

KISHINCHAND CHELLARAM COLLEGE, Mumbai - 20.

FY / SY / TY B. Sc. (I. T.) Semester

Practical 1

1 A

(i) Addition

clc()

//Define complex numbers

a1 = 2;

b1 = 1;

a2 = 1;

b2 = 2;

z1 = complex(a1, b1);

z2 = complex(a2, b2);

//mathematical operation

z3 = z1 + z2;

a3 = real(z3);

b3 = imag(z3);

//plot

figure(0)

clf()

hf.background = 2;

ha = gca()

ha.data_bounds = [-5, -5, 5, 5];

xgrid();

plot([0 a1], [0 b1], 'b', 'LineWidth', 3)

plot([0 a2], [0 b2], 'r', 'LineWidth', 3)

plot([0 a3], [0 b3], 'g', 'LineWidth', 3)

xlabel('Real axis (Re)', 'FontSize', 2)

ylabel('Imaginary axis (Im)', 'FontSize', 2)

legend('\$\backslash Large \{z_1\}\$', '\$\backslash Large \{z_2\}\$', '\$\backslash Large \{z_3\}\$')

plot(0, 0, 'sk')

```
plot(a1, b1, 'sk')
```

```
plot(a2, b2, 'sk')
```

```
plot(a3, b3, 'sk')
```

```
xstring(a1, b1, '$\\Large z_1 = 2+i$')
```

```
xstring(a2, b2, '$\\Large z_2 = 1+2i$')
```

```
xstring(a3, b3, '$\\Large z_3 = 3+3i$')
```

// calculate exp form

```
r1 = Sqr t (a1^2 + b1^2);
```

```
r2 = Sqr t (a2^2 + b2^2);
```

```
r3 = Sqr t (a3^2 + b3^2);
```

```
phi1 = atan(b1/a1) * 180/%.pi;
```

```
phi2 = atan(b2/a2) * 180/%.pi;
```

```
phi3 = atan(b3/a3) * 180/%.pi;
```

// display polynomial and polar parameters

```
mprintf('%.s\t%.s\t%.s\t%.s\n', 'a', 'b', 'r', 'phi')
```

```
mprintf('%.4.2f\t%.4.2f\t%.4.2f\t%.4.2f\n', a1, b1, r1, phi1)
```

```
mprintf('%.4.2f\t%.4.2f\t%.4.2f\t%.4.2f\n', a2, b2, r2, phi2)
```

```
mprintf('%.4.2f\t%.4.2f\t%.4.2f\t%.4.2f\n', a3, b3, r3, phi3)
```

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(ii) Subtraction

dc()

// Define complex numbers

a1 = 2 ;

b1 = 1 ;

~~a2 = 1 ;~~

b2 = 2 ;

z1 = complex(a1, b1);

z2 = complex(a2, b2);

// mathematical operation

z3 = z1 + z2

a3 = real(z3);

b3 = imag(z3);

// plot

figure(0)

clf()

hf.background = 2;

ha = gca()

ha.data_bounds = [-5, -5, 5, 5];

xgrid();

plot([0 a1], [0 b1], 'b', 'LineWidth', 3)

plot([0 a2], [0 b2], 'r', 'LineWidth', 3)

plot([0 a3], [0 b3], 'g', 'LineWidth', 3)

xlabel('Real axis (Re)', 'FontSize', 2)

ylabel('Imaginary axis (Im)', 'FontSize', 2)

legend('\$\backslash Large \{z_1\}\$', '\$\backslash Large \{z_2\}\$', '\$\backslash Large \{z_3\}\$')

plot(0, 0, 'sk')

plot(a1, b1, 'sk')

plot(a2, b2, 'sk')

```

plot(a3,b3,'sk')
xstring(a1,b1,'$ \Large {z_1} = 2 + i $')
xstring(a2,b2,'$ \Large {z_2} = 1 + 2i $')
xstring(a3,b3,'$ \Large {z_3} = 3 + 3i $')

```

// calculate exp from

```

r1 = sqrt(a1^2 + b1^2);
r2 = sqrt(a2^2 + b2^2);
r3 = sqrt(a3^2 + b3^2);
phi1 = atan(b1/a1)*180/%pi;
phi2 = atan(b2/a2)*180/%pi;
phi3 = atan(b3/a3)*180/%pi;

```

// display polynomial and polar parameters

```

mprintf(' %s \t %s \t %s \t %s \n', 'a', 'b', 'r', 'phi')
mprintf(' %.4.2f \t %.4.2f \t %.4.2f \t %.4.2f \n', a1, b1, r1, phi1)
mprintf(' %.4.2f \t %.4.2f \t %.4.2f \t %.4.2f \n', a2, b2, r2, phi2)
mprintf(' %.4.2f \t %.4.2f \t %.4.2f \t %.4.2f \n', a3, b3, r3, phi3)

```

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(iii) Multiplication

clc()

//Define complex numbers

a1 = 2;

b1 = 1;

a2 = 1;

b2 = 2;

z1 = complex(a1, b1);

z2 = complex(a2, b2);

//mathematical operation

z3 = z1 * z2;

a3 = real(z3);

b3 = imag(z3);

//plot

figure(0)

clf()

hf.background = 2;

ha = gca()

ha.data_bounds = [-5, -5, 5, 5];

xgrid();

plot([0 a1], [0 b1], 'b', 'LineWidth', 3)

plot([0 a2], [0 b2], 'r', 'LineWidth', 3)

plot([0 a3], [0 b3], 'g', 'LineWidth', 3)

xlabel('Real axis(Re)', 'FontSize', 2)

ylabel('Imaginary axis(Im)', 'FontSize', 2)

legend('\$\backslash Large{z_1}\$', '\$\backslash Large{z_2}\$', '\$\backslash Large{z_3}\$')

plot(0, 0, 'sk')

plot(a1, b1, 'sk')

plot(a2, b2, 'sk')

```
plot(a3,b3,'sk')
```

```
xstring(a1,b1,'$\\Large \\{z_1\\}=2+i\\sqrt{3}$')
```

```
xstring(a2,b2,'$\\Large \\{z_2\\}=1+2i\\sqrt{3}$')
```

```
xstring(a3,b3,'$\\Large \\{z_3\\}=3+3i\\sqrt{3}$')
```

```
//calculate exp form
```

```
r1 = Sqrt(a1^2 + b1^2);
```

```
r2 = Sqrt(a2^2 + b2^2);
```

```
r3 = Sqrt(a3^2 + b3^2);
```

```
phi1 = atan(b1/a1)*180/%.pi;
```

```
phi2 = atan(b2/a2)*180/%.pi;
```

```
phi3 = atan(b3/a3)*180/%.pi;
```

```
//display polynomial and polar parameters
```

```
mprintf('%.5s\\t %.5s\\t %.5s\\n','a','b','r','phi')
```

```
mprintf('%.4.2f \\t %.4.2f \\t %.4.2f \\t %.4.2f\\n',a1,b1,r1,phi1)
```

```
mprintf('%.4.2f \\t %.4.2f \\t %.4.2f \\t %.4.2f\\n',a2,b2,r2,phi2)
```

```
mprintf('%.4.2f \\t %.4.2f \\t %.4.2f \\t %.4.2f\\n',a3,b3,r3,phi3)
```

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(iv) Division

clc()

//Define complex numbers

a1 = 2;

b1 = 1;

a2 = 1;

b2 = 2;

z1 = complex(a1, b1);

z2 = complex(a2, b2);

//mathematical operation

z3 = z1/z2;

a3 = real(z3);

b3 = imag(z3);

