



# Advanced AI 课程

罗平

Autumn 2016

*Pattern Mining  
over Transaction Database*

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# FREQUENT PATTERN MINING

# 1992年， IBM， Rakesh Agrawal

- IBM客户交流会
  - 衔接大客户和IBM研究人员
- 超市：超市扫码机的普及
- 数据
  - 积累大量用户购买记录数据



# 1992年， IBM， Rakesh Agrawal

## ■ 用户购买数据

购买编号	购买记录
1	B C E
2	A B
3	A B C
4	A B D
5	A B C D E F G

# 1992年， IBM， Rakesh Agrawal

- 频繁模式： 经常被一起购买的商品

购买编号	购买记录
1	B C E
2	A B
3	A B C
4	A B D
5	A B C D E F G

# 1992年， IBM， Rakesh Agrawal

## ■ 啤酒和尿布的故事



# Problem Statement

- Frequent pattern mining
- ***Support***

Transaction No.	Items
1	B C E
2	A B
3	A B C
4	A B D
5	A B C D E F G

The support of {BC} = 3/5



# Problem Statement

- *Frequent patterns*

support is bigger than a parameter  $\alpha$

Transaction No.	Items
1	B C E
2	A B
3	A B C
4	A B D
5	A B C D E F G

The support of {BC} = 3/5  
{BC} is frequent when  $\alpha = 0.5$

# Frequent Pattern Mining

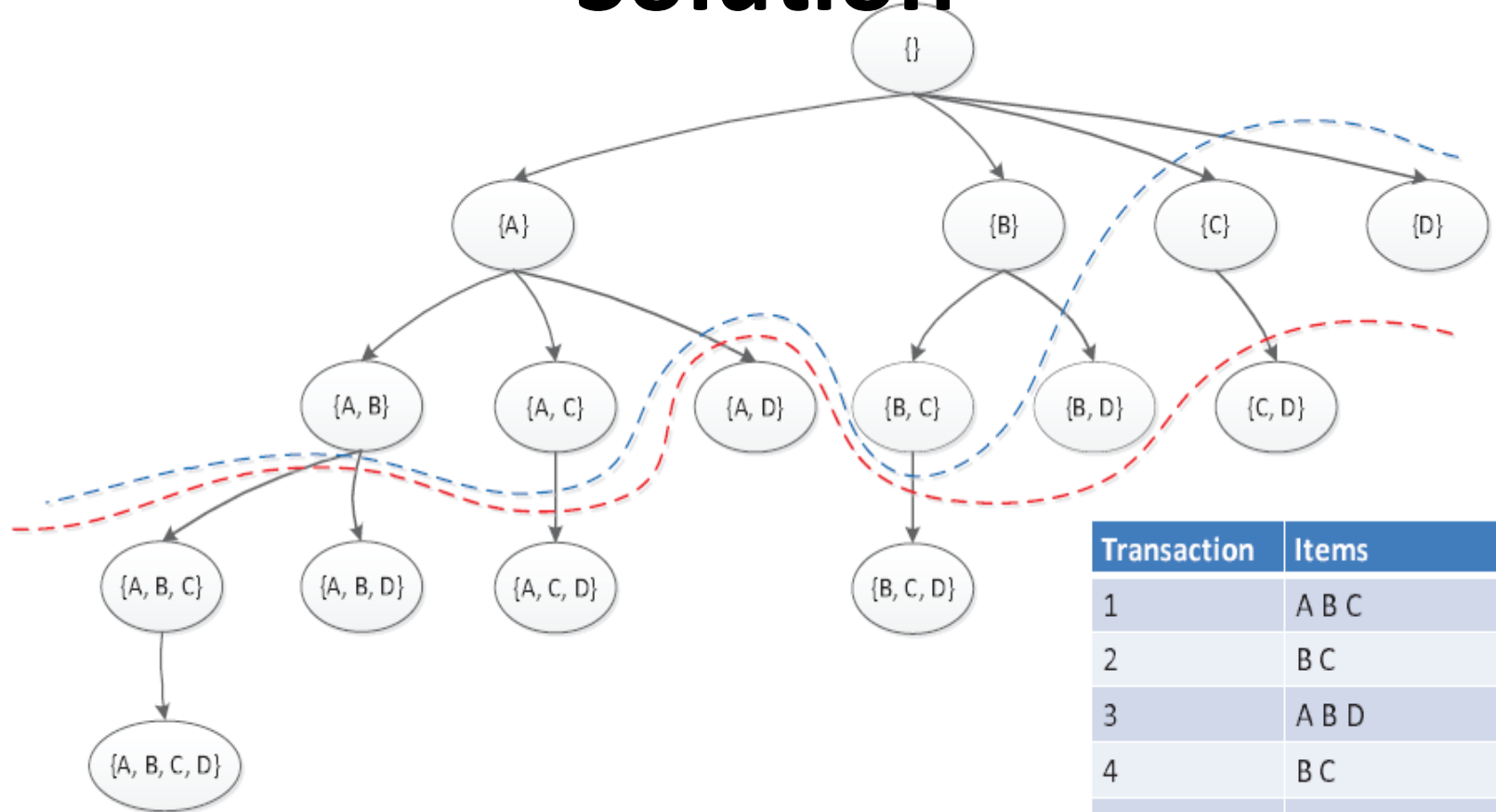
- *Given: a transaction database, and min\_sup  $\alpha$*
- *Output: all the frequent patterns*

