

Thank you, next: demographic consequences of partner diversity and turnover in a multi-species ant-plant mutualism

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Abstract

¹ Mutualisms are widespread species interactions with diverse and dynamic consequences. They are considered more context dependent than other species interactions, meaning there are many different factors which change the outcomes of interactions between mutualists, including partner diversity. Partner diversity has become a central focus in the field of mutualisms, expanding previous work from primarily pairwise to multispecies mutualisms. It has been shown that pairwise studies are poor predictors of the effects of multispecies mutualistic interactions. The diversity of partners in a multi-species mutualism causes varied demographic effects on the population of the focal mutualist which can be explained by several mechanisms: portfolio effect, complementarity, and sampling effect.

I use the plant-ant multi-species mutualism in which, the cactus *Cylindropuntia imbricata* (tree cholla) produce extrafloral nectar and the ants, *Crematogaster opuntiae*, *Liometopum apiculatum*, *Forelius pruinosus*, and rarer species, provide defense from various herbivores and seed predators. I used 18 years of data collected from plant demographic censuses, which includes data such as size, survival, reproductive status, flowers produced, and ant partner for all plants in 8 30×30 m plots at the Sevilleta National Wildlife Refuge in central New Mexico. With this data I parameterize a series of Bayesian hierarchical generalized linear vital rate models to determine the impacts of different partners on the focal mutualists. I found that different ant partners had different impacts on the vital rates of the tree cholla. Specifically, *C. opuntiae* tended plants had advantages in both growth and survival when small, and large *L. apiculatum* tended plants had floral viability advantages. With these models I constructed an Integral Projection Model in which I could vary the presence of each partner, creating different “diversity scenarios”, to determine under which diversity scenario the focal mutualist experienced the highest plant fitness, and which mechanism(s) may explain the effects of partner diversity. I found that the all scenar-

¹I think this is too long for Am Nat requirements. Also, use “we”. I think you just pasted in an abstract that you used elsewhere, so I will work on this once you write a real abstract for the Am Nat paper.

ios which included the partner *L. apiculatum* resulted in the highest possible fitness for the tree cholla. Results further suggest that diversity benefits in this system are driven by sampling effect
27 , meaning *L. apiculatum* ants are the "best" partner. I also found that partner diversity benefits the focal mutualist in this system in the form of portfolio effect by buffering the tree cholla from the effects of inter-annual variation. This study highlights how partner diversity can increase
30 the overall benefits a focal mutualist receives. It also highlights the importance of a mechanistic understanding to explain the benefits of this diversity across systems.

Introduction

Mutualisms are species interactions where all participants receive net benefits, leading to higher individual fitness and increased population growth rates. They are widespread species interactions (Axelrod and Hamilton, 1981; Bronstein, 1994; Chamberlain et al., 2014; Frederickson, 2013; Leigh, 2010) but can deteriorate into commensalism or parasitism under conditions that elevate costs or dampen benefits (Bahia et al., 2022; Mandyam and Jumpponen, 2014; Rodriguez-Rodriguez et al., 2017; Song et al., 2020; Thrall et al., 2007). Mutualisms are considered more context dependent than other species interactions (Chamberlain et al., 2014; Frederickson, 2013), meaning the magnitude and sign of interaction strength are often determined by environmental conditions and species' identities (Leigh, 2010; Noe and Hammerstein, 1994).

Mutualism is defined at the level of a species pair (+/+) but these interactions are embedded within multi-species communities, and growing evidence suggests that pairwise interactions are poor predictors of the net effects of multi-species mutualism (Afkhami, 2014; Bascompte, 2009; Dattilo et al., 2014; Palmer et al., 2010). A focal mutualist may interact with multiple guilds of partner types (e.g., plants that interact with pollinators, seed dispersers, soil microbes, and ant defenders) or with multiple partner species within the same guild (e.g., plants visited by multiple pollinator species). Within a mutualist guild, partner species often differ in the amount or type of goods or services they provide, making partner identity an important source of contingency in mutualism (Stanton, 2013). Whether and how partner diversity modifies the demographic effects of mutualistic interactions remain open questions within relevance in **applied settings**² (Rogers et al., 2014).

There are multiple mechanisms by which partner diversity can influence the net benefits accrued by a focal mutualist, mirroring the mechanisms by which, at a larger scale of organization, biodiversity can influence ecosystem function Barrett et al. (2015); Ushio (2020); Yeung et al. (2006). First, when there is a hierarchy of fitness effects (a consistent ranking of best to worst

²would be good if you could find another applied example to cite here

mutualists), a more diverse sample of the partner community may be more likely to include the best partner Frederickson (2013). This can lead to an apparent benefit of diversity driven by a sampling effect Batstone (2018) – but there is no benefit of diversity *per se*, only better and worse partners. If partner associations are mutually exclusive (a focal mutualist may engage with only one partner at a time), then partner diversity may impose opportunity costs, leading to negative effects of a diverse mutualist assemblage relative to exclusive association with the single best partner (Miller, 2007). Second, even within a single mutualist guild, the benefits conferred by alternative partner species can vary in type and not just degree Bronstein et al. (2006); Stachowicz and Whitlatch (2005); Stanton (2013). This can lead to a positive effect of partner diversity through complementarity of alternative functions Batstone (2018). Interference or synergies between partners can make their combined effect different than the expected from the sum of complementary functions Afkhami (2014). Third, partner species can have species-specific responses to environmental variation, either spatially (Ollerton et al., 2006) or temporally (Alarcón et al., 2008). Multiple partners can therefore act as a ‘portfolio’ that stabilizes fitness benefits across spatial or temporal heterogeneity, leading to positive effects of partner diversity through the portfolio effect Batstone (2018); Horvitz and Schemske (1990); Lázaro et al. (2022).

Partner diversity can have different effects depending on whether partners are present all at once or sequentially (partner turnover) (Barrett et al., 2015; Bruna et al., 2014; Dattilo et al., 2014; Djiéto-Lordon et al., 2005; Ness et al., 2006; Ushio, 2020). Sequential associations are likely when alternative partners engage in interference competition for access to a shared mutualist Batstone (2018); Kiers et al. (2003); Trøjelsgaard et al. (2015); Wulff (2008). Turnover can happen at different timescales, from minutes to years (Horvitz and Schemske, 1986; Oliveira et al., 1999). The frequency of partner turnover can impact the level of benefits received by the focal mutualist, particularly if the benefits continue to accumulate with successive turnover (e.g., when sequential partners provide complementary functions) or if they saturate over time (Fiala et al., 1994; Sachs et al., 2004). Directionality of turnover can also influence effects of partner diversity if partner identity changes consistently across ontogeny of a focal mutualist (Dejean et al., 2008; Fonseca

et al., 2003; Noe and Hammerstein, 1994). For example, plant susceptibility to enemies can change across life stages (Barton and Koricheva, 2010; Boege and Marquis, 2005), so the benefits of defensive mutualism with ants are greatest when more defensive partner species align with more vulnerable life stages (Dejean et al., 2008; Djiéto-Lordon et al., 2005).

Defensive ant-plant mutualisms – where plants provide food and/or housing to ants that in turn defend them from enemies – are widespread interactions that offer valuable model systems for the ecology and evolution of mutualism (Bronstein, 1998; Bronstein et al., 2006). Extrafloral nectar (EFN) -bearing plants can serve as dietary resources that promote ant abundance and colony size (Byk and Del-Claro, 2011; Donald and Miller, 2022; Ness et al., 2006, 2009). Presence of defensive ant partners is often linked to reductions in herbivory (Rudgers, 2004; Trager et al., 2010) and demographic advantages for the plant partner (Báez et al., 2016). Defensive ant-plant mutualisms are commonly multi-species, where a guild of ant partner species share, and often compete for, a plant mutualist (Agrawal and Rutter, 1998; Beattie, 1985; Bronstein, 1998; Trager et al., 2010). Ant partners can vary in their ability to deter herbivores (Bruna et al., 2014), and visitation by low quality ant partners can prevent visitation by higher quality partners, consequently causing a reduction in fitness through missed opportunity costs (Fraser et al., 2001; Frederickson, 2005). Susceptibility to herbivory can also vary significantly throughout the life stages of the plant (Boege and Marquis, 2005), suggesting that the order and timing of successive partners is important to the fitness impacts of the combined partner guild (Barton and Koricheva, 2010; Boege and Marquis, 2005; Fonseca et al., 2003). Herbivore identity and pressure can vary inter-annually (Wetzel et al. (2023)), much like mutualist identity and presence, meaning the threat plants face can vary just as much as the protection they receive due to temporal stochasticity. Previous studies have investigated how ant partner diversity affects plant fitness (Afkhami, 2014; Dattilo et al., 2014; Fiala et al., 1994; Gaume et al., 1998; Ludka et al., 2015; Palmer et al., 2010). However, little is known about the combined effects of partner identity, directional partner turnover, and temporal stochasticity, particularly because the necessary long-term data are rarely available.

111 This study examined the consequences of partner diversity in a food-for-protection mutu-
alism between the tree cholla cactus (*Cylindriopuntia imbricata*), a long-lived EFN-bearing plant,
and multiple species of ant partners. Previous studies have shown that herbivory by specialized
114 insect herbivores negatively affects plant fitness Miller et al. (2009), and ant defense reduces her-
bivore damage Miller (2007). Tree cholla are tended by two common ant species (*Liometopum*
apiculatum and *Crematogaster opuntiae*) and several additional rarer species, all of which collect
117 EFN during foraging visits but their colonies are ground-nesting and not housed by the plants.
These ant species locally co-occur but individual plants are typically tended by only one species
that patrols the plant around-the-clock and maintains control of the plant's nectar resources for
120 an entire growing season (Donald and Miller, 2022; Ohm and Miller, 2014). Switches between
partner species, or between vacancy and ant occupancy, commonly occur from one growing
season to the next (Miller, 2007). Prior experiments suggested a hierarchy of mutualist quality,
123 with *Liometopum apiculatum* providing strong anti-herbivore defense and *Crematogaster opuntiae*
having net negative effects because herbivore deterrence is outweighed by deterrence of pollina-
tors (Miller, 2007; Ohm and Miller, 2014). However, previous studies in this system focused on
126 single life stages (adult plants) or vital rates (seed production) and did not integrate the demo-
graphic effects of ant defense across the life cycle, which may be essential for understanding net
fitness effects (e.g., Palmer et al., 2010). To our knowledge no previous study has incorporated
129 inter-annual stochasticity into models of ant-plant dynamics, which limits our understanding of
diversity benefits that may arise through the portfolio effect.

We used a unique long-term data set that allows us to explore mutualistic associations with
132 multiple partner species, longitudinal turnover in partner identity at the individual level, and
how the demographic effects of alternative partner species varied across plant size structure
and nearly 20 years of inter-annual fluctuations. We used this observational data set of ant-
135 plant associations, informed by previous ant exclusion experiments, to ask whether and through
which mechanism(s) partner diversity affects the fitness benefits of ant visitation for the focal
plant partner. Specifically, we asked:

1. What are the demographic effects of association with alternative partners and how do these effects fluctuate across years?
2. What are the frequency and direction of partner turnover across the plant life cycle?
3. What is the net effect of partner diversity on plant fitness, and what mechanism(s) explain(s) this effect?

We used a hierarchical Bayesian statistical approach to estimate demographic vital rates for hosts in different states of ant occupancy and to quantify state-dependent partner turnover from the long-term data. We then used a stochastic, multi-state integral projection model (IPM) that combines diverse effects on vital rates and pathways of partner turnover to quantify effects of partner diversity on plant fitness.

Methods

Study System

This study was conducted in the Los Piños mountains, a small mountain chain located on the Sevilleta National Wildlife Refuge, a Long-term Ecological Research site (SEV-LTER) in central New Mexico, USA. This is an area characterized by steep, rocky slopes, and perennial vegetation including grasses (*Bouteloua eriopoda* and *B. gracilis*), yuccas, cacti, and junipers. Tree cholla cacti are common in high Chihuahuan desert habitats, with their native range spanning the southwestern USA (Benson, 1982). These arborescent plants produce cylindrical segments with large spines. In the growing season (May to August in New Mexico), the plants initiate new vegetative segments and flower buds at the ends of existing segments. While most plants produce new segments every season, only those which are reproductively mature produce flower buds. Like other EFN-bearing cacti, tree cholla secrete nectar from specialized glands on young vegetative segments and flower buds (Ness et al., 2006; Oliveira et al., 1999). Flower buds produce more

and higher-quality EFN than vegetative segments, making reproductive cholla valuable mutualist
162 partners (Miller, 2014).

Tree cholla EFN is harvested by various ant species. At SEV-LTER, cholla are visited primarily by two species of ground-nesting ants, *Crematogaster opuntiae* and *Liometopum apiculatum*,
165 as well as other rarer species, including *Forelius pruinosus* and unidentified species in the genera *Aphaenogaster* and *Camponotus*. *L. apiculatum* are the most frequent visitors with 25% – 60% of tree cholla tended by these ants, followed by *C. opuntiae* visiting between 5% – 20% of cacti
168 depending on the year (Donald and Miller, 2022). Between 30% – 80% of cacti remain vacant in any given year. Workers of different species rarely co-occur on individual plants, likely due to interspecific competition (Miller, 2007): staged introductions of *C. opuntiae* to *L. apiculatum*-
171 tended plants, and vice versa, provoke aggressive responses by residents (A. Campbell, *personal observation*). In Fall, tree cholla stop producing EFN and the ants vacate until the next growing season.

