

FLIGHT TESTING SMALL UAVS FOR AERODYNAMIC PARAMETER ESTIMATION

A Thesis

Presented to

the Faculty of California Polytechnic State University

San Luis Obispo

In Partial Fulfillment

of the Requirements for the Degree

Master of Science in Aerospace Engineering

by

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September 2013



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ESTIMATION

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ABSTRACT

FLIGHT TESTING SMALL UAVS FOR AERODYNAMIC PARAMETER ESTIMATION

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## ACKNOWLEDGMENTS

Thank you...

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## 0.1 Introduction

Aircraft designers often use model fits and “rules of thumb” to successfully complete designs, with many of these guidelines available in various design textbooks. [2],[3],[4] These models and practices have been established based on years of data analysis and validation that the designs perform as expected. However, the scope of these empirical design techniques is limited to the input of the regression model: an intelligent designer will not use a general aviation weight model for a transport category aircraft. To this end, there is a significant lack of small UAV-class guidelines for designing an aircraft.

Accurate estimations of a small-scale vehicle’s lift and drag characteristics are extremely critical to the aircraft designer, and affect both point performance (turn rates, climb rates, stall speeds, etc.) and mission performance (range and endurance). Much of the prediction tools available in the classic lift and drag textbooks from Hoerner<sup>[5],[6]</sup> only apply to larger scale structures. In addition, drag prediction is extremely difficult on small vehicles, as some sources of drag are not easily modeled. For instance, actuator control horns and protruding screw heads are not typically included in the CFD analysis of aircraft. However, for small vehicles, these sources of “crud” drag can be a significant portion of the total vehicle’s drag value.

One advantage of small UAVs is that they are fairly inexpensive, which makes building multiple fully-functioning prototypes a viable option. The authors chose to take advantage of this fact and develop a flight data acquisition system with a primary goal of measuring the lift and drag characteristics of a small UAV. This would enable vehicle designers to build a conceptual-design-level prototype, and both develop and validate predictive, regression-based models. The system would also allow designers to conduct quantitative trade studies, such as the trade between drag reduction technologies (wheel pants, retractable landing gear, winglets, etc.) and the weight associated with them.

The authors also desired additional sensors to aid designers with more than just lift and drag characteristics. Some areas of interest are estimating stability and control derivatives, as well as possible control algorithm testing, in-flight thrust measurement, and payload integration capabilities. To accomplish these goals, sensors not directly necessary to lift and drag estimation were included in the overall system. The system was also designed in a manner that made it reconfigurable. This allows future designers to decide what combination of accuracy, risk, and sensing capabilities they need on a given flight test, and to then package the sensors in a manner that meets vehicle integration requirements.

For this paper, the authors chose to integrate the necessary sensors to estimate lift and drag forces, as well as those necessary for a basic INS, ambient temperature measurement, and servo and motor signals. The system will be validated by measuring the as-built drag polar of an R/C aircraft, as well as all other available states the system is capable of measuring.

## 0.2 Method

Some basic assumptions will apply throughout the modeling of dynamics in this paper. They are as follows:

1. The vehicle is a fixed mass.
2. Coriolis effects are negligible.
3. Thrust will be assumed to be 0.

Note that a stationary atmosphere is not assumed. The fixed mass assumption is consistent with the electric aircraft used to test the system. At the altitude and speed at which the vehicles will be tested, Coriolis effects can be ignored<sup>[7]</sup>. The zero-thrust assumption is in place to minimize drag error. Any error in a measured state will decrease the accuracy of the drag measurement, and the accuracy of a given drag measurement can be no better than the worst state measurement error. In-flight thrust is difficult to measure accurately, so a folding propeller will be used, and the motor will be turned off during data acquisition. This will allow the propeller to fold back, eliminating most of the wind-mill drag associated with a stalled propeller.

## Reference Frames

The reference frames used in this paper will follow standard convention<sup>[7]</sup>, but will be repeated for clarity. The NED frame is a vehicle carried frame, with the  $+\hat{i}$  axis pointing due North, the  $+\hat{j}$  axis pointing due East, and the  $+\hat{k}$  axis pointing toward the center of the earth. The body axis system, defined by the body-mounted accelerometer, is a right handed coordinate system, with the  $+\hat{i}$  axis pointing out the nose of the aircraft, the  $+\hat{j}$  axis pointing out the right wing, and the  $+\hat{k}$  axis pointing out the bottom of the vehicle. The wind axes are a vehicle-carried coordinate system, with the origin at the same location as the

body reference frame. The  $\hat{i}$  axis of the wind reference frame points in the direction of the free-stream velocity. The  $\hat{k}$  direction lies in the x-z plane of the body reference frame. The  $\hat{j}$  direction is then defined to be out the right side of the vehicle, in order to follow the right hand rule.

## Equations of Motion

Newton's 2nd Law of Motion states

$$\Sigma \vec{F} = \frac{d}{dt}(m\vec{V}) \quad (0.2.1)$$

where  $\Sigma \vec{F}$  is the sum of all applied forces,  $m$  is the mass of the vehicle, and  $\vec{V}$  is the vehicle's velocity. Using the fixed mass assumption, this reduces to

$$\Sigma \vec{F} = m \frac{d\vec{V}}{dt} \quad (0.2.2)$$

$$= m\vec{a} \quad (0.2.3)$$

The applied forces on the vehicle for drag polar estimation are

$$\Sigma \vec{F} = \vec{F}_A + \vec{F}_G + \vec{F}_T \quad (0.2.4)$$

where  $\vec{F}_A$  accounts for all aerodynamic forces acting on the vehicle,  $\vec{F}_G$  is the force due to gravity, and  $\vec{F}_T$  accounts for forces from the propulsion system, which are assumed to be zero. Aerodynamic forces can be described in the wind reference frame. In general, they are defined as

$$\vec{F}_{A_w} = D\hat{i}_w + Y\hat{j}_w + L\hat{k}_w \quad (0.2.5)$$

where  $D$  is drag force,  $Y$  is side force, and  $L$  is lift force.

