

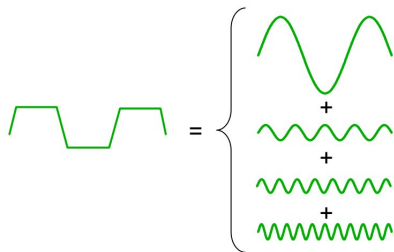
# Foundations of Data Science DSL201

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# Decomposition of signal using Fourier transform



# Decomposition of signal using Fourier transform

■ Original (sampled at 48KHz): Original

■ LPF 2000Hz: LPF 2000Hz

■ LPF 3000Hz: LPF 3000Hz

■ LPF 4000Hz: LPF 4000Hz

■ LPF 5000Hz: LPF 5000Hz

■ LPF 6000Hz: LPF 6000Hz

■ LPF 7000Hz: LPF 7000Hz

■ HPF 8000Hz: HPF 8000Hz

■ Original (sampled at 48KHz): Original

■ LPF 2000Hz: LPF 2000Hz

■ LPF 3000Hz: LPF 3000Hz

■ LPF 4000Hz: LPF 4000Hz

■ LPF 5000Hz: LPF 5000Hz

■ LPF 6000Hz: LPF 6000Hz

■ LPF 7000Hz: LPF 7000Hz

■ LPF 8000Hz: LPF 8000Hz

■ HPF 8000Hz: HPF 8000Hz

## 2-D sinusoidal function

$$\sin\left(2\pi\left(\frac{u}{M}m + \frac{v}{N}n\right)\right)$$

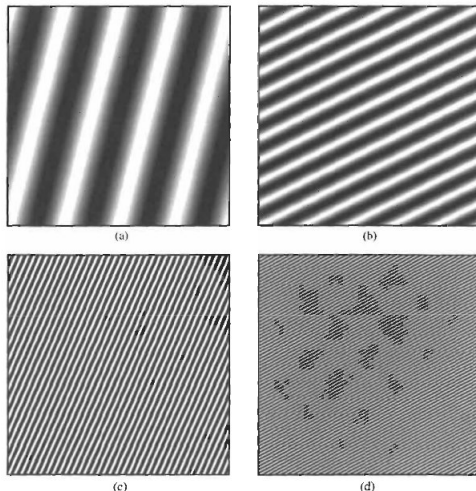
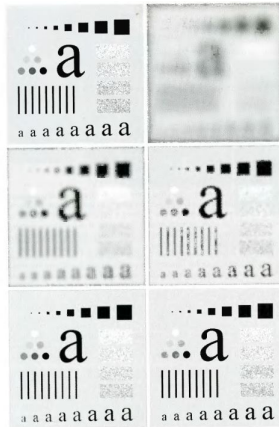


FIGURE 1 Examples of finite two-dimensional discrete-space sinusoidal functions. The scaled frequencies of Eq. (6) measured in cycles/image are (a)  $u = 1$ ,  $v = 4$ ; (b)  $u = 10$ ,  $v = 5$ ; (c)  $u = 15$ ,  $v = 35$ ; and (d)  $u = 65$ ,  $v = 35$ .

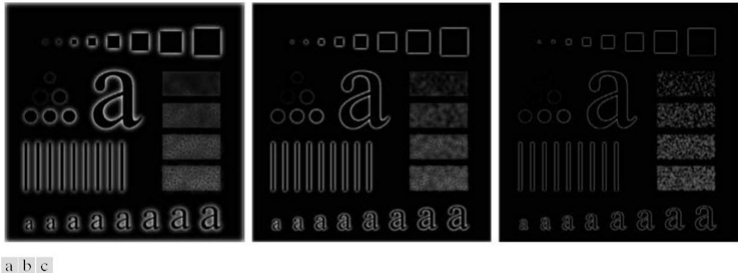
# Results of Gaussian lowpass filter



**FIGURE 4.18** (a) Original image. (b)–(f) Results of filtering with Gaussian lowpass filters with cutoff frequencies set at radii values of 5, 15, 30, 80, and 200, as shown in Fig. 4.11(b). Compare with Figs. 4.12 and 4.15.

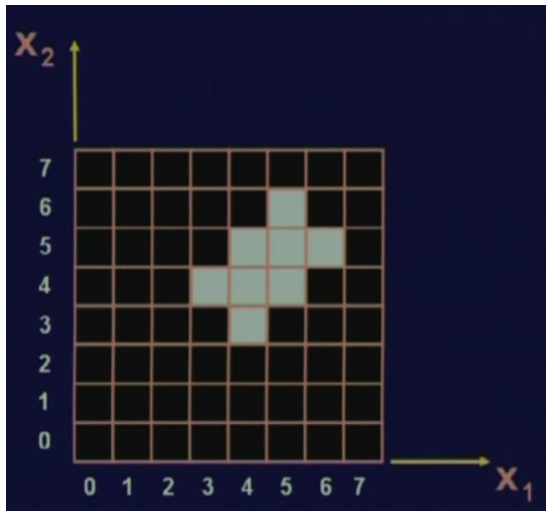
a b  
c d  
e f

## Results of Gaussian highpass filter for different cut-off frequency



**FIGURE** Results of highpass filtering the image in Fig. 4.41(a) using a GHPF with  $D_0 = 30, 60$ , and  $160$ , corresponding to the circles in Fig. 4.41(b). Compare with Figs. 4.54 and 4.55.