R. Agrawal, T. Imielinski, A.N. Swami: [Mining Association Rules between Sets of Items in Large Databases](#), SIGMOD 1993. Won the [2003 SIGMOD Test of Time Award](#) for the most impactful paper over the intervening decade. [Citations](#).

# Frequent Pattern Mining

- *Naïve solution*
- *Check all the patterns (itemset) one by one*

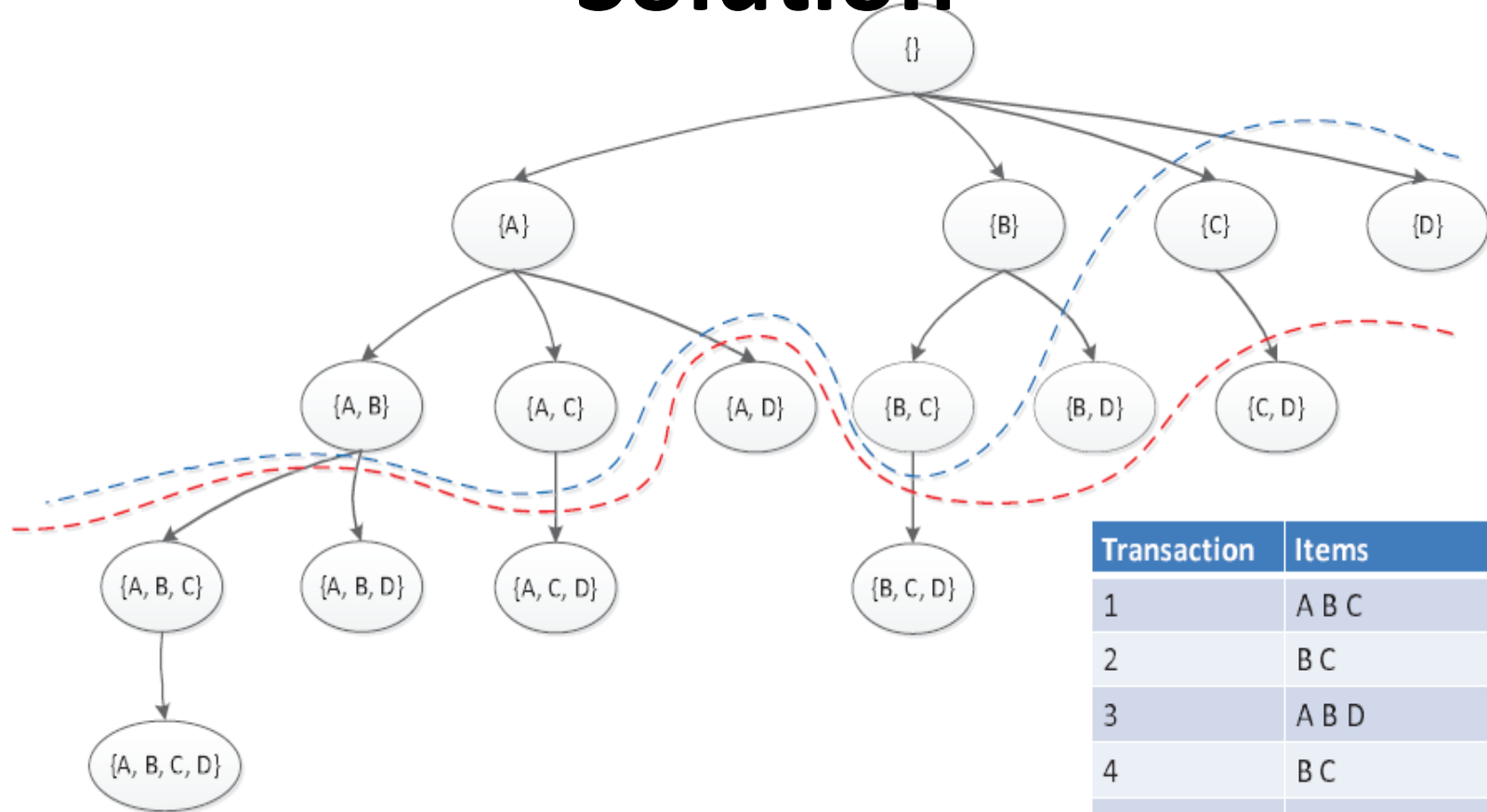
# Solution



Transaction	Items
1	A B C
2	B C
3	A B D
4	B C
5	A C
6	B C D

