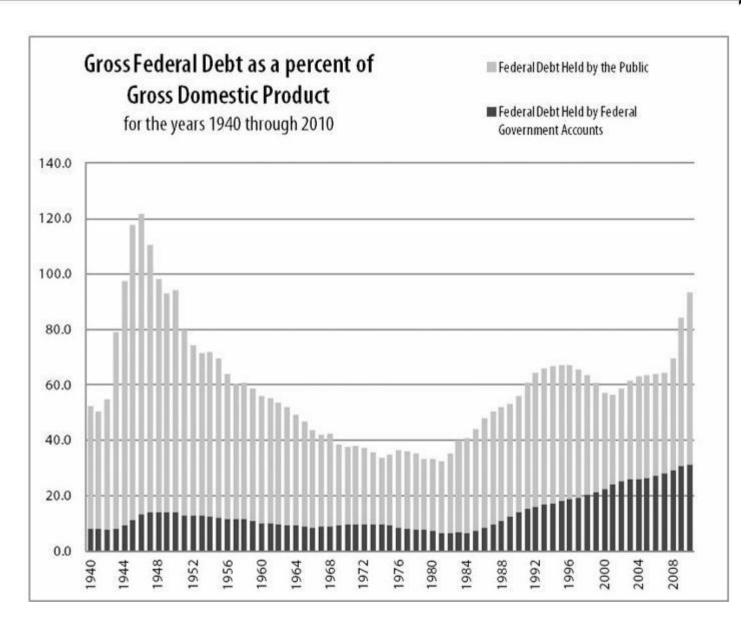
 $14.a^3b^4c^7 > 0.W$  hich of the follow ing statem ents m ust be true? Indicate <u>all</u> such statem ents.

ab is negative

abc is positive

ac is positive

Q uestions 15-17 are based on the following chart.



15.In how m any years betw een 1940 and 2010,inclusive,did the gross federal debt exceed the gross dom estic product?

- (A)3
- (B) 4
- (C) 5
- (D)6

(E) m ore than 6
16.D uring w hich decade w as federal debt held by federal governm ent accounts closest to half of all federal debt?
(A ) 1960's (B ) 1970's (C ) 1980's (D ) 1990's (E) 2000's
17.A t its highest point,w hat w as the approxim ate ratio of federal debt held by the public to that held by federal governm ent accounts?
(A) 1:1 (B) 2:1 (C) 5:1 (D) 8:1 (E) 12:1
18.A num ber x is 32% of a num ber y. If y is 20% of z, then, expressed in term s of $x, z =$
(A) $0.064x$ (B) $0.64x$ (C) $6.4x$ (D) $0.064$
(E) $\frac{x}{0.64}$
19.If $S^2 > T^2$ , w hich of the follow ing m ust be true?
(A) $S > T$ (B) $S^2 > T$ (C) $ST > 0$ (D) $ S  >  T $ (E) $ST < 0$
20.In a certain nation, every citizen is assigned an identification num ber consisting of the last two digits of the person's birth year, followed by five other num erical digits. For instance, a person born in 1963 could have the identification num ber 6344409. How many identification num bers are possible for people born in the years 1980–1982, inclusive?
(A) 360 (B) 2,880 (C) 288,800 (D) 300,000 (E) 2,400,000

## Q uantitative D iagnostic T est: A nsw er T ally Sheet

Q uestion #	Y our A nsw er	C orrect A nsw er	Tally your correctly answ ered questions. N o partial credit!	F ind m ore questions like this in chapter:
1		(C)		11
2		(A)		17
3		(D)		15
4		(A)		28
5		(B)		29
6		(B)		14
7		(D)		8
8		(B)		27
9		(B)		13
10		7		8
11		(B)		14
12		4,800		20
13		917		15
14		III only		15
15		(A)		24
16		(E)		24
17		(D)		24
18		(D)		12,19
19		(D)		9,15
20		(D)		23
R aw V erbal Score: (# of quant questions answ ered correctly)		uant questions		

# Q uantitative D iagnostic T est: Scoring G uide

R aw Q uantitative Score	Q uantitative R easoning D iagnostic Scaled Score
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-	
20	169 – 170
19	167 – 169
18	164 – 166
17	161 – 163
16	159 – 161
15	157 – 159
14	155 – 157
13	153 – 155
12	152 – 154
11	150 – 152
10	149 – 151
9	147 – 149
8	145 – 147
7	143 – 145
6	142 – 144
5	139 – 141
4	136 – 138
3	133 – 135
2	130 – 132
1	130 – 131
0	130

#### NOTES:

D iagnostic Scaled Score is approxim ate.

