

Regular expression

$L = \{ w \mid w \text{ starts with } 0 \text{ & ends with } 1 \}$

$$0 \cdot (0 \cup 1)^* \cdot 1$$

$L = \{ w \mid w \text{ contains substring } 101 \}$

$$\cancel{(001)^*} 101 \cancel{(001)^*}$$

$$(0 \cup 1)^* 101 (0 \cup 1)^*$$

$L = \{ w \mid w \text{ contains at least three } 1 \}$

$$(0 \cup 1)^* 1 (0 \cup 1)^* 1 (0 \cup 1)^* 1 (0 \cup 1)^*$$

$L = \{ w \mid w \text{ contains exactly three } 1 \}$

$$0^* 1 0^* 1 0^* 1 0^*$$

U

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Regular Expression

U

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1. $L = \{ \omega / \omega \text{ starts with } 0 \text{ and ends with } 1 \}$

$$0 \cdot (01)^* \cdot 1$$

$$(0 \cdot 1)^* (1 \cdot 0)$$

2. $L = \{ \omega / \omega \text{ starts and ends with same symbol} \}$

$$0 \cdot (01)^* \cdot 0 \cup 1 \cdot (01)^* \cdot 1$$

3. $L = \{ \omega / \omega \text{ contains at least three characters} \}$

$$(0 \cdot 1)^* (0 \cdot 1)^* (0 \cdot 1)^* (0 \cdot 1)^*$$

4. $L = \{ \omega / \omega \text{ contains at least three 1's} \}$

$$(01)^* 1 (01)^* 1 (01)^* 1 (01)^*$$

5. $L = \{ \omega / \omega \text{ contains exactly three 1's} \}$

$$0^* \cdot 1 \cdot 0^* \cdot 1 \cdot 0^* \cdot 1 \cdot 0^*$$

6. $L = \{w \mid w \text{ contains at most three } 1's\}$

$$0^* \cup 0^* 10^* \cup 0^* 10^* 10^* \cup 0^* 10^* 10^* 10^*$$

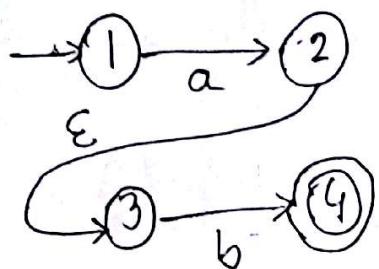
7. $L = \{w \mid w \text{ contains even no. of characters}\}$

$$\cdot ((0U1)(0U1))^* \quad \cdot ((1U0)(1U0))^*$$

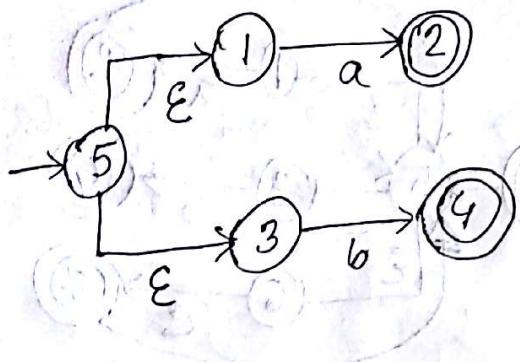
8. $L = \{w \mid w \text{ contains odd no. of characters}\}$

$$\cdot (\cancel{(0U1)^*}(0U1)^*(0U1)^*)^* \quad \cdot ((0U1)(0U1)\cancel{(0U1)})^*(0U1)$$

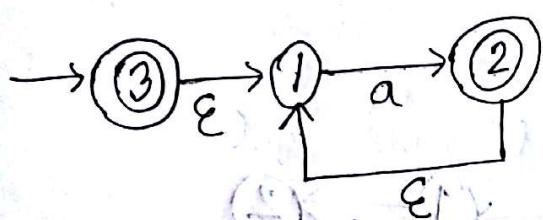
$a \cdot b$



$a \cup b$



a^*



$$1. (\cancel{a \cup b})(\cancel{a \cup b} \cup c)^*$$

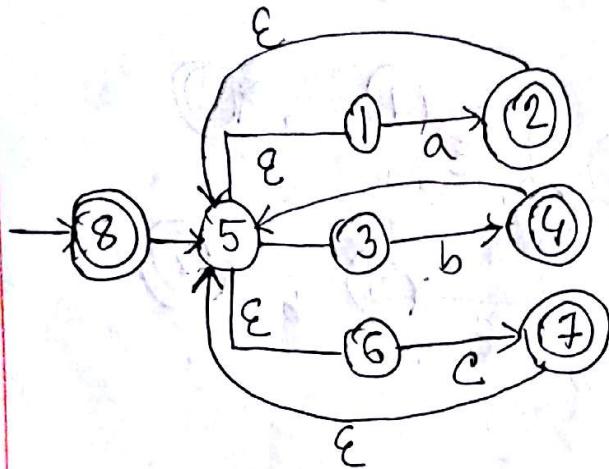
$$2. abc \cup cb\bar{a}$$

$$3. (a^*b \cup b^*a)c$$

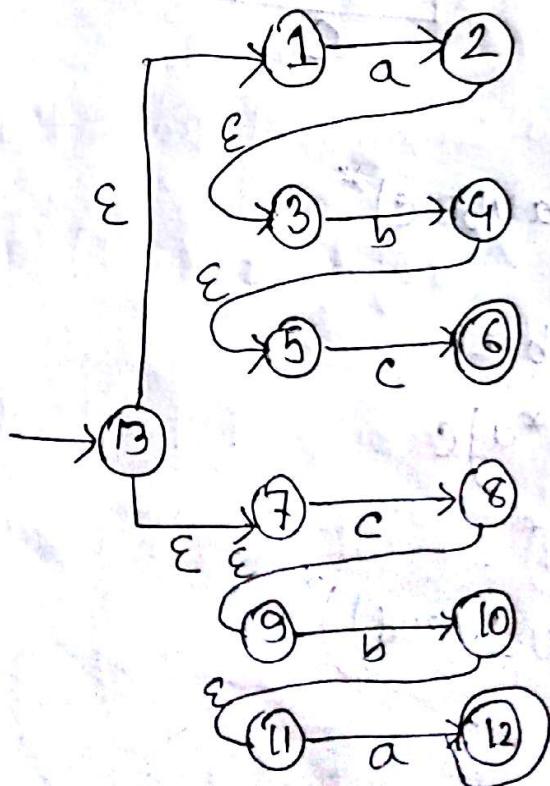
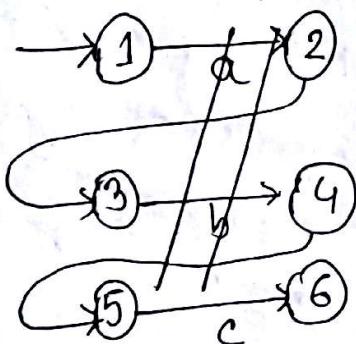
$$4. a^* \cdot b^* \cdot c^*$$

