Regression models Course Assignment

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Introduction and executive summary

The goal of this document is to respond to 2 main questions: “is an automatic or manual transmission better for MPG”, “what is the MPG difference between automatic and manual transmissions”.

Material

The *mtcars* data are the input data. More information can be found about this data set by typing ?*mtcars* in R.

Methods and results

We first explore the data.
Using a scatterplot matrix , one can see that most of the predictors seem to have some impact on MPG. At this point, we do not see obvious outliers. Let’s fit a linear model with all variables.

```
fit <- lm(mpg ~ ., data=df)
summary(fit)
```

None of the variables shows a P-value smaller than 0.05. Let’s select a subset of these variables using the AIC stepwise selection and the regsubsets function from the R *leaps* package.

```
# AIC stepwise selection (both direction)
library(MASS)
stepB <- stepAIC(fit, direction="both")

# confirming our variable selection with a second method
library(leaps)
leaps <- regsubsets(mpg ~ ., data = df, nbest = 10)
```

Both methods recommend to use the variables *wt, am, hp and cyl* as predictors in the model, where we retrieve our variable of interest *am* (see Appendix for the results of the regsubsets function).

```
fitR <- lm(mpg ~ wt + am + hp + cyl, data=df)
summary(fitR)
```

The intercept and the variables *wt*, *hp* and *cyl6* show p-values smaller than 0.05 (more details in the appendix). Let’s have a look at the residuals plots to assess how well this model fits the data. Based on the residuals plots, it seems that the model has some difficulty to fit the data with low or high MPG values. Let’s see how we may correct this based on our scatterplot matrix (see Appendix).

There seems to be some non linear function between MPG and WT. Let’s see whether a log(wt) instead of wt may improve the model and how the residual plots have changed.

```r
fitR2 <- lm(mpg ~ log(wt) + hp + cyl + am, data=df)
anova(fitR2)
```

The curvature of the residuals vs fitted values has been reduced. Similarly, the squared of the standardized residuals plot does not show any more an increasing slope. The normal Q-Q plots seem to show less deviation from the normality for the error term. Based on the plot “standardized residuals vs leverage”, none of the points is above a Cook’s distance threshold of 0.5, which indicates that none of the point distorts the outcome and accuracy of our regression model. See Appendix for more details.

The hat values obtained with the influence function describes the influence each observed value has on each fitted value. 1 point seems to have more influence on the fitted values: “Maserati Bora. However this point is not dramatically high (see Appendix). The final selected model is *mpg ~ log(wt) + hp + cyl + am*.

Discussion

In this section both questions mentioned in the Introduction are answered based the model built in Section Methods and results. Summary of the model is given the Appendix.

Here is how to understand the coefficients of the model: Numerical variables

- for every 1% increase in *log(wt)* we expect a decrease of 10.133 in *mpg*, all the other variables constant,
- for every 1% increase in *hp* we expect a decrease of 0.027 in *mpg*, all the other variables constant,

Factor variables

- if we have 6 cylinders (*cyl6*), *mpg* changes by -2.205 compared to having 4 cylinders, all the other variables constant,
- if we have 8 cylinders (*cyl8*), *mpg* changes by -1.789 compared to having 4 cylinders, all the other variables constant,
- if we have a manual transmission (*am1*), *mpg* changes by 0.867 compared to having an automatic transmission, all the other variables constant.

```r
(ci <- confint(fitR2))
```