The gravitational force on the vehicle acts in the  $+z_{NED}$  direction and is equal in magnitude to the vehicle's weight  $W$ , leading to

$$\vec{F}_{G_{NED}} = 0\hat{i}_{NED} + 0\hat{j}_{NED} + W\hat{k}_{NED} \quad (0.2.6)$$

The aerodynamic and gravity forces can be combined and expressed in the body frame

$$m\vec{a}_b = \vec{F}_{G_b} + \vec{F}_{A_b} \quad (0.2.7)$$

which can then be expressed as

$$m\vec{a}_b - m\vec{g} = \vec{F}_{A_b} \quad (0.2.8)$$

$$m(\vec{a}_b - \vec{g}) = \vec{F}_{A_b} \quad (0.2.9)$$

Then, it is noted that a body mounted accelerometer will not measure  $\vec{a}_b$ , but will instead measure the quantity  $\vec{a}_b - \vec{g}$ . This means Equation 0.2.9 is really

$$\vec{F}_{A_b} = -m\vec{r}_b \quad (0.2.10)$$

where  $\vec{r}_b$  is the reading from a body mounted accelerometer. The aerodynamic forces in wind axes, which is the goal, can then be calculated using a rotation matrix

$$\vec{F}_{A_w} = \bar{R}_w^b \vec{F}_{A_b} \quad (0.2.11)$$

Equations 0.2.10 and 0.2.11 are important, and show that the only sensors necessary for drag polar estimation during gliding flight are a body-mounted accelerometer and an air data system.

## Kalman Filter Usage

This paper utilizes multiple Kalman filters to estimate both regression coefficients and improved states. As a brief overview, the Kalman filter combines the measured state with a predicted state to give an optimal<sup>[8]</sup> estimate of the actual system state.

### Linear Kalman Filter

A linear Kalman filter can be applied<sup>[9]</sup> where the system in question can be described in the form

$$x_k = \bar{A}x_{k-1} + \bar{B}u_{k-1} + w_{k-1} \quad (0.2.12)$$

where  $\bar{A}$  is the state transition matrix,  $x_{k-1}$  is the previous state,  $\bar{B}$  is the input matrix,  $u_{k-1}$  is the input vector, and  $w_{k-1}$  is random process noise.

The measured state is then

$$z_k = \bar{H}x_k + v_k \quad (0.2.13)$$

where  $\bar{H}$  is the output matrix and  $v_k$  is measurement noise.

The Kalman filter operates in a predictor-corrector manner, where the predictor step is often called the *a priori* estimate, and the corrector step is often called the *a posteriori* estimate. The *a priori* state estimate is calculated using prior states and inputs, while assuming no process noise

$$\hat{x}_k^- = \bar{A}\hat{x}_{k-1} + \bar{B}u_{k-1} \quad (0.2.14)$$

The *a priori* estimate of the covariance matrix is projected in a similar manner

$$\bar{P}_k^- = \bar{A}\bar{P}_{k-1}\bar{A}^T + \bar{Q} \quad (0.2.15)$$

where  $\bar{P}$  is the covariance matrix and  $\bar{Q}$  is the process noise matrix.

The Kalman gain is calculated by combining the predicted, *a priori* covariance matrix with the measurement noise covariance matrix  $\bar{R}$

$$\bar{K}_k = \bar{P}_k^- \bar{H}^T (\bar{H}\bar{P}_k^- \bar{H}^T + \bar{R})^{-1} \quad (0.2.16)$$

This optimal Kalman gain is then used to estimate the *a posteriori* estimate of the state and covariance matrix

$$\hat{x}_k = \hat{x}_k^- + \bar{K}_k(z_k - y_k) \quad (0.2.17)$$

$$\bar{P}_k = (\bar{I} - \bar{K}_k \bar{H}) \bar{P}_k^- \quad (0.2.18)$$

where  $y_k$  is the predicted value of  $z_k$  found using the output matrix  $\bar{H}$  and the *a priori* state estimate

$$y_k = \bar{H} \hat{x}_k^- . \quad (0.2.19)$$

Note that Equation 0.2.17 is essentially a weighted average of a measured state and an expected state. The weighting is the Kalman gain, which is related to the ratio of confidence in the measured state and the expected state. For a 1-D case with equal confidence between the measured state and the expected state, the Kalman gain  $\bar{K}_k = 0.5$ , and the Kalman filter becomes a simple mean.

### Extended Kalman Filter

The Extended Kalman filter is used for a non-linear system and is essentially a linearization of a nonlinear plant. A nonlinear system can be described as [9]

$$x_k = f(x_{k-1}, u_{k-1}, w_{k-1}) \quad (0.2.20)$$

$$z_k = h(x_k, v_k) \quad (0.2.21)$$

The process noise  $w_{k-1}$  and measurement noise  $v_k$  are not known (or the Kalman filter would not be necessary), so the states are approximated assuming both noise sources are 0

$$\tilde{x}_k = f(\hat{x}_{k-1}, u_{k-1}, 0) \quad (0.2.22)$$

$$\tilde{z}_k = h(\tilde{x}_k, 0) \quad (0.2.23)$$

The actual states are related to the approximate states by

$$x_k \approx \tilde{x}_k + \bar{A}(x_k - \hat{x}_{k-1}) + \bar{W}w_{k-1} \quad (0.2.24)$$

