컴퓨터그래픽스

김준호

Visual Computing Lab.

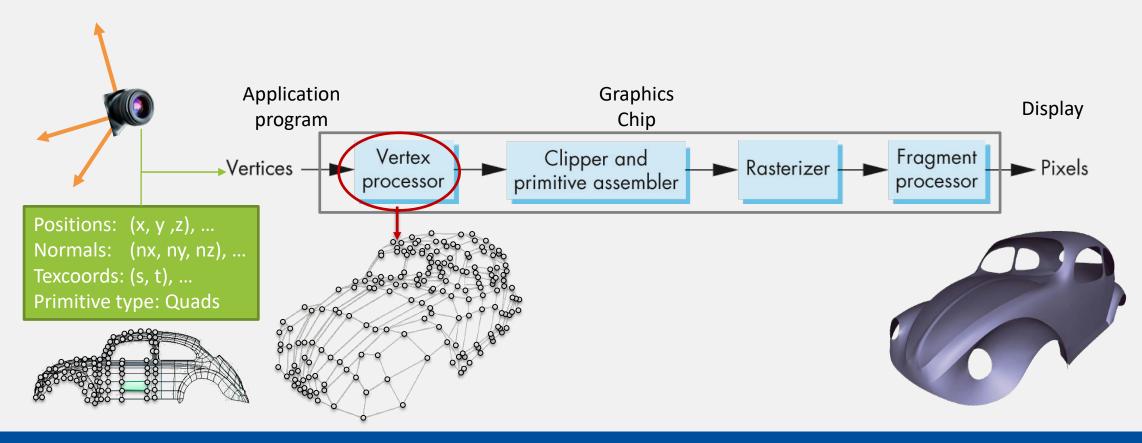
국민대학교 소프트웨어학부

- Overview of Vertex Processor
- Coordinate System & Coordiante Values
- ModelView matrix
- Projection matrix
- Viewport

Vertex Processor

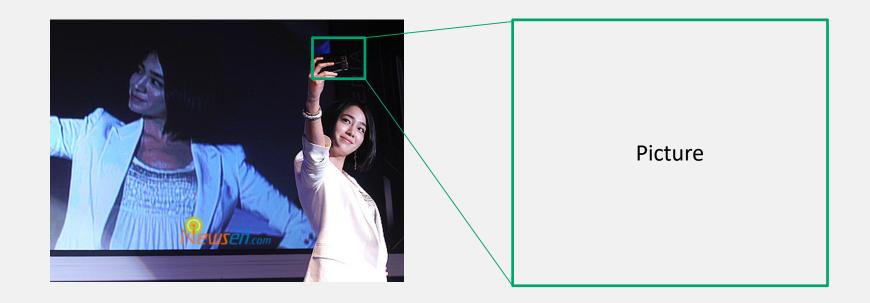
Overview of Vertex Processor

- Vertex processor
 - Converting object representations from one coordinate system to another
 - Object coordinates → Camera coordinates → Screen coordinates



Objectives

- We are interested in an image captured from the camera
 - First of all, we should know the coordinate of a 3D point, from camera's viewpoint
 - It means, we have to understand the change of coordinates
 - Coordinate values in object space → Coordinate values in camera space

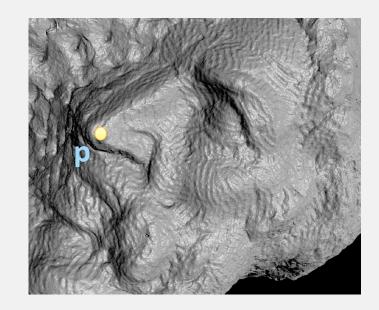


- Coordinate system & Coordinate Values
- MovelView matrix

Coordinate System and Coordinate Values

Coordinate Value – Representation of a Point

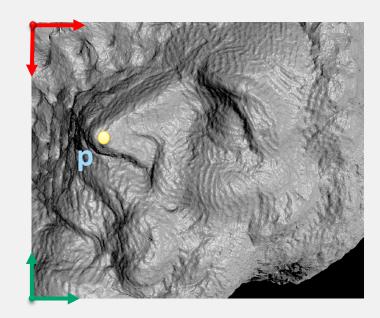
- Where is a point p?
 - For the same point, we can represent it with different coordinates