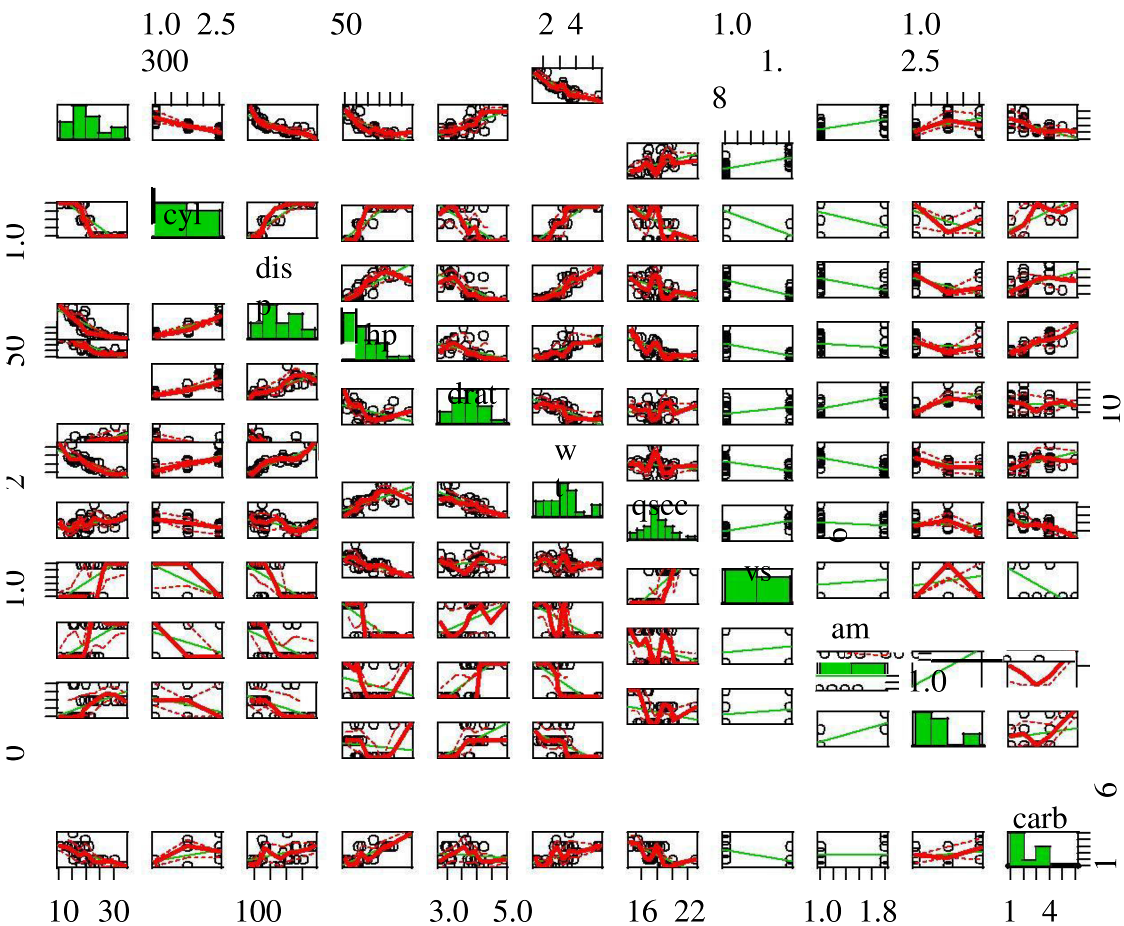
```
> (ci <- confint(fitR2))
                   2.5 %        97.5 %
(Intercept)  30.52014642 42.2557456987
log(wt)     -16.07153044 -4.1945572966
hp           -0.05441425 -0.0003648742
cyl6         -5.04344839  0.6333139289
cyl8         -6.22770611  2.6496674261
am1          -2.03562296  3.7688902021
```

Looking at the 95%-confidence interval of the estimates, one can see that the AM variable shows the interval [-2.04,3.77]. So it is not possible to tell whether an automatic transmission is better for MPG than a manual one. With the likelihood ratio test, we can say at least that adding the AM term in our model is not significantly better for estimating MPG as shown in the Appendix.

