$$h := 6.636 \cdot 10^{-34} \cdot m^2 \cdot \frac{kg}{s} \qquad m_n := 1.6749 \cdot 10^{-27} \cdot kg \qquad \qquad k_b := 1.38064852 \cdot 10^{-23} \cdot \frac{J}{K}$$

$$eV := 1.60218 \cdot 10^{-19} \cdot J$$

$$\omega := 500 \cdot 2 \cdot \pi \cdot \sec^{-1}$$

Merlin Gd chopper:
$$R_{ch} := 5 \cdot mm$$
 $H_{ch} := 0.2 \cdot mm$ $\rho := 10^6 \cdot m$

$$= 5 \cdot \text{mm}$$
 $H_{ch} := 0.2 \cdot \text{mm}$

$$\rho := 10^6 \cdot \text{m}$$

$$\gamma := \frac{\omega \cdot R_{\text{ch}}^2}{H_{\text{ch}}} = 392.699 \frac{\text{m}}{\text{s}}$$
 $\omega = 3.142 \times 10^3 \frac{1}{\text{s}}$

$$\omega = 3.142 \times 10^3 \frac{1}{s}$$

MERLIN distances (counted from moderator)

$$L_2 := 2.5 \cdot m$$

$$L_{chop} := 10m$$
 $L_{samp} := 11.8 \cdot m$

$$L_{\text{camp}} := 11.8 \cdot \text{m}$$

$$L_{det} := L_2 + L_{samp}$$

Assuming L_chop=L_Ei_mon1

$$\varepsilon_{\text{beg}} := 150$$

$$\varepsilon_{\text{end}} := 11$$

Chopper opening time:

$$v(\varepsilon) := \sqrt{\frac{2 \cdot 1.60218 \cdot 10^{-22} \cdot J}{m_n} \cdot \varepsilon}$$

$$\Delta t := \frac{R_{ch}}{\gamma} \qquad \Delta t = 1.273 \times 10^{-5} \, \mathrm{s}$$

$$v(\varepsilon_{end}) = 1.451 \times 10^3 \frac{m}{s}$$

$$v(\varepsilon_{\text{beg}}) = 5.357 \times 10^3 \frac{\text{m}}{\text{s}}$$

TOF for energy
$$\epsilon$$
 at the positon L in chopper opening time units:

$$\tau_{e}(\varepsilon, L) := \frac{L \cdot \omega \cdot R_{ch}}{v(\varepsilon) \cdot H_{ch}}$$

$$\tau_{e}(151.9276, L_{chop}) = 145.678$$

$$\begin{split} &V_{char} \coloneqq \frac{L_{det} - L_{samp}}{\Delta t} \qquad \quad V_{char} = 1.963 \times 10^5 \, \frac{m}{s} \\ &V_{sc} \coloneqq \frac{v \left(\varepsilon_{beg}\right)}{V_{char}} \cdot 1000 \end{split}$$

$$\mathbf{a}_1 \coloneqq 10 \quad \sigma_1 \coloneqq 0.01 \cdot \mathbf{V}_{sc} \quad \mathbf{v}_1 \coloneqq 0$$

$$a_2 := 15$$
 $\sigma_2 := 0.05 \cdot V_{sc}$ $v_2 := 0.2 \cdot V_{sc}$

$$a_3 := 10$$
 $\sigma_3 := 0.1 \cdot V_{sc} \ v_3 := 0.5 \cdot V_{sc}$

$$N_p := 1000$$

$$\sigma_{V} := 0.1 \cdot V_{SC}$$

$$v0 := V_{sc}$$

$$\mathsf{L}_{\mathsf{v}} \coloneqq 3\!\cdot\!\mathsf{V}_{\mathsf{sc}}$$

$$\mathrm{fs}(\Delta v) \coloneqq \frac{a_1}{\sqrt{2\pi} \cdot \sigma_1} \cdot e^{-0.5 \cdot \left(\frac{\Delta v}{\sigma_1}\right)^2} + \underbrace{\frac{\left[\frac{-\left(\Delta v - v_2\right)^2}{2 \cdot \sigma_2^2} - \frac{-\left(\Delta v + v_2\right)^2}{2 \cdot \sigma_2^2}\right]}{\sqrt{2 \cdot \pi} \cdot \sigma_2} \cdot a_2 + \frac{a_3}{\sqrt{2 \cdot \pi} \cdot \sigma_3} \cdot e^{-\left(\Delta v - v_3\right)^2}$$

