

Étude et modélisation de la propagation d'un feu de forêt

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CPGE MP

- Modélisation informatique de la propagation d'un incendie en milieu forestier
- Modélisation physique de la propagation d'un incendie en milieu forestier



Hypothèses de modélisation

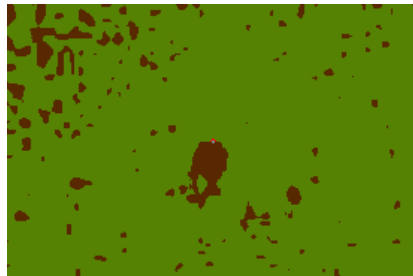
- Discrétisation du temps et de l'espace
- Structure de la forêt : uniforme, deux dimensions
- Structure du feu : probabilité de propagation dans 4 directions
- Combustion Complète

Modèle de l'automate cellulaire : 1 arbre = 1 cellule

- matrice d'états de la forêt
- 3 états possibles : (0, arbre en vie) ; (1, arbre en feu) ; (2, arbre carbonisé)
- $e_{i,j}$ état de la cellule
- $k_{i,j}$: itération où l'arbre en (i,j) brûle, -1 si l'arbre est en vie

$$\begin{pmatrix} e_{11}, k_{11} & e_{12}, k_{12} & \dots & e_{1n}, k_{1n} \\ e_{21}, k_{21} & e_{22}, k_{22} & \dots & e_{2n}, k_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ e_{n1}, k_{n1} & e_{n2}, k_{n2} & \dots & e_{nn}, k_{nn} \end{pmatrix}$$

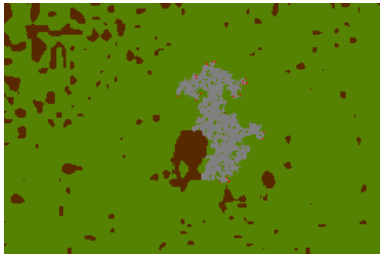
- Traitement d'Image : Conversion en automate



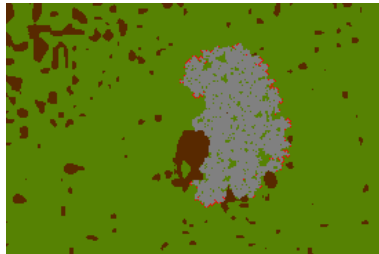
Paramètres de la simulation

- 1 Densité de la forêt (élaguage)
- 2 Vent
- 3 Durée de combustion d'un arbre
- 4 Probabilité de propagation du feu

- forêt non élaguée, pas de vent,
- $T_c=1$ itération
- 100 itérations

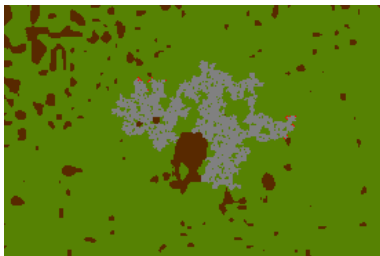


$$p = 0.49$$

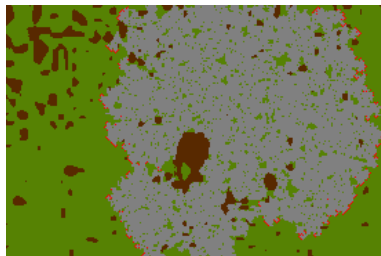


$$p = 0.51$$

- 200 itérations

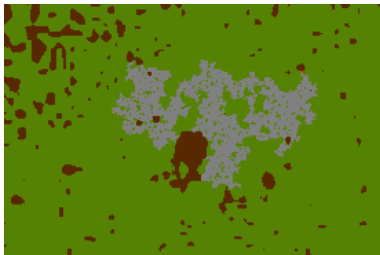


$p = 0.49$

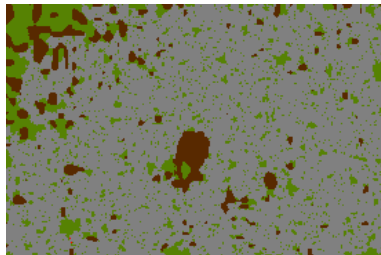


$p = 0.51$

- Dernière Itération



$$p = 0.49$$



$$p = 0.51$$

- Proportion de forêt Brulée : 22% ; 91%

Phénomène de Percolation

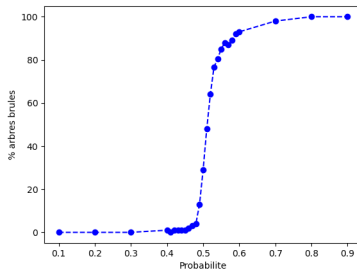
Définition

- 1 système = réseau de sites en liens
- 2 différents états, transmission de l'information aux voisins
- 3 phénomène de seuil associé à la transmission d'une information