174 Multiple insect herbivores and seed predators specialize on tree cholla (Mann, 1969). The Cerambycid beetle *Moneilema appressum* and a weevil (Coleoptera: Curculionidae) of the genus *Gerstaekeria* feed on vegetative and reproductive structures as adults and their larvae feed inter-
177 nally. A cactus bug, *Narnia pallidicornis* (Hemiptera: Coreidae), feeds on all cholla parts with a preference for the reproductive structures (Miller et al., 2006). A seed predator, *Cahela ponderosella* (Lepidoptera: Pyralidae), oviposits in open flowers and larvae eat seeds in developing
180 fruits. These predators can have significant negative impacts on plant fitness of and depress population growth (Miller et al., 2009). Prior experiments showed that ant-tended tree cholla experience less herbivory and seed predation than plants from which ants were excluded (Miller,
183 2007; Ohm and Miller, 2014).

Data Collection

This study is based on long-term demographic data spanning 2004 to 2023 at SEV-LTER. From
186 2004 to 2008, we censused 134 plants distributed across three spatial blocks. This initial census

group was discontinued in 2009, when we established six 30×30 -meter plots and tagged all tree cholla within those plots. Two additional 30×30 -meter plots were added in 2011, and this group of eight plots has since been censused annually through 2023 (with the exception of 2020 due to the pandemic shutdown). For all plants, in May or early June of each year we recorded plant survival since the last survey and, for survivors, we recorded height (cm), maximum crown width (cm), and crown width perpendicular to the maximum (cm). Size measurements were used to calculate plant volume (cm^3) based on the volume of an elliptical cone. We measured reproduction as counts of viable and aborted flowerbuds. We recorded the ant species present (or vacancy if no ants present). Occurrences of more than one ant species on one plant were rare (less than 5% of observations), and for the purpose of this analysis we classified the plant as being occupied by the more abundant species. Plots were searched for new recruits each year, and these were added to the census. In total, the data set included 1141 unique individuals and 19 plant-year observations³.

We used additional, smaller data sets from previously published studies to estimate seed and seed bank parameters. Ohm et al. 2014 provide data on the number of seeds per fruit for plants tended by *L. apiculatum*, *C. opuntiae*, or no ants (experimental exclusion), accounting for their effects on pollinator visitation. Elder and Miller 2016 provide data on seed entry to the seed bank and seedling germination and survival rates.

Multi-state Integral Projection Model

Integral Projection Models describe population dynamics in discrete time, with functions that relate vital rates to continuous state variables (Ellner et al., 2016). While IPMs are a natural choice for populations with continuous size structure, they can also be modified to accommodate a combination of continuous and discrete state variables, as we do here. We constructed a stochastic, multi-state IPM that stitches together population structure associated with plant size and ant state, allowing us to determine the individual fitness effects of each ant species and the

³*It is 19 years but the number of plant-year observations should be the total number of rows in the data set*

composite effects of multiple partners, with ant transition dynamics and inter-annual variability modeled explicitly.

Given the low frequency of ant occupancy states other than *L. apiculatum* and *C. opuntiae* (<8% of observations) we combined all other ants into an “other” category, such that our multi-state IPM included four ant states: vacant, *L. apiculatum*, *C. opuntiae*, and Other. The “Other” category was made up of *Forelius pruinus* (3.5% of observations), unidentified species belonging to the genera *Camponotus* (0.9%), *Aphaenogaster* (0.4%), *Myrmecocystus* (0.08%), *Tetramorium* (0.02%), *Brachymyrmex* (0.02%), and additional ants not identified to genus or species (2.8%).

Ant state is included as a predictor variable in IPM sub-models where there are biologically realistic pathways through which ants could impact the outcome of that process. For example, ant partners defend cacti from herbivores, and prior experimental work indicates that ant tending can reduce vegetative tissue loss and floral abortion. Therefore, ant state was included in sub-models for survival, growth, and flowerbud viability. In contrast, we have no reason to expect that ant tending can directly influence the probability of flowering or flowerbud production independently of its influence on plant size, so these sub-models do not include ant state as a predictor variable.

We modeled the tree cholla life cycle using continuously size-structured plants where $n(x, a)_t$ gives the number of plants of size x and ant state a in year t , plus two discrete seed banks (B_t^1 and B_t^2) corresponding to 1 and 2-year old seeds. Seed bank dynamics are given by:

$$B_{t+1}^1 = \delta \sum_{a=1}^A \int_L^U \kappa(a') P(x; \tau^P) F(x; \tau^F) V(a; \tau_a^V) n(x, a)_t dx$$

$$B_{t+1}^2 = (1 - \gamma_1) B_t^1$$

Functions $P(x; \tau^P)$ and $F(x; \tau^F)$ give the probability of flowering in year t and the number of flowerbuds produced in year t , respectively, by plants of size x . The proportion of flowerbuds that remain viable through fruit set ($V(a; \tau_a^V)$) and the number of seeds per fruit ($\kappa(a)$)⁴ is dependent

⁴This is correct but in the equation above it is shown as $\kappa(a')$ – I am flagging that so you can update the equation and check

on ant state a . The vectors $\boldsymbol{\tau}$ give year-specific deviates (mean zero) and appear in functions for which we can estimate temporal stochasticity from the long-term data; superscripts indicate the corresponding vital rate and, when present, the a subscript indicates that deviates are specific to plants in ant state a . For example, temporal deviates $\boldsymbol{\tau}_a^V$ describe better- and worse-than-average years for flowerbud viability and plants in different ant states can fluctuate independently (good years for *L. apiculatum*-occupied plants may not be good years for *C. opuntiae*-occupied plants, for example). Seed production is integrated over the size distribution, from the lower L to upper U size limits, and summed over all possible ant states ($A = 4$) giving total seed production. Seeds are multiplied by the probability of seed dispersal and survival (δ) to give the number of seeds that enter the one-year old seed bank. Plants can recruit out of the year-one seed bank with probability γ_1 or transition to the two-year seed bank with a probability of $1 - \gamma_1$. Seeds in the two-year seed bank are assumed to either germinate with probability γ_2 or die.

For the above-ground part of the life cycle, the number of plants of size x' and ant state a' in year $t + 1$ ($n(x', a')_{t+1}$) is given by survival/growth transitions from size x and ant state a in year t , plus germination out of the seed banks:

$$n(x', a')_{t+1} = (\gamma_1 B_t^1 + \gamma_2 B_t^2) \eta(x') \omega \rho_0(a') + \sum_{a=1}^A \int_L^U S(x, a; \boldsymbol{\tau}_a^S) G(x', x, a; \boldsymbol{\tau}_a^G) \rho(x, a, a'; \boldsymbol{\tau}^\epsilon) n(x, a)_t dx$$

The first term in Eq. ⁵ estimates the number of individuals recruiting from a one or two-year seed bank to a plant of size x' and ant state a' based on the recruit size distribution $\eta(x')$ and the probability of seedling survival (ω) from germination (late summer) to the census (May). This term is multiplied by $\rho_0(a')$, which gives the probability that a new recruit has ant state a' at its first appearance in our census ($\sum \rho_0(a') = 1$). The second term represents all possible transitions from size x and ant a to size x' and ant a' , conditioned on survival. Survival ($S(x, a; \boldsymbol{\tau}_a^S)$) and

that the code is consistent.

⁵We should label equations. I am not sure why the equation label is not working here and I did not try to figure it out. It is probably something with the linenomath formatting.

growth from size x to x' ($G(x', x, a; \tau_a^G)$) are both dependent on initial size and ant state. As above, these functions include inter-annual variability through year-specific deviates that can vary by ant state (τ_a). Finally, ant transition function $\rho(a', a, x; \tau^\rho)$ gives the probability that an individual transitions from ant state a to a' in the next census, conditional on initial size x . This function includes inter-annual variability through year-specific intercepts which are consistent across ant states (τ^ρ).

Statistical modeling and parameter estimation

We parameterized the IPM using a series of generalized linear mixed models in a hierarchical Bayesian framework. Vital rate models included spatial and temporal random effects associated with plot and year variation, respectively (only year variation is used in the IPM), and included plant size ($\log(\text{cm}^3)$; x, x'), ant partner state (a, a'), or both as fixed-effect predictor variables. In addition to vital rate models describing plant demographic performance, we also fit a sub-model to predict transitions between ant states conditional on plant size and previous ant state. As in the IPM, our statistical modeling assumed that demographic effects of ant occupancy are limited to survival, growth, and flowerbud viability.

Growth. We fit the growth sub-model ($G(x', x, a; \tau_a^G)$) to data on size in year $t + 1$ (y^G) using the skewed normal distribution to account left-skewed size transitions:

$$y_i^G \sim \text{SkewedNormal}(\hat{G}_i, \sigma_i, \alpha_i)$$

$$\hat{G}_i = \beta_{a[i]}^0 + \beta_{a[i]}^1 x_i + \beta_{a[i]}^2 x_i^2 + u_{\text{year}[i], a[i]} + w_{\text{plot}[i]}$$

The **mean**⁶ of the i th observation \hat{G}_i is a second-order polynomial with ant-size interactions because preliminary analysis found this was an improvement over a linear relationship. The year- and ant-specific random effect u (which parameterizes the τ_a^G vector) and plot-specific random

⁶I rewrote this for the skewed normal but I cannot remember if the location parameter is the mean, so you should double check this.

effect w are normally distributed with variances σ_{year}^2 and σ_{plot}^2 , respectively. Parameters σ_i and α_i control residual variance and skewness, respectively, and were defined as linear functions of initial size x_i (σ_i is strictly positive and was modeled with a log link function).

Survival. The survival sub-model ($S(a, x; \tau_a^S)$) estimates the probability of survival from year t to year $t + 1$, with fixed effects of size x and ant partner a in year t . We fit this model to the survival data (alive or dead) using a Bernoulli distribution and the logit link function, with a similar linear predictor as the growth model but without the second-order influence of size.

Reproduction. The flowering sub-model ($P(x; \tau^P)$) estimates the probability of reproducing in year t , with fixed effects for the size x and random effects of plot and year. We fit this model to the reproductive status data (vegetative or flowering) using a Bernoulli distribution and a logit link function, similar to the survival model above but with no ant effects. The flower bud function $F(x; \tau^F)$ estimates the total flowers produced by a reproducing plant in year t , with fixed effects of size x . We fit this model to flowerbud count data (sum of viable and aborted buds) using a zero-truncated negative binomial distribution with a log link and normally distributed year and plot random effects.

The flowerbud viability sub-model ($V(a; \tau_a^V)$) estimates the proportion of flowers produced by a plant that are viable (not aborted) in year $t + 1$, with fixed effects of ant partner a in year t ⁷. We fit this model to floral abortion data⁸ using a binomial distribution where trials and successes are given by the total number of flower buds and the number that are viable, respectively. This model used a logit link function and included random effects for plot and year following the same structure as the growth and survival models.

Additional reproductive parameters for the number of seeds per fruit⁹, probability of entry to the seed bank, germination rates, and recruit size were estimated following methods described

⁷The way this is written here is not correct. Viability in year t should be a function of ants in year t . I would double check that this is what the model is actually doing.

⁸The way this is written it's unclear whether you are modeling probability of viability or probability of abortion

⁹We need to briefly explain that this was any-specific, where those values come from, and how we deal with Other.

in Appendix XX.

Ant Transitions. The ant transition model ($\epsilon(x, a, a'; \tau^\epsilon)$) estimates the probability of a cactus being occupied by ant partner a' in year $t + 1$, with fixed effects of the previous size x and the previous ant partner a in year t . We fit this model to ant partner data using a multinomial distribution with a logit link function and random effects for plot and year.

Parameter estimation. We fit models using Markov chain Monte Carlo (MCMC) simulations via STAN run through version 4.0.2 of R R Core Team (2023); Stan Development Team (2023). We used vague priors for all parameters. For each model, we obtained three chains of 10,000 iterations, discarding the first 1,500 iterations. We visually assessed parameter convergence between and within chains (Figures 1 – 7 b) and assessed overall model fit with posterior predictive checks to examine how well the fitted model can generate simulated data similar to the real data (Figures 1 – 7 a).

IPM Analysis

Analyzing an IPM requires discretizing the continuous IPM kernel into an approximating matrix. Size variable x is discretized into b bins, resulting in a $b \times b$ matrix. In our model there is additional complexity in the form of transitions between A ant partners and two additional discrete states (year one and year two seed banks), leading to a matrix size of $A(b + 2) \times A(b + 2)$. We used $b = 200$ bins (sufficient for numerically stable model outputs) and extended the integration limits beyond the minimum (L) and maximum (U) observed sizes to avoid unintentional eviction Williams et al. (2012).