//plot

figure(0)

clf()

hf.background = 2;

ha = gca()

ha.data_bounds = [-5, -5, 5, 5];

xgrid();

plot([0 a1], [0 b1], 'b', 'LineWidth', 3)

plot([0 a2], [0 b2], 'r', 'LineWidth', 3)

plot([0 a3], [0 b3], 'g', 'LineWidth', 3)

xlabel('Real axis(Re)', 'FontSize', 2)

ylabel('Imaginary axis (Im)', 'FontSize', 2)

legend('\$\{z_1\}\$', '\$\{z_2\}\$', '\$\{z_3\}\$')

plot(0, 0, 'sk')

plot(a1, b1, 'sk')

plot(a2, b2, 'sk')

```
plot(a3, b3, 'sk')
```

```
xstring(a1, b1, '$\backslash large{z - \{1\} = 2 + i \{2\} \$}')  
xstring(a2, b2, '$\backslash large{z - \{2\} = 1 + 2i \{3\} \$}')  
xstring(a3, b3, '$\backslash large{z - \{3\} = 3 + 3i \{4\} \$}')
```

```
// calculate exp form
```

```
r1 = sqrt(a1^2 + b1^2);
```

```
r2 = sqrt(a2^2 + b2^2);
```

```
r3 = sqrt(a3^2 + b3^2);
```

```
phi1 = atan(b1/a1) * 180/%pi;
```

```
phi2 = atan(b2/a2) * 180/%pi;
```

```
phi3 = atan(b3/a3) * 180/%pi;
```

```
// display polynomial and polar parameters
```

```
mprintf('%.s\n%.s\n%.s\n%.s\n', 'a', 'b', 'r', 'phi')
```

```
mprintf('%.4.2f %.4.2f %.4.2f %.4.2f\n', a1, b1, r1, phi1)
```

```
mprintf('%.4.2f %.4.2f %.4.2f %.4.2f\n', a2, b2, r2, phi2)
```

```
mprintf('%.4.2f %.4.2f %.4.2f %.4.2f\n', a3, b3, r3, phi3)
```

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B

uc()

$a1 = 1; b1 = 2; a2 = 1; b2 = -1; a3 = 1; b3 = 2; a4 = 1; b4 = 1;$

$z1 = \text{complex}(a1, b1);$

$z2 = \text{complex}(a2, b2);$

$z3 = \text{complex}(a3, b3);$

$z4 = \text{complex}(a4, b4);$

$n1 = 2;$

$n2 = 1;$

$n3 = -1;$

$n4 = 1;$

$z11 = z1^n1;$

$z22 = z2^n2;$

$z33 = z3^n3;$

$z44 = z4^n4;$

$z = (z11 * z22) / (z33 * z44);$

$\text{disp}(z11);$

$\text{disp}(z22);$

$\text{disp}(z33);$

$\text{disp}(z44);$

$\text{disp}(z);$

$a = \text{real}(z);$

$b = \text{imag}(z);$

$r1 = \text{Sqr}t(a1^2 + b1^2);$

$r2 = \text{Sqr}t(a2^2 + b2^2);$

$r3 = \text{Sqr}t(a3^2 + b3^2);$

$r4 = \text{Sqr}t(a4^2 + b4^2);$

$r = \text{Sqr}t(a^2 + b^2).$

$\phi_{11} = \text{atan}(b1/a1);$

$\phi_{22} = \text{atan}(b2/a2);$

$\phi_{33} = \text{atan}(b3/a3);$

$$\phi_4 = \tan(b_4/a_4);$$

$$\phi = \tan(b/a)$$

$$r_{11} = r_1^n n_1$$

$$r_{22} = r_2^n n_2$$

$$r_{33} = r_3^n n_3$$

$$r_{44} = r_4^n n_4$$

$$\phi_{11} = \phi_1 * n_1$$

$$\phi_{22} = \phi_2 * n_2$$

$$\phi_{33} = \phi_3 * n_3$$

$$\phi_{44} = \phi_4 * n_4$$

$$p_{11} = r_{11} * (\cos(\phi_{11}) + \%i * \sin(\phi_{11}));$$

$$p_{22} = r_{22} * (\cos(\phi_{22}) + \%i * \sin(\phi_{22}));$$

$$p_{33} = r_{33} * (\cos(\phi_{33}) + \%i * \sin(\phi_{33}));$$

$$p_{44} = r_{44} * (\cos(\phi_{44}) + \%i * \sin(\phi_{44}));$$

$$p = (p_{11} * p_{22}) / (p_{33} * p_{44});$$

~~disp(p);~~

mprintf ('%.5f %.5f %.5f %.5f\n', 'a', 'b', 'r', 'phi')

mprintf ('%.4.2f %.4.2f %.4.2f %.4.2f\n', a1, b1, r1, phi1)

mprintf ('%.4.2f %.4.2f %.4.2f %.4.2f\n', a2, b2, r2, phi2)

mprintf ('%.4.2f %.4.2f %.4.2f %.4.2f\n', a3, b3, r3, phi3)

mprintf ('%.4.2f %.4.2f %.4.2f %.4.2f\n', a4, b4, r4, phi4)

mprintf ('%.4.2f %.4.2f %.4.2f %.4.2f\n', a, b, r, phi)

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PRACTICAL 2

A] Laplace Transform

1. e^{-t}

$$e^{-at} = \frac{1}{s+a}$$

$$\therefore e^{-t} = \frac{1}{s+1}$$

2. $\sin t$

$$\sin at = \frac{a}{s^2 + a^2}$$

$$\sin t = \frac{1}{s^2 + 1}$$

3. $\cosh 2t$

$$\cosh at = \frac{s}{s^2 - a^2}$$

$$\therefore \cosh 2t = \frac{s}{s^2 - 4}$$

4. t^2

$$t^n = n! \frac{1}{s^{n+1}}$$

$$t^2 = \frac{2!}{s^3} = \frac{2}{s^3}$$

5. $1 - e^{-t}$

$$1 = \frac{1}{s}$$

$$e^{-at} = \frac{1}{s+a}$$

$$1 - e^{-t} = \frac{1}{s} - \frac{1}{s+1}$$

$$6. \quad 1 + e^{-t}$$

$$1 = \frac{1}{s}$$

$$e^{-at} = \frac{1}{s+a}$$

$$1 + e^{-t} = \frac{1}{s} + \frac{1}{s+1}$$

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B] Inverse Laplace Transform

$$1. \frac{s^2 - 3s + 4}{s^3}$$

$$\frac{s^2 - 3s + 4}{s^3} = \frac{s^2}{s^3} - \frac{3s}{s^3} + \frac{4}{s^3} = \frac{1}{s} - \frac{3}{s^2} + \frac{4}{s^3}$$

$$L^{-1} \left[\frac{s^2 - 3s + 4}{s^3} \right] = 1 - 3t + 2t^2$$

$$2. \frac{s+2}{(s^2 - 4s + 13)}$$

$$= \frac{s+2}{(s-2)^2 + 3^2}$$

$$= \frac{s+2}{(s-2)^2 + 9} = \frac{s-2+4}{(s-2)^2 + 9} = \frac{s-2}{(s-2)^2 + 9} + \frac{4}{(s-2)^2 + 9}$$

$$\therefore L^{-1} \left[\frac{s-a}{(s-a)^2 + b^2} \right] = e^{at} \cdot \cos(bt)$$

$$L^{-1} \left[\frac{b}{(s-a)^2 + b^2} \right] = e^{at} \cdot \sin(bt)$$

$$\text{Here } a=2, b=3$$

$$\therefore e^{2t} \cdot \cos(3t) \neq 0$$

$$\therefore \frac{s-2}{(s-2)^2 + 9} = e^{2t} \cdot \cos(3t)$$

$$\therefore \frac{4}{(s-2)^2 + 9} = 4e^{2t} \cdot \frac{\sin(3t)}{3}$$

$$\therefore L^{-1} \left[\frac{s+2}{s^2 - 4s + 13} \right] = e^{2t} \cdot \cos(3t) + \frac{4}{3} e^{2t} \cdot \sin(3t)$$

$$F(s) = 0$$

$$3) \quad (s^2 - 6s + 5)$$

$$(s^3 - 6s^2 + 11s - 6)$$

$$\therefore \frac{s^2 - 6s + 5}{(s-1)(s-2)(s-3)} = \frac{A}{s-1} + \frac{B}{s-2} + \frac{C}{s-3}$$

$$\therefore s^2 - 6s + 5 = A(s-2)(s-3) + B(s-1)(s-3) + C(s-1)(s-2)$$

When $s=1$

$$1^2 - 6(1) + 5 = A(1-2)(1-3)$$

$$\therefore 1 - 6 + 5 = 2A$$

$$\therefore A = 0$$

When $s=2$

$$2^2 - 6(2) + 5 = B(2-1)(2-3)$$

$$4 - 12 + 5 = -B$$

$$\therefore B = 3$$

When $s=3$

$$3^2 - 6(3) + 5 = C(3-1)(3-2)$$

$$9 - 18 + 5 = 2C$$

$$\therefore C = -2$$

$$\therefore \frac{s^2 - 6s + 5}{s^3 - 6s^2 + 11s - 6} = \frac{3}{s-2} - \frac{2}{s-3}$$

