

Database Management System (DBMS)

L-3:

Relational Algebra

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Lecture Content

- Relational Algebra
- Relational Database Operations
- Set Theoretic Operations
- Additional Relational Operations

Relational Algebra

“The relational algebra is a theoretical language with operations that work on one or more relations to define another relation without changing the original relation/s.”

Three Types of operations:

- Relational Database Operations
 - select, project, join*
- Set Theoretic Operations
 - Union, Intersect, Set Difference, Cartesian Product*
- Additional Relational Operations
 - Aggregate, Grouping, and Outer Join*

Selection

“Selection operation works on a single relation R and defines a relation that contains only those tuples of R that satisfy the specified condition.”

$$\sigma_{\text{condition}}(R)$$

Selection cont.

For example, We have a relation called **Student**.

Student

| <i>LName</i> | <i>FName</i> | <i>StudId</i> | <i>Major</i> |
|--------------|--------------|---------------|--------------|
| Smith | Susan | 131313 | Comp |
| Bond | James | 007007 | Math |
| Smith | Susan | 555555 | Comp |
| Cecil | John | 010101 | Math |

Student1

$\sigma_{\text{StudId}} (\text{Student})$

| <i>LName</i> | <i>FName</i> | <i>StudId</i> | <i>Major</i> |
|--------------|--------------|---------------|--------------|
| Bond | James | 007007 | Math |

Projection

“Projection operation works on a single relation R and defines a relation that contains a vertical subset of R, extracting the values of specified attributes and eliminate duplicates.”

$$\pi_{A_1, \dots, A_n}(R)$$

Projection cont.

For example, We have a relation called **Student**.

Student

| <i>LName</i> | <i>FName</i> | <i>StudId</i> | <i>Major</i> |
|--------------|--------------|---------------|--------------|
| Smith | Susan | 131313 | Comp |
| Bond | James | 007007 | Math |
| Smith | Susan | 555555 | Comp |
| Cecil | John | 010101 | Math |

Student1

$\pi_{Lname, FName} (Student)$

| <i>Lname</i> | <i>FName</i> |
|--------------|--------------|
| Smith | Susan |
| Bond | James |
| Cecil | John |

Union

“The union of two relations R and S defines a relation that contains all the tuples of R, or S, or both R and S, duplicate tuples being eliminated. R and S must be union compatible.”

R U S

Union cont.

For Example,

“List all cities where there is either a branch office or property for rent”

Branch

| <i>branchNo</i> | <i>city</i> |
|------------------------|--------------------|
| B005 | London |
| B007 | Aberdeen |
| B003 | Glasgow |
| B004 | Bristol |
| B002 | London |

PropertyForRent

| <i>propertyNo</i> | <i>city</i> |
|--------------------------|--------------------|
| PA14 | Aberdeen |
| PL94 | London |
| PG4 | Glasgow |
| PG36 | Glasgow |
| PG21 | Glasgow |
| PG 16 | Glasgow |

How do we list them?

Union cont.

Branch

| <i>branchNo</i> | <i>city</i> |
|-----------------|-------------|
| B005 | London |
| B007 | Aberdeen |
| B003 | Glasgow |
| B004 | Bristol |
| B002 | London |

PropertyForRent

| <i>propertyNo</i> | <i>city</i> |
|-------------------|-------------|
| PA14 | Aberdeen |
| PL94 | London |
| PG4 | Glasgow |
| PG36 | Glasgow |
| PG21 | Glasgow |
| PG 16 | Glasgow |

| <i>city</i> |
|-------------|
| London |
| Aberdeen |
| Glasgow |
| Bristol |

First project them to make union compatible then union operation.

$\pi_{city} (Branch) \ U \ \pi_{city} (PropertyForRent)$

Intersection

“The intersection operation defines a relation consisting of the set of all tuples that are in both R and S. R and S must be union compatible.”

$R \cap S$

Intersection cont.

For Example,

“List all cities where there is both a branch office and at least one property for rent”

Branch

| <i>branchNo</i> | <i>city</i> |
|------------------------|--------------------|
| B005 | London |
| B007 | Aberdeen |
| B003 | Glasgow |
| B004 | Bristol |
| B002 | London |

PropertyForRent

| <i>propertyNo</i> | <i>city</i> |
|--------------------------|--------------------|
| PA14 | Aberdeen |
| PL94 | London |
| PG4 | Glasgow |
| PG36 | Glasgow |
| PG21 | Glasgow |
| PG 16 | Glasgow |

How do we list them?

Intersection cont.

