

Thank You, Next

Ali M. Campbell
Tom E.X. Miller

July 29, 2022

Abstract

Mutualisms are among the most widespread species interactions with diverse and dynamic consequences. Depending on environmental context the outcome of the interaction can range from parasitic to mutualistic. Most studies focus on a pair of species interacting in a mutualism, however most observed mutualistic interactions include more than two species. These are multi-species mutualisms, where there are multiple partners interacting with the same focal species. The partners can directly impact the focal species through the interactions, The cactus *Cylindriopuntia imbricata* reward partners with extrafloral nectar in exchange for defense by various ant species (primarily *Crematogaster opuntiae* and *Liometopum apiculatum*, though there are many other ant species with smaller populations) from herbivores and seed predators. Using a 20-year collection of demographic data (growth, survival, reproduction, ant partners, herbivory, etc.) from these cacti in New Mexico, we estimate the fitness of the cacti populations with every combination of partners, allowing us to *** understand what accounts for partner diversity in this system *** understand if the current partner diversity of the system is associated with the optimal fitness *** and the impacts of these partners on different vital plant processes across their life history (such as partner impacts on reproduction, survival, or growth). We found that different ant partners had different impacts on cacti vital rates suggesting there may be a different 'best' partner during pre-reproductive life stages than during reproductive life stages, and that the highest cacti fitness is associated with the current partner set (all possible ant partners are available). Together, these results suggest that complementarity may account for the benefits that these plants experience with partner diversity. Our results demonstrate the importance of evaluating a mutualism within a community context and suggest that even slight differences of rewards between mutualist partners can help promote fitness of the cacti².

Each of the ant partners³ in this system are within the same guild, all offering defense from herbivores, with only one ant species interacting with each individual cactus in a given period of time⁴. Though these ants may offer very similar rewards, they likely differ in some way⁵. Two possible ways they could differ are the fitness boost⁶ they offer the

² Nothing you have reported in the abstract so far really supports this statement.

³ Again, abstract should briefly state how many and which.

⁴ Redundant with statement above.

⁵ Vague

⁶ Vague and too colloquial.

focal species or the **period of ontogeny**⁷ in which they offer the greatest fitness boost. Using a long-term data-set, we show that there are differences in the impacts of different ant partners on various vital rates of the cacti across ontogeny. Our results demonstrate the importance of evaluating a mutualism within a community context and suggest that even slight differences of rewards between mutualist partners can help promote fitness of the cacti.^{8 9}

Context/Introduction

BASELINE OF MUTUALISMS Mutualisms are species interactions in which all involved participants benefit. They are among the most widespread species interactions[Chamberlain2014, Stachowicz2005, BoucherDouglasH.1985] with diverse and dynamic consequences. The benefits from these interactions are called rewards, but they require investment of resources into the interaction¹⁰.

Historically, scientists focused on pairwise mutualisms[Bascompote2019], however, in recent years multi-species mutualisms have been more heavily studied. It has become apparent that partner diversity in mutualisms often leads to non-additive fitness benefits for the focal mutualist[Afkhami2014, Palmer2010]. This means the benefits can be greater than, less than, or equal to the sum of the benefits observed in each of the pairwise interactions with the focal mutualist that makes up the multi-species mutualism. This is true for many complicated reasons, including interactions between the various partners, niche overlap, temporal resource variation, and differences in partner quality, functional benefit, and competitive ability[stanton2013, Afkhami2014, Boucher1982]. Often partners have similar resource needs, particularly if they are in the same guild, which can lead to resource competition and fighting, potentially reducing benefits, or to increased quality and frequency of benefits[Bascompote2019, Stanton2003]. For this reason, pairwise studies cannot be accurately used to predict the outcomes of multi-species mutualisms[Palmer2010, Stanton2013. Chamberlain2014, Song2020] which are more common. ***** Biodiversity ecosystem function?¹¹ Observational studies on the effects of diverse multi-species mutualism systems are necessary to help us understand the demographic effects of partner diversity in mutualisms.

The diversity of partners in a multi-species mutualism causes varied demographic effects on the population of the focal mutualist which can be explained by a number of mechanisms. Partners can vary in many ways: in some cases, the quality varies leading to some true mutualist partners, some freeloaders, and even some parasites{Bronstein1994, Afkhami2014, Song2020, West2007, Frederickson2013; in other cases, the function of the

⁷ *We have size structure data but we are not really dealing with ontogeny per se, so I think it is safer to discuss things in terms of size.*

⁸ *I am a little confused - maybe these two paragraphs are two different versions of the abstract?*

⁹ *I know this was just a first stab at the abstract, and written when you don't yet have your final results. But eventually this will need to be tightened up and edited to better describe the conceptual motivation, what was done, and what was found.*

¹⁰ *I'm honestly not sure if I need to explain this idea? Do I need to include more basic mutualism background? I have tried to shift this so that I cover a small amount and then jump into the idea of partner diversity in mutualisms instead*