Appendix

Scatterplot matrix of all variables including MPG.

```
scatterplotMatrix(df,diagonal='histogram')
```



Fit using all variables.

```
summary(fit)
```

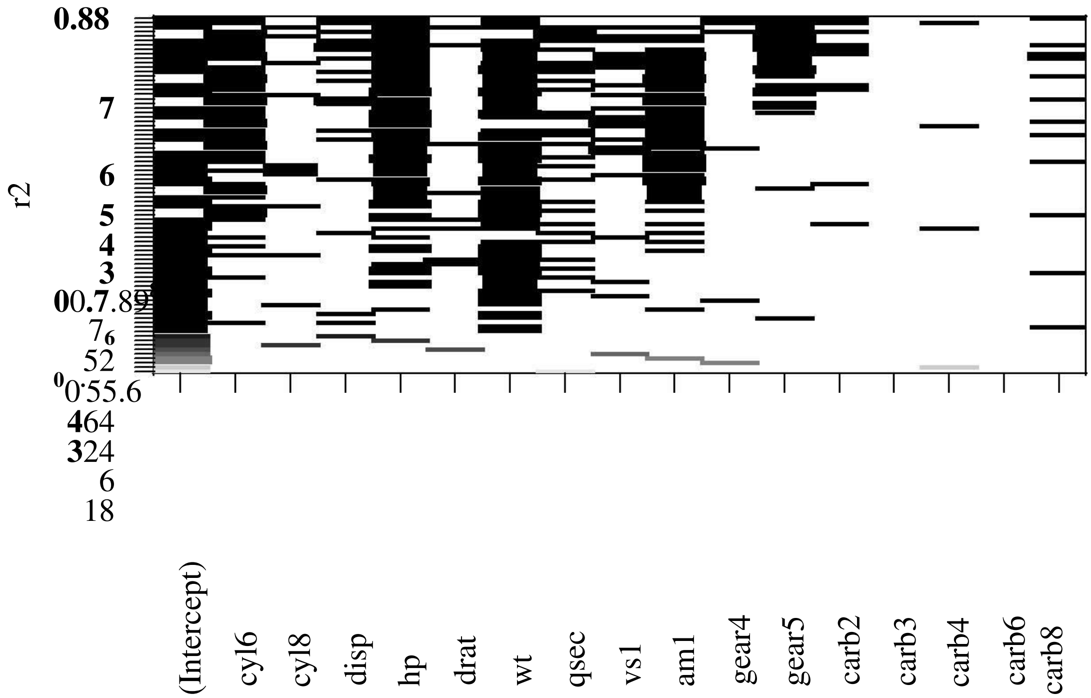
```
Call:
lm(formula = mpg ~ ., data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-3.5087 -1.3584 -0.0948  0.7745  4.6251 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)  
(Intercept) 23.87913   20.06582   1.190   0.2525  
cyl6        -2.64870    3.04089  -0.871   0.3975  
cyl8        -0.33616    7.15954  -0.047   0.9632  
disp         0.03555    0.03190   1.114   0.2827  
hp          -0.07051    0.03943  -1.788   0.0939 .
drat         1.18283    2.48348   0.476   0.6407  
wt          -4.52978    2.53875  -1.784   0.0946 .
qsec         0.36784    0.93540   0.393   0.6997  
vs1          1.93085    2.87126   0.672   0.5115  
am1          1.21212    3.21355   0.377   0.7113  
gear4        1.11435    3.79952   0.293   0.7733  
gear5        2.52840    3.73636   0.677   0.5089  
carb2       -0.97935    2.31797  -0.423   0.6787  
carb3        2.99964    4.29355   0.699   0.4955  
carb4        1.09142    4.44962   0.245   0.8096  
carb6        4.47757    6.38406   0.701   0.4938  
carb8        7.25041    8.36057   0.867   0.3995  
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.833 on 15 degrees of freedom
Multiple R-squared:  0.8931, Adjusted R-squared:  0.779 
F-statistic:  7.83 on 16 and 15 DF,  p-value: 0.000124
```

Variable selection using the stepAIC from the MASS package and the regsubsets function from the leaps package.

