```
1
     // Adam Doussan AD844156 04/13/2017
 2
 3
     public class CombPerm
 4
     {
 5
         // ans needs to be intialized before calling, take.length needs to equal
 6
         // words.length
 7
         public static <T> void genCombs(T[] words, ArrayList<ArrayList<T>> ans,
8
                                           boolean [] take, int depth)
9
         {
10
              if(depth == words.length)
11
              {
12
                  ArrayList<T> temp = new ArrayList<>();
13
14
                  for(int i = 0; i < take.length; i++)</pre>
15
                      if(take[i])
16
                          temp.add(words[i]);
17
18
                  ans.add(temp);
19
                  return;
20
             }
21
22
             take[depth] = true;
             genCombs(words,ans,take,depth+1);
23
24
25
              take[depth] = false;
26
              genCombs (words, ans, take, depth+1);
27
         }
28
29
         // ans & now needs to be intialized before calling, take.length needs to equal
30
         // words.length
31
         public static <T> void genPerms(T[] words, ArrayList<ArrayList<T>> ans,
32
                                           boolean [] take, int depth, ArrayList<T> now)
33
         {
34
             if(depth == words.length)
35
              {
36
                  ans.add(new ArrayList<>(now));
37
                  return;
38
              }
39
40
             for(int i = 0; i < words.length; i++)</pre>
41
              {
42
                  if(!take[i])
43
                  {
44
                      take[i] = true;
45
                      now.add(words[i]);
46
                      genPerms(words, ans, take, depth+1, now);
47
                      now.remove(now.size()-1);
48
                      take[i] = false;
49
                  }
50
              }
51
         }
52
     }
53
54
     // Adam Doussan AD844156 04/11/2017
55
56
     public class Graphs
57
     {
58
         public static void dfs(ArrayList[] graph, boolean [] visited, int v)
59
         {
60
             visited[v] = true;
61
             for(Integer next : ((ArrayList<Integer>[])graph)[v])
62
                  if(!visited[next])
63
                      dfs(graph, visited, next);
64
         }
65
66
         public static int[] bfs(ArrayList[] graph, int v)
67
68
              int n = graph.length;
69
              int [] distance = new int [n];
```

```
71
               Arrays.fill(distance, -1);
 72
               distance[n] = 0;
 73
 74
               Queue<Integer> q = new ArrayDeque<Integer>();
 75
               q.add(v);
 76
 77
              while(!q.isEmpty())
 78
 79
                   int cur = q.remove();
 80
                   for(Integer next : ((ArrayList<Integer>[])graph)[cur])
 81
 82
                       if(distance[next] == -1)
 83
 84
                           distance[next] = distance[cur] + 1;
 85
                           q.add(next);
 86
                       }
 87
                   }
 88
               }
 89
 90
               return distance;
 91
          }
 92
      }
 93
 94
      // Adam Doussan AD844156 04/13/2017
 95
 96
      public class Dijkstras
 97
 98
          final public static int oo = (int) 1e9;
 99
          private static int n;
100
101
          // pass in a value of true to stop if you want early termination for
102
          // destination d, false if you want the entire dist array to be filled in
103
          public static int[] run(ArrayList<Edge>[] g, int s, int d, boolean stop)
104
105
               n = g.length;
106
107
              boolean [] visited = new boolean[n];
108
               int [] dist = new int [n];
109
              Arrays.fill(dist, oo);
110
111
               PriorityQueue<Edge> pq = new PriorityQueue<Edge>();
112
              pq.add(new Edge(s, 0));
113
              dist[s] = 0;
114
115
              while(!pq.isEmpty())
116
117
                   Edge at = pq.remove();
118
                   if(visited[at.e]) continue;
119
                   visited[at.e] = true;
120
121
                   if(stop && at.e == d) return dist;
122
123
                   for (Edge adj : g[at.e])
124
                       if(!visited[adj.e] && adj.w + at.w < dist[adj.e])</pre>
125
                           pq.add(new Edge(adj.e, dist[adj.e] = adj.w + at.w));
126
               }
127
128
               return dist;
129
          }
130
      }
131
132
      class Edge implements Comparable<Edge>
133
      {
134
          int e, w;
135
136
          public Edge(int e, int w)
137
          {
138
               this.e = e; this.w = w;
```

```
139
          }
140
141
          public int compareTo(Edge o)
142
143
               return this.w - o.w;
144
          }
145
      }
146
147
      // Adam Doussan AD844156 04/13/2017
148
149
      public class BellmanFord
150
      {
1.51
           final public static int oo = (int) 1e9;
152
153
          // returns null if there is a negative cycle, edges are directional
154
          public static int[] run(Edge[] eList, int n, int s)
