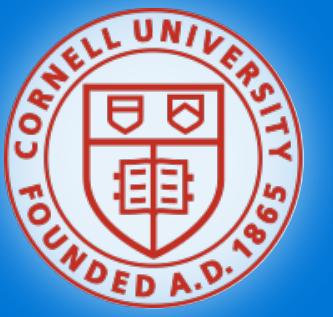


A Language-Based Approach to Network Verification and Synthesis

Nate Foster
Cornell University

Microsoft Research
Faculty Summit 2015

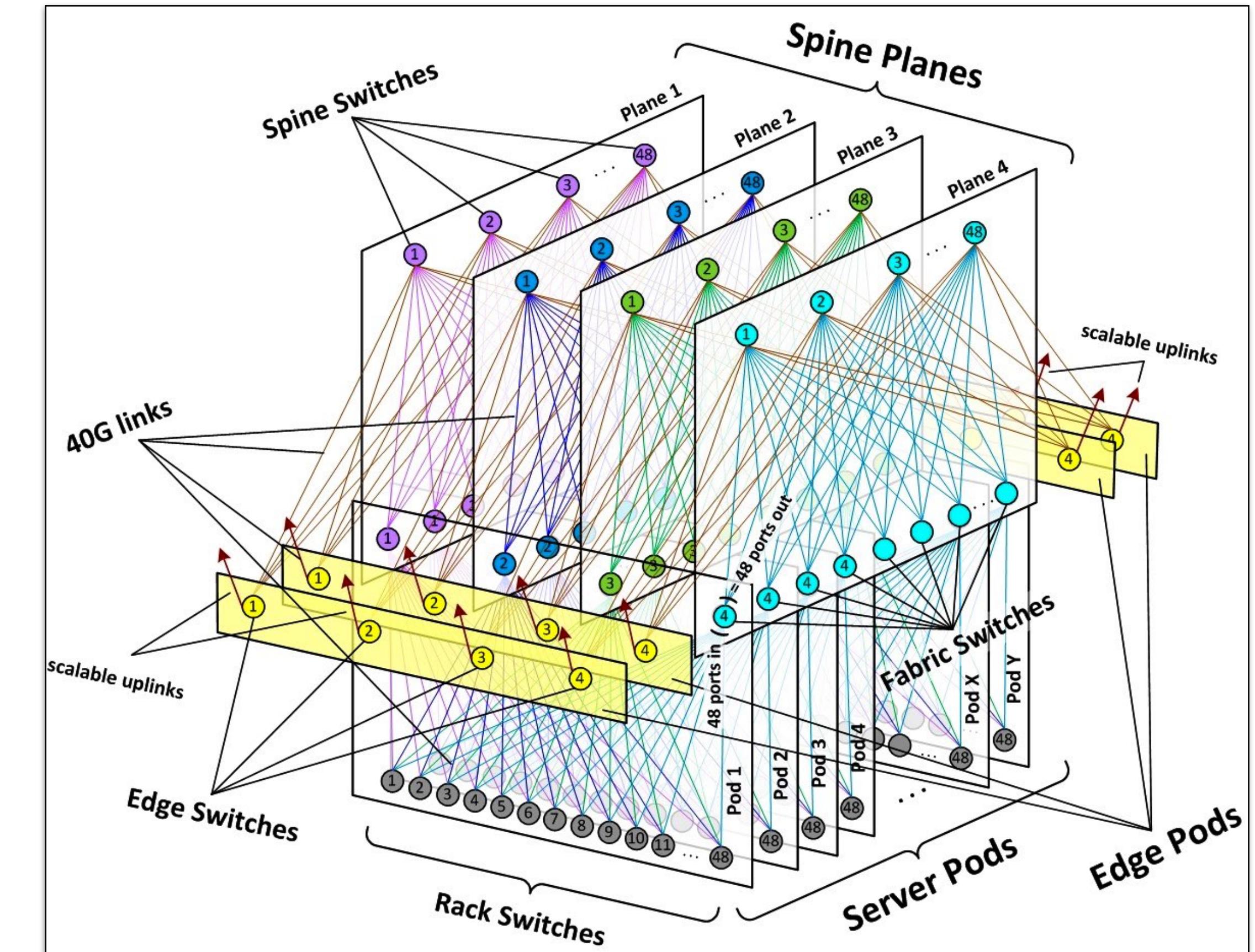


Challenges

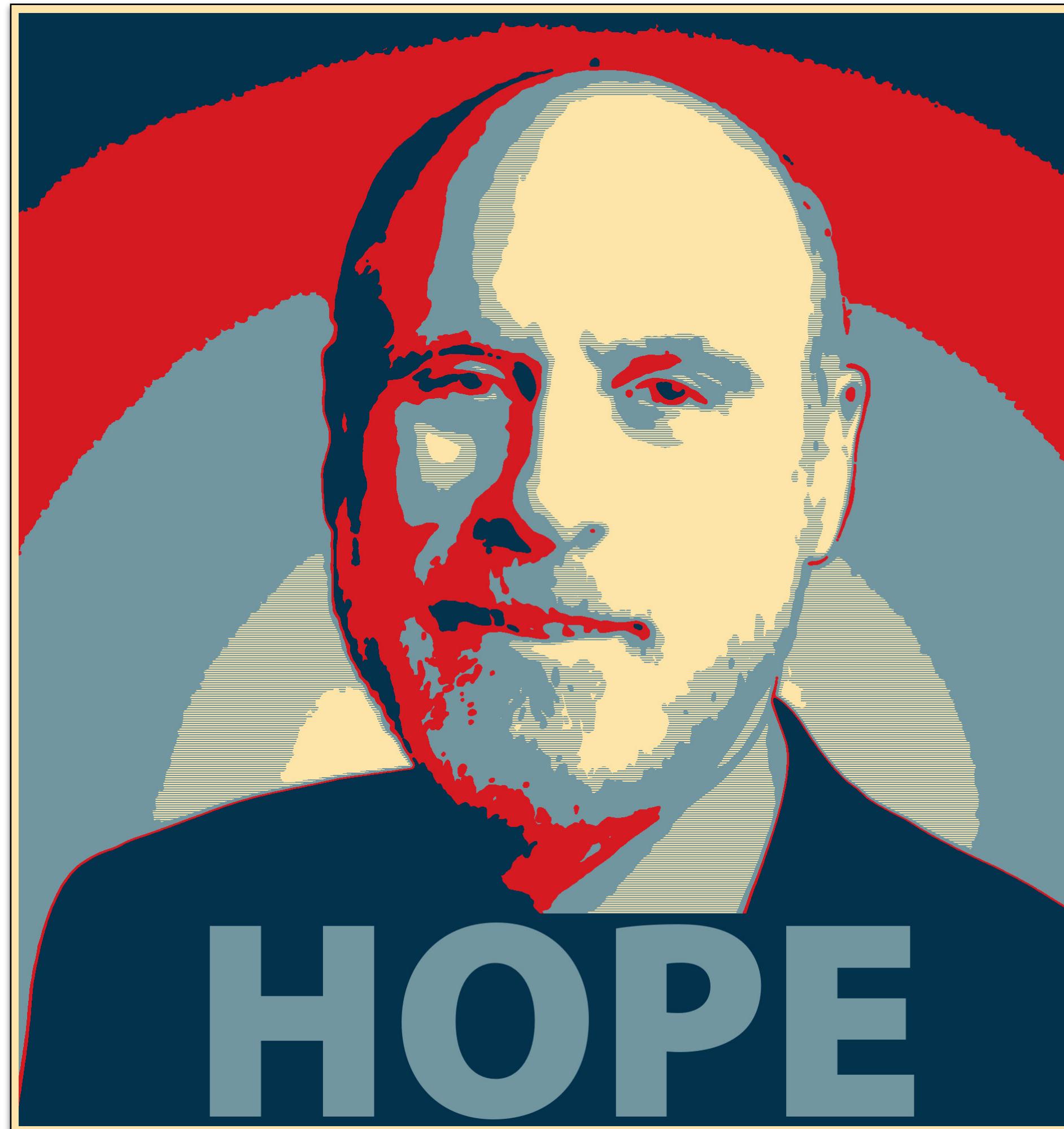
Networks are a critical part of our computing infrastructure...

...they have grown dramatically in size and complexity...

... and are quickly becoming unwieldy for operators to manage!