stepB$anova

```
> stepB$anova # display results
Stepwise Model Path
Analysis of Deviance Table

Initial Model:
mpg ~ cyl + disp + hp + drat + wt + qsec + vs + am + gear + carb

Final Model:
mpg ~ cyl + hp + wt + am


    Step Df   Deviance Resid. Df Resid. Dev      AIC
1                             15   120.4027 76.40339
2 - carb  5 13.5988573        20   134.0015 69.82769
3 - gear  2  5.0215145        22   139.0230 67.00492
4 - drat  1  0.9672159        23   139.9903 65.22678
5 - disp  1  1.2473996        24   141.2377 63.51066
6 - qsec  1  2.4420033        25   143.6797 62.05921
7   - vs  1  7.3459298        26   151.0256 61.65483
```

plot(leaps,scale="r2")



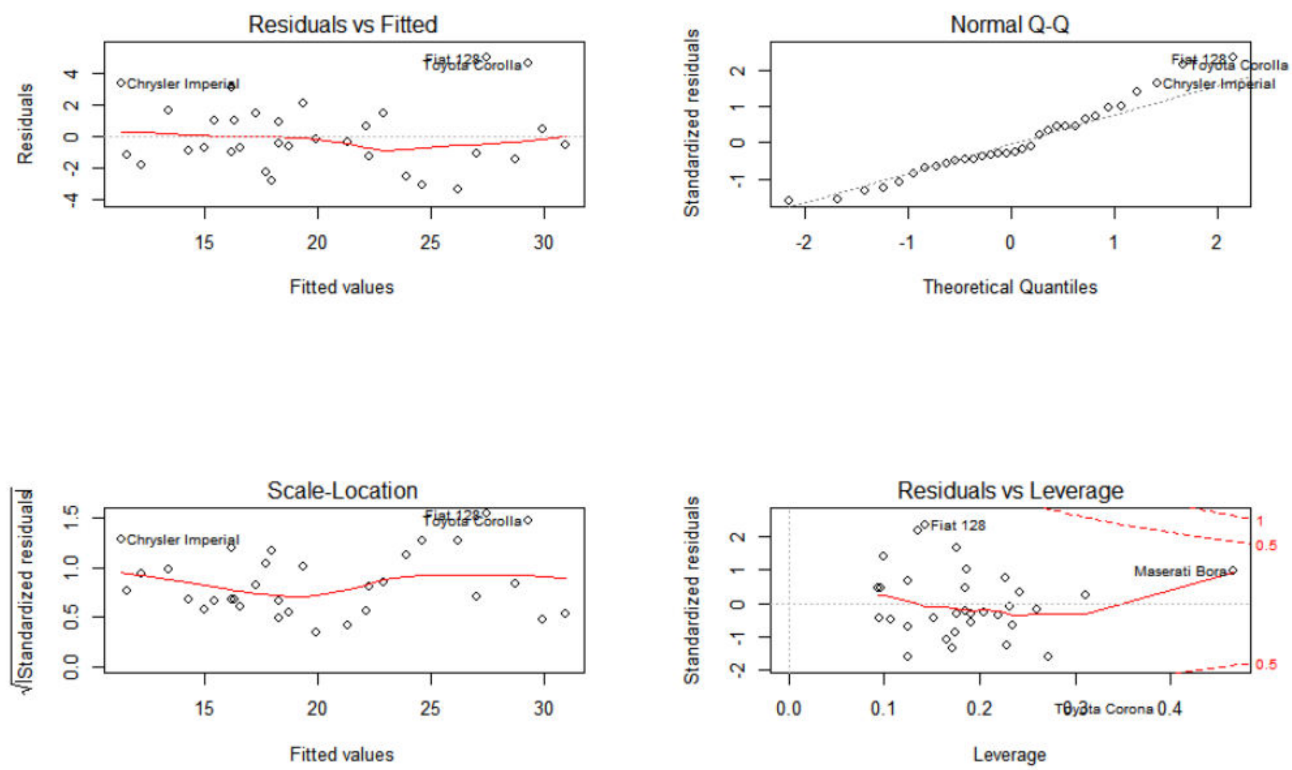
Summary of the model *mpg ~ wt + am + hp + cyl*

summary(fitR)

```
> summary(fitR)

Call:
lm(formula = mpg ~ wt + am + hp + cyl, data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-3.9387 -1.2560 -0.4013  1.1253  5.0513 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) 33.70832    2.60489  12.940 7.73e-13 ***
wt          -2.49683    0.88559  -2.819  0.00908 ** 
am1          1.80921    1.39630   1.296  0.20646    
hp          -0.03211    0.01369  -2.345  0.02693 *  
cyl6        -3.03134    1.40728  -2.154  0.04068 *  
cyl8        -2.16368    2.28425  -0.947  0.35225    
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 2.41 on 26 degrees of freedom
Multiple R-squared:  0.8659, Adjusted R-squared:  0.8401 
F-statistic: 33.57 on 5 and 26 DF,  p-value: 1.506e-10
```