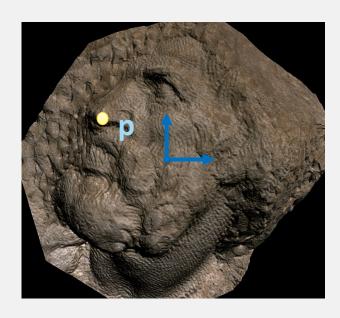




Coordinate Value – Representation of a Point

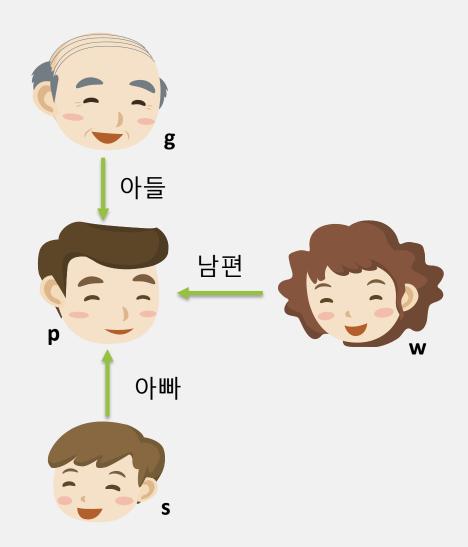
- The coordinate value of a point is meaningful, only when we specify a coordinate system
 - The same point can be reprsented with different coordinate values!
 - p = (1.5, 3) = (1.5, 2.5) = (-1.2, 1)





Coordinate Value – Representation of a Point

- Analogy in real-world
 - A point p
 - 존재
 - Coordinate system (or Frame)
 - 관점
 - Coordinate value of p
 - 특정 관점에서 해당 존재를 부르는 호 칭 (representation)
 - 동일한 존재는 여러가지 호칭으로 불릴 수 있음
 - p_[g] = 아들
 - p_[w] = 남편
 - $\mathbf{p}_{[s]} = O \mid \mathsf{HH} \mid$

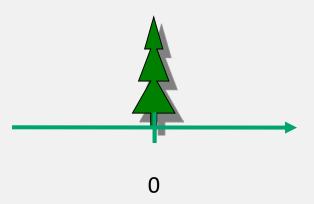


ModelView matrix

What is ModelView Matrix?

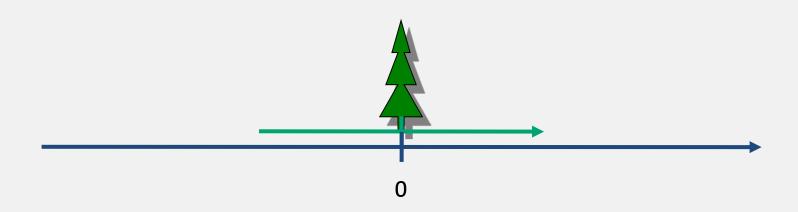
- The composition of a model matrix and a view matrix
 - OpenGL manages the model matrix and the view matrix together
 - c.f.) Direct3D seperates the model matrix and the view matrix
 - Model matrix
 - 3D transformation of an object (or model) in the world coordinate system
 - View matrix
 - 3D transformation of a camera in the world coordinate system
 - This is the extrinsic parameters of the camera!
- We can obtain the camera coordinates by multiplying the ModelView matrix to the object coordinates
 - $\mathbf{x}_{view} = \mathbf{V}^{-1} \mathbf{M} \mathbf{x}_{obi}$
 - V-1M is called the modelview matrix

