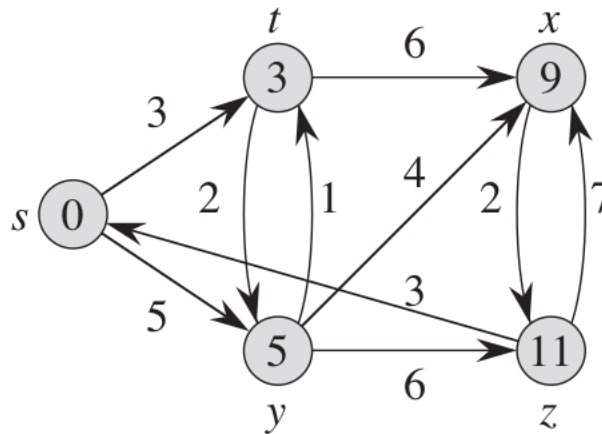


## TUTORIAL X

Date: Nov 13, 2024.

1. Run the Dijkstra's algorithm on the following weighted directed graph and find the shortest distance from source  $s$  to every other vertex. Draw the shortest-path tree.



2. Run the Dijkstra's algorithm on the above graph using priority queue implementation. Show the priority queue after every step.
3. Give an example of a directed graph with negative-weight edges for which Dijkstra's algorithm produces incorrect answers.
4. (a) Consider a directed graph which has **exactly one** negative edge leaving  $s$ ; all other edges are positive. Can Dijkstra's algorithm, started at  $s$ , fail on such a graph? justify your answer.  
 (b) Consider a directed graph in which the only negative edges are those that leave  $s$ ; all other edges are positive. Can Dijkstra's algorithm, starting at  $s$ , fail on such a graph? justify your answer.
5. We know that Dijkstra's algorithm may not work if the graph has negative-weight edges.

Let  $G$  be a weighted (edge weights may be negative) directed **acyclic** graph with a source vertex  $s$ . Design an algorithm to compute the length of the shortest path from  $s$  to every other vertex of  $G$ .