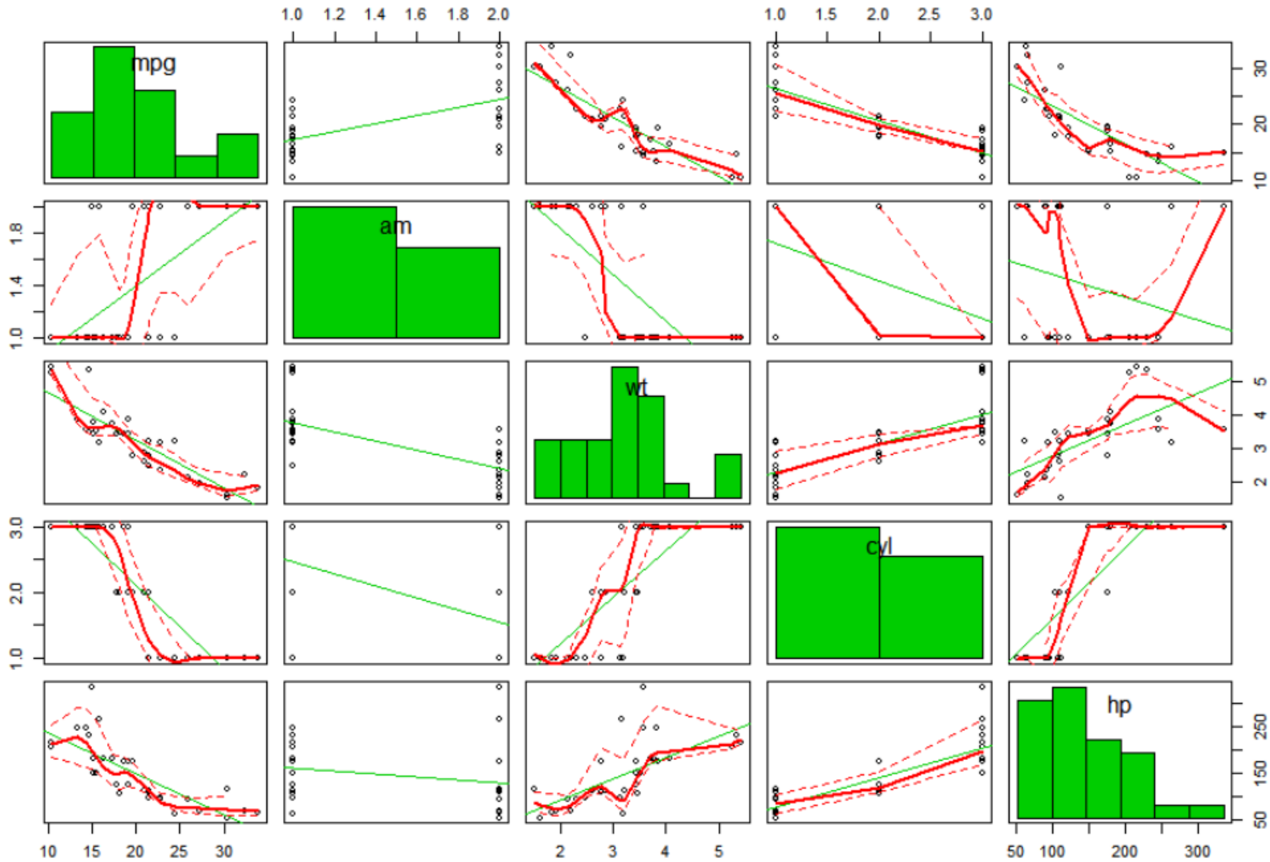
Residuals for the model *mpg ~ wt + am + hp + cyl*

```
par(mfrow=c(2,))
plot(fitR)
```