- You model an object in the object-space coordinate system
 - Every point is represented with object-space coordinates \mathbf{x}_{obj}
 - 3D positions specified in <u>glVertexPointer()</u> are in the objects-space coordinate system

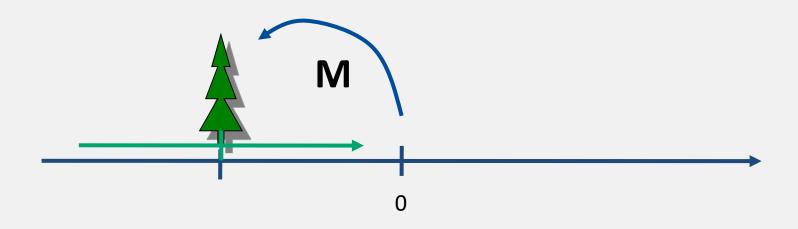


You may place the object in the origin of the world

$$-\mathbf{x}_{world} = \mathbf{x}_{obj}$$



- You move the object to somewhere in the world
 - M: world-transform matrix
 - You set **M** by using the composition of glRotate(), glRo
 - $-\mathbf{x}_{world} = \mathbf{M}\mathbf{x}_{obj}$



• Now, let's consider a camera

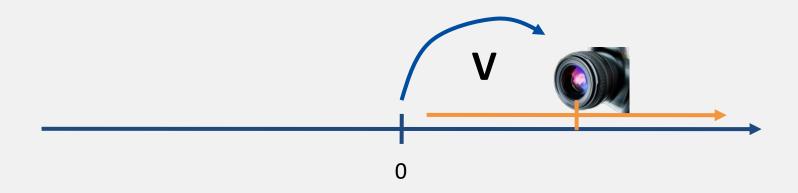


You may place the camera in the origin of the world

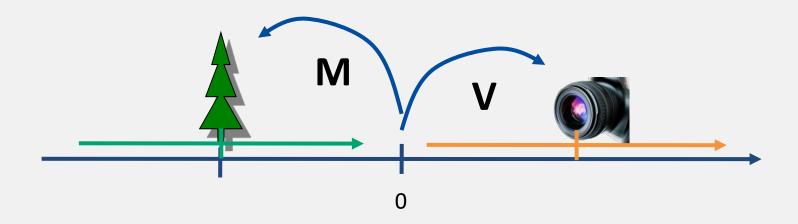
$$- \mathbf{x}_{world} = \mathbf{x}_{view}$$



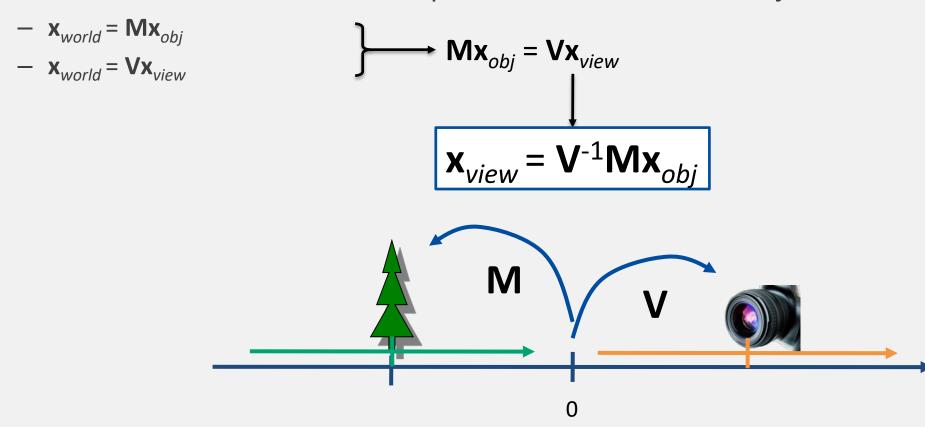
- You move the camera to somewhere in the world
 - V: view-transform matrix
 - You set **V**⁻¹ by using **gluLookAt**()
 - $\mathbf{x}_{world} = \mathbf{V} \mathbf{x}_{view}$