- (a) If your time for this diagnostic section exceeded the 35-m inute guideline, this approximate score may not be indicative of your performance under standard time conditions.
- (b) Scaled Score depends not only on how m any ques-tions w ere answ ered correctly (R aw Score), but also on the overall difficulty of the set of questions. This diagnostic test approxim ates the difficulty of the official G R E <sup>®</sup> revised G eneral Test.

## M ath D iagnostic T est A nsw ers

1.**(C)**.In a repeating decim al, the portion under the bar repeats w ithout end. In Q uantity A, the portion "1410" repeats, after an initial 0.0 that does not repeat. In Q uantity B, the portion "0141" repeats, starting im m ediately after the decim al. To compare, w rite out m ore digits of each decim al:

Q uantity A:0.0141014101410... Q uantity B:0.0141014101410...

The two numbers are identical; Quantity A and Quantity B are simply different ways of writing the same number.

2.(A ).B ecause there are twice as m any paperbacks as hardbacks in stock, the overall average price will be closer to the price of the paperbacks than the price of the hardbacks. How ever, the fact that the problem gives price *ranges* instead of prices complicates m atters a bit. C alculate the low est possible overall average and the highest possible overall average to see whether that average can be both low er and higher than \$9.99.

To calculate the low est possible overall average, assume the low est price for all paperbacks and all hardbacks (\$8 and \$14, respectively). Note that there are twice as many paperbacks as hardbacks, which essentially double-weights the \$8:

$$\frac{200(\$8) + 100(\$14)}{200 + 100} = \frac{2(\$8) + 1(\$14)}{3} = \frac{\$30}{3} = \$10$$

This m inim um price is already greater than \$9.99, so the m axim um price w ould also be greater, and there is no need to calculate it.

Q uantity A is greater.

3.(D ). Since 2 < x < 4, test values betw een 2 and 4 in both Q uantities to see which Q uantity is larger for each example. You must ALW AYS test more than one value to determine the answer to a Q uantitative C omparison, as you should try to prove (D), or at least test whether you can.

If 
$$x = 2.5$$
, Q uantity  $A = \frac{2.5 - 3}{-5} = \frac{-0.5}{-5} = \frac{5}{-1} = \frac{1}{-1}$  and Q uantity  $A = \frac{3 - 2.5}{-1} = \frac{0.5}{-1} = \frac{-1}{-1}$ . In this case, Q uantity A is larger.

B efore just random ly trying other values betw een 2 and 4,try to strategize: could you find an exam ple in w hich Q uantity B is greater? Since the two Q uantities have the sam e denom inator, focus on the num erators. x - 3 is positive w hen x > 3 and negative w hen x < 3. Since the first num ber tested w as less than 3, next try som ething greater than 3.

If 
$$x = 3.5$$
, Q uantity  $A = \frac{3.5 - 3}{-3.5} = \frac{0.5}{-3.5} = \frac{-5}{35} = \frac{-1}{7}$  and Q uantity

 $B = \frac{3-x}{-x} = \frac{3-3.5}{-3.5} = \frac{-0.5}{-3.5} = \frac{5}{35} = \frac{1}{7}$  In this case,Q uantity B is larger.(N ote: you could have stopped calculating the exact values of Q uantity A and Q uantity B for this exam ple once it became clear that Q uantity A w as negative and Q uantity B w as positive.)

A Iternatively, it would also be strategic to think about what number, if any, could make the two quantities equal. If x = 3, Quantity A = Q uantity B = 0 because both numerators will be 0 and 0 divided by any non-zero number is just 0.

Since Q uantity A is greater than Q uantity B for som e exam ples of x w here 2 < x < 4, but Q uantity B is greater than Q uantity A for other exam ples w here 2 < x < 4, the correct answ er is (D).

4.(A ).W hile there are no num bers on the graph, both lines have clearly positive slopes (the lines rise upw ard w hen reading from left to right) and segm ent AB is clearly steeper than segm ent AC. Thus, segm ent AB has a greater slope.

W hile you should be cautious about m aking assum ptions on the G R E, the fact that the two lines form two sides of a triangle and meet at vertex A shows that the lines are not parallel, and segment AB, which rises above segment AC to the right of their meeting point, is definitely steeper.

5.**(B)**.If the area of the square is 16,then the side of the square is 4. Since the circle is inscribed in the square,its diam eter is 4 and its radius is 2. Since the area of a circle is  $\pi r^2$ , the area of this circle is  $4\pi$ . Thus, the combined area of the four "corners," outside the circle but inside the square, is 16 -  $4\pi$ . The shaded region is one of these four

identical "corners," so the area of the shaded region is  $\frac{16-4\pi}{4}=4-\pi\approx 4-3.14=0.86$  ,which is less than 1.

Q uantity B is greater.

6.**(B).**Since both quantities have the sam e exponent as well as at least one *b* inside the parentheses, one way to compare the quantities is to distribute that exponent.