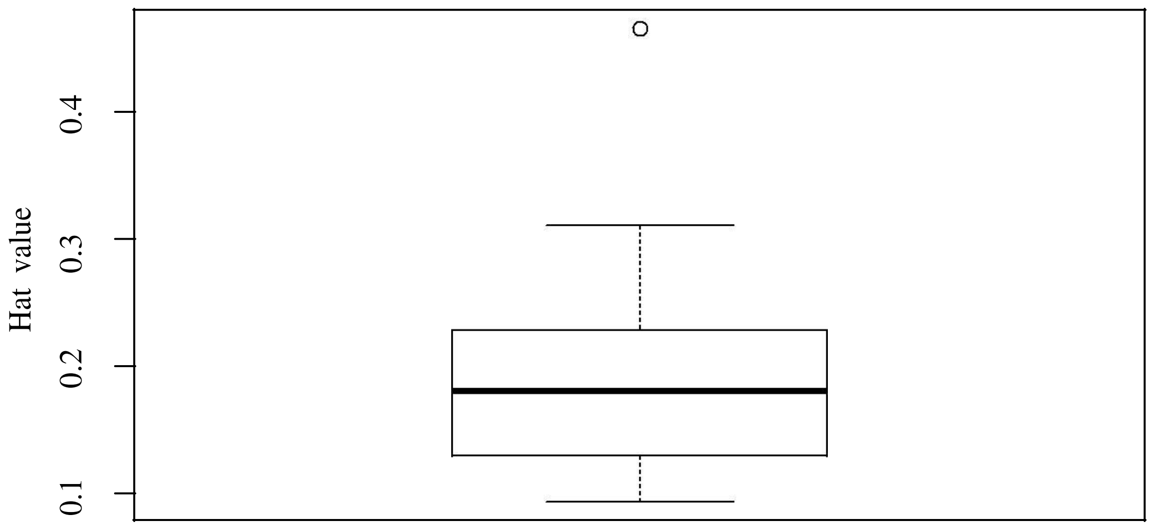
Scatterplot matrix for the model *mpg ~ wt + am + hp + cyl*

```
scatterplotMatrix(df[,c('mpg','am','wt','cyl','hp')],diagonal='histogram')
```