For stochastic analyses, we estimated the approximating matrix corresponding to each t to $t + 1$ transition year. To estimate population mean fitness in a stochastic environment (λ_S) we simulated population dynamics for 500 years by randomly sampling among the 19¹⁰ annual

¹⁰Is this right? The number of transition matrices should be one fewer than then number of years, but I don't remember what happens with 2020.

transition matrices, discarding the first 100 years of the simulation to minimize the influence of
 327 initial conditions. Sampling observed transition matrices (rather than independently sampling
 regression coefficients) produces models that realistically capture inter-annual variation by pre-
 serving correlations between vital rates Metcalf et al. (2015). We tallied the total population size
 330 at each time step as $N_t = B_t^1 + B_t^2 + \sum_{a=1}^A \int n(x, a)_t dx$ and calculated the stochastic growth rate as
 $\log(\lambda_S) = E[\log(\frac{N_t}{N_{t+1}})]$?. We propagated uncertainty from the vital rate models using 1000 draws
 from the joint posterior distribution of model parameters, resulting in a posterior distribution of
 333 λ_S and other derived quantities.

Partner diversity experiments

Using the fully parameterized multi-state IPM, we conducted simulation “experiments” to quan-
 336 tify how diversity and identity of ant partners influenced plant fitness (λ_S). From the fullest
 version of the model corresponding to the observed assemblage of partners, we created subsets
 corresponding to all eight possible scenarios of diversity and composition: no ant partners (com-
 339 plete vacancy); one ant partner (*C. opuntiae* only, *L. apiculatum* only, Other only); two partners
 (all pairwise combinations of *C. opuntiae*, *L. apiculatum*, and Other); and three partners (observed
 scenario of all ant states). These simulation experiments were made possible by extrapolating
 342 ant-specific demographic performance across the size distribution, even for combinations of size
 and ant occupancy that were rarely observed. For example, the no-partner simulation scenario
 modeled a hypothetically ant-free cactus population, even though no such population exists to
 345 our knowledge, by applying the statistical knowledge gleaned from vacant plants (which were
 mostly small and non-reproductive) across the size distribution.

In all scenarios that included any ant partners, we preserved the observed pattern of size-
 348 dependent vacancy/occupancy (estimated through the ant transition sub-model) and manipu-
 lated partner identity conditional on occupancy. This means, for example, that the *C. opun-*
tiae-only scenario included two possible states, vacancy and occupied by *C. opuntiae*. Small,
 351 non-reproductive plants are typically vacant because they do not produce extrafloral nectar, and

once plants begin producing nectar they are nearly always ant-tended (Miller, 2014). Our simulation experiments preserved this basic biology, avoiding tiny ant-occupied plants that do not
354 and could not occur in nature.

Temporal stochasticity experiments

Under the portfolio effect hypothesis, partner diversity may confer a fitness advantage when the
357 benefits of alternative partners are not perfectly synchronized across temporal environmental variation, yielding an advantage of a diverse “portfolio” of partners when the environment fluctuates. Our statistical estimation of ant-specific year random effects in the vital rates allows for
360 this possibility. We constructed two versions of the stochastic, multi-state IPMs that allowed us to test this hypothesis by exploring two different scenarios of environmental variation. First, we evaluated the model using empirical estimates for the τ_a vectors that describe ant-specific year
363 deviates. In this scenario, good years and bad years can differ between ant states, according to the empirical parameter estimates. *We also quantified from the fitted random effects how tightly inter-annual variation was correlated between ant states.*¹¹ Second, we *re-fit*¹² the ant-dependent
366 vital rates (survival, growth, flowerbud viability) without ant-specific year random effects, thus assuming that plants in all ant states fluctuated synchronously in response to temporal environmental variation. We evaluated a second, “synchronized” version of the model that effectively
369 turns off any portfolio effect, holding all else equal. Both scenarios of temporal stochasticity, non-synchronized and synchronized, were run for all eight ant partner scenarios described above.

Statistical inference on fitness consequences of partner identity and diversity

372 The range of models we created generated many outputs; we focus our inference on the following specific contrasts. First, to determine whether ant occupancy and partner diversity are beneficial, we calculated a posterior distribution of λ_S for each of four partner richness levels

¹¹*Worth doing!*

¹²*I think this is correct? The alternative would be to choose one ant state to define the year effects, or perhaps average them.*

375 (zero, one, two, three), averaging over composition scenarios within each level. Second, to determine whether each partner, in isolation, confers a fitness advantage and to rank alternative partners, we contrasted the fitness of each single partner scenario (*C. opuntiae* only, *L. apiculatum* only, Other only) against vacancy (zero partners). Third, to determine whether apparent benefits of diversity are due to the sampling effect or complementarity, we contrasted the fitness of multi-partner scenarios against the single best partner scenario. If the best multi-partner scenarios exceed the fitness associated with the best single partner, this would be interpreted as evidence of complementarity, a true benefit of diversity *per se*. Alternatively, a sampling effect hypothesis predicts that no multi-partner scenario yields higher plant fitness than the best single partner. It is also possible that multi-partner scenarios yield lower fitness than the single best partner, which would be consistent with opportunity costs of diversity. Fourth, to quantify any contribution of the portfolio effect, we contrasted λ_S of the full (three-partner) scenario for synchronized and non-synchronized responses to temporal stochasticity.

We base our inferences on the posterior probability distributions of the contrasts described above. For example, the contrast of *C. opuntiae* with vacancy yields a posterior distribution of the difference in λ_S ($\Delta\lambda_{C-V}$). We can quantify from this distribution our certainty in the effect of *C. opuntiae*, given the data, as $Pr(\Delta\lambda_{C-V} > 0)$. We apply similar logic to other contrasts described above.

393 We can compare the distributions of λ_S in many ways, but have chosen two moments in particular: the means and the proportion of each distribution that is greater than another. To calculate this second moment, we can subtract each λ_S distribution from the others (e.g.¹³ $\lambda_{S,Vacant}$ - $\lambda_{S,C.opuntiae\&Vacant}$) to determine which partner scenario leads to a higher fitness for the cactus population. The proportion of the resulting vector that is greater than zero allows us to give a probabilistic estimate of which combination results in the greatest fitness. The magnitude of this proportion is how we determine the magnitude of difference between the resulting population fitnesses.

¹³This notation may need to be revised somewhat

Using only the λ_S distributions from the stochastic IPM we can determine which scenario leads to the highest fitness, which will tell us if there are benefits to diversity in this system, any other finding indicates that there is quantitative evidence that diversity benefits this system. If the partner scenario which leads to the highest possible population fitness is vacancy, this indicates that there are no benefits to partner diversity. If all of the highest scenarios include a common ant partner, this indicates that there is a single best partner. This quantitative finding that one particular partner leads to all highest possible population fitnesses is evidence that sampling effect explains the benefits of partner diversity. If the highest scenario includes all possible ant partners, this indicates there is a synergy which occurs when all partners interact. This quantitative finding indicates that complementarity is the mechanism which explains the benefits of partner diversity in this system.

Using the λ_S distribution and the λ_{SN} distribution, from both the stochastic IPM and the stochastic null IPM, we can determine if having multiple partners can buffer the cactus population from environmental variation. The difference in the full partner scenario and vacancy ($\lambda_{S,All} - \lambda_{S,Vacant}$) can be interpreted as the effect of having all partners when each ant species has unique effects on the cacti in response to annual variation. The difference in the full partner scenario and vacancy ($\lambda_{SN,All} - \lambda_{SN,Vacant}$) can be interpreted as the effect of having all partners when each ant species has the same effects on the cacti in response to annual variation. The proportion of the resulting vectors that are greater than 0 allows us to give probabilistic estimates of the effects of partner diversity on the fitness of the cacti in a varying environment under two ant scenarios. These two distributions can again be subtracted ($\lambda_S - \lambda_{SN}$), allowing us to determine the difference in effects of partner diversity in two annually varying scenarios. The proportion of the resulting vector that is greater than 0 gives us a probabilistic estimate of how strongly partner diversity buffers the population from environmental variation when the effects of each partner fluctuate uniquely. This quantitative finding that the effects of partner diversity in the stochastic IPM are greater than those in the stochastic null IPM indicate that portfolio effect can explain some benefits of partner diversity in this system.

Results

What are the demographic effects of association with alternative parnters and how do these effects fluctuate across years?

The demographic effects of alternative ant partners

Growth Model. We found evidence that ant visitation enhances cactus growth and that partner identity can influence the growth trajectory of cholla (Figure 1). Tree cholla experience positive mean growth rates across all partners at small to medium sizes with the highest chances of shrinking occurring at the largest sizes (Figure 1e). Plants with *C. opuntiae* ant partners experience the highest mean growth rates across all but the largest sizes, where they experience comprable growth to the other tended plants (Figure 1a). Plants with *L. apiculatum* ants experience the lowest mean growth rates at the smallest sizes and the second lowest at all other sizes (Figure 1b). Plants with other ants experience the second highest mean growth rates across all but the largest sizes, where they experience the highest growth rates (Figure 1c.) Plants with no partners experience the second lowest growth rates at small sizes, after which they experience the lowest growth rates (Figure 1d).

Using the method of subtracting one size distribution from another we were able to determine how confident we are that the size of cholla visited by one combination of ant partners is greater than another. $G_{Crematogaster} - G_{Vacant}$ returns a vector which is 89% positive, meaning we are 89% confident that when *C. opuntiae* ants are partners the size of the cholla is greater than the size of the cholla with no ant partners. Given the evidence that plants visited by *C. opuntiae*

¹⁴*I focused on several things throughout this rewrite of the methods: I tried to go straight into talking about the stochastic IPM, I focused on explaining rationale for specific numbers better, I tried to update notation to be clearer, and I tried to explain more clearly... not sure if I've accomplished these, let me know*

experience the highest mean growth rates we have reported our confidence that this partner
450 is associated with the highest growth rates below. We are 88% and 70% confident that plants
tended by *C. opuntiae* ants experience higher mean growth rates across sizes than plants tended
by *L. spiculatum* ants or other ants respectively. We are 89%, 65%, and 94% confident that plants
453 with no partners experience lower mean growth rates across all sizes than plants tended by *C.*
opuntiae, *L. apiculatum*, or other ants respectively.

Survival Model. We found evidence that ant visitation enhances the survival of medium to large
456 plants, and that partner identity has a significant impact on survival for smaller plants (Figure
2). Tree cholla experience between 7.7% and 99.9% survival rates depending on their size and
ant partner (Figure 2e). Smaller cacti all have lower survival rates, while larger cacti have higher
459 survival rates, all nearing 100% when they reach their largest observed sizes. Plants with *C.*
opuntiae ants experience the highest mean survival rates across all sizes (Figure 2a). Plants with
L. apiculatum ants experience the lowest mean survival rates when small and the second highest
462 mean survival rates across all other sizes (Figure 2b). Plants with other ants experience the
second lowest mean survival rates across all sizes (Figure 2c). Plants with no partners experience
the second highest survival rates at small sizes, after which they experience the lowest survival
465 rates (Figure 2d).

Using the method of subtracting one survival distribution from another we were able to
determine how confident we are that the survival of cholla visited by one combination of ant
468 partners is more likely than another. $S_{Crematogaster} - S_{Vacant}$ returns a vector which is 82% positive,
meaning we are 82% confident that when *C. opuntiae* ants are partners the survival of the cholla
is more likely than the survival of the cholla with no ant partners. Given the evidence that
471 plants visited by *C. opuntiae* experience the highest mean survival rates we have reported our
confidence that this partner is associated with the highest survival rates below. We are 63%
and 100% confident that plants tended by *C. opuntiae* ants experience higher mean survival rates
474 across all sizes than plants tended by *L. spiculatum* ants or other ants respectively. We are 82%,