155
           {
156
               int [] dist = new int [n];
157
               Arrays.fill(dist, oo);
158
               dist[s] = 0;
159
160
               for (int i = 0; i < n - 1; i++)
161
                   for(Edge e : eList)
162
                       if(dist[e.v1] + e.w < dist[e.v2])</pre>
163
                            dist[e.v2] = dist[e.v1] + e.w;
164
165
               for (Edge e : eList)
166
                   if(dist[e.v1] + e.w < dist[e.v2])</pre>
167
                       return null;
168
169
               return dist;
170
          }
171
      }
172
173
      class Edge
174
175
          public int v1, v2, w;
176
177
          public Edge(int v1, int v2, int w)
178
          {
179
               this.v1 = v1; this.v2 = v2; this.w = w;
180
          }
181
      }
182
183
      // Adam Doussan AD844156 04/13/2017
184
185
      public class Floyd
186
187
          public static int [][] path;
188
          final public static int oo = (int)1e9;
189
190
          // gets answer without destroying passed in array
191
          public static int [][] run(int [][] adj)
192
           {
193
               int n = adj.length;
194
               int [][] m = copy(adj);
195
               path = new int[adj.length][adj.length];
196
197
               for (int i = 0; i < adj.length; i++)
198
                   for(int j = 0; j < adj.length; j++)</pre>
199
                       if(adj[i][j] != 00)
200
                            path[i][j] = j;
201
                       else
202
                           path[i][j] = oo;
203
204
               for (int k = 0; k < n; k++)
                   for(int i = 0; i < n; i++)</pre>
205
206
                       for (int j = 0; j < n; j++)
207
                            if(m[i][k] != oo && m[k][j] != oo)
```

```
208
                                if(m[i][k] + m[k][j] < m[i][j])</pre>
209
210
                                    m[i][j] = m[i][k] + m[k][j];
211
                                    path[i][j] = path[i][k];
212
                                }
213
214
              return m;
215
          }
216
217
          public static int [][] copy(int [][] a)
218
          {
219
               int [][] res = new int [a.length][a[0].length];
220
                   for (int i = 0; i < a.length; i++)
221
                       for (int j = 0; j < a[0].length; j++)
222
                            res[i][j] = a[i][j];
223
               return res;
224
          }
225
226
          public static ArrayList<Integer> getPath(int i, int j)
227
          {
228
               if(path[i][j] == 00)
229
                   return null;
230
231
              ArrayList<Integer> myPath = new ArrayList<>();
232
233
              myPath.add(i);
234
235
              while(i != j)
236
237
                   i = path[i][j];
238
                   myPath.add(i);
239
               }
240
241
               return myPath;
242
          }
243
      }
244
245
      // Adam Doussan AD844156 05/01/2017
246
247
      public class myFordFulkerson
248
249
          public int n, s, t;
250
          public int [][] g;
251
252
          public myFordFulkerson(int n)
253
254
               this.n = n+2; this.s = n; this.t = n+1;
255
               g = new int [n+2][n+2];
256
          }
257
258
          public void addEdge(int v1, int v2, int cap)
259
260
               g[v1][v2] = cap;
261
          }
262
263
          public int flow()
264
          {
265
               int ans = 0;
266
               int [] prev = new int [n];
267
268
               while (bfs (prev))
269
270
                   int myNext = prev[t];
271
                   int myFlow = g[myNext][t];
272
273
                   while (myNext != s)
274
                   {
275
                       myFlow = Math.min(myFlow, g[prev[myNext]][myNext]);
276
                       myNext = prev[myNext];
```

```
277
                   }
278
279
                   ans += myFlow;
280
                   myNext = t;
281
282
                   while (myNext != s)
283
284
                       int temp = prev[myNext];
285
                       g[myNext][temp] += myFlow;
286
                       g[temp][myNext] -= myFlow;
287
                       myNext = temp;
288
                   }
289
               }
290
291
               return ans;
292
          }
293
294
          public boolean bfs(int[] prev)
295
296
               Queue<Integer> q = new ArrayDeque<>();
297
               boolean [] visited = new boolean [n];
298
299
               q.add(s);
300
               visited[s] = true;
301
302
              while(!q.isEmpty())
303
304
                   int myNext = q.remove();
305
306
                   for(int i = 0; i < n; i++)</pre>
307
308
                       if(!visited[i] && g[myNext][i] > 0)
309
                       {
310
                           visited[i] = true;
311
                           q.add(i);
312
                           prev[i] = myNext;
313
                       }
314
                   }
315
               }
316
317