$$= \cancel{\frac{3}{s-2}} - \frac{2e^{2t}}{s-3}$$

4)

$$\frac{s}{(2s-1)(3s-1)}$$

$$\therefore \frac{s}{(2s-1)(3s-1)} = \frac{A}{2s-1} + \frac{B}{3s-1}$$

$$\therefore s = A(3s-1) + B(2s-1)$$

$$3A + 2B = 1 \quad \rightarrow \text{Coefficient of } s$$

$$-A - B = 0 \quad \rightarrow \text{constant term}$$

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$$-A + B = 0$$

$$\therefore -A = B$$

Substitute $B = -A$ in $3A + 2B = 1$

$$3A + 2(-A) = 1$$

$$\therefore 3A - 2A = 1$$

$$A = 1$$

$$\therefore B = -1, A = 1$$

$$\begin{aligned} \frac{s}{(2s-1)(3s-1)} &= \frac{1}{2s-1} - \frac{1}{3s-1} \\ &= L^{-1}\left(\frac{1}{2s-1}\right) - L^{-1}\left(\frac{1}{3s-1}\right) \\ &= \frac{1}{2} e^{\frac{1}{2}t} - \frac{1}{3} e^{\frac{1}{3}t} \end{aligned}$$

5)

$$\frac{s}{(s^2-1)^2}$$

$$\therefore \frac{s}{((s-1)(s+1))^2}$$

$$L^{-1}\left(\frac{s}{s^2-1}\right) = \cosh(t)$$

$$L[t \cdot \cosh(t)] = -\frac{d}{ds} \left[\frac{s}{s^2-1} \right]$$

$$\frac{d}{ds} \left(\frac{s}{s^2-1} \right) = \frac{(s^2-1) - s(2s)}{(s^2-1)^2} = \frac{-s^2-1}{(s^2-1)^2} = \frac{-(s^2+1)}{(s^2-1)^2}$$

$$\frac{s}{(s^2-1)^2} = -\frac{1}{2} \frac{d}{ds} \left(\frac{s}{s^2-1} \right)$$

$$L^{-1} \left[-\frac{1}{2} \frac{d}{ds} \left(\frac{s}{s^2-1} \right) \right] = \frac{1}{2} t \cosh(t)$$

$$\therefore L^{-1} \left[\frac{s}{(s^2-1)^2} \right] = \frac{1}{2} t \cosh(t)$$

$$6. \frac{s}{s^4+s^2+1}$$

$$s^2 = \frac{-1 \pm \sqrt{3}i}{2}$$

$$L^{-1} \left(\frac{s}{s^4+s^2+1} \right) = \frac{1}{3} \left(e^{-\frac{1}{2}t} \cos \left(\frac{\sqrt{3}}{2}t \right) + \cos(t) \right)$$

$$7. \frac{s+2}{s^2(s+1)(s-2)}$$

$$\therefore \frac{s+2}{s^2(s+1)(s-2)} = \frac{A}{s} + \frac{B}{s^2} + \frac{C}{s+1} + \frac{D}{s-2}$$

$$\therefore s+2 = As(s+1)(s-2) + B(s+1)(s-2) + C(s^2(s-2)) + D(s^2(s+1))$$

$$s=0$$

$$2=0+ -2B+0+0$$

$$\boxed{B=-1}$$

$$s=-1$$

$$-1=0+0+ -3C+0$$

$$\boxed{C=-\frac{1}{3}}$$

$$4=0+0+0+12D$$

$$\boxed{D=\frac{1}{3}}$$

$$s=1$$

$$3=-2A-2B-C+2D$$

$$3=-2A+2+\frac{1}{3}+\frac{2}{3}$$

$$3=-2A+2+\frac{1}{3}$$

$$\therefore \boxed{A=0}$$

$$F(s)=0+\frac{-1}{s^2}-\frac{\frac{1}{3}}{s+1}+\frac{\frac{1}{3}}{s-2}$$

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$$f(t) = -t - \frac{1}{3} e^{-t} + \frac{1}{3} e^{2t}$$

8.

$$\frac{1}{(s^2+1)(s^2+9)} = As+B$$

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Practical 3 - Differential Equation

1. $x0 = 0$; $xinc = 0.001$; $xf = 1$; $x = x0$; $xinc : xf$;
 // Define x

// calculate analytic solution

$$y = \text{Sqrt}(x^2 + 2*x + 0.01);$$

// Plot analytic solution

Subplot(2, 1, 1), plot(x, y), xgrid
 ylabel('y(x)', 'fontsize', 2)

title('Analytic Solution', 'fontsize', 2)

// Define differential equation

deff('yprim = f(x, y)', 'yprim = (x+1)/y');

// Solve differential equation

$$y0 = 0.1;$$

Subplot(2, 1, 2), plot(x, ydiff, 'r'), xgrid

title('Numeric Solution', 'fontsize', 2)

ylabel('y(x)', 'fontsize', 2)

ydiff = ode(y0, x0, x, f); // Plot numeric solution

xlabel('x', 'fontsize', 2)

2. function ydot = f(t, y)

$$ydot = y^2 - y * \sin(t) + \cos(t)$$

endfunction

$$y0 = 0;$$

$$t0 = 0;$$

$$t = 0:0.1:\pi;$$

$$y = \text{ode}(y0, t0, t, f);$$

plot(t, y)

3) function $\dot{x} = \text{linear}(t, x, A, v, B, \omega)$
 $\dot{x} = A^* x + B^* v(t, \omega)$

endfunction

function $v(t, \omega)$
 $v = \sin(\omega * t)$

endfunction

$A = [1 \ 1:0 \ 2];$

$B = [1; 1];$

$\omega = 5;$

$y_0 = [1; 0];$

$t_0 = 0;$

$t = [0.1, 0.2, 0.5, 1];$

{
ode($y_0, t_0, t, \text{list}(\text{linear}, A, v, B, \omega))$

plot(t, v);}

4) function $y = v(t)$

$$y = (\text{sign}(t) + 1)/2$$

endfunction

$L = 0.001$

$R = 10$

$C = 0.000001$

function $\dot{z} = f(t, z)$

$$\dot{z}_1 = z_2;$$

$$\dot{z}_2 = (v(t) - z_1 - L^* z_2/R)/(L^* C);$$

endfunction

$y_0 = [0; 0];$

$t_0 = 0;$

$t = 0:0.000001:0.001;$

$out = \text{ode}(y_0, t_0, t, f);$

$\text{clf}();$

$\text{plot}(out);$

function $y = v(t)$

$$y = (\text{sign}(t) + 1) / 2$$

endfunction

$$L = 0.001$$

$$R = 10$$

$$C = 0.000001$$

function zdot = f(t, y)

$$zdot = [y(2); (v(t) - y(1) - L * y(2) / R) / (L * C)];$$

endfunction

$$y_0 = [0; 0];$$

$$t_0 = 0;$$

$$t = 0:0.000001:0.001;$$

$$\text{out} = \text{ode}(y_0, t_0, t, f);$$

clf();

subplot(2, 1, 1)

plot(t, out(1, :), "r--");

subplot(2, 1, 2)

plot(t, out(2, :), "b-..");

5) function dx = f(t, x)

$$dx(1) = x(2);$$

$$dx(2) = 1/(t+1) + \sin(t) * \sqrt{t};$$

endfunction

$$t = 0:0.01:5*\pi;$$

$$t_0 = \min(t);$$

$$y_0 = [0; -2];$$

$$y = \text{ode}(y_0, t_0, t, f);$$

plot(t, y(1, :), 'LineWidth', 2)

plot(t, y(2, :), 'r', 'LineWidth', 2)

xgrid();

xlabel('\$t \\quad [s]\$', 'FontSize', 3)

ylabel('\$f(t, x)\$', 'FontSize', 3)

title('Integration of '\$\\frac{dx}{dt} = x^2\$' '\$\\int dx = \\frac{1}{2}x^2 + C\$')

$\sqrt{t+3}$ \$], 'FontSize', 3}
legend(['\$Large{x^2}\$' \$Large{dx/dt^3}\$], 2)

6) funcprot(0)

clf;

function $dx = f(x, y)$

$dx = \exp(-x_0);$

endfunction

$y_0 = 0;$

$x_0 = 0;$

$x = [0:0.5:10];$

$sol = \text{ode}(y_0, x_0, x, f);$

$\text{plot2d}(x, sol, 5)$

$xlabel('x');$

$ylabel('y(x)');$

$ntitle('y(x) vs. x')$

7) funcprot(0)

clf;

function $dx = f(x, y)$

$dx = x^2 - \exp(-x)*y$

endfunction

$y_0 = 0;$

$x_0 = 0;$

$x = [0:0.5:10];$

$sol = \text{ode}(y_0, x_0, x, f);$

$\text{plot2d}(x, sol, 5)$

$xlabel('x');$

$ylabel('y(x)');$

$ntitle('y(x) vs. x')$

$$vt = \sin(\omega_n * t)$$

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Practical 5

A) Z Transform.

