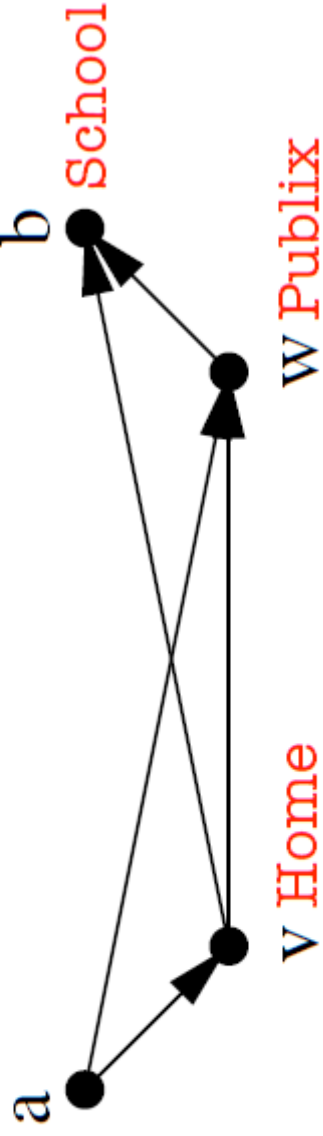


Applications of Search

landmarks

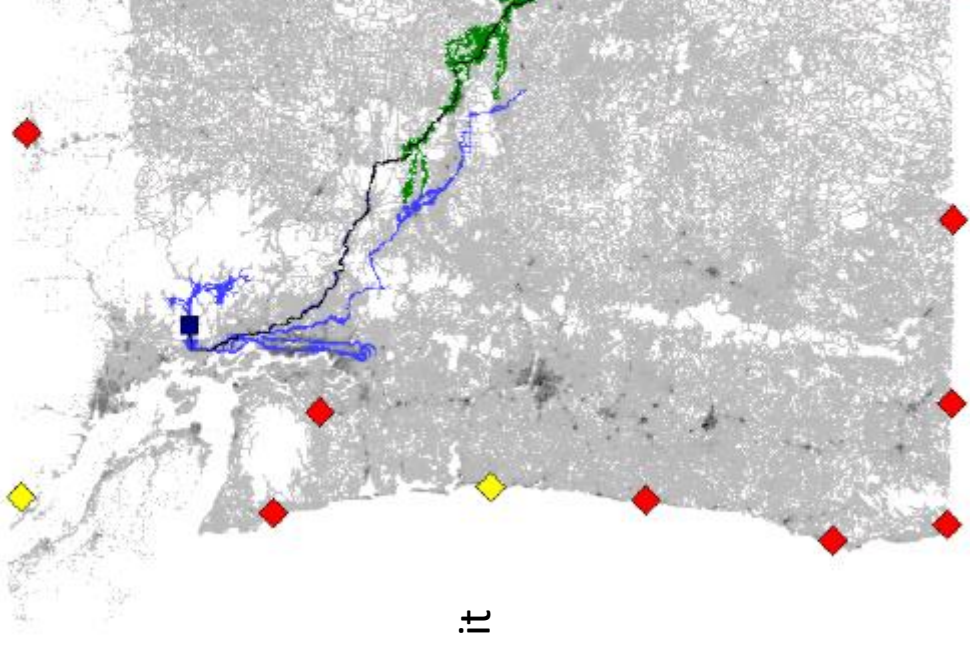
triangle inequality

$$\geq \text{dist}(a, w) - \text{dist}(a, v) \quad \text{dist}(v, w) \geq \text{dist}(v, b) - \text{dist}(w, b)$$



action that serves as a heuristic! This may be Euclidean Distance but it

- : computation
- er bounds (depending on landmark) than simple Euclidean
- ance
- ending on the landmark, heuristic cost can be 0!!



Images from Goldberg (2011), R

Each

Given a vertex v , calculate all the shortest paths through it.

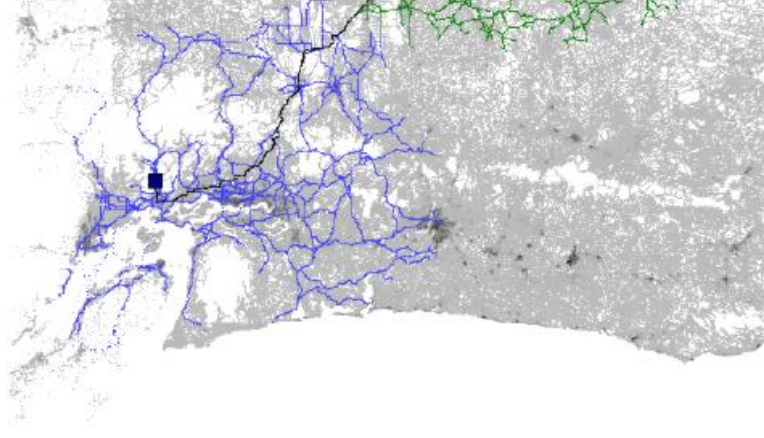
- For a shortest path P , the reach of the vertex:

$$r_P(v) = \min(\text{cost}(s, v), \text{cost}(v, t))$$

- Total reach across all paths: $r(v) = \max_p(r_P)$

Choose v when $r(v) < \min(\text{dist}(s, v), \text{cost}(v, t))$

Forces you to prioritize highways



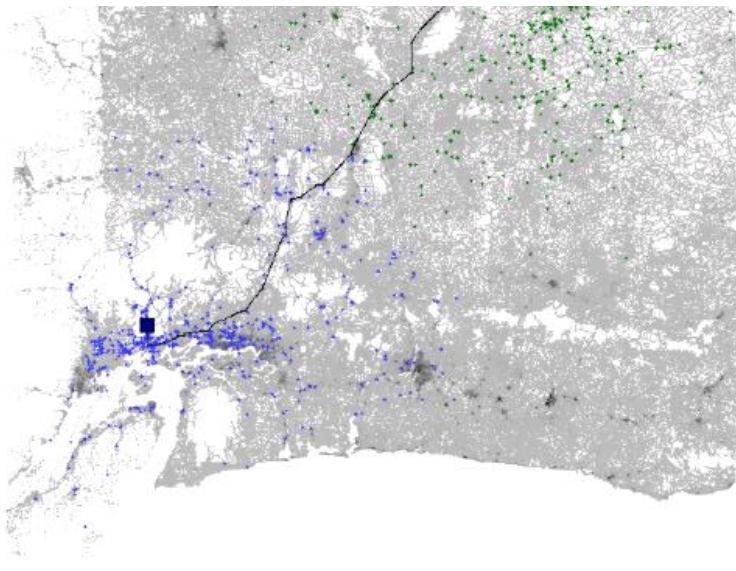
Images from Goldberg (2011), R

ortcuts

dd in vertices to reduce the number of shortest paths through a k
: nodes

- Reduces the Reach of intermediate nodes

an prune more paths as a result



Images from Goldberg (2011), R

Impact of Landmark, Reach and Shortcuts

West (1.6M vertices), random queries, 16 landmarks.

| method | preprocessing | | query | | |
|------------------------|--|---------------|---------|------------|------------|
| | minutes | MB | avgscan | maxscan | |
| Bidirectional Dijkstra | — | 28 | 518 723 | 1 197 607 | |
| | North America (30M vertices), random queries, 16 landmarks | | | | |
| | 4 | | | | |
| | 1 100 | | | | |
| | 17 | | | | |
| +Short | 21 | | | | |
| +Short+ALT | | | | | |
| | | preprocessing | | query | |
| | | hours | GB | avgscan | maxscan |
| Bidirectional Dijkstra | | — | 0.5 | 10 255 356 | 27 166 866 |
| ALT | | 1.6 | 2.3 | 250 381 | 3 584 377 |
| Reach | | impractical | | | |
| Reach+Short | | 11.3 | 1.8 | 14 684 | 24 618 |
| Reach+Short+ALT | | 12.9 | 3.6 | 1 595 | 7 450 |

Alber (2011), Reach for A*

More Resources

test version of slides explaining Landmarks, Reach, and Shortcuts
<http://www.columbia.edu/~cs2035/courses/ieor6614.S16/goldberg.pdf>)

Hyper Introducing Landmarks

<http://www.cs.princeton.edu/courses/archive/spr06/cos423/Handouts/GH05.pdf>)

Hyper Introducing Reach (<http://www.siam.org/meetings/alensex04/abstracts/rgutman1.p>

Hyper Comparing all of these algorithms (<https://www.microsoft.com/en-research/wp-content/uploads/2004/07/tr-2004-24.pdf>)

Google Maps – Transfer Patterns

add time dependent nodes to your graph and precompute lowest cost routes for disjoint subsets (http://ad-publications.informatik.uni-freiburg.de/ESA_transferpatterns_BCEGHRV_2010.pdf)

encode time domain data in frequency space and modify Dijkstra to work in that sparse representation (http://ad-publications.informatik.uni-freiburg.de/SIGSPATIAL_frequency_BS_2014.pdf)

cluster nodes in subgraphs to minimize precomputation costs (http://ad-publications.informatik.uni-freiburg.de/ALENEX_scalable_tp_BHS_2016.pdf)