$$5. ((a \cup b) \cdot (b \cup c) \cdot (c \cup d))^*$$

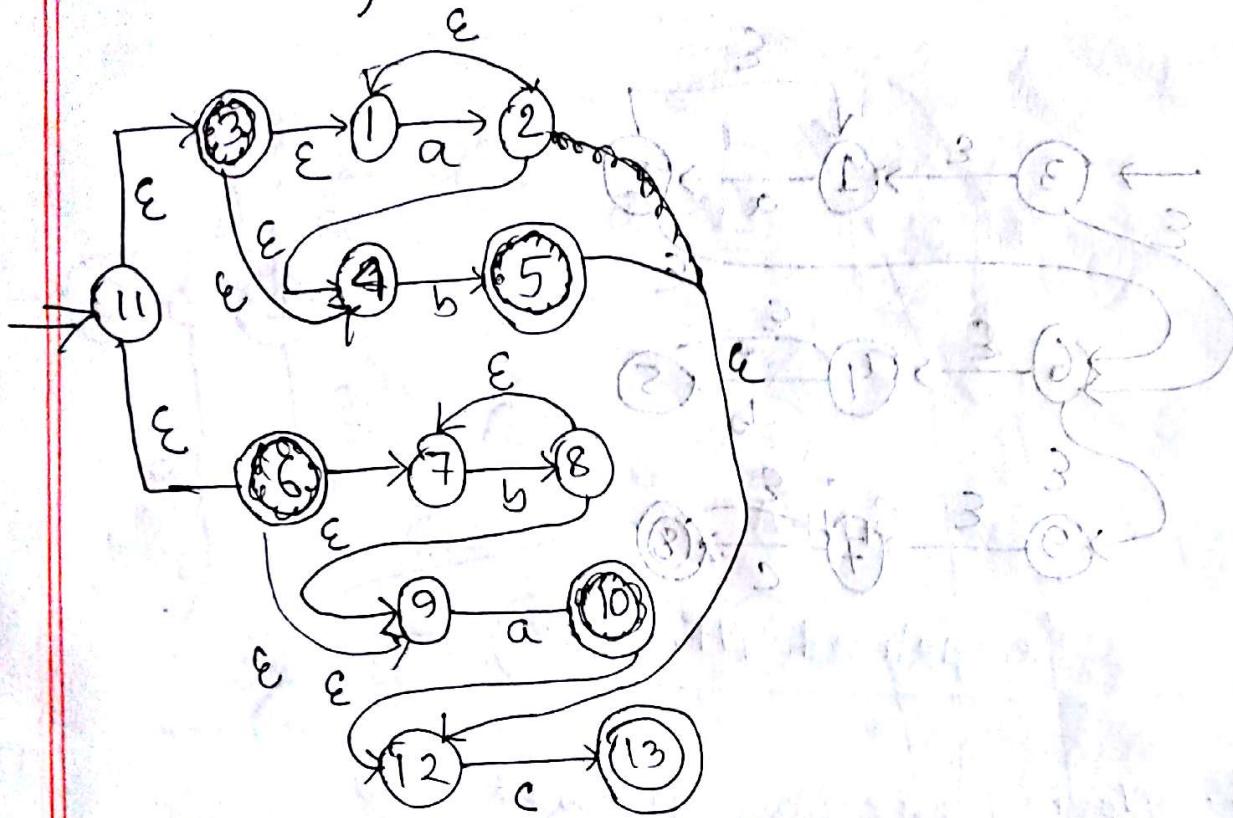
1. $(a \cup b \cup c)^*$



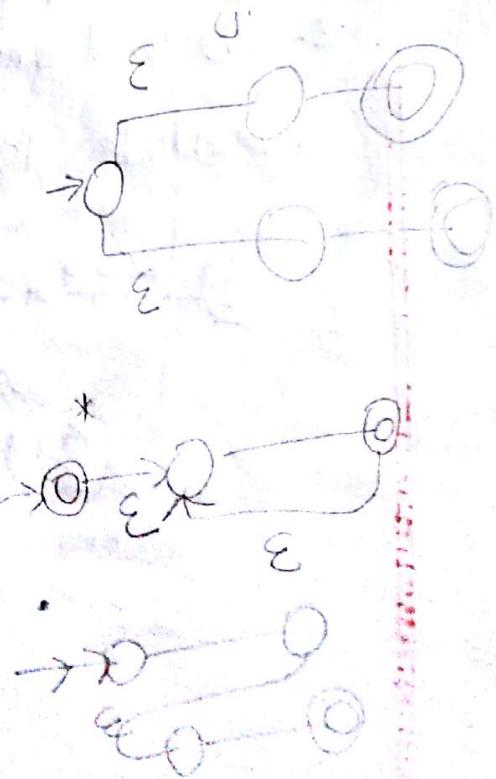
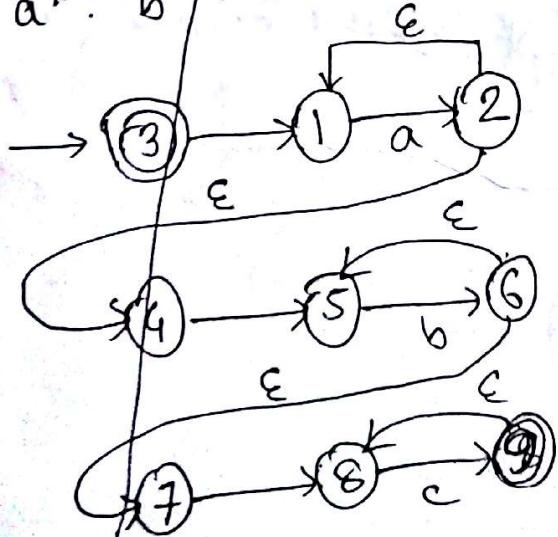
2. abc ∪ cba



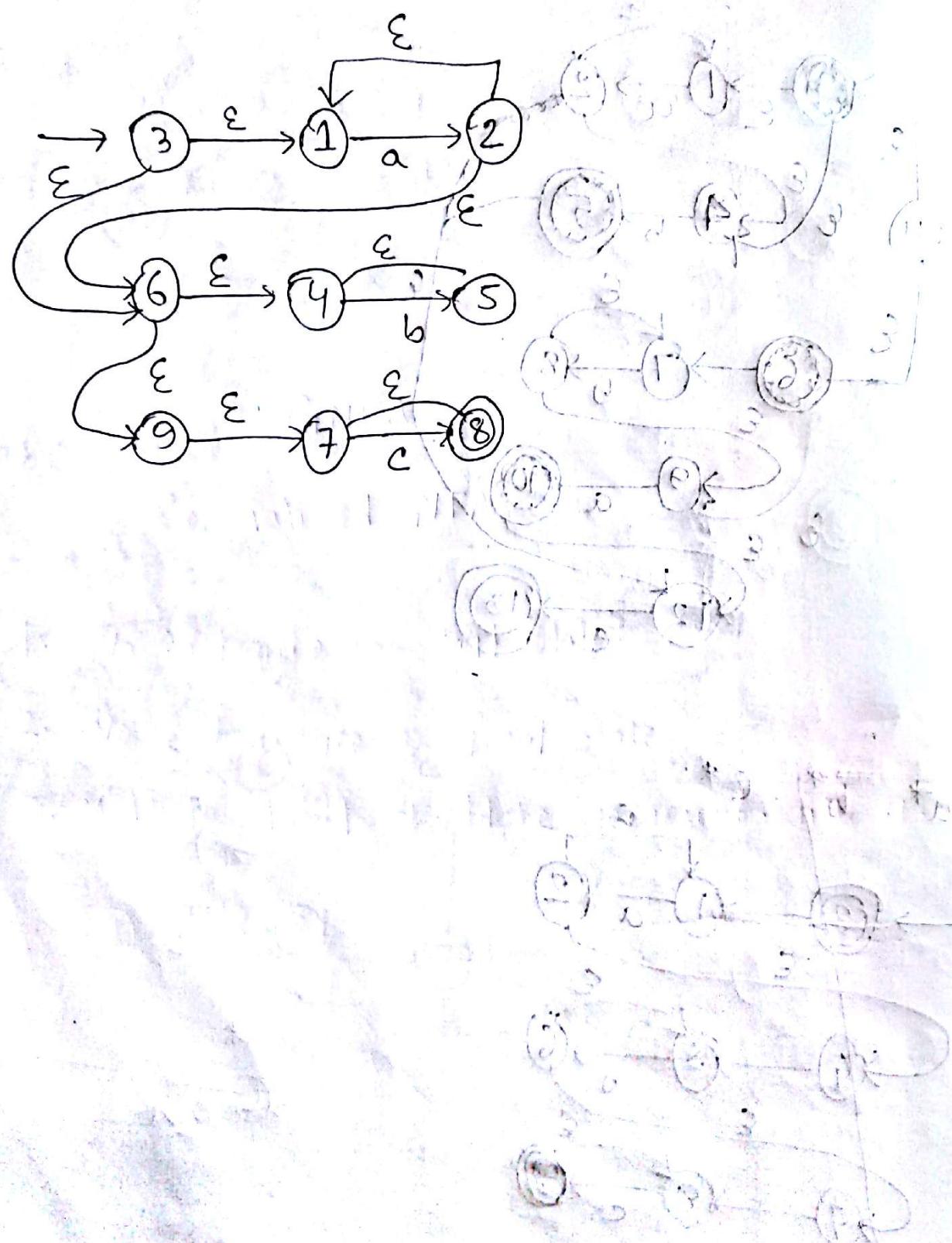
$$3. (a^* b \cup b^* a) c$$



$$4. a^* \cdot b^* \cdot c^*$$

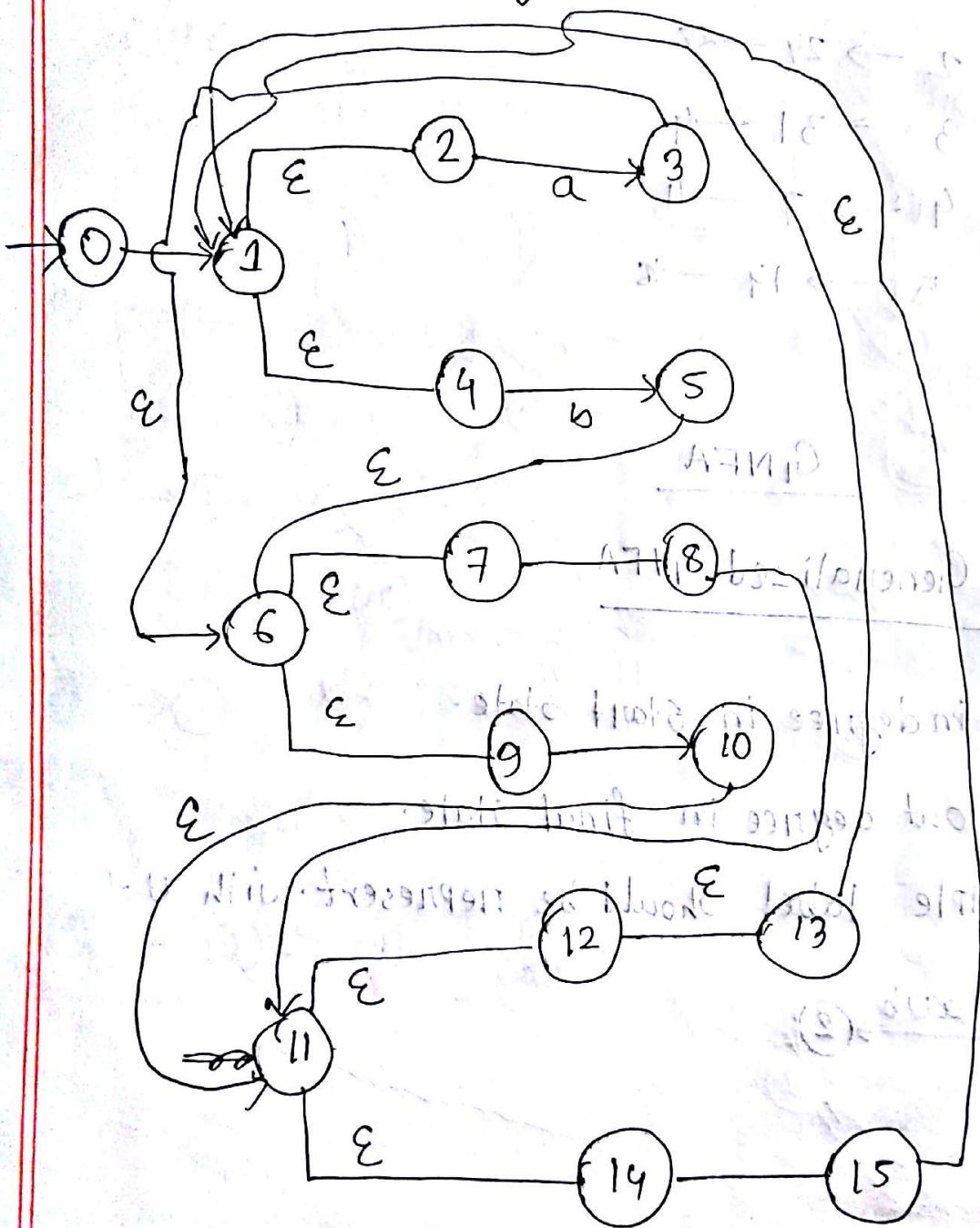


$$4. \quad a^*. b^*. c^*$$



5.