Network Management

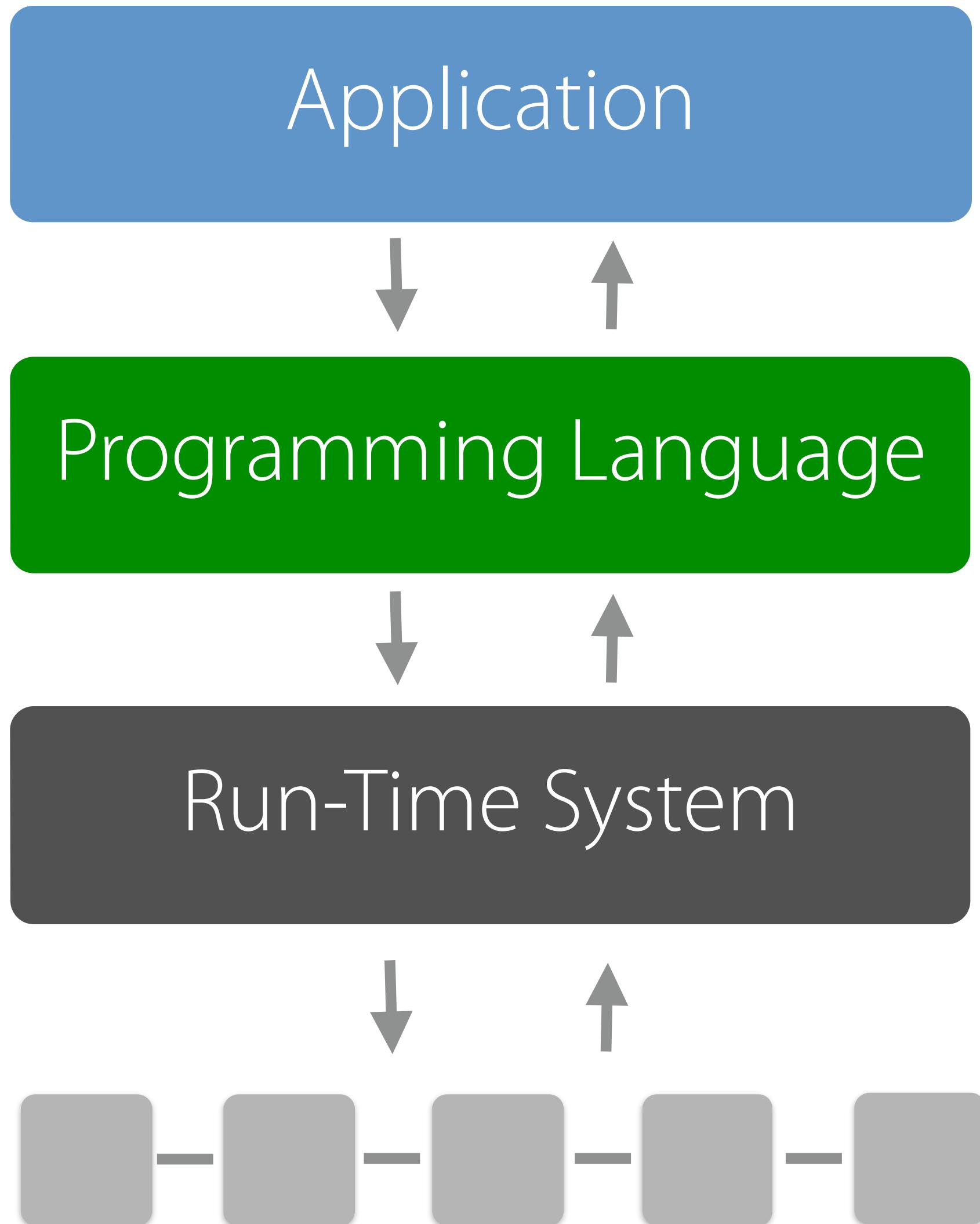


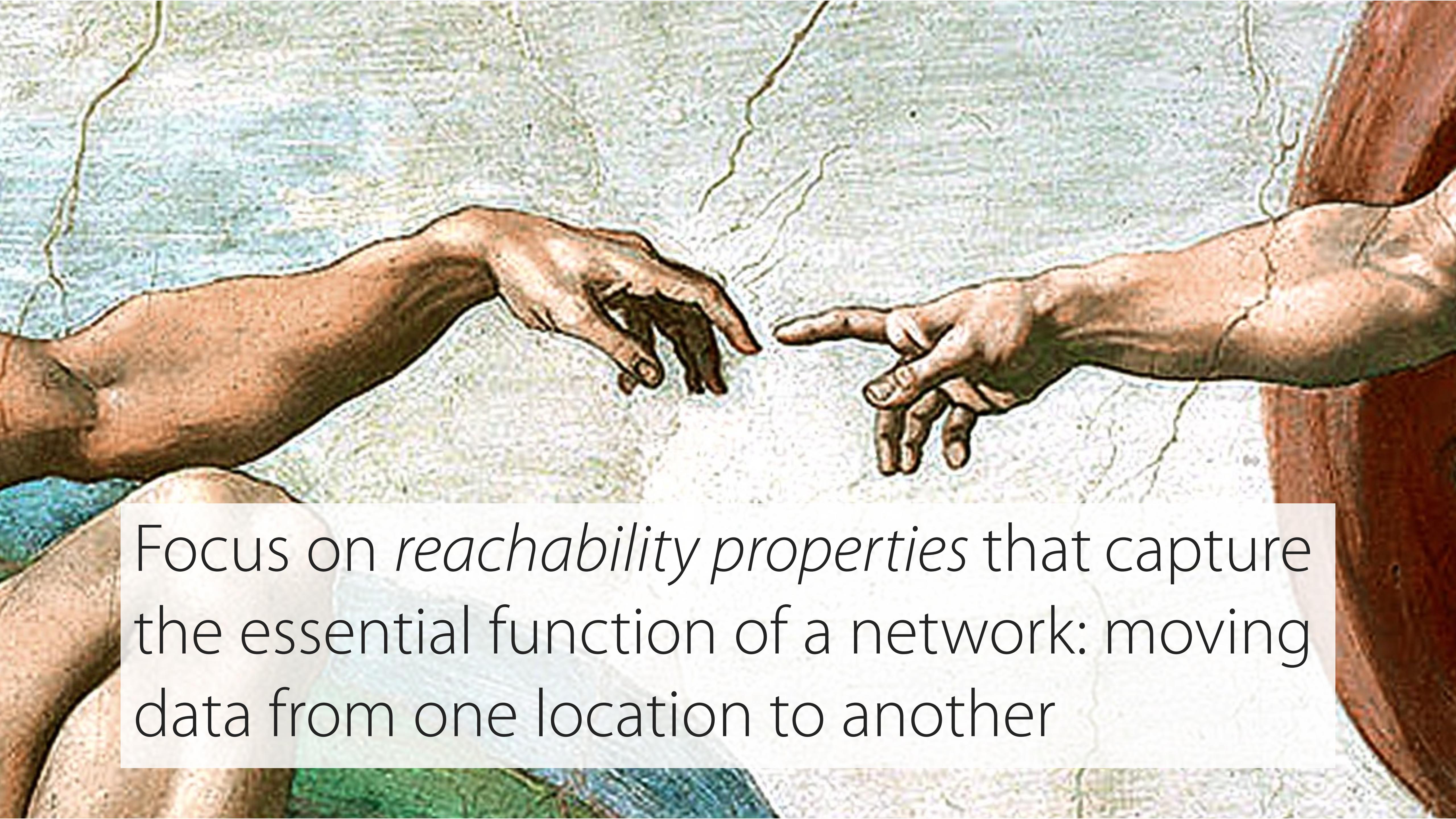
Operators use a variety of techniques to keep networks running such as:

- Generating low-level configurations from high-level policies
- Scraping configurations using command-line interfaces
- Diagnosing errors using **ping** and **traceroute**

Toward Design Automation

1. Design high-level languages that model essential network features
2. Develop semantics that enables reasoning precisely about behavior
3. Build tools to synthesize low-level implementations automatically





Focus on *reachability properties* that capture the essential function of a network: moving data from one location to another

Machines

A *machine model* describes behavior in terms of concepts like pipelines of hardware lookup tables



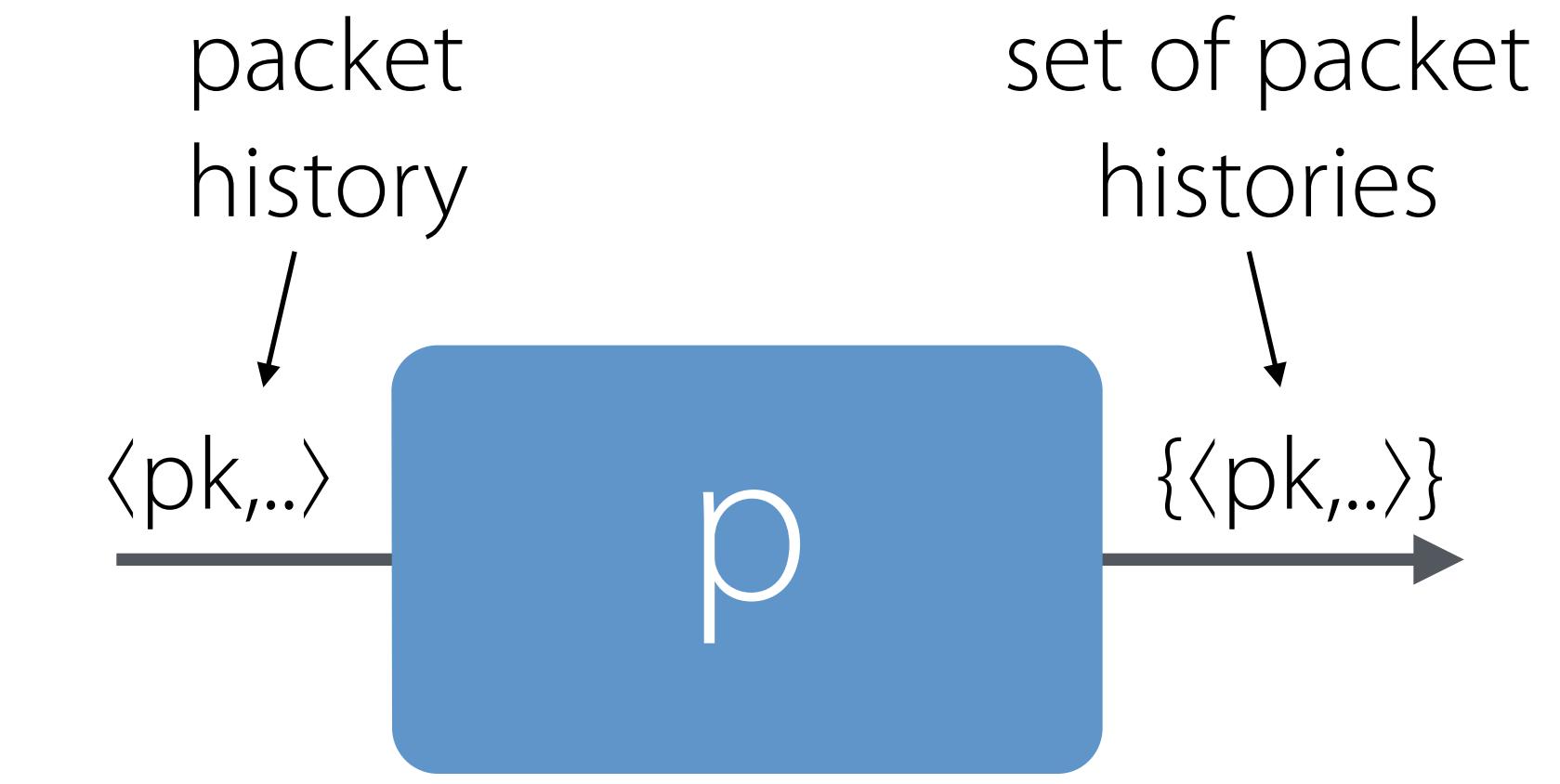
Languages

A programming model describes behavior in terms of concepts like mathematical functions on packets

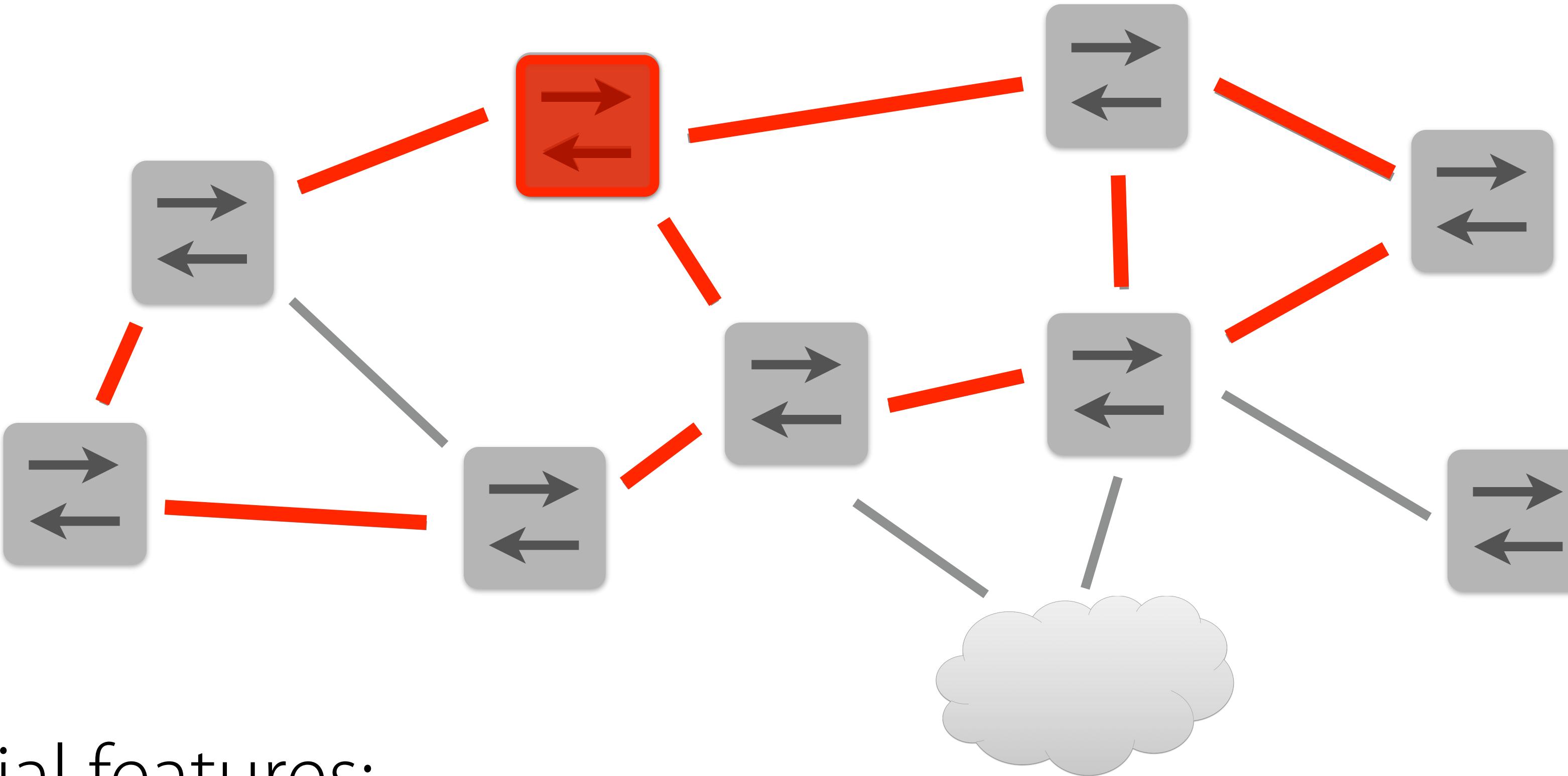
Machines

A machine model describes behavior in terms of concepts like pipelines of hardware lookup tables

Match	Actions
ethType=0x800, ipProto=0x06, tcpDstPort=22, ethSrc=00:00:00:00:00:01	Drop
ethType=0x800, ipProto=0x06, tcpDstPort=22, ethSrc=00:00:00:00:00:02	Drop
ethType=0x800, ipProto=0x06, tcpDstPort=22,	Inport
ethType=0x800, ipProto=0x06	Inport
ethType=0x800	Inport
*	Inport



What should a network programming language provide?