Branch

| branchNo | city |
|-----------------|-------------|
| B005 | London |
| B007 | Aberdeen |
| B003 | Glasgow |
| B004 | Bristol |
| B002 | London |

PropertyForRent

| propertyNo | city |
|-------------------|-------------|
| PA14 | Aberdeen |
| PL94 | London |
| PG4 | Glasgow |
| PG36 | Glasgow |
| PG21 | Glasgow |
| PG 16 | Glasgow |

First project them to make union compatible then intersect operation.

$$\pi_{\text{city}}(\text{Branch}) \cap \pi_{\text{city}}(\text{PropertyForRent})$$

| city |
|-------------|
| Aberdeen |
| London |
| Glasgow |

Cartesian Product

“The Cartesian Product operation defines a relation that is the concatenation of every tuple of relation R with every tuple of relation S.”

$R \times S$

Cartesian Product

For Example,

R

| A | B |
|---|---|
| 1 | 2 |
| 3 | 3 |
| 4 | 4 |

S

| B | C |
|----------|---|
| 2 | 7 |
| 4 | 9 |
| ω | 0 |

\times

$=$

R x S

| A | B | B | C |
|---|---|----------|---|
| 1 | 2 | 2 | 7 |
| 1 | 2 | 4 | 9 |
| 1 | 2 | ω | 0 |
| 3 | 3 | 2 | 7 |
| 3 | 3 | 4 | 9 |
| 3 | 3 | ω | 0 |
| 4 | 4 | 2 | 7 |
| 4 | 4 | 4 | 9 |
| 4 | 4 | ω | 0 |

Join

“Join operation joins two relations by merging those tuples from two relations that satisfy some given condition.”

There are various forms of join operations -

- Theta join
- Equi join
- Natural join
- Outer join
- Semi join

Theta Join (θ -join)

“Theta join operation defines a relation that contains tuples satisfying the condition F from the Cartesian Product of R and S. The condition is in the form $R.a_i \theta S.b_i$, where θ may be one of the comparison operations ($<$, \leq , $>$, \geq , $=$, \neq).”

$R \bowtie_F S$

Theta Join (θ -join)

Is this correct?

$$R \bowtie_F S = \sigma_F(R \times S)$$

*So we can say, a **join operation** is nothing but a “Selection operation with some condition on a Cartesian Product”.*

Equi join

R

| A | B |
|---|---|
| 1 | 2 |
| 3 | 3 |
| 4 | 4 |

S

| B | C |
|---|---|
| 2 | 7 |
| 4 | 9 |
| ω | 0 |

R x S

| A | B | B | C |
|---|---|---|---|
| 1 | 2 | 2 | 7 |
| 1 | 2 | 4 | 9 |
| 1 | 2 | ω | 0 |
| 3 | 3 | 2 | 7 |
| 3 | 3 | 4 | 9 |
| 3 | 3 | ω | 0 |
| 4 | 4 | 2 | 7 |
| 4 | 4 | 4 | 9 |
| 4 | 4 | ω | 0 |

Equi join Example,

R  **R.B = S.B** **S**

| A | B | B | C |
|---|---|---|---|
| 1 | 2 | 2 | 7 |
| 4 | 4 | 4 | 9 |

Natural Join

“The natural join is an Equijoin of the two relations R and S over all common attributes. One occurrence of each common attribute is eliminated from the result.”

R \bowtie S

Natural join

R

| A | B |
|---|---|
| 1 | 2 |
| 3 | 3 |
| 4 | 4 |

S

| B | C |
|---|---|
| 2 | 7 |
| 4 | 9 |
| ω | 0 |

R x S

=

| A | B | B | C |
|---|---|---|---|
| 1 | 2 | 2 | 7 |
| 1 | 2 | 4 | 9 |
| 1 | 2 | ω | 0 |
| 3 | 3 | 2 | 7 |
| 3 | 3 | 4 | 9 |
| 3 | 3 | ω | 0 |
| 4 | 4 | 2 | 7 |
| 4 | 4 | 4 | 9 |
| 4 | 4 | ω | 0 |