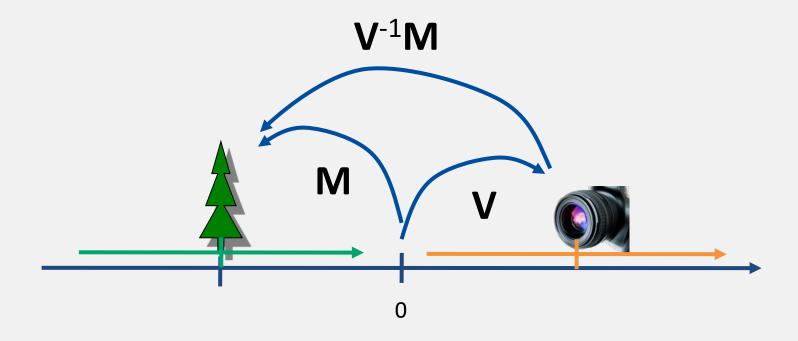
- Let's consider both of camera & object
 - $\mathbf{x}_{world} = \mathbf{M} \mathbf{x}_{obj}$
 - $\mathbf{x}_{world} = \mathbf{V} \mathbf{x}_{view}$



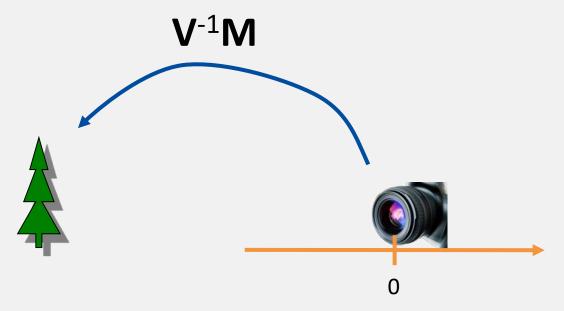
How can we obtain the camera-space coordinates of the object?



• What does " $\mathbf{x}_{view} = \mathbf{V}^{-1} \mathbf{M} \mathbf{x}_{obj}$ " mean?



- What does " $\mathbf{x}_{view} = \mathbf{V}^{-1} \mathbf{M} \mathbf{x}_{obj}$ " mean?
 - 3D Position of **x**, measured from the coordinate system of the camera
 - World-frame-independent representation
 - Now, you may think the world frame as an illusion.

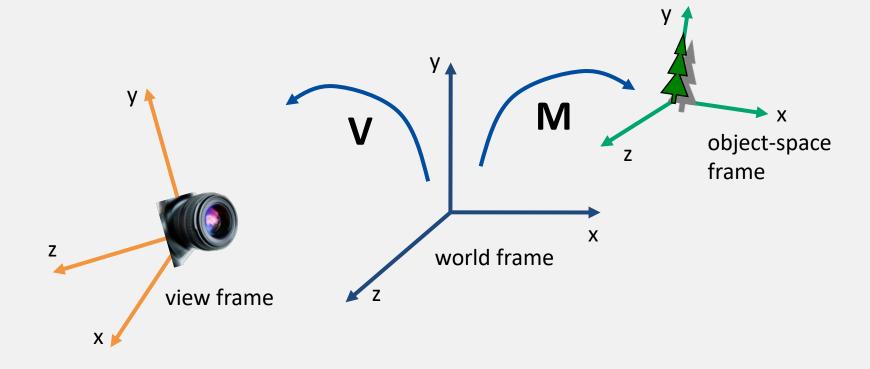


Exactly same!