1. clear;

// z transform of [2 -1 3 2 1 0 2 3 -1]

clear; clc;

close;

function [za] = ztransfer(Sequence, n)

z = poly(0, 'z', 'r')

za = Sequence * (1/z)^n'

endfunction

z1 = [2 -1 3 2 1 0 2 3 -1]

n = 4:4

zz = ztransfer(z1, n);

// Display the result in command window

disp(zz, "z-transform of sequence is: ")

disp('ROC is the entire plane except z=0 and z=%intf;')

$$\Rightarrow x_1 = [2, -1, 3, 2, 1, 0, 2, 3, -1]$$

n = 4:4

$$x(z) = \sum_{n=-\infty}^{\infty} x[n] \cdot z^{-n}$$

$$X(z) = 2z^4 - z^3 + 3z^2 + 2z + 1 + 0 + \frac{2}{z} + \frac{3}{z^2} + \frac{1}{z^3}$$

For a finite length sequence, the ROC is entire z-plane except at $z=0$ and $z=\infty$. Therefore

ROC = The entire z-plane except $z=0$ and $z=\infty$

2. clear;
// z Transform of [1, 2, 3, 4, 5, 6, 7]

dc;

function [za] = ztransfer(sequence, n)

z = poly(0, 'z', 'r')

za = sequence * (1/z)^n

endfunction

x = [1, 2, 3, 4, 5, 6, 7];

n1 = 0: length(x) - 1;

x = ztransfer(x, n1);

disp(`x(z) = ');

disp(x)

funcprot(0);

$$\Rightarrow x = [1, 2, 3, 4, 5, 6, 7]$$

length is 0 to 6

$$X(z) = \sum_{n=0}^6 x[n] z^{-n}$$

$$X(z) = 1 \cdot z^0 + 2 \cdot z^{-1} + 3z^{-2} + 4 \cdot z^{-3} + 5 \cdot z^{-4} + 6z^{-5} + 7z^{-6}$$

$$= 1 + \frac{2}{z} + \frac{3}{z^2} + \frac{4}{z^3} + \frac{5}{z^4} + \frac{6}{z^5} + \frac{7}{z^6}$$

3. clear;

// z transform of [1, 2, 3, 4, 5, 6, 7] with different range

dc;

function [za] = ztransfer(sequence, n)

z = poly(0, 'z', 'r')

za = sequence * (1/z)^n

endfunction

x = [1, 2, 3, 4, 5, 6, 7]

n1 = 2: length(x) - 3

WISH

X = ztransfer
disp(X, X(2))

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$x = \text{ztransfer}(x, n)$

$\text{disp}(x, 'x(z) = ')$

$\text{funcprot}(0);$

$$\Rightarrow x = [1, 2, 3, 4, 5, 6, 7]$$

$$n1 = -2 : \text{length}(x) - 3 \quad \text{i.e. } -2, -1, 0, 1, 2, 3, 4$$

$$x(z) = \sum_{n=-2}^4 x(n) \cdot z^{-n}$$

$$= 1 \cdot z^2 + 2 \cdot z^1 + 3 \cdot z^0 + 4 \cdot z^{-1} + 5 \cdot z^{-2} + 6 \cdot z^{-3} + 7 \cdot z^{-4}$$

$$= 1 \cdot z^2 + 2z + 3 + \frac{4}{z} + \frac{5}{z^2} + \frac{6}{z^3} + \frac{7}{z^4}$$

4. clear;

// z Transform of $[1, 2, 3, 4, 5, 0, 7]$

clc;

function $[za] = \text{ztransfer}(\text{sequence}, n)$

$z = \text{poly}(0, 'z', 'r')$

$za = \text{sequence} * (1/z)^n$

endfunction

$x = [1, 2, 3, 4, 5, 0, 7]$

$n1 = 0 : \text{length}(x) - 1;$

$x = \text{ztransfer}(x, n1)$

$\text{disp}(x);$

$\text{funcprot}(0);$

$$\Rightarrow x = [1, 2, 3, 4, 5, 0, 7]$$

$$n1 = 0 : \text{length}(x) - 1 \quad \text{i.e. } 0 : 6 = 0, 1, 2, 3, 4, 5, 6$$

$$x(z) = \sum_{n=0}^6 x(n) z^{-n}$$

$$= 1 \cdot z^0 + 2 \cdot z^{-1} + 3 \cdot z^{-2} + 4 \cdot z^{-3} + 5 \cdot z^{-4} + 6 \cdot z^{-5} + 7 \cdot z^{-6}$$

$v_t = 5 \sin(\omega t)$

$$= 1 + \frac{2}{z} + \frac{3}{z^2} + \frac{4}{z^3} + \frac{5}{z^4} + \frac{6}{z^5} + \frac{7}{z^6}$$

5. // z Transform of $[4, 2, -1, 0, 3, -4]$

clc;
 function [za] = ztransfer(sequence, n)
 $z = \text{poly}(0, 'z', 'r')$
 $za = \text{sequence} * (1/z)^n'$

endfunction

$$x = [4, 2, -1, 0, 3, -4]$$

$$n1 = -2 : \text{length}(x) - 3$$

$$x = \text{ztransfer}(x, n1);$$

$$\text{disp}(x, 'x(z) = ');$$

$$\text{funcprot}(0);$$

$$\Rightarrow x = [4, 2, -1, 0, 3, -4]$$

$$n1 = -2 : \text{length}(x) - 3 \quad \text{i.e. } -2, -1, 0, 1, 2, 3$$

$$x(z) = \sum_{n=-2}^3 x(n) \cdot z^{-n}$$

$$= 4 \cdot z^{-2} + 2 \cdot z^{-1} + 0 \cdot \frac{1}{z} + \frac{3}{z^2} + -\frac{4}{z^3}$$

$$= 4z^2 + 2z^{-1} + \frac{3}{z^2} - \frac{4}{z^3}$$

6 // Convolution of two signals x_1 and x_2

clc;
 function [za] = ztransfer(sequence, n)
 $z = \text{poly}(0, 'z', 'r')$
 $za = \text{sequence} * (1/z)^n'$

endfunction;

$$x1 = [1, -3, 2];$$

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$$n1 = 0; \text{length}(x1) - 1;$$

$$x1 = z\text{transfer}(x1, n1);$$

$$x2 = [1, 2, 1];$$

$$n2 = 0; \text{length}(x2) - 1;$$

$$x2 = z\text{transfer}(x2, n2);$$

$$x = x1 * x2;$$

$$\text{disp}(x, 'x(z) = ');$$

$$z = \text{poly}(0, 'z');$$

$$x = [1; -z^{-1}; -3z^{-2}; z^{-3}; 2z^{-4}];$$

$$n = 0: 4;$$

$$z1 = z^n;$$

$$x = (x * z1);$$

$$\text{disp}(x, 'x[n] = ');$$

$$\Rightarrow x1 = [1, -3, 2] \quad n1 = [0, 1, 2]$$

$$x2 = [1, 2, 1] \quad n2 = [0, 1, 2]$$

$$\therefore x_1(z) = 1 - \frac{3}{z} + \frac{2}{z^2} \quad & \quad x_2(z) = 1 - \frac{2}{z} + \frac{1}{z^2}$$