Seuil de Percolation

- 1 $p > P_c \Rightarrow$ Percolation
- 2 $p < P_c \Rightarrow$ Pas de Percolation
- 3 $p = P_c \Rightarrow$ Instable

Percolation : déterminer expérimentalement le seuil de percolation

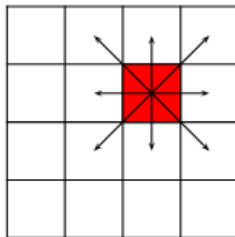


- Théorie : $P_c = 0.5$
- Expérimentalement : $P_c \simeq 0.5$

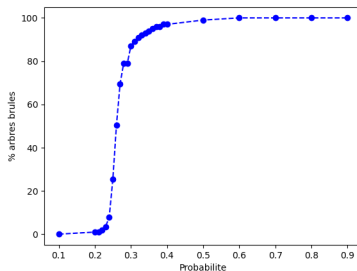
Complexification de la modélisation

Propagation

- 1 Propagation dans 8 directions
- 2 Résultat Théorique pour 4 voisins plus valable
- 3 Détermination expérimentale du seuil de propagation pour une propagation plus complexe



Propagation dans 8 directions



- Expérimentalement : $P_c \simeq 0.25$

Extraire des Informations

❶ évolution d'états d'une case, V, R, N : $X_{i,j,n}$

❷ nombre de cases vertes à k :

$$V_k$$

❸ nombre de nouvelles cases en feu à k :

$$F_k$$

❹ nombre de cases vertes atteignables par le feu à l'itération k :

$$N_k$$

❺ Mesure de P_p : déterminer

$$P(X_{i,j,k+1} = R | X_{i,j,k} = V)$$

- exemple pour un cas à 2 itérations :
- $k=0$, $E_0 : V_0 = 10$ et $F_0 = 0$
- $k=1$, $E_1 : V_1 = 8$ et $F_1 = 2$
- $k=2$, $E_2 : V_2 = 5$; $F_2 = 3$
- Fonction de vraisemblance :

$$j(p) = P([V_2 = 5, F_2 = 3] \cap [V_1 = 8, F_1 = 2])$$

- Loi des probabilités composées :

$$P(E_0 \cap E_1 \cap E_2) = P(E_2|E_1 \cap E_0) \cdot P(E_1|E_0) \cdot P(E_0)$$

- case dans N_k à l'itération K : probabilité P_p de devenir rouge à $k+1$
 \Rightarrow Loi de Bernouilli, paramètre P_p
- Ensemble des cases de l'espace à l'itération k : loi binomiale ($n = N_k$, $p = P_p$)

Vraisemblance

$$j(P_p) = \prod_{k=1}^N \binom{N_k}{F_{k+1}} \cdot P_p^{F_{k+1}} \cdot (1 - P_p)^{N_k - F_{k+1}}$$

Objectif : Estimation au sens du maximum de vraisemblance P_p

$$\log(j(P_p)) = \sum_{k=1}^N \log \binom{N_k}{F_{k+1}} + F_{k+1} \log(P_p) + (N_k - F_{k+1}) \log(1 - P_p)$$

$$\frac{\partial \log(j(P_p))}{\partial P_p} = \sum_{k=1}^N \frac{F_{k+1}}{P_p} - \frac{N_k - F_{k+1}}{1 - P_p}$$

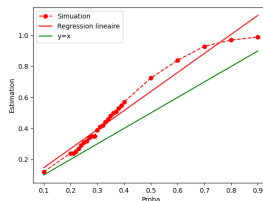
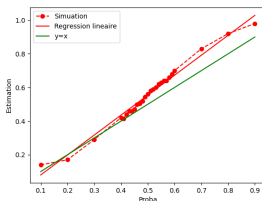
$$\frac{\partial \log(j(P_p))}{\partial P_p} = 0$$

\Rightarrow

$$\hat{P}_p = \frac{\sum_{k=1}^N F_{k+1}}{\sum_{k=1}^N N_k}$$

Résultats de l'estimation

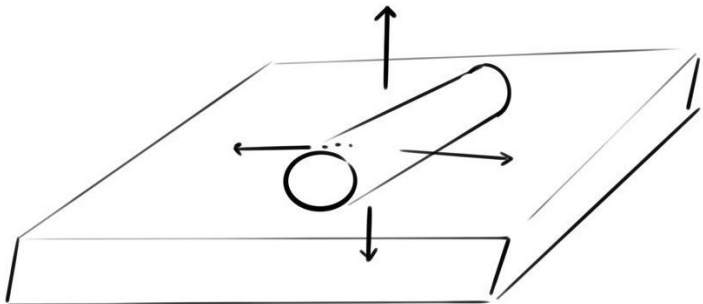
- Médiane de \hat{P}_p sur 50 simulations



Foret Initiale $y = 1.18, r^2 = 0.98$ Foret élaguée $y = 1.29, r^2 = 0.98$

Objectifs

- 1 Modéliser la propagation du feu à une échelle Locale
- 2 Tige enflammée sur le sol