Two essential features:

- Packet classifiers
- Forwarding paths

NetKAT Language

[POPL '14]

```
pol ::= false
      | true
      | field = val
      | pol1 + pol2
      | pol1; pol2
      | !pol
      | pol*
      | field := val
      | S  $\Rightarrow$  T
```

NetKAT Language

[POPL '14]

```
pol ::= false
      | true
      | field = val
      | pol1 + pol2
      | pol1; pol2
      | !pol
      | pol*
      | field := val
      | S  $\Rightarrow$  T
```

Boolean
Algebra

NetKAT Language

[POPL '14]

pol ::= **false**

| **true**

| field = val

| pol₁ + pol₂

| pol₁; pol₂

| !pol

| pol*

| field := val

| S \Rightarrow T

Boolean
Algebra

+

Kleene
Algebra

NetKAT Language

[POPL '14]

pol ::= false	Boolean
true	Algebra
field = val	+
pol ₁ + pol ₂	Kleene
pol ₁ ; pol ₂	Algebra
!pol	+
pol*	Packet
field := val	Primitives
S \Rightarrow T	

NetKAT Language

[POPL '14]

```
pol ::= false
      | true
      | field = val
      | pol1 + pol2
      | pol1; pol2
      | !pol
      | pol*
      | field := val
      | S  $\Rightarrow$  T
```

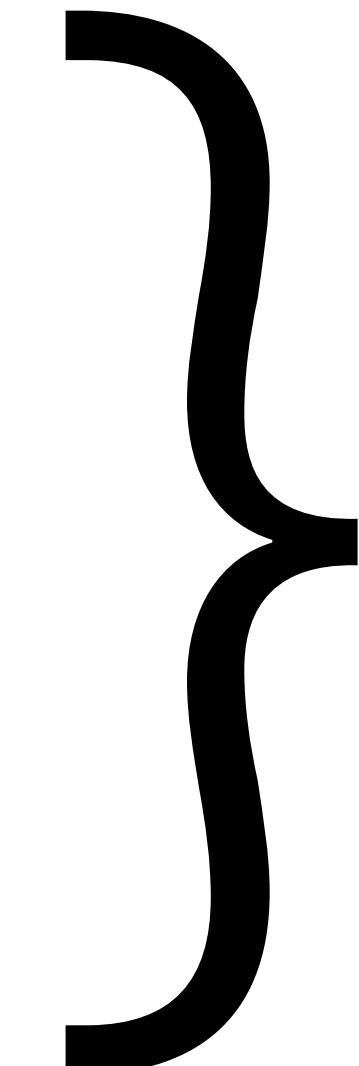
Boolean
Algebra

+

Kleene
Algebra

+

Packet
Primitives



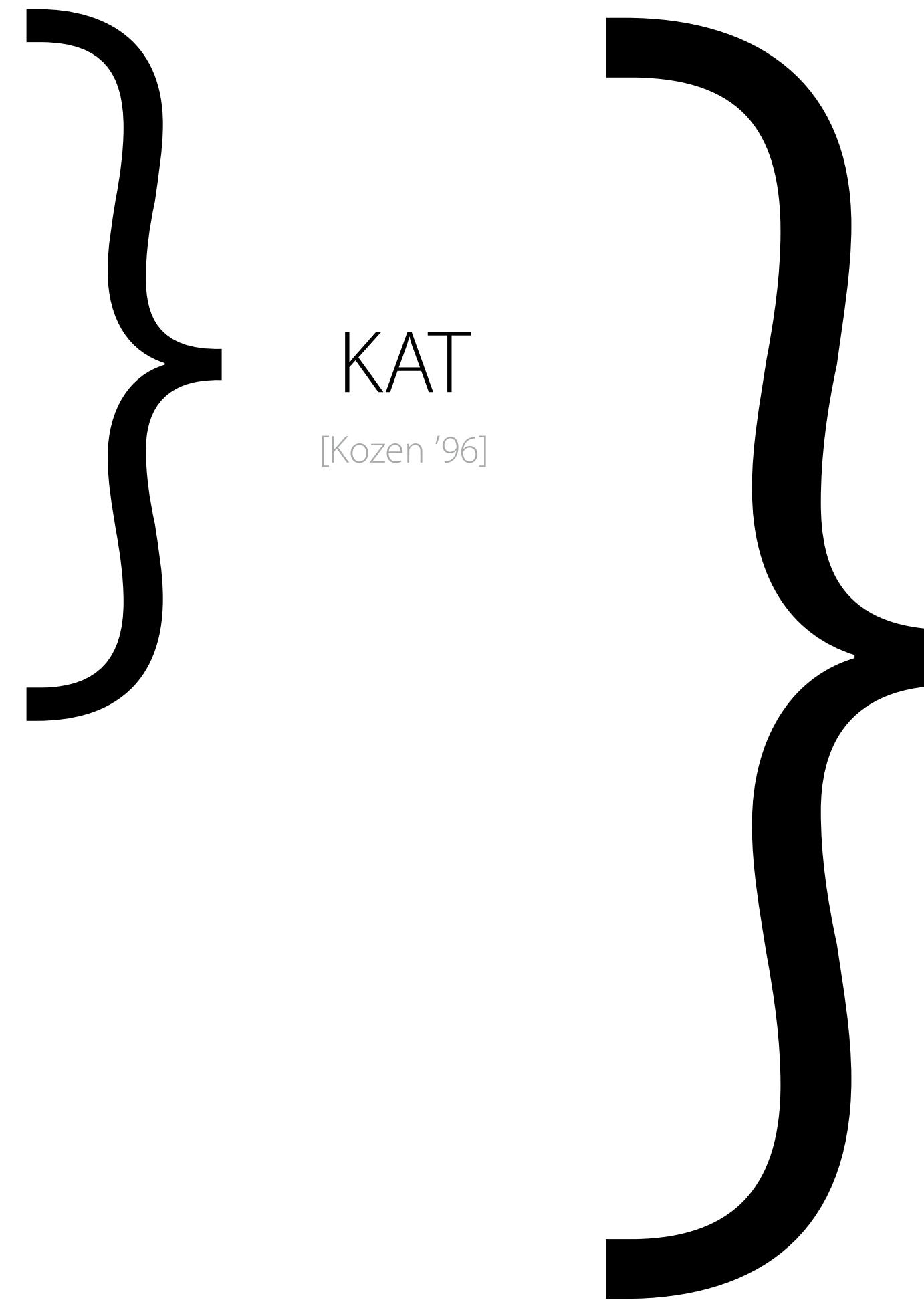
KAT
[Kozen '96]

NetKAT Language

[POPL '14]

```
pol ::= false
      | true
      | field = val
      | pol1 + pol2
      | pol1; pol2
      | !pol
      | pol*
      | field := val
      | S  $\Rightarrow$  T
```

Boolean
Algebra
+
Kleene
Algebra
+
Packet
Primitives



NetKAT
[Anderson et al.'14]

NetKAT Language

[POPL '14]

```
pol ::= false  
| true  
| field = val  
| pol + pol
```

Boolean
Algebra

+

KAT
[Kozen '96]

if p₁ **then** p₂ **else** p₃ \triangleq (p₁; p₂) + (!p₁; p₃)

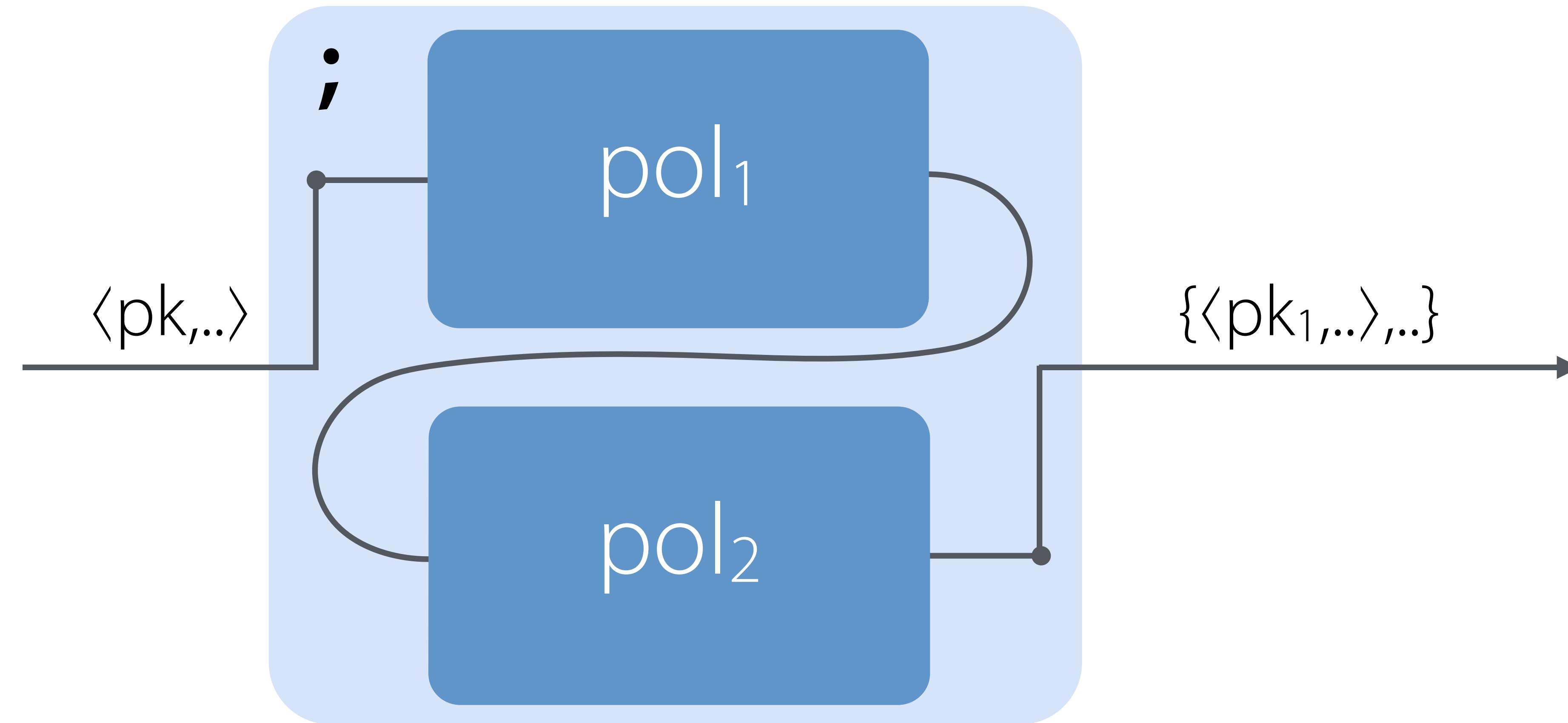
```
| p1  
| pol*  
| field := val  
| S  $\Rightarrow$  T
```

+

Packet
Primitives

```

pol ::= false
      | true
      | field = val
      | pol1 + pol2
| pol1; pol2
      | !pol
      | pol*
      | field := val
      | S⇒T
  
```



Sequential composition $\text{pol}_1 ; \text{pol}_2$ runs the input through pol_1 and then runs every output through pol_2

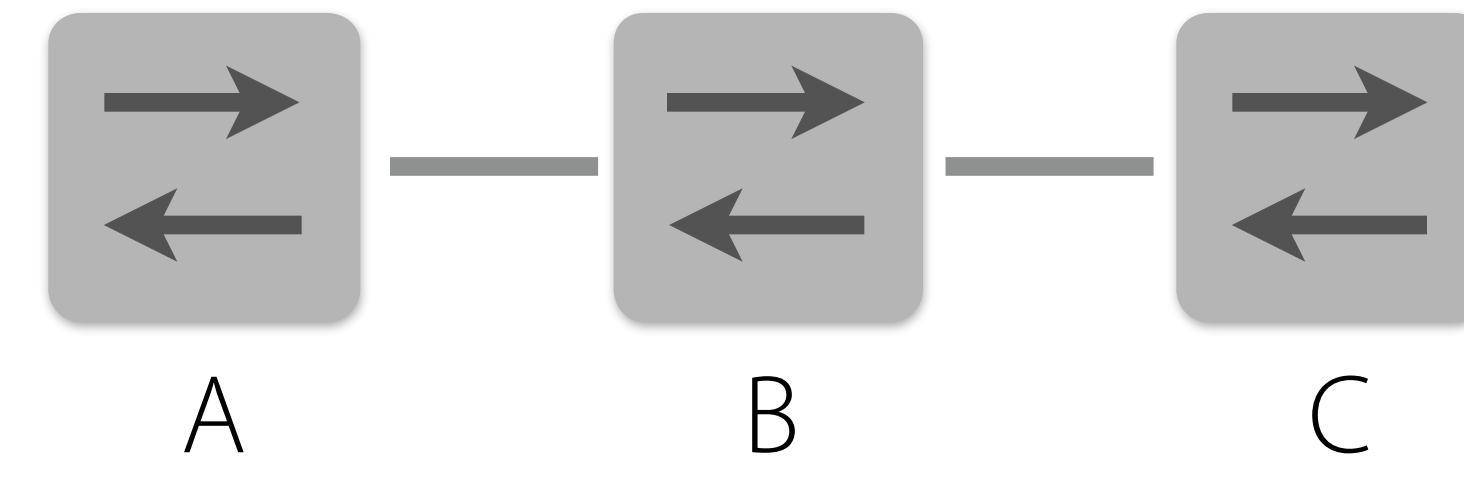
Encodings

Switch forwarding tables and network topologies can be represented in NetKAT using simple encodings