$$\begin{aligned} \therefore x_1 * x_2 &= \left(1 - \frac{3}{z} + \frac{2}{z^2}\right) * \left(1 + \frac{2}{z} + \frac{1}{z^2}\right) \\ &= 1 + \frac{2}{z} + \frac{1}{z^2} + \left(-\frac{3}{z} - \frac{6}{z^2} - \frac{3}{z^3}\right) + \left(\frac{2}{z^2} + \frac{4}{z^3} + \frac{2}{z^4}\right) \\ &= 1 + 2z^{-1} + 1z^{-2} - 3z^{-3} - 6z^{-4} - 3z^{-5} + 2z^{-6} + 4z^{-7} + 2z^{-8} \\ &= 1 + (2z^{-1} - 3z^{-2}) + (z^{-2} - 6z^{-3} + 2z^{-4}) + (-3z^{-5} + 4z^{-6}) + 2z^{-7} \\ &= 1 - z^{-1} - 3z^{-2} + z^{-3} + 2z^{-4} \end{aligned}$$

$$x(n) = \begin{array}{c|c|c|c|c|c} 1 & -1 & -3 & 1 & 2 & 0 \\ \hline \text{where } n=0 & 1 & 2 & 3 & 4 & \text{otherwise} \end{array}$$



$$vt = \sin(\omega_n * t)$$

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B] Inverse Z Transform

- // find the inverse Z-transform using long division method
clc;

clear;

$$z = \text{poly}(0, 'z')$$

$$x = 1 \text{div}(z^3 - 10z^2 - 4z + 4, 2z^2 - 2z - 4, 4);$$

$$\text{disp}(x, 'x[n] = ');$$

$$\Rightarrow x(z) = \frac{z^3 - 10z^2 - 4z + 4}{2z^2 - 2z - 4}$$

$$= \frac{z^3 - 10z^2 - 4z + 4}{2(z-2)(z+1)} = \frac{A}{z-2} + \frac{B}{z+1} = \frac{A(z+1) + B(z-2)}{z(z-2)(z+1)}$$

$$\therefore z^3 - 10z^2 - 4z + 4 = A(z+1) + B(z-2)$$

i) When $z = 2$

$$z^3 - 10(2)^2 - 4(2) + 4 = A(3)$$

$$-36 = 3A$$

$$\boxed{A = -12}$$

ii) When $z = -1$

$$(-1)^3 - 10(-1)^2 - 4(-1) + 4 = B(-3)$$

$$-3 = -3B$$

$$\boxed{B = 1}$$

$$\therefore \frac{z^3 - 10z^2 - 4z + 4}{2(z-2)(z+1)} = \frac{-12}{z-2} + \frac{1}{z+1}$$

$$= -12 \cdot 2^n \cdot u(n) + (-1)^n \cdot u(n)$$

- // find the inverse Z-transform

clc;

clear;

$$z = \text{poly}(0, 'z');$$

$$x = 1 \text{div}((z+1), (z-1/3), 4);$$

$$\text{disp}(x, 'x[n] = ');$$

$$\Rightarrow x(z) = \frac{z+1}{z-\frac{1}{3}} = \frac{z - \frac{1}{3} + \frac{4}{3}}{z - \frac{1}{3}} = \frac{z - \frac{1}{3}}{z - \frac{1}{3}} + \frac{\frac{4}{3}}{z - \frac{1}{3}}$$

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$$x(z) = \frac{1 + \frac{4}{z}}{z - \frac{1}{3}}$$

$$x(n) = + \frac{4}{3} \cdot \left(\frac{1}{3}\right)^n \cdot u(n)$$

3. clear;

// Inverse Z-transform using long division method.
clc;

clear;

$$z = poly(0, 'z');$$

$$x = ldiv(z, (z - 0.5), 4);$$

$$disp(x, 'x[n] = ');$$

$$\Rightarrow x(z) = \frac{z}{z - 0.5}$$

$$= \frac{z - 0.5 + 0.5}{z - 0.5} = \frac{z - 0.5}{z - 0.5} + \frac{0.5}{z - 0.5}$$

$$x(z) = 1 + \frac{0.5}{z - 0.5}$$

$$x(n) = 1 + \frac{0.5}{0.5} = 1 + 0.5(0.5)^n \cdot u(n)$$

4. Clear.

// To find input x(n)

$$// x(z) = 1 / (2 * z^{-2} + 2 * z^{-1} + 1);$$

clear;

clc;

close;

$$z = \%z;$$

$$a = (2 + 2 * z + z^2);$$

$$b = z^2;$$

$$h = ldiv(b, a, 6);$$

disp(h, "first six values of h(n) = ")

$$\Rightarrow H(z) = \frac{1}{2z^{-2} + 2z^{-1} + 1} \times \frac{z^2}{z^2}$$

$$= \frac{z^2}{2 + 2z + z^2} = \frac{z^2}{z^2 + 2z + 2}$$

$$\text{For } z^2 + 2z + 2 \quad a = 1, b = 2, c = 2$$

$$z = \frac{-2 \pm \sqrt{2^2 - 4(1)(2)}}{2(1)} = \frac{-2 \pm \sqrt{4-8}}{2} = \frac{-2 \pm \sqrt{-4}}{2} = \frac{-2 \pm 2i}{2}$$

$$z_1 = \frac{-2+2i}{2} \quad \text{or} \quad z_2 = \frac{-2-2i}{2}$$

$$z_1 = -1+i \quad z_2 = -1-i$$

$$H(z) = \frac{z^2}{(z-(-1+i))(z-(-1-i))} = \frac{A}{z-(-1+i)} + \frac{B}{z-(-1-i)}$$

$$\text{i) } z = -1+i$$

$$(-1+i)^2 = A(2i) \quad \therefore A = \frac{1-2i}{2i} = -i$$

$$\boxed{A = -i}$$

$$\text{ii) } z = -1-i$$

$$(-1-i)^2 = A(0) + B(-2i) \quad 1+2i = -2Bi \quad \therefore B = \frac{1+2i}{-2i} = i$$

$$\therefore \frac{z^2}{(z-(-1+i))(z-(-1-i))} = \frac{i}{(z-(-1+i))} + \frac{i}{z-(-1-i)}$$

$$x(n) = -i(-1+i)^n \cdot v(n) + i(-1-i)^n \cdot v(n)$$

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Practical 6

$$1. e^{2t} \cdot \cos 3t$$

$$\text{let } f(t) = \cos 3t$$

$$f(s) = \frac{s}{s^2 + 9}$$

$$L[e^{2t} \cdot \cos 3t] = F(s-2)$$

$$\therefore L[e^{2t} \cdot \cos 3t] = \frac{s-2}{(s-2)^2 + 9} \quad \dots \text{First Shifting Property.}$$

$$2. e^{-t} \cdot \sin t$$

$$\text{let } f(t) = \sin t$$

$$F(s) = \frac{a}{s^2 + 1}$$

$$L[e^{-t} \cdot \sin t] = F(s+1)$$

$$\therefore L[e^{-t} \cdot \sin t] = \frac{s+1}{(s+1)^2 + 1} \quad \dots \text{First Shifting Property}$$

$$3. t \cdot \cos t$$

$$\text{let } f(t) = \cos t$$

$$F(s) = \frac{s}{s^2 + 1}$$

By multiplication by t property

$$L[t \cdot f(t)] = (-1)' \frac{d}{ds} \cdot \frac{s}{s^2 + 1}$$

$$= -\frac{d}{ds} \left(\frac{s}{s^2 + 1} \right)$$

$$= - \left[\frac{(s^2 + 1) \cdot ds}{ds} - s \cdot \frac{d}{ds} (s^2 + 1) \right] \frac{(s^2 + 1)^2}{(s^2 + 1)^2}$$

$$= \left[\frac{s^2 + 1 - 2s^2}{(s^2 + 1)^2} \right]$$

$$\begin{aligned}
 & \text{vishincha} \\
 & \text{Cost. } \sin 2t = \frac{1}{2} \sin 2t \\
 & \text{Cost. } \sin 2t = \frac{1}{2} \sin 2t
 \end{aligned}$$

$$4 \quad \frac{\sin t}{t}$$

$$\text{let } f(t) = \sin t$$

$$F(s) = \frac{1}{s^2 + 1}$$

$$\begin{aligned}
 L\left[\frac{\sin t}{t}\right] &= \int_s^\infty \frac{1}{u^2 + 1} \cdot du \quad [\text{Division by } t \text{ property}] \\
 &= \left(\tan^{-1} \frac{1}{u}\right)_s^\infty \\
 &= \tan^{-1} \frac{1}{\infty} - \tan^{-1} \frac{1}{s} \\
 &= \tan^{-1} 0 - \tan^{-1} \frac{1}{s} \\
 &= \frac{\pi}{2} - \tan^{-1} \frac{1}{s}
 \end{aligned}$$

$$5 \quad t^2 \cdot e^{-2t}$$

$$f(t) = t^2$$

$$F(s) = \frac{2}{s^3} = \frac{2}{s^3}$$

$$\begin{aligned}
 L[e^{2t} \cdot t^2] &= \frac{2}{s^3} \Big|_{s=s+2} \\
 &= \frac{2}{(s+2)^3}
 \end{aligned}$$