$$z_k \approx \tilde{z}_k + \bar{H}(x_k - \tilde{x}_{k-1}) + \bar{V}v_k \quad (0.2.25)$$

where the matrices  $\bar{A}$ ,  $\bar{W}$ ,  $\bar{H}$ , and  $\bar{V}$  represent the different Jacobian matrices:

$$\bar{A} = \frac{\partial f_i}{\partial x_j}(\hat{x}_{k-1}, u_{k-1}, 0) \quad (0.2.26)$$

$$\bar{W} = \frac{\partial f_i}{\partial w_j}(\hat{x}_{k-1}, u_{k-1}, 0) \quad (0.2.27)$$

$$\bar{H} = \frac{\partial h_i}{\partial x_j}(\hat{x}_k, 0) \quad (0.2.28)$$

$$\bar{V} = \frac{\partial h_i}{\partial v_j}(\hat{x}_k, 0). \quad (0.2.29)$$

The Extended Kalman filter uses these linearized equations to perform the same process as the linear Kalman filter. Again, the first step is to calculate the *a priori* estimate of the state and the covariance matrix

$$\hat{x}_k^- = f(\hat{x}_{k-1}, u_{k-1}, 0) \quad (0.2.30)$$

$$\bar{P}_k^- = \bar{A}_k \bar{P}_{k-1} \bar{A}_{k-1}^T + \bar{W}_k \bar{Q}_{k-1} \bar{W}_k^T. \quad (0.2.31)$$

Next, the Kalman gain is calculated

$$\bar{K}_k = \bar{P}_k^- \bar{H}_k^T (\bar{H}_k \bar{P}_k^- \bar{H}_k^T + \bar{V}_k \bar{R}_k \bar{V}_k^T)^{-1}. \quad (0.2.32)$$

The Kalman gain is then used to calculate the *a posteriori* estimate of the state and covariance matrix

$$\hat{x}_k = \hat{x}_k^- + \bar{K}_k(z_k - y_k) \quad (0.2.33)$$

$$\bar{P}_k = (\bar{I} - \bar{K}_k \bar{H}_k) \bar{P}_k^- \quad (0.2.34)$$

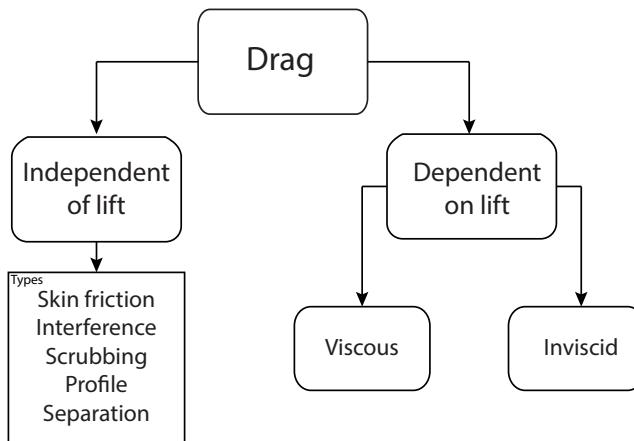
where  $y_k$  is, as in the linear case, the predicted value of  $z_k$ , but calculated using the nonlinear output function and the *a priori* state estimate

$$y_k = h(\hat{x}_k^-, 0). \quad (0.2.35)$$

Unlike the linear Kalman filter, the Extended Kalman filter is not proven to be optimal. However, it has been utilized for a wide range of applications with excellent results.

## 1.0 Drag Meta-Modeling

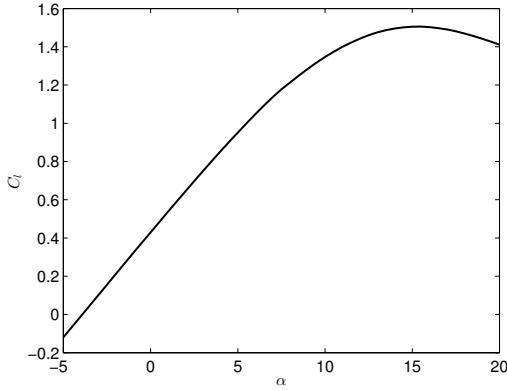
Drag force comes from many different contributions, but can generally be split into drag that is independent of lift, and drag that is due to lift [10]. The summation of all sources of drag that are independent of lift is often called minimum drag ( $C_{D_{min}}$  often used for the coefficient)[2], and is roughly constant, for a given Reynold's number and Mach number. The drag due to lift can be split into viscous drag-due-to-lift and inviscid drag-due-to-lift.



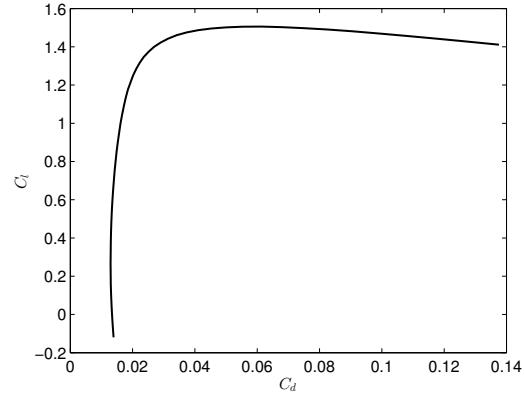
**Figure 1.1: Drag Contribution Types**

The viscous drag-due-to-lift is a type pressure drag that increases when the angle of attack of the wing increases, therefore generating more lift. It is a function of airfoil geometry, such as leading edge radius, thickness distribution, and camber. This type of drag is independent of finite wing vortices, and can be seen on two-dimensional airfoil data charts. To show an example of viscous drag-due-to-lift, a NACA 4412 was analyzed using XFOIL<sup>[11]</sup>.