Boxplot of the hat values for the model *mpg ~ log(wt) + am + hp + cyl*

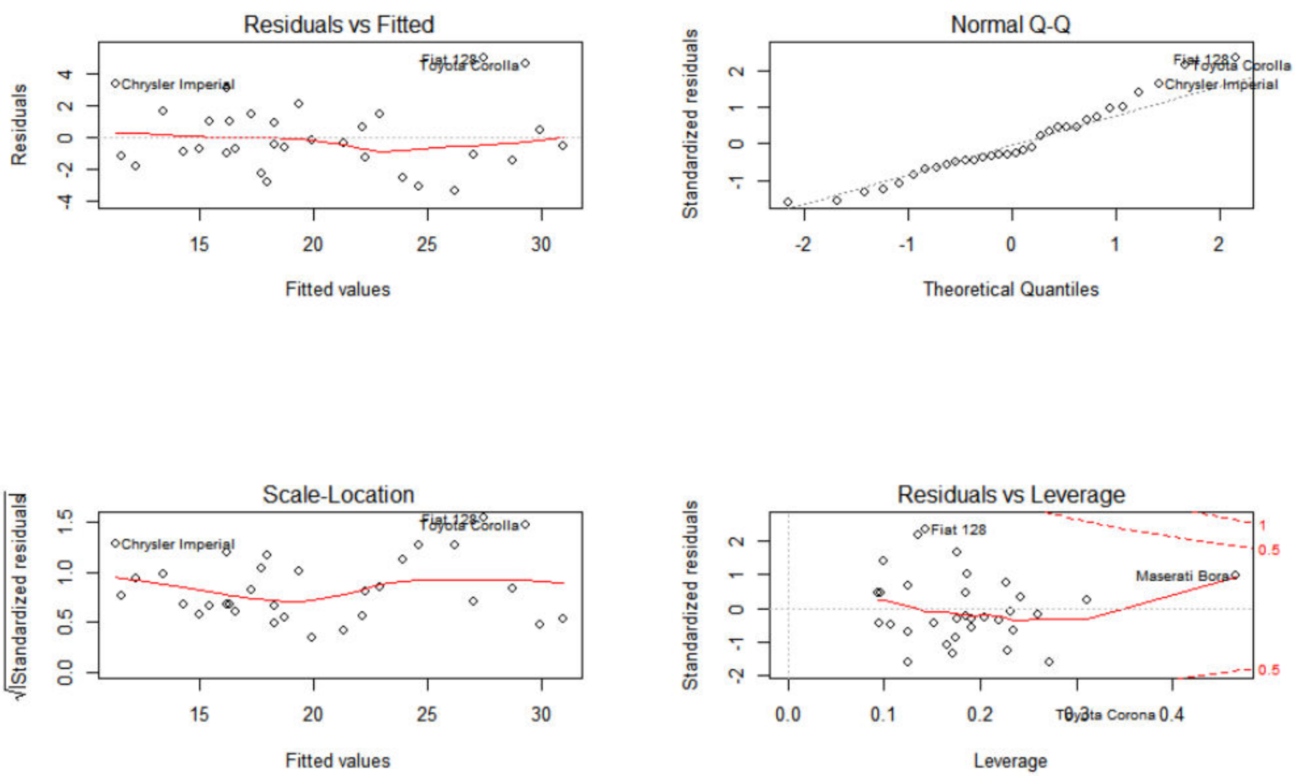
```
boxplot(hat,ylab="Hat value")
```




```
#identify(rep(1, length(hat)), hat, labels = names(hat))
```

Residuals for the model *mpg ~ log(wt) + am + hp + cyl*

```
par(mfrow=c(2,))
plot(fitR2)
```



```
hp            -0.02739    0.01315  -2.083  0.04720 *
cyl6          -2.20507    1.38085  -1.597  0.12237
cyl8          -1.78902    2.15939  -0.828  0.41494
am1            0.86663    1.41193   0.614  0.54468
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 2.269 on 26 degrees of freedom
Multiple R-squared:  0.8811, Adjusted R-squared:  0.8583
F-statistic: 38.54 on 5 and 26 DF,  p-value: 3.214e-11
```

```
> summary(fitR2)

Call:
lm(formula = mpg ~ log(wt) + hp + cyl + am, data = df)

Residuals:
   Min     1Q Median     3Q    Max
-3.380 -1.202 -0.534  1.081  4.943

Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept)  36.38795    2.85464  12.747 1.09e-12 ***
log(wt)     -10.13304    2.88903  -3.507  0.00166 **
hp           -0.02739    0.01315  -2.083  0.04720 *
cyl6         -2.20507    1.38085  -1.597  0.12237
cyl8         -1.78902    2.15939  -0.828  0.41494
am1           0.86663    1.41193   0.614  0.54468
---
Signif. codes:  0 ‘***’ 0.001 ‘**’ 0.01 ‘*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 2.269 on 26 degrees of freedom
Multiple R-squared:  0.8811, Adjusted R-squared:  0.8583
F-statistic: 38.54 on 5 and 26 DF,  p-value: 3.214e-11
```

Comparing the models with and without *am* (*mpg ~ log(wt) + am + hp + cyl* VS *mpg ~ log(wt) + hp + cyl*)

```
> lrtest(fitR2, fitR2R)
Likelihood ratio test

Model 1: mpg ~ log(wt) + hp + cyl + am
Model 2: mpg ~ log(wt) + hp + cyl
  #Df  LogLik Df  Chisq Pr(>Chisq)
1   7 -68.303
2   6 -68.533 -1 0.4604     0.4975
```