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cost. $\sin 2t$.

$$\begin{aligned}\text{Cost. } \sin 2t &= \sin 2t \cdot \text{cost} = \frac{\sin(2t+t) + \sin(2t-t)}{2} \\ &= \frac{\sin 3t + \sin t}{2}\end{aligned}$$

$$F(s) = \frac{1}{2} \left[\frac{3}{s^2+9} + \frac{1}{s^2+1} \right]$$

$$= \frac{1}{2} \left[\frac{3}{s^2+9} \right] + \frac{1}{2} \left[\frac{1}{s^2+1} \right]$$

7. $t \cdot e^{-t} \cdot \text{cost}$

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Practical 7 - System Response Using Laplace Transform

1) clear;

clc;

clear;

close;

$$S = \text{poly}(0, 's')$$

$$N = (s+1) * (s+3);$$

$$D = (s+2) * (s+4);$$

$$F = N/D;$$

disp(F, 'Given Transfer Function:');

zero = roots(N);

pole = roots(D);

disp(zero, 'Zeros of transfer function:');

disp(pole, 'Poles of transfer function:');

plzr(F)

2)

Clear;

clc;

Clear;

close;

$$S = \text{poly}(0, 's');$$

$$L = 3 * S / (s+2) / (s+4)$$

disp(L, 'Given Transform function:');

zero = roots(3 * S);

pole = roots((s+2) * (s+4));

disp(zero, 'Zeros of transfer function:');

disp(pole, 'Poles of transfer function:');

plzr(L)

3) clear;
clc;
clear;
close;
 $s = \text{poly}(0, 's')$
 $F = 10*s / (s^2 + 2*s + 2);$
disp(F, 'Given Transfer Function:');
zero = roots(10*s);
pole = roots(s^2 + 2*s + 2);
disp(zero, 'Zeros of transfer function:');
disp(pole, 'Poles of transfer function:');
plzr(F)

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5.] System Response Using Laplace Transform

1. clear;

clc;

$$S = \% s;$$

$$N = 0.1 * S^2 + 0.35 * S$$

$$D = S^2 + 3 * S + 2;$$

G = syslin('c', N, D);

t = linspace(6, 8, 200);

U = ones(1, 200);

y = csim(u, t, G);

plot(t, y);

xtitle()

xtitle('Response to Initial Condition', 'tsec', 'Response');

xgrid(color('gray'));

2. clear;

clc;

$$S = \% s;$$

G = syslin('c', 1, s^2 + 0.2 * s + 1);

t = 0:0.5:50;

y = csim('impuls', t, g);

plot(t, y);

xtitle('Impulse Response of 1/(s^2 + 0.2 * s + 1)', 'tsec', 'Response');

xgrid(color('gray'));

Practical 8

System Response Using z Transform

A] // to plot the response of the system analytically and using scilab
clear;

clc;

close;

 $n = 0 : 1 : 20;$ $x = [1 \text{ zeros}(1, 20)];$ $b = [1 - 1 3/16];$ $y_{analy} = 0.5 * (0.75)^n + 0.5 * (0.25)^n; // \text{Analytical Solution.}$ $ymat = filter(b, a, x);$

subplot(3, 1, 1);

plot2d3(n, x);

xlabel('n');

ylabel('x(n)');

title('INPUT SEQUENCE (IMPULSE FUNCTION));

subplot(3, 1, 2);

plot2d3(n, yanaly);

xlabel('n');

ylabel('y(n)');

title('OUTPUT SEQUENCE yanaly');

B] // to plot the response of system analytically and using scilab.

Clear;

clc;

close;

 $n = 0 : 1 : 20;$ $x = n;$ $b = [0 1 1];$ $a = [1 - 0.7 0.12];$ $y_{analy} = 38.89 * (0.4)^n - 26.53 * (0.3)^n - 12.36 + 4.76 * n;$

```
ymat = filter(b,a,n);
subplot(3,1,1);
plot2d3(n,n);
xlabel('n');
ylabel('x(n)');
title('INPUT SEQUENCE (RAMP FUNCTION)');
subplot(3,1,2);
plot2d3(n,yanaly);
xlabel('n');
ylabel('y(n)');
title('OUTPUT SEQUENCE yanaly');
subplot(3,1,3);
plot2d3(n,ymat);
xlabel('n');
ylabel('y(n)');
title('OUTPUT SEQUENCE ymat');
```

c] // To plot the response of system analytically and using scilab.

```
clear;
```

```
clc;
```

```
close;
```

```
n=0:1:20;
```

```
x=ones(1,length(n));
```

```
b=[0 1];
```

```
a=[1 -1 -1];
```

```
yanaly=0.447*(1.618)^n-0.447*(-0.618)^n; //Analytical Solution.
```

```
[ymat,zf]=filter(b,a,x);
```

```
subplot(3,1,1);
```

```
plot2d3(n,n);
```

```
xlabel('n');
```

```
ylabel('x(n)');
```

```
title('Input Sequence (Step Function)');
```

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```
subplot(3,1,2);
plot2d3(n,yanaly);
xlabel('n');
ylabel('y(n)');
title('Output Sequence yanaly');
Subplot(3,1,3);
plot2d3(n,ymat,zf);
xlabel('n');
ylabel('y(n)');
title('Output Sequence ymat')
```

```
clear;
// To find input h(n)
//  $x(z) = (z+0.2) / ((z+0.5)(z-1))$ 
clear;
uc;
close;
z = %z;
a = (z+0.5)* (z-1);
b = z+0.2;
h = 1 div(b,a,4)
disp(h, "h(n) = ")
```

B] Plot zero plot using Z Transform

1. // to draw the pole-zero plot

clear;

clc;

close;

$Z = \%z$;

$$H1Z = ((z) * (z + i)) / (z^2 - z + 0.5);$$

plzr(H1Z)

2. // to draw pole-zero plot

clear;

clc;

close;

$Z = \%z$;

$$H1Z = (z) / (z^2 - z - 1);$$

plzr(H1Z);

3. // to draw pole-zero plot

clear;

clc;

close;

$Z = \%z$

$$H1Z = ((z) * (z - 1)) / ((z - 0.25) * (z - 0.5));$$

plzr(H1Z);

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4) clear;

clc;

close;

$z = \text{poly}(0, (2));$

$H = (1+z) / (1+3/4 * z^2 + 1/8 + z^2);$

pole = roots(1+z);

zero = roots(1+3/4 * z^2 + 1/8 + z^2);

disp(H, 'System Transfer Function H(z) = ');

disp(zero, 'System zeros are at');

disp(pole, 'System poles are at');

plzr(H);

\Rightarrow

1 + 2

1 + 0.75z + 0.125z²

'System Transfer function H(z) = '

-4 + 0j

-2 + 0j

'System zero are at'

-1

'System poles are at'

5) // Pole - Zero plots

clear;

$z = \% z;$

$az = 2 * z * (z + 1);$

$bz = (z - 1/3) * ((z^2) + 1/4) + 4 * z + 5;$

poles = roots(bz);

zeros = roots(az);

$h = az / bz$

plzr(h)

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Practical 4 - Fourier Transform

A] Continuous Time Fourier Transform

1. clear;

$$// x(t) = A * \cos(\omega_0 * t) * \text{gate}(t/T)$$

$$// T = 1/2 * f_0$$

$$// f_0 = 0.5 \text{ Hz}$$

clear;

clc;

// Fourier Transform

$$A = 1;$$

$$T = 0.5;$$

$$f_0 = 1/(2*T);$$

$$\omega_0 = 2 * \%pi * f_0;$$

$$\text{for } f = 20:1:20;$$

$$x(f+2) = A * \text{integrate}(`\cos(\omega_0 * t) * \cos(2 * \%pi * f * t)', 't', -0.25, 0.25);$$

end

$$\text{disp}(x, 'x(0) \rightarrow x(20)').$$

$$t = 0.25:0.01:0.25;$$

$$q = \cos(\omega_0 * t);$$

$$a = \text{gca}();$$

$$a.y_location = "origin";$$

$$a.x_location = "origin";$$

$$\text{plot}(t, q);$$

$$\text{xlabel}("Time in seconds");$$

$$\text{title}('Signal x(t)');$$

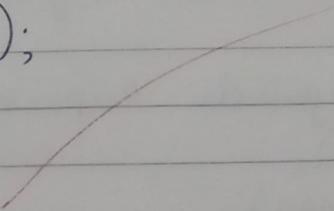
$$\text{figure}(1);$$

$$a = \text{gca}();$$

$$a.y_location = "origin";$$

$$a.x_location = "origin";$$

$$f = 20:1:20;$$