Figure 1.3 shows the airfoils viscous drag-due-to-lift. Since the shape is roughly parabolic through the linear region of the lift curve, the contribution to the total aircraft drag is



**Figure 1.2: NACA 4412 Lift Curve**

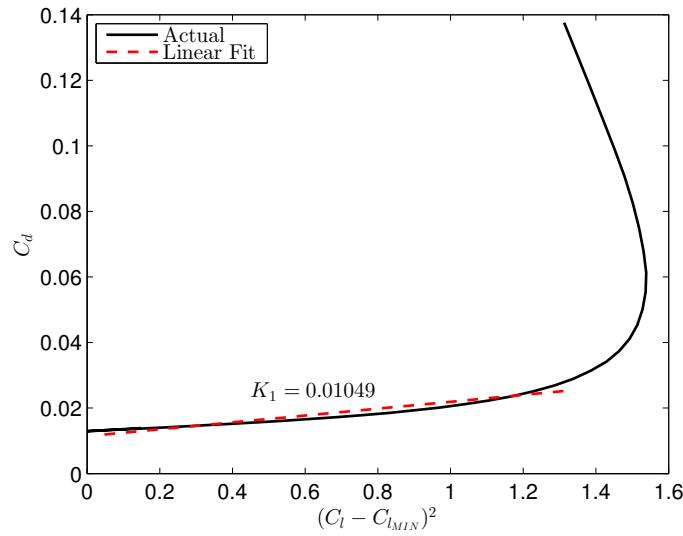


**Figure 1.3: NACA 4412 Drag Polar**

approximated using the Equation 1.0.1<sup>[10]</sup>.

$$C_{D_{Visc,Lift}} = K_1 * (C_L - C_{L_{Min,Drag}})^2 \quad (1.0.1)$$

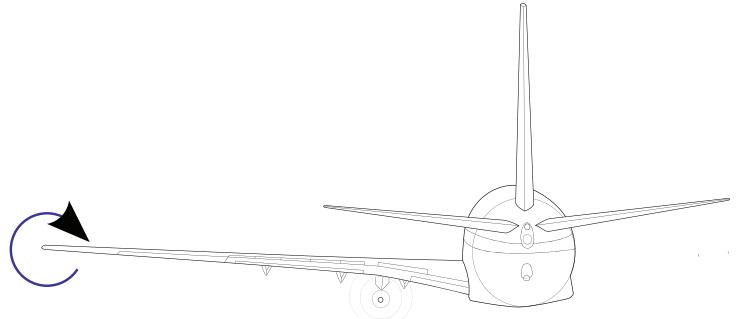
where  $K_1$  is the slope of the line shown in Figure 1.4, and  $C_{L_{Min,Drag}}$  is the lift coefficient at which minimum drag occurs (roughly 0.25 for this airfoil).



**Figure 1.4: NACA 4412  $K_1$  Estimation**

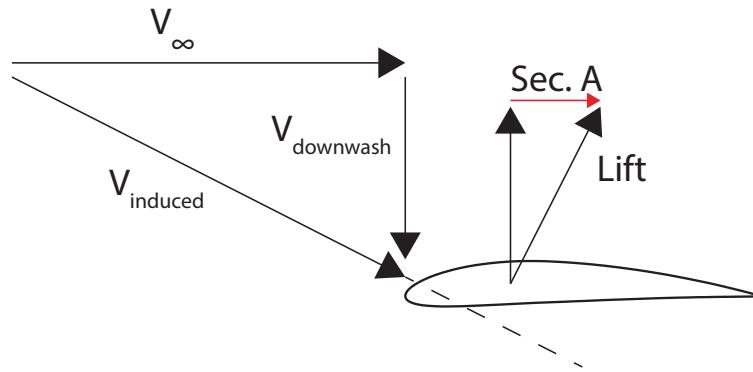
*Inviscid* drag-due-to-lift occurs because of the pressure difference between the top and bottom of a finite wing. This pressure difference causes the high pressure flow underneath

the wing to slip over to the top of the wing, causing a downwash velocity on the free stream velocity, shown in Figure 1.5.



**Figure 1.5: Downwash Caused By Wingtip Vortices<sup>[1]</sup>**

This downwash changes the direction of the flow going into the airfoil. Since lift acts perpendicularly to the flow going into airfoil, there will be an induced angle between the free-stream lift vector (perpendicular to  $V_\infty$ ) and the airfoil's lift vector.



**Figure 1.6: Induced Drag Free Body Diagram**

The red section, labeled Sec. A in Figure 1.6, is a component of the airfoil's lift which is parallel to  $V_\infty$ , meaning the airfoil's lift causes drag on the vehicle.

Induced drag is affected by the span lift distribution and the wing aspect ratio<sup>[12]</sup>, and is governed by Equation 1.0.2.

$$C_{D_i} = \frac{C_L^2}{\pi e A R} = K_2 C_L^2 \quad (1.0.2)$$

These three coefficients ( $C_{D_0}$ ,  $K_1$ , and  $K_2$ ) are combined to result in a parabolic drag polar of the form

$$C_D = C_{D_{min}} + K_1(C_L - C_{L_{MIN}})^2 + K_2 C_L^2 \quad (1.0.3)$$

This drag polar gives valuable insight into how a vehicle will perform. The complete drag polar can be found using various regression techniques, discussed in the following sections.