- cylindre : $r(t)$, $h(t)$
- Hypothèse : $r(t) \sim \text{constante} = r_0$

$$\frac{dh(t)}{dt} = -C$$

$$h(t) = h_0 - C \cdot t$$

$$A(t) = 2 \cdot \pi \cdot r_0 \cdot (h(t) + r_0)$$

$$m(t) = m_0 - k \cdot t$$

$$k = \rho \cdot \pi \cdot r_0^2 \cdot k$$

- Flux Radiatif
- Flux Convectif
- Loi de Stefan, Loi de Newton :

$$m(t) \cdot c_p \cdot \frac{dT}{dt} = -A(t)(\sigma \cdot (T^4 - T_0^4) + h(T - T_0)) \quad (1)$$

- c_p : capacité calorifique massique
- σ : constante de Boltzmann
- h : coefficient de transfert thermique
- T_0 : Température Ambiante

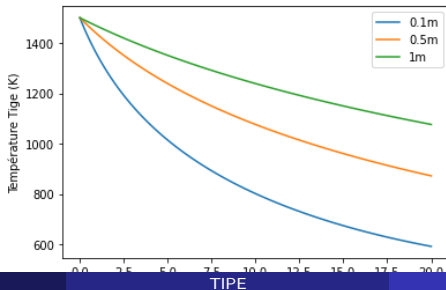
- Température d'ignition des feuillages : $T_i = 505 \text{ K}$
- Chaleur échangée : isotrope

$$dH_{\text{portion}} = m_{\text{portion}} \cdot c_{\text{sol}} \cdot dT_{\text{portion}} = \frac{1}{4} \cdot \delta Q_{\text{perdue}} = -\frac{1}{4} \cdot dH_{\text{tige}} \quad (2)$$

$$m_{\text{portion}} \cdot c_{\text{sol}} \cdot \frac{dT_{\text{portion}}}{dt} = -\frac{1}{4} \cdot m(t) \cdot C_p \cdot \frac{dT}{dt} \quad (3)$$

Modélisation Physique : Courbes Théoriques

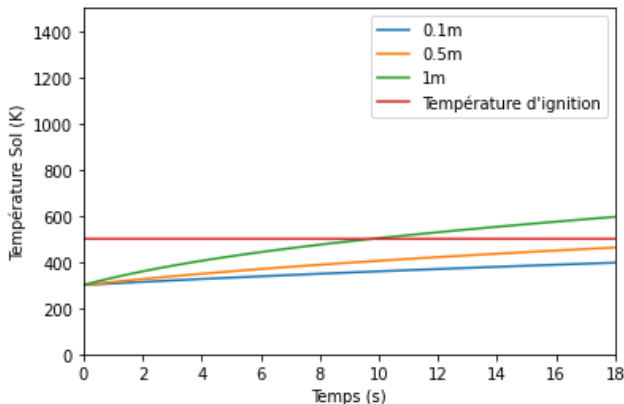
- Température de la tige
- $h = 5 \frac{W}{m^2 K}$: Coefficient de transfert thermique
- $T_0 = 300K$: Température de référence
- $T_{initiale} = 1500K$: Température initiale
- $c_{sol} = 0.001 \frac{J}{kg K}$: Capacité thermique massique du sol
- $m_{tranche} = 1kg$: Masse de la tranche de sol considérée



Modélisation Physique

Courbes Théoriques

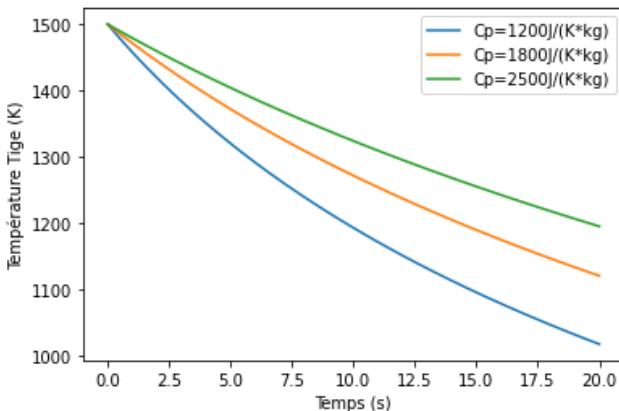
- Équations différentielles non linéaires \Rightarrow Résolution Numérique
- Température du sol



Modélisation Physique

Courbes Théoriques

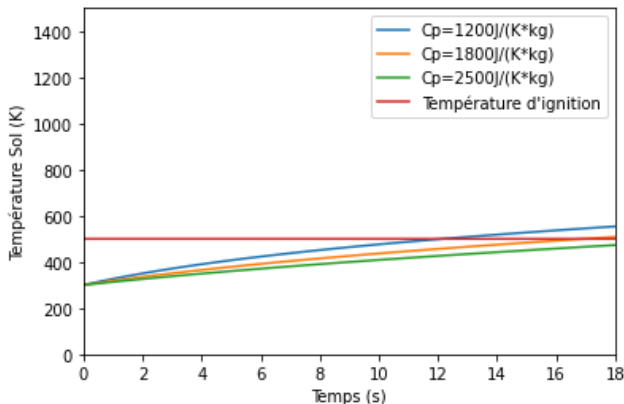
- Équations différentielles non linéaires \Rightarrow Résolution Numérique
- Température de la tige