¹¹ *After this I feel like I go straight into the mechanisms which explain the potential positive effects of diversity, but I don't specify that I am talking about those and I also don't talk about any explanations of negative effects? Maybe if I include the connection between BEF theory and mutualisms here it will make a nice bridge to the benefits of diversity?*

partner can vary, each offering a different type of reward to the focal mutualist {Stanton2003}. Partner quality variations can remain consistent across years and life stages of the focal mutualist or they can shift year to year. When partner quality remains consistent across time, meaning one partner is always better or worse than another, the effects of partner diversity on the focal mutualist can be explained by a mechanism called sampling effect. This is the concept that if partners vary in quality, then a more diverse sample of the partner community may be more likely to include the “best” one[Afkhami2014]. When a focal mutualist in a multi-species mutualism *experiences*¹² sampling effect the fitness of that focal mutualist should be equal to the fitness of the focal mutualist if they interacted only with the “best” partner. They can vary across years – portfolio effect. Alternatively, partners can vary

Sampling effect *states*¹³ that if partners vary in quality, then a more diverse sample of the partner community may be more likely to include the most beneficial one[Afkhami2014]. Particularly, this means that increased diversity of partners means increased probability that some of the partners will be highly beneficial. The fitness of a *multi-species mutualistic population*¹⁴ experiencing sampling effect will be equal to the fitness of the same population if they interacted only with their strongest partner.

Complementarity states that each partner may account for some part of the benefits, but each has different functional pathways, which together can aid in a broader benefit[Winfree2020]. This means that in populations where there is *sufficient interaction*¹⁵ with the diverse partners there is likely to be increased rewards and *fitness*¹⁶. The fitness of a multi-species mutualistic population *experiencing complementarity*¹⁷ is likely to be higher than that of any pairwise *mutualistic population*¹⁸.

Portfolio effect states that each partner is the best under a *different set of conditions*¹⁹, meaning across all conditions, meaning there is likely to be an *increase in potential benefits*²⁰[Winfree2020]. Thus, in populations experiencing highly diverse conditions, diverse partners are likely to increase the rewards and fitness of the focal mutualist. The fitness of a multi-species mutualistic population experiencing portfolio effect is likely to have a different strongest partner under different conditions, such as year to year, *and will experience similar fitness as they would in a pairwise mutualism with their best partner under any condition*^{21, 22}

These *biodiversity ecosystem functions*²³ are three which *can be used to explain the*

¹² *not sure if this is the right word*

¹³ *The effect does not state anything.*

¹⁴ *awkward*

¹⁵ *What do you mean by “sufficient”?*

¹⁶ *Whose fitness?*

¹⁷ *I don’t think sampling effect, complementarity, etc. are “experienced”.*

¹⁸ *What is a mutualistic population?*

¹⁹ *I could be wrong but I think the standard use of portfolio effect specifically refers to temporal variation.*

²⁰ *Increase relative to what? Benefits to who? What are they potential?*

²¹ *I don’t follow this last part.*

²² *You do a good job describing the mechanisms for positive diversity effects. I think you could rely more heavily on literature for these mechanisms, which is substantial.*

²³ *This is not what they are. They are mechanisms for positive effects of diversity that are most closely associated with the biodiversity-ecosystem function literature, which asks how changes in biodiversity affect ecosystem function*

diversity of mutualistic relationships in nature²⁴[Afkhami2014]. If a system benefits²⁵ from the existence of multiple partners, one of these functions may be at play. Within the section of mutualistic interaction which have multiple partners, there are many different classifications.²⁶ One type of mutualism that is historically well documented is the interaction between ants and plants[Boege2005, Barton2010]. These interactions can take many forms²⁷, including pollination²⁸, defense, dispersal, etc²⁹[Bronstein2006]. This paper focuses on defensive ant-plant mutualisms. These often involve long-lived³⁰ plants providing extra-floral nectar and/or habitats³¹ to ants which in turn defend them from herbivores[Bronstein1998]. These are very common interactions and have provided many opportunities for empirical studies of mutualisms.³² However, many of these studies have been pairwise rather than investigating the impacts that multiple partners may have on the costs and benefits of a system.³³

This study focuses on the long lived, facultative³⁴ *Cylindropuntia imbricata* (Cholla cacti³⁵) and its ant mutualists. The³⁶ cacti interact with several ant partners, *Crematogaster opuntiae* (Crem.) and *Liometopum apiculatum* (Liom.) are the most common partners though there are a number of other rarer ant partners, which visit these cacti in smaller population sizes^{37, 38}. The ant partners all provide defense to the cacti from predators³⁹ in return for exclusive interaction⁴⁰ with the plant to take the extra-floral nectar, meaning they are considered to be within one guild⁴¹. Predators of the cholla include insect herbivores and seed predators, which influence the reproductive output of the cacti⁴². Though many multi-species mutualisms result in both costs and benefits, it has been shown that the relationship between these cacti and ants does not result in any major costs for the cacti[Miller2007].⁴³ However, there are still some small costs which could influence the optimal set of partners.⁴⁴ This is part of what we will be analyzing

²⁴This is not correct, and it's an important point. These mechanisms cannot explain diversity in mutualisms. They could explain positive effects of partner diversity on a focal species, if any such effects occur

²⁵I don't think a "system" can benefit from anything.

²⁶Awkward and vague - what do you mean by "classification"?

²⁷I know what you mean, but use more precise language.

²⁸ant pollination is rare

²⁹are these any others besides these three?