               return visited[t];
318
          }
319
      }
320
321
      // Credit Arup Guha
322
323
      class FordFulkerson
324
325
          int[][] cap; boolean[] vis; int n, s, t, oo = (int)(1E9);
326
327
          public FordFulkerson(int size) { n = size + 2; s = n - 2; t = n - 1; cap = new
          int[n][n]; }
328
          void add(int v1, int v2, int c) { cap[v1][v2] = c; }
329
330
          int ff()
331
          {
332
               vis = new boolean[n]; int f = 0;
333
               while (true)
334
335
                   Arrays.fill(vis, false);
336
                   int res = dfs(s, oo);
337
                   if (res == 0) break;
338
                   f += res;
339
               }
340
               return f;
341
          }
342
343
          int dfs(int pos, int min)
344
```

```
345
               if (pos == t) return min;
346
               if (vis[pos]) return 0;
347
              vis[pos] = true; int f = 0;
348
349
               for (int i = 0; i < n; i++)</pre>
350
351
                   if (cap[pos][i] > 0) f = dfs(i, Math.min(cap[pos][i], min));
352
                   if (f > 0) { cap[pos][i] -= f; cap[i][pos] += f; return f; }
353
354
               return 0;
355
          }
356
      }
357
358
      // Credit Arup Guha
359
      public class Dinic
360
361
      {
362
          ArrayDeque<Integer> q;
363
          ArrayList<Edge>[] adj;
364
          int n, s, t, oo = (int)1E9;
365
          boolean[] blocked;
366
          int[] dist;
367
368
          public Dinic (int N)
369
370
               n = N; s = n++; t = n++;
              blocked = new boolean[n];
371
               dist = new int[n];
372
373
               q = new ArrayDeque<Integer>();
374
               adj = new ArrayList[n];
375
               for (int i = 0; i < n; ++i)
376
                   adj[i] = new ArrayList<Edge>();
377
          }
378
379
          void add(int v1, int v2, int cap, int flow)
380
381
               Edge e = new Edge (v1, v2, cap, flow);
382
               Edge rev = new Edge (v2, v1, 0, 0);
383
               adj[v1].add(rev.rev = e);
384
               adj[v2].add(e.rev = rev);
385
          }
386
387
          boolean bfs()
388
          {
389
               q.clear();
390
               Arrays.fill(dist, -1);
391
               dist[t] = 0;
392
               q.add(t);
393
394
               while(!q.isEmpty()) {
395
                   int node = q.poll();
396
                   if(node == s)
397
                       return true;
398
                   for (Edge e : adj[node])
399
                   {
400
                       if(e.rev.cap > e.rev.flow && dist[e.v2] == -1)
401
                       {
402
                            dist[e.v2] = dist[node] + 1;
403
                            q.add(e.v2);
404
                       }
405
                   }
406
               }
407
               return dist[s] != -1;
408
          }
409
410
          int dfs(int pos, int min)
411
          {
412
               if(pos == t)
413
                   return min;
```

```
414
               int flow = 0;
415
               for (Edge e : adj[pos])
416
417
                   int cur = 0;
418
                   if(!blocked[e.v2] && dist[e.v2] == dist[pos]-1 && e.cap - e.flow > \frac{0}{1}
419
420
                       cur = dfs(e.v2, Math.min(min-flow, e.cap - e.flow));
421
                       e.flow += cur;
422
                       e.rev.flow = -e.flow;
423
                        flow += cur;
424
425
                   if(flow == min)
426
                       return flow;
427
428
               blocked[pos] = flow != min;
429
               return flow;
430
          }
431
432
          int flow()
433
          {
434
               clear();
435
               int ret = 0;
               while(bfs())
436
437
438
                   Arrays.fill(blocked, false);
439
                   ret += dfs(s, oo);
440
441
               return ret;
442
          }
443
444
          void clear()
445
          {
446
               for(ArrayList<Edge> edges : adj)
447
                   for (Edge e : edges)
448
                       e.flow = 0;
449
          }
450
      }
451
452
      class Edge
453
      {
454
          int v1, v2, cap, flow;
455
          Edge rev;
456
          Edge (int V1, int V2, int Cap, int Flow)
457
458
               v1 = V1; v2 = V2; cap = Cap; flow = Flow;
459
          }
460
      }
461
462
      // Conner 04/29/2017
463
464
      public class TopologicalSort
465
466
          public static ArrayList<Integer> run(Graph g)
467
468
               int degrees[] = new int[g.numVerts];
469
               for(int i = 0; i < degrees.length; i++)</pre>
470
               {
471
                   ArrayList<Integer> tempArr = g.matrix[i];
472
473
                   for(int k = 0; k < tempArr.size(); k++)</pre>
474
                       degrees[tempArr.get(k)]++;
475
               }
476
477
               Queue<Integer> q = new ArrayDeque<Integer>();
478
479
               for(int i = 0; i < g.numVerts; i++)</pre>
480
