

Exercise No. 1

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2 - Numerical Integration

a)

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 a = 5
5 n = np.array([1,5,10,20,30,50])
6 xdata = np.linspace(0,1, 1000)
7
8 y = lambda x, a, n: x**n/(x+a)
9
10
11 plt.figure(figsize=(10,5))
12
13 plt.xlabel('x')
14 plt.ylabel('y')
15
16 for it in n:
17     plt.plot(xdata, y(xdata, a, it))
```

Listing 1: h

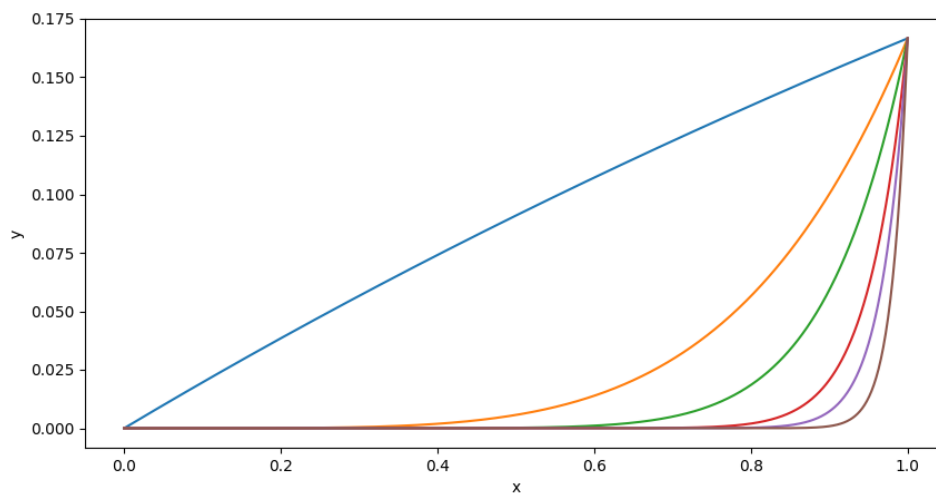


Figure 1: h

b)

```
1 import numpy as np
2 import sys
3 import pandas as pd
4
5 def y(a, n, y0):
6     if n == 0:
7         return y0
8     else:
9         return 1/n - a* y(a, n-1, y0)
10
11 if __name__ == '__main__':
12
13     # accepting args as: a, n0, y0, n1
14
15     print(sys.argv)
16
17     a = int(sys.argv[1])
18     n0 = int(sys.argv[2])
19     n1 = int(sys.argv[4])
20     y0 = int(sys.argv[3])
21
22     ndata = range(min(n0, n1), max(n0, n1)+1)
23     print(ndata)
24     ydata = [y(a, i, y0) for i in ndata]
25     print(ydata)
```

w2

| | n | $y_n(5)$ |
|----|------|---------------|
| 0 | 10.0 | -1.780484e+06 |
| 1 | 11.0 | 8.902420e+06 |
| 2 | 12.0 | -4.451210e+07 |
| 3 | 13.0 | 2.225605e+08 |
| 4 | 14.0 | -1.112802e+09 |
| 5 | 15.0 | 5.564012e+09 |
| 6 | 16.0 | -2.782006e+10 |
| 7 | 17.0 | 1.391003e+11 |
| 8 | 18.0 | -6.955015e+11 |
| 9 | 19.0 | 3.477508e+12 |
| 10 | 20.0 | -1.738754e+13 |

c)