

## Lab 11/28

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1. Please write a function **int gcd(int a, int b)** to compute the gcd of a and b. In this problem you are required to output the gcd of a set of number. Please write a main program to let user continuously input the number in the set and stop when input data is Ctrl+Z or Ctrl+D.

Example: 72 96 24 66 6 18 12 30 60 48 -> 6

2147483647 1 2147483647 2147483647 2147483647 -> 1

2. There are N boxes with balls in them. All the balls have different colors so they are distinguishable. First box has M balls, 2nd box has M+1 balls, 3rd box has M+2 balls and so on. So Nth box have N + M - 1 balls. You choose one of the N boxes and take M balls from this. How many numbers of ways are there to do it? For each test case input two integers N, M and output the result. Program stops when input data is Ctrl+Z or Ctrl+D.

In this problem, you will need to write the function **int C(int n, int k)** that has two parameters n and k of type int. The function returns the result of the equation:

$$C_k^n = \frac{n!}{(n-k)!k!}$$

Note that, with the formula  $C(m, k+1) + C(m, k) = C(m+1, k+1)$  you can complete the main program without for-loop.

Example: 9 9 -> 43758

3. Write a function **int powmod(int n, int k, int m)** to compute  $n^k \% m$ . For k is very big, you can't multiple k times to complete it. Following is the algorithm:

$$a = b * c \rightarrow a \% k = ((b \% k) * (c \% k)) \% k$$

$$a^2 \% k = ((a \% k) * (a \% k)) \% k$$

$$a^4 \% k = ((a^2 \% k) * (a^2 \% k)) \% k$$

$$a^8 \% k = \dots\dots$$

$$111_{\text{dec}} = 1101111_{\text{bin}}$$

$$13^{111} \% 113 = (13^{64} * 13^{32} * 13^8 * 13^4 * 13^2 * 13^1) \% 113$$

$$= ((13^{64} \% 113) * (13^{32} \% 113) * (13^8 \% 113) * (13^4 \% 113) * (13^2 \% 113) * (13^1 \% 113)) \% 113$$

Every multiplication must follow by modulo to avoid overflow.

For each test case input three integer n, k, m, and output the result. Program stops when input data is Ctrl+Z or Ctrl+D.

Example: 13 112111 113 -> 87

13 1008112111 113 -> 87