                   if(degrees[i] == 0)
481
                       q.add(i);
482
```

```
483
               int visited = 0;
484
              ArrayList<Integer> result = new ArrayList<Integer>();
485
486
               while(!q.isEmpty())
487
488
                   int currentEdge = q.poll();
489
                   result.add(currentEdge);
490
491
                   for(int i = 0; i < g.matrix[currentEdge].size(); i++)</pre>
492
                       if(--degrees[q.matrix[currentEdge].get(i)] == 0)
493
                            q.add(g.matrix[currentEdge].get(i));
494
495
                   visited++;
496
               }
497
498
               if(visited != g.numVerts) // cycle
499
                   return null;
500
501
               return result;
502
          }
503
504
      }
505
506
      class Graph
507
508
          int numVerts;
509
          ArrayList<Integer> matrix[];
510
511
          public Graph(int numVerts)
512
513
               this.numVerts = numVerts;
514
              matrix = new ArrayList[numVerts];
515
516
               for(int i = 0; i < matrix.length; i++)</pre>
517
                   matrix[i] = new ArrayList<Integer>();
518
          }
519
520
          public void newEdge (int v1, int v2)
521
          {
522
               matrix[v1].add(v2);
523
          }
524
      }
525
526
      // Conner 04/29/2017
527
528
      public class Kruskals
529
530
          private static int count = 0;
531
          private static int sort = 0;
532
533
          public static Edge[] run(Graph g)
534
535
               Arrays.sort(g.edgeArray);
536
               Edge mst[] = new Edge[g.numVerts];
537
               for(int i = 0; i < g.numVerts; i++)</pre>
538
539
                   mst[i] = new Edge(0,0,0);
540
541
542
               SubTree stArray[] = new SubTree[g.numVerts];
543
               for(int i = 0; i < g.numVerts; i++)</pre>
544
545
                   stArray[i] = new SubTree();
546
                   stArray[i].parent = i;
547
                   stArray[i].rank = 0;
548
               }
549
550
               while(sort < g.numVerts - 1)</pre>
551
```

```
552
                   Edge next = g.edgeArray[count++];
553
554
                   int v1Base = g.findSet(stArray, next.v1);
555
                   int v2Base = q.findSet(stArray, next.v2);
556
                   if(v1Base != v2Base)
557
558
559
                       mst[sort++] = next;
560
                       g.union(stArray, v1Base, v2Base);
561
562
               }
563
              return mst;
564
          }
565
      }
566
567
      class Graph
568
      {
569
          int numVerts;
570
          int numEdges;
571
          Edge edgeArray[];
572
573
          public Graph(int numVerts, int numEdges)
574
          {
575
               this.numVerts = numVerts;
576
               this.numEdges = numEdges;
577
               edgeArray = new Edge[numEdges];
578
               for(int i = 0; i < numEdges; i++)</pre>
579
580
                   edgeArray[i] = new Edge(0,0,0);
581
               }
582
          }
583
          public int findSet(SubTree stArray[], int key)
584
585
              if(stArray[key].parent != key)
586
               {
587
                   stArray[key].parent = findSet(stArray, stArray[key].parent);
588
589
590
               return stArray[key].parent;
591
          }
592
          public void union(SubTree[] stArray, int v1, int v2)
593
594
               int v1Base = findSet(stArray, v1);
595
               int v2Base = findSet(stArray, v2);
596
597
               if(stArray[v1Base].rank < stArray[v2Base].rank)</pre>
598
                   stArray[v1].parent = v2Base;
599
600
               else if(stArray[v2Base].rank < stArray[v1Base].rank)</pre>
601
                   stArray[v2Base].parent = v1Base;
602
               else
603
               {
604
                   stArray[v2Base].parent = v1Base;
605
                   stArray[v1Base].rank++;
606
               }
607
608
          }
609
610
611
      class Edge implements Comparable<Edge>
612
613
               int v1, v2, w;
614
615
              public Edge(int v1, int v2, int w)
616
               {
617
                   this.v1 = v1; this.v2 = v2; this.w = w;
618
               }
619
620
              public int compareTo(Edge e)
```

```
621
               {
622
                   return this.w - e.w;
623
               }
624
625
626
      class SubTree
627
628
          int parent;
629
          int rank;
630
631
      // Adam Doussan AD844156 04/13/2017
632
633
634
      public class MyMath
635
636
          public static long lcm(long a, long b)
637
638
               return a / gcd(a,b) * b;
639
          }
640
641
          public static long gcd(long a, long b)
642
          {
643
               return (b == 0) ? a : gcd(b, a%b);
644
          }
645
646
          public static int MCSS(int [] days)
647
648
               int maxSum = days[0];
649
               int runningSum = days[0];
650
651
               for(int i = 0; i < days.length; i++)</pre>
652