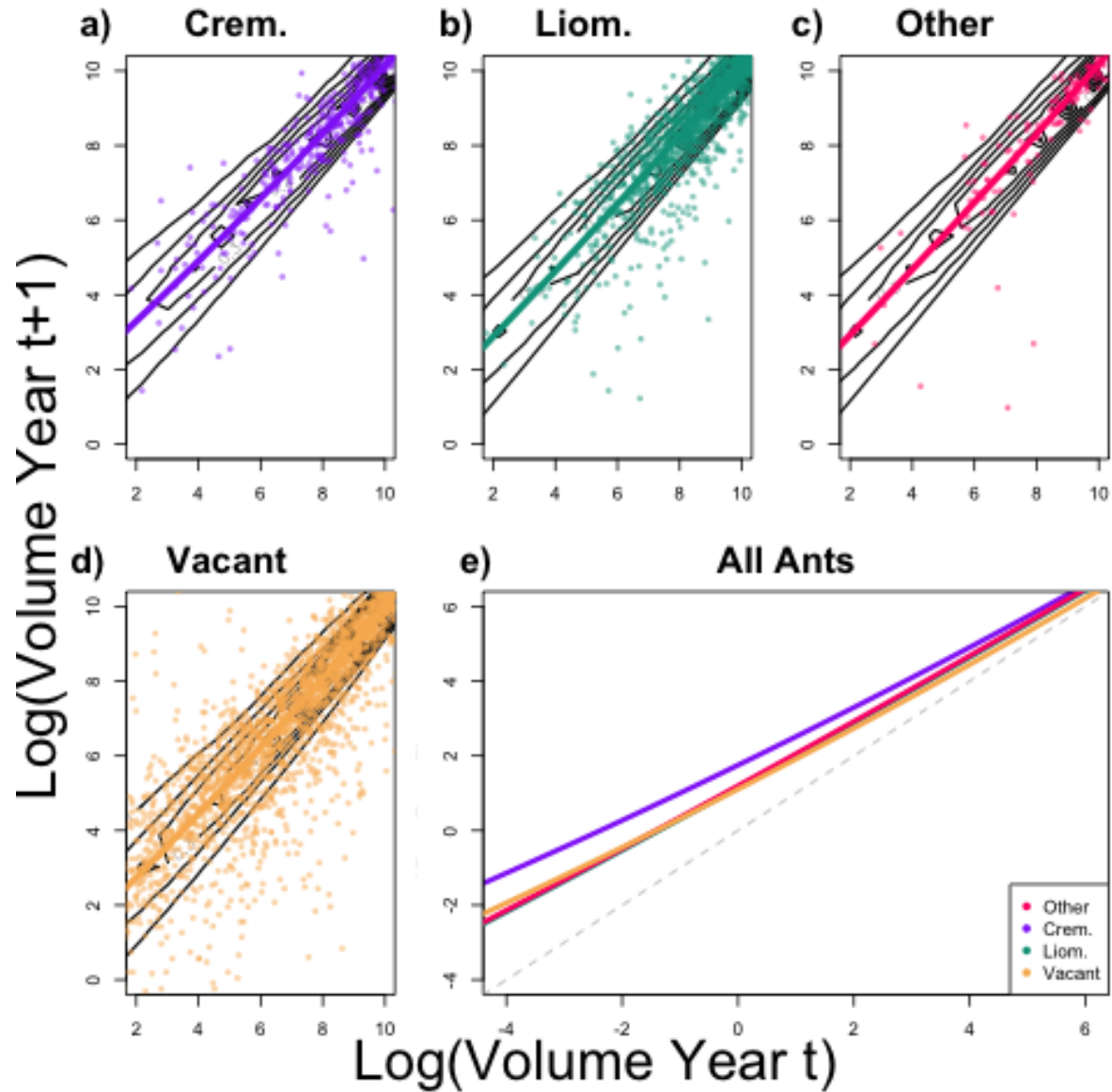


Figure 1: This figure shows the next predicted size of cholla based on previous size with each individual ant partner. The solid colored lines (seen in all panels) are the next mean predicted size of cholla. The points (seen in panels a-d) are the observed data which informs these estimates. The black countour lines (seen in a-d) appear at 5% increments showing where 5%, 10%, etc. of the data is expected to fall. The grey dashed line (in panel e only) shows the line where the next predicted size is the same as the previous (aka there is no growth on this line and below this line is shrinkage).

68%, and 64% confident that plants with no partners experience lower mean survival rates across all sizes than plants tended by

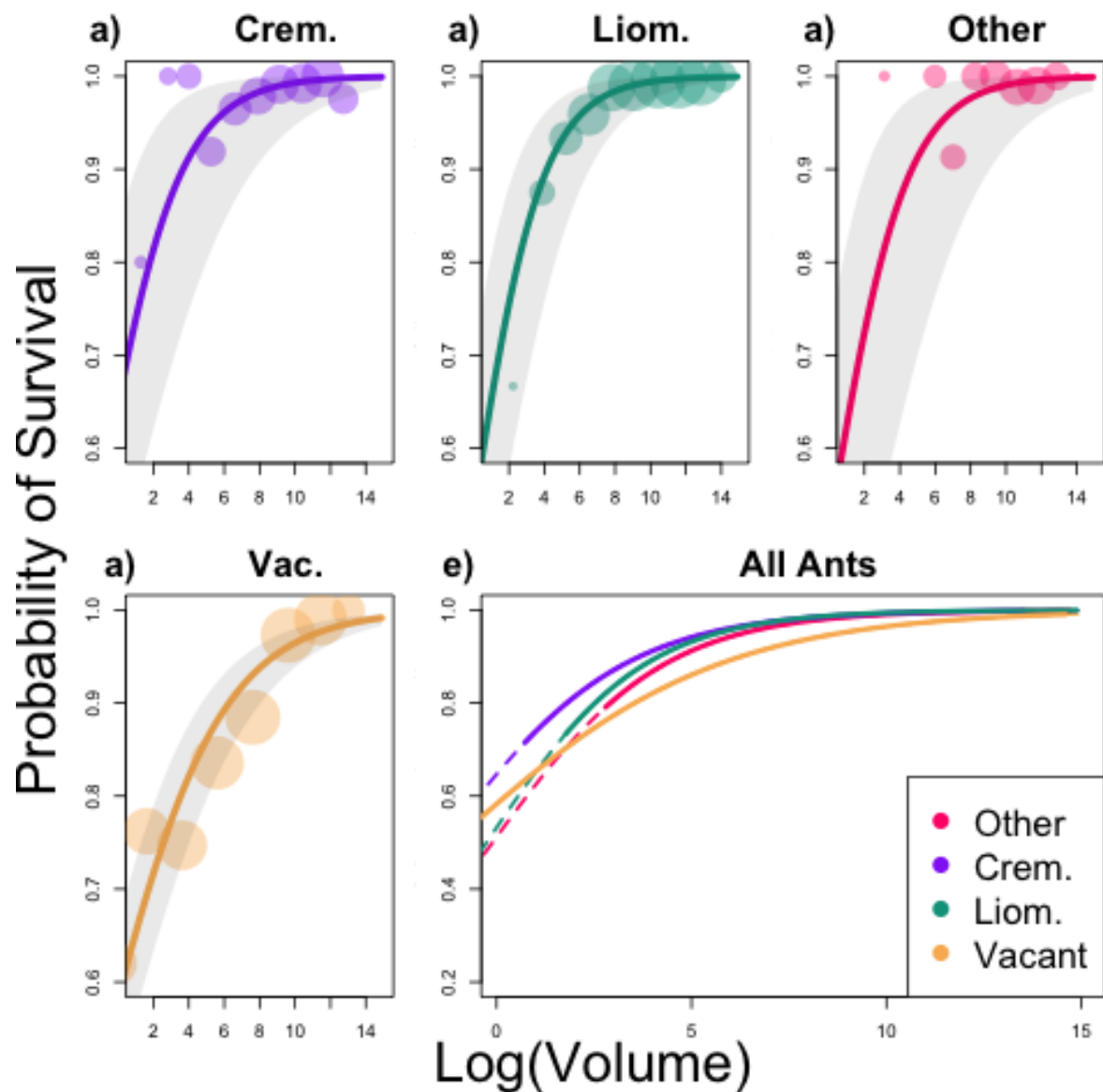


Figure 2: This figure shows the estimated survival rates based on the size of the cactus with each individual ant partner. The solid colored lines (shown on all panels) indicate the mean estimated survival rates. The dashed lines (shown in panel e) indicate extrapolations beyond existing data (where we estimated survival for plants tended by ants where we had never seen a tended cactus of that size). The grey area around the solid lines (shown in panels a-d) show the 90% confidence interval for the estimates. The colored dots are the real data binned by size to show how our estimates align with real survival observations. A larger circle means we had more data on survival of plants of this size with this partner.

477 *Viability Model.* We found evidence that ant visitation leads to increased floral viability rates and
that ant identity can influence the strength of viability. Tree cholla that are reproducing in year t
experience between 39% and 96% viability rates of flowers (Figure ??). The ant partners make a
480 difference in the mean viability rate of flowers, with *L. apiculatum* tended plants experiencing the
highest mean viability rate (at 86%, Figure 3b), followed by other tended plants (at 75%, Figure
3c), *C. opuntiae* tended plants (at 74%, Figure 3a) and vacant plants (at 71%, Figure 3d).

483 Using the method of subtracting one viability distribution from another we were able to
determine how confident we are that the floral viability of cholla visited by one combination of
ant partners is greater than another. $V_{Liomatopum} - V_{Vacant}$ returns a vector which is 99% positive,
486 meaning we are 99% confident that when *L. apiculatum* ants are partners the floral viability of
the cholla is greater than the cholla with no ant partners. Given the evidence that plants visited
by *L. apiculatum* experience the highest viability rates we have reported our confidence that this
489 partner is associated with the highest viability rates below. We are 98% and 97% confident that
L. apiculatum tended plants experience higher viability rates than plants tended by *C. opuntiae*
or other ants respectively. We are 95% and 69% confident that vacant plants experience lower
492 viability rates than plants tended by *C. opuntiae* ants or other ants respectively.

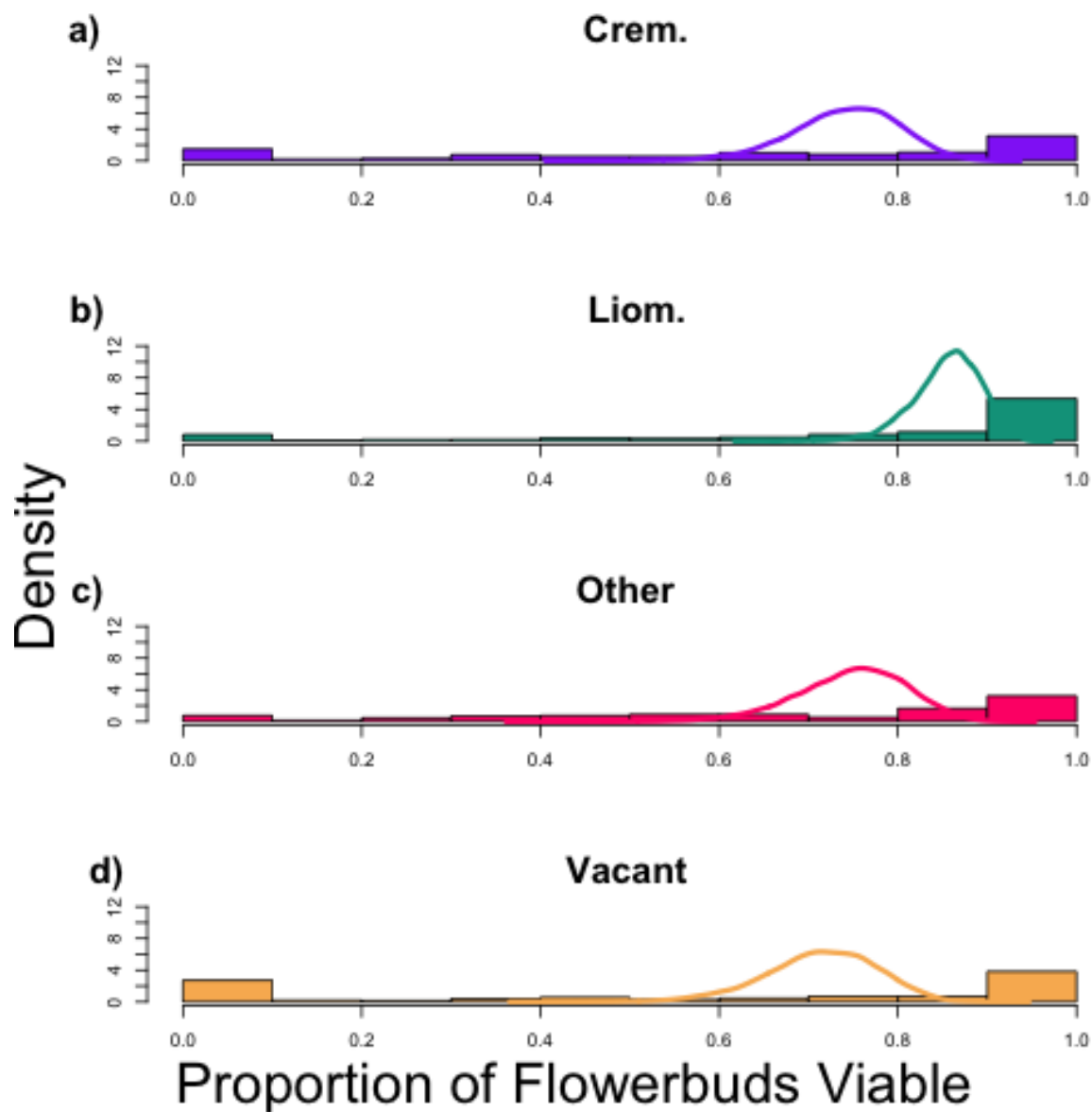


Figure 3: This figure shows the estimated distributions of floral viability rates compared to observed distributions of floral viability rates of cholla based on ant partner identity. The solid lines indicate the estimated viability distribution. The colored histograms represent the observed viability rates of plants with that partner.

The role of annual fluctuations in demographic effects of ant partners

We found evidence that annual variation impacts the effect of ant partner on various demographic traits (Figure 4). The effects of each partner on demographic measure vary uniquely across temporal fluctuations, making partner identity important to track in conjunction with annual variation. Specifically, where some ants offered greater than average benefits in one year, other species offered reduced benefits in the same year, indicating that each ant partner reacts differently to the fluctuating environment.

Each demographic trait was not affected equally by the intersection of ant partner and annual fluctuations. We looked at the mean effect of each ant partner on growth (figure 4a), survival (Figure 4b), and viability (Figure 4c) rates across all the years included in our study. Where the mean effect is exactly 0 there is missing ant data due to variation in censusing focus. This is an indirect way to analyze how temporal fluctuation impacts our system without attributing the effects to a specific climate variables. Where the mean effect is positive, ant presence increases the respective estimated growth, survival, or viability rates in response to environmental fluctuations, and where the mean effect is negative, the opposite occurs. We found the general magnitude of variation was the smallest for the growth rate, meaning annual variation affected the growth of plants the least, followed by survival then viability.