³⁰not necessarily

³¹better to call this "housing"

³²No information here.

³³Hard to follow what gap in the literature you are trying to identify here. There are in fact many studies of ant-plant mutualism that include multiple partners. I think the new thing that you are contributing is asking how diversity in the ant defender guild affects the overall benefits of mutualism for the plant partner.

³⁴this is not an adjective that can be applied to a species

³⁵There are many species of cholla cacti. The common name of this one is tree cholla.

³⁶weird grammar in this sentence

³⁷We don't know anything about their population sizes.

³⁸These are the ant partners at the SEV. But the plants have a very wide distribution and likely interact with other ant species elsewhere. So I would not make it sound like this is an exhaustive list of partners for the entire species.

³⁹insect herbivores and seed predators

⁴⁰explain

⁴¹awkward

⁴²also growth, survival, etc.

⁴³I don't know what you mean. EFN production is a pretty clear cost.

⁴⁴This is vague, and tbh I don't know what you mean when you talk about costs.

in this paper.⁴⁵

Though all the ants associated with the Cholla⁴⁶ are within one guild, they may not all be equal, meaning the impacts on the Cholla are complex⁴⁷. In this study, we will answer a number of questions⁴⁸:

1. Do the Cholla cacti benefit from the multi-species mutualism with multiple ant partners?
2. What combination of, or individual, ant(s) result in the highest fitness for the Cholla cacti?
3. Is there evidence of sampling effect, complementarity, or portfolio effect to encourage the current multi-species state of the mutualism?

In order to answer these questions, I am constructing an Integral Projection Model (IPM)⁴⁹ to calculate the fitness of the Cholla cacti under different conditions⁵⁰. I will be able to quantitatively estimate⁵¹ the fitness of the cholla population if they were to interact with any combination of ant partners, allowing me to determine the best combination of partners. Similar approaches have been used to assess the individual qualities of multiple partners[Palmer2010] but not to determine the optimal combination of partners in a multi-species mutualism⁵².

We hypothesize that the cacti will experience the highest fitness when interacting with all partners observed in the field, meaning the current mutualism is the optimal outcome⁵³. We also hypothesize that complementarity and sampling effect will play roles in encouraging this⁵⁴ diverse mutualism⁵⁵.

Methods

Study System

To determine how interactions with multiple partners impacts the cacti over time, we have monitored a population of Cholla cacti annually since 2004. This study was conducted in the Los Pinos mountains, a small mountain chain located on the Sevilleta National Wildlife Refuge, a Long-term Ecological Research (LTER) site in central New Mexico. The tree cholla cacti are common in high Chihuahuan desert habitats, with their native

⁴⁵Awkward and unnecessary.

⁴⁶common names are not capitalized

⁴⁷no information here

⁴⁸I think this is a good list of questions. Following up on our conversation, we will probably want to re-orient the language to be clear that we are essentially asking about one vs two partners, which is still technically a diversity question but we don't want to oversell the 'diversity'.

⁴⁹This is only one piece of what you are doing. I think the value of the long-term data should be better emphasized.

⁵⁰What conditions?

⁵¹Use plural pronouns and don't use future tense, this is not a proposal.

⁵²The Palmer paper and perhaps others have done this. I think the novel contribution of this paper needs to be better explained.

⁵³I would avoid mention of optimality, which has an evolutionary implication that we are not addressing here

⁵⁴vague - sharpen this

⁵⁵A mutualism cannot be 'diverse'.

range spanning the southwestern USA *** Benson 1982***. These arborescent cacti produce new cylindrical segments every year which develop either into fruits which produce seeds or into vegetative segments with large spine which increase the size of the cactus. In central New Mexico, vegetative growth occurs from May – August.

Cholla cacti secrete extra-floral nectar (EFN) from glands on young vegetative segments and reproductive segments. This extra-floral nectar varies in chemical makeup across the lifespan of the cactus *** Miller ??***.⁵⁶ At the Sevilleta, the cacti are visited by multiple species⁵⁷ of ground-nesting ants, *Crematogaster opuntiae*, *Liometopum apiculatum*, and many other species⁵⁸ which occur at small⁵⁹ frequencies. These ants are attracted to the EFN and in return fight off the seed predators⁶⁰ which also visit the cacti⁶¹. These ants never co-occur on the same plant, instead competing for plant services⁶². Over the lifetime of the cacti each plant interacts with multiple partners as they tend to switch out season to season.⁶³

There⁶⁴ are a variety of insect herbivores and seed predators which attack the cacti, focusing either on the vegetative segments and the reproductive segments. There are a number of insects which occur commonly on these cacti at the Sevilleta. These include the weevil, the NP, and the *** (I think there is a moth as well?). The weevil⁶⁵ feeds on ***. The NP feeds on ***. Finally, the moth?? feeds on ***. All of these predators can have significant impacts on the fitness of both individual cacti and the population. *** Miller 2009***.

The⁶⁶ data collected on these cacti are from an 18-year⁶⁷ data-set. There are 8 30 × 30 meter plots from which this data is taken. Each plot is surveyed⁶⁸, and each plant within each plot is tagged and logged⁶⁹ each year. For every plant we take data on their survival, size⁷⁰, ant state⁷¹, herbivore presence⁷², flowering data⁷³, and seed data⁷⁴. This allows us to track the progression of individual plants across many years.⁷⁵ The length of this data-set

⁵⁶ This is pretty vague, so if you are going to say this you should add more detail.