               {
653
                   if(runningSum < 0)</pre>
                        runningSum = 0;
654
655
656
                   runningSum += days[i];
657
658
                   if(runningSum > maxSum)
659
                        maxSum = runningSum;
660
               }
661
662
               return maxSum;
663
          }
664
665
          public static boolean[] primeSieve(int n)
666
667
               boolean[] isPrime = new boolean[n+1];
668
               Arrays.fill(isPrime, true);
669
               isPrime[0] = false;
670
               isPrime[1] = false;
671
672
               for(int i = 2; i*i <= n; i++)</pre>
673
                   if(isPrime[i])
674
                        for(int j = i + i; j <= n; j += i)</pre>
675
                            isPrime[j] = false;
676
677
               return isPrime;
678
          }
679
680
          public static long[] extendedEuclid(long a, long b)
681
682
               if(b == 0)
683
                   return new long []{1,0,a};
684
               else
685
               {
686
                   long q = a / b;
687
                   long r = a % b;
688
                   long [] rec = extendedEuclid(b,r);
689
                   return new long [] {rec[1], rec[0] - q*rec[1], rec[2]};
```

```
690
               }
691
          1
692
693
          public static BigInteger sumOfDivisors(ArrayList<pair> primeFac)
694
695
               BigInteger sum = new BigInteger("1");
696
697
               for(pair a : primeFac)
698
699
                   BigInteger prime = new BigInteger("" + a.prime);
700
701
                   BigInteger temp = prime.pow((int)a.exp + 1).subtract(BigInteger.ONE);
702
                   temp = temp.divide(prime.subtract(BigInteger.ONE));
703
704
                   sum = sum.multiply(temp);
705
               }
706
707
               return sum;
708
          }
709
710
          public static ArrayList<pair> primeFactorize(int n)
711
712
               ArrayList<pair> res = new ArrayList<>();
713
               int div = 2;
714
715
              while(div*div <= n)</pre>
716
717
                   int exp = 0;
718
                   while(n % div == 0)
719
720
                       n /= div;
721
                       exp++;
722
                   }
723
724
                   if(exp > 0) res.add(new pair(div, exp));
725
                   div++;
726
727
728
               if (n > 1) res.add (new pair(n,1));
729
               return res;
730
          }
731
      }
732
733
      class pair
734
735
          public int prime, exp;
736
737
          public pair(int p, int e)
738
          {
739
               prime = p; exp = e;
740
          }
741
      }
742
743
      // Credit Arup Guha
744
      // Cleaned up by Adam Doussan AD844156 04/15/2017
745
746
      public class ConvexHull
747
748
          public static void main(String [] args)
749
750
               Scanner in = new Scanner(System.in);
751
               int cases = in.nextInt();
752
753
               for (int i = 0; i < cases; i++)
754
755
                   int numCase = in.nextInt();
756
                   int numPoints = in.nextInt();
757
                   pt[] pts = new pt[numPoints];
758
```

```
759
                   for (int k = 0; k < numPoints; k++)
760
                       pts[k] = new pt(in.nextInt(), in.nextInt());
761
762
                   pt.ref = getRef(pts, numPoints);
763
764
                   ArrayList<pt> ans = grahamScan(pts, numPoints);
765
               }
766
          }
767
768
          // returns the point in pts with min y breaking tie by min x
769
          public static pt getRef(pt[] pts, int n)
770
771
               pt ans = pts[0];
772
773
               for(int i = 1; i < n; i++)</pre>
774
                   if (pts[i].y \prec ans.y || (pts[i].y == ans.y && pts[i].x \prec
                   ans.x))
775
                       ans = pts[i];
776
777
               return ans;
778
          }
779
780
          public static ArrayList<pt> grahamScan(pt[] pts, int n)
781
           {
782
               Arrays.sort(pts);
783
784
               Stack<pt> st = new Stack<>();
785
               st.push(pts[0]);
786
               st.push(pts[1]);
787
788
               for(int i = 2; i < n; i++)</pre>
789
               {
790
                   pt next = pts[i];
                   pt mid = st.pop();
791
792
                   pt prev = st.pop();
793
794
                   while(!prev.isRightTurn(mid, next))
795
                   -{
796
                       mid = prev;
797
                       prev = st.pop();
798
                   }
799
800
                   st.push(prev);
801
                   if(!prev.isStraight(mid, next)) // deleting collinear points
802
                       st.push (mid);
803
                   st.push(next);
804
               }
805
806
              ArrayList<pt> ans = new ArrayList<>();
807
808
               while(!st.isEmpty())
809
                   ans.add(st.pop());
810
811
               return ans;
812
          }
813
814
      }
815