Modélisation Physique

Courbes Théoriques

- Équations différentielles non linéaires \Rightarrow Résolution Numérique
- Température du sol



Conclusion

- ① Bilan :
- ② échelle globale
- ③ phénomènes de percolation
- ④ échelle locale

- Ce que le TIPE m'a apporté :
- Progresser en programmation
- Apprendre à écrire en Latex
- Étudier des documents scientifiques
- Apprendre à développer un modèle scientifique

```

22 from PIL import Image
23 from numpy import asarray
24 import numpy as np
25 #import random
26 import argparse
27 import sys
28 import random
29 import os
30 import re
31 import matplotlib.pyplot as plt
32 import statistics
33 from scipy import stats
34
35
36 # RGB colors
37 rgb_alive = [86, 130, 3]
38 rgb_notree = [88, 41, 0]
39 rgb_burning = [255, 0, 0]
40 rgb_burned = [128, 128, 128]
41
42 # labels used for trees
43 alive = 0
44 burning = 1
45 burned = 2
46 notree = 3
47
48 # Convert an image into an RGB matrix, with 2 colors: one for trees, one for the
49 # remaining pixels
50 def get_rgb_matrix(filename):
51     img = Image.open(filename)
52
53     t = asarray(img)
54     n = len(t)
55     m = len(t[0])
56     I = np.zeros((n,m,3), dtype="uint8") # creates a matrix n x m with triples of zeroes
57
58     # for each pixel, if g dominates: creates a green cell; red otherwise
59     for i in range(n):
60         for j in range(m):
61             if (t[i][j][1]>t[i][j][0] and t[i][j][1]>t[i][j][2]):
62                 I[i][j] = rgb_alive
63             else:
64                 I[i][j] = rgb_notree
65     return I
66
67
68 # get the offsets (-1, 0, +1) of the neighbors of the cell (i,j) in matrix M
69 # NB: topology==4 or 8, that is 4 or 8 neighbors
70 # NB: a list of pairs (a,b) is returned
71 def get_neighbors_offsets(M, i, topology):

```

```

71 def get_neighbors_offsets(M,i,j, topology):
72     L = []
73     n = len(M)
74     m = len(M[0])
75     # (-1,0,1): offset with respect to i; likewise for j
76     for a in range(-1,2):
77         for b in range(-1,2):
78             # select the four neighbors above/below/left/right; remove center + corners
79             if 0<=i+acm-1 and 0<=j+bcam-1:
80                 if topology == 4:
81                     if not ((a==0 and b==0) or (a== -1 and b== -1) or (a== -1 and b== 1) or (a== 1 and b== -1) or (a== 1 and b== 1)):
82                         L.append((a, b))
83                 # antoi a toi de jour
84                 elif topology == 8:
85                     if not (a==0 and b==0):
86                         L.append((a, b))
87             else:
88                 sys.exit("Connectivity must be 4 or 8")
89     return(L)
90
91 # if voxel (i,j) is not burning: return empty list
92 def alive_neighbors_offsets_of_burning_voxel(M,i,j, topology):
93     if M[i][j][0] != burning:
94         return []
95
96     L = get_neighbors_offsets(M, i, j, topology) # neighbor: pair of indices [i,j]
97     P=[]
98     for k in range(len(L)):
99         # coords of the neighbors
100         a=L[k][0]; b=L[k][1]
101         if M[i+a][j+b][0] == alive:
102             P.append(L[k])
103     return P
104
105 ## NB: neighbors presented as tuples [i,j] not lists [i,j], to make them hashable in sets
106 #####
107 class Fire_simulation:
108
109     # create the forest matrix M; set the simulation parameters
110     def __init__(self, options):
111         self.options = options
112
113         self.num_trees_total = 0
114         self.wind = [0, 0] # wind: default is no wind
115
116         self.obufname_prefix = "" # prefix used for the output files
117         self.dfname_stats = "" # filename to dump stats
118         self.dfname_pict = "" # filename to dump images
119
120         self.n_hat_estimation = [] # list of pairs of integers to estimate n: see below