$$((a \cup b) \cdot (b \cup c) \cdot (c \cup d))^*$$



Week 1 \rightarrow 17 - 21

Week 2 \rightarrow 24 - 28

" 3 \rightarrow 31 - 4

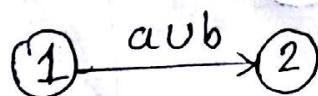
" 4 \rightarrow 7 - 11

" 5 \rightarrow 14 - 18

GNFA

Generalized NFA

1. No indegree in start state.
2. No out degree in final state.
3. Multiple label. Should be represent with U-



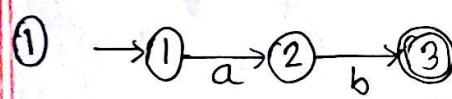
DFA \rightarrow RE

\downarrow

GNFA

\downarrow

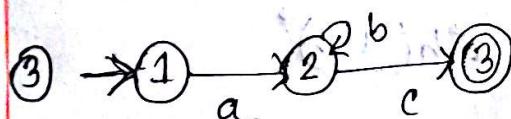
RE



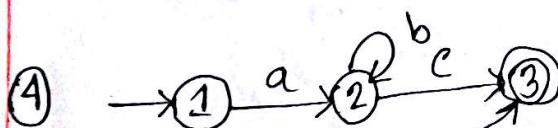
$a \cdot b$



$a \cdot (b \cup c)$

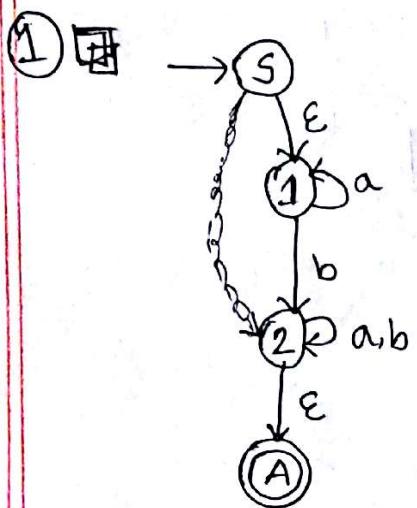


$a \cdot b^* \cdot c$



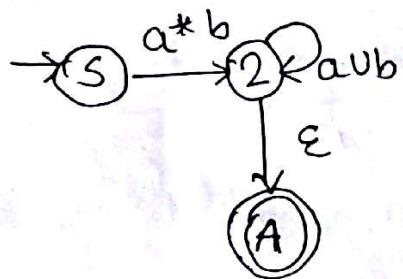
$(a \cdot b^* \cdot c) \cup d$

DFA (থেকে) GNFA (জে convert.



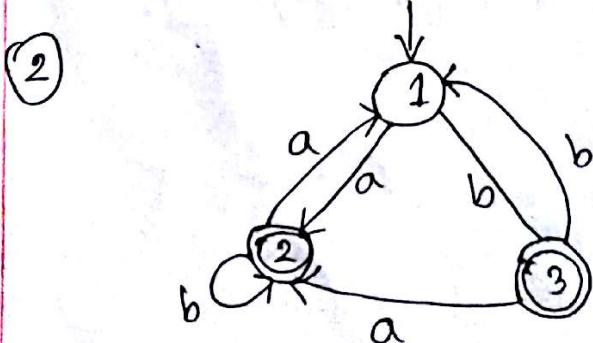
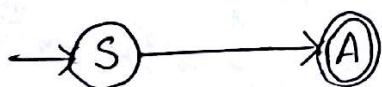
$$S \rightarrow 1 \rightarrow 2$$

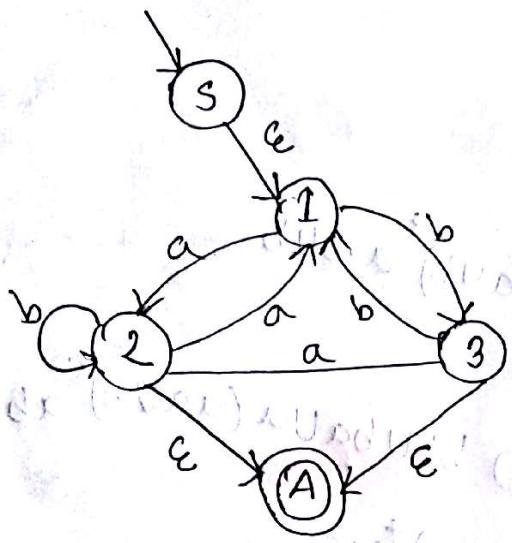
$$\epsilon \cdot a^* \cdot b$$



$$S \rightarrow 2 \rightarrow A$$

$$\epsilon \cdot a^* b (a \cup b)^*$$





$$S \rightarrow 1 \rightarrow 2 = \epsilon \cdot a = a$$

$$S \rightarrow 1 \rightarrow 3 = \epsilon \cdot b = b$$

$$2 \rightarrow 1 \rightarrow 2 = a \cdot a$$

$$2 \rightarrow 1 \rightarrow 3 = a \cdot b$$

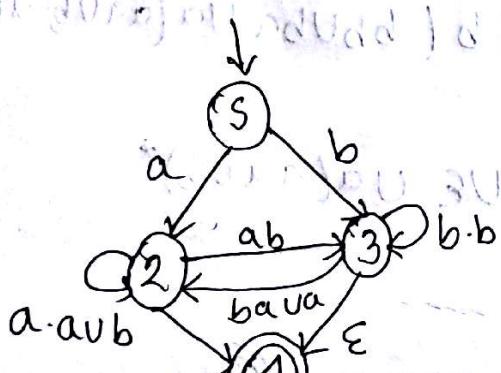
$$3 \rightarrow 1 \rightarrow 2 = b \cdot a$$

$$3 \rightarrow 1 \rightarrow 3 = b \cdot b$$

$$\Rightarrow 2 \rightarrow 2 \rightarrow a \cdot a \cup b$$

$$3 \rightarrow 2 = b \cdot a \cup a$$

1- राहि नियः



$$S \rightarrow 2 \rightarrow A = a(a \cdot a \cup b)^* \cdot \epsilon$$

$$S \rightarrow 2 \rightarrow 3 = a(a \cdot a \cup b)^* a \cdot b$$

$$3 \rightarrow 2 \rightarrow A = b \cdot a \cup a(a \cdot a \cup b)^* \cdot \epsilon$$

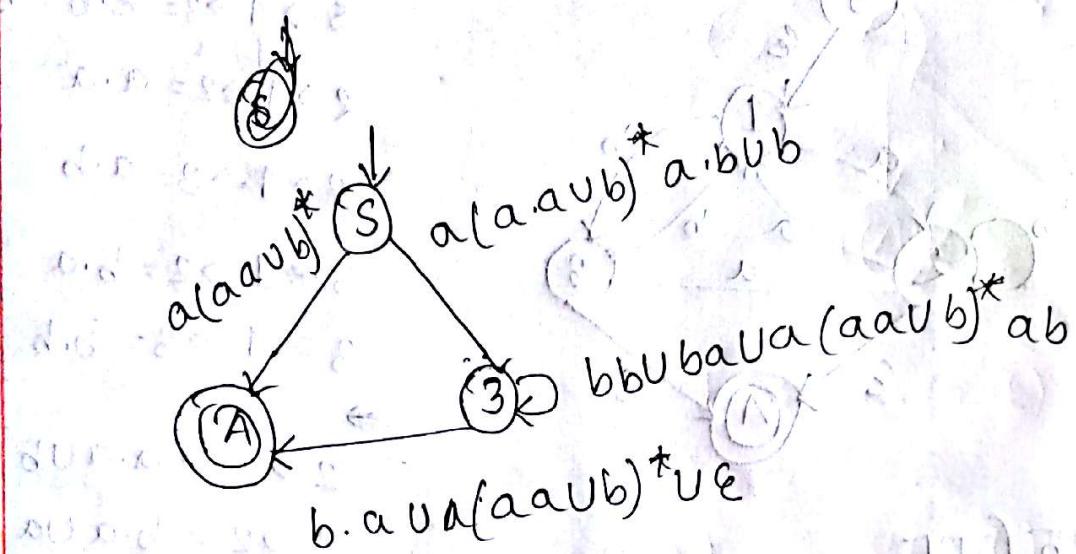
$$3 \rightarrow 2 \rightarrow 3 = b \cdot a \cup a(a \cdot a \cup b)^* ab$$

$$\Rightarrow S \rightarrow 3 = a(a \cdot a \cup b)^* a \cdot b \cup b$$

$$3 \rightarrow A = b \cdot a \cup a(a \cdot a \cup b)^* \cdot \epsilon \cup \epsilon$$

$$3 \rightarrow 3 = b \cdot b \cup b \cdot a \cup a(a \cdot a \cup b)^* ab$$

২ বাহু নেটু



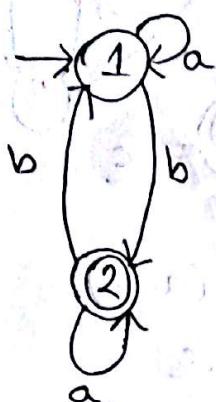
$$S \rightarrow 3 \rightarrow A = a(a \cup b)^* ab \cup b (bb \cup ba \cup a(a \cup b)^* ab)^*$$

$$\Rightarrow S \rightarrow A = ba \cup a(a \cup b)^* \cup \epsilon \cup a(a \cup b)^*$$

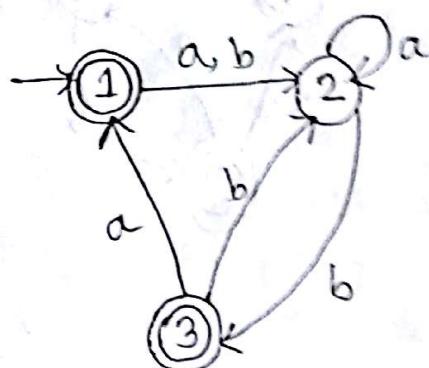
$$\xrightarrow{S} \xrightarrow{ba \cup a(a \cup b)^* \cup \epsilon \cup a(a \cup b)^*} A$$

Exercise:

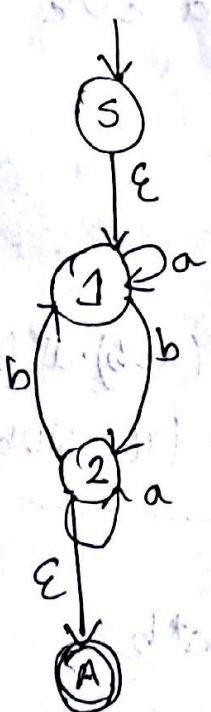
①



②



①

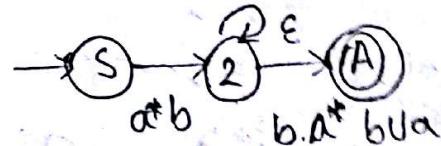


$$S \rightarrow 1 \rightarrow 2 = \epsilon \cdot a^* \cdot b = a^* \cdot b$$

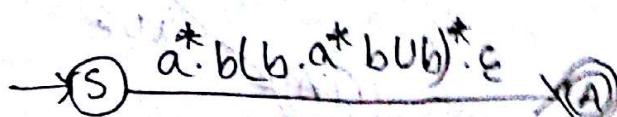
$$2 \rightarrow 1 \rightarrow 2 = b \cdot a^* \cdot b$$

$$2 \rightarrow 2 = b \cdot a^* \cdot b \cup a$$

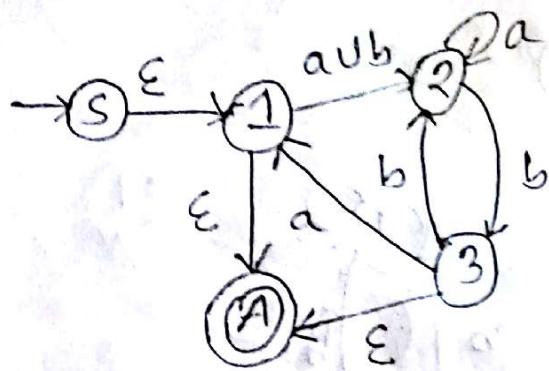
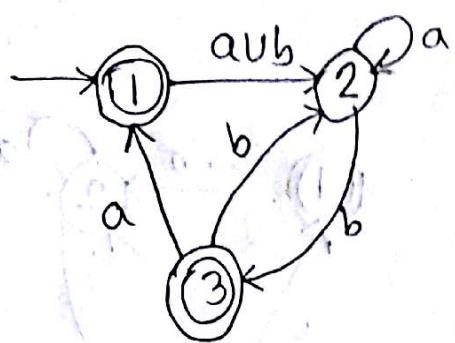
1 वाले मियां



$$S \rightarrow 2 \rightarrow A = a^* b (b \cdot a^* \cdot b \cup a)^* \cdot \epsilon$$