816
      class pt implements Comparable<pt>
817
      {
818
          public static pt ref;
819
          public int x, y;
820
821
          public pt(int x, int y)
822
          {
823
               this.x = x; this.y = y;
824
          }
825
826
          public pt vect(pt pt2)
```

```
827
          {
828
               return new pt(pt2.x-x, pt2.y-y);
829
          }
830
831
          public double dist(pt pt2)
832
833
               return Math.sqrt(Math.pow(pt2.x-x, 2) + Math.pow(pt2.y-y, 2));
834
          }
835
836
          public int cross(pt pt2)
837
          -{
838
               return x*pt2.y - y*pt2.x;
839
          }
840
          public boolean isRightTurn(pt mid, pt next)
841
842
843
              pt v1 = vect(mid);
844
              pt v2 = mid.vect(next);
845
               return v1.cross(v2) >= 0;
846
847
848
          // used to get rid of collinear points that are already accounted for by
849
          // points on either end
850
          public boolean isStraight(pt mid, pt next)
851
852
               pt v1 = vect(mid);
853
               pt v2 = mid.vect(next);
854
               return v1.cross(v2) == 0;
855
          1
856
          public boolean isZero()
857
858
          {
859
               return x == 0 && y == 0;
860
          }
861
862
          public int compareTo(pt other)
863
864
              pt v1 = ref.vect(this);
865
              pt v2 = ref.vect(other);
866
867
              if (v1.isZero()) return -1;
868
              if (v2.isZero()) return 1;
869
870
               if (v1.cross(v2) != 0)
871
                   return -v1.cross(v2);
872
873
               if (ref.dist(v1) < ref.dist(v2))</pre>
874
                   return -1;
875
               return 1;
876
          }
877
      }
878
879
      // Adam Doussan AD844156 04/28/2017
880
881
      public class Polygon
882
      {
883
          public static boolean ptInPoly(pt intersect, pt [] poly)
884
885
               double totalAngle = 0;
886
887
               for(int i = 0; i < poly.length; i++)</pre>
888
889
                   pt v1 = intersect.vect(poly[i]);
890
                   pt v2 = intersect.vect(poly[(i+1)%poly.length]);
891
892
                   try
893
                   {
894
                       totalAngle += Math.acos((v1.dot(v2)) / (v1.mag() * v2.mag()));
895
                   }
```

```
896
                   catch (Exception e)
897
898
                   }
899
               }
900
901
               return (2*Math.PI) - totalAngle < 1e-9;</pre>
902
          }
903
904
          // assumes polygon is 2d, z is unused and set to 0, and points are ordered
905
          // such that pt[x] \rightarrow pt[(x+1) % pt.length] is connected with a line. Also
906
          // assumes simple polygon
907
          public static double area(pt [] poly)
908
          {
909
               double ans = 0;
910
              pt ori = new pt(0,0,0);
911
               for(int i = 0; i < poly.length; i++)</pre>
912
913
914
                   pt v1 = ori.vect(poly[i]);
915
                   pt v2 = ori.vect(poly[(i+1)%poly.length]);
916
                   ans += v1.cross(v2).z;
917
               }
918
919
              return 0.5 * Math.abs(ans);
920
          }
921
      }
922
      class pt
923
924
      {
925
          public double x, y, z;
926
927
          pt (double x, double y, double z)
928
929
               this.x = x; this.y = y; this.z = z;
930
          1
931
932
          public pt vect(pt pt2)
933
          -{
934
               return new pt(pt2.x-x, pt2.y-y, pt2.z-z);
935
          1
936
937
          public pt cross(pt pt2)
938
          {
939
               double x = this.y * pt2.z - pt2.y * this.z;
940
              double y = this.z * pt2.x - pt2.z * this.x;
941
              double z = this.x * pt2.y - pt2.x * this.y;
942
943
               return new pt(x,y,z);
944
          }
945
946
          public double mag()
947
948
               return Math.sqrt(Math.pow(this.x,2) + Math.pow(this.y,2) + Math.pow(this.z,2));
949
950
951
          public double dot(pt vect)
952
               return (this.x * vect.x) + (this.y * vect.y) + (this.z * vect.z);
953
954
          }
955
      }
956
957
      // Ross 4/24/2017
958
959
      public class LineCircleIntersect
960
961
          // returns true if the segment intersects the circle, false otherwise
962
          public static boolean intersect(pt start, pt end, circ circle)
963
          {
964
               double dx = end.x - start.x;
```

```
965
               double dy = end.y - start.y;
 966
 967
               double a = ((dx*dx)+(dy*dy));
               double b = 2 * (dx * (start.x - circle.x) + dy * (start.y - circle.y));
 968
 969
               double c = ((start.x - circle.x) * (start.x - circle.x))
 970
                            + ((start.y - circle.y) * (start.y - circle.y))
 971
                            - (circle.radius * circle.radius);
 972
 973
               double det = (b*b) - (4 * a * c);
 974
 975
               // Answer will be non-real; discard.