# KL transform



# KL Transform

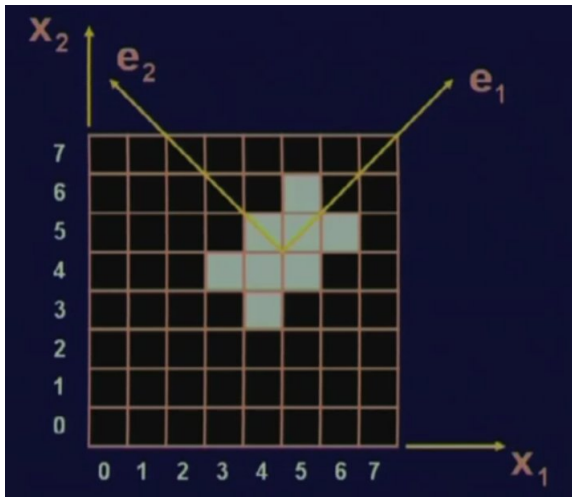






Figure: Examples of images used to compute the principal components

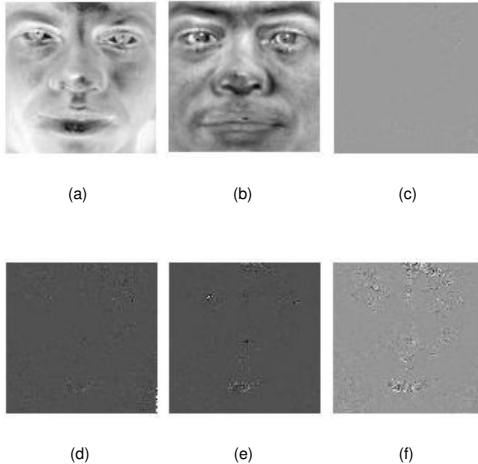
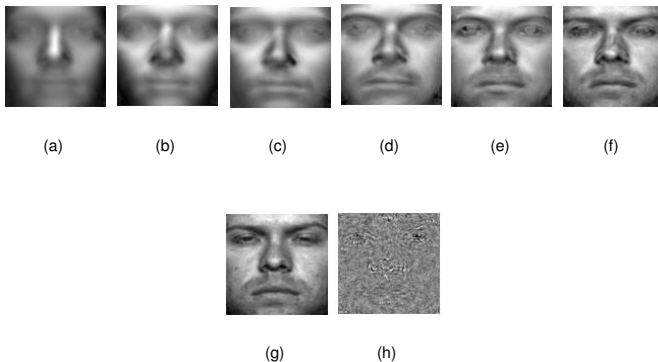


Figure: Eigen Vectors- (a)1st, (b) 3rd, (c)5th, (d)10th, (e) 15th, (f)100th

Eigen vectors are also known as eigenfaces in the literature of face recognition.



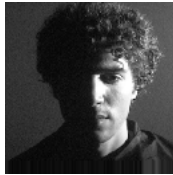
**Figure:** Reconstructed image using Eigen Vectors-  
 (a)1-5,(b)1-10,(c)1-20,(d)1-50,(e)1-100,(f)1-200,(g)1-500,(h)500-Remaining



(a)

(b)

**Figure:** (a)Original Image,(b) Reconstructed using first 500 eigen vectors from the previous datasets subspace



(c)



(d)

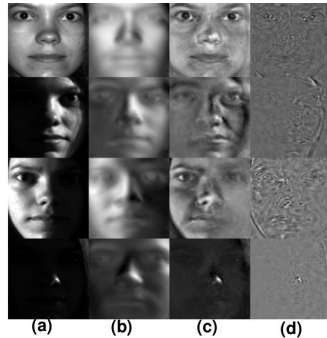
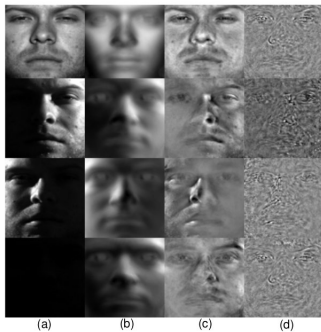
**Figure:** (a)Original Image,(b) Reconstructed using first 500 eigen vectors from the previous datasets subspace



(a)



(b)



**Figure:** Illustration of subject specific unique information derived using eigen decomposition. (a) Gray level image. The reconstructed face image using (b) first 10 eigenvectors, (c) 11-350 eigenvectors, (d) 351-10000 eigenvectors.