2



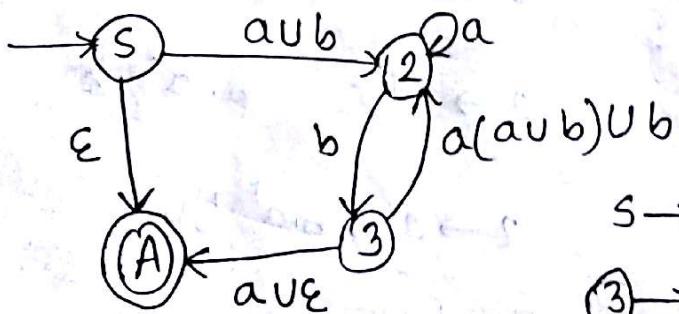
$$S \rightarrow 1 \rightarrow 2 = \epsilon \cdot (a \cup b)$$

$$S \rightarrow 1 \rightarrow A = \epsilon \cdot \epsilon$$

$$3 \rightarrow 1 \rightarrow 2 = a(a \cup b) \cup b$$

$$3 \rightarrow 1 \rightarrow A = a \cdot \epsilon \cup \epsilon$$

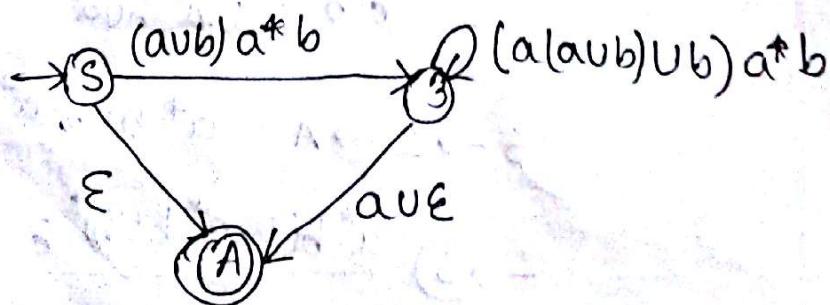
1 बाट नियम



$$S \rightarrow 2 \rightarrow 3 = (a \cup b) \cdot a^* b$$

$$(3) \rightarrow 2 \rightarrow 3 = (a(a \cup b) \cup b) \cdot a^* b$$

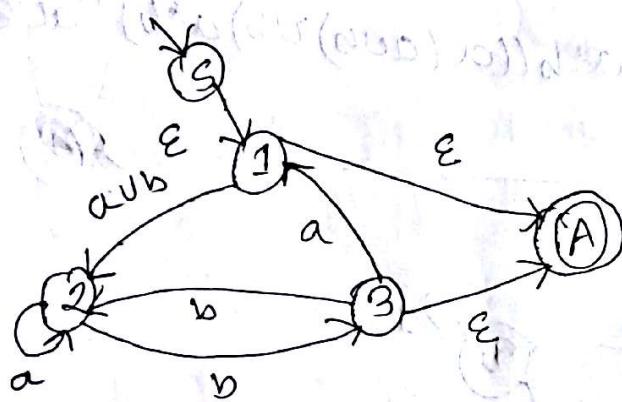
2 बाट नियम



$$S \rightarrow 3 \rightarrow A = (a \cup b) \cdot a^* b ((a(a \cup b) \cup b) a^* b)^* a \cup c \cdot c^*$$



24-7-2016



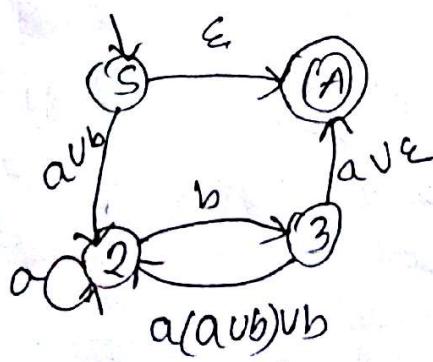
$$S \rightarrow A = \epsilon \cdot \epsilon \rightarrow \epsilon$$

$$S \rightarrow 2 \rightarrow \epsilon \cdot (a \cup b) \rightarrow a \cup b$$

$$3 \rightarrow A \rightarrow a \cdot \epsilon \rightarrow a \cup \epsilon$$

$$3 \rightarrow 2 \rightarrow a \cdot (a \cup b) \cup b$$

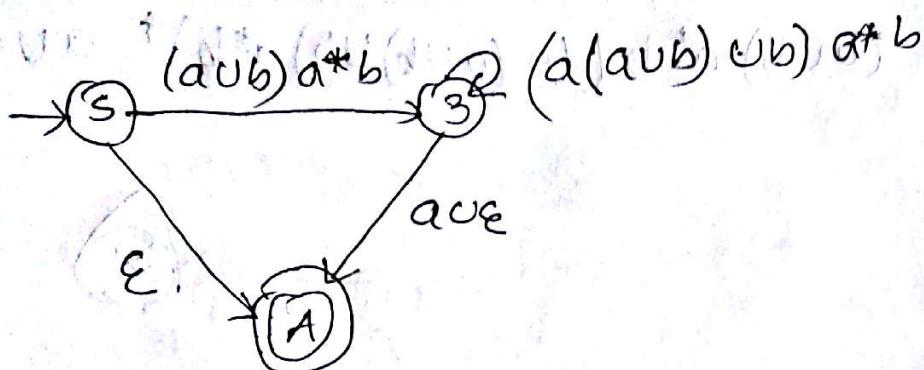
$$[a \cdot \epsilon \cup \epsilon]$$



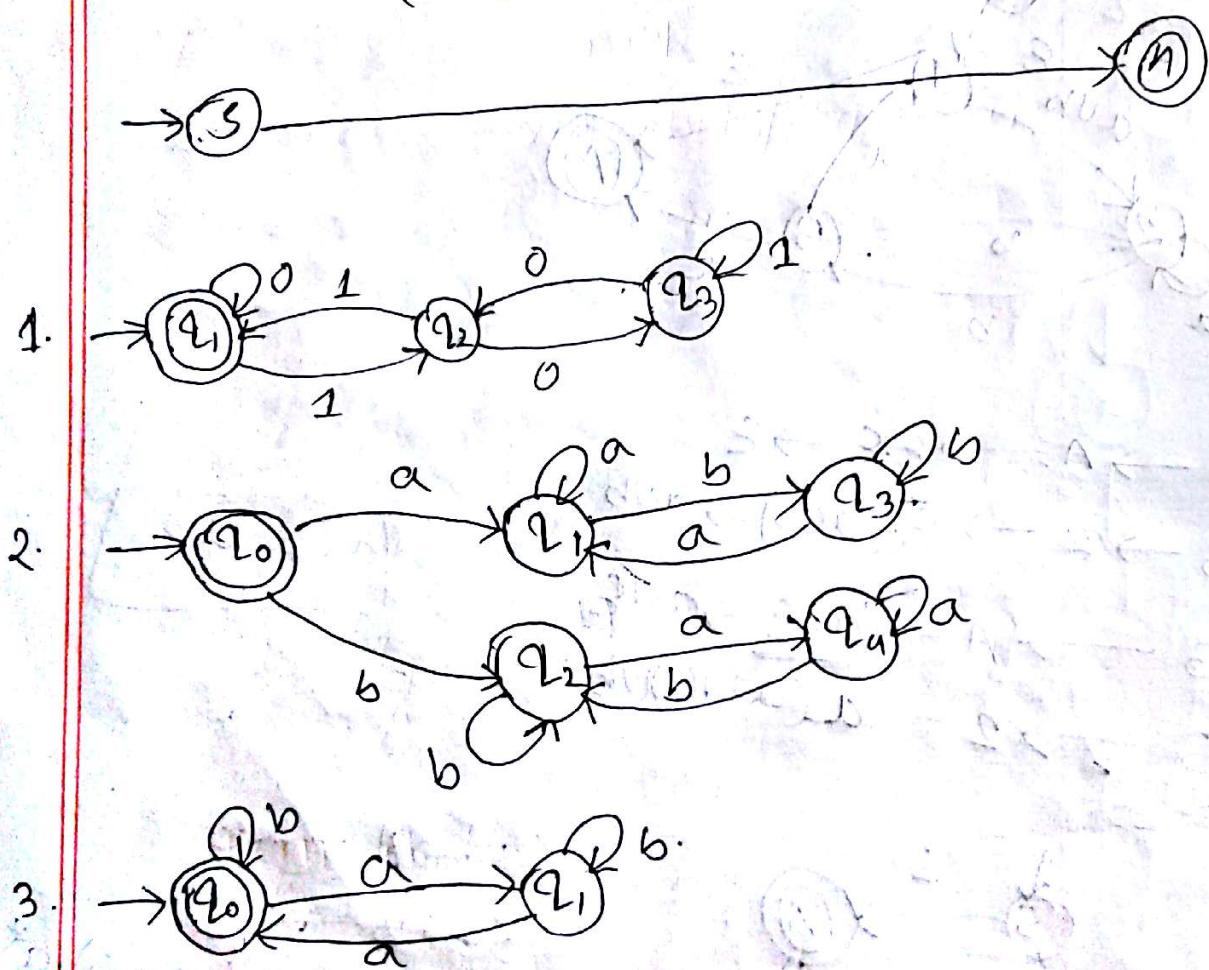
$$\begin{aligned} S &\rightarrow A \rightarrow \epsilon \\ S &\rightarrow 2 \rightarrow \end{aligned}$$