⁵⁷ I think it would be better to say primarily two species plus other rare species, and giving the frequencies

⁵⁸ which ones?

⁵⁹ low

⁶⁰ which ones?

⁶¹ An example of words that make sentences clunky without adding any information

⁶² This is a hypothesis, not something that has been demonstrated.

⁶³ I would guess that most plants do not have much switching. I think you also need to talk about vacancy and the start of EFN production at larger reproductive sizes, more detail on transitions in ant state between vs within years. All of this should be in a separate subsection about natural history.

⁶⁴ This paragraph should also be in a natural history subsection and obviously needs more detail. See my earlier papers and references therein and let me know if you have specific questions.

⁶⁵ what species?

⁶⁶ This should be a subsection for data collection, with significantly more information than what you have here so that the methods could be reproduced.

⁶⁷ Which years?

⁶⁸ what does this mean?

⁶⁹ what does this mean

⁷⁰ how is size measured?

⁷¹ what is this?

⁷² this makes it sounds like presence/absence which is not what we record

⁷³ what does this mean?

⁷⁴ what does this mean?

⁷⁵ No new information here.

Statistical Modeling

To understand the impacts of multiple species interactions on the cacti populations, we constructed **bayesian demographic models of many vital rates**⁷⁶. With these models, we were able to ask (i) Do the impacts of ant presence on **cacti fitness**⁷⁷ differ across ant species? (ii) What are the probabilities of an individual cactus interacting with each ant species?⁷⁸

The vital rates of the cacti considered in this model include survival rate, growth rate, reproductive state, floral abortion rate, **seed production, and germination**⁷⁹. We fit **generalized linear mixed effects models in a heirarchical Bayesian framework to quantify each of the vital rates**.⁸⁰ Each model takes the data from year t and estimates the values **in year $t+1$** .⁸¹ This allows us to predict a vital rate for any plant with a given set of characteristics, **such as size and ant state**⁸².

Demographic Modeling

The statistical models described above parameterize the Integral Projection Model (IPM) that we used to estimate population growth under various partner conditions. This model was used to estimate the growth rate of the cactus population, effectively a quantitative measure of the fitness of the population. The fitness was estimated under the **range of all different conditions, no ants present, one ant species present, two ant species present, all ant species present**. These allow us to compare the fitness of the cacti under no mutualistic interactions, pairwise mutualisms, and various multi-species mutualisms to **show which case results in the highest fitness for the cacti**.⁸³

Following previous studies, we modeled the life cycle of *C. imbricata* using continuously size-structured plants, $n_i(x)$, and two discrete seed banks ($\beta_{1,t}$ and $\beta_{2,t}$) corresponding to 1 and 2-year old seeds.

$$B_{1,t+1} = \kappa \delta \sum_i^4 \int_L^U P(x) A_i(x) F(x) n_i(x) dx$$

$$B_{2,t+1} = (1 - \gamma_1) B_{1,t}$$

The functions P , F , and A give the probability of flowering, the number of flowerbuds produced, and the proportion of flowerbuds which will create seeds. Each of these functions, estimated by a Bayesian model calculates these values for an x -sized plant in year t . The proportion of flowerbuds which will produce seeds (A) is also dependent on the

⁷⁶ *What are bayesian demographic models? WHat are the many vital rates?*

⁷⁷ *these models are not measuring fitness*

⁷⁸ *I think it's good that you have these as separate questions but I think each one needs a lot more context and detail.*

⁷⁹ *You have not described where these data come from.*

⁸⁰ *Not a reproducible description of the methods. e.g., what distributions were used, what were the fixed and random effects, which models included ant effects, what were the priors, how many chain and iterations, and were convergence and fit assessed, etc?*

⁸¹ *This is true only for growth and survival.*

⁸² *Not such as, it is really just these two things.*

⁸³ *This needs a more thorough explanation, but I would also do this later after the model has been introduced and explained.*

ant species present on the plant i in year t . The integral is multiplied by the number of seeds per fruit (κ) and the probability of seed dispersal/survival (δ) to give the number of seeds that enter the 1-year old seed bank. Parameters U and L are the upper and lower bounds, respectively, of the plant size distribution. Plants can recruit out of the 1-year seed bank with the probability of γ_1 or transition to the 2-year seed bank with a probability of $1 - \gamma_1$. Seeds in the 2-year seed bank are assumed to either germinate with a probability of γ_2 or die.

The size dynamics of the plants are given by:

$$n(y, i)_{t+1} = (\gamma_1 B_{1,t} + \gamma_2 B_{2,t}) \eta(y) \omega \beta_i + \sum_j^4 \int_L^U S_j(x) G_j(y, x) \tau_{ij}(x) n_j(x) dx$$

The final equation gives the **size**⁸⁴ of the *C. imbricata* population n in year $t + 1$ based on the vital rates and size n of the population in year t . The first term gives the recruitment from 1 and 2-year seedbanks to size y . $\eta(y)$ gives the seedling size distribution, which is assumed to be normally distributed, and ω gives the proportion of seedlings which survive from germination (late summer) to the census (May). The second term gives the changes in the population of the cacti which are not recruits. The functions S and G give the probabilities of surviving from year t to $t + 1$ and growing to size y from year t to year $t + 1$, respectively. Each depends on the size x in year t and the ant state j in year $t + 1$. Finally, τ_{ij} is the probability of a cactus which is size x with ant partner i in year t being tended by ant partner j in year $t + 1$.