Pattern	Actions
dstport=22	Drop
srcip=10.0.0.1	Forward 1
*	Forward 2

```
if dstport=22 then false  
else if srcip=10.0.0.1 then port := 1  
else port := 2
```

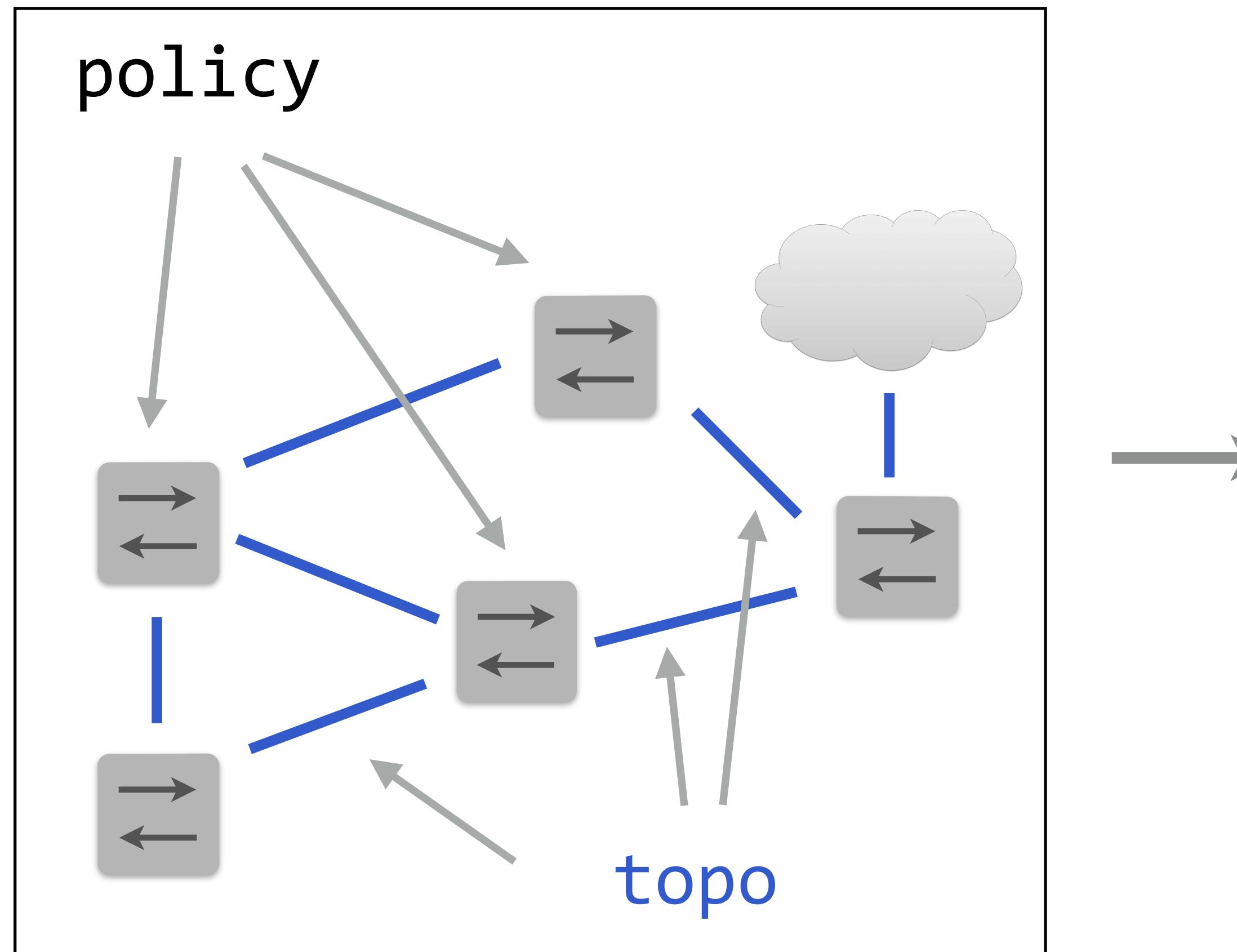
⋮



```
A ⇒ B + B ⇒ A + B ⇒ C + C ⇒ B
```

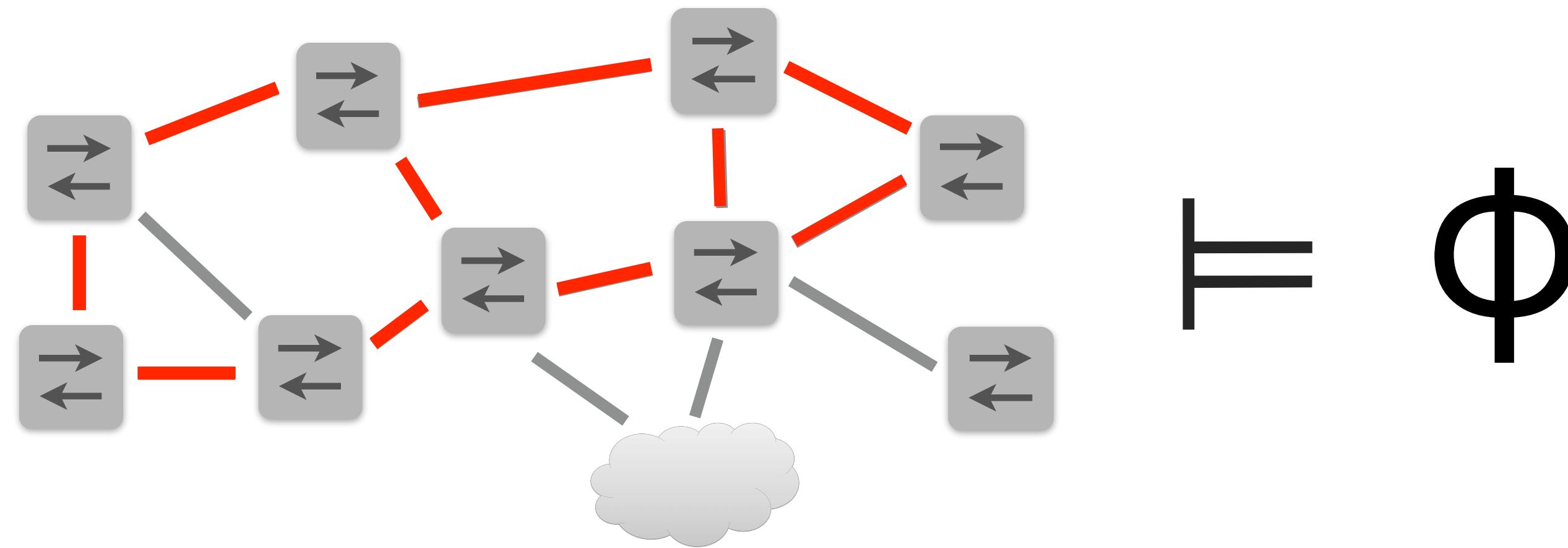
Networks

The behavior of an entire network can be encoded in NetKAT by interleaving steps of processions by switches and topology



policy
+
(policy; topo); policy
+
(policy; topo; policy; topo); policy
⋮
(policy; topo)*; policy

Reachability



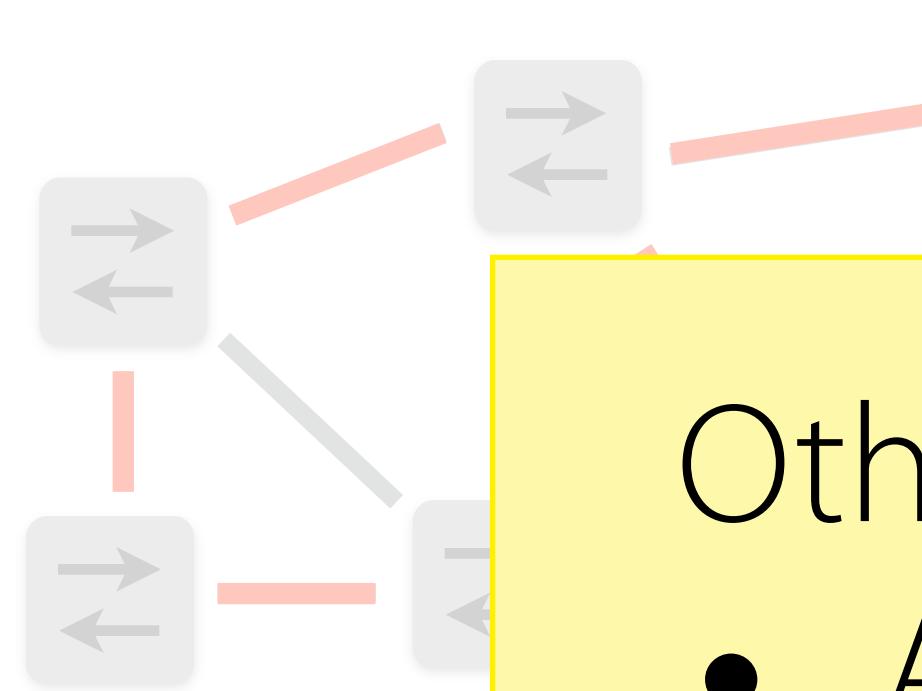
Given a network, want to be able to answer questions like:

“Does the network forward from ingress to egress?

Can reduce this question (and many others) to equivalence

in; (policy; topo)*; policy; out = in; out

Reachability



- Given a network,
“Does the network have progress?”
- Other properties:
- Access control
 - Traffic Isolation
 - Loop freedom
 - Blackhole freedom

φ

questions like:
Is there progress?

Can reduce this question (and many others) to equivalence

in; (policy; topo)*; policy; out = in; out

NetKAT Proof System

Kleene Algebra Axioms

$$p + (q + r) \equiv (p + q) + r$$

$$p + q \equiv q + p$$

$$p + \mathbf{false} \equiv p$$

$$p + p \equiv p$$

$$p; (q; r) \equiv (p; q); r$$

$$p; (q + r) \equiv p; q + p; r$$

$$(p + q); r \equiv p; r + q; r$$

$$\mathbf{true}; p \equiv p$$

$$p \equiv p; \mathbf{true}$$

$$\mathbf{false}; p \equiv \mathbf{false}$$

$$p; \mathbf{false} \equiv \mathbf{false}$$

$$\mathbf{true} + p; p^* \equiv p^*$$

$$\mathbf{true} + p^*; p \equiv p^*$$

$$p + q; r + r \Rightarrow p^*; q + r \equiv r$$

$$p + q; r + q \Rightarrow p; r^* + q \equiv q$$

Boolean Algebra Axioms

$$a + (b ; c) \equiv (a + b) ; (a + c)$$

$$a + \mathbf{true} \equiv \mathbf{true}$$

$$a + !a \equiv \mathbf{true}$$

$$a ; b \equiv b ; a$$

$$a ; !a \equiv \mathbf{false}$$

$$a ; a \equiv a$$

Packet Axioms

$$f := n; f' := n' \equiv f' := n'; f := n \quad \text{if } f \neq f'$$

$$f := n; f = n' \equiv f' = n'; f := n \quad \text{if } f \neq f'$$

$$f := n; f = n \equiv f := n$$

$$f = n; f := n \equiv f = n$$

$$f := n; f := n' \equiv f := n'$$

$$f = n; f = n' \equiv \mathbf{false} \quad \text{if } n \neq n'$$

$$A \Rightarrow B; f = n \equiv f = n; A \Rightarrow B \quad \text{if } f \neq \text{switch}$$

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$$\mathbf{true}$$

$$p$$

$$p$$

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$$(p + q); r \equiv p; r + q; r$$

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$$\boxed{f := n; f = n \equiv f := n}$$

$$f = n; f := n \equiv f = n$$

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$$p \equiv p; \mathbf{true}$$

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$$p + \text{false} \equiv p$$

$$p + p \equiv p$$

$$p; (q; r) \equiv (p; q); r$$

$$p; (q; r) \equiv (r; q); p$$

$$(p + q) + r \equiv p + (q + r)$$

$$\text{true}; p \equiv p$$

$$p \equiv p; \text{true}$$

$$\text{false}; p \equiv \text{false}$$

$$p; \text{false} \equiv \text{false}$$

$$\text{true}$$

$$\text{true}$$

$$p$$

$$p$$

Boolean Algebra Axioms

$$a + (b ; c) \equiv (a + b) ; (a + c)$$

$$a + \text{true} \equiv \text{true}$$

Soundness: If $\vdash p \equiv q$, then $\llbracket p \rrbracket = \llbracket q \rrbracket$