```

plot(f, x);
xlabel("Frequency in Hz");
title('Continuous Time Fourier Transform x(jw)');

2) clear;
//Fourier Transform of x(t) = exp(-a*t)* cos(wc*t)* u(t)
clear;
clc;
a=1;
wc=1;
Dt = 0.005;
t = 0:Dt:10;
xt = (exp(t*(-a+wc))+exp(t*(-a-wc)))/2;
Wmax = 2* %pi* 1;
K=4;
k = 0:(K/1000):K;
W= k* Wmax / K;
XW= xt * exp(-sqrt(-1)*t'* w)* Dt;
XW_Mag = abs(XW);
[XW_Phase, db] = phasemag(XW);
//Plotting Continuous Time Signal
figure(1)
plot(t, xt);
ylabel('x(t)');
title('continuous time signal')
figure(2)
//Plotting Magnitude Response of CTS
subplot(2,1,1);
plot(w, XW_Mag);
xlabel('Frequency in Radians/Seconds > w');
ylabel('abs(x(jw))');
title('Magnitude response ((TFT))')

```

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//Plotting phase response of CTS

subplot (2, 1, 2);

plot (W, XW_Phase * %pi / 180);

xlabel ('Frequency in radians/seconds > W');

ylabel ('<W(jW)');

title ('Phase Response (CTFT) in radians');

3) //Continuous time fourier transform of sinusoidal waveforms

//(a) sin(Wot) (b) cos(Wot)

clear;

clc;

close;

//CTFT

T1 = 2;

T2 = 2;

T = 4 * T1;

W0 = 2 * %pi / T;

W = [-W0, 0, W0];

ak = [2 * %pi * W0 * T1 / %pi] / sqrt(-1);

XW = [-ak, 0, ak];

ak1 = (2 * %pi * W0 * T1 / %pi);

XWI = [ak1, 0, ak1];

figure

a = gca();

a.y_location = "origin";

a.x_location = "origin";

plot 2d3('gnn', W, imag(XW), 2);

poly1 = a.children(1).children(1);

poly1.thickness = 3;

xlabel (' W');

title ('(CTFT of sin(Wot))');

figure

```

a=gca();
a.y_location = "origin";
a.z_location = "origin";
plot2d3('gnn', W, xW1, 2);
poly1=a.children(1).children(1);
poly1.thickness=3;
xlabel(' w');
title('CTFT of cos(w_0 t)')

```

4) clear; //Continuous Time Fourier of a Signal $x(t) = \exp(-A*t) u(t)$

clc;
close;

//Analog Signal

A=-1; //Amplitude

T=1;

Dt=0.005;

t=0: Dt: 10;

xt=A*exp(-t/T);

//CTFT

wmax=2*pi*1;

k=4;

k=0:(k/1000):K;

W=k*wmax/K;

xw=xt*exp(-sqrt(-1)*t'*w)*Dt;

xw_mag=abs(xw);

[xw_Phase, db]=phase_mag(xw);

//Plotting Continuous Time Signal

a=gca();

a.y_location = "origin";

plot(t, xt);

xlabel('t in sec.');

ylabel('x(t)'),

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title ('Continuous Time Signal')

figure

//Plotting Magnitude Response of CTS

subplot(2,1,1);

a=gca();

a.y_location = "origin";

plot(xW,xW-Mag);

xlabel('Frequency in Radians/Seconds --> w');

ylabel('abs(x(jw))')

title('Magnitude Response ((TFT))')

//Plotting Phase Response of CTS

subplot(2,1,2);

a=gca();

a.y_location = "origin";

a.x_location = "origin";

plot(xW,xW-Phase * %pi/180);

xlabel('Frequency in Radians/Seconds --> w');

ylabel(' <x(jw))')

title('Phase Response ((TFT) in Radians)')

5) clear;

/Fourier Transform of $x(t) = \exp(-t) * \sin(\omega_c t) * u(t)$

clear;

clc;

$\omega_c = 1;$

$Dt = 0.005;$

$t = 0 : Dt : 10;$

$xt = (\exp(t * (-1 + \omega_c)) - \exp(t * (-1 - \omega_c))) / (2 * \%i);$

$\omega_{max} = 2 * \%pi * 1;$

$K = 4;$

$R = 0 : (K / 1000) : K;$

$$W = R^* W_{max} / K;$$

$$x_W = xt^* \exp(-\sqrt{-1})^* t^* W)^* D t;$$

~~$$x_W - Mag = \text{abs}(x_W);$$~~

$$[x_W - \text{Phase, db}] = \text{phase.mag}(x_W);$$

figure(1)

plot(t, xt);

xlabel('t in sec.');

ylabel('x(t)');

title('Continuous time Signal')

figure(2)

subplot(2, 1, 1);

plot(W, xW_Mag);

xlabel('Frequency in Radians/Seconds > W');

ylabel('abs(x(jW))');

title('Magnitude Response (TFT)')

subplot(2, 1, 2);

plot(W, xW_Phase * %pi / 180);

xlabel('Frequency in Radians/Seconds > W');

ylabel('<x(jW)');

title('Phase Response (TFT) in Radians')

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B] Inverse CTFT

// Inverse CTFT

// $x(j\omega) = 1$, from $-T_1$ to T_1

clear;

clc;

close;

//CTFT

$A = 1$; //Amplitude

$D\omega = 0.005$;

$W_1 = 4$; //Time in seconds

$\omega = -W_1/2 : D\omega : W_1/2$;

for $i = 1 : \text{length}(\omega)$

$xw(i) = A$;

end

$xw = xw'$;

plot (ω , xw);

xlabel (' ω in radians');

title ('Continuous Time Fourier Transform $x(t)$ ')

$t = 3 * \%pi : \%pi / \text{length}(\omega) : 3 * \%pi$;

$xt = (1 / (2 * \%pi)) * xw * \exp(Sqr(-1) * \omega * t) * D\omega$;

$xt = \text{real}(xt)$;

figure

plot (t , xt);

figure

plot (t , xt);

xlabel (' t sec');

title ('Time domain signal $x(t)$ ')

2. clear;
 // Inverse Continuous Time Fourier Transform
 clear;
 clc;
 close;
 //CTFT
 A = 1;
 $Dw = 0.005$;
 $W1 = 4$;
 $W_0 = 2$ // Assume $W_0 = 2$
 $w = W1/2 : Dw : W1/2$;
 for i=1:length(w)
 if $w(i) == W_0$ then
 $xw(i) = 2 * \%pi$
 else
 $xw(i) = 0$;
 end
 $xw = xw'$;
 // Inverse CTFT
 $t = 3 * \%pi : \%pi / \text{length}(w) : 3 * \%pi$;
 $xt = (1/2 * \%pi)^* xw * \exp(\sqrt{-1} * w^* t)^* Dw$;
 $xt = \text{real}(1 + xt)$;
 plot(t, xt);
 xlabel('t sec');
 title('Time domain signal x(t)')

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```
clear;
// Inverse CTFT
// x(jw) = 2 * pi, at w = 0
clear;
clc;
close;
// CTFT
A = 1;
Dw = 0.005;
W1 = 4;
w = W1/2 : Dw : W1/2
for i = 1 : length(w)
    if w(i) == 0 then
        xw(i) = 2 * %pi;
    else
        xw(i) = 0;
    end
end
xw = xw';
subplot(2, 1, 1)
plot(w, xw);
// Inverse CTFT
t = 3 * %pi : %pi / length(w) : 3 * %pi;
xt = (1/2 * %pi) * xw * exp(sqrt(-1) * w' * t) * Dw;
xt = real(1 + xt)
subplot(2, 1, 2)
plot(t, xt)
xlabel('t sec')
title('Time domain Signal x(t)')
```