## 1.1 Regression Model - Least Squares Fit

The standard model for a polynomial regression is

$$\hat{y} = \beta_0 + \beta_1 x + \beta_2 x^2 + \dots \quad (1.1.1)$$

When Equation 1.0.3 is expanded and like-terms of  $C_L$  are combined, equation 1.1.1 becomes

$$C_D = (C_{D_{min}} + K_1 C_{L_{min}}^2) - 2K_1 C_{L_{min}} C_L + (K_1 + K_2) C_L^2 \quad (1.1.2)$$

The value  $(C_{D_{min}} + K_1 C_{L_{min}}^2)$  is referred to as the parasite drag coefficient, and is represented by  $C_{D_0}$ <sup>[2]</sup>. These coefficients can be estimated using an Ordinary Least Squares fit. The Ordinary Least Squares problem statement is as follows

$$\bar{A}\vec{x} = \vec{b} \quad (1.1.3)$$

If  $\bar{A}$  is an  $m \times n$  matrix of measured state data,  $\vec{x}$  is an  $n \times 1$  vector of correlation coefficients, and  $\vec{b}$  is an  $m \times 1$  vector of measured function data, the solution to the Ordinary Least Squares problem is

$$\bar{A}\vec{x} = \vec{b} \quad (1.1.4)$$

$$\bar{A}^T \bar{A}\vec{x} = \bar{A}^T \vec{b} \quad (1.1.5)$$

$$(\bar{A}^T \bar{A})^{-1} (\bar{A}^T \bar{A})\vec{x} = (\bar{A}^T \bar{A})^{-1} \bar{A}^T \vec{b} \quad (1.1.6)$$

$$\bar{I}\vec{x} = (\bar{A}^T \bar{A})^{-1} \bar{A}^T \vec{b} \quad (1.1.7)$$

When applied to estimating a parabolic drag polar, the  $\bar{A}$  matrix becomes

$$\bar{A}_{i,:} = \begin{bmatrix} 1 & C_{L_i} & C_{L_i}^2 \end{bmatrix} \quad (1.1.8)$$

the  $\vec{b}$  vector becomes

$$\vec{b}_i = \begin{bmatrix} C_{D_i} \end{bmatrix} \quad (1.1.9)$$

and the  $\vec{x}$  vector, which is the vector of interest, becomes

$$\vec{x} = \begin{bmatrix} C_{D_0} & -2K_1 C_{L_{min}} & (K_1 + K_2) \end{bmatrix}^T \quad (1.1.10)$$

The coefficients  $C_{D_0}$ ,  $K_1$ , and  $K_2$  can then be found, assuming  $C_{L_{min}}$  is known through wind tunnel testing, XFOIL, CFD, or other means.

## 1.2 Regression Model - Kalman Filter

The coefficients in question can also be estimated using an Extended Kalman filter. The system can again be described as

$$C_D = C_{D_0} - 2K_1 C_{L_{min}} C_L + (K_1 + K_2) C_L^2 \quad (1.2.1)$$

For the Kalman filter regression, the state to be estimated are the coefficients  $C_{D_0}$ ,  $-2K_1 C_{L_{min}}$ , and  $K_1 + K_2$ . For ease of notation, substitute

$$C_1 = -2K_1 C_{L_{min}} \quad (1.2.2)$$

$$C_2 = K_1 + K_2 \quad (1.2.3)$$

Since the regression coefficients should not change, the state transition matrix is an identity matrix, leading to

$$\hat{x}_k = \begin{bmatrix} C_{D_0} & C_1 & C_2 \end{bmatrix} \quad (1.2.4)$$

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (1.2.5)$$

The measured data  $z_k$  is a vector containing the lift and drag coefficients at the  $k$ -th instant in time

$$z_k = \begin{bmatrix} C_D \\ C_L \end{bmatrix} = h(x_k, 0) \quad (1.2.6)$$

The vector  $y_k$  contains the estimates of  $C_D$  and  $C_L$  found using the *a priori* state vector  $\hat{x}_k^-$  and is equal to

$$y_k = \begin{bmatrix} C_{D_0k}^- + C_{1k}^- C_L + C_{2k}^- C_L^2 \\ C_L \end{bmatrix} = h(\hat{x}_k^-, z_k, 0) \quad (1.2.7)$$

To implement into the Extended Kalman filter, the Jacobian of  $h(\hat{x}_k^-, z_k, 0)$  with respect to  $x_k$  needs to be calculated. Once done, the  $H$  matrix in the EKF becomes

$$H_k = \begin{bmatrix} 1 & C_L & C_L^2 \\ 0 & 0 & 0 \end{bmatrix} \quad (1.2.8)$$

With the  $H$  matrix calculated, the EKF algorithm can be implemented as described in Section 0.2. The measurement noise covariance at each instant was calculated by doing error propagation as described in Section 1.3 and the process noise covariance was set to zero because the parabolic regression coefficients should be exactly constant.

### 1.3 Error Analysis

Without estimates of the error in data, the data itself is fairly meaningless. There are two main types of error in the system: model regression error and the error of a single data point. The error of a single data point comes from random noise in sensors, and can be decreased by improving the accuracy of the sensor or filtering the results. The model regression error comes from the fact that every aspect of the dynamics of the system are not precisely modeled. This type of error can be reduced by improving the accuracy of the dynamics being modeled, choosing a better regression model, or by increasing the number of data points collected, discussed later.

#### Random Error

The equations of motion can be used to propagate uncertainty in a signal, and they allow the uncertainty in the coefficients to be estimated based on sensor noise.