```

```

120     self.p_hat_estimation = [] #list of pairs of integers to estimate p: see below
121
122     # prepares self.M_forest, and counts the total number of trees
123     def get_forest_matrix(self, rgb_matrix):
124         self.num_trees_total = 0
125         n = len(rgb_matrix)
126         m = len(rgb_matrix[0])
127         #self.M_forest = np.zeros((n, m, 2), dtype="uint8")
128         self.M_forest = np.zeros((n, m, 2), dtype="int16")
129
130         for i in range(n):
131             for j in range(m):
132                 keep_tree = True
133                 a = random.randint(0,100) # percentage
134                 if a < 100*self.options.trim_proba:
135                     keep_tree = False
136
137                 if rgb_matrix[i][j][0] == rgb_alive[0] and keep_tree:
138                     self.M_forest[i][j] = [alive,0]
139                     self.num_trees_total += 1
140                 else:
141                     self.M_forest[i][j] = [notree, 0]
142
143         print("Image n m size num-trees:", n, m, n*m, self.num_trees_total)
144
145     # collect all simulation files from the current directory
146     # stats
147     # Format for a stats file is:
148     #id proba iteration burning_trees burned_trees_total burned_trees_total_perc
149     # run-id 0.35 1 1.4 0
150     def stats_burning(self):
151         cmd = "ls %s/*-stats.txt" % self.options.odir
152         files = os.popen(cmd).readlines()
153         results = []
154         proba_to_fraction = dict()
155         for afile in files:
156
157             lines = open(afile.rstrip()).readlines()
158             if len(lines)==1: # header only found: nothing has been dumped
159                 continue
160
161             # from line, retrieve run_id + proba + fraction of burned trees
162             last_line = lines[-1].rstrip()
163             aux = re.split(" ", last_line) # split the last line using blanks: we expect 5 numbers
164             simul_id = int(aux[0])
165             proba = float(aux[1])
166             fraction = float(aux[2])
167
168             if proba in proba_to_fraction:
169                 proba_to_fraction[proba] += fraction
170             else:
171                 proba_to_fraction[proba] = fraction

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```

167
168     if proba in proba_to_fraction:
169         proba_to_fraction[ proba ].append(fraction)
170     else:
171         proba_to_fraction[ proba ] = [fraction]
172
173 # for each proba value: pick the median fraction
174 for proba in proba_to_fraction.keys():
175     m = statistics.median( proba_to_fraction[proba] )
176     results.append([proba, m])
177
178 xs = [r[0] for r in results]
179 ys = [r[1] for r in results]
180 plt.plot(xs, ys, '--bo')
181 plt.xlabel('Probabilite')
182 plt.ylabel('% arbres brules')
183
184 dfname = "%s/%s-burned-trees-topo%s-trim%.2f-res.png" % \
185     (self.options.odir, self.ofname_prefix, self.options.topo, self.options.trim_proba)
186 plt.savefig(dfname)
187 plt.clf()
188 # plt.show()
189
190 cmd = "cp %s ~/attach/tipe" % dfname
191 os.system(cmd)
192
193 def stats_p_hat(self):
194     proba_to_fraction = dict()
195
196     xs = []; ys = []; zs = []
197     lines = open(self.dfname_hat).readlines()
198     for line in lines:
199         aux = re.split("\s+", line.rstrip())
200         proba = float(aux[0])
201         phat = float(aux[1])
202         if proba in proba_to_fraction:
203             proba_to_fraction[ proba ].append(phat)
204         else:
205             proba_to_fraction[ proba ] = [phat]
206
207     tmp = []
208     for proba in proba_to_fraction.keys():
209         tmp.append( (proba, statistics.median(proba_to_fraction[proba])) )
210     ord = sorted(tmp)
211     for t in ord:
212         xs.append(t[0])
213         ys.append(t[1])
214         zs.append(t[0])
215
216 # linear regression

```

```

216 # linear regression
217 ls = []
218 slope, intercept, r_value, p_value, std_err = stats.linregress(xs, ys)
219 print("slope and r-squared:", slope, r_value**2)
220 for x in xs:
221     ls.append(intercept + slope*x)
222
223 # plot: simulation
224 plt.plot(xs, ys, '--bo', color='r', label='Simulation') # Simulation
225 # plot: linear regression
226 plt.plot(xs, ls, color='r', label='Regression lineaire')
227 # plot: y=x for reference
228 plt.plot(xs, xs, color='g', label='y=x')
229
230 plt.xlabel('Proba')
231 plt.ylabel('Estimation')
232
233 plt.legend()
234 dfname = "%s/%s-ML-estimation-topo%s-trim%.2f-res.png" % \
235     (self.options.odir, self.ofname_prefix, self.options.topo, self.options.trim_proba)
236 plt.savefig(dfname)
237 plt.clf()
238 # plt.show()
239
240 cmd = "cp %s ~/attach/tipe" % dfname
241 os.system(cmd)
242
243 # return a pair (number of burned trees, new matrix)
244 def one_iteration(self, iteration):
245     Mpl = self.M_forest # M plus one: forest at the nex iteration
246     n=len(self.M_forest); m=len(self.M_forest[0])
247
248     burned_trees = 0
249     burning_trees = 0
250
251     # now compute for this iteration: #new_burning #candidate
252     candidates = set()
253     burning_new = set()
254
255     for i in range(n):
256         for j in range(m):
257             if self.M_forest[i,j,0] == burning:
258                 neighbors_offsets = alive_neighbors_offsets_of_burning_voxel(self.M_forest, i, j, self.options.
259
260                 # tree is burning, but was not lit during this iteration
261                 if self.M_forest[i,j,1] != iteration:
262                     for x in neighbors_offsets:
263                         a = x[0]; b = x[1]
264
265                 candidates.add((ias, iah))