Model analysis

TOM STOPPED EDITING HERE

Results

Vital Rates

We used field data on cholla cacti to evaluate the differing impacts that the ant mutualism has on the fitness of the cacti. The fitness can be broken down into a number of vital rate components, including survival, growth, probability of flowering, number of fruits and seeds produced, etc. called vital rates. We found that many of these vital rates differ in the presence of different ant species.

The first vital rate we analyzed was the survival of the cacti. As you can see in Figure ??, the survival rate of cacti vary significantly across their lifetimes as they grow. Young (small) cacti have relatively low survival rates, near 30% while the older mature cacti have much higher survival rates, near 100%. This means cacti are at their most vulnerable to death when they are young. The survival rates differ with more than just the size of the cacti, the ant species present on the cactus is also important.

There are no very small cacti tended by ant partners because they do not produce EFN. This is reflected in Figure ?? where only the vacant data (yellow) in panel (d)

⁸⁴not just population size but also composition in terms of size and ant state - this needs to be explained better

Survival Rates of Cacti of by Ant State and Size

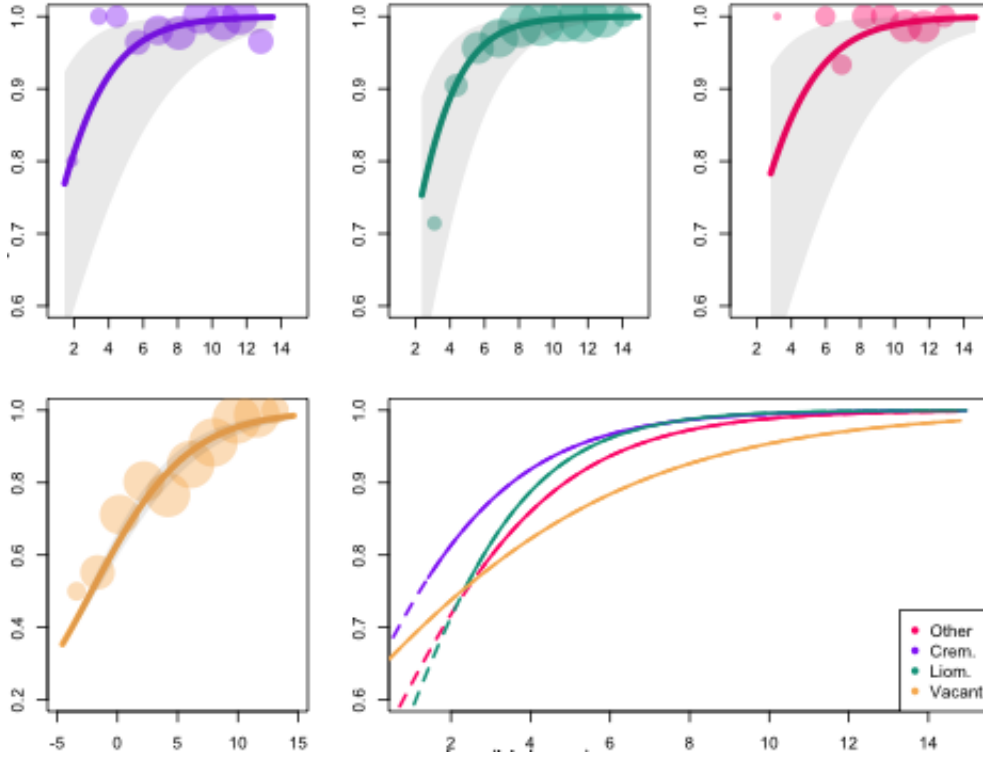


Figure 1: Probability of cactus survival from year t to year $t+1$ when tended by (a) *Crem.* (Purple), (b) *Liom.* (Teal), (c) ants in the other category (Pink), or (d) no ants (Yellow). Panels (a-d) show the best-fit line estimating the survival probabilities of cacti, with a grey area representing the uncertainty, and circles representing the actual data (scaled to represent number of observations). (e) shows the best-fit probabilities of survival of different-sized cacti with all ant partners.

extends to the smallest sizes. Once cacti reach a size large enough to attract ant partners with EFN, the cacti which are partnered with *Crem.* have the highest survival rates compared to all other cacti. When the cacti reach their larger sizes, the partnered plants all reach a nearly 100% survival rate while plants with no partners have a slightly lower survival rate for all large cacti. This result indicates that *Crem.* tended plants may have an advantage, when they are relatively small, over other cacti.