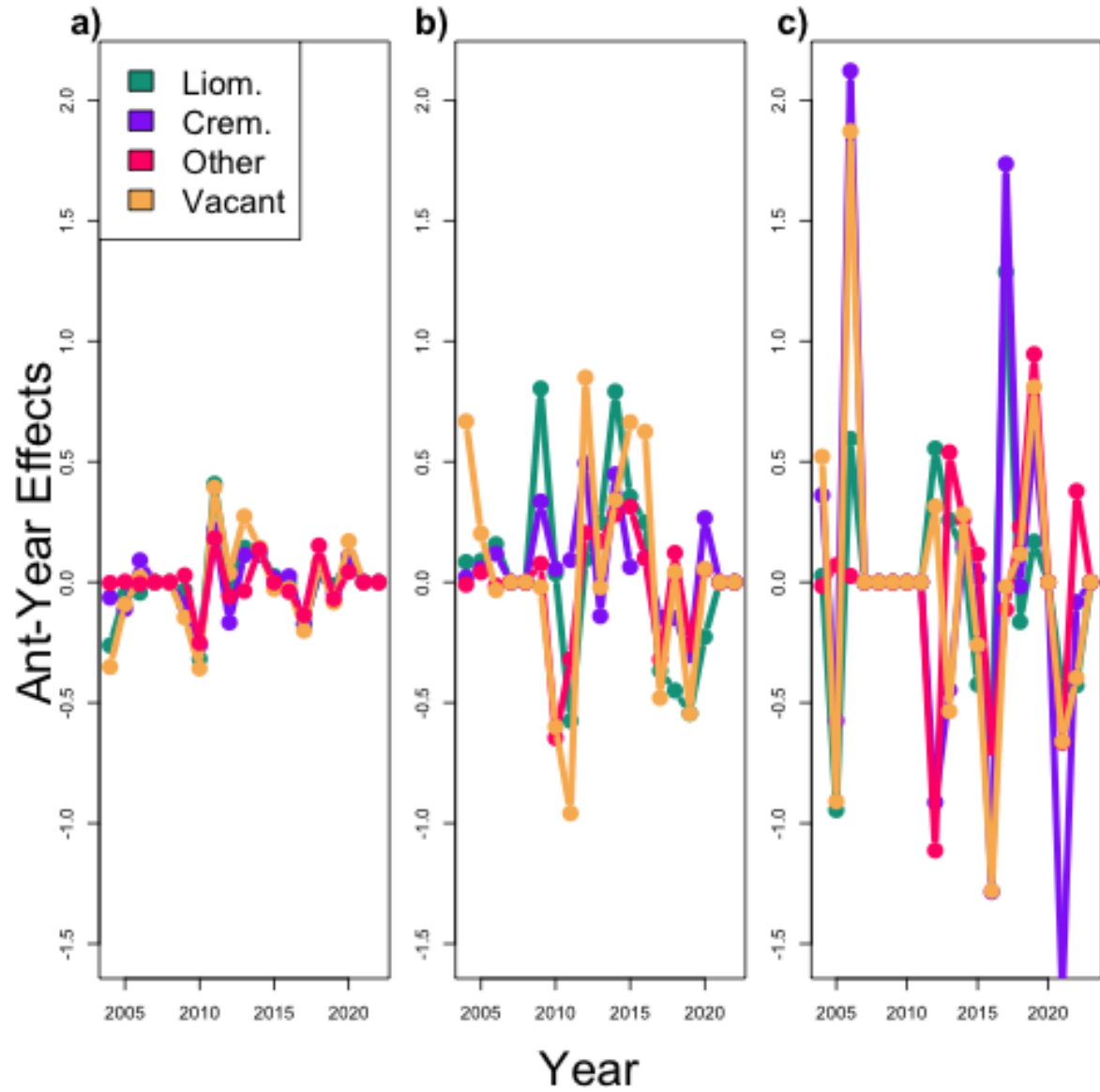


Figure 4: This figure shows the mean affect of each ant partner on a) the estimated next size, b) the estimated survival, and c) the floral viability of cacti across every year of our study. These values are estimated from the fitted random effects of ant and year in our models. Each point represents the mean of the random effect of the identified model, ant, and year (e.g. the lowest dot in panel b) represents the mean effect of vacancy on survival rates in year 2011).

What are the frequency and direction of partner turnover across the plant life cycle?

513 We found that there is a high frequency of partner turnover observed in this system with very distinct directional patterns. Small plants are almost always vacant (Figure 5b-d), if they were previously tended by a partner, they are likely to become vacant again (Figure 5a). As the size
516 of the plants increases, the probability of becoming tended increases as well, though it is not equally likely to be tended by all partners.

L. apiculatum ants become the most likely next partner in the case of most large plants, with
519 the exception of a large plant which was previously tended by *C. opuntiae*. Plants which were previously tended by *C. opuntiae* ants are most likely to remain tended by *C. opuntiae* ants. This indicates that these species may follow the well documented retention-discovery trade off exhib-
522 ited by many ants, with *L. apiculatum* ants excelling at discovery and colonization of new plants and *C. opuntiae* ants excelling at plant retention season after season. The overall frequency of these partners, however is a potential alternative explanation to this discovery-retention trade
525 off. *L. apiculatum* ants are by far the most frequent ant partners, accounting for 75% of the occupied cacti, while *C. opuntiae* and other ants account for 17% and 8% of occupied cacti respectively. This high frequency of *L. apiculatum* ants may lead to the inflation of turnover to *L. apiculatum*
528 from other ants.

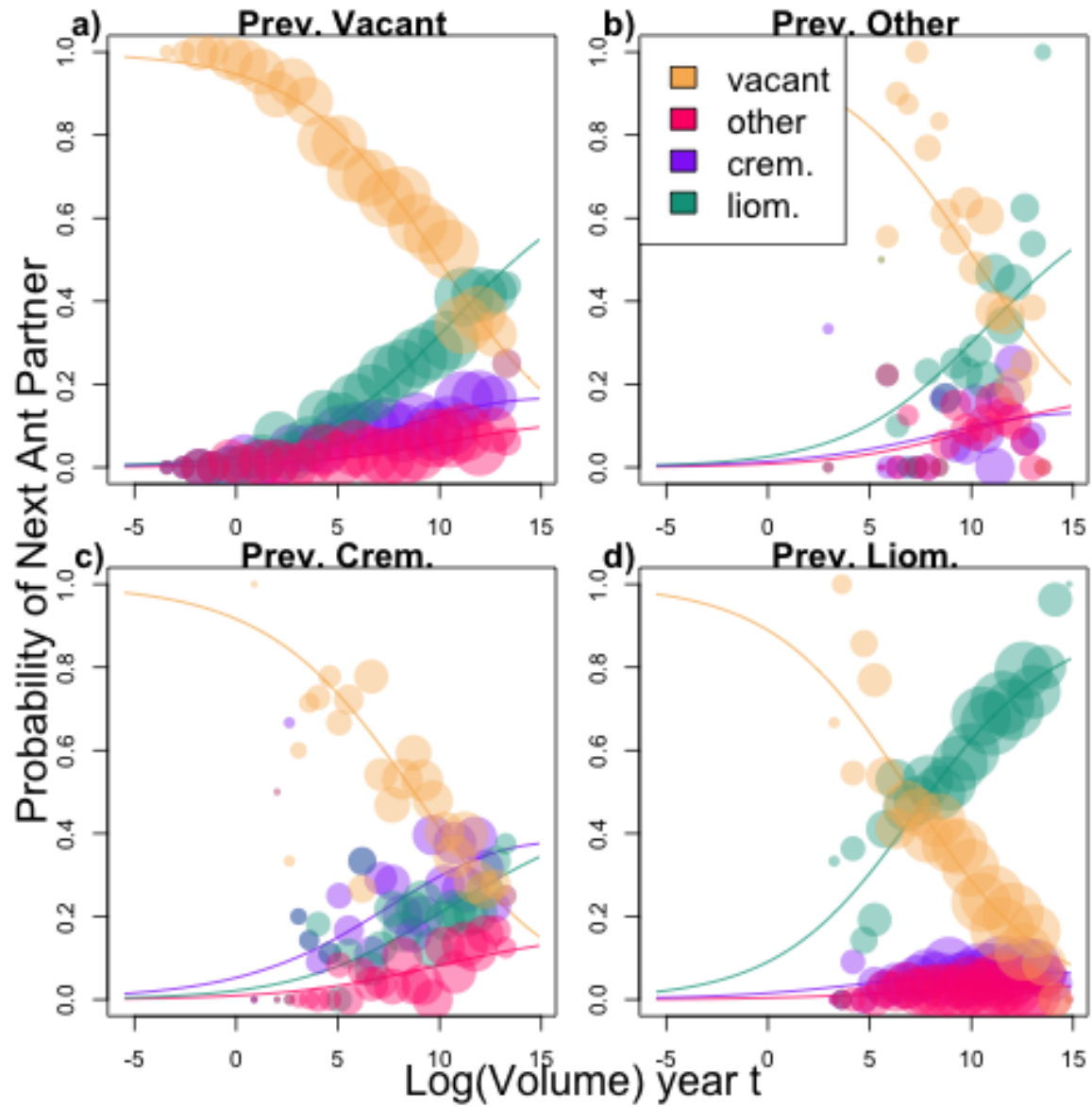


Figure 5: This figure shows the probability of being tended by each ant partner or vacant based on the size of the plant. Each panel shows these probabilities for a different previous ant state. The solid lines represent the mean probability of being tended by a specific partner. The colored points are the real data binned by size to show how our estimates align with real visitation observations. A larger circle means we had more data on visitation of plants of this size with this previous partner.

What is the net effect of partner diversity on plant fitness, and what mechanism(s) explain(s) this effect?

531 We found that partner diversity was beneficial in this system. The lowest mean fitness was $\lambda_{S,Vacant}$, the fitness of the cholla with no partners (Figure 6b). By subtracting the distributions $\lambda_{S,any} - \lambda_{S,Vacant}$, we found that we are between 82% and 100% confident that having any partner
534 leads to a higher population fitness than having no partner. If you consider just the number of partners (ignoring the identity), what you find is actually that the more partners are present, the higher the fitness of the cacti (Figure 6b), though this increase is primarily driven by the presence
537 of *L. apiculatum*.

Despite this apparent synergy, when partner identity was considered, we found the benefits of partner diversity could be explained by Sampling Effect. We believe the benefits of partner
540 diversity are heavily driven by the presence of a single best partner rather than overall synergy. All simulated combinations of ant partners which included *L. apiculatum* were nearly equal and the highest possible fitness estimated for the cholla. This indicates that *L. apiculatum* are the
543 single best partner for the cholla under existing conditions. Based on the definitions of Sampling Effect and Complementarity we use in this study (Batstone, 2018), it is clear that Sampling Effect can explain the benefits of partner diversity in the cholla system.

546 It is possible that this, like the frequency of partner turnover to *L. apiculatum*, is driven by the extreme frequency of *L. apiculatum* ants in comparison to others. With this in mind, we simulated the population fitness with equal probability for transitioning to any ant state. We found
549 from the simulations with different transition probabilities.¹⁶

We found evidence of portfolio effect, meaning the presence of multiple partners did not buffer against the potentially negative effects of annual fluctuations. The effect of all ant partners
552 can be measured as $\lambda_{All} - \lambda_{Vacant}$ (Figure 7). We are 94% confident that when all ants are present the cholla experience higher fitness than when no ants are present according to both the

¹⁶*This feels like the most natural progression to me.*

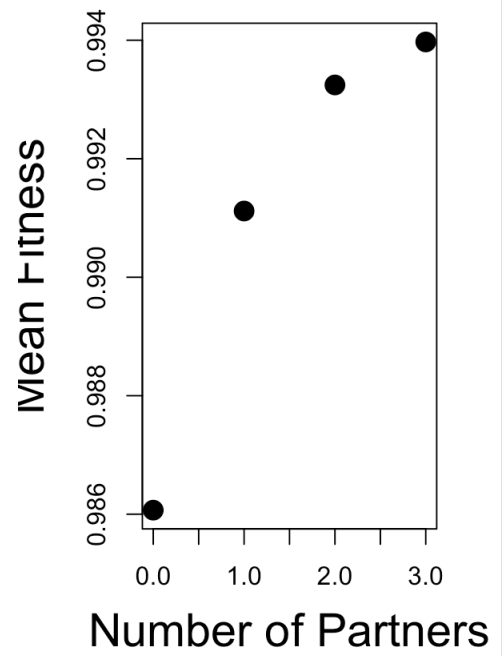
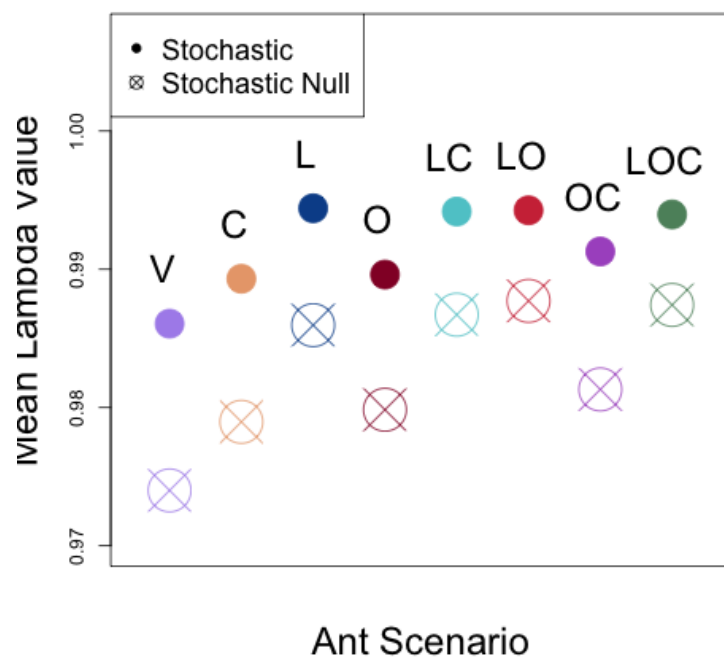


