

GeeksQuiz

Computer science mock tests for geeks

Binary Insertion Sort

We can use binary search to reduce the number of comparisons in **normal insertion sort**. Binary Insertion Sort find use binary search to find the proper location to insert the selected item at each iteration. In normal insertion, sort it takes $O(i)$ (at ith iteration) in worst case. we can reduce it to $O(\log i)$ by using **binary search**.

```
// C program for implementation of binary insertion sort
#include <stdio.h>

// A binary search based function to find the position
// where item should be inserted in a[low..high]
int binarySearch(int a[], int item, int low, int high)
{
    if (high <= low)
        return (item > a[low])? (low + 1): low;

    int mid = (low + high)/2;

    if(item == a[mid])
        return mid+1;

    if(item > a[mid])
        return binarySearch(a, item, mid+1, high);
    return binarySearch(a, item, low, mid-1);
}

// Function to sort an array a[] of size 'n'
void insertionSort(int a[], int n)
{
    int i, loc, j, k, selected;

    for (i = 1; i < n; ++i)
    {
        j = i - 1;
        selected = a[i];

        // find location where selected should be inserted
        loc = binarySearch(a, selected, 0, j);

        // Move all elements after location to create space
        while (j >= loc)
        {
            a[j+1] = a[j];
            j--;
        }
    }
}
```

```
        a[j+1] = selected;
    }
}

// Driver program to test above function
int main()
{
    int a[] = {37, 23, 0, 17, 12, 72, 31,
               46, 100, 88, 54};
    int n = sizeof(a)/sizeof(a[0]), i;

    insertionSort(a, n);

    printf("Sorted array: \n");
    for (i = 0; i < n; i++)
        printf("%d ", a[i]);

    return 0;
}
```

Output:

```
Sorted array:
0 12 17 23 31 37 46 54 72 88 100
```

Time Complexity: The algorithm as a whole still has a running worst case running time of $O(n^2)$ because of the series of swaps required for each insertion.

This article is contributed by **Amit Auddy**. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

Category: Algorithms Searching and Sorting



Tweet

0

+1

0

8 Comments

GeeksQuiz

1 Login

Recommend

Share

Sort by Best



Join the discussion...

Aditya Goel · 3 months ago

I don't think the program is reducing the complexity, it is just reducing the number of

comparisons. The program is unnecessary creating an overhead of $O(\log n)$. Standard Insertion sort will be faster.

1 ^ | v • Reply • Share ›

creeping_death ➔ Aditya Goel • a month ago

I think this particular implementation is actually worse than standard insertion sort, because of the memory overhead needed for recursive binary search

1 ^ | v • Reply • Share ›

RK • 3 months ago

The tightest upper bound for time complexity is still $O(n^2)$. How is this any better than the usual insertion sort? I don't think that it reduces the constant factor or lower order terms of the time complexity either.

^ | v • Reply • Share ›



Morphine • 4 months ago

using binary search to reduce the number of comparisons, isn't the complexity is $O(n \log n)$

^ | v • Reply • Share ›

Aditya Goel ➔ Morphine • 3 months ago

Binary search just gives us the location where selected should be inserted. We still have to move all elements after location to create space. That can take $O(n)$ in worst case.

^ | v • Reply • Share ›

gooseberry • 9 months ago

I think there is a problem with the while loop used in function insertionSort. The while loop continues endlessly. there should be a lower check for $j \geq 0$.

Please correct me if I am wrong.

^ | v • Reply • Share ›

GeeksforGeeks Mod ➔ gooseberry • 9 months ago

Please take a closer look. loc is a value returned by binary search and binary search returns an index.

If you still feel it's incorrect, please provide an example array for which it fails.

^ | v • Reply • Share ›

Zsw-seu ➔ GeeksforGeeks • 2 months ago

I think there is a problem with binarySearch. Example is:

1,2,3,4,5,7

and I want to insert 7, then

the binarySearch will not be Stable. But the normal Insertion Sort will be Stable.

So I think the function binarySearch should be:

```
int binarySearch(int a[], int item, int low, int high)
{
    if (high <= low)
        return (item < a[low]) ? low : (low+1);

    int mid = (low + high)/2;

    if (item == a[mid])
        return mid+1;

    if (item > a[mid])
        return binarySearch(a, item, mid+1, high);
    return binarySearch(a, item, low, mid-1);
}
```

^ | v • Reply • Share ›