

NAME: .....

CSCI S-89c Deep Reinforcement Learning

Part I of Assignment 2

Please consider a Markov Decision Process with two states:  $s^A$  and  $s^B$ .

Assume that the sets of admissible actions in states  $s^A$  and  $s^B$  are  $\mathcal{A}(s^A) = \{a_1^A, a_2^A\}$  and  $\mathcal{A}(s^B) = \{a_1^B, a_2^B\}$ , respectively. Further, assume that the transition probabilities are given by:

$$p(s', r | s^A, a_1^A) = \begin{cases} 1, & \text{if } s' = s^A, r = r_1^A, \\ 0, & \text{otherwise,} \end{cases}$$

$$p(s', r | s^A, a_2^A) = \begin{cases} 1, & \text{if } s' = s^A, r = r_2^A, \\ 0, & \text{otherwise,} \end{cases}$$

$$p(s', r | s^B, a_1^B) = \begin{cases} 1, & \text{if } s' = s^B, r = r_1^B, \\ 0, & \text{otherwise,} \end{cases}$$

$$p(s', r | s^B, a_2^B) = \begin{cases} 1, & \text{if } s' = s^B, r = r_2^B, \\ 0, & \text{otherwise,} \end{cases}$$

where  $r_1^A$ ,  $r_2^A$ ,  $r_1^B$ , and  $r_2^B$  are known.

If policy  $\pi(a|s)$  is to always take action  $a_1^A$  in state  $s^A$  and action  $a_1^B$  in state  $s^B$ , find

(a)  $v_\pi(s^A)$

(b)  $q_\pi(s^A, a_1^A)$

(c)  $q_\pi(s^A, a_2^A)$

SOLUTION: