1 Category Partition Method

1.1 Prerequisites Consideration

1.1.1 Type of data structure

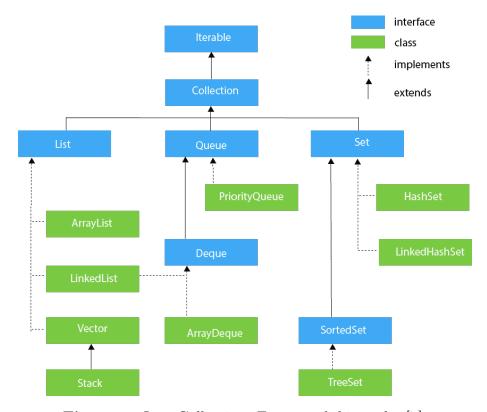


Figure 1: Java Collections Framework hierarchy [7].

As shown in **Figure 1**, **Collection** is an interface that is implemented by three different sub-interfaces, and each sub-interface is extended by different data structure classes. Therefore, it is worth to investigate the relationship between the type of data structure used and the output of the testing implementation.

1. List:

- (a) ArrayList, LinkedList, and Vector implement the List interface. The main difference between them is their implementation which causes different performance for different operations [1, 8, 12].
- (b) Both Collections.sort and Collections.rotate use interface over concrete types for the list parameter. This implies that both methods will only call methods that are defined by the List interface (so no ArrayList etc. specific methods).

Hence, assume that ArrayList, LinkedList, and Vector have been correctly implemented, the testing results of Collections.sort and Collections.rotate should not be affected by the type of data structure used.

2. Collection:

(a) List, Queue, and Set are fundamentally different from each other in terms of storing and manipulating the data. One crucial difference is that Set does not

allow duplicate elements [11], which means that there will be certain categories that are not applicable when the input coll is a Set.

(b) Collections.min uses interface over concrete types for the coll parameter, which implies that the min method will only use methods that are defined by the Collection interface.

Assume that List, Queue, and Set have been correctly implemented, the testing results of min should not be affected by the type of data structure used as well.

1.1.2 Type of elements

Another aspect to consider is the type of the elements stored in the List or Collection. Since, all elements must be an instance of a class that implements the Comparable interface [4], the correctness of Collections.sort and Collections.min is then dependent on the implementation of the compareTo method.

The **premise** for this assessment is that all classes that implemented the Comparable interface have defined their respective compareTo method correctly, otherwise it would have **contradict** with the assumption for the output result of each test case. Hence, it is assumed that the type of elements used in the testing (e.g. Integer, Double, Date etc.) would not affect the test results, thus it would not be taken into consideration as one of the category partition for test inputs.

Based on this statement, the category partitions and metamorphic relations will be more focused on investigating and modifying the **structure** rather than the **content** of the List or Collection.

1.2 Parameter: List

N.B. All elements in the list must be an instance of a class that implements the Comparable interface and must be mutually comparable.

Category L1 Empty list

Input: list = []

Reason: One of the edge cases of the List interface. Given this as the input, both Collections.sort and Collections.rotate should return an empty list as the output.

Category L2 Single element in the list

Input: list = [x]

Reason: One of the edge cases of the List interface. The output returned by both Collections.sort and Collections.rotate should be the same as the input.

Category L3 More than one element in the list

Input: list = $[x_0, x_1, ..., x_n]$ for n > 1, where n is the total number of elements in the list

Reason: The is the minimum viable case for testing the actual functionality of both Collections.sort and Collections.rotate. This is the base form that is used to define other variants of the input (Category L4 - L7).

Category L4 Repeated elements in the list

Input: list = $[x_0, x_1, ..., x_n]$ for n > 1. In addition, there exists some a, b for all $0 \le a, b \le n$, the value of x_a is equal to x_b .

Reason:

- 1. This is to test the stability of the Collections.sort sorting algorithm. The sorting algorithm should sort the repeated elements in the same order that they appear in the input.
- 2. This is to test that Collections.rotate only modifies the position of the elements. The value of each element should not affect the final output.

Category L5 List contains elements of different class

Input: list = $[x_0, x_1, ..., x_n]$ for n > 1, there exists some i, j such that for all $0 \le i, j \le n$, $i \ne j$, the type of $x_i \ne$ type of x_j .

Reason: This is a special category for Collections.rotate. Since the purpose of Collections.rotate is to modify the index of each element in the list, the actual value of each element should have no significant effect for the method. Therefore, the rotate method should work correspondingly when the list contains elements of different types.

Category L6 List is sorted in ascending natural order of its elements

Input: list = $[x_0, x_1, \ldots, x_n]$ for n > 1, where the list is arranged according to the natural ordering [4] of its elements such that $x_k \leq x_{k+1}$ for all $0 \leq k \leq n$. The list can contain repeated elements.

Reason: This is to test the sorting stability of Collections.sort. Since the input list is already sorted, then the elements in the output list should have the same order as the input list.

Category L7 List is sorted in descending natural order of its elements

Input: list = $[x_0, x_1, ..., x_n]$ for n > 1, where the list is arranged according to the reverse natural ordering [4] of its elements such that $x_k \ge x_{k+1}$ for all $0 \le k < n$.

Reason: This is the inverse case of Category L6, where the input list is sorted in reverse order. The aim is to test the sorting stability of Collections.sort and also ensure that it can handle the cases where certain parts of the list (i.e. sub-list) are inversely sorted.

Category L8 List size is large

Input: list = $[x_0, x_1, ..., x_n]$ for n > 200

Reason: According to the documentation of Collections.rotate [3], the method uses two different algorithms depending on the list size (another condition is related to RandomAccess interface, which is not considered). The aim is to validate that both algorithms are able to correctly rotate the input list by the specified distance.

1.3 Parameter: distance

Category D1 Negative number

Input: distance < 0</pre>

Reason: To ensure that the Collections.rotate method will work with negative distance input by covering the negative domain of int data type.

Category D2 Zero

Input: distance == 0

Reason: 0 is the default value of int data type in Java, and also the starting index value of List. This is to ensure that the Collections.rotate method will work when the input distance is zero.

Category D3 Positive number

Input: distance > 0

Reason: To ensure that the Collections.rotate method will work with positive distance input by covering the positive domain of int data type.

Category D4 Larger than list size

Input: distance > list.size()

Reason: A derivative of Category D3. Since the rotate method uses modulo operation on the input distance [3], this is to test whether the behaviour of inputting a distance larger than list.size() is the same as inputting the value of distance % list.size() [3].

Category D5 Equal to list size

Input: distance == list.size()

Reason: This is to validate that if the distance is equal to the list.size(), then Collections.rotate will return the same output as the input.

Category D6 Smaller than list size

Input: distance < list.size()</pre>

Reason: A derivative of Category D1 - D3 and the inverse case of Category D4. This is to validate the assumption that there exists some d for all d > list.size() and n for all n < list.size() such that rotate(list, d) == rotate(list, n).

Category D7 Equal to minimum boundary value of int

Input: distance == Integer.MIN_VALUE

Reason: The minimum value an int can have in Java is -2^{31} [6]. The aim is to validate the assumption that if Collections.rotate works for the minimum value of int, then it should work correctly for any value larger than the minimum value.

Category D8 Equal to maximum boundary value of int

Input: distance == Integer.MAX_VALUE

Reason: The maximum value an int can have in Java is $2^{31} - 1$ [5]. The aim is to validate the assumption that if Collections.rotate works for the maximum value of int, then it should work correctly for any value smaller than the maximum value.

1.4 Parameter: Collection

N.B. All elements in the collection must be an instance of a class that implements the Comparable interface and must be mutually comparable.

Category C1 Single element in collection

Input: $coll = \{x\}$

Reason: Edge case of the Collections.min method. The method should only return the single element as the minimum element of the given collection.

Category C2 More than one element in collection

Input: coll = $\{x_0, x_1, ..., x_n\}$ for n > 1

Reason: To test whether the Collections.min method is able to find and return the minimum element of the given collection.

Category C3 Repeated elements in collection

Input: coll = $\{x_0, x_1, \dots, x_n\}$ for n > 1. In addition, there exists some a, b for all $0 \le a, b \le n$, $a \ne b$, the value of x_a is equal to x_b .

Reason: To test whether the Collections.min method is able to handle repeated elements and correctly return the minimum element of the given collection.

Category C4 Repeated minimum elements in collection

Input: coll = $\{x_0, x_1, \ldots, x_n\}$ for n > 1. In addition, there exists some a, b for all $0 \le a, b \le n$, $a \ne b$, the value of x_a is equal to x_b and both x_a and x_b are the minimum elements in the collection.

Reason: A derivative of Category C3 to test the stability of Collections.min method. It is expected that the method will treat the repeated minimum elements as the same element and return correctly.

Category C5 Collection contains the minimum possible value of the class

Input: coll = $\{x_0, x_1, \dots, x_n\}$ for n > 1, and there exists a k where $0 \le k \le n$ such that x_k is the minimum possible value of the element's class.

Reason: To cover the boundary case of Collections.min, and to test whether the method always return the minimum possible value of the class when the given collection contains it.

Category C6 Collection is in ascending natural order of its elements

Input: coll = $\{x_0, x_1, \ldots, x_n\}$ for n > 1, where the collection is arranged according to the natural ordering [4] of its elements such that $x_k \leq x_{k+1}$ for all $0 \leq k \leq n$. The collection can contain repeated elements.

Reason: Since the given collection is already sorted, then the minimum element returned should have the same value as first element of the collection.

Category C7 Collection is in descending natural order of its elements

Input: coll = $\{x_0, x_1, \ldots, x_n\}$ for n > 1, where the collection is arranged according to the natural ordering [4] of its elements such that $x_k \geq x_{k+1}$ for all $0 \leq k < n$. The collection can contain repeated elements.

Reason: The inverse case of **Category C6**. Since, the given collection is sorted in reverse order, then the minimum element returned should have the same value as the last element of the collection.

2 Test Cases

- 2.1 Collections.sort(List<T> list)
 - 1. Test Case 1

Categories: L2

Input: list = [1]

Reason: For testing the edge case

2. Test Case 2

Categories: L3 \wedge L4

Input: list = [6, 8, 2, 4, 7, 5, 3, 2, 9]

Reason: To test the stability of the method. After the list is sorted, the relative order of the Integer 2 will not be changed (i.e. the one came before the other in the input will also come before the other in the output.)

3. Test Case 3

Categories: L3 \wedge L7

Input: list = [9, 8, 7, 6, 5, 4, 3, 2, 1]

Reason: To test the sorting capability when there are no partially sorted elements in the list

- 2.2 Collections.rotate(List<?> list, int distance)
 - 1. Test Case 1

Categories: L1, D2 \wedge D5

Input: list = [], distance = 0

Reason: For testing the edge case

2. Test Case 2

Categories: L3 \wedge L5, D3 \wedge D4 \wedge D8

Input: list = [1, 2, 'a', 'b', 3.7, 4, "str"], distance = $2^{31} - 1$

Reason:

- (a) To validate and test the assumption that this method is not dependent on the value of each element in the list.
- (b) To test the edge case where the distance is the maximum possible value of int data type
- 3. Test Case 3

Categories: L3 \wedge L8, D1 \wedge D6 \wedge D7

Input: list = [1, 2, ..., 200, 201], distance = -2^{31}

Reason:

- (a) To verify the statement stated in the reason of Category L8
- (b) To test the edge case where the distance is the minimum possible value of int data type
- 2.3 Collections.min(Collection<? extends T> coll)
 - 1. Test Case 1

Categories: C1

Input: $coll = \{1\}$

Reason: For testing the edge case

2. Test Case 2

Categories: $C2 \wedge C7$

Input: $coll = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

Reason: A general test case to test the correctness of method under normal circumstances

3. Test Case 3

Categories: $C2 \wedge C3 \wedge C4 \wedge C5$

Input: coll = $\{6, -2^{31}, 2, 4, 7, -2^{31}, 5, 3, 2, 9\}$

Reason: To test the edge where the collection contains the minimum possible value of the element's class (in this case -2^{31})

3 Metamorphic Relations

- 3.1 Collections.sort(List<T> list)
 - 1. Reverse the original input list

Input transformation: Collections.reverse(listTransformed)

Relation after transformation: listTransformed == list

2. Double the size and content of original input list by adding itself

Input transformation: listTransformed.reverse(listTransformed)

Relation after transformation:

- (a) listTransformed.size() == 2 * list.size()
- (b) listTransformed[2n] == list[n]
- (c) listTransformed[2n + 1] == list[n]
- 3.2 Collections.rotate(List<?> list, int distance)
 - 1. Reverse the original input list, and convert the distance to opposite sign after modulo with the list size

Input transformation:

- (a) Collections.reverse(listTransformed)
- (b) distanceTransformed = -(distance % list.size())

Relation after transformation: listTransformed is the reverse of list. After reversing listTransformed again, listTransformed == list

2. Decrease distance to observe the index different of each element

Input transformation: distanceTransformed < distance % list.size()</pre>

Relation after transformation: Every element in listTransformed is Δd indices "behind" list, where Δd is the difference between distanceTransformed and distance % list.size()

N.B.

- 1. For both relations, if the original list is empty, then distanceTransformed = 0.
- 2. Example for second relation: rotate([1,2,3,4,5], 3) will yield [3,4,5,1,2]; After input transformation, rotate([1,2,3,4,5], 1) will yield [5,1,2,3,4].
- 3.3 Collections.min(Collection<? extends T> coll)
 - 1. Add an element smaller than the minimum element in the original collection

Input transformation: collTransformed.add(y), where y is a random generated element

Relation after transformation: outputTransformed < output

2. Remove all minimum elements from the original collection

Input transformation: collTransformed.removeIf(output::equals)

Relation after transformation: outputTransformed > output

N.B.

- 1. For the first relation, if the minimum element in the original collection is already the minimum possible element for the class, then the new element added is equal to the minimum element in the original collection. The relation will then be outputTransformed == output.
- 2. For the second relation, if all elements in the original collection are the minimum elements (i.e. duplicate), then removing them will cause collTransformed to be an empty collection. In this case, the relation is outputTransformed == output as there are no elements greater than the minimum element in the original collection.

4 Remarks

4.1 Outcome of the Tests

All three methods have managed to pass all their respective test cases, and all transformed outputs are proved to obey their respective metamorphic relation. As a result, it is suggested that all three methods are correct and complete.

- 1. Collections.sort: The method is able to rearrange the original list into ascending order, according to the natural ordering of its elements for all test cases. For all transformed inputs, the method is able to satisfy the expected relations.
- 2. Collections.rotate: The two metamorphic relations have shown that this method alters the index but not the value of each element in the list. After the rotation, all elements in the list are preserved, but each of them is moved by the specified distance.
- 3. Collections.min: This method is assumed to be the least possible one to generate errors as it only performs read operation to find the minimum element [2]. After applying the metamorphic relations to alter the minimum element in the list, the method is still able to find and return the next minimum element in the list.

4.2 Likelihood of Faults

After searching the CVE archive for Oracle JDK [10] and Oracle JRE [9], no vulnerabilities that are related to these three methods have been found. Hence, it is suggested that all three methods are well implemented by the developers and have a low likelihood of failure.

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