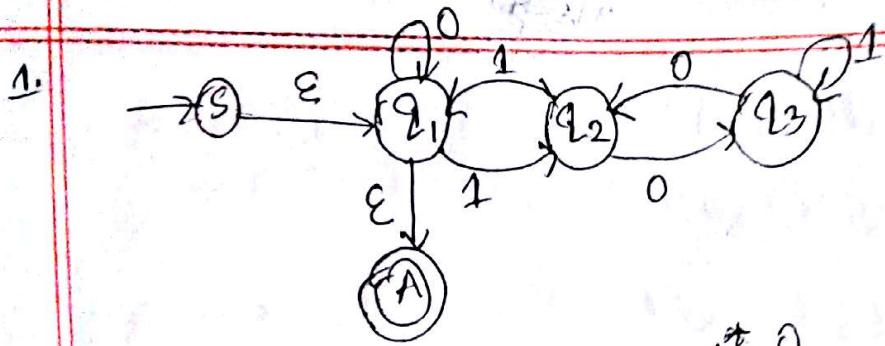
$$S \rightarrow 2 \rightarrow 3 = (a \cup b) \cdot a^* b$$

$$3 \rightarrow 2 \rightarrow 3 = (a(a \cup b) \cup b) a^* b$$

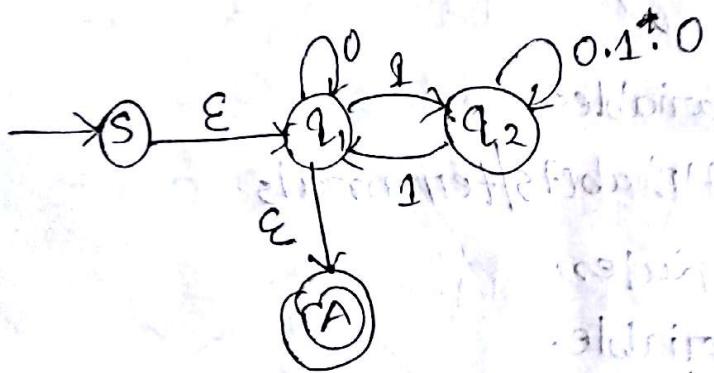


$$S \xrightarrow{} 3 \xrightarrow{} A = (a \cup b) a^* b ((a(a \cup b) \cup b) a^* b)^* a \cup b \cdot b \epsilon$$

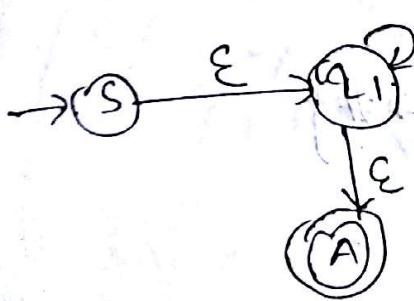




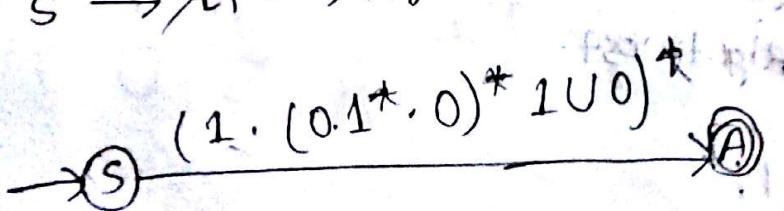
$$q_2 \rightarrow q_3 \rightarrow q_2 : 0 \cdot 1^* \cdot 0$$



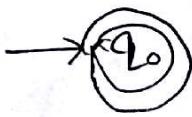
$$q_1 \rightarrow q_2 \rightarrow q_1 : 1 \cdot (0 \cdot 1^* \cdot 0)^* \cdot 1 \cup 0$$



$$s \rightarrow q_1 \rightarrow A : \epsilon \cdot (1 (0 \cdot 1^* \cdot 0)^* \cdot 1 \cup 0)^* \cdot \epsilon$$



2.



CFG

4 tuple (V, Σ, R, S)

$V \rightarrow$ set of variables

$\Sigma \rightarrow$ set of Alphabets/terminals

$R \rightarrow$ set of rules

$S \rightarrow$ start variable

$$V = \{A, B\}$$

$$\Sigma = \{0, 1, \#\}$$

$$R = \{A \rightarrow 0A1, A \rightarrow B, B \rightarrow \#\}$$

$$S \rightarrow A$$

Derivation

Leftmost

Rightmost

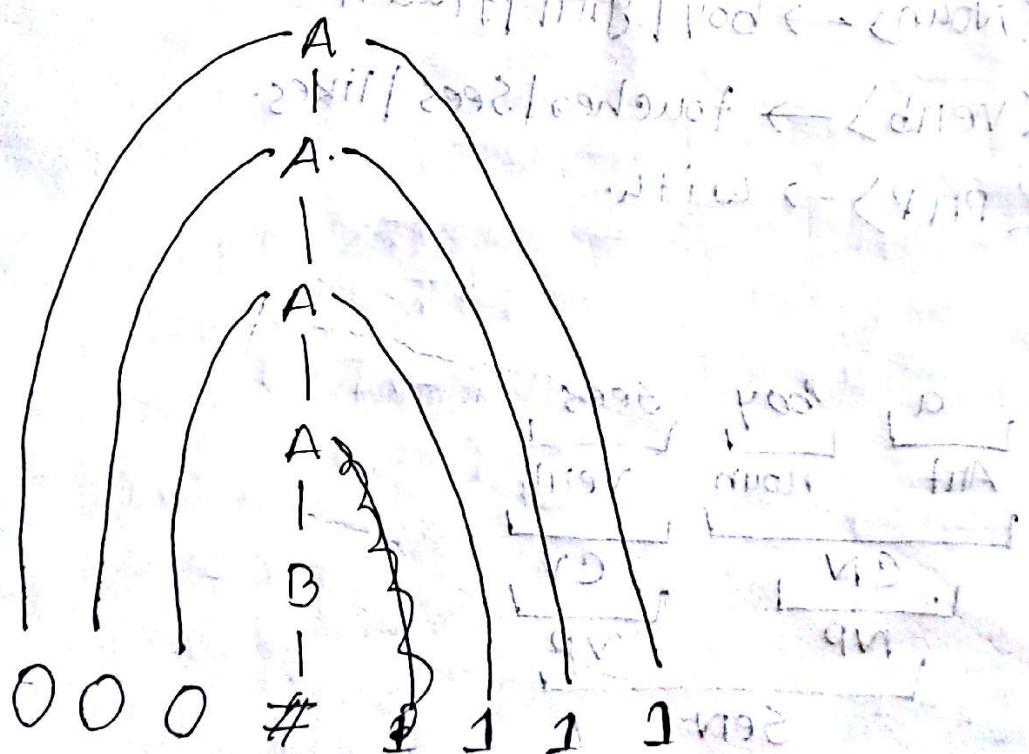
000 # 111

$$A \rightarrow 0A1 \mid B$$

$$B \rightarrow \#$$

$A \rightarrow 0 A 1$
 $\rightarrow 0 0 A 1 1$

$A \rightarrow 0 A$
 $\rightarrow 0 0 A 1 1$
 $\rightarrow 0 0 0 A 1 1$
 $\rightarrow 0 0 0 0 B 1 1$
 $\rightarrow 0 0 0 \# 1 1 1$



$\langle \text{Sen} \rangle \rightarrow \langle \text{NP} \rangle \langle \text{VP} \rangle$

$\langle \text{NP} \rangle \rightarrow \langle \text{CN} \rangle | \langle \text{CN} \rangle \langle \text{PP} \rangle$

$\langle \text{VP} \rangle \rightarrow \langle \text{CV} \rangle | \langle \text{CV} \rangle \langle \text{PP} \rangle$

$\langle \text{PP} \rangle \rightarrow \langle \text{PnPr} \rangle \langle \text{CN} \rangle$

$\langle \text{CN} \rangle \rightarrow \langle \text{Art} \rangle \langle \text{Noun} \rangle$

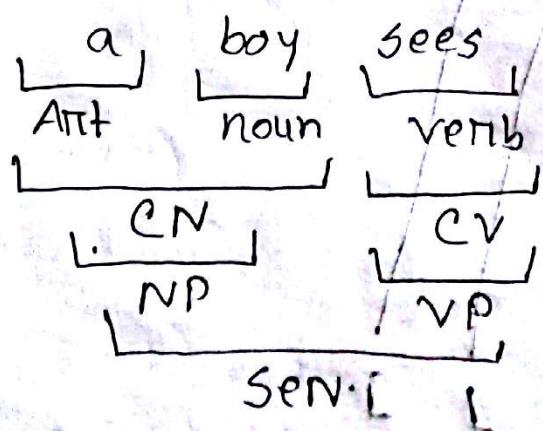
$\langle \text{CV} \rangle \rightarrow \langle \text{verb} \rangle | \langle \text{verb} \rangle \langle \text{NP} \rangle$

$\langle \text{Art} \rangle \rightarrow \text{a} | \text{the}$

$\langle \text{Noun} \rangle \rightarrow \text{boy} | \text{girl} | \text{flower}$

$\langle \text{verb} \rangle \rightarrow \text{touches} | \text{Sees} | \text{Likes}$

$\langle \text{PnPr} \rangle \rightarrow \text{with}$



$\text{Sen} \rightarrow \langle \text{NP} \rangle \langle \text{VP} \rangle$

$\rightarrow \langle \text{CN} \rangle \langle \text{VP} \rangle$

$\rightarrow \langle \text{Art} \rangle \langle \text{Noun} \rangle \langle \text{VP} \rangle$

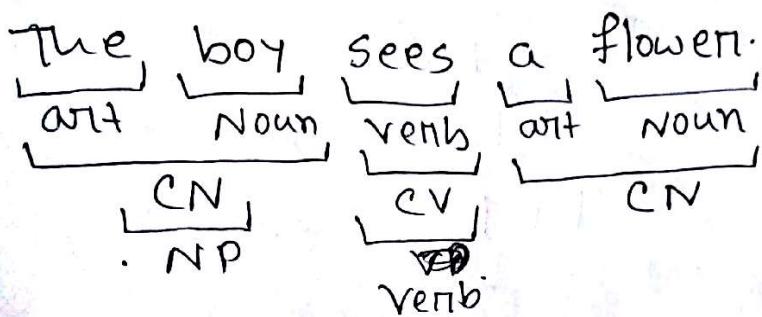
$\rightarrow \text{a} \langle \text{Noun} \rangle \xleftarrow{\text{verb}} \langle \text{VP} \rangle$

→ a boy ~~verb~~ <VP>

→ a boy sees <CV>

→ a boy <verb>

→ a boy sees.



