

2019-09-26 Stacks and Queues

Thursday, September 26, 2019 8:59 AM


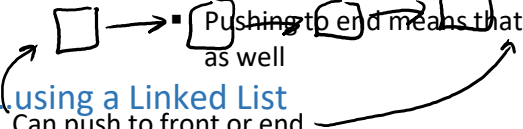
- Both stacks and queues define how we insert, access, and retrieve data
 - NOTE: neither stack nor queue specify how data should be contained (e.g. in Vector or LL)
- A stack has the following rules
 - The order in which things are inserted are the opposite of the order in which things are removed
 - In other words, what goes into the stack first must come out of the stack last (FILO)
 - In other words, what comes into the stack last must come out first (LIFO)
- A queue has the following rules
 - Items are removed from the queue in the order in which they are inserted
 - In other words, what goes in first, comes out first (FIFO)
 - In other words, what goes in last comes out last (LILO)
- The quintessential stack is a stack of boxes



- Stacks are pretty common in programming. In fact, every program has at least one stack - call stack
- Stacks are also used in recursion and searching (depth-first search)
- Stacks are also very handy implementing undo and redo
- Stacks have two operations:
 - Push() -> add item to "top" stack
 - Pop() -> remove item from "top" of stack
- Queues are also very common in real life
 - Lines of people
- Also popular in computing
 - Networking
 - Printing
- Queues are also used in searching (breadth-first search)
- Queue operations
 - Enqueue() / (C++) Push() -> add item to "end" of queue
 - Dequeue() / (C++) Pop() -> remove item from "front" of queue
- Bonus Data Structure: Deque (pronounced "deck")
 - Works like a deck of cards
 - Add to top of deque
 - Add to bottom of deque
 - Remove from top of deque
 - Remove from bottom of deque

Implementing A Stack

...using a Vector

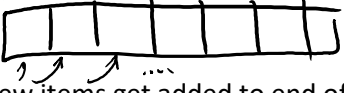
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 - Where should push() put new elements?
 - Push to front is bad idea because it is $O(N)$
 - Push to end is good because $O(1)$
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...using a Linked List

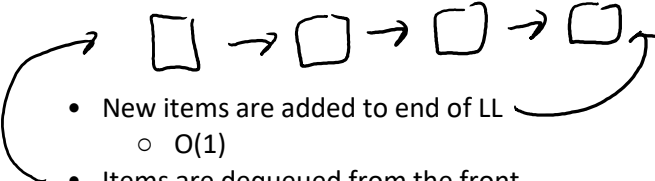
- Can push to front or end
 - Push to front $O(1)$
 - Push to end $O(1)$ assuming intelligent LL design
 - Regardless of choice $O(1)$ on pop()

Implementing a Queue

...using a vector

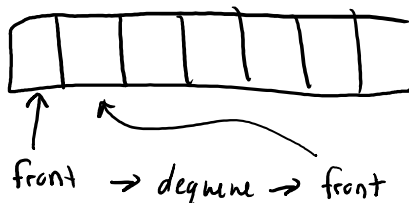
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- New items get added to end of vector $O(1)$
 - Therefore, items must be dequeued from element 0
 - $O(N)$

...using a linked list

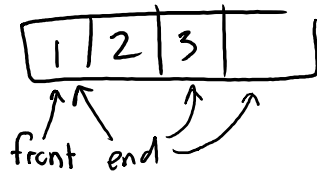
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- New items are added to end of LL
 - $O(1)$
 - Items are dequeued from the front
 - $O(1)$

Improve a vector-based queue's performance

- Observation: performance is slow because we must always dequeue from element 0 (physical constraint)
- Why must the front of the queue be tied to a physical location?
 - Why can't we make the "front" of the queue a logical construct? $O(1)$

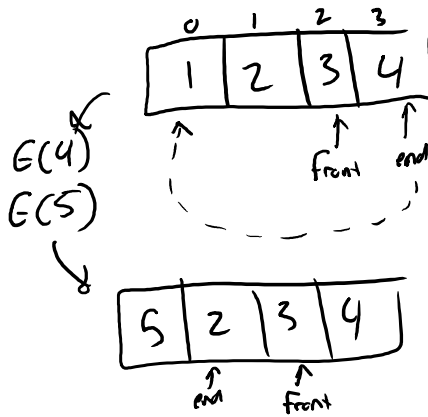


- Major downside: After a dequeue operation, the vector will contain empty wasted space.
 - E.g. if we do 1k enqueues and dequeues, there will be 1k empty boxes that can't ever be used again.
- Observation #2: make enqueue a logical operation
 - I.e. add to "logical" end of queue



Enqueue
 $\text{data}[\text{end}] = \text{value};$
 $\text{end}++;$

- Operation: E(1), E(2), E(3), D(), D()



$$\text{end} = (\text{end} + 1) \% \text{size};$$

- Resize when $\text{end} == \text{front}$ AND logical size == physical size
- This data structure has $O(1)$ enqueue and $O(1)$ dequeue
- This queue structure is called "circular queue"

