

# Calculus Basics

Definite vs Indefinite Integral:

A definite integral computes the net area under a curve between two limits, producing a numeric value.

An indefinite integral represents a family of functions (antiderivative) and includes +C.

Mean Value Theorem:

If  $f$  is continuous on  $[a, b]$  and differentiable on  $(a, b)$ , then there exists some  $c$  in  $(a, b)$  such that

$$f'(c) = (f(b) - f(a)) / (b - a).$$

Fundamental Theorem of Calculus:

Part 1 links differentiation and integration, showing that the derivative of the integral function equals the integrand.

Part 2 allows evaluation of definite integrals via antiderivatives.

# Additional Notes

Integration by Substitution:

Use u-substitution to simplify integrals where  $u = g(x)$  appears with its derivative.

Integration by Parts:

$\int u \, dv = uv - \int v \, du$ . Choose  $u$  and  $dv$  appropriately.