$$\begin{array}{c} R_{V}(v,v0) := & vp \leftarrow v - v0 \\ \text{return 0 if } vp < 0 \\ \text{otherwise} \\ & vp2 \leftarrow vp \cdot vp \\ & \frac{3}{2} \\ \text{return } \sigma_{V}^{2} \cdot vp2 \cdot \sqrt{2 \cdot \pi} \, e \\ \end{array}$$

$$fm(v) := \int_{-\frac{L_v}{2} + v0}^{v0} R_v(v - \delta v, v0) \cdot fs(\delta v) d\delta v + \int_{v0}^{\frac{L_v}{2} + v0} R_v(v - \delta v, v0) \cdot fs(\delta v) d\delta v$$

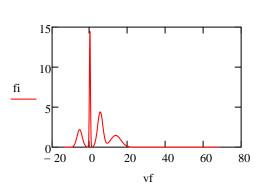
$$\Delta_{\mathbf{v}} := \frac{\mathbf{L}_{\mathbf{v}}}{\mathbf{N}_{\mathbf{p}} - 1} \qquad i := 0$$

$$vf_i := \frac{-L_V}{2} + v0 + i \cdot \Delta_V$$

$$\Delta_{\mathbf{V}} \coloneqq \frac{\mathbf{L}_{\mathbf{V}}}{\mathbf{N}_{\mathbf{p}} - 1} \qquad \qquad \mathbf{i} \coloneqq \mathbf{0} \ldots \mathbf{N}_{\mathbf{p}} - 1 \qquad \qquad \mathbf{vf}_{\mathbf{i}} \coloneqq \frac{-\mathbf{L}_{\mathbf{V}}}{2} + \mathbf{v}\mathbf{0} + \mathbf{i} \cdot \Delta_{\mathbf{V}} \qquad \mathbf{fi}_{\mathbf{i}} \coloneqq \mathbf{fs} \Big(\mathbf{vf}_{\mathbf{i}} \Big) \qquad \qquad \mathbf{Rf}_{\mathbf{i}} \coloneqq \mathbf{R}_{\mathbf{V}} \Big(\mathbf{vf}_{\mathbf{i}}, \mathbf{v}\mathbf{0} \Big)$$

$$fsi_i := fm(vf_i)$$

$$v0 = 27.283$$



▼

$$M(v) := \begin{bmatrix} 0 & \text{if } v < \frac{-L_v}{2} + v0 \lor v > \frac{L_v}{2} + v0 \\ \text{linterp}(vf, fsi, v) & \text{otherwise} \end{bmatrix}$$

high frequency filter for spectra:

$$\varepsilon_{\text{Res}} := 1 \cdot 10^{-6}$$

$$\begin{split} & \text{filts}(I,R,\text{Nf ,Shift}) := & & \text{np} \leftarrow \text{length}(I) \\ & \text{cent} \leftarrow \frac{np}{2} \\ & \text{cutR} \leftarrow \epsilon_{\text{Res}} \cdot \left| R_0 \right| \\ & \text{for } k \in 0 ... \, \text{np} - 1 \\ & & \text{rez}_k \leftarrow 0 \text{ if } \left| k - \text{cent} \right| < \text{Nf} \\ & \text{otherwise} \\ & & \Delta s \leftarrow e^{2\pi \cdot i \cdot k \cdot \text{Shift}} \text{ if } k < \text{cent} \\ & \Delta s \leftarrow e^{2\pi \cdot i \cdot k \cdot \text{Shift}} \text{ otherwise} \\ & & \text{rez}_k \leftarrow 0 \text{ if } \left| R_k \right| < \text{cutR} \\ & & \text{rez}_k \leftarrow \frac{I_k \cdot \Delta s}{R_k + \epsilon_{\text{Res}}} \text{ otherwise} \end{split}$$

high frequency filter for spectra:

$$if(|n-50|<40,0,D_n)$$

$$\varepsilon_{\text{Res}} = 10^{-9}$$

$$\begin{split} \text{filt}(I,R,Nf) &:= & | np \leftarrow \text{length}(I) \\ \text{cent} \leftarrow \frac{np}{2} \\ \text{for } i \in 0 ... np - 1 \\ & | \text{rez}_i \leftarrow 0 \text{ if } |i - \text{cent}| < Nf \\ \text{otherwise} \\ & | \text{rez}_i \leftarrow 0 \text{ if } |R_i| < \epsilon_{Res} \\ & | \text{rez}_i \leftarrow \frac{I_i}{R_i + \epsilon_{Res}} \text{ otherwise} \end{split}$$