The next vital rate we analyzed was the viability rate of the cacti, the proportion of fruits produced which are viable for reproduction. It is clear from Figure ?? that the cacti tended by *Liom.* ants experience significantly higher proportions of viable fruits. This result aligns with much of the literature which shows that *Liom.* are more aggressive against herbivores and seed predators, therefore are very high quality defenders. This high-quality defense is imperative for high viability rates on reproducing cacti which are likely to attract many antagonists due to the quality of their EFN.

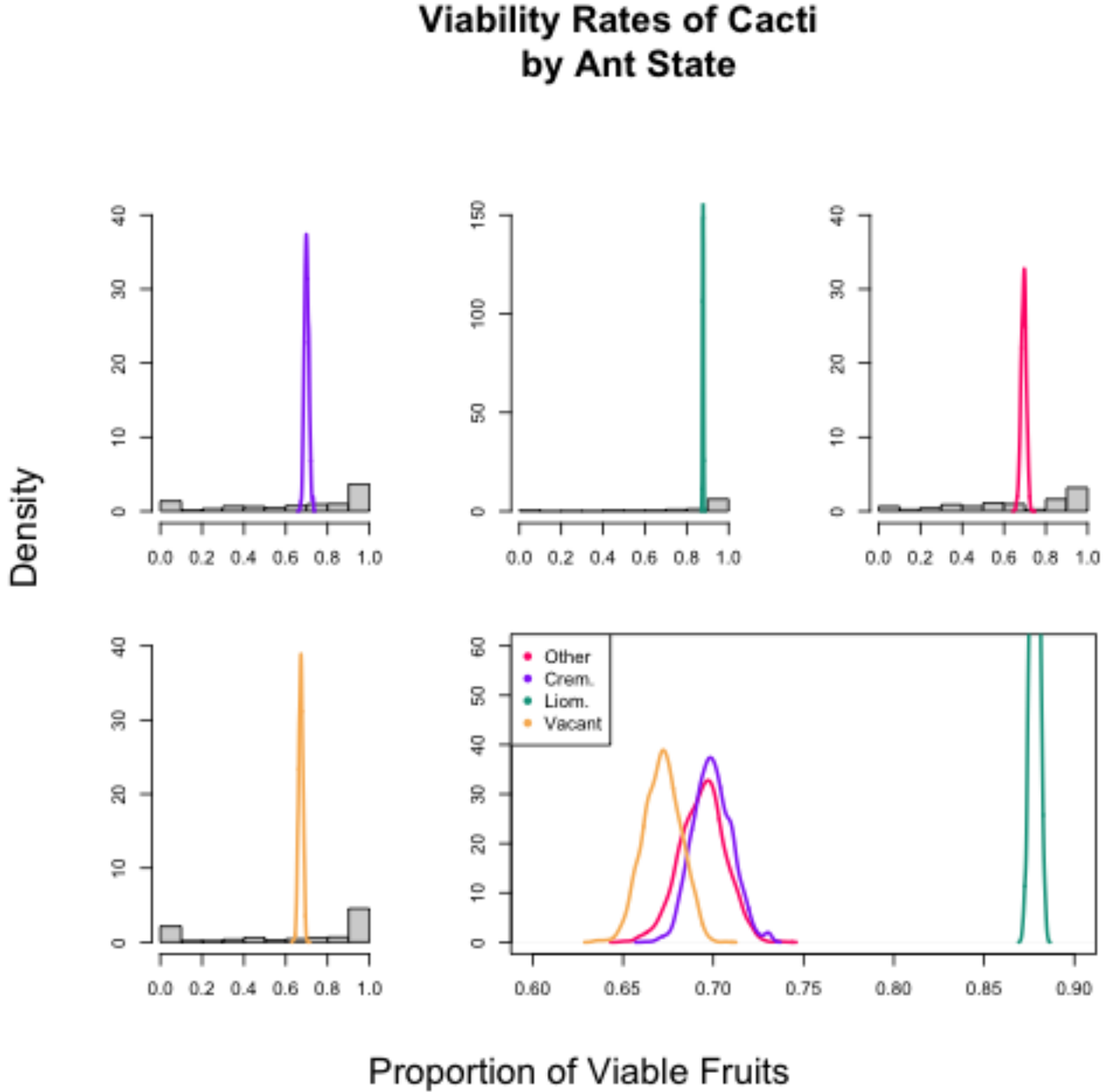


Figure 2: Proportion of viable fruits produced by a cactus in year $t+1$ when tended in year t by (a) *Crem.* (Purple), (b) *Liom.* (Teal), (c) ants in the other category (Pink), or (d) no ants (Yellow). Each panel (a-d) shows a histogram of the actual data overlaid with a density distribution of the predicted viability rate of the cacti. Panel (e) shows the predicted distributions of viability rates separated by ant species.

A third vital rate considered in this paper is the growth rate. Cacti who are attacked by herbivores are likely to lose sections of their growth, leading to a lower, or even negative, growth rate. In Figure ?? you can clearly see that untended plants are the only cacti which experience a negative growth rate at any size. This again aligns with expectations that tended cacti are being defended from herbivores and are therefore unlikely to lose enough vegetation to result in a negative growth rate.