The error of a single point is assumed to be random and normally distributed. The first step in error propagation is to define  $y_i$  to be the  $i$ -th entry of the true function vector,  $\hat{y}_i$  to be the  $i$ -th entry of the measured function vector, and to then do a Taylor series expansion about the operating point.

$$\hat{y}_i = y_i + \frac{\partial y_i}{\partial x_j} dx_j \quad (1.3.1)$$

where  $x_j$  is the  $j$ -th element of the state vector. Note that the term  $\frac{\partial y_i}{\partial x_j}$  is the Jacobian matrix ( $J_{ij}$ ) of the state transition function. The error can then be defined as

$$dy_i = \hat{y}_i - y_i = J_{ij} dx_j. \quad (1.3.2)$$

If the error is then interpreted as a discrete difference instead of a continuous difference, Equation 1.3.2 becomes

$$\Delta y_i = J_{ij} \Delta x_j. \quad (1.3.3)$$

If the  $\Delta$  values are further assumed to represent standard deviations of normally distributed error, Equation 1.3.3 becomes

$$\sigma_{y_i} = J_{ij}\sigma_{x_j}. \quad (1.3.4)$$

For the purposes of this research,  $\sigma_{y_i}$  is a vector of the standard deviations of the aerodynamic force coefficients,

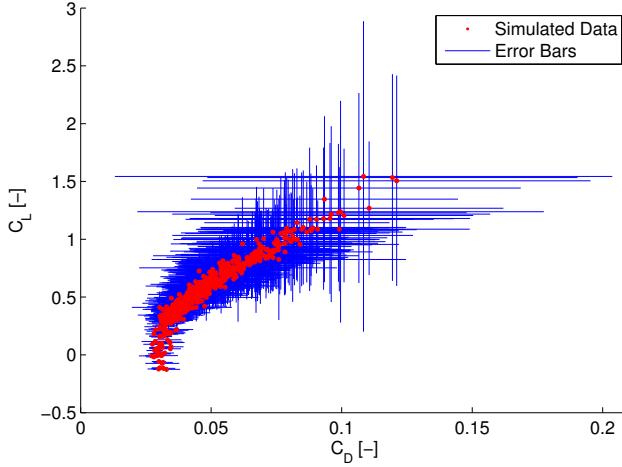
$$\sigma_{y_i} = \begin{bmatrix} \sigma_{C_{D_i}} & \sigma_{C_{Y_i}} & \sigma_{C_{L_i}} \end{bmatrix}^T \quad (1.3.5)$$

and  $\sigma_{x_j}$  is a vector of the standard deviations of the state values,

$$\sigma_{x_j} = \begin{bmatrix} \sigma_{r_{b_j}} & \sigma_{\alpha_j} & \sigma_{\beta_j} \end{bmatrix}^T. \quad (1.3.6)$$

For initial error estimation, the noise levels reported by instrument manufacturers was assumed to be one standard deviation of a normal distribution with mean equal to zero. The Jacobian matrix was calculated at each observed data point and combined with the sensors' standard deviation to produce estimates of the standard deviations of the aerodynamic coefficients.

One of the key findings of this section is that the error of the coefficient depends on the coefficient itself. This means that the error varies from data point to data point, which is called *heteroskedasticity* (as opposed to *homoskedasticity*, which means the error is independent of the state itself). To account for this, an error estimate function was created in MATLAB, which used the error propagation outlined in this section. This function was used whenever an estimate of point error was required, such as for the variance matrix  $P_k$  used in the Kalman filters utilized for state estimation. A plot of simulated flight data is shown in Figure 1.7, where the error bounds shown were calculated using the error estimate function. Note that this figure also shows the heteroskedastic nature of the error.



**Figure 1.7: Heteroskedastic Error from Simulated Flight**

While heteroskedasticity does not color the estimate of  $\hat{\beta}_i$ , it does color the confidence intervals. The method of dealing with this problem is discussed in the next section.

### Least Squares Model Error

The error of a single data point is not the main driving factor in the accuracy of a regression model. The important factor in the model is how accurately the coefficients are known, which is a function of the accuracy of each point, as well as the number of points sampled. The main parameter that describes the accuracy of the regression coefficients are the confidence intervals. A confidence interval is a range of values such that, if the experiment were repeated, the parameter calculated would be within the range some percentage of the time. A parameter can be represented as an estimated value, with a confidence bound

$$\beta = \beta_{EST} \pm t \frac{\sigma}{\sqrt{n}} \quad (1.3.7)$$

where  $\beta$  is the parameter in question,  $\beta_{EST}$  is the estimated value of the parameter,  $t$  is the Student's  $t$  value based on the number of samples and the desired confidence interval,  $\sigma$  is the standard deviation of the sample, and  $n$  is the number of data points collected. Since

the number of data points collected during flight will be large ( $n > 100$ ), the  $t$  value will be taken as 1.96 for a 95% confidence interval.

As previously mentioned, one of the assumptions made in a Least Squares regression is homoskedasticity. However, the error using standard uncertainty propagation is heteroskedastic. This becomes a problem in estimating confidence intervals, because the standard error can be driven by outliers. If each data point had the same error, these outliers could be valid. However, if the data is heteroskedastic, the outlier may have larger error bounds (see Figure 1.7,) meaning the data point is not as likely as it first appears. This fact can drive the standard error estimate to be larger than is appropriate, which leads to a larger confidence interval and possibly a false lack of rejection of the confidence interval's hypothesis test. To account for this, the `robustfit` function in MATLAB was used to estimate both the coefficients and robust standard error estimates. The `robustfit` function calculates heteroskedastically-robust standard error estimates by doing a weighted average, where the weighting is based on a radial basis function. This means that the farther away a data point is from the estimated regression model, the less impact it has on the standard error of the model. The default weighting function used by `robustfit` is bisquare, and it was used for this research.