```

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265     candidates.add( (i+a, j+b) )
266
267     # fire transmission proba is the sum of the default proba + contribution of the wind;
268     # the latter is the dot product between offset vector and the wind vector
269     # if success: the neighbor will burn too
270     r = random.randint(1,100)
271     if r <= (self.options.p*100+ 10*(a*self.wind[0]+b*self.wind[1])):
272         burning_new.add( (i+a,j+b) )
273         Mpl[i+a,j+b]=[burning, iteration]
274         self.M_rgb[i+a,j+b]=rgb_burning
275         burning_trees += 1
276
277     # tree burned during self.burning_time steps: dead
278     if iteration-self.M_forest[i,j,1] >= self.options.burning_time:
279         Mpl[i][j][0] = burned
280         self.M_rgb[i][j] = rgb_burned
281         burned_trees += 1
282
283     # update the forest data structure for the next iteration
284     msg = "iteration - burning trees - burned trees: %s %s %s" % (iteration, burning_trees, burned_trees)
285     #print(msg)
286
287     for i in range(n):
288         for j in range(m):
289             self.M_forest[i,j]=Mpl[i,j]
290
291     # record the information to estimate p_hat
292     if burning_trees != len(burning_new):
293         sys.exit("problem")
294     self.p_hat_estimation.append( [len(burning_new), len(candidates) ] )
295     return (burning_trees, burned_trees, Mpl)
296
297
298 #n= taille du carré, p= probabilité de transmission, d=nombre de départs de feu, t=nombre de tours durant les
299 def simulation(self):
300     n=len(self.M_forest); m=len(self.M_forest[0])
301     msg = "Running iteration on matrix of size %s and %s for %s voxels" % (n,m,n*m)
302     print(msg)
303
304     c = n//2; d = m//2
305     self.M_forest[c,d] = [burning,0]
306     self.M_forest[c+1, d] = [burning,0]
307     self.M_forest[c, d+1] = [burning,0]
308     self.M_forest[c+1, d+1] = [burning,0]
309
310     iteration=1
311     burned_trees_total = 0
312
313     f=open(self.dfname stats, "w") # open file to append a line
314     f.write("#nrnha iteration burning trees burned trees burned trees burned trees total burned trees total nrn\n")

```



```

313 f=open(self.dfname_stats, "w") # open file to append a line
314 f.write("#proba iteration burning_trees burned_trees burned_trees_total burned_trees_total_perc\n")
315 f.close()
316
317 while True:
318     (burning_trees, burned_trees, Mpl) = self.one_iteration(iteration)
319     # print("Iter burning_trees, burned_trees", iteration, burning_trees, burned_trees)
320     burned_trees_total += burned_trees
321
322     burned_perc = 100.0*burned_trees_total / self.num_trees_total
323     if burning_trees == 0:
324         break
325
326     # store image
327     # output_filename = "forestM-windx%s-windy%s-iteration%s.png" % (self.wind[0], self.wind[1], iteration)
328     # X = Image.fromarray(Mpl)
329     # X.save(output_filename)
330
331     if self.options.picts:
332         X = Image.fromarray(self.M_rgb)
333         self.dfname_pict = "%2f-iteration%s-pict.png" % (self.options.p, iteration)
334         X.save(self.dfname_pict)
335
336     # update statistics
337     f=open(self.dfname_stats, "a") # open file to append a line
338     line = "%d %2f %s %s %s %2.f" % \
339           (self.options.id, self.options.p, iteration, burning_trees, burned_trees, burned_perc)
340     print("Simul-id / proba / iteration / burning trees / burned trees:", line)
341     f.write(line + "\n")
342     f.close()
343
344     iteration = iteration+1
345
346     # when done: store the last pict in any case
347     X = Image.fromarray(self.M_rgb)
348     X.save(self.dfname_pict_final)
349
350     # at least 2 iterations needed
351     if iteration == 1:
352         return
353
354     # estimation of the proba from the trees reached / starting to burn at each iteration
355     nn = 0; nm = 0
356     for k in range(0, len(self.p_hat_estimation)):
357         nn += self.p_hat_estimation[k][0] # new burning
358         nm += self.p_hat_estimation[k][1] # candidates
359     p_hat = float(nn)/nm
360     print("Estimation: ", p_hat)
361
362     f=open(self.dfname_nhat, "a") # nhat file to append a line

```