Growth Rates of Cacti of by Ant State and Size

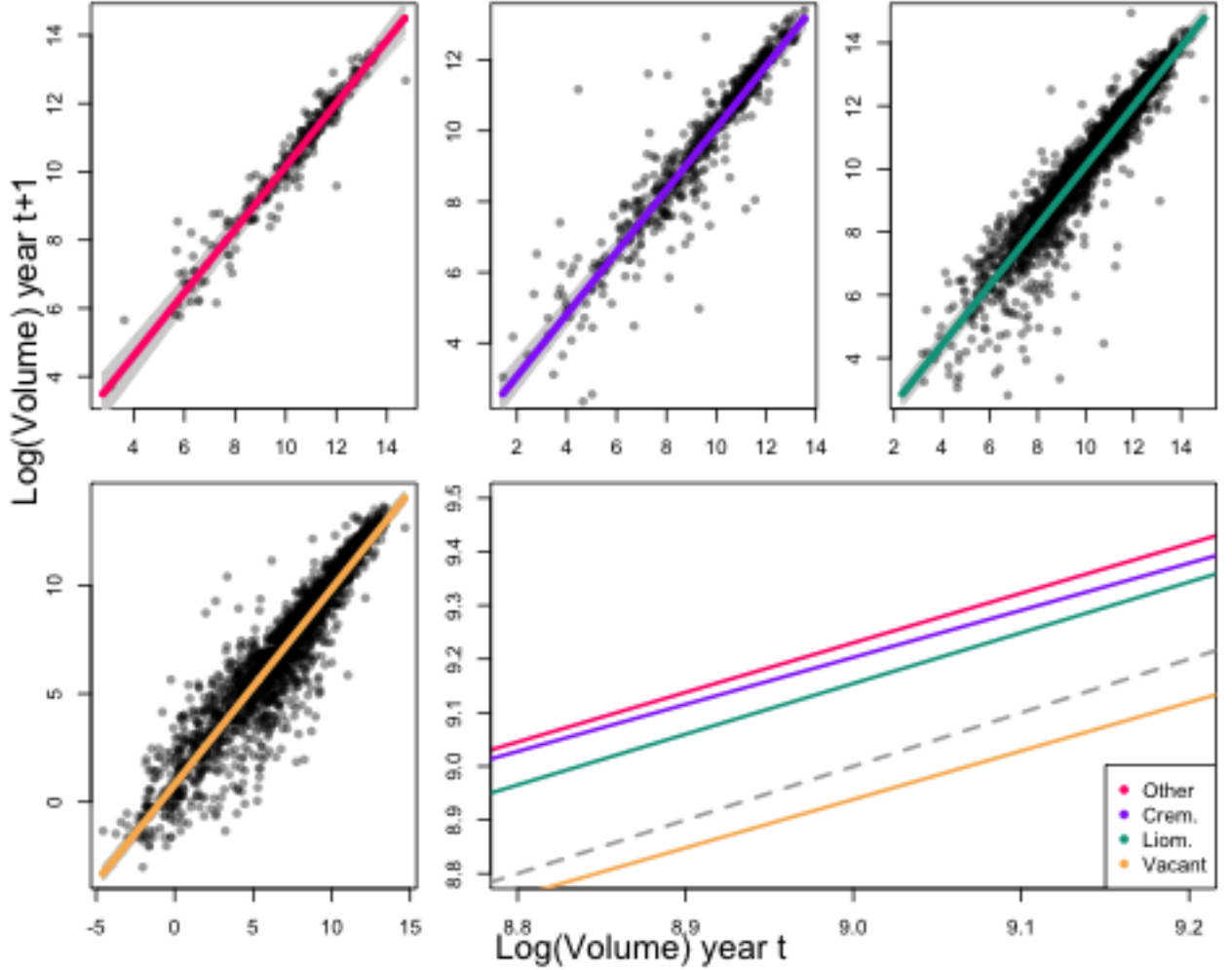


Figure 3: The size of a cactus in year $t+1$ given a previous size in year t and being tended by (a) *Crem.* (Purple), (b) *Liom.* (Teal), (c) ants in the other category (Pink), or (d) no ants (Yellow). Each panel (a-d) shows a best-fit prediction of the future size based on the previous size, the uncertainty in grey surrounding the best-fit, and the actual data in (circles scaled to represent the number of observations). Panel (e) shows all best-fit lines together in the same colors as above and a line (grey, dashed) above which plants are growing (have a positive growth rate) and below which plants have a negative growth rate.

Ant Transition Rates

In addition to the vital rates of the cacti, we also analyzed the transition rates from one ant partner to another across years.