 976
               if (det < 0)
 977
                   return false;
 978
 979
               double soln1 = ((-1 * b) + Math.sqrt(det))/(2*a);
 980
               double soln2 = ((-1 * b) - Math.sqrt(det))/(2*a);
 981
 982
               if (((soln1 < 0) || (soln1 > 1)) && ((soln2 < 0) || (soln2 > 1)))
 983
                   return false;
 984
               return true;
 985
           }
 986
       }
 987
 988
       class pt
 989
 990
           double x,y;
 991
       }
 992
 993
       class circ
 994
       {
 995
           double x,y;
 996
           double radius;
 997
       }
 998
 999
       // Adam Doussan 4/24/2017
1000
       public class LineLineIntersection
1001
1002
       {
1003
           // java.awt.geom.Line2D.linesIntersect()
1004
1005
           public static boolean intersect(line a, line b)
1006
           {
1007
               return a.intersect(b);
1008
           }
1009
       }
1010
1011
       class vect
1012
1013
           public double x,y;
1014
1015
           public vect(pt start, pt end)
1016
1017
               x = end.x - start.x;
1018
               y = end.y - start.y;
1019
           }
1020
       }
1021
1022
       class pt
1023
       {
1024
           public double x, y;
1025
1026
           public pt(double x, double y)
1027
           {
1028
               this.x = x; this.y = y;
1029
           }
1030
       }
1031
1032
       class line
1033
```

```
1034
           public pt p;
1035
           public vect dir;
1036
1037
           public line(pt start, pt end)
1038
1039
               p = start;
1040
               dir = new vect(start, end);
1041
           }
1042
1043
           public boolean intersect(line other)
1044
           -{
1045
               double den = det(dir.x, -other.dir.x, dir.y, -other.dir.y);
1046
               double numLam = det(other.p.x-p.x, -other.dir.x, other.p.y-p.y, -other.dir.y);
1047
                // paralell
1048
1049
               if(den < 1e-9)
1050
                    return false;
1051
1052
               else if(numLam/den > 1)
1053
                    return false;
1054
1055
               else
1056
                    return true;
1057
           }
1058
1059
           public static double det(double a, double b, double c, double d)
1060
1061
               return a*d-b*c;
1062
           }
1063
       }
1064
1065
       // Adam Doussan AD844156 04/14/2017
1066
1067
       public class LinePlaneIntersect
1068
1069
           // example where input is given as points
1070
           public static void main(String [] args)
1071
           -{
1072
               Scanner in = new Scanner(System.in);
1073
1074
               int run = in.nextInt();
1075
1076
               for(int r = 1; r <= run; r++)</pre>
1077
1078
                    pt p1 = new pt(in.nextInt(),in.nextInt(),in.nextInt());
1079
                    pt p2 = new pt(in.nextInt(),in.nextInt(),in.nextInt());
1080
1081
                    line l = new line(p1.vect(p2), p1);
1082
1083
                   pt p3 = new pt(in.nextInt(),in.nextInt(),in.nextInt());
1084
                    pt p4 = new pt(in.nextInt(),in.nextInt(),in.nextInt());
1085
                    pt p5 = new pt(in.nextInt(),in.nextInt(),in.nextInt());
1086
1087
                    plane p = new plane(p3.vect(p4), p3.vect(p5), p3);
1088
1089
                    System.out.format("Data Set #%d:\n", r);
1090
                    solve(1,p);
1091
                    System.out.println();
1092
                }
1093
           }
1094
1095
           public static void solve(line 1, plane p)
1096
1097
                int right = p.d - (1.p.x*p.orth.x + 1.p.y*p.orth.y + 1.p.z*p.orth.z);
1098
               int left = (1.vect.x*p.orth.x + 1.vect.y*p.orth.y + 1.vect.z*p.orth.z);
1099
1100
               if(right == 0)
1101
1102
                    System.out.println("The line lies on the plane.");
```

```
1103
               }
1104
1105
               else if(left == 0)
1106
1107
                   System.out.println("There is no intersection.");
1108
1109
               else
1110
1111
               {
1112
                   double lam = ((double)right) / left;
1113
                   System.out.format("The intersection is the point (%.1f, %.1f, %.1f).\n",
1114
                   1.p.x + 1.vect.x*lam, 1.p.y + 1.vect.y*lam, 1.p.z + 1.vect.z*lam);
1115
               }
1116
           }
1117
1118
1119
       class pt
1120
       {
1121
           int x, y, z;
1122
1123
           pt(int x, int y, int z)
1124
1125
               this.x = x; this.y = y; this.z = z;
1126
           }
1127
           public pt vect(pt pt2)
1128
1129
1130
               return new pt(pt2.x-x, pt2.y-y, pt2.z-z);
1131
           1
1132
1133
           public pt cross(pt pt2)
1134
           {
1135
               int x = this.y * pt2.z - pt2.y * this.z;
               int y = this.z * pt2.x - pt2.z * this.x;
1136
1137
               int z = this.x * pt2.y - pt2.x * this.y;
1138
1139
               return new pt(x,y,z);
1140
           }
1141
1142
           public int solve(pt pt2)
1143
1144
               return this.x*pt2.x + this.y*pt2.y + this.z*pt2.z;
1145
           }
1146
       }
1147
       class line
1148
1149
1150
           pt vect, p;
1151
1152
           public line(pt vect, pt p)
1153
           {
1154
               this.vect = vect; this.p = p;
1155
           }
1156
       }
1157
1158
       class plane
1159
       {
1160
           pt orth;
1161
           int d;
1162
1163
           public plane(pt vect1, pt vect2, pt ori)
1164
1165
               orth = vect1.cross(vect2);
1166
               d = orth.solve(ori);
1167
           }
1168
       }
1169
1170
       // Adam Doussan AD844156 04/14/2017
1171
```

```
1172
       public class KnapSack
1173
       {
1174
           // unlim = true means can take unlimited times, otherwise each thing can be
1175
           // taken only once. Add multiple times if multiple limited number of same
1176
           // object. kp[money] contains the answer for money.