```

362 f=open(self.dfname_hat, "a") # open file to append a line
363 line = "%.2f %.2f" % (self.options.p, p_hat)
364 f.write(line + "\n")
365 f.close()
366
367
368 def run(self):
369     (dd, ff) = os.path.split(self.options.fname)
370     self.ofname_prefix = re.sub("\.lw(3)", "", ff); # name of the file containing the image
371
372     # output directory: exists, or create
373     if self.options.odir:
374         if not os.path.exists(self.options.odir):
375             sys.exit("You passed a directory which does not exist")
376     else:
377         # prepare the prefix of output filenames
378         self.options.odir = "%s-topo%s-wind%s-windy%s-trim%.2f" % \
379             (self.ofname_prefix, self.options.topo, self.wind[0], self.wind[1], self.options.trin_proba)
380
381     # run mode only: if self.options.odir pre-exists, remove and re-create
382     if self.options.mode == "run" and os.path.exists(self.options.odir):
383         cmd = "rm -rf %s" % self.options.odir; print(cmd); os.system(cmd)
384         cmd = "mkdir %s" % self.options.odir; print(cmd); os.system(cmd)
385
386     self.dfname_stats = "%s/proba%.2f-id%s-stats.txt" % (self.options.odir, self.options.p, self.options.p)
387     self.dfname_pict_final = "%s/proba%.2f-id%s-pict.png" % (self.options.odir, self.options.p, self.options.p)
388     self.dfname_hat = "%s/p-hat.txt" % self.options.odir
389
390     # run the simulation
391     if self.options.mode == "run":
392         # directory into which results are stored
393         self.M_rgb = get_rgb_matrix(self.options.fname)
394         self.get_forest_matrix(self.M_rgb)
395         self.simulation()
396     # run the stats
397     elif self.options.mode == "stats":
398         self.stats_burning()
399         self.stats_p_hat()
400     else:
401         print("Provide the option run for the simulation, and stats for the statistics")
402
403
404 # =====
405 # Options of the simulation in the command line of the shell
406 parser = argparse.ArgumentParser(description='My parser')
407
408 parser.add_argument("-f", "--fname", dest="fname", default="data/foret-ciel-small.jpg", help="Image filename")
409 parser.add_argument("--trim", dest="trim_proba", type=float, default=0.0, help="Trim proba. If 0 (default), no")
410
411 parser.add_argument("-n", "--nproba", dest="n", default=0.2, type=float, help="Fire propagation probability")

```

```

381 if self.options.mode == "run" and os.path.exists(self.options.odir):
382     cmd = "rm -rf %s" % self.options.odir; print(cmd); os.system(cmd)
383     cmd = "mkdir %s" % self.options.odir; print(cmd); os.system(cmd)
384
385 self.dfname_stats = "%s/proba%.2f-id%s-stats.txt" % (self.options.odir, self.options.p, self.options.id)
386 self.dfname_pict_final = "%s/proba%.2f-id%s-pict.png" % (self.options.odir, self.options.p, self.options.id)
387 self.dfname_phat = "%s/p-hat.txt" % self.options.odir
388
389
390 # run the simulation
391 if self.options.mode == "run":
392     # directory into which results are stored
393     self.M_rgb = get_rgb_matrix(self.options.fname)
394     self.get_forest_matrix(self.M_rgb)
395     self.simulation()
396 # run the stats
397 elif self.options.mode == "stats":
398     self.stats_burning()
399     self.stats_p_hat()
400 else:
401     print("Provide the option run for the simulation, and stats for the statistics")
402
403
404 # =====
405 # Options of the simulation in the command line of the shell
406 parser = argparse.ArgumentParser(description="My parser")
407
408 parser.add_argument("-f", "--fname", dest="fname", default="data/foret-ciel-small.jpg", help="Image filename")
409 parser.add_argument("--trim", dest="trim_proba", type=float, default=0.0, help="Trim proba. If 0 (default), no trim")
410
411 parser.add_argument("-p", "--proba", dest="p", default=0.3, type=float, help="Fire propagation probability")
412 parser.add_argument("-b", "--burning_time", dest="burning_time", default=3, type=int, help="Burning time")
413 parser.add_argument("-t", "--topo", dest="topo", default=4, type=int, help="Connectivity of a pixel: 4 or 8 neighbors")
414
415 parser.add_argument("--odir", dest="odir", help="Output directory name for the results")
416 parser.add_argument("-i", "--id", dest="id", type=int, default=0, help="Simulation id when running repeats")
417 parser.add_argument("--pict", action="store_true", default=False, dest="picts", help="Store pictures at every step")
418
419 parser.add_argument("-m", dest="mode", help="Mode: run or stats")
420
421 options = parser.parse_args()
422
423 # The simulation
424 fire = Fire_simulation(options) # create the instance of the simulation
425 fire.run() # run the simulation
426
427 firesim.py
428 Displaying firesim.py.

```