Figure 6: Panel a) shows the mean values of the estimated λ_S (filled in circles) and λ_{SN} (empty circles with an X) for each simulated combination of ant partners. The letters above the points correspond to what ant partners are present (V = Vacant, C = *C. opuntiae*, L = *L. apiculatum*, O = other). Panel b) shows the mean values of the estimated λ_S for

stochastic and stochastic null model. When subtracting these two resulting vectors from each other $((\lambda_{S,All} - \lambda_{S,Vacant}) - (\lambda_{SN,All} - \lambda_{SN,Vacant}))$, we found that we are only 52% confident that partners offer higher benefits when able to respond uniquely to a fluctuating environment. There is no real difference between the two scenarios, meaning we have no evidence of portfolio effect.¹⁷

Discussion

¹⁸ The large, long-lived tree cholla produce EFN which tempts several species of ant partners to protect them from herbivores and seed predators. Many studies have looked at multispecies mutualisms and the how having a variety of partners leads to variation in demographic effects Bascompte (2019); Báez et al. (2016); Ford et al. (2015); Palmer et al. (2010); Stachowicz and Whitlatch (2005). Because these tree cholla interact with only one ant partner at a time, it is a unique system in which to parse out the individual effects of each ant partners, both in isolated settings or in combinations we cannot test in the real world.¹⁹

We asked what effects the partners which interact with tree cholla (*C. opuntiae*, *L. apiculatum*, and more²⁰) have on the vital rates of tree cholla. Using a system of heirarchical bayesian models we found that there were discernable differences in the effects that each partner had on vital processes of the focal mutualist. The different vital rates vary in importance across tree cholla ontogeny. Several of them are negatively impacted by the presence and pressure of herbivores and seed predators Miller et al. (2009, 2006) and positively impacted by the presence of ant partners Miller (2007). The predators and herbivores target new growth and flowers, leading

¹⁷I am not sure if I have explained enough here honestly.

¹⁸I have not commented too heavily here because I would like to talk through what we want this section to achieve. Currently, most of this section is actually describing results, whereas the pupose is to interpret and contextualize results, and connect them to the broader literature. Some of your content here is actually better at describing results than you had in the Results section, because it includes that element of "how is this connected to the question" that was missing from the Results section.

¹⁹This is a good start. In general, I suggest opening the Discussion section with a brief summary of what you were trying to learn in this study, what you found, and its broader significance. This paragraph does a little of that, but I think it can be stronger.

²⁰I would not say this.

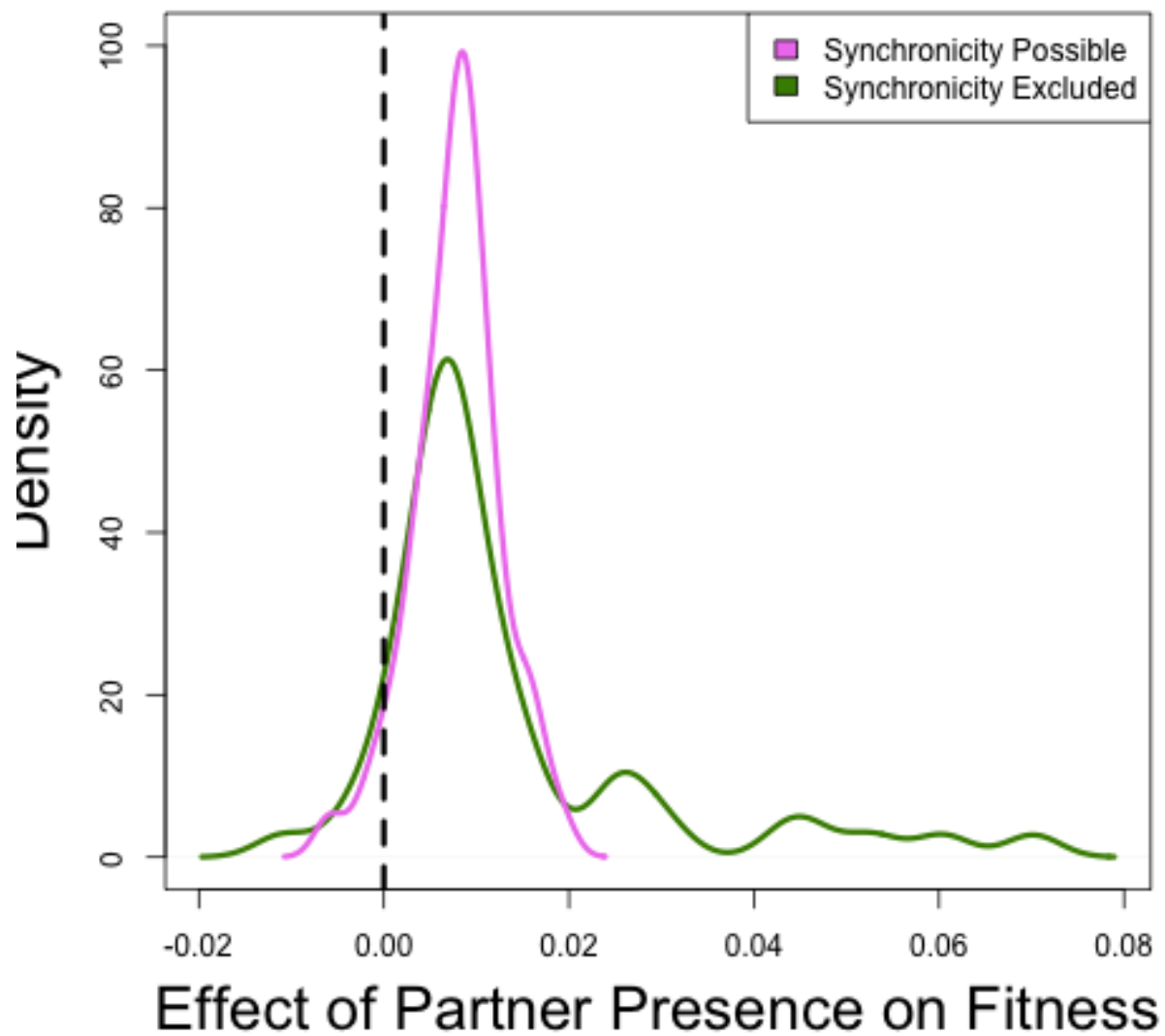


Figure 7: This figure shows the distribution of $\lambda_{S,All} - \lambda_{S,Vacant}$ in pink and $\lambda_{SN,All} - \lambda_{SN,Vacant}$ in green. The vertical dashed line shows where the effect of partners on the fitness of the cholla is 0 (to the left the partners have a negative effect, to the right the partners are beneficial).

573 to negative impacts on the growth rates, survival rates, and floral viability rates of tree cholla
Agrawal (2004); Louda and Potvin (1995). The presence of the ant partners can reduce those
negative effects.

576 It has been previously hypothesized that there is a hierarchy of partners due to the ability for
L. apiculatum ants to defend the cacti from seed predators and herbivores Miller (2007). These
prior results would suggest that all vital rates that are affected by ant partners would be boosted
579 the most by the presence of *L. apiculatum* ants, this is not what we found. Our results suggest
that different partners differ significantly in their effects on vital rates.

Prior to reproduction, the tree cholla experience only growth and survival. *C. opuntiae* tended
582 ants are associated with the highest growth rates and survival rates of plants. This indicates that
C. opuntiae ants may be good ants for pre-reproductive tree cholla plants. Reproducing plants
experience a probability of reproducing, flower production, and floral abortion. **Floral abortion is**
585 **heavily affected by seed predators Miller et al. (2008)²¹**, which the ants defend the cacti, leading
to increased floral viability. We specifically found that tree cholla experienced the highest floral
viability rates when tended by *L. apiculatum* ants. This indicates that *L. apiculatum* ants may be
588 good partners for reproducing plants.

These results together would suggest that complementarity may be the underlying mechanism
that explains why partner diversity is beneficial in this system.

591 We have shown that the identity of partners is important to the processes that define tree
cholla fitness. Now we need to analyze the dynamics of partner turnover which dictate the
identity of tree cholla partners and therefore the effects of vital rates on the tree cholla. With our
594 models we were able to identify both the direction, frequency, and distinct patterns of partner
turnover.

In the literature, it is clear that the frequency of partner turnover can have big effects on
597 the fitness of the focal mutualist Fiala et al. (1994); Horvitz and Schemske (1986); Oliveira et al.
(1999); Sachs et al. (2004). In some systems high frequency of turnover is necessary to resiliency

²¹ *Seed predators do not influence floral abortion.*

and leads to higher fitness benefits Trøjelsgaard et al. (2015), while in other systems loyalty is
the most beneficial Batstone (2018). While the purpose of this paper is not to establish which
would be most beneficial in this system, we were able to identify the pattern. Small plants are
almost entirely vacant in this system until they grow large enough to begin producing significant
amounts of EFN. Our model shows that once they do produce EFN, plants experience a relatively
significant amount of turnover. Mid-sized and large plants which were either vacant or tended
by other ants are most likely to become tended by *L. apiculatum* ants in the next year, thereby
experiencing partner turnover. Plants which were tended by *L. apiculatum* or *C. opuntiae* ants are
most likely to remain tended by the same partners multiple years in a row. This indicates that
C. opuntiae ants and *L. apiculatum* ants are loyal partners which retain the same plants year after
year with regularity.

As established in previous studies, the direction of partner turnover is important when the
identity of partners impacts the quality of benefits recieved Alonso (1998); Dejean et al. (2008);
Fonseca et al. (2003); Noe and Hammerstein (1994). In our study we found that there are distinct
patterns to the direction of partner turnover. Specifically, most plants are tended by *L. apiculatum*
ants at some point, because vacant plants, other tended plants, and *L. apiculatum* tended plants
are all most likely to be tended by *L. apiculatum* ants. This indicates that while *L. apiculatum* ants
are loyal to their own plants and return multiple years in a row to the same ones, they are also
strong colonizers.

The combination of partner identity, partner turnover, and temporal stochasticity gives us the
unique power to consider both the fitness of the tree cholla under different partner scenarios
(as some have done before Palmer et al. (2010)²²) and a unique set of mechanisms (Batstone
(2018)) which explain how the multi-partner interactions lead to fitness differences. We found
that the combination of accurate partner transitions with partner identity²³ affected the fitness of
the tree cholla in interesting and dynamic ways. Namely, a best partner emerged in this analysis,

²²There is more than just the Palmer pape. Be sure that you are comprehensive in your use of the literaure, include non-ant-plant studies,

²³Not sure what this means.

624 which was surprising given the nature of our vital rate findings. The variation in best partner for
each vital rate suggested the potential that the different ant partners had some level of unique
specialty in what they offered, which would support complementarity as the mechanism which
627 explained the effects of partner diversity Stachowicz and Whitlatch (2005); Stanton (2013). The
results of our IPM however differ from this prediction.

Using the stochastic IPM we developed, we found evidence of sampling effect rather than
630 complementarity. We found that *L. apiculatum* was the single best partner, and that all diversity
scenarios where *L. apiculatum* was present resulted in the highest possible fitness of tree cholla.
This indicates that despite the fact that *L. apiculatum* partnership does not result in the highest
633 growth and survival rates, it is still the overall best partner.

Using the stochastic null IPM and the stochastic IPM we compared the fitness boost received
by all ant partners when ants effects varied separately across years and when they did not.
636 When all ants responded to inter-annual variability the same way (shown in the stochastic null
IPM) we found that the fitness boost received from partners was larger than the fitness boost
received when ants responded to inter-annual variability differently. This indicates that having
639 multiple possible partners benefits the tree cholla by buffering the potentially negative effects of
inter-annual variation.

²⁴ This paper shows the importance of long-term datasets in investigating species interactions
642 and calls for further use of long-term data. Previously studies have analyzed how partner identity
and partner turnover impact focal mutualist fitness Barrett et al. (2015); Bruna et al. (2014);
Dejean et al. (2008); Fonseca et al. (2003); Noe and Hammerstein (1994); Trøjelsgaard et al. (2015).
645 Separate studies have analyzed how inter-annual variability impacts focal mutualists Alarcón
et al. (2008); Alonso (1998); Horvitz and Schemske (1990); Lázaro et al. (2022); Ollerton et al.
(2006). The long term dataset we used gave us the unique ability to consider the combined
648 effects of partner identity, partner turnover, and temporal stochasticity.²⁵

²⁴What this all means more broadly?? I'm currently not sure what to do with this. Tom: that's the entire Discussion!

²⁵This is really good. More of this!

This paper has limitations, specifically surrounding the driving forces behind the ant-plant interactions. We revealed the dynamics of partner turnover and showed that different ant partners are correlated with different fitness benefits. As of now, the driving mechanisms behind how ant species come to interact with individual plants is still unknown and could be subject to future work.²⁶

Acknowledgments

This should be drafted.