Natural join Example,

R ⋈ S

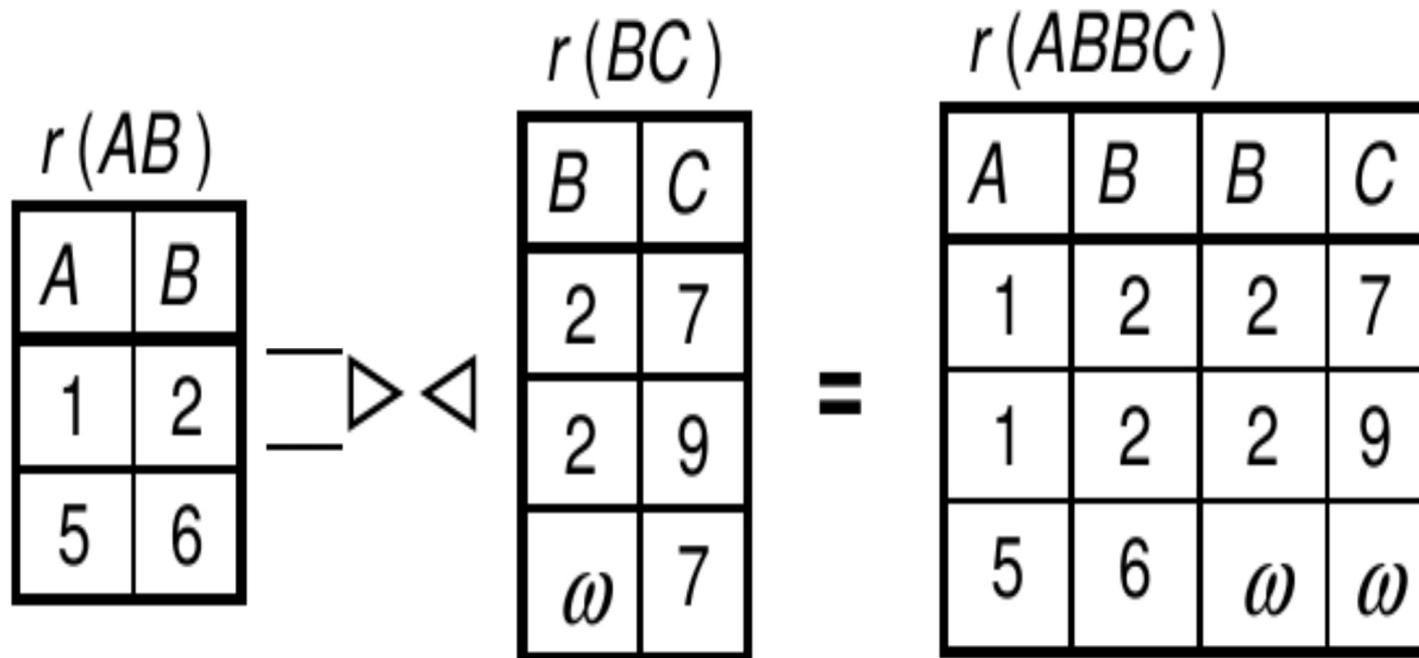
| A | B | C |
|---|---|---|
| 1 | 2 | 7 |
| 4 | 4 | 9 |

Outer Join

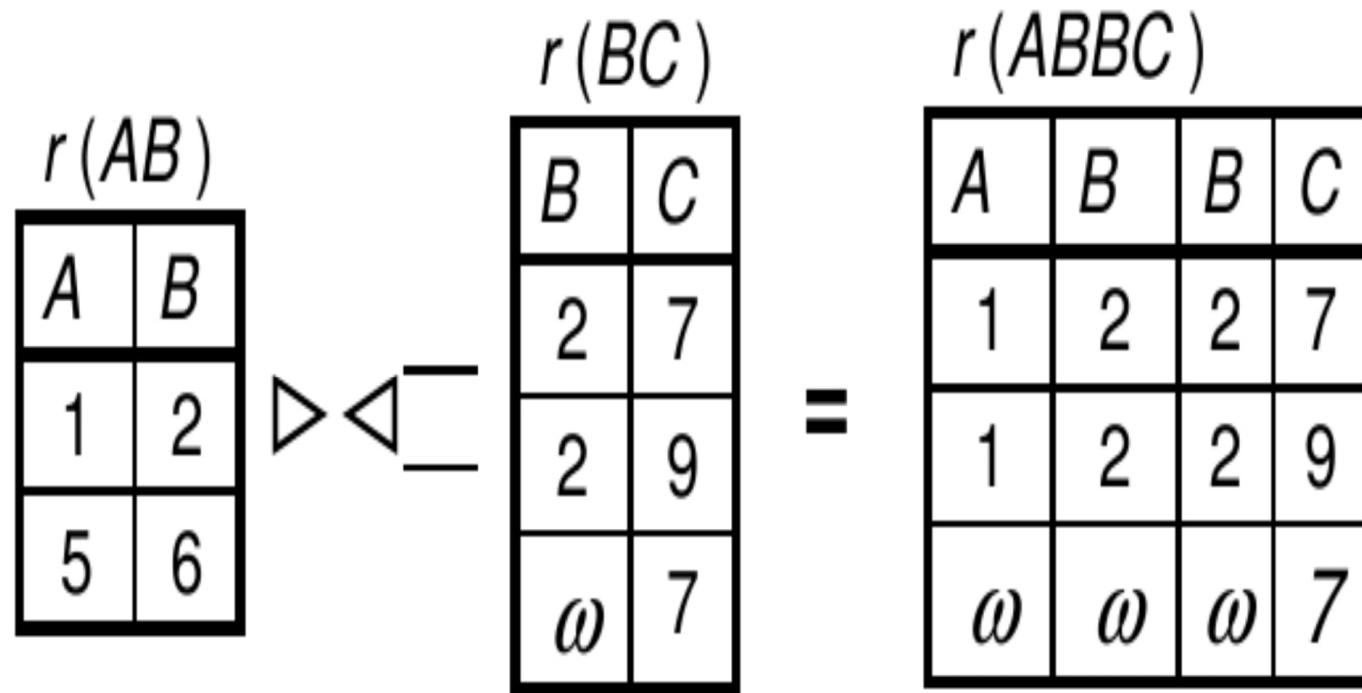
“The (left) outer join is a join in which tuples from R that do not have matching values in the common attributes of S are also included in the result relation. Missing values in the second relation are set to null.”