**lexicographic subset tree: list all the itemsets**  
(all the items are ranked in a fixed sequence)

# Solution



Transaction	Items
1	A B C
2	B C
3	A B D
4	B C
5	A C
6	B C D

**Property on lexicographic subset tree**

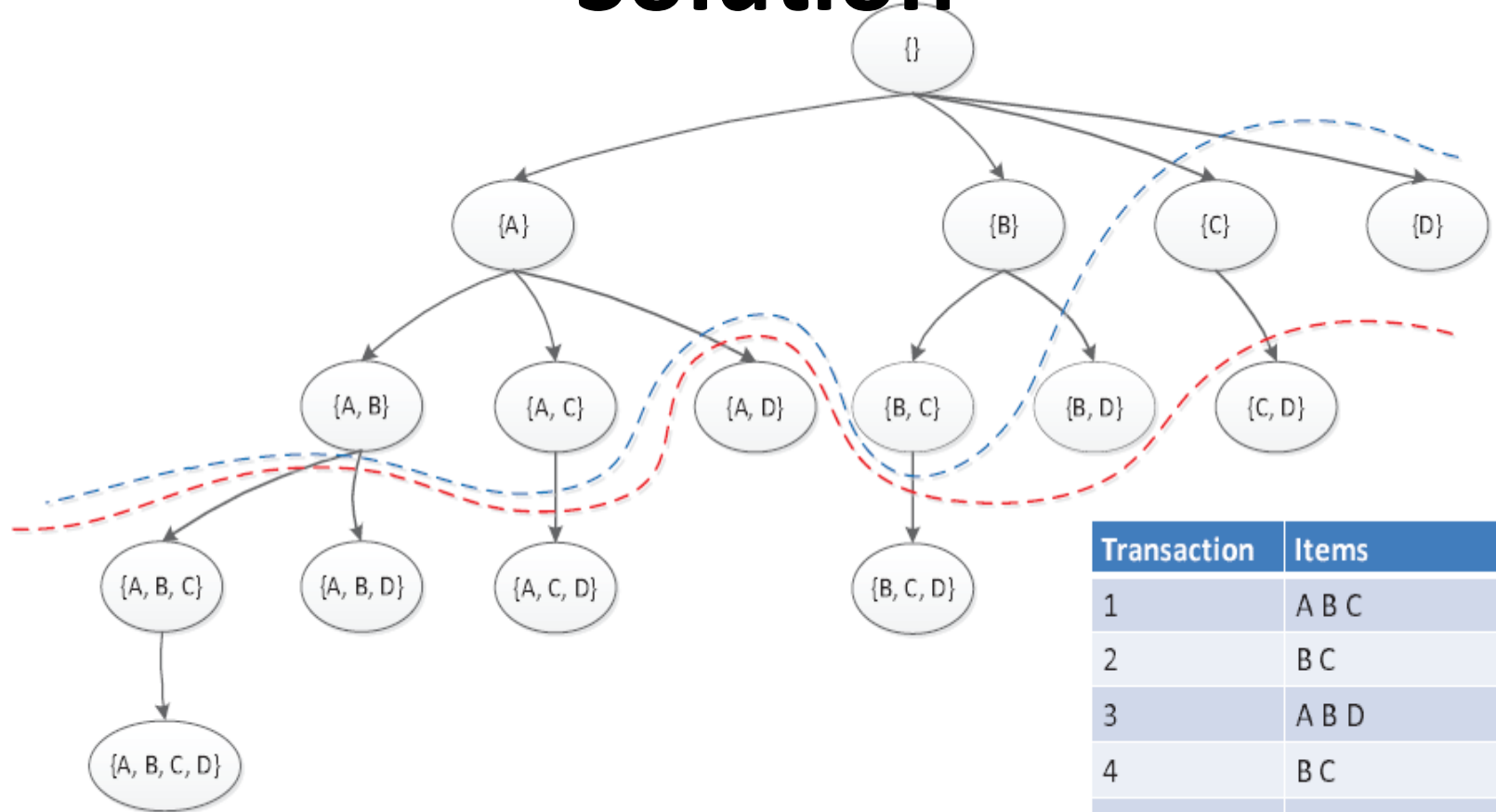
子树根节点对应的itemset是子树上的任意节点对应的itemset的子集

# Frequent Patterns

- ***Anti-Monotone*** 重要性质
- Frequent itemset的任何子集都是frequent的
- 等价的形式：对于一个itemset，只要它的任意一个子集不frequent，那么它就不frequent
- 推出：如果一个itemset不frequent，那么任何包含它的itemset都不frequent