Data and Code Availability

This should be drafted.

Appendix A: Additional Methods and Parameters

Seeds Per Fruit. With dataMiller et al. (2006), we fit a model for the number of seeds produced by every fruit on a cholla ($\kappa(a')$) in year $t + 1$ based on the ant partner a' in year $t + 1$. We fit this model to seed data y^κ using a Negative Binomial distribution and the log link function:

$$y^\kappa \sim \text{NegativeBinomial}(\hat{\kappa}, \hat{\phi})$$

$$\hat{\phi} = \beta_0^\phi$$

The data used for this model did not include data on ants in the “other” category, so we used the data from vacant plants to parameterize seeds per flower for plants with “other” ants in the IPM.

²⁶*This feels a little weak and incomplete.*

Recruit Size Distribution. We fit this model to recruit size data y^η using a Normal distribution with the identity link function:

$$y^\eta \sim N(\hat{\eta}, \hat{\sigma})$$

where $\hat{\sigma}$ is estimated with a non-informative prior.

Germination. With germination data Miller (2007), we fit two models for the probability of germinating from the first year seedbank (γ_1) or the second year seedbank (γ_2) in year $t + 1$, with no fixed or random effects. These models were fit to germination data $y^{\gamma_1}, y^{\gamma_2}$ using the binomial distribution with logit link functions:

$$y^{\gamma_1} \sim \text{Binomial}(\hat{\gamma}_1)$$

$$y^{\gamma_2} \sim \text{Binomial}(\hat{\gamma}_2)$$

Pre-Census Survival. With recruit census data Miller et al. (2006), we fit a model for the probability of a seedling (which germinates in early Fall) surviving to when we census in May (δ) of year $t + 1$ (accounting for missed mortality events), with fixed effects of the previous size x and random effects of the transect m . We fit this model to pre-census survival data y^δ using a Bernoulli distribution with a logit link function:

$$y^\delta \sim \text{Bern}(\hat{\delta})$$

663 where $m \sim N(0, \sigma_{\text{transect}}^2)$ is the random effect of transect where the recruited individual was analyzed for survival.

This is not referenced in the paper, to my knowledge, and I think you need to think more
666 deeply about what content should go into appendices and why.

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831

Tables

Figure legends

Supplementary Materials

834

Herbivory Data

Model Checks

For each model fitted, we conducted two tests to determining if the fit was acceptable to use in
 837 our IPM. First, we checked the convergence of each parameter. Below we show the convergence
 of all β terms listed in the Statistical Modeling subsection of Methods. Second, we checked the
 posterior fit, comparing the estimated values of each model to the y values of the actual data. We
 840 show these posterior checks below, split by ant partner where relevant.

Statistical Models – Results

Below are the results reorted of all statistical models not described in the main body of the text.

843 *Reproduction Model.* The probability of a plant reproducing in a given year is highly size de-
 pendent. The mean probability of reproducing remains at about 0% until the plant reaches a
 medium size, after which the mean probability of reproducing increases steadily before reaching
 846 about 100% at large sizes.

Seeds Per Flower Model. Each viable flower on a plant produces between 97 and 257 seeds. This
 number is affected by the ant partner present. *C. opuntiae* tended plants produce a mean of 148
 849 seeds per flower. *L. apiculatum* tended plants produce a mean of 149 seeds per flower. ²⁷ Vacant

²⁷These results are not consistent with Ohm and Miller, where *Crem* had lower seeds than *Liom*. I would check this. This
 section should also reference that paper because these are not new results.

Parameter	Median (95% CI)	Prior Distribution
growth xi intercept vacant β_{01}^g	-5.210899(-5.686865, -5.491787)	sDE
growth xi intercept other β_{02}^g	-5.8288(-5.956217, 1.766021)	asdf
growth xi intercept <i>C. opuntiae</i> β_{03}^g	-4.529523(-6.0770390, 0.1222112)	asdf
growth xi intercept <i>L. apiculatum</i> β_{04}^g	-5.106802(-5.4499944, 0.5453901)	asdf
growth xi size dependent vacant β_{11}^g	asdf	asdf
growth xi size dependent other β_{12}^g	asdf	asdf
growth xi size dependent <i>C. opuntiae</i> β_{13}^g	asdf	asdf
growth xi size dependent <i>L. apiculatum</i> β_{14}^g	sadf	asdf
growth omega intercept ω_0^g		
growth omega size dependent ω_1^g		
growth alpha intercept α_0^g		
growth alpha size dependent α_1^g		
1-year germination intercept α^{γ_1}		
2-year germination intercept α^{γ_2}		
survival intercept vacant β_{01}^s		
survival intercept other β_{02}^s		
survival intercept <i>C. opuntiae</i> β_{03}^s		
survival intercept <i>L. apiculatum</i> β_{04}^s		
survival size dependent vacant β_{11}^s		
survival size dependent other β_{12}^s		
survival size dependent <i>C. opuntiae</i> β_{13}^s		
survival size dependent <i>L. apiculatum</i> β_{14}^s		
flowering intercept β_0^f		
flowering size dependent β_1^f		
viability intercept vacant β_{01}^v		
viability intercept other β_{02}^v		
viability intercept <i>C. opuntiae</i> β_{03}^v		
viability intercept <i>L. apiculatum</i> β_{04}^v	48	

Table 1: This table includes the median estimates, the 95% confidence intervals, and the prior distribution for each parameter in each model.

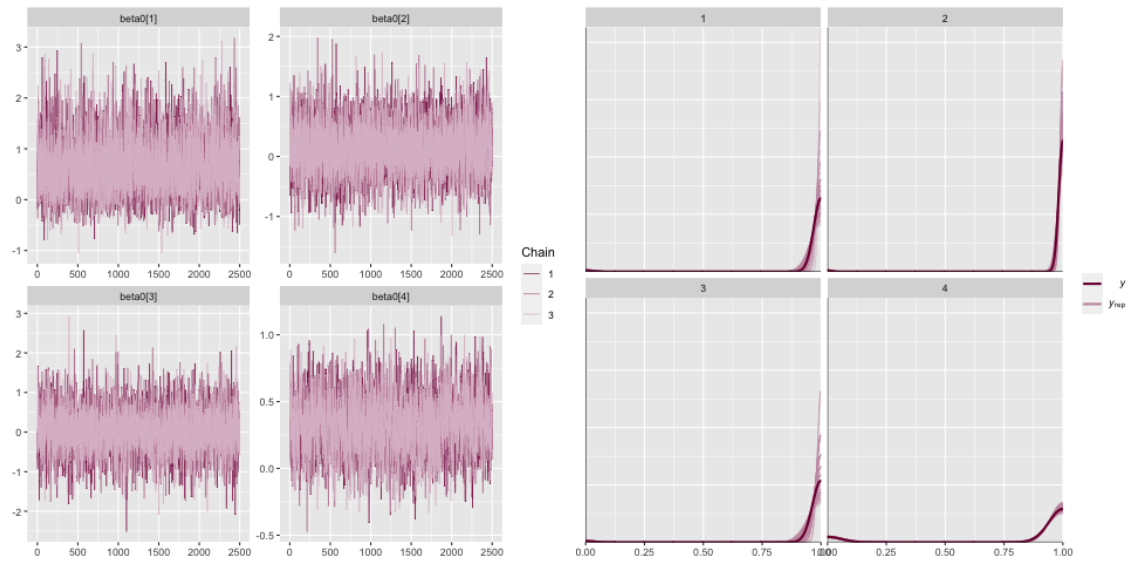


Figure 1: The a) posterior convergence of the parameters estimated by the survival model and the b) posterior distribution of survival estimates (pink lines) for each ant species (1 = *C. opuntiae*, 2 = *L. apiculatum*, 3 = other, 4 = vacant) compared to the mean survival distribution (black line) of the real data.

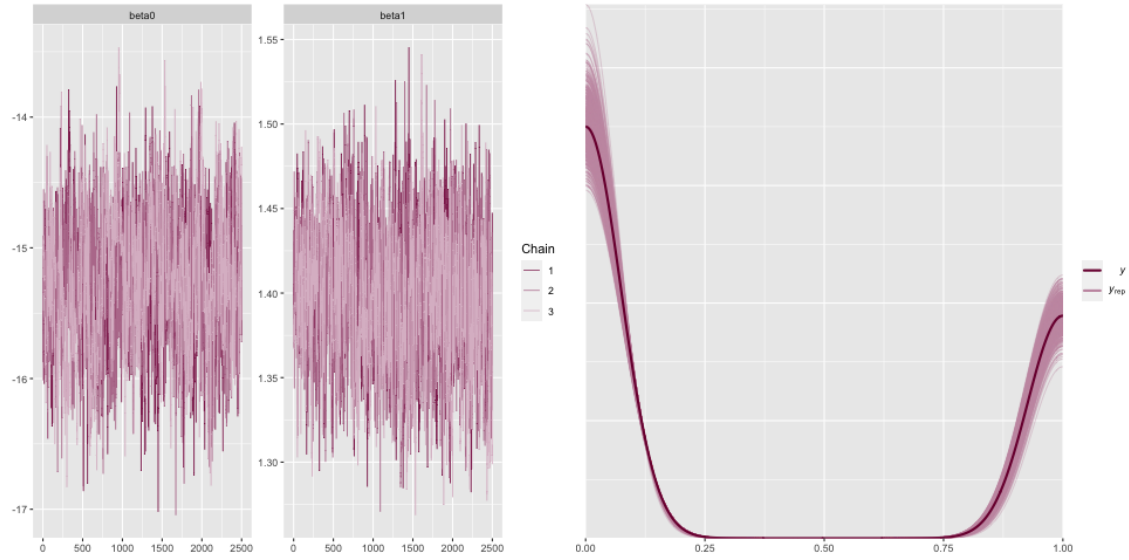


Figure 2: The a) posterior convergence of the parameters estimated by the reproduction model and the b) posterior distribution of reproductive status estimates (pink lines) for each ant species (1 = *C. opuntiae*, 2 = *L. apiculatum*, 3 = other, 4 = vacant) compared to the mean reproductive status distribution (black line) of the real data.

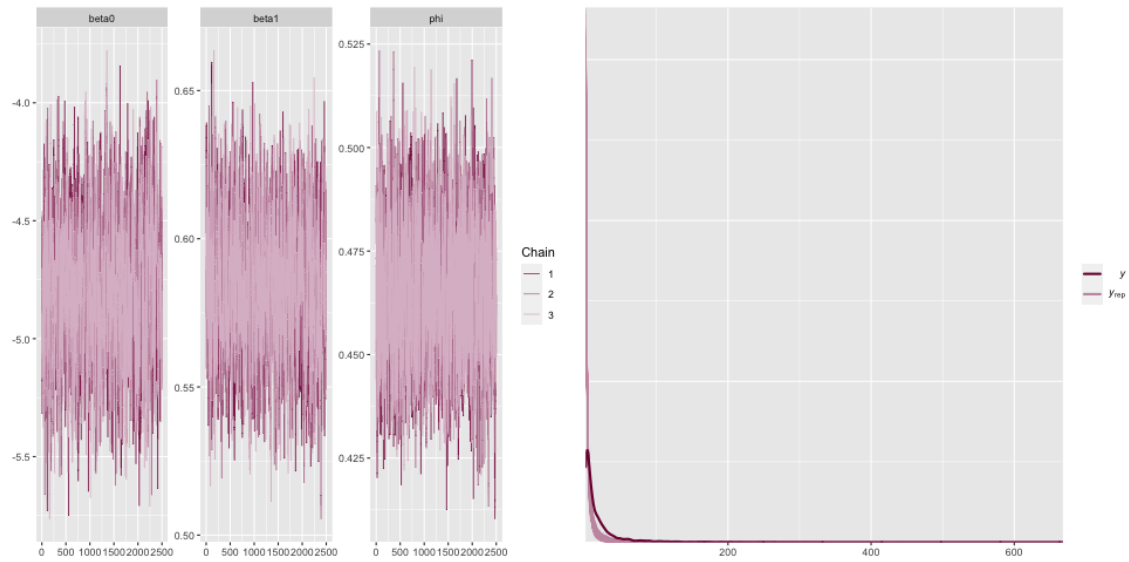


Figure 3: The a) posterior convergence of the parameters estimated by the number of flowers model and the b) posterior distribution of the number of flowers estimated (pink lines) compared to the mean distribution of observed flowers (black line).