$$\begin{split} \tau_1 &\coloneqq 1 & \tau_2 \coloneqq 0.1 & \text{R1} \coloneqq 0.5 \\ R_t(\tau) &\coloneqq \begin{bmatrix} \text{return 0 if } \tau < 0 \\ & -\frac{\tau}{\tau_1} \\ \text{return } \tau^2 \cdot \frac{e}{\tau_1} \cdot \left[(1 - \text{R1}) + \frac{\text{R1}}{\tau_2 + \tau_1} \cdot e^{\frac{-\tau}{\tau_2}} \right] & \text{otherwise} \\ \end{split}$$

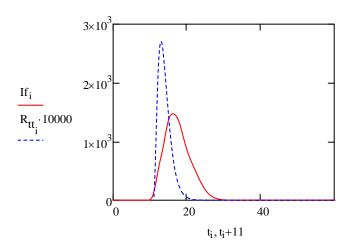
$$t_{min} := \frac{L_2}{R_{ch} \cdot max(vf)}$$
 $t_{min} = 7.331$ $L_p := \frac{L_2}{R_{ch}}$ $L_v = 81.849$

$$L2_{p} = 500$$

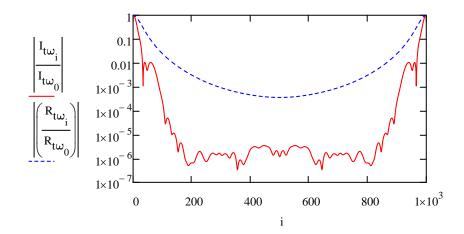
$$I(t) := \int_{0.1}^{\frac{L_v}{2}} R_t \left(t - \frac{L2_p}{v} \right) \cdot M(v) \, dv + \int_{\frac{L_v}{2}}^{3 \cdot L_v} R_t \left(t - \frac{L2_p}{v} \right) \cdot M(v) \, dv + \int_{3L_v}^{\infty} R_t \left(t - \frac{L2_p}{v} \right) \cdot M(v) \, dv$$

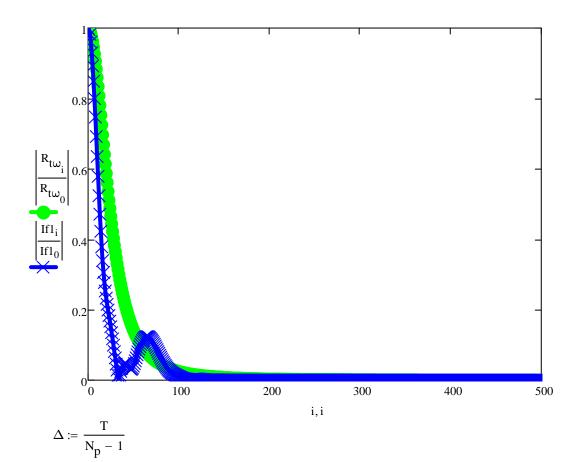
$$\delta t \coloneqq \frac{200 - t_{min}}{N_p}$$

$$\mathbf{t}_{i} \coloneqq 0.1 + \delta \mathbf{t} \cdot \mathbf{i} \qquad \qquad \mathbf{If}_{i} \coloneqq \mathbf{I} \begin{pmatrix} \mathbf{t}_{i} \end{pmatrix} \qquad \qquad \mathbf{R}_{\mathbf{t} t_{i}} \coloneqq \mathbf{R}_{\mathbf{t}} \begin{pmatrix} \mathbf{t}_{i} \end{pmatrix} \qquad \qquad \mathbf{T} \coloneqq \max(\mathbf{t}_{i})$$

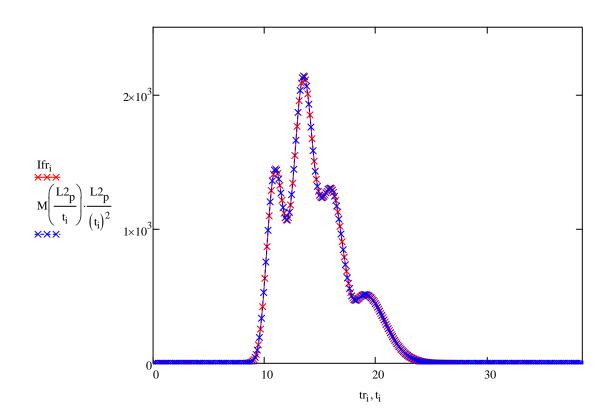


$$I_{t\omega} := cfft(If)$$
 $R_{t\omega} := cfft(R_{tt})$





$$Ifr := \frac{1}{\Delta \cdot \sqrt{N_p - 1}} \cdot icfft(If1) \qquad \qquad \underset{\text{Wy}}{\text{tr}} := \Delta \cdot i + 0.001$$



$$v2_{i} := \frac{L2_{p}}{t_{N_{p}-1-i}} \qquad M_{rr_{i}} := \frac{Ifr_{N_{p}-i-1} \cdot \left(t_{N_{p}-i-1}\right)^{2}}{L2_{p}}$$

$$v_{max} := max(v2) \qquad v_{min} := min(v2)$$

 $\max(tr) = 192.578$ $v_{max} = 5 \times 10^3$ $v_{min} = 2.596$

$$v_{\min} := 2^{\blacksquare}$$

$$v_{max} = 100$$

$$Npi := 1N_p$$

$$ii := 0 ... Npi - 1$$

$$ii := 0..Npi - 1$$
 $Npi = 1 \times 10^3$

$$\Delta v := \frac{v_{max} - v_{min}}{Npi - 1}$$

$$v_{r_{ii}} := v_{min} + ii \cdot \Delta v$$

$$length(v_r) = 1 \times 10^3$$

$$tr_{min} := min(tr)$$
 $tr_{max} := max(tr)$

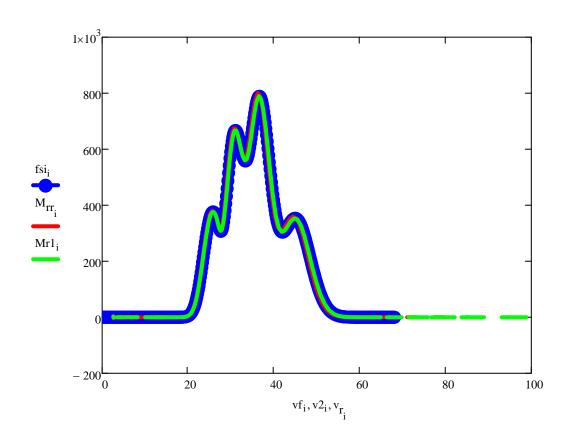
$$tr_{max} := max(tr)$$

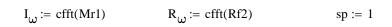
$$\begin{aligned} \text{Mif}(v) &:= & \left| ti \leftarrow \frac{L2_p}{v} \right| \\ \text{In} \leftarrow 0 & \text{if } ti < tr_{min} \lor ti > tr_{max} \\ \text{In} \leftarrow \text{linterp}(tr, Ifr, ti) & \text{otherwise} \\ \text{rez} \leftarrow \frac{\text{In} \cdot ti^2}{L2_p} \end{aligned}$$

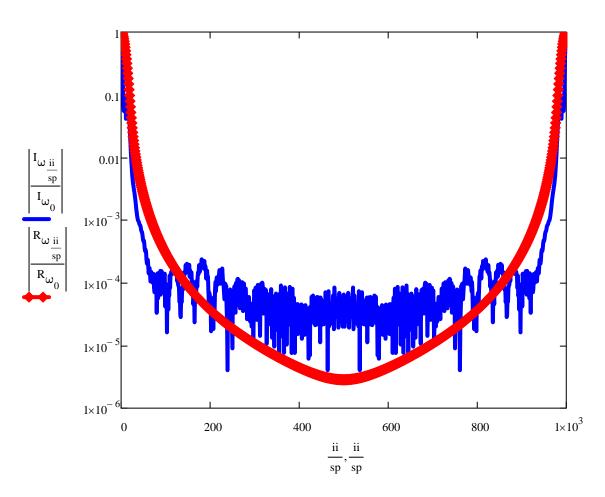
$$\operatorname{Mrl}_{ii} := \operatorname{Mif}\left(v_{r_{ii}}\right)$$