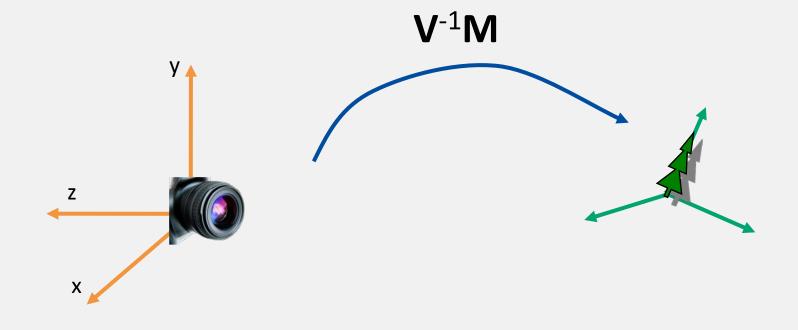
$$- \mathbf{x}_{world} = \mathbf{M} \mathbf{x}_{obj}$$

$$- \mathbf{x}_{world} = \mathbf{V} \mathbf{x}_{view}$$

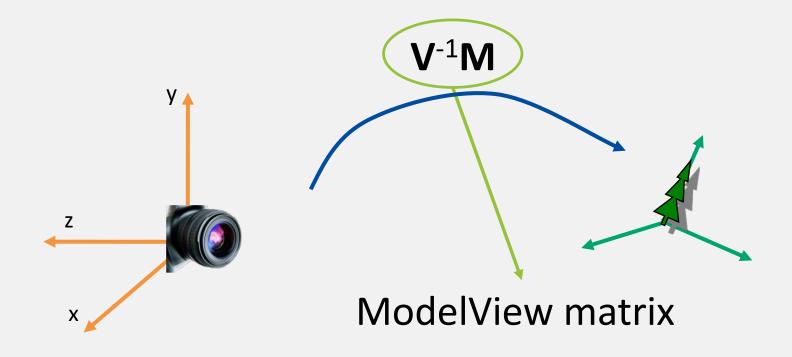
$$\mathbf{x}_{view} = \mathbf{V}^{-1} \mathbf{M} \mathbf{x}_{obj}$$



• $\mathbf{x}_{view} = \mathbf{V}^{-1}\mathbf{M} \ \mathbf{x}_{obj}$



- In OpenGL, V⁻¹M is called as the ModelView matrix
 - GL_MODELVIEW_MATRIX



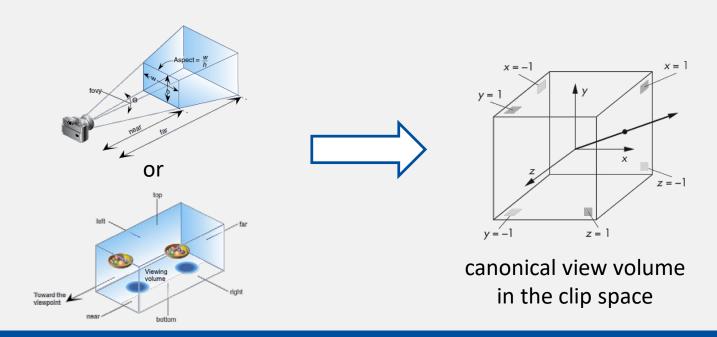
Projection matrix

What is Projection Matrix?

• Projection matrix **P** transforms camera coordinates into clip coordinates

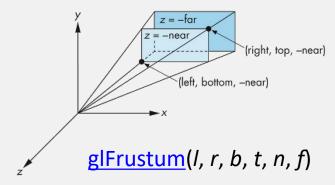
$$- \mathbf{x}_{clip} = \mathbf{P} \mathbf{x}_{view}$$
$$= \mathbf{P} \mathbf{V}^{-1} \mathbf{M} \mathbf{x}_{obj}$$

The canonical view volume is defined in the clip space



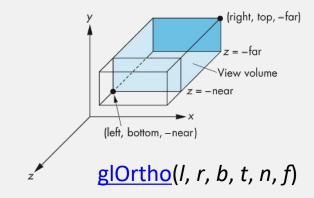
Projection Matrix

Perspective projection



$$\mathbf{P} = \begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0\\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0\\ 0 & 0 & -\frac{f+n}{f-n} & \frac{-2fn}{f-n}\\ 0 & 0 & -1 & 0 \end{bmatrix}$$