Anti-monotone: 随着itemset的item增加，它的frequency不增加

# Solution

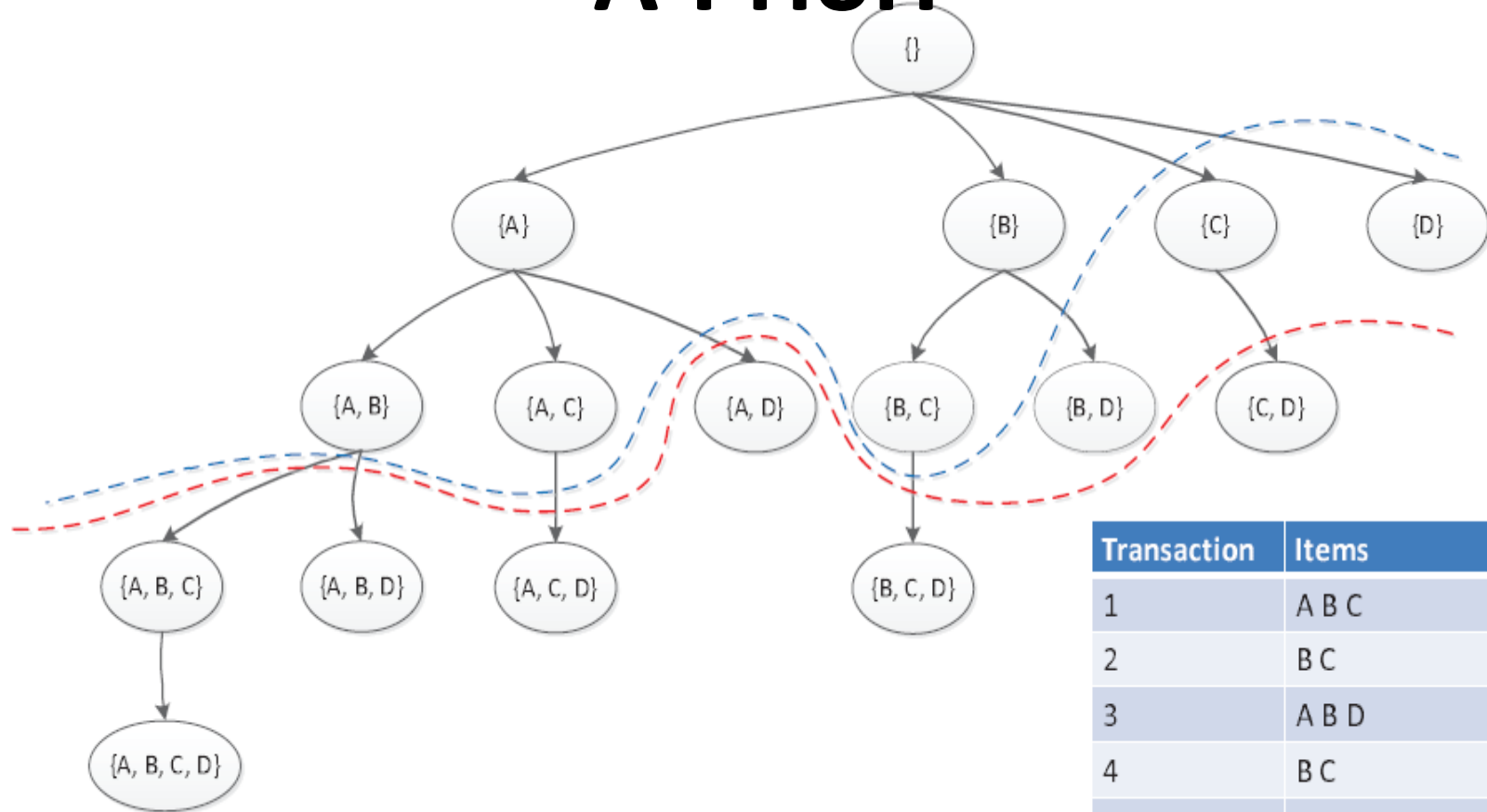


Transaction	Items
1	A B C
2	B C
3	A B D
4	B C
5	A C
6	B C D

**Pruning by anti-monotone**  
**The red line in the graph**

剪枝的本质：对每棵子树，估算出该棵子树上所有节点的frequency的最大值(upper bound)