## Kalman Filter Error

Kalman filters are often used to propagate states. The filter does this by combining the system dynamics with a measured state. The variance is propagated using Equation 0.2.34. When estimating coefficients using the Kalman filter, the  $\bar{A}$  state transition matrix is an identity matrix, which is due to the fact that the coefficients stay constant. When propagated through the filter, this means the state estimate  $x_k$  is essentially a variance-weighted-average of the coefficient estimates. The matrix  $P_k$  contains the variance of the coefficient estimates. Equation 1.3.7 calculates the confidence interval of regression coefficients and needs the standard deviation of the mean, also called the standard error. The matrix  $P_k$  can be used

to calculate the confidence intervals by noting

$$\bar{P}_k = \begin{bmatrix} \sigma_1^2 & 0 & \dots & 0 \\ 0 & \sigma_2^2 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & \sigma_i^2 \end{bmatrix} \quad (1.3.8)$$

The confidence interval for coefficient  $\beta_i$  can be calculated using  $\sigma_i$  in Equation 1.3.7.

## 1.4 Simulation

A 6-DOF flight simulator was used to validate the drag prediction method before hardware was purchased. The main utility of the simulator was to provide simulated flight test data with signals that contained no errors. The actual sensors used for flight testing contain noise, and this noise can be added onto the pure simulator signals to test the sensitivity of the drag polar regression to sensor accuracy.

### Simulation Environment

The flight simulator used was a model of the de Haviland Beaver that comes as a demo in the Aerospace Toolbox of Simulink. The Simulink model was modified to output required signals to the workspace, which essentially created a sensor with zero noise. The mass, moments of inertia, and reference lengths were then scaled to those of a Zagi R/C aircraft<sup>[13]</sup>. The original Simulink model was already connected to a FlightGear Flight Sim, used as a visualization engine. This model was slightly altered to make flight gauges function properly.

### Simulation Inputs

The engine forces and moments were set to zero in the simulator, to match the assumption of a folding propeller. The drag force calculation built into the Beaver Simulink model was replaced with a parabolic drag polar of the form

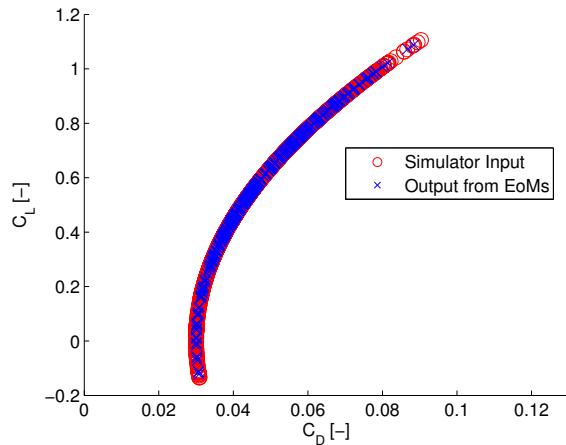
$$C_D = C_{D_0} + K_1(C_L(\alpha) - C_{L_{min}})^2 + \frac{(C_L(\alpha))^2}{\pi e A R} \quad (1.4.1)$$

Airfoil data, including  $K_1$ ,  $C_{L_{min}}$ , and  $C_L(\alpha)$ , was taken from nonlinear aerodynamic data of a NACA 0012<sup>[14]</sup>. While this approximation to a drag polar does not capture the nonlinear

section of profile drag rise due to stall, it does represent the limited lifting capability of a real wing, making it more realistic than assuming the wing does not stall.

## Simulation Results

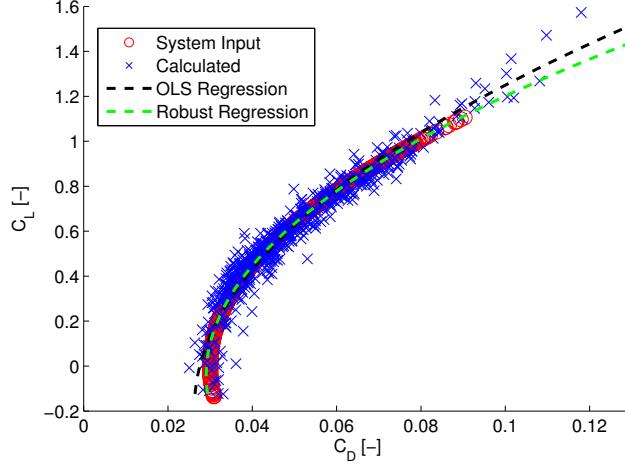
The first goal of the simulation testing was to verify the drag polar equations were correct, and that the data analysis routines developed in MATLAB did in fact match inputs to outputs. The simulation was initialized with various initial states to ensure there was no dependency on initial conditions. The vehicle was then flown by an R/C aircraft pilot using a joystick attached to the simulation. It was noted early in the simulation testing that flying a sweep of speeds was beneficial, as a wider range of the drag polar was flown. This result was included in much of the flight test planning. After adequate data had been taken, the data was analyzed without adding simulated sensor noise. The results in Figure 1.8 show that the equations of motion used in the data analysis functions properly calculate the coefficients being passed into the system.



**Figure 1.8: Data Analysis Verification (No Noise)**

With this result, noise was added to the system to see how sensitive coefficient estimation was to noise in each sensor. This process was a balancing act between available sensor accuracy

and the desired accuracy of the final solution. The final result guided sensor selection to those discussed in Section 1.5. To check if the final sensors chosen were acceptable, Gaussian noise was added to each state, with a mean of zero and a standard deviation equal to the RMS error listed in the manufacturer’s data sheet for each sensor.