Q uantity A: 
$$(5b) = 5$$
 b  
 $2a$  a a a  
Q uantity B:  $(b) = (b \times b) = b$  b

B ecause  $b^{a}$  is positive (i.e.,a positive base to a positive pow er) and com m on to both quantities,it can be ignored or canceled from both.

Q uantity A: 5<sup>a</sup>

Q uantity B:  $b^{a}$ 

B ecause the positive exponent is com m on to both quantities, a larger base indicates the greater quantity. B ecause b > 5, Q uantity B is greater.

7.(D).FO IL the term s in Q uantity A:

$$(5 + a)(3 + a) = 15 + 5a + 3a + a^2 = a^2 + 8a + 15.$$

Since  $a^2$  and 15 appear in both quantities, elim inate them .

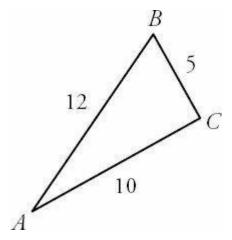
Q uantity A = 8a

Q uantity B = 2a

If a is positive,Q uantity A is greater. If a is negative,Q uantity B is greater. If a is zero, the two quantities are equal. W ithout inform ation about a, it cannot be determined which quantity is greater.

(N ote also, because neither quantity is set equal to zero or any other num ber, you cannot actually "solve" either quantity to get roots or solutions for a.)

8.(B).B egin by draw ing the triangle described by the text and labeling the sides:



A ccording to the properties of triangles, the longer the side opposite an angle, the larger the angle itself m ust be. Since angle A opens to the shortest side length 5 but angle C opens to the longest side length 12, it m ust be true that angle C > angle A . Thus, Q uantity B is greater.

52

9.**(B).**If x is a positive integer, then x is a factor of 52 (i.e., x divides evenly into 52). This question can m ost easily be solved by listing factor pairs for 52, as listing in pairs will help prevent om issions. Each pair multiplies to 52.

The factors of 52 are:

1 & 52

2 & 26

4 & 13

H ow can you be sure this list is complete? Looking down the left column,1 and 2 m ade the list, then 3 didn't divide evenly into 52, then 4 did. Since 4 pairs with 13, check the other integers between 4 and 13. Since 5,6,7,8,9,10,11, and 12 don't divide evenly into 52, this list is complete. There are 6 factors, so the answer is (B).

10.7.M ultiply each term of the second equation by 6: 12x - 6y = 66.W hy do this? B ecause the first equation has a

6y, and the y term s will now cancel when the equations are added.

N ew second equation: 12x - 6y = 66+ First equation: 3x + 6y = 69Sum: 15x = 135x = 9

Plug x = 9 back into an original equation to get y.

$$2x - y = 11$$
  
 $2(9) - y = 11$   
 $18 - 11 = y = 7$ 

In sum m ary, x = 9 and y = 7.B e sure to answ er for y, not x.

11.**(B).**Factor  $7^9$  out of  $7^9 + 7^9 + 7^9 + 7^9 + 7^9 + 7^9 + 7^9$  to get:

$$7^9 (1 + 1 + 1 + 1 + 1 + 1 + 1) = 7^9 (7)$$

O r,just count that there are seven  $7^9$ 's in the original sum ,w hich can be w ritten as  $7 \times 7^9$ .

Since  $7^9$  (7) is the sam e as  $7^9$  (7<sup>1</sup>), sim plify further:  $7^9$  (7<sup>1</sup>) =  $7^{(9+1)}$  =  $7^{10}$ . Thus, x = 10.

N ote: it is N O T correct to sim ply add the original exponents together.W hen adding or subtracting exponential expressions with the same base, it is not possible to directly combine exponents. Factoring out is the correct procedure.

12.**4,800.** If votes for C andidate A and votes for C andidate B w ere in a 4 to 3 ratio, then for every 4 votes C andidate A got, C andidate B got 3.Y ou can think of these votes as existing in "sets" of 7 votes.

D ivide 8,400 by 7 to get 1,200. Thus, the votes were cast in 1,200 "sets" of 7. In each "set," the votes went A A A B B B (4 votes for A ,3 for B). Thus, the total number of votes for A is 1,200  $\times$  4 = 4,800.

13.**917.**There m ust be a trick to this,as it w ould be im possible to sum so m any num bers under G R E tim e constraints, even w ith a calculator. To see the trick, try an exam ple w ith m uch sm aller num bers. For instance, w hat is the sum of all the integers from -2 to 4, inclusive?

NEW EXAMPLE: 
$$2 + 1 + 6 + 1 + 2 + 3 + 4 = 7$$

That is,-2 and 2 cancel,-1 and 1 cancel,and 0 has no im pact on the sum .So the sum is simply the leftover num bers at the end,3 + 4 = 7.