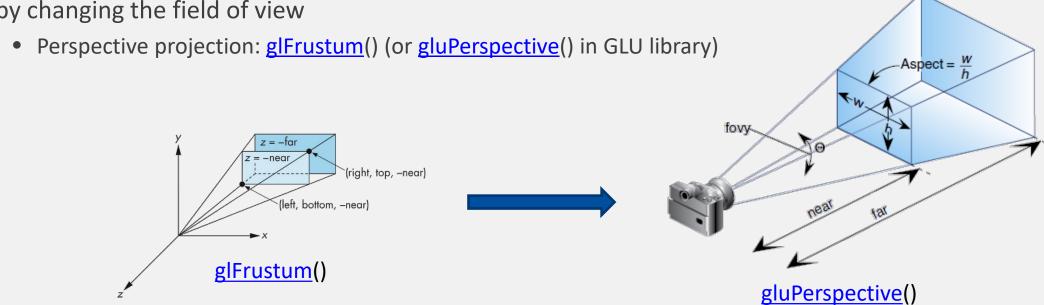
Orthographic projection



$$\mathbf{P} = \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & -\frac{2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

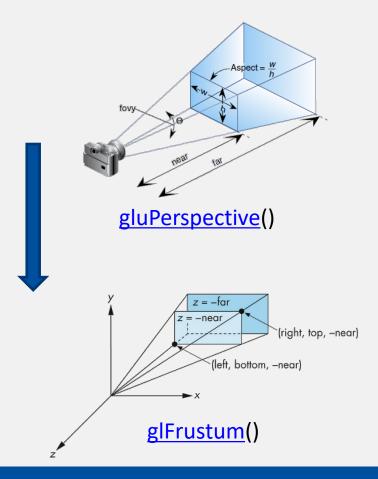
Perspective Projection

- Focal length
 - In OpenGL, there is no physical meaning
- Field of view (FOV)
 - In OpenGL, zoom-in/-out is handled by changing the field of view



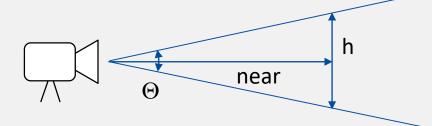
Perspective Projection: gluPerspective() → glFrustum()

3D case

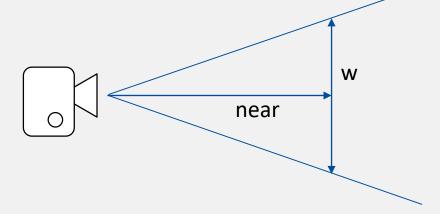


Side-/Top-view of gluPerspective()

Side-view



Top-view



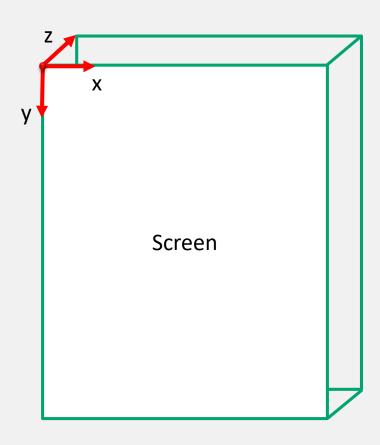
Viewport

What is Viewport?