Completeness: If $\llbracket p \rrbracket = \llbracket q \rrbracket$, then $\vdash p \equiv q$

$$f := n; f' := n' \equiv f' := n'; f := n \quad \text{iff } f \neq f'$$

$$f := n; f' = n' \equiv f' = n'; f := n \quad \text{iff } f \neq f'$$

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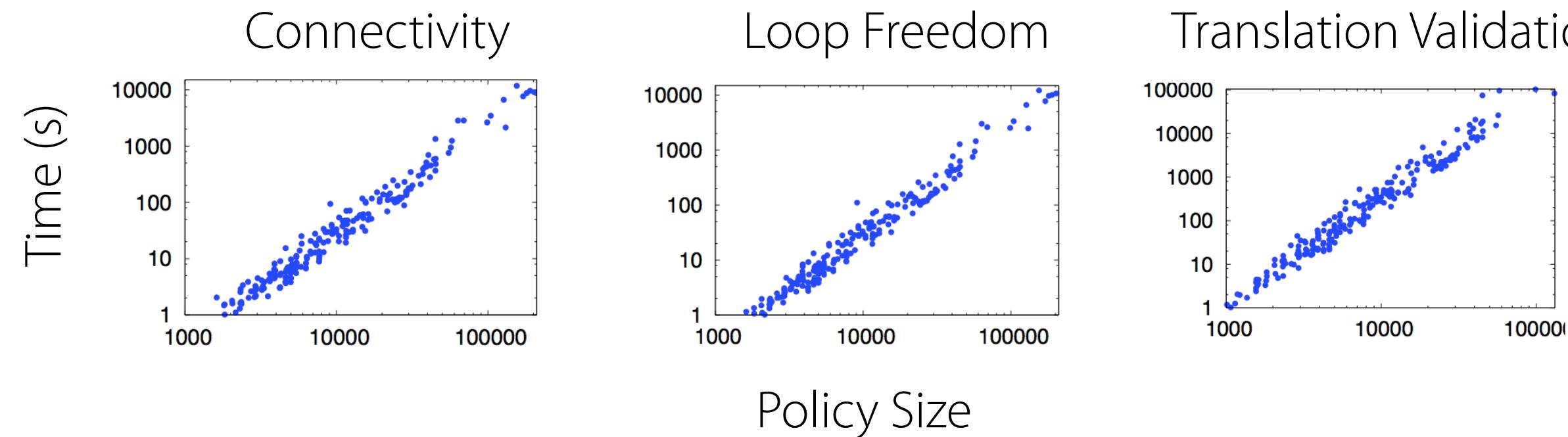
NetKAT Automata

[POPL '15]

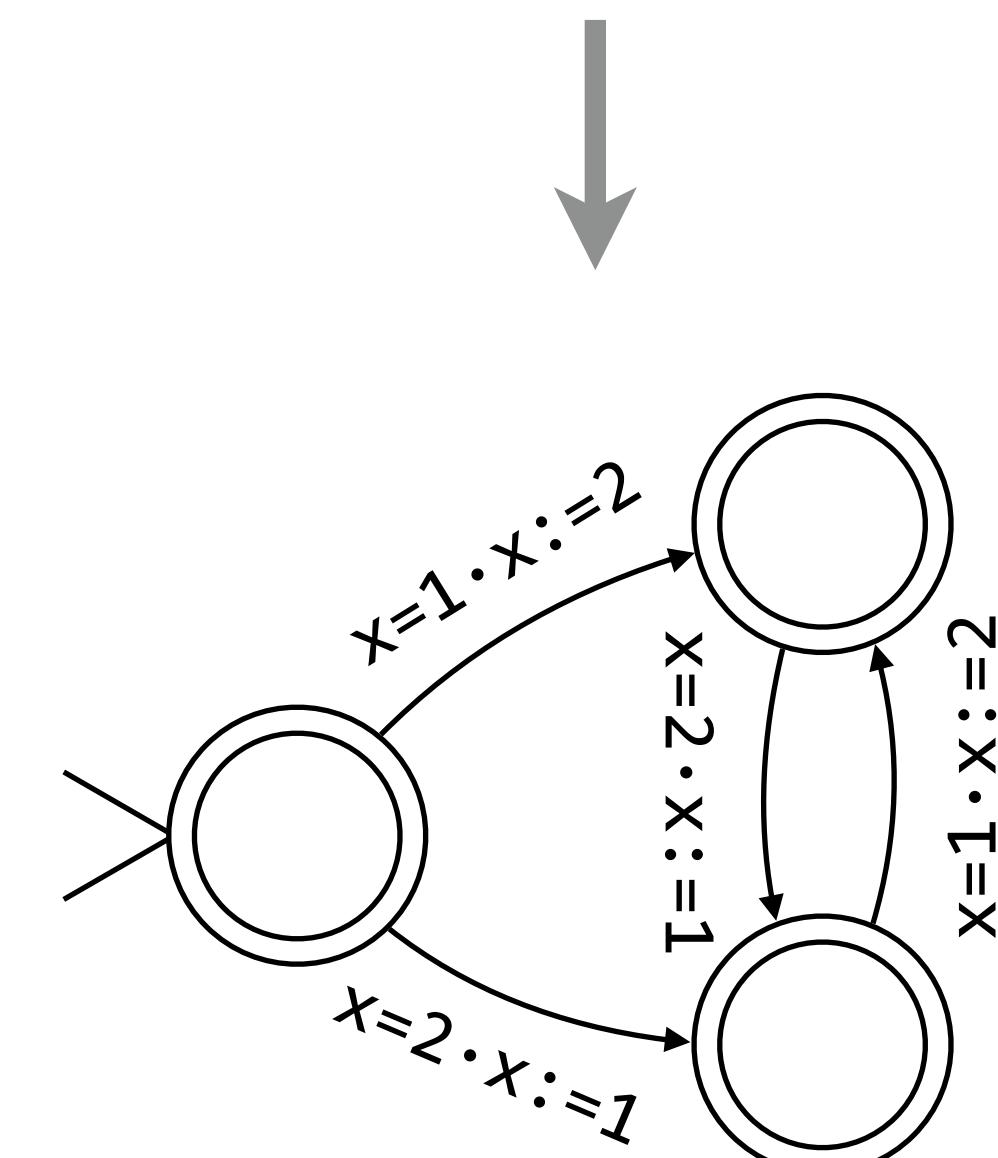
Can exploit NetKAT's regular structure
to build equivalent finite automata

Automata provide a practical way to
decide program equivalence

Prototype implementation performs
well on Topology Zoo benchmarks



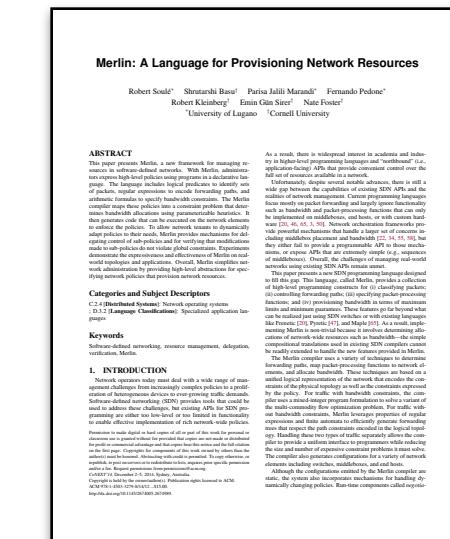
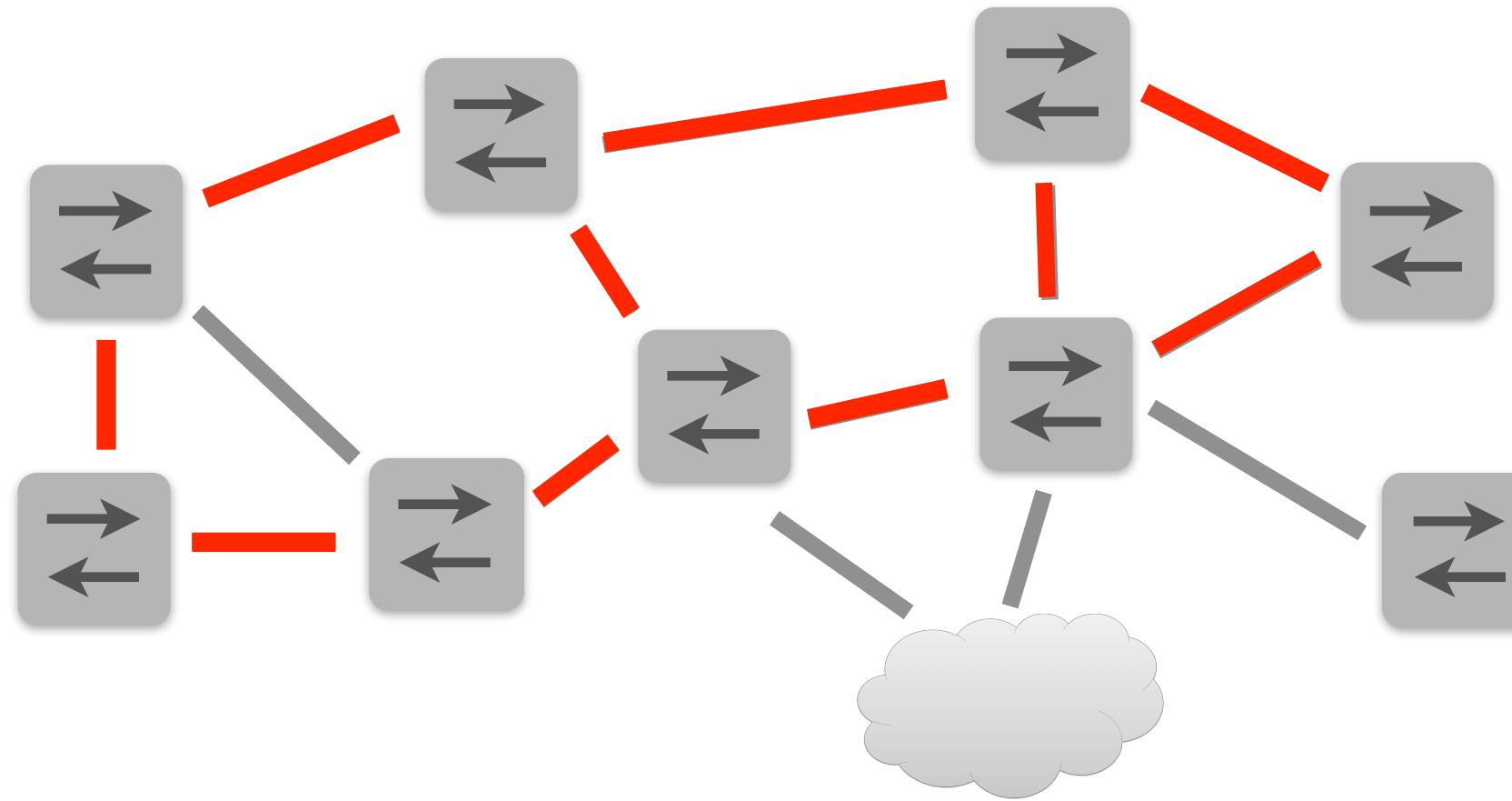
$(x=1; x:=2; A \Rightarrow B +$
 $x=2; x:=1; B \Rightarrow A)^*$



Other Applications

Regular paths have many uses:

- Network Virtualization
- Traffic Engineering
- Fault Tolerance
- Application Intent