$R \bowtie S$

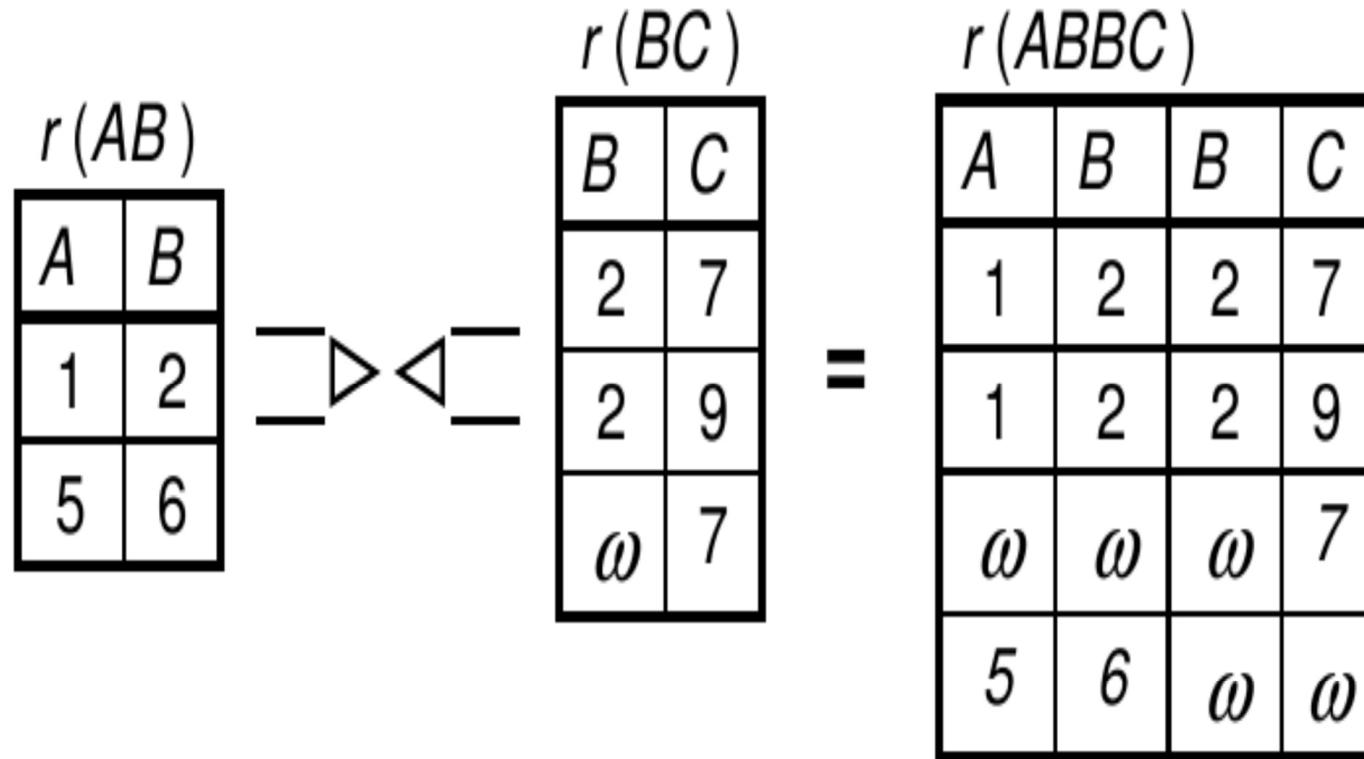
Left Outer Join cont.