1177
           public static long[] solve(int [] cost, int [] value, int money, boolean unlim)
1178
1179
                long [] kp = new long [money+1];
1180
                int n = cost.length;
1181
1182
                if (unlim)
1183
                {
1184
                    for (int j = 0; j < n; j++)
1185
1186
                        for (int k = cost[j]; k < money+1; k++)
1187
                        {
1188
                             if(kp[k-cost[j]] + value[j] > kp[k])
1189
                                 kp[k] = kp[k - cost[j]] + value[j];
1190
                        }
1191
                    }
1192
                }
1193
1194
                else
1195
                {
1196
                    for (int j = 0; j < n; j++)
1197
1198
                        for (int k = money+1; k \ge cost[j]; k--)
1199
1200
                             if(kp[k-cost[j]] + value[j] > kp[k])
1201
                                 kp[k] = kp[k - cost[j]] + value[j];
1202
                        }
1203
                    }
1204
                }
1205
1206
                return kp;
1207
           }
1208
1209
1210
       // Ross 04/30/2017
1211
1212
       public class MatrixChain
1213
1214
           public static void main(String [] args)
1215
1216
                //Matrix A is 2x4, Matrix B is 4x2, Matrix C is 2x3 and so on.
1217
                int matr[] = new int[] {2, 4, 2, 3, 1, 4};
1218
                int size = matr.length;
1219
1220
                int res = MCM(matr, size);
1221
                System.out.println(res);
1222
           }
1223
1224
           static int MCM(int[] matr, int size)
1225
           {
1226
                int a;
1227
                int memo[][] = new int[size][size];
1228
1229
                for(int i=0; i<size; i++)</pre>
1230
                {
1231
                    memo[i][i] = 0;
1232
                }
1233
1234
                for (int sub=2; sub <= (size-1); sub++)</pre>
1235
1236
                    for(int j=1; j <= ((size-1) - sub + 1); j++)</pre>
1237
1238
                        memo[j][sub+j-1] = Integer.MAX VALUE;
1239
                        for(int k=j; k <= (sub+j-2); k++)</pre>
1240
```

```
1241
                             a = memo[j][k] + memo[k+1][j+sub-1] + (matr[j-1] * matr[k] *
                             matr[sub+j-1]);
1242
                             if (a < memo[j][j+sub-1])</pre>
1243
1244
                                 memo[j][j+sub-1] = a;
1245
                             }
1246
                        }
1247
                    }
1248
                }
1249
1250
                return memo[1][size-1];
1251
            }
1252
       }
1253
1254
       // Ross 04/30/2017
1255
       public class LCS
1256
1257
       {
1258
            static int LCS(String str1, String str2, int len1, int len2)
1259
1260
                int[][] memo = new int[len1+1][len2+1];
1261
1262
                for (int i=1; i<=len1; i++)</pre>
1263
1264
                    for(int j=1; j<=len2; j++)</pre>
1265
1266
                        if((i == 0) || (j == 0))
1267
1268
                             memo[i][j] = 0;
1269
1270
                        else if(str1.charAt(i-1) == str2.charAt(j-1))
1271
1272
                             memo[i][j] = 1 + memo[i-1][j-1];
1273
                        }
1274
                        else
1275
                         {
1276
                             int sub = Math.max(memo[i][j-1], memo[i-1][j]);
1277
                             memo[i][j] = sub;
1278
                         }
1279
                    }
1280
1281
                return memo[len1][len2];
1282
            }
1283
       }
```