Growth Rates of Cacti of by Ant State and Size

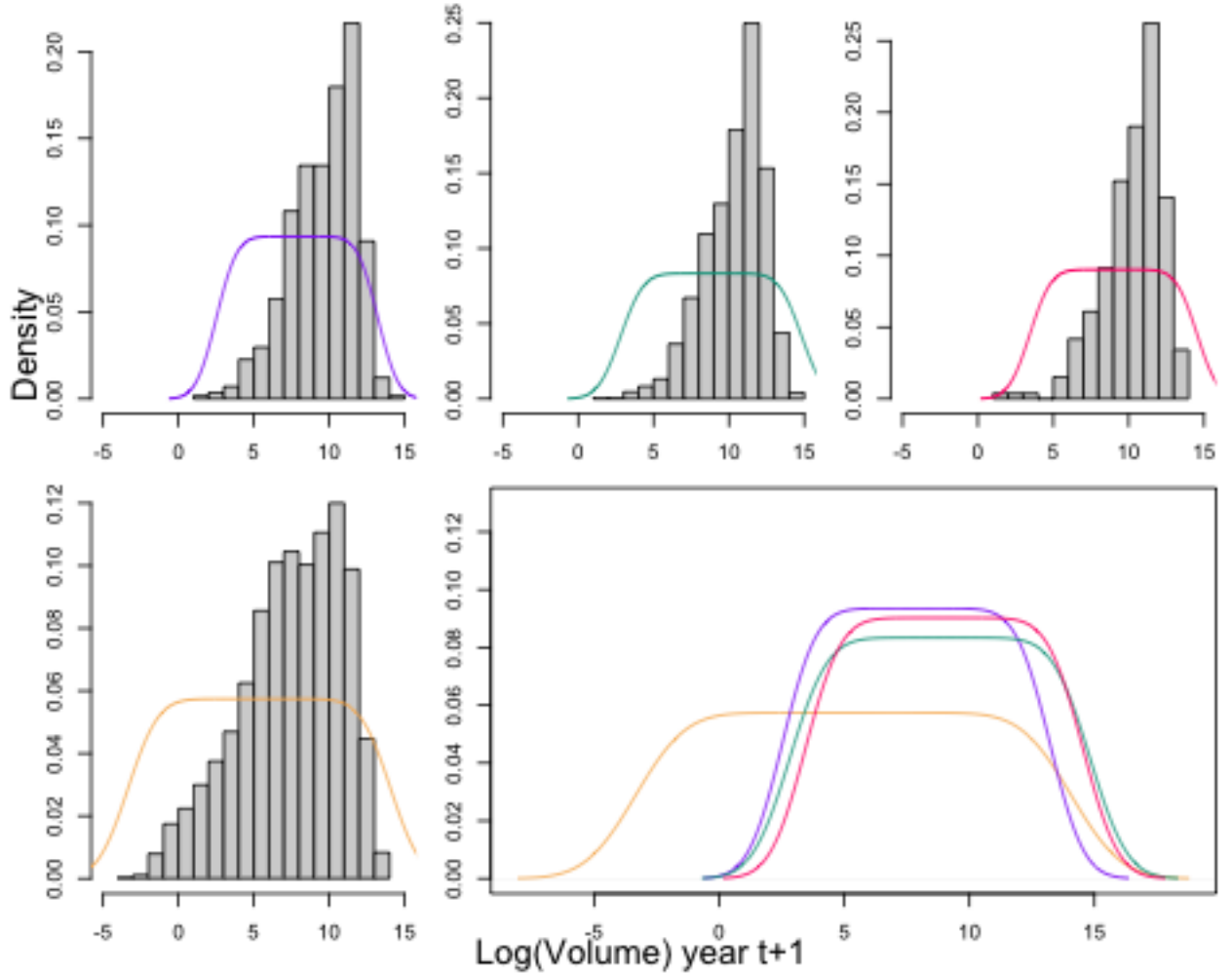


Figure 4: The size of a cactus in year $t+1$ given a previous size in year t and being tended by (a) *Crem.* (Purple), (b) *Liom.* (Teal), (c) ants in the other category (Pink), or (d) no ants (Yellow). Each panel (a-d) shows a distribution of the predicted future size based on the previous size and a histogram of the actual data. Panel (e) shows all predicted distributions together in the same colors as above.

Discussion

There is a constant tension within life cycles between energy and resource allocation. Individuals often have the ability to either put significant resources towards one process or split their resources between multiple. Full energy allocation to one process generally means better results, but splitting resources is a form of bet hedging^{***}. The cacti studied here experience a certain tension between their many vital rates, particularly growth and reproduction because each year they produce new floral buds and new vegetative

Ant States Possible	Growth Rate ($\frac{n_{t+1}}{n_t}$)	Population λ
No ants		
<i>Liom.</i>		
<i>Crem.</i>		
Other		
<i>Liom.</i> & <i>Crem.</i>		
<i>Liom.</i> & Other		
<i>Crem.</i> & Other		
<i>Liom.</i> , <i>Crem.</i> & Other		

Table 1: Caption

growth. Small plants rarely put out flowers and instead focus on growth, but larger plants must choose each year. The analyses of the individual vital rates indicate that different ant species may protect different processes better than others. In particular *Crem.* may offer advantages to smaller plants by protecting their new vegetation well. This is seen in the higher survival rates and growth rates of small and medium cacti with *Crem.* tenders in Figure ?? and Figure ?. *Liom.* ants alternatively may protect reproductive focus more than other partners. The *Crem.* tended plants however, have lower viability rates than any other ant tended plants, indicating they do not protect flowers well from herbivores(Figure ?). This is seen in Figure ? where it is shown that plants tended by *Liom.* have the highest viability rates of their flowers, resulting in higher pollination rates. Larger plants are also less likely to lose branches when they are tended by *Liom.* (Figure ?), keeping them healthy and more able to generate new plants. Each of these ants individually offer both benefits and drawbacks but considered together may indicate complementarity across ontogeny.