Sim ilarly, in the set -457,-456 ... 0 ... 456,457,458,459, all the integers from -457 to 457 cancel each other out. O nly 458 and 459 rem ain. The sum is 458 + 459 = 917.

14.**III only.**Since  $b^4$  m ust be positive, if  $a^3b^4c^7$  is positive,  $a^3c^7$  m ust also be positive. Since putting an *odd* exponent on a num ber doesn't change w hether the num ber is positive or negative, ac m ust be positive, so Statem ent III is true. The other statem ents require know ledge of the sign of b, w hich is not know n here, since the even exponent "hides" w hether the underlying base is positive or negative.

15.(A). The chart expresses gross federal debt as a percent of gross dom estic product, so federal debt exceeded gross dom estic product in any year in w hich the value of the graph rose above 100. Only during 3 years in the 1940s does the graph extend above 100.

16.**(E).**Federal debt held by federal governm ent accounts would be half of all federal debt in any year in which the dark, bottom portion of the bar equaled the lighter, top portion. A Ithough it never actually reached 50% of the total federal debt, the dark portion of the bar came closest to equaling the light portion during the 2000s.

17.**(D).**The ratio of federal debt held by the public to that held by federal governm ent accounts for any given year would be the measure of the lighter,top bar over the measure of the darker,bottom bar for that year.(To get the measure of the lighter,top bar,you must subtract the value of the darker,bottom bar.)

W hile the federal governm ent accounts percentage hovered near the low teens throughout m ost of the graph, debt held by the public rose above 100% during portions of the 1940s. Identify the year in w hich the lighter, top bar is the largest in comparison to the darker, low er portion. In this chart, it happens to be the tallest bar overall, w hich w as 1946, although it's not necessary to identify the exact year.

Total bar: 120 (actually a bit m ore) D ark,bottom bar: 15 (or a bit less)

Light,top bar: 120 (or m ore) - 15 (or less) = 105 (or a bit m ore)

The ratio is thus 105 (slightly m ore): 15 (m aybe less), w hich is 7 : 1 (or a bit higher). A m ong the given options, this ratio is closest to 8 : 1.

18.**(D).** Translate the percent relations in the problem into algebraic statem ents. First, "a num ber x is 32% of a num ber y" becomes

$$x = 0.32y$$

Sim ilarly, "y is 20% of z" becomes

$$y = 0.2z$$

Substituting for y from the second equation into the first elim inates y and gives the following relationship betw een x and z:

x = 0.32(0.2z)

x = 0.064z

Finally, the problem asks for z in term s of x, so isolate the variable z by dividing both sides of the equation by 0.064.

$$z = \frac{x}{0.064}$$

19.**(D ).**The square root of a squared variable is equal to the absolute value of that variable:  $\sqrt{x^2} = |x|$ , not x. So, taking the square root of both sides of this inequality results in |S| > |T|. A nsw er choice (A) does not have to be true because S could be negative while T is positive. For example, if S = -5 and T = 4, then  $S^2 > T^2$ . Testing fractions in answ er choice (B) shows that it does not have to be true. If  $S^2 = 1/9$  and  $T^2 = 1/16$ , then T = 1/4 or -1/4. 1/4 is greater than 1/9, which means that T can be greater than  $S^2$ . A nsw er choice (C) does not have to be true because S and T could have opposite signs. A nsw er choice (E) does not have to be true because S and T could have the same sign.

20.**(D).**This is a com binatorics problem in w hich *order m atters* (as it alw ays does w ith passcodes,ID codes,etc.) Since the identification num bers each have 7 digits,draw 7 slots.In each slot,list the num ber of possibilities for that slot.

Since the question asks only about identification num bers for people born in 1980,1981,and 1982,the identification num bers m ust begin w ith 80,81,or 82. Thus, only 8 (1 option) can go in the first slot. O nly 0,1,or 2 (3 options) can go in the second slot.

1 3 \_\_\_\_\_\_

N ote that there is no rule against repeating a num ber in an identification num ber (the problem gives the exam ple "a person born in 1963 could have the code 6344409"), so each rem aining slot can each contain any of the digits 0–9 (10 options).

1 3 10 10 10 10 10

This fundam ental counting principle states that the total num ber of choices is equal to the product of the independent choices. To calculate the answ er, multiply  $1 \times 3 \times 10 \times 10 \times 10 \times 10 \times 10 = 300,000$ .

A Iternatively, note that for each birth year, the part of the identification num ber unique to the individual is a 5-digit num ber. These could be 00000-99999 (99,999 + 1 = 100,000 options). There are 100,000 possible num bers for each of 3 years, or 300,000 identification num bers possible.