Sen → <NP> <VP>

→ <CN> <VP>

→ <Art> <Noun> <VP>

→ a <Noun> <VP>

→ a boy <VP>

→ a boy <CV>

→ a boy <V> <NP>

→ a boy sees <NP> <CN>

→ a boy sees <Art> <Noun>

→ a boy sees a <Nouns>

→ a boy sees a flower.

$$E \rightarrow E + T \mid T$$
$$T \rightarrow T \times F \mid F$$
$$F \rightarrow (E) \mid a$$

1. (a)

2. $(a+a) \times a$

3. $(a+a \times a)$

4. $((a+a))$

1. (a) \rightarrow

$$\begin{aligned} F &\rightarrow (E) \\ &\rightarrow (T) \\ &\rightarrow (F) \\ &\rightarrow (a) \end{aligned}$$

3. $(a+a \times a)$

$$\begin{aligned} F &\rightarrow (E) \\ &\rightarrow (E+T) \\ &\rightarrow (E+E+T \times F) \\ &\rightarrow (T+F \times a) \\ &\rightarrow (F+a \times a) \\ &\rightarrow (a+a \times a) \end{aligned}$$

2. $(a+a) \times a$

$$\begin{aligned} F &\rightarrow (E) \\ &\rightarrow (E+T) \\ &\rightarrow (T+T \times F) \end{aligned}$$

~~$F \rightarrow E+T$~~

~~$T \rightarrow T \times F$~~

~~$\oplus F \times a \rightarrow F \times F$~~

~~$(E) \times a$~~

~~$(E+T) \times a$~~

~~$(T+F) \times a$~~

~~$(F+a) \times a$~~

~~$(a+a) \times a$~~

4. $((\alpha + \alpha))$

$F \rightarrow (E)$

$\rightarrow (\cancel{E+T})$

$\rightarrow (T)$

$\rightarrow (F)$

$\rightarrow ((E))$

$\rightarrow ((E+T))$

$\rightarrow ((T+\cancel{F})) \rightarrow ((T+T))$

$\rightarrow ((\cancel{F}+\alpha)) \rightarrow ((F+T))$

$\rightarrow ((\alpha+\alpha)) \rightarrow ((\alpha+T))$

$\rightarrow ((\alpha+F))$

3. $(\alpha + \alpha \times \alpha) \rightarrow ((\alpha + \alpha))$

$F \rightarrow (E)$

$\rightarrow (E+T) \rightarrow (\cancel{T+T})$

$\rightarrow (\cancel{E}+T) \rightarrow (E+T)$

$\rightarrow (\cancel{E}+T) \rightarrow (T+T)$

$\rightarrow (T+T) \rightarrow (F+T)$

$\rightarrow (F+TXF) \rightarrow (\alpha+T)$

$\rightarrow (\alpha+FX\alpha) \rightarrow (\alpha+TXF)$

$\rightarrow (\alpha+\cancel{\alpha}\times\alpha) \rightarrow (\alpha+FXF)$

$\rightarrow (\alpha+\alpha\times F) \rightarrow ((\alpha+\alpha)\times\alpha)$

$\rightarrow ((\alpha+\alpha)\times\alpha)$

2. $(a+a) \times a$

$$\begin{array}{l} E \rightarrow E/F/T \\ \quad\quad\quad\diagdown \\ \rightarrow T+T \\ \rightarrow F+T \\ \quad\quad\quad\diagup \end{array}$$

$$\begin{array}{l} E \rightarrow T \\ \rightarrow \emptyset T \times F \\ \rightarrow (\cancel{E}) F \times F \\ \rightarrow (\cancel{E}) (E) \times F \\ \rightarrow (E+T) \times F \\ \rightarrow (T+T) \times F \\ \rightarrow (F+T) \times F \\ \rightarrow (a+T) \times F \\ \rightarrow (a+F) \times F \\ \rightarrow (a+a) \times F \\ \rightarrow (a+a) \times a \end{array}$$

$L = \{ w | w \text{ starts and ends with same symbol} \}$

$(0 \cup 1)^*$

$R \rightarrow 0R \mid 1R \mid \epsilon$

~~OR~~

$((0+0))$

$((1))$

$((0+1))$

$((1))$

$((1))$

$((0+1))$

$((1+1))$

$((0+1))$

$((1+1))$

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$((0+1))$

$((1+1))$

$((0+1))$

$((1+1))$

Q L = {w | w starts and ends with same symbol}

$$S \rightarrow ORO \mid 1R1$$

$$R \rightarrow OR \mid 1R \mid \epsilon$$

Q L = {w contains at least three 1's}

$$S \rightarrow R1 \ R1 \ R1 \ R$$

$$R \rightarrow OR \mid 1R \mid \epsilon.$$

Q L = {w contains exactly three 1's}

$$S \rightarrow R1 \ R1 \ R1 \ R$$

$$S \rightarrow OR \mid \epsilon.$$

Q L = {w | w contains substring 101}

$$\boxed{R \rightarrow \epsilon \mid OR \mid 1R}$$

$$(OU1)^*$$

$$\boxed{O(OU1)^* O \ U1(OU1)^* 1}$$

$$S \rightarrow ORO \mid 1R1$$

$$\boxed{R \rightarrow \epsilon \mid OR}$$

$$O^*$$

Q L = {w | length of w is even}

Q L = {w | length of w is odd}



□ $L = \{ w \mid w \text{ contains substring } 10^1 \}$

$$S \rightarrow R101R$$

$$R \rightarrow \epsilon | OR11R$$

□ $L = \{ w \mid \text{length of } w \text{ is even} \}$

$$S \rightarrow \cancel{RR} + \epsilon | RSS$$

$$R \rightarrow 0/1$$

$$S \rightarrow \epsilon | RSS$$

$$R \rightarrow 0/1$$

□ $L = \{ w \mid \text{length of } w \text{ is odd} \}$

$$S \rightarrow AR$$

$$A \rightarrow \epsilon | RRA$$

$$R \rightarrow 011$$

□ $L = \{ w \mid w = a^m b^n \text{ and } m=n \}$

$$\begin{array}{ccc} a^m & b^n & m=n \\ a^i & b^j c^k & \end{array}$$

□ $S \rightarrow \epsilon | ab | asb$

$$S \rightarrow \epsilon | asb$$

④

$L = \{ \omega | \omega = a^m b^n \text{ and } m = 2n \}$

$S \rightarrow \epsilon | aab$

④

$L = \{ \omega | \text{length of } \omega \text{ is odd and middle symbol is } 0 \}$