```

8 import math
9 import numpy as np
10 from scipy.integrate import odeint
11 from random import *
12 import matplotlib.pyplot as plt
13
14 #constantes
15 taux_combustion=0.0001 #taux de combustion
16 p = 450 # KG/m3, masse volumique du sapin
17 h0 = 0.2 # tige de 10 centimetre de haut
18 r0 = h0/10
19 C_l= p*math.pi*(h0/10)**2*taux_combustion
20 T0 = 500 # k, température ambiante
21 Tig = 500 #température d'embrassement de la pelouse
22 Cp = 1500 #capacité thermique du sapin
23 s= 5.67 *10**(-8) # constante de steffan Boltzmann
24 e=0.05 #emissivite, comprise entre 0 et 1
25 Ti = 1500 #température de l'incendie et donc de la tige enflammée a t=
26 msol= 1 # parallelepiped de sol de 1kg
27 csol = 0.00016 # capacite thermique de la pelouse
28 h=5 #coefficient de transfert thermique
29
30 ##### COurbe 1
31
32 #masse du cylindre en fonction du temps
33 def hauteur_cylindre(t):
34     if h0 - taux_combustion*t >= 0 :
35         return (h0 - taux_combustion*t)
36     else :
37         return 0
38
39 def masse_cylindre (t) :
40     m0 = 4*math.pi*r0**2*h0
41     return (m0-C_l*t)

```

```

33 def hauteur_cylindre(t):
34     if h0 - taux_combustion*t >= 0 :
35         return (h0 - taux_combustion*t)
36     else :
37         return 0
38
39 def masse_cylindre (t) :
40     m0 = 4*math.pi*r0**2*h0
41     return (m0-C_1*t)
42     """
43     if m0 - C_1*t >= 0 :
44         return m0 - C_1*t
45     else :
46         return 0
47     """
48
49 def surface_cylindre (t):
50     return 2*math.pi*r0*(r0+hauteur_cylindre(t))
51
52 def modell (T,t) :
53     dTdt = - (surface_cylindre(t)/(masse_cylindre(t)*Cp)) * (s*e*(T**4
54
55 temps = np.linspace(0,20,20000) # tableaux des temps, 10 milles valeur
56 valeurs_T = odeint(modell, Ti, temps ) # obtention de la temperature d
57
58
59 #print (valeurs_T)
60 #print (len(valeurs_T))
61
62 def Temperature_tige(t):
63     n=int(t/0.002)
64     #print (valeurs_T[n][0])
65     return valeurs_T[n][0]
66

```

```

54
55 temps = np.linspace(0,20,20000) # tableaux des temps, 10 milles valeur
56 valeurs_T = odeint(modell1, Ti, temps ) # obtention de la temperature d
57
58
59 #print (valeurs_T)
60 #print (len(valeurs_T))
61
62 def Temperature_tige(t):
63     n=int(t/0.002)
64     #print (valeurs_T[n][0])
65     return valeurs_T[n][0]
66
67 Temperature_tige_liste = [Temperature_tige(t) for t in temps[:20000]]
68
69
70 def model2 (Ts,t):
71     terme1=s*e*(Temperature_tige(t)**4-T0**4)
72     terme2=h*(Temperature_tige(t)-T0)
73     dTsdt = 0.25*(1/(msol*csol))*(surface_cylindre(t)/(masse_cylindre(
74     return dTsdt
75
76
77 valeurs_Tsol = odeint(model2,T0,temps) #initialement le sol est a tempe
78
79 def Temperature_sol(t):
80     n=int(t/0.002)
81     #print (valeurs_T[n][0])
82     return valeurs_Tsol[n][0]
83
84 Temperature_sol_liste = [Temperature_sol(t) for t in temps[:20000]]
85
86
87 ##### Courbe 2

```

```

203
204
205 plt.plot (temps, Temperature_tige_liste, label='0.1m' )
206 plt.plot (temps, Temperature_tige_liste_2, label='0.5m')
207 plt.plot (temps, Temperature_tige_liste_3, label='1m')
208 plt.xlabel('Temps (s)')
209 plt.ylabel('Température Tige (K)')
210 plt.legend()
211 plt.show()
212
213
214 #print (Temperature_sol_liste, len(Temperature_sol_liste))
215
216 tableau_tig = y1 = [Tig for i in temps] # tableau de T=Tig cste
217 plt.plot (temps, Temperature_sol_liste_3, label='0.1m')
218 plt.plot (temps, Temperature_sol_liste_2, label='0.5m')
219 plt.plot (temps, Temperature_sol_liste, label='1m')
220 plt.plot(temps,tableau_tig, label="Température d'ignition")
221 plt.xlim([0, 18])
222 plt.ylim([0,1500 ])
223 plt.xlabel('Temps (s)')
224 plt.ylabel('Température Sol (K)')
225 plt.legend()
226 plt.show()
227
228
229
230
231
232
233
234
235
236

```