Computational Statistics and Data Analysis Sheet No. 4

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1 Generating Gaussian distributed random variables

We are to create uniformly distributed points in a unit circle and show the values for z_1 and z_2 are gaussian distributed

```
1 | \text{num randoms} = 10000
 3 orig set = runif(num randoms*2, min = -1, max = 1)
 4 | dim(orig_set) = c(2,num_randoms)
 6 | calc set = orig set[1,]**2 + orig set[2,]**2
 7 used_set = orig_set[,calc_set <= 1]</pre>
 8
 9
    z1 <- function(vec) {</pre>
        return(vec[1]*sqrt(-2*(log(vec[1]**2+vec[2]**2))/(vec[1]**2+vec[2]**2)))
10
11
   }
12
13 | z2 <- function(vec) {
        return(vec[2]*sqrt(-2*(log(vec[1]**2+vec[2]**2))/(vec[1]**2+vec[2]**2)))
14
15 }
16
17 | z1_set = 1:length(used_set[1,])
18 | z2 set = 1:length(used set[1,])
19 | for (i in 1:length(used set[1,])) {
20
        z1_{set[i]} = z1(used_{set[,i]})
21
        z2 \text{ set}[i] = z2(\text{used set}[,i])
22 }
23
24 pos_set = seq(-5,5,.1)
25
26 | png('ex11.png')
27 h1 = hist(z1 set, breaks=pos set, xlab='z1')
28 | yfit1 = dnorm(pos set, mean=0, sd=sd(z1 set))
```

```
29  yfit1 = yfit1 * diff(h1$mids[1:2])*length(z1_set)
30  points(pos_set, yfit1, cex=1, pch=20, col='red')
31
32
33  png('ex12.png')
44  h2 = hist(z2_set, breaks=pos_set, xlab='z2')
35  yfit2 = dnorm(pos_set, mean=0, sd=sd(z2_set))
36  yfit2 = yfit2 * diff(h2$mids[1:2])*length(z2_set)
37  points(pos_set, yfit2, cex=1, pch=20, col='red')
```

Histogram of z1_set

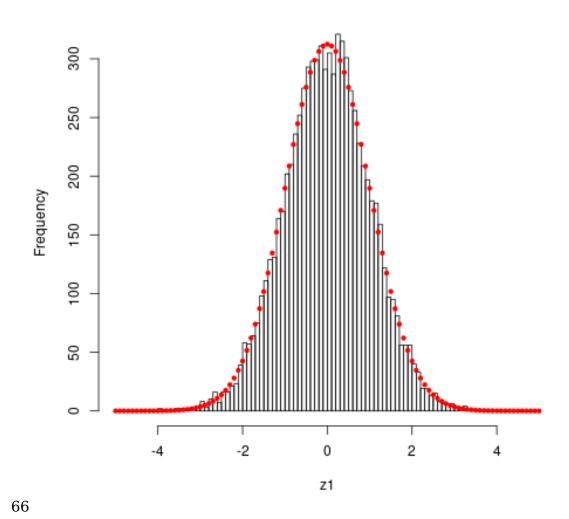


Figure 1: histogram of z1 and gauss-fit

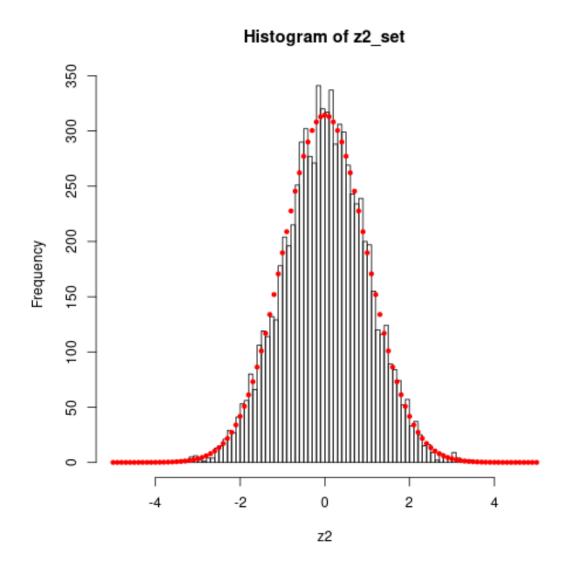


Figure 2: histogram of z2 and gauss-fit

2 Random Walk

We generate the mean number of steps needed for a 1D random walk as a function of the distance n

```
1
    rand_walk <- function(nmax) {</pre>
 2
        pos = 0
 3
        steps = 0
 4
        while (pos < nmax && pos > -nmax){
 5
            step = sample(0:1,1) *2 -1
 6
            pos = pos + step
 7
            steps = steps +1
 8
        }
 9
10
        return(steps)
   }
11
12
13
   dist_rand_walk <- function(n){</pre>
14
15
        num tests = 100
16
        res = 1:num_tests
17
        for (i in 1:num_tests) {
18
            res[i] = rand_walk(n)
19
        }
20
21
        return(res)
22
   }
23
24
   nset = 1:50
   means = 1:max(nset)
26
   for (i in nset){
27
        means[i] = mean(dist_rand_walk(i))
28
        print(i)
29
   }
30
31
   png('ex2.png')
32
   plot(
33
        nset, means, pch=20, cex=1,
34
        xlab='n:_width_of_exprimental_area', ylab='average_number_of_steps_needed'
35 )
```

Figure 3: ex2.R

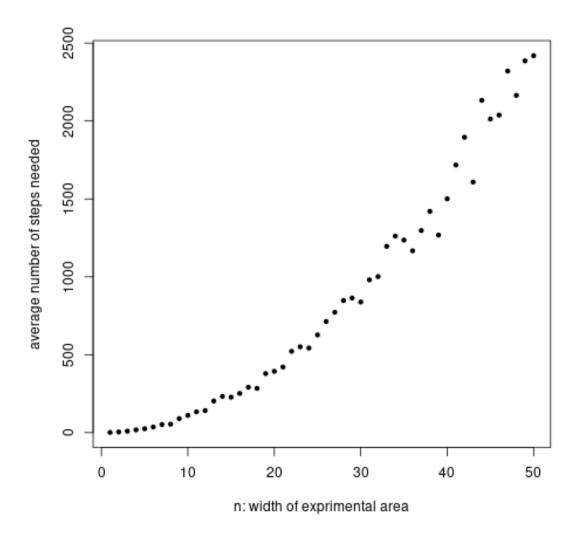


Figure 4: average number of steps taken as a function of n, in 50 tests per n

we can assume the number of steps required rises exponentially with the distance \boldsymbol{n}