$S \rightarrow 0 | 0S0 | 1S0 | 0S1 | 1S1 \cdot$

~~0~~
0
0 0 1
1 0 0
1 0 1

④

$L = \{ \omega | \omega \text{ contains more } a's \text{ than } b's \}$

$S \rightarrow R a R$

$R \rightarrow \epsilon | aRb | bRa | aR$

④

$L = \{ \omega | \omega^* = a^m b^n \text{ and } m > n \}$

$S \rightarrow aSR | \epsilon$

$R \rightarrow \epsilon | aRb | bRa$

Q L = { each a in w. is followed by at least one b }

$$S \rightarrow \epsilon \mid abS \mid bS$$

$$S \rightarrow TR \mid RT$$

$$T \rightarrow abTE$$

$$R \rightarrow bR \mid \epsilon$$

$$S \rightarrow ASA \mid aB$$

$$A \rightarrow B \mid S$$

$$B \rightarrow b \mid \epsilon$$

$$CFG \rightarrow CNF$$

1. $S \rightarrow aXbX$

$$X \rightarrow aY \mid bY \mid \epsilon$$

$$Y \rightarrow X \mid c$$

2. $S \rightarrow XaX \mid bX \mid Y$

$$X \rightarrow XaX \mid XbX \mid \epsilon$$

$$Y \rightarrow ab$$

3. $S \rightarrow XaX \mid YY \mid XY$

$$X \rightarrow b \mid \epsilon$$

$$Y \rightarrow Xa$$

1. $S \rightarrow aXbX$

$X \rightarrow aY|bY|\epsilon$

$Y \rightarrow X|c$

\rightarrow Remove $X \rightarrow \epsilon$

$S_0 \rightarrow S$

$S \rightarrow aXbX|abX|axb|ab$

$X \rightarrow aY|bY$

$Y \rightarrow X|c|\epsilon$

\rightarrow Remove $Y \rightarrow \epsilon$

$S_0 \rightarrow S$

$S \rightarrow aXbX|abX|axb|ab$

$X \rightarrow aY|bY|a|b$

$Y \rightarrow X|c$

\rightarrow Remove ~~$X \rightarrow aY|bY|a|b$~~ $X \rightarrow X$

$S_0 \rightarrow S$

$S \rightarrow aXbX|abX|axb|ab$

$X \rightarrow aY|bY|a|b$

$Y \rightarrow aY|bY|a|bc$

\rightarrow Remove $S_0 \rightarrow S$

$S_0 \rightarrow aXbX|abX|axb|ab$

$S \rightarrow aXbX|abX|axb|ab$

$X \rightarrow aY|bY|a|b$

$Y \rightarrow aY|bY|a|bc$

\rightarrow Add $U \rightarrow a$

$S_0 \rightarrow UXbX | UbX | UXb | Ub$

$S \rightarrow UXbX | UbX | UXb | Ub$

$X \rightarrow UY | bY | a1b$

$Y \rightarrow UY | bY | a1b | c$

$U \rightarrow a$

\rightarrow add $V \rightarrow b$

$S_0 \rightarrow UXVX | UVX | UXV | UV$

$S \rightarrow UXVX | UVX | UXV | UV$

$X \rightarrow UY | VY | a1b$

$Y \rightarrow UY | VY | a1b | c$

$U \rightarrow a$

$V \rightarrow b$

\rightarrow add $W \rightarrow U$

$S_0 \rightarrow WVX | UVX | WV | UV$

$S \rightarrow WVX | UVX | WV | UV$

$X \rightarrow UY | VY | a1b$

$Y \rightarrow UY | VY | a1b | c$

$U \rightarrow a$

$V \rightarrow b$

$W \rightarrow UX$

\rightarrow add $Z \rightarrow VX$

$S_0 \rightarrow WZ | UZ | WV | UV$

$S \rightarrow WZ | UZ | WV | UV$

$X \rightarrow UY | VY | a1b$

$Y \rightarrow UY | VY | a1b | c$

$U \rightarrow a$

$V \rightarrow b$

$W \rightarrow UX$

$Z \rightarrow VX$

3. $S \rightarrow XaX | YY | XY$

$X \rightarrow b | \epsilon$

$Y \rightarrow Xa$

\rightarrow

$S_0 \rightarrow S$

$S \rightarrow XaX | YY | XY$

$X \rightarrow b | \epsilon$

$Y \rightarrow Xa$

\rightarrow

$S_0 \rightarrow S$

$S \rightarrow XaX | YY | XY | ax | Xa | a | Y$

$X \rightarrow b$

$Y \rightarrow Xa | \epsilon$

\rightarrow

$S_0 \rightarrow S$

$S \rightarrow XaX | YY | XY | ax | Xa | a | Y | x | \epsilon$

$X \rightarrow b$

$Y \rightarrow Xa$

\rightarrow

$S_0 \rightarrow S | \epsilon$

$S \rightarrow XaX | YY | XY | ax | Xa | a | Y | x$

$X \rightarrow b$

$Y \rightarrow Xa$

$\rightarrow s_0$

$s \rightarrow s|\epsilon$

$s \rightarrow xux|yy|xy|ux|xu|a|y|x$

$x \rightarrow b$

$y \rightarrow xu$

$u \rightarrow a$

\rightarrow

$s_0 \rightarrow s|\epsilon$

$s \rightarrow vx|yy|xy|ux|xu|a|b|xa$

$x \rightarrow b$

$y \rightarrow xu$

$u \rightarrow a$

$v \rightarrow xv$

$\rightarrow s$

$s_0 \rightarrow s|\epsilon$

$s \rightarrow vx|yy|xy|ux|xu|a|b|xo$

$x \rightarrow b$

$y \rightarrow xu$

$u \rightarrow a$

$v \rightarrow xo$

2. $S \rightarrow XaX \mid bX \mid Y$

$X \rightarrow XaX \mid XbX \mid \epsilon$

$Y \rightarrow ab$

$S_0 \rightarrow S$

$S \rightarrow XaX \mid bX \mid Y$

$X \rightarrow XaX \mid XbX \mid \epsilon$

$Y \rightarrow ab$

Remove $X \rightarrow \epsilon$

$S_0 \rightarrow S$

$S \rightarrow XaX \mid bX \mid Y \mid aX \mid Xa \mid a \mid b$

$X \rightarrow XaX \mid XbX \mid Xa \mid aX \mid a \mid Xb \mid bX \mid b$

$Y \rightarrow ab$

Remove $S \rightarrow Y$

$S_0 \rightarrow S$

$S \rightarrow XaX \mid bX \mid ab \mid aX \mid Xa \mid a \mid b$

$X \rightarrow XaX \mid XbX \mid Xa \mid aX \mid a \mid Xb \mid bX \mid b$

$Y \rightarrow ab$

Remove $S_0 \rightarrow S$

$S_0 \rightarrow XaX \mid bX \mid ab \mid aX \mid Xa \mid a \mid b$

$S \rightarrow XaX \mid bX \mid ab \mid aX \mid Xa \mid a \mid b$

$X \rightarrow XaX \mid XbX \mid Xa \mid aX \mid a \mid Xb \mid bX \mid b$

$Y \rightarrow ab$

Add

$$P \rightarrow a \quad R \rightarrow b$$

$$S_0 \rightarrow X P X | R X | P R | a P X | X P | a | b$$

$$S \rightarrow X P X | R X | P R | P X | X P | a | b$$

$$X \rightarrow X P X | X R X | X P | P X | a | X R | R X | b$$

$$Y \rightarrow PR$$

$$P \rightarrow a$$

$$R \rightarrow b$$

Add $T \rightarrow P X \quad U \rightarrow R X$

$$S_0 \rightarrow P X T | R X | P R | P X | X P | a | b$$

$$S \rightarrow X T | R X | P R | P X | X P | a | b$$

$$X \rightarrow X T | X U | X P | P X | a | X R | R X | b$$

$$Y \rightarrow PR$$

$$P \rightarrow a$$

$$R \rightarrow b$$

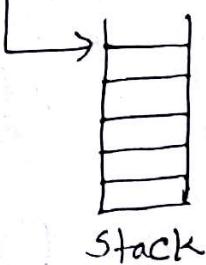
$$T \rightarrow P X$$

$$U \rightarrow R X$$

TOC

Push Down Automata

Finite Automata



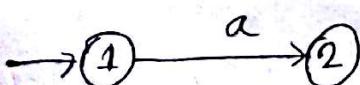
$Q \rightarrow$
 $\Sigma \rightarrow$
 $S \rightarrow$
 $z_0 \rightarrow$
 $F \rightarrow$
 $\Gamma \rightarrow$

FA

$$S: Q \times \Sigma \rightarrow Q$$

PDA

$$S: Q \times \Sigma \times \Gamma \rightarrow Q \times \Gamma$$



$x, y \rightarrow z$

$x \rightarrow$ input alphabet from Σ .

ϵ if no input.

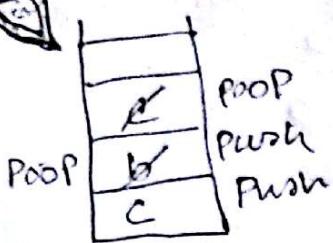
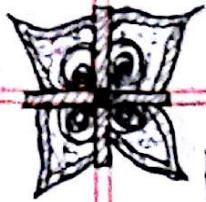
\varnothing if end of input.

$y \rightarrow$ stack top symbol to be popped.

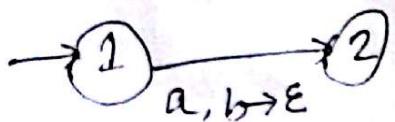
ϵ if no pop.

$z \rightarrow$ symbol to be pushed.

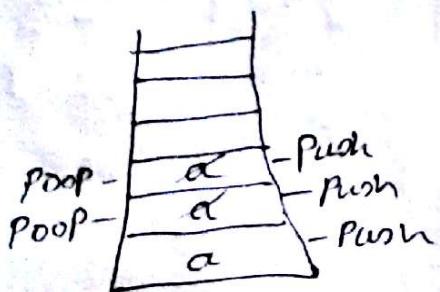
ϵ if no push.



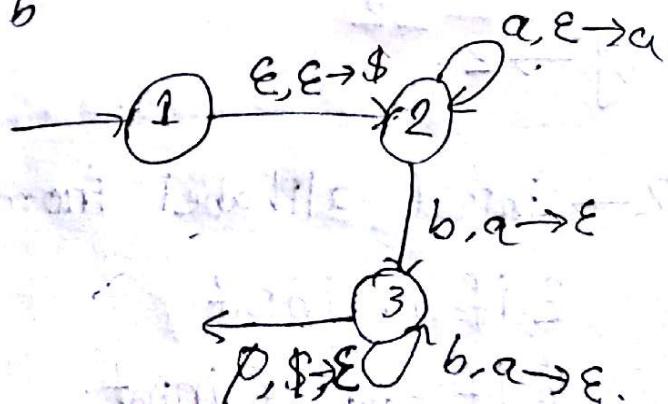
$a, \epsilon \rightarrow c$
 $a, \epsilon \rightarrow b$
 $\epsilon, \epsilon \rightarrow c$
 $a, c \rightarrow \epsilon$
 $\emptyset, b \rightarrow \epsilon$
 $a, b \rightarrow c$