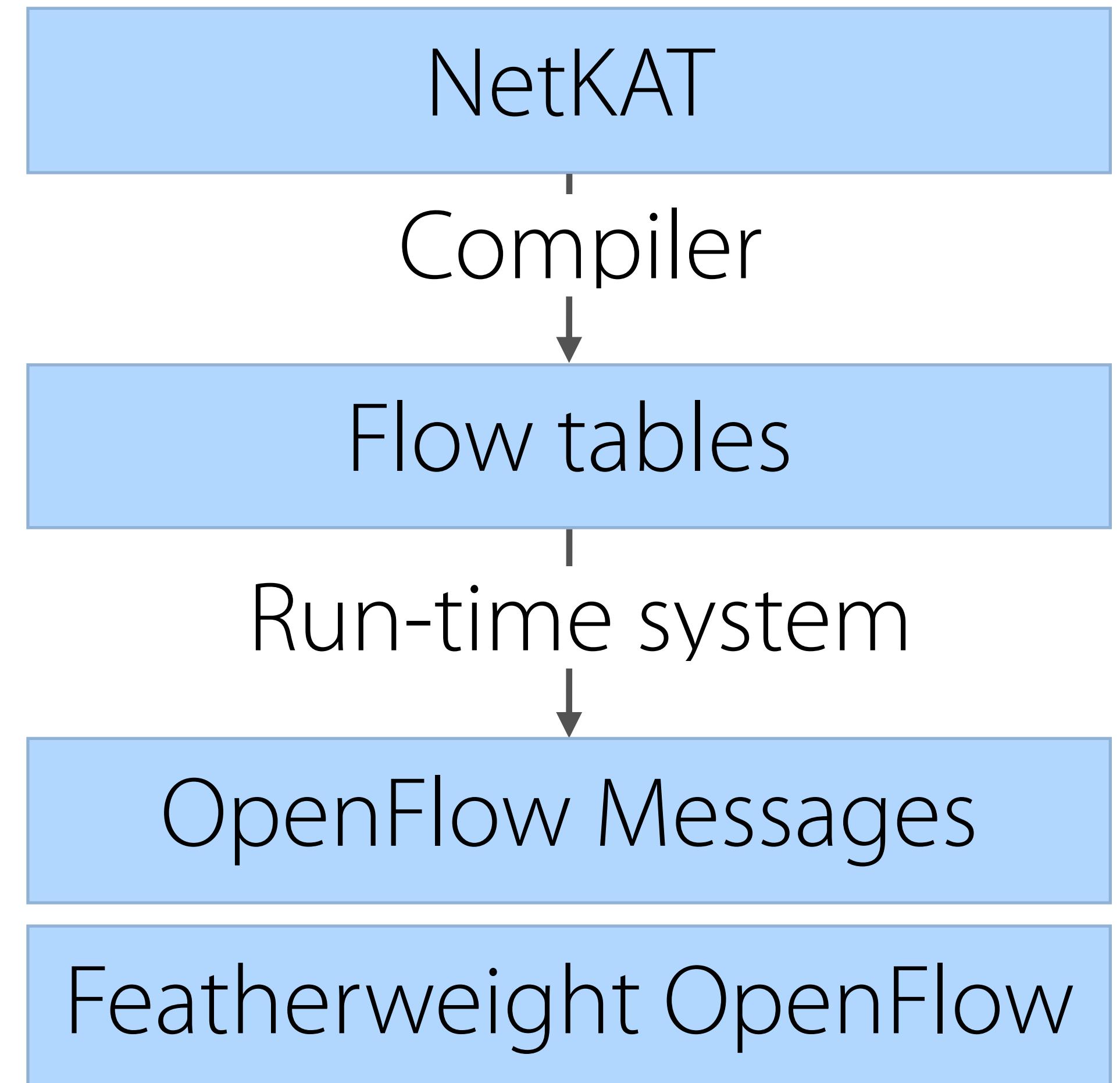
Verified Implementation

[PLDI '13]

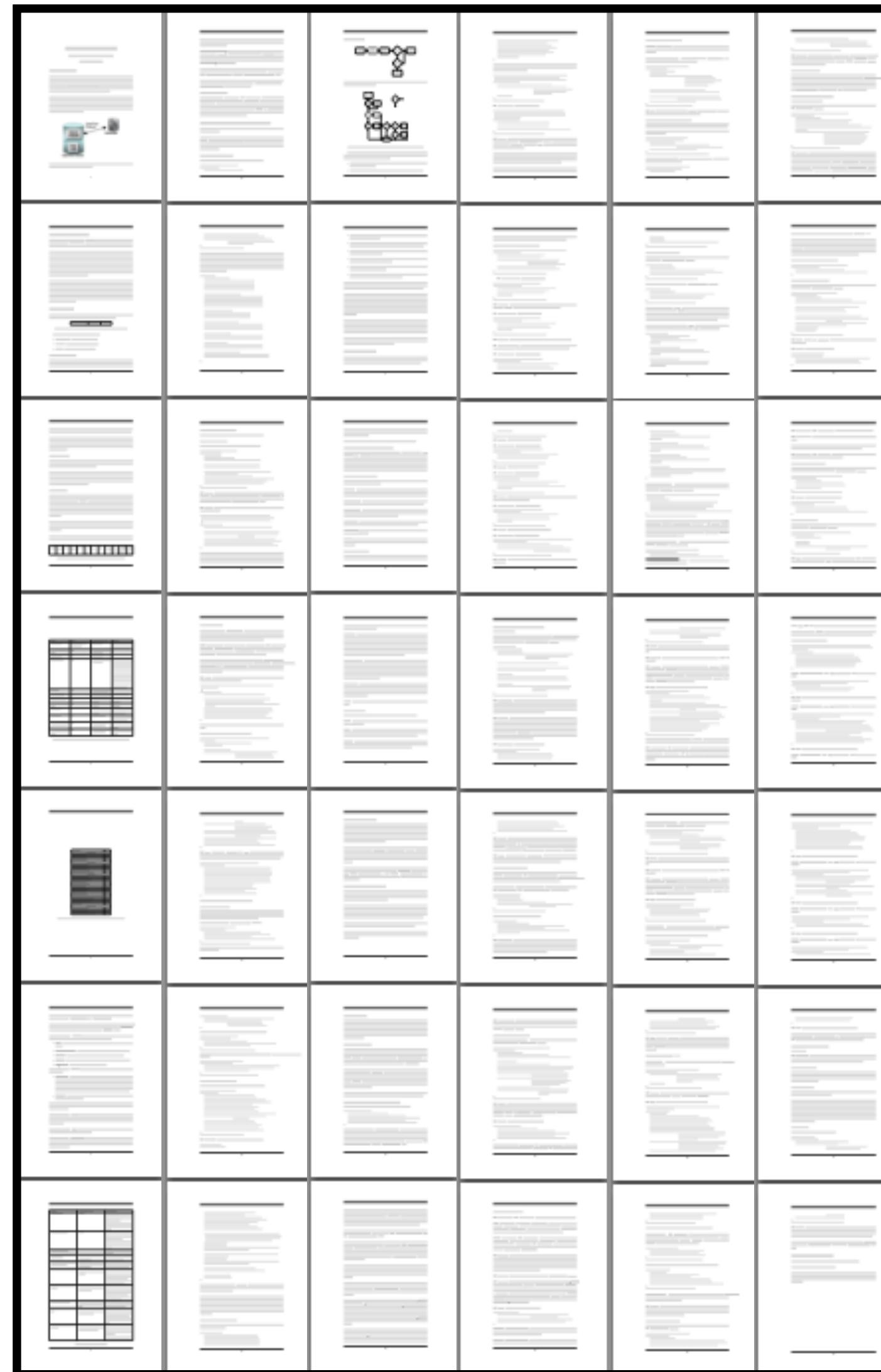
Question: How can we know the NetKAT compiler is correct?

Answer: implement it in a proof assistant!

- Formalize source and target languages in Coq
- Prove that transformations preserve semantics
- Extract code to OCaml and execute on real hardware



OpenFlow Specification



42 pages...

...of informal prose

...diagrams and flow charts

...and C struct definitions

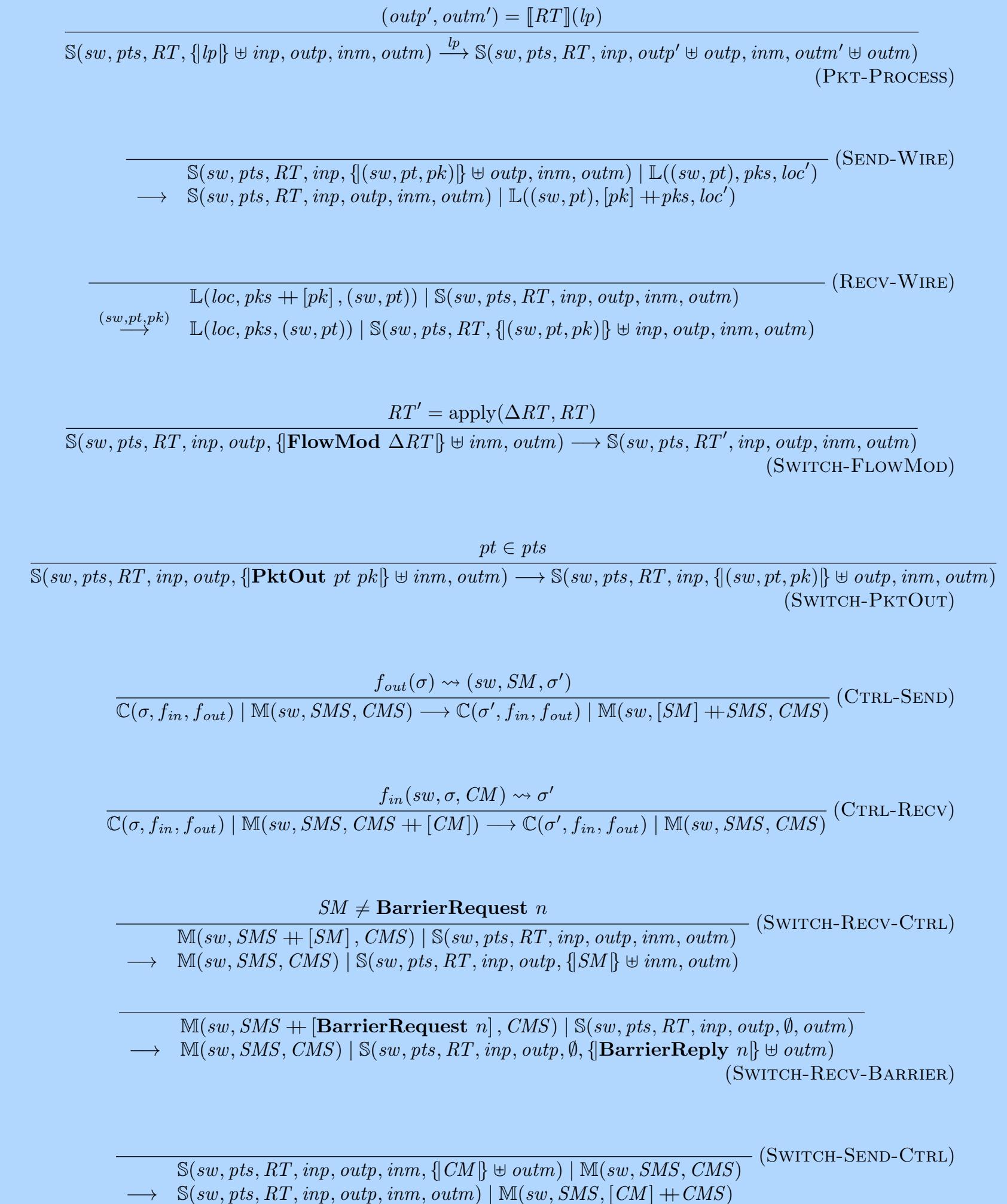
Syntax

Featherweight OpenFlow

Semantics

Devices	Switch Controller Link OpenFlow Link to Controller	S C L M	$\ ::= \mathbb{S}(sw, pts, RT, inp.outp, inm, out)$ $\ ::= \mathbb{C}(\sigma, f_{in}, f_{out})$ $\ ::= \mathbb{L}(loc_{src}, pks, loc_{dst})$ $\ ::= \mathbb{M}(sw, SMS, CMS)$
Packets and Locations	Packet Switch ID Port ID Location Located Packet	pk sw pt loc lp	$\ ::= abstract$ $\in \mathbb{N}$ $\in \mathbb{N}$ $\in sw \times pt$ $\in loc \times pk$
Controller Components	Controller state Controller input relation Controller output relation	σ f_{in} f_{out}	$\ ::= abstract$ $\in sw \times CM \times \sigma \rightsquigarrow \sigma$ $\in \sigma \rightsquigarrow sw \times SM \times \sigma$
Switch Components	Rule table Rule table Interpretation Rule table modifier Rule table modifier interpretation Ports on switch Consumed packets Produced packets Messages from controller Messages to controller	RT $[RT]$ ΔRT $apply$ pts inp $outp$ inm $outm$	$\ ::= abstract$ $\in lp \rightarrow \{lp_1 \dots lp_n\} \times \{CM_1 \dots C\}$ $\ ::= abstract$ $\in \Delta RT \rightarrow RT \rightarrow \Delta RT$ $\in \{pt_1 \dots pt_n\}$ $\in \{lp_1 \dots lp_n\}$ $\in \{lp_1 \dots lp_n\}$ $\in \{SM_1 \dots SM_n\}$ $\in \{CM_1 \dots CM_n\}$
Link Components	Endpoints Packets from loc_{src} to loc_{dst}	loc_{src}, loc_{dst} pks	$\in loc$ where $loc_{src} \neq loc_{dst}$ $\in [pk_1 \dots pk_n]$
Controller Link	Message queue from controller Message queue to controller	SMS CMS	$\in [SM_1 \dots SM_n]$ $\in [CM_1 \dots CM_n]$
Abstract OpenFlow Protocol	Message from controller Message to controller	SM CM	$\ ::= \text{FlowMod } \Delta RT \mid \text{PktOut } pt \ i$ $\ ::= \text{PktIn } pt \ pk \mid \text{BarrierReply } n$

- Models all features related to packet forwarding and *all* essential asynchrony
- Supports arbitrary controllers



