

# Exam CompStat: 26.7.17 16:00

July 18, 2017

- $y_i, \hat{y}$  RV
- $\langle y \rangle = \mu_y$  not random  $\rightarrow$  Prior

## 1 Basic Properties of random Variables

- Transitional, cond.prob., joint prob. margin

$$\int p(x, y) dy = f(x)$$

- law of error propagation

$$\sigma_y^2 = \sigma_x^2 * (dy/dx)^2$$
$$P(x|y) = P(x, y)/P(y)$$

## 2 Distributions

- uniform, binomial, poissonian, (multivariate-) gaussian,  $\chi^2$ , exponential

$$f(x) > 0$$
$$\int f(x) dx = 1$$

- PDF

$$f(x) dx$$

- CDF

$$\text{int}(f(x), x, -\text{Inf}, y) = g(y)$$

- MGF

$$\langle e^{tx} \rangle = \int e^{tx} f(x) dx$$

- moments

$$\int x^m f(x) dx$$
$$\int (x - \alpha)^m f(x) dx$$

## 3 Bayes Theorem

- hi

$$P(d, t)$$

$$G(x, \mu) = e^{-\frac{1}{2} \frac{(x-\mu)^2}{\sigma^2}}$$

$$P(D|T) = P(D, T)/P(T)$$

$$P(T|D) = P(D, T)/P(D)$$

- frequentists approach

$$P(D, T) = \dots$$

$$d_i, \hat{d} = \sum_i \frac{d_i}{N} = f \text{ of data}$$

$$\langle \hat{d} \rangle = \mu$$

$$\rightarrow \text{PDF}(\hat{\theta}) \text{ (PDF of estimator)}$$

- Bayes Theorem

$$P(T|D) = P(D|T) \frac{P(T)}{P(D)}$$

$$E(D) = \int L(D|T) \pi(T) dT$$

$$B_{a,b} = \frac{E_a(D)}{E_b(D)}$$

## 4 Fisher Estimation

$$F_{\alpha, \beta} = \left. \frac{\partial^2 \log(L)}{\partial \theta_\alpha \partial \theta_\beta} \right|_{L_{max}}$$

- we assume gaussian distributed parameters around the peak for a found maximum likelihood estimator

$$e^{-\frac{1}{2} (x_i - \mu_i) C_{i,j}^{-1} (x_j - \mu_j)}$$

## 5 fitting

$$t = f(x) = A_0 + A_1 f_1(x) + A_2 f_2(x)$$

$$e^{-\frac{1}{2} \sum_i \frac{(d_i - t_i)^2}{\sigma_i^2}} \Rightarrow C_{i,j}$$

$$A|_{L_{max}} = G^{-1} D, F_{\alpha, \beta} = G$$