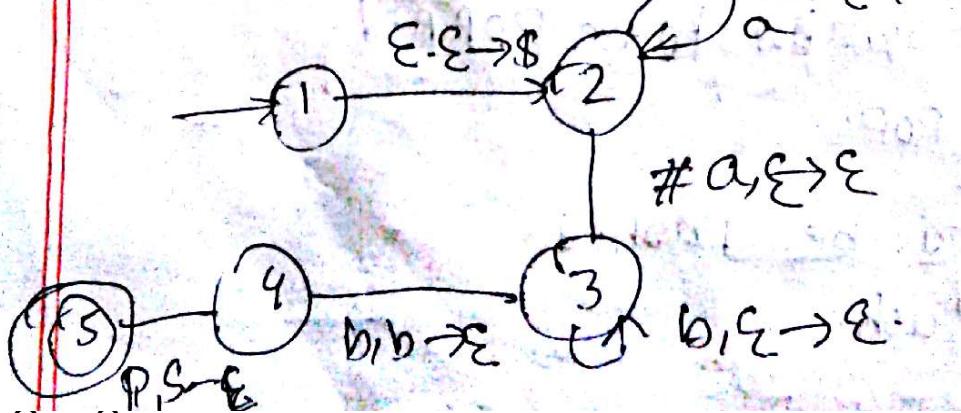
$a^n b^n$



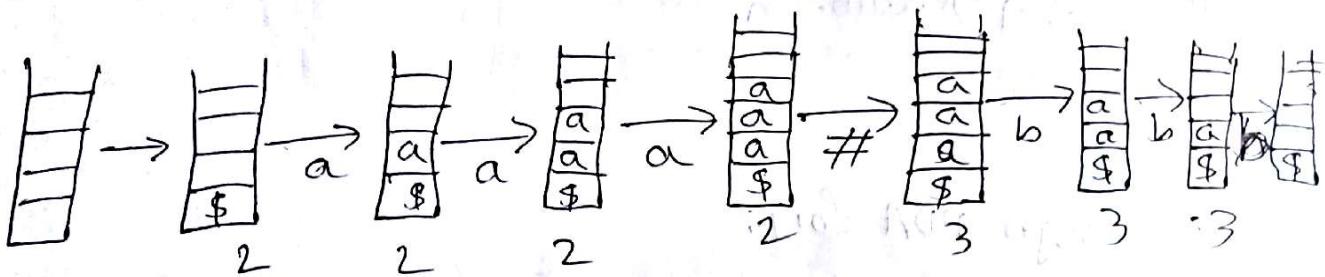
aaabb



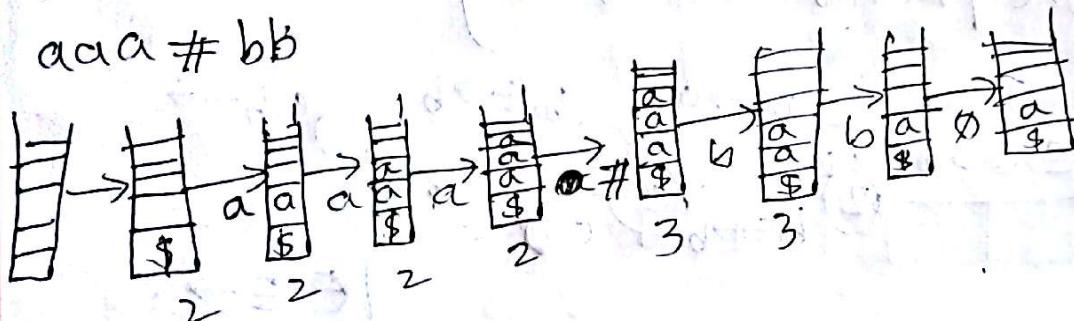
$a^n \# b^n$



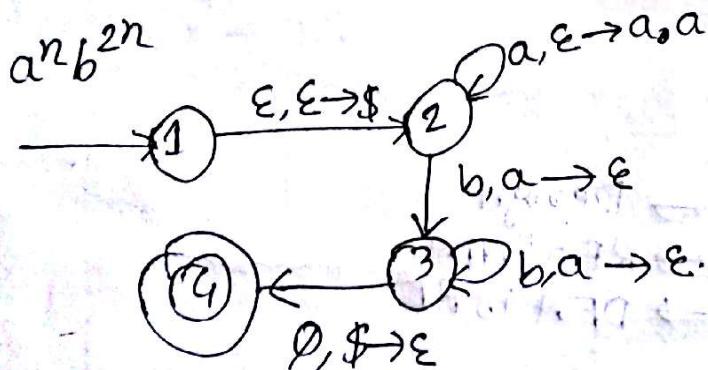
aaa # bbb



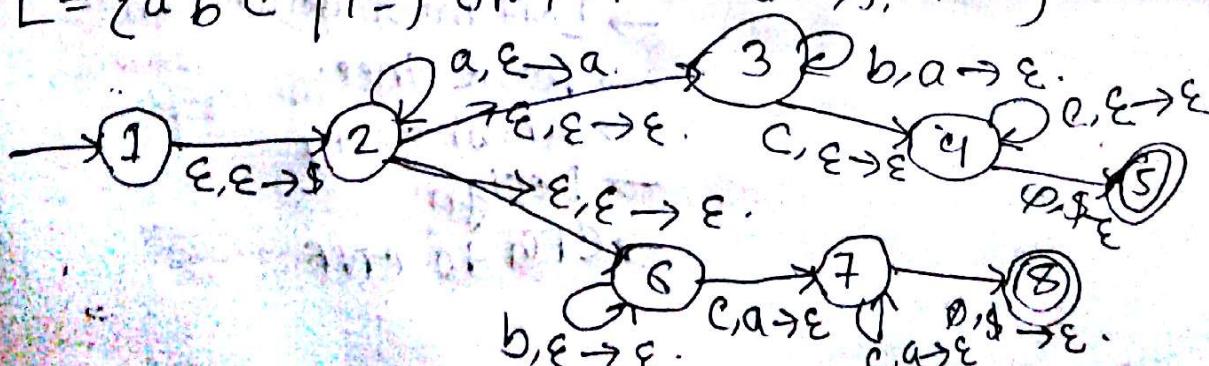
aaa # bb



$L = \{ \omega \omega^r / \omega \text{ any combination of } a, b \}$



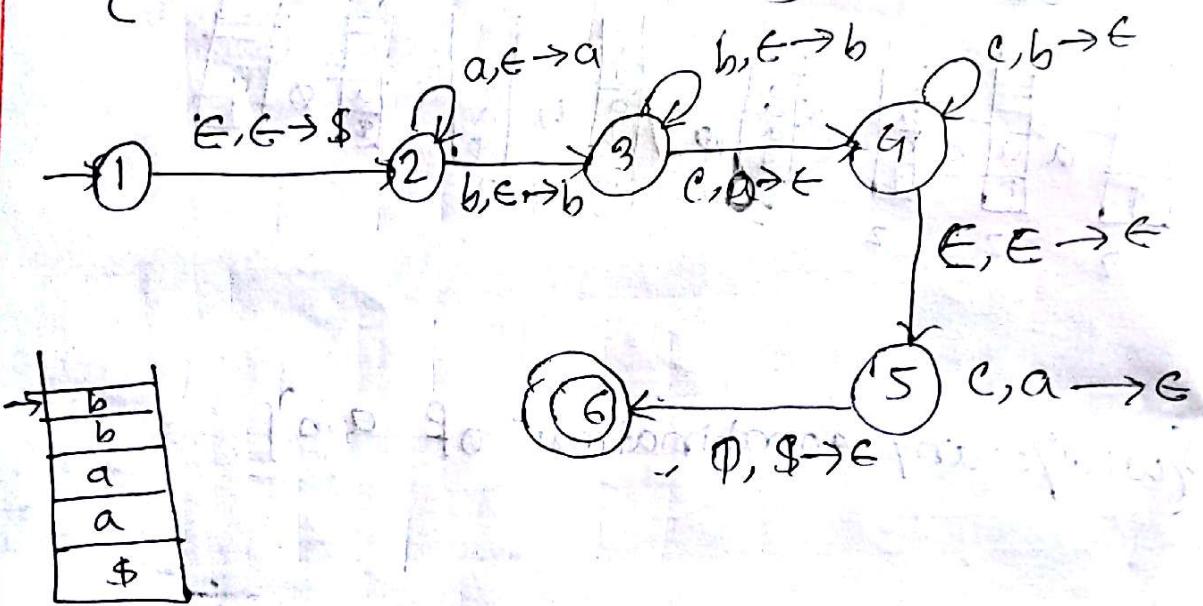
$L = \{ a^i b^j c^K \mid i=j \text{ or } i=k \text{ and } i, j, k > 0 \}$



PDN
Label Depenition
Design.

Design PDA for:

$$L = \{a^i b^j c^k \mid k = i + j \text{ and } i, j, k > 0\}$$



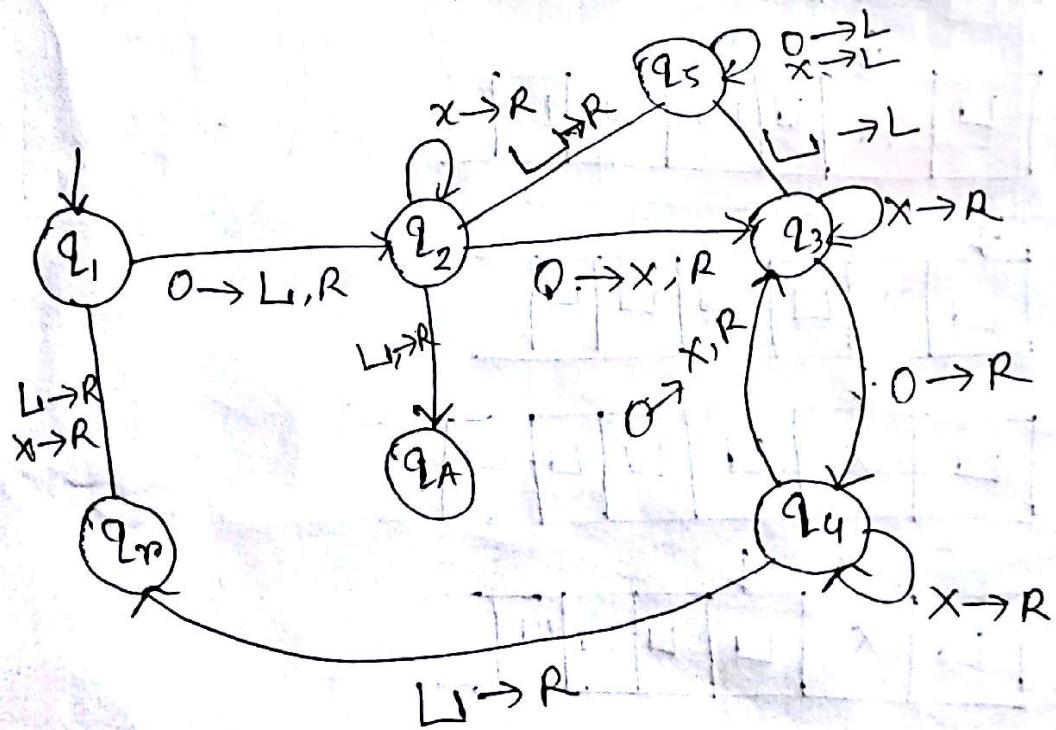
Syllabus
Regular Expression \rightarrow Design
 \rightarrow RE of NFA
 \rightarrow DFA to RE

Context free Grammar \rightarrow Formal def
 \rightarrow Left most derivation.
 \rightarrow Parse tree.
 \rightarrow Ambiguity
 \rightarrow Design.
 \rightarrow CFG to CNF

Push down Automata \rightarrow Design.
 \rightarrow Formal def.
 \rightarrow Simulation.
 \rightarrow Label desc.

Turning Machine \rightarrow Formal def.

\rightarrow Label desc
 \rightarrow Simulation.



$a \rightarrow b, \{L, R\} \rightarrow \Gamma$

↓
Replace value.

input to read | Γ alphabet.

1st	0	0	U	U	U	U
2nd	U	0	U	U	U	U
3rd	U	X	U	U	U	U
4th	U	X	U	U	U	U
5th	U	X	U	U	U	U
6th	U	X	U	U	U	U
7th	U	X	U	U	U	U
8th	U	X	U	U	U	U

	0 0 0
q_1	0 0 0
q_2	◻ 0 0
q_3	◻ × 0
q_4	◻ × 0 ◻
q_5	◻ × 0 ◻ ◻

	0 0 0 0 0
q_1	0 0 0 0 0
q_2	◻ 0 0 0 0
q_3	◻ × 0 0 0
q_4	◻ × 0 0 0
q_5	1 1 × 0 0 1
q_6	◻ × × ◻
q_7	◻ × × ◻
q_8	◻ ×

	0	0	0	0	0	0	0
q ₁	0	0	0	0	0	0	0
q ₂	◻	0	0	0	0	0	0
q ₃	◻	x	0	0	0	0	0
q ₄	◻	x	0	0	0	0	0
q ₅	◻	x	0	x	0	0	0
q ₆	◻	x	0	x	0	0	0
q ₇	◻	x	0	x	0	0	0
q ₈	◻	x	0	x	0	0	0
q ₉	◻	x	0	x	0	0	0
q ₁₀	◻	x	0	x	0	0	0
q ₁₁	◻	x	0	x	0	0	0
q ₁₂	◻	x	0	x	0	0	0
q ₁₃	◻	x	0	x	0	0	0
q ₁₄	◻	x	0	x	0	0	0
q ₁₅	◻	x	x	x	x	x	x

q_5	$\square \times \times \times \square$
q_5	$\square \times \cancel{\times} \times \square$
q_5	$\square \uparrow \times \times \times \square$
q_2	$\square \times \times \times \square$
q_2	$\square \times \times \times \square$
q_2	$\square \times \times \times \square$
q_2	$\square \times \times \times \square$
q_A	$\square \times \times \times \square \sqcap$