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C] Discrete time Fourier Transform

//Discrete time fourier transform of discrete sequence

$$x[n] = (a^n) \cdot v[n], a > 0 \text{ and } a < 0$$

clear;

clc;

close;

//DTS signal

$$a1 = 0.5;$$

$$a2 = -0.5;$$

$$\text{max_limit} = 10;$$

for n=0:max_limit-1

$$x1(n+1) = (a1^n);$$

$$x2(n+1) = (a2^n);$$

end

$$n = 0: \text{max_limit} - 1;$$

//discrete time fourier transform

$$W_{\text{max}} = 2^* \% \pi;$$

$$k = 4;$$

$$k = 0: (k/1000):K;$$

$$w = k^* W_{\text{max}} / K;$$

$$x1 = x1';$$

$$x2 = x2';$$

$$xw1 = x1 * \exp(-\sqrt{-1} * n' * w);$$

$$xw2 = x2 * \exp(-\sqrt{-1} * n' * w);$$

$$xw1_Mag = \text{abs}(xw1);$$

$$xw2_Mag = \text{abs}(xw2);$$

$$[xw1_Phase, db] = \text{phasemag}(xw1);$$

$$[xw2_Phase, db] = \text{phasemag}(xw2);$$

//plot for a>0

figure

$$\text{subplot}(3, 1, 1);$$

```
plot2d3('gnn', n, n1);
xtitle('Discrete Time Sequence n[n] for a>0')
Subplot(3,1,2);
a=gca();
a.y_location = "origin";
a.x_location = "origin";
plot2d(w, xw1-Mag);
title('Magnitude Response abs(x(jw))')
Subplot(3,1,1);
a=gca();
a.y_location = "origin";
a.x_location = "origin";
plot2d(w, xw1-Phase);
title('Phase Response <(x(jw))>')
// plot for a<0
figure
subplot(3,1,1);
plot2d3('gnn', n, n2);
xtitle('Discrete Time Sequence n[n] for a>0')
Subplot(3,1,2);
a=gca();
a.y_location = "origin"
a.x_location = "origin"
plot2d(w, xw2-Phase);
title('Magnitude Response abs(x(jw))')
subplot(3,1,3);
a=gca();
a.y_location = "origin";
a.x_location = "origin";
plot2d(w, xw2-Phase);
title('Phase Response <(x(jw))>')
```

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//discrete Time Fourier Transform of $x[n]=1$, $\text{abs}(n) \leq N$

clear;

clc;

close;

//DTS Signal

N1 = 2;

n = -N1 : N1;

x = ones (1, length(n));

//Discrete time Fourier Transform

wmax = 2 * %pi

K = 4;

k = 0 : (K/1000) : K;

w = k * wmax / K

xw = x * exp(-sqrt(-1) * n' * w);

xw_mag = real(xw);

//plot for abs(a)<1

figure

subplot(2, 1, 1);

a = gca();

a.y_location = "origin";

a.x_location = "origin";

plot2d3('gnn', n, x);

title('Discrete Time Sequence $x[n]$ ')

subplot(2, 1, 2);

a = gca();

a.y_location = "origin";

a.x_location = "origin";

plot2d3(w, xw_mag);

title('Discrete Time Fourier Transform $x(\exp(jw))$ ')

3) // Discrete Time Fourier Transform : $x[n] = \cos(n\omega_0)$

clear;

clc;

close;

N = 5;

$\omega_0 = 2 * \%pi / N;$

$w = [-\omega_0, 0, \omega_0];$

$x_w = [\%pi, 0, \%pi];$

figure

a = gca();

a.y_location = "origin";

a.x_location = "origin";

plot2d3('gnn', w, x_w, 2);

poly1 = a.Children(1).Children(1);

poly1.thickness = 3;

zlabel('w');

title('DTFT of cos(n\omega_0)')

disp(w_0)

4) // Discrete Time Fourier Transform of discrete sequence

⇒ $x[n] = (n)^*(a_1^n) \cdot v[n]$

$a > 0$ and $a < 0$

clc;

close;

$a1 = 0.5;$

$a2 = 0.5;$

max_limit = 10;

for n = 0 : max_limit - 1

$x1(n+1) = (n)^*(a1^n) \cdot$

$x2(n+1) = (n)^*(a2^n) \cdot$

end

$n = 0 : max_limit - 1;$

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$$W_{max} = 2\pi \% \pi ;$$

$$k=4;$$

$$K = 0 : (K/1000) : K;$$

$$W = k * W_{max} / K;$$

$$x_1 = x_1';$$

$$x_2 = x_2';$$

$$x_{W1} = x_1 * \exp(-\sqrt{-1} * n_1 * W);$$

$$x_{W2} = x_2 * \exp(-\sqrt{-1} * n_2 * W);$$

$$x_{W1_Mag} = \text{abs}(x_{W1});$$

$$x_{W2_Mag} = \text{abs}(x_{W2});$$

$$[x_{W1_Phase}, db] = \text{phasemag}(x_{W1});$$

$$[x_{W2_Phase}, db] = \text{phasemag}(x_{W2});$$

figure

subplot(3, 1, 1);

plot2d3('gnn', n, x1);

title('Discrete Time Sequence x[n] for a>0')

subplot(3, 1, 2);

a=gca();

a.y_location = "origin";

a.x_location = "origin";

plot2d(W, x_{W1_Mag});

title('Magnitude Response abs(x(jW)))')

subplot(3, 1, 3);

a=gca();

a.y_location = "origin";

a.x_location = "origin";

plot2d(W, x_{W1_Phase});

title('Phase Response <(x(jW))>')

figure

subplot(3, 1, 1);

plot2d3('gnn', n, x2);

title('Discrete Time Sequence x[n] for a>0')

subplot(3,1,2)

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D] Inverse DTFT.

clear; uc;

$\omega_c = 1;$

$y = 1;$

for $n = -\%pi : \%pi / 80 : \%pi$

if $n < -\omega_c$ | $n > \omega_c$ then

$x(1, y) = 1;$

$y = y + 1;$

else $x(1, y) = 0;$

$y = y + 1;$

end

end

$n = -\%pi : \%pi / 80 : \%pi;$

$a = gca();$

$a.y_location = "origin";$

$a.x_location = "origin";$

$plot(n, x);$

$xlabel('frequency in Radians/Seconds');$

$title('x(e^{jw}) at \omega=1');$

$A = 1 \%pi;$

for $k = 10 : 10$

$x(k+1) = A * integrate('cos(\omega*k)', 'w', \omega_c, \%pi);$

end

$figure(1);$

$k = 10 : 10;$

$a = gca();$

$a.y_location = "origin";$

$a.x_location = "origin";$

$plot2d3(k, x);$

$xlabel('Time in Seconds');$

$title('x(n) at \omega_c = 1');$

2 clear; clear;

clc;

wc = 1;

y = 1;

for n = -%pi : %pi/80 : %pi

if n < -wc | n > wc then

x(1,y) = 1;

y = y + 1;

end x(1,y) = 0;

y = y + 1;

end

end

n = -%pi : %pi/80 : %pi

a = gca();

a.y_location = "origin";

a.x_location = "origin";

plot(n, x);

xlabel('frequency in Radians / Seconds');

title('x(e^gw) at wc=1');

A = 1/%pi;

for K = 10:10

n(K+1) = A * integrate('cos(w*K)', 'w', wc, %pi);

end

figure(1);

k = -10:10;

a = gca();

a.y_location = "origin";

a.x_location = "origin";

plot2d3(k, n);

xlabel('Time in Seconds');

title('n(n) at wc=1');