Viewport matrix W transforms clip coordinates into screen-space coordinates

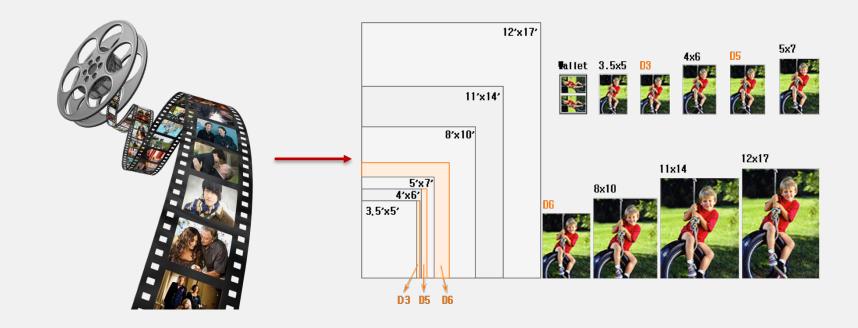
$$\begin{array}{l} - \mathbf{x}_{screen} = \mathbf{W} \mathbf{x}_{clip} \\ = \mathbf{WP} \mathbf{x}_{view} \\ = \mathbf{WPV}^{-1} \mathbf{M} \mathbf{x}_{obj} \end{array} = \begin{bmatrix} win_{\chi} \\ win_{y} \\ win_{z} \end{bmatrix}$$

- (win_x, win_y) are screen-space coordinates
 - (win_x , win_y) units are in pixel (with fractions)
- win, is depth coordinate
 - win_z is in range of 0.0 to 1.0, or depth range
 - See details in glDepthRange()



Camera Specification – Viewport

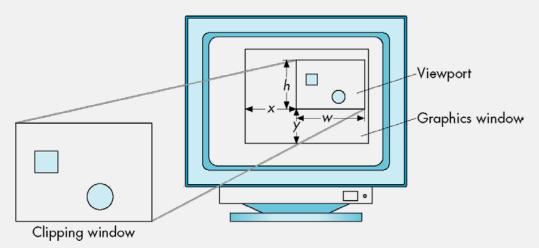
- Viewport
 - Similar to the size of photo printing
 - A film → Photos of different sizes
 - A rectangular area of the display window



Camera Specification – Viewport

Viewport

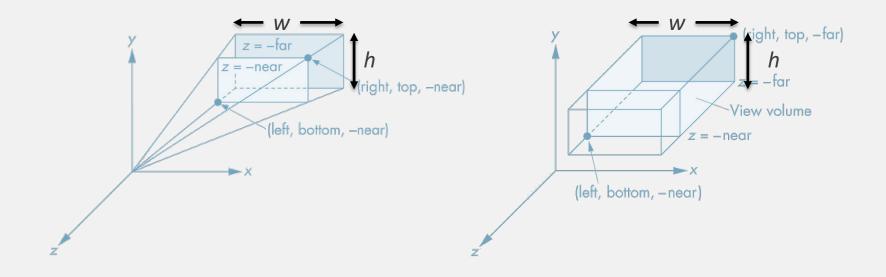
- Similar to the size of photo printing
 - A film → Photos of different sizes
- A rectangular area of the display window: x, y, w, h
 - (x, y): the lower-left corner of the viewport
 - w, h: the width and height of the viewport



A mapping to the viewport

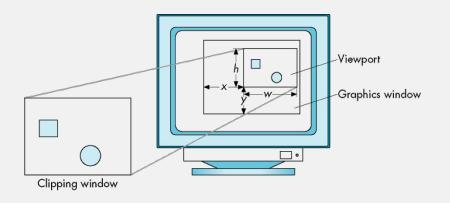
Camera Specification – Aspect ratio

- Aspect ratio
 - width / height
 - For aspect ratio, absolute sizes of width & height are meaningless
 - Aspect ratio of display window (i.e., device screen) is important

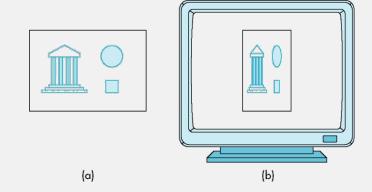


Camera Specification – Aspect ratio

- Aspect ratio
 - width / height
 - For aspect ratio, absolute sizes of width & height are meaningless
 - Aspect ratio of display window (e.g., device screen) is important



A mapping to the viewport



Aspect-ratio mismatch.
(a) viewing rectangle, (b) display window

감사합니다

Contacts:

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