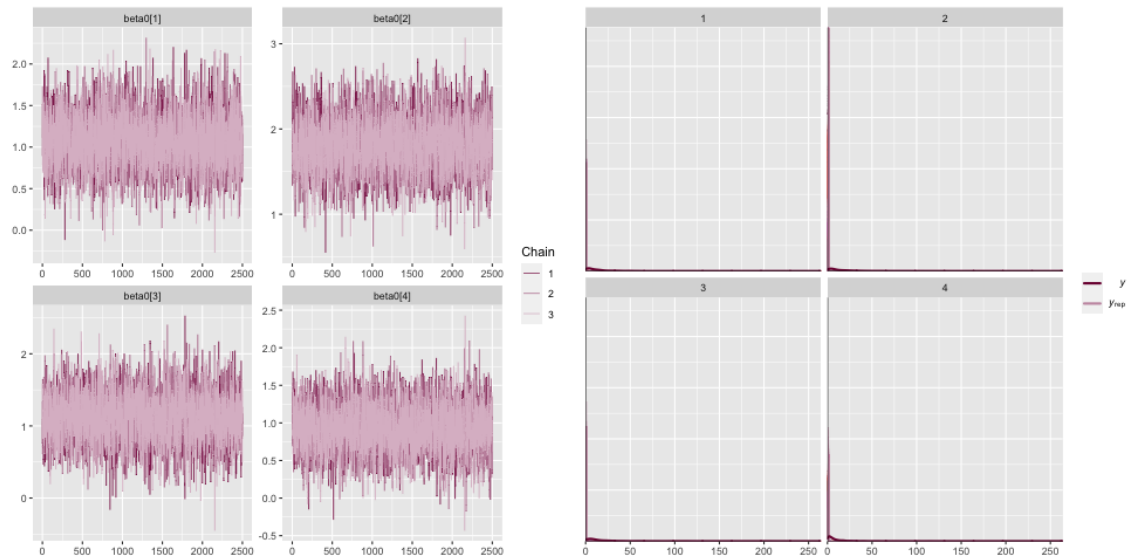


Figure 4: The a) posterior convergence of the parameters estimated by the viability model and the b) posterior distributions of floral viability estimates (pink lines) for each ant species (1 = *C. opuntiae*, 2 = *L. apiculatum*, 3 = other, 4 = vacant) compared to the mean floral viability distribution (black line) of the real data.

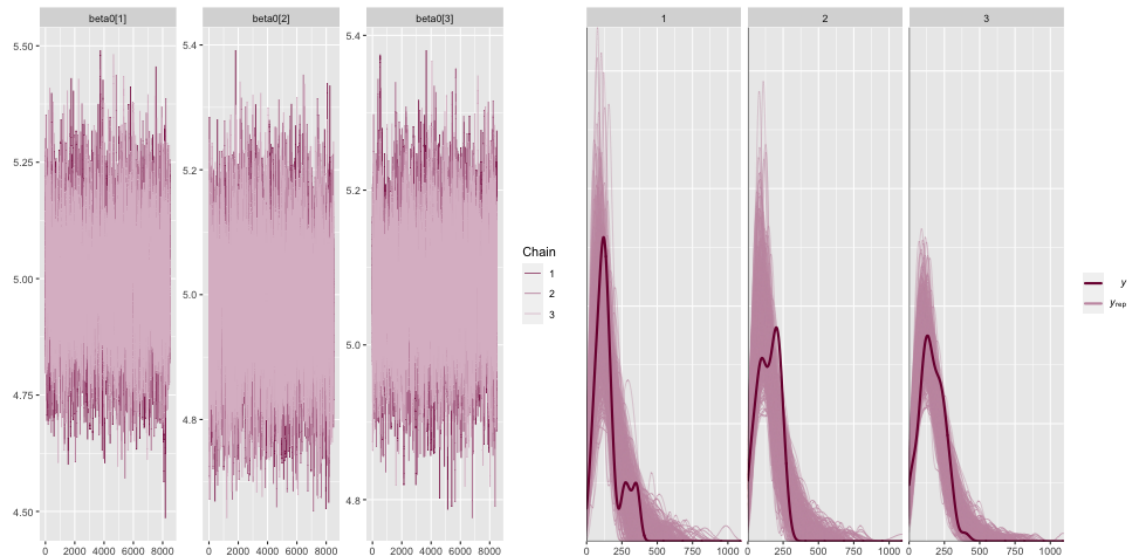


Figure 5: The a) posterior convergence of the parameters estimated by the seeds per fruit model and the b) posterior distributions of seeds per fruit estimates (pink lines) for each ant species (1 = *C. opuntiae*, 2 = *L. apiculatum*, 3 = vacant) compared to the mean seeds per fruit distribution (black line) of the real data.

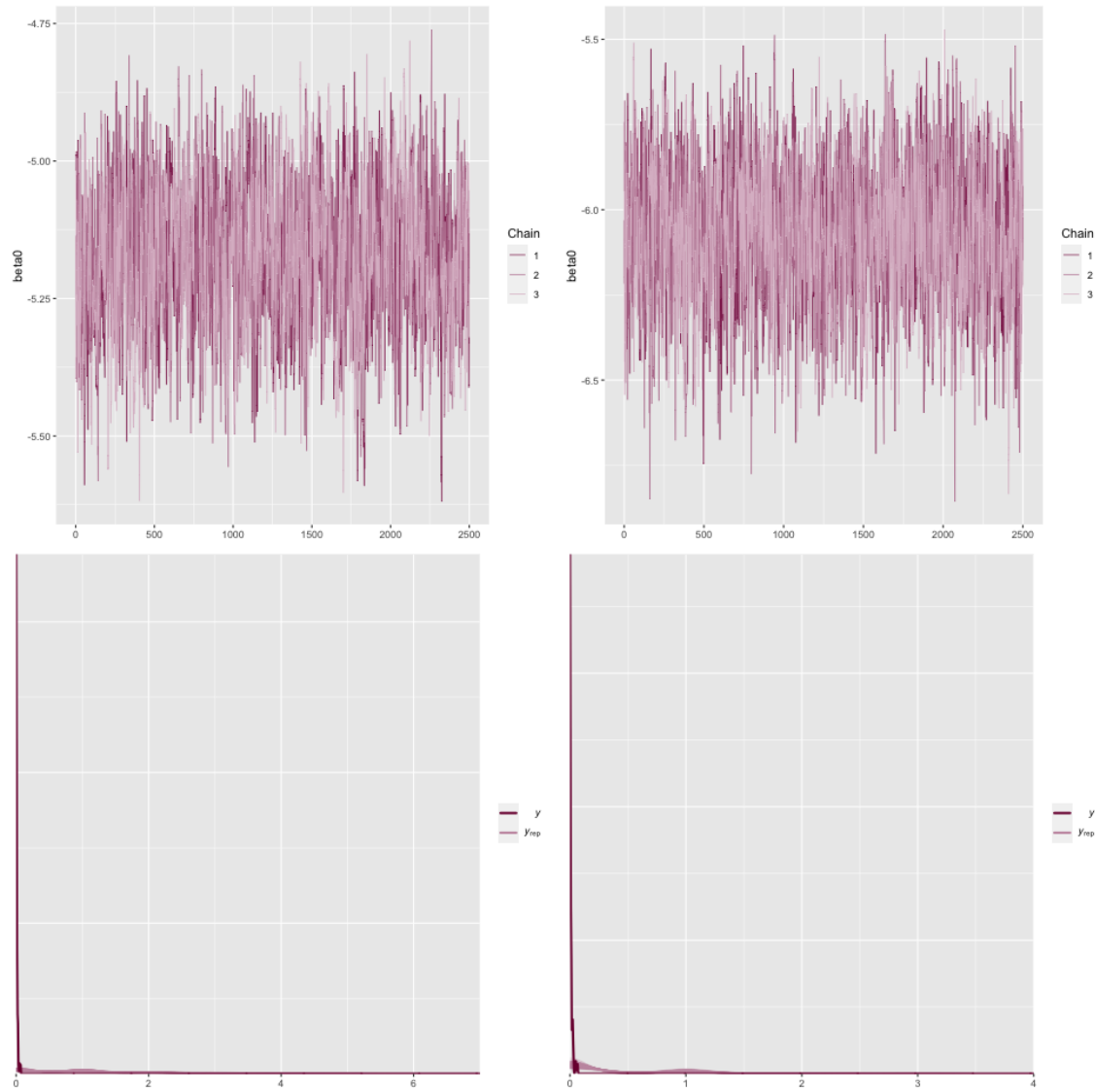


Figure 6: The a-b) posterior convergence of the parameters estimated by the germination from year one seedbank and germination from year two seedbank models respectively. The c-d) posterior distributions of floral viability estimates (pink lines) compared to the mean germination distribution (black line) of the real data for first year germinants and second year germinants respectively.

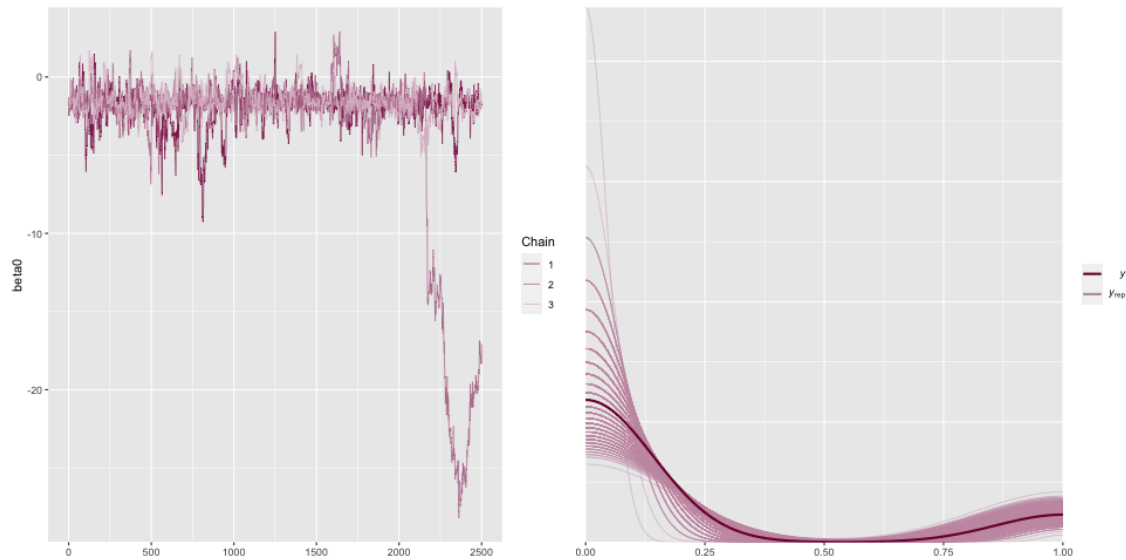


Figure 7: The a) posterior convergence of the parameters estimated by the pre-census survival model and the b) posterior distribution of the pre-census survival estimated (pink lines) compared to the mean distribution of observed pre-census survival (black line).

plants produce a mean of 160 seeds per flower. We are 73% and 78% confident that vacant plants produce more seeds per flower on average than plants tended by *C. opuntiae* and *L. apiculatum* ants respectively.

Precensus Survival Model. Pre-census seed survival rates fall between 0% and 95% with the mean pre-census seed survival at 18%.

Germination Model. Seeds have a significantly higher probability of germinating in year one than in year two. Seeds in year one experience germination rates between 50% and 100% with a mean of 62% germination. Seeds in year two experience germination rates between 50% and 98% with a mean of 58% germination.

New recruits are expected to be between the sizes of 0.11 cm^3 and 0.38 cm^3 with a mean size of 0.20 cm^3 .²⁸

²⁸Move to an appendix. These results are not relevant for the questions at hand.

Videos If you have videos, journal style for them is generally similar to that for figures.

Discussion brainstorming:

1. Mini abstract paragraph - synthesis of question plus answers, and overall significance Topic

sentence: Mutualisms commonly involve multiple partners but the ecological consequences of partner diversity remain poorly understood. Here we show...

2. COnnecting to broader patterns in the literature - address how complementarity or synergies are commonly reported – why did we not see this, especially since the vital rates suggest some complementarity - may involve the simulation experiments - some contrast with other systems where benefits of diversity have been found Topic sentence: similar studies have reported complementarity while we found sampling effect explains the benefits of diversity in our system. This may have to do with the sheer number of "liom" in the system.

3. If there is one best partner then diversity should impose opportunity costs – why do we not see this? - should address how some systems can host multiple partners at a time while others (ours) can exclusive associations; for the latter diversity should only be costly if there is one best partner?

4. Turnover - what's going on with turnover? what processes may drive the patters we see - what is seen elsewhere in the lit (invertase papers may be an interesting reference? showing plant "choice") - patterns could be consistent with ant and or plant choice (currently a "black box") - this might address both frequency and direction (direction may lead to some discussion of competition)

5. Portfolio effect - what is it, what does it predict, what did we find - what have other studies found? Topic sentence: Our work explicitly incorporated temporal environmental stochasticity, which raises the opportunity for portfolio effect as a mechanism of diversity benefits. Yet, we find...

6. Value of long-term data - includes turnover, portfolio effect - also address how the full demographic data provides the correct insight into ant effects (eg We thought Crem was a parasite based on less complete data)

888 7. Herbivory - this should underlie why these interactions are beneficial, so we need to
address this - this connects to portfolio effect, because fluctuations in herbivores (in conjunction
with ant-specific defenses against herbivores) would be why portfolio effect could occur

891 8. Limitations - confounds fundamental to observational data regarding ant effects on plant
demography (correlation/causation problem) – maybe plants that attract Liom through nectar
have a different pattern of allocation o growth and survival - cite experiments to support causal
894 interpretation of observational patterns (ants really do stuff) - extrapolating effects of ants beyond
the interactions that we can actually see (e.g., new recruits with Liom); and the counterfactual of
a Liom-only population is another form of extrapolation

897 9. Future directions – maybe embed these into paragraphs above where we see opportunity
to address limitations or extend the results – probably lots we can do with herbivory
Conclusion.

900 Appendices: 1. Herbivory 2. Additional methods and results 3. Posterior predictive checks
and model convergence 4. Maybe ant transition simulations