Right Outer Join cont.



Full Outer Join cont.



Semi Join

“The semi join operation defines a relation that contains the tuples of R that participates in the join of R with S.”

$R \ltimes S$

Semi join cont.

| <i>R</i> | <i>S</i> | <i>R x S</i> | <i>Semi join Example,</i> <i>R</i> \bowtie <i>R.B = S.B</i> <i>S</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|----------|--------------|---|---|---|---|---|---|---|----------|----------|---|---|---|---|----------|---|---|----------|----------|----------|----------|---|---|---|---|---|---|---|---|---|---|----------|---|---|---|---|---|---|---|---|---|---|---|----------|---|---|---|---|---|---|---|---|---|---|---|----------|---|--|----------|----------|---|---|---|---|
| <table border="1"> <thead> <tr> <th><i>A</i></th><th><i>B</i></th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td></tr> <tr> <td>3</td><td>3</td></tr> <tr> <td>4</td><td>4</td></tr> </tbody> </table> | <i>A</i> | <i>B</i> | 1 | 2 | 3 | 3 | 4 | 4 | <table border="1"> <thead> <tr> <th><i>B</i></th><th><i>C</i></th></tr> </thead> <tbody> <tr> <td>2</td><td>7</td></tr> <tr> <td>4</td><td>9</td></tr> <tr> <td>ω</td><td>0</td></tr> </tbody> </table> | <i>B</i> | <i>C</i> | 2 | 7 | 4 | 9 | ω | 0 | \bowtie = <table border="1"> <thead> <tr> <th><i>A</i></th><th><i>B</i></th><th><i>B</i></th><th><i>C</i></th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td><td>2</td><td>7</td></tr> <tr> <td>1</td><td>2</td><td>4</td><td>9</td></tr> <tr> <td>1</td><td>2</td><td>ω</td><td>0</td></tr> <tr> <td>3</td><td>3</td><td>2</td><td>7</td></tr> <tr> <td>3</td><td>3</td><td>4</td><td>9</td></tr> <tr> <td>3</td><td>3</td><td>ω</td><td>0</td></tr> <tr> <td>4</td><td>4</td><td>2</td><td>7</td></tr> <tr> <td>4</td><td>4</td><td>4</td><td>9</td></tr> <tr> <td>4</td><td>4</td><td>ω</td><td>0</td></tr> </tbody> </table> | <i>A</i> | <i>B</i> | <i>B</i> | <i>C</i> | 1 | 2 | 2 | 7 | 1 | 2 | 4 | 9 | 1 | 2 | ω | 0 | 3 | 3 | 2 | 7 | 3 | 3 | 4 | 9 | 3 | 3 | ω | 0 | 4 | 4 | 2 | 7 | 4 | 4 | 4 | 9 | 4 | 4 | ω | 0 | <table border="1"> <thead> <tr> <th><i>A</i></th><th><i>B</i></th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td></tr> <tr> <td>4</td><td>4</td></tr> </tbody> </table> | <i>A</i> | <i>B</i> | 1 | 2 | 4 | 4 |
| <i>A</i> | <i>B</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| <i>B</i> | <i>C</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| ω | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| <i>A</i> | <i>B</i> | <i>B</i> | <i>C</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 2 | 2 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 2 | 4 | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 2 | ω | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | 3 | 2 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | 3 | 4 | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | 3 | ω | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 4 | 2 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 4 | 4 | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 4 | ω | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| <i>A</i> | <i>B</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Division Join

“The division operation defines a relation over the attributes C that consists of the set of tuples from R that match the combination of every tuples in S.”

$R \div S$

Division cont.

R

| <i>ClientNo</i> | <i>PropertyNo</i> |
|-----------------|-------------------|
| CR56 | PA14 |
| CR76 | PG4 |
| CR56 | PG4 |
| CR62 | PA14 |
| CR56 | PG36 |

S

| <i>PropertyNo</i> |
|-------------------|
| PG4 |
| PG36 |

Semi join Example,

$R \div S$

| <i>ClientNo</i> |
|-----------------|
| CR56 |

Summary

- ◆ Relational Algebra
- ◆ Relational Database Operations: **select, project, join**
- ◆ Set Theoretic Operation
 - **union, intersect, set difference, Cartesian product**
- ◆ Join Operations
 - **theta join, equijoin, natural join, left outer join**
 - right outer join, full outer join, semi join, division**