Exercise No. 1

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2 - Numerical Integration

a)

```
import numpy as np
  import matplotlib.pyplot as plt
n = np.array([1,5,10,20,30,50])
   xdata = np.linspace(0,1, 1000)
   y = lambda x, a, n: x^* * n/(x+a)
9
10
   plt.figure(figsize=(10,5))
11
12
   plt.xlabel('x')
13
   plt.ylabel('y')
14
15
   for it in n:
16
       plt.plot(xdata, y(xdata, a, it))
17
18
   plt.savefig('01-2a.png')
```

Listing 1: h

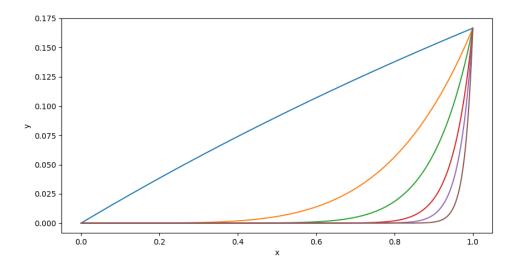


Figure 1: h

b)

```
1 import numpy as np
2 import sys
3 import pandas as pd
   def y(a, n, y0):
5
       if n == 0:
7
           return y0
       else:
8
           return 1/n - a* y(a, n-1, y0)
9
10
   if name == ' main ':
11
12
13
       # accepting args as: a, n0, y0, n1
14
       print(sys.argv)
15
16
       a = int(sys.argv[1])
17
       n0 = int(sys.argv[2])
18
       n1 = int(sys.argv[4])
19
       y0 = int(sys.argv[3])
20
21
22
       ndata = range(min(n0,n1),max(n0,n1)+1)
23
       print(ndata)
24
       ydata = [y(a, i, y0) \text{ for } i \text{ in } ndata]
25
       print(ydata)
```

	n	y_n
0	10.0	-1.780484e+06
1	11.0	8.902420e+06
2	12.0	-4.451210e+07
3	13.0	2.225605e+08
4	14.0	-1.112802e+09
5	15.0	5.564012e+09
6	16.0	-2.782006e+10
7	17.0	1.391003e+11
8	18.0	-6.955015e+11
9	19.0	3.477508e+12
10	20.0	-1.738754e+13

c)