Weak Bisimulation

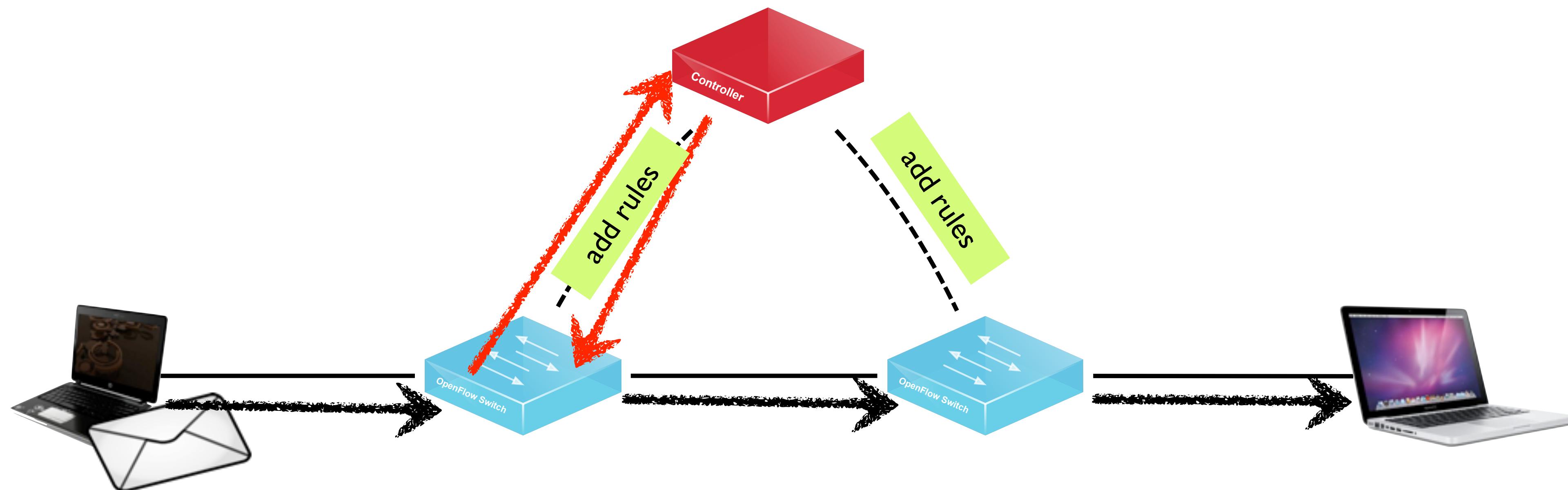
$(\mathcal{H}_1, \text{✉})$

Weak Bisimulation

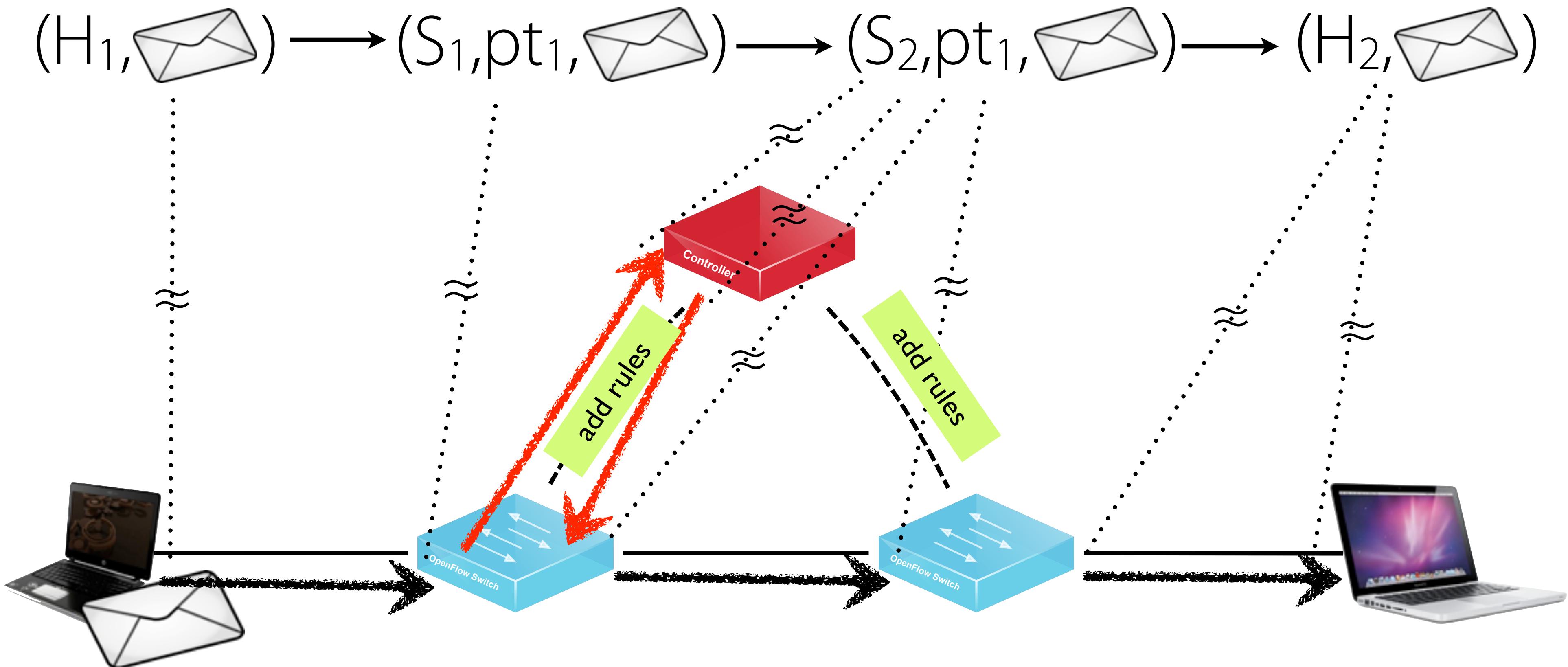
$(H_1, \text{✉}) \rightarrow (S_1, pt_1, \text{✉}) \rightarrow (S_2, pt_1, \text{✉}) \rightarrow (H_2, \text{✉})$

Weak Bisimulation

$(H_1, \text{✉}) \rightarrow (S_1, pt_1, \text{✉}) \rightarrow (S_2, pt_1, \text{✉}) \rightarrow (H_2, \text{✉})$



Weak Bisimulation



Theorem: NetKAT semantics is weakly bisimilar
to Featherweight OpenFlow + run-time system

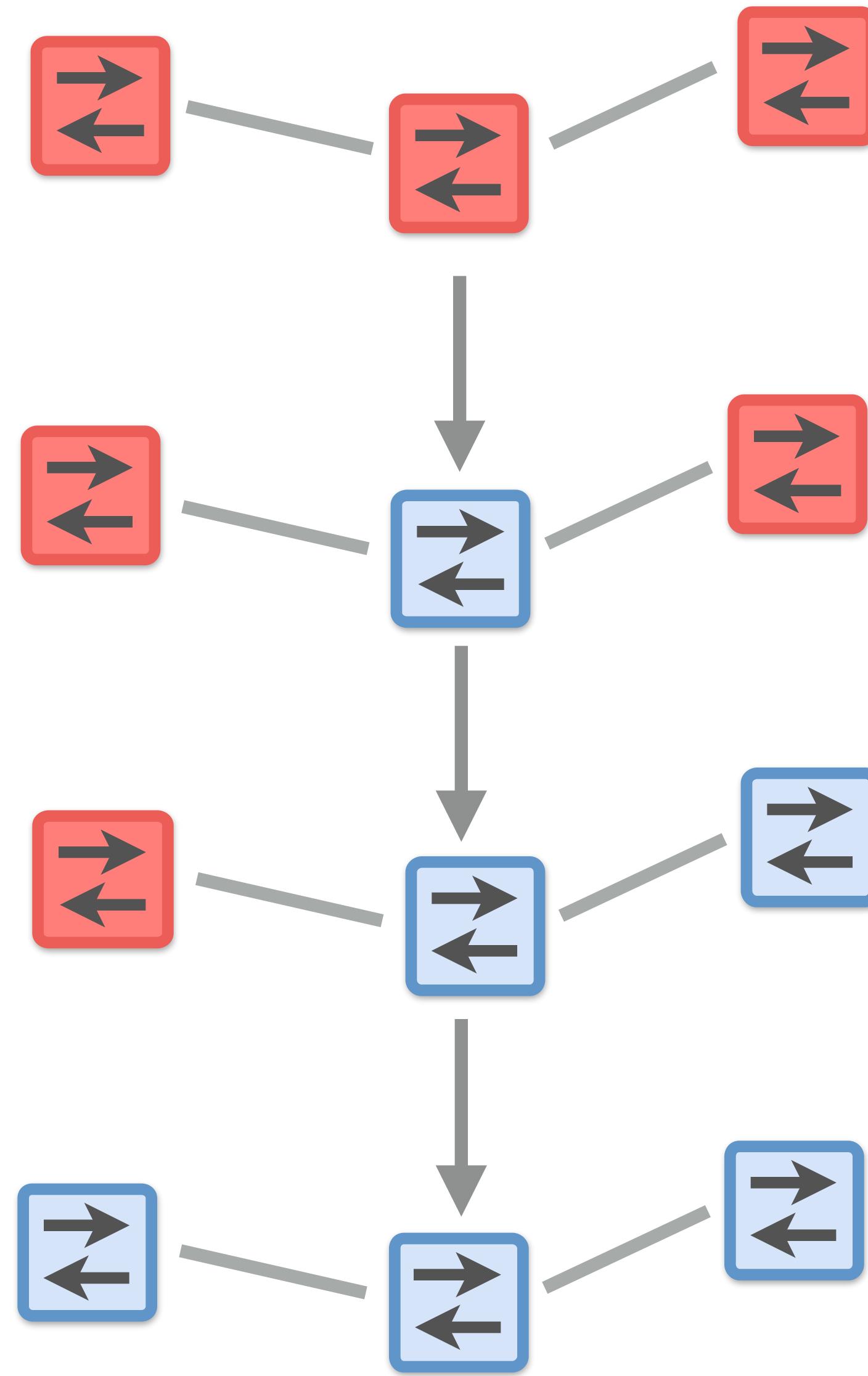
Network Updates

Question: how can we gracefully transition the network from one program to another?

Initial Program



Final Program



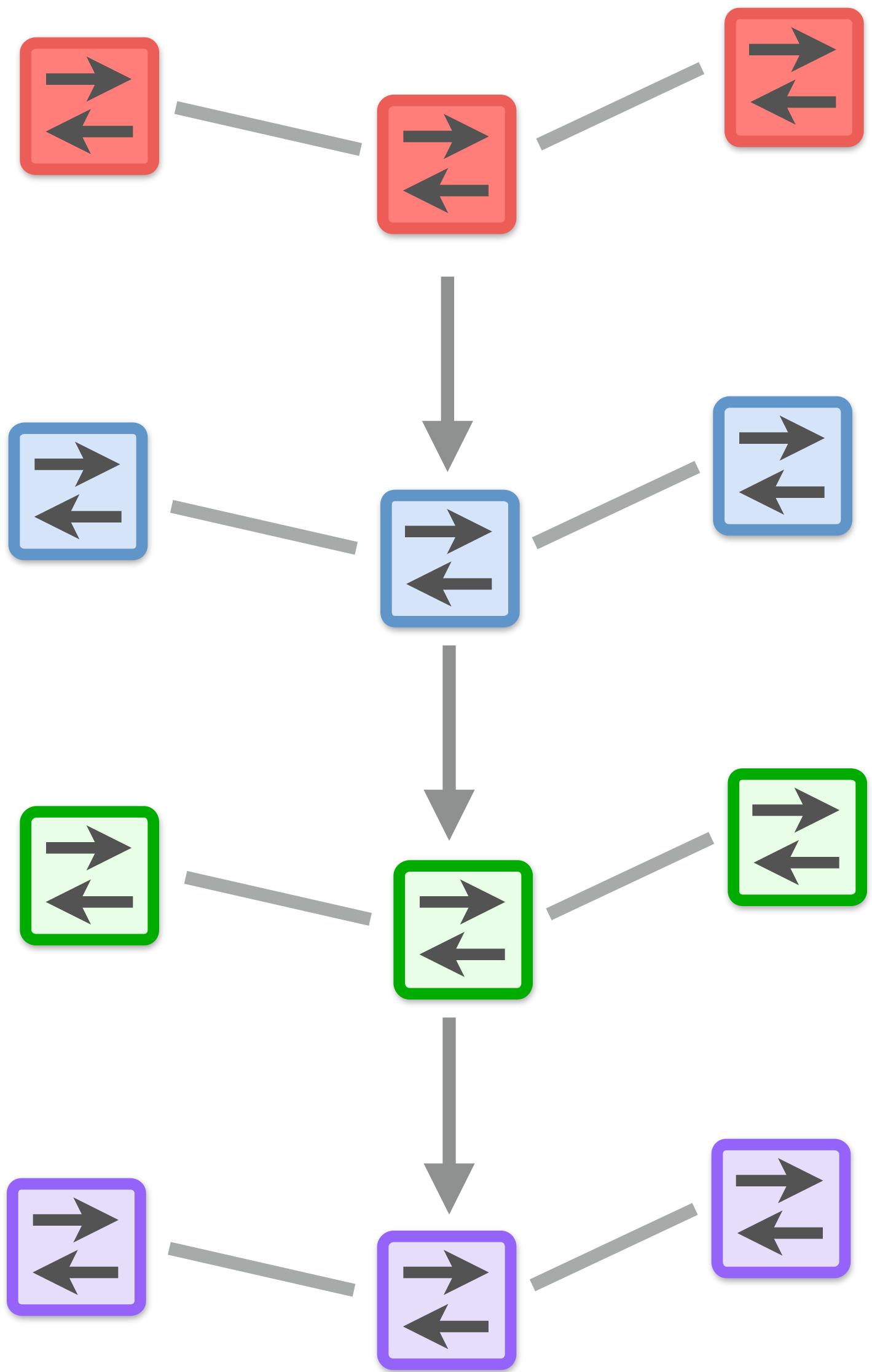
Consistent Updates

[SIGCOMM '12]