**Figure 1.9: Drag Polar Prediction of Simulated Test Flight**

For the particular simulated test flight shown in Figure 1.9, the estimated drag polar coefficients are shown in Table 1.1.

**Table 1.1: Nonlinear Model Results**

	$C_{D_0}$	$K_1$	$K_2$
System Inputs	0.0493	0	0.03
OLS Estimate	0.0355	-0.0136	0.0275
Robust LS Estimate	0.0460	-0.0037	0.0292

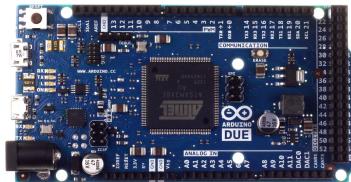
The results of this simulated flight test showed that the measurement system outlined in Section 1.5 predicted the simulated drag polar with a reasonable error. It also demonstrates the necessity of the heteroskedasticity correction, as the OLS regression has a 39% error on  $K_2$  and a 9% error on  $C_{D_0}$ , while the robust regression has a 7% error on  $K_2$  and a 3% error on  $C_{D_0}$ .

## 1.5 Hardware

One of the main goals of this research was to give the designer flexibility in choosing the appropriate sensors for a given flight test. To this end, hardware that is available in breakout boards was given preference, since it gives the aircraft designer more flexibility. The aircraft designer could utilize surface mount components if vehicle integration space is extremely limited, or can use the available breakout boards to make circuit-level integration easier if vehicle space is not a driving flight test concern.

### Flight Computer

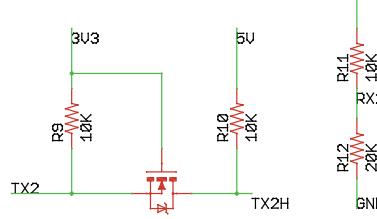
The flight computer chosen was an Arduino Due. This board has a 32-bit ARM processor, 54 digital I/O pins, 12 analog input pins, and 2 analog output pins. The main driver in the decision to use an Arduino-based platform was the vast support community, which allows quicker code development. The Arduino also offers a package that integrates well into most of the available airframes, and the stackable header pins allowed for easy integration with other boards. The Due in particular was chosen as it is (at the time of writing) the most advanced Arduino available. The main advantages it has over the comparable Arduino Mega is its increased clock speed (84 MHz for the Due<sup>[15]</sup> vs 16 MHz for the Arduino Mega<sup>[16]</sup>) and its 32-bit architecture (vs. 8-bit for the Arduino Mega).



**Figure 1.10: Arduino Due Flight Computer**

The Arduino Due uses a 3.3V architecture instead of the usual Arduino architecture, which uses a 5V operating voltage. This was mainly beneficial, since most of the selected

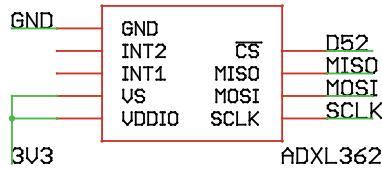
sensors used 3.3V as both supply and logic voltage. Logic level circuits, shown in Figure 1.11, were used to translate to 5V signals where required. The board is powered through the 3.5mm barrel jack, using a 3-cell LiPo battery, with a nominal voltage of 11.1V.



**Figure 1.11: Logic Level Converter Circuit**

## Accelerometer

The accelerometer chosen for the data acquisition system was the ADXL-362 from Analog Devices. It has a noise error of  $175\mu\text{G}/\sqrt{\text{Hz}}$  and uses a 3.3V digital SPI interface<sup>[17]</sup>. The accelerometer is in an LGA package and was surface mounted to the main PCB.



**Figure 1.12: ADXL-362 Schematic**

The accelerometer is calibrated in the field through an optimization routine using MATLAB's `fmincon` nonlinear constrained optimization function. For any given orientation, the accelerometer's reading can be expressed as

$$\begin{bmatrix} r_x & 0 & 0 \\ 0 & r_y & 0 \\ 0 & 0 & r_z \end{bmatrix} \begin{bmatrix} m_x \\ m_y \\ m_z \end{bmatrix} + \begin{bmatrix} b_x & b_y & b_z \end{bmatrix} = \begin{bmatrix} (G_x - a_x) & (G_y - a_y) & (G_z - a_z) \end{bmatrix} \quad (1.5.1)$$

where the  $r$  terms are the bit readings from the accelerometer for each axis, the  $m$  terms are the slope of a linear fit for each axis, the  $b$  terms are the zero offset of a linear fit for each axis, and the  $a$  terms are the actual accelerations.

The slope and offset terms can be found through field calibration and a nonlinear optimization routine. The algorithm uses the fact that, while in a static orientation, the magnitude of the measured vector should be exactly 1G. The optimization problem is then

$$\underset{x}{\text{minimize}} \quad f(x) = \sqrt{(1G - |\vec{t}|)^2} \quad (1.5.2)$$

where  $\vec{t}$  is the right hand side of Equation 1.5.1, and the variable of interest  $x$  is the vector of slopes and offsets in Equation 1.5.1. The slope terms in  $x$  are constrained to be positive. To be a deterministic system of equations, at least six static orientations are required. To avoid the noise of a single reading, the problem was expanded to take 100 data points in six different static orientations, and Equation 1.5.1 was expanded to become a least squares problem. The main benefit of this technique is that field calibration can be accomplished without needing precise knowledge of the orientation of gravity with respect to the sensor during the calibration routine. When tested, the results of the calibration were consistent between this algorithm and using known orientations. For error propagation, the noise during calibration was taken as the sensor's noise level.

## Vehicle Mass

All test vehicles were weighed