$$Rf2_{ii} := R_{v}(v_{r_{ii}}, v0)$$

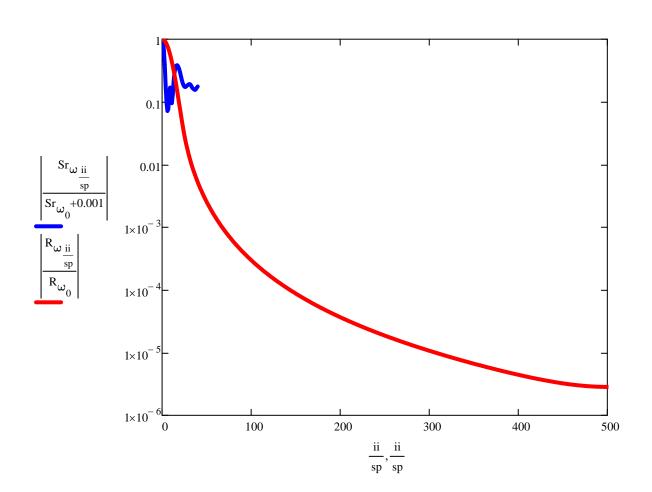
 $length(Mr1) = 1 \times 10^3$



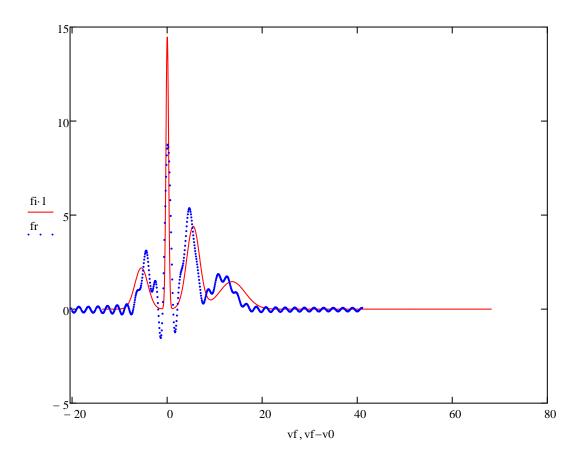


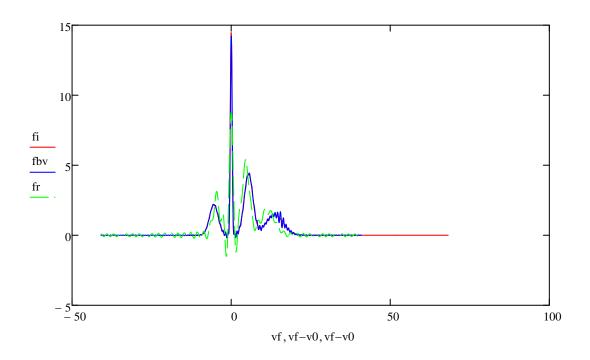


 $Sr_{\omega} := filts(I_{\omega}, R_{\omega}, 460, 0.5)$

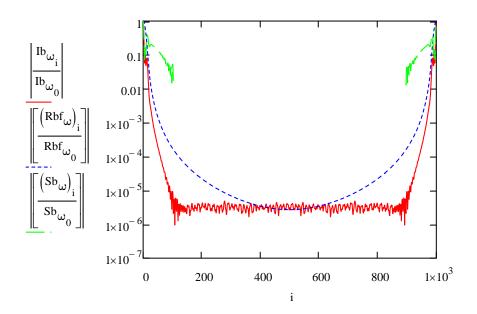


$$\mathrm{fr} := \frac{1}{\Delta_{_{\boldsymbol{V}}} \cdot \sqrt{\mathrm{Npi}}} \cdot \mathrm{icfft} \! \left(\mathrm{Sr}_{\boldsymbol{\omega}} \right)$$





$$\begin{split} \text{Ib}_{\omega} &\coloneqq \text{cfft(fsi)} & \text{Rbf}_{\omega} \coloneqq \text{cfft(Rf)} \\ & \frac{\text{v0}}{\Delta_{\text{v}} \cdot \text{N}_{\text{p}}} = 0.333 \\ & \text{Sb}_{\omega} \coloneqq \text{filts} \big(\text{Ib}_{\omega}, \text{Rbf}_{\omega}, 396, 0.5 \big) \end{split}$$



$$\mathit{fbv} := \frac{1}{\Delta_v \cdot \sqrt{N_p}} \cdot \mathit{icfft} \big(\mathit{Sb}_\omega \big)$$