Operationally: every packet (or flow) processed using a consistent version of the network-wide configuration

Semantically: guarantee preserves all safety properties

Implementations: many different possibilities—e.g., one option is to use a two-phase distributed protocol

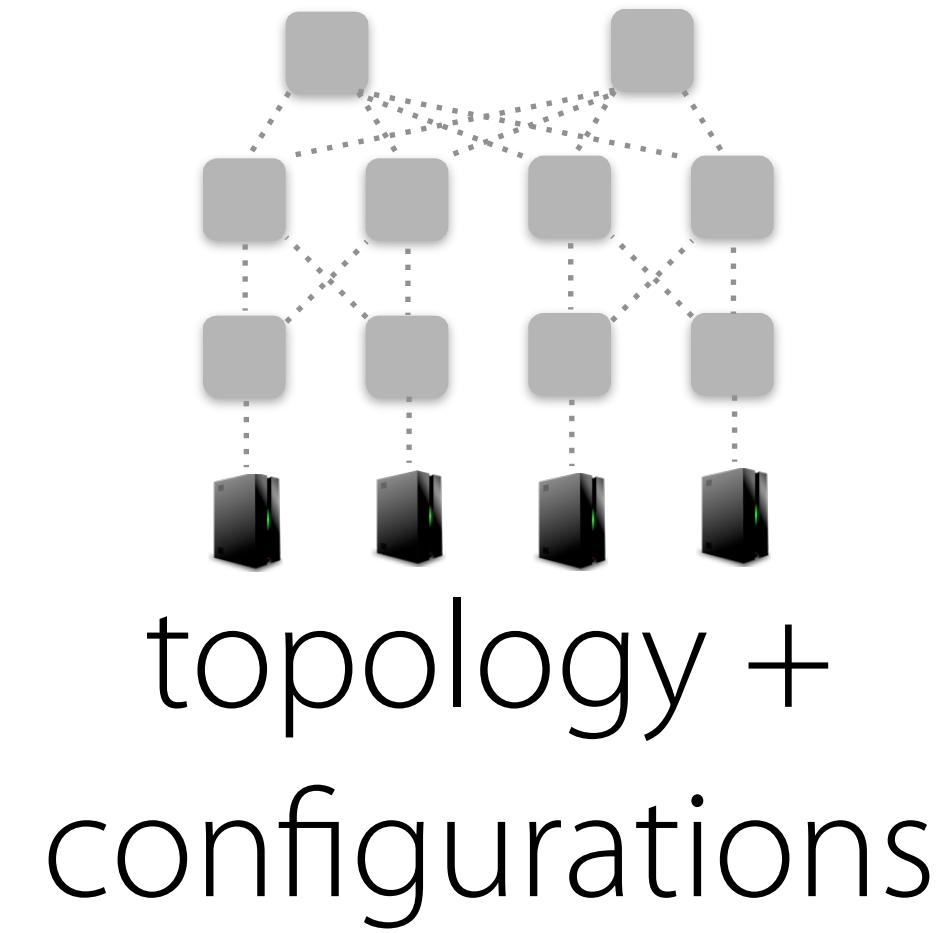


Update Synthesis

[PLDI '15]

ϕ

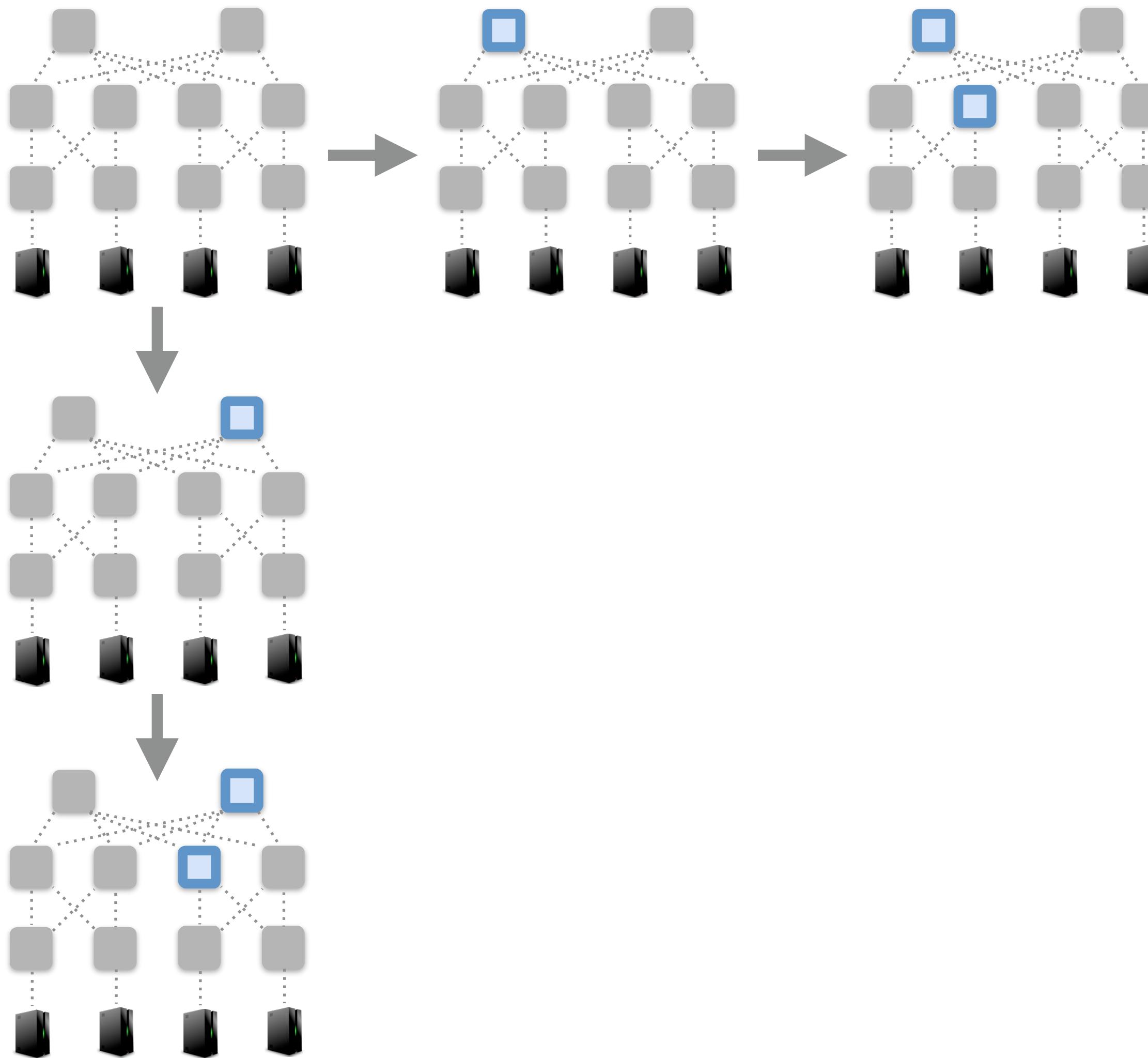
Logical
property



Update Synthesis

[PLDI '15]

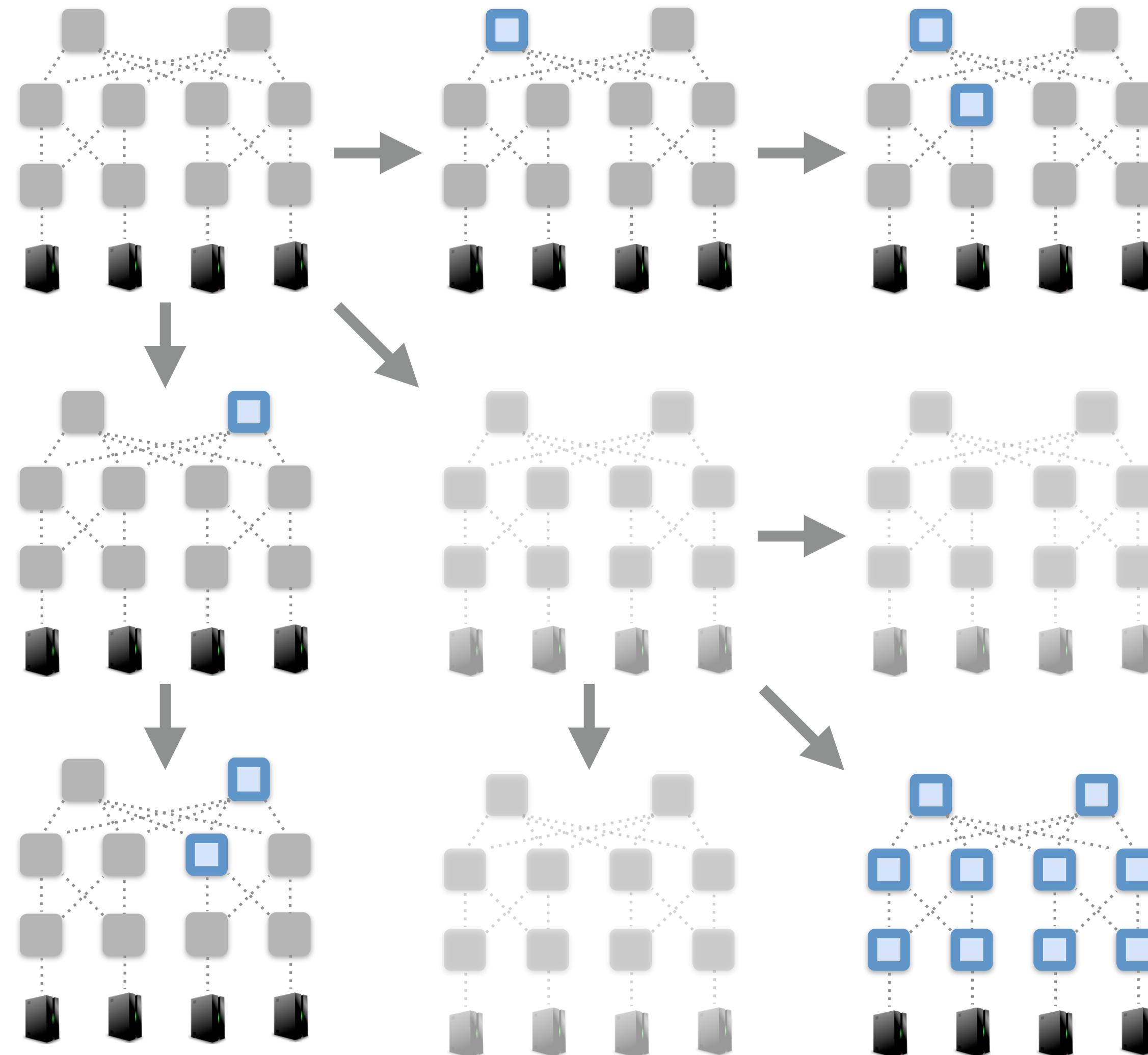
ϕ



Update Synthesis

[PLDI '15]

ϕ



Conclusion

- Programming languages and formal methods have a key role to play in next-generation networking platforms
- The NetKAT language offers expressive constructs for specifying and verifying network functionality
- Formal methods are ready for prime time!

Ongoing Work

- Probabilistic semantics
- Stateful functions
- Multi-packet properties

Thank you!

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frenetic

<http://frenetic-lang.org/>