# A-Priori



Transaction	Items
1	A B C
2	B C
3	A B D
4	B C
5	A C
6	B C D

**Breadth-first traverse on the lexicographic subset tree with pruning by anti-monotone**

**Trick: if BC is infrequent, we don't need to extend ABC**

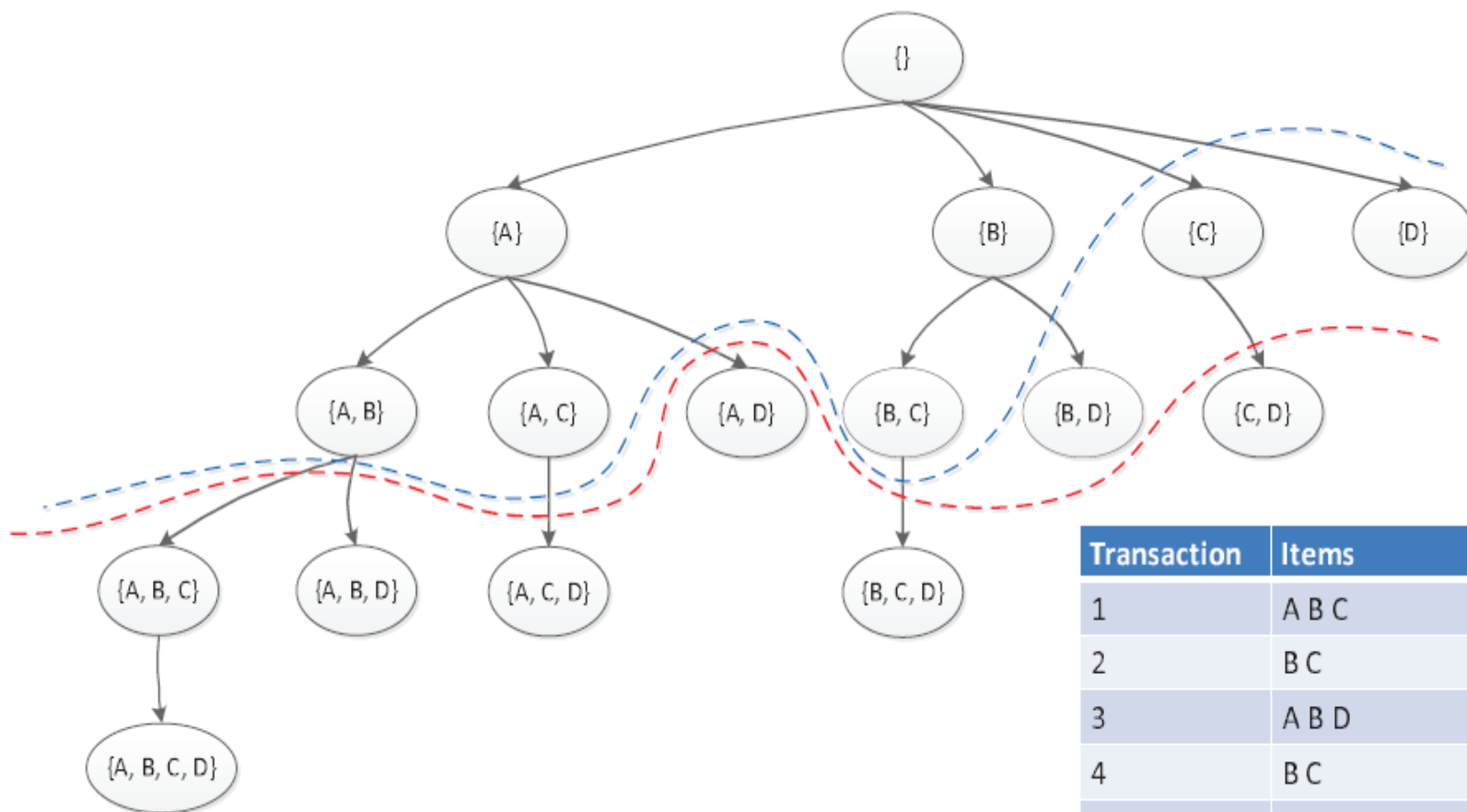


# Maximal Frequent Patterns

- 在某个frequent itemset上，添加任意的item后，都会变为infrequent
- 那么，它是一个maximal frequent itemset
- maximal frequent itemset是最大可能的长

# Maximal Frequent Patterns

- 那么，紧贴着红线的节点都是maximal frequent itemsets吗？



Transaction	Items
1	A B C
2	B C
3	A B D
4	B C
5	A C
6	B C D

# More Works on Frequent Pattern Mining

- More efficient algorithm for FPM:
  - J. Han, J. **Pei**, Y. Yin, and R. Mao. "[Mining Frequent Patterns without Candidate Generation: A Frequent-pattern Tree Approach](#)". *Data Mining and Knowledge Discovery: An International Journal*, Volume 8, Issue 1, pages 53-87, January 2004, Kluwer Academic Publishers.
- Mining maximal frequent patterns
  - J. Wang, J. Han, and J. Pei, "[CLOSET+: Searching for the Best Strategies for Mining Frequent Closed Itemsets](#)", in Proc. 2003 ACM SIGKDD Int. Conf. on Knowledge Discovery and Data Mining (KDD'03), Washington, D.C., Aug. 2003.
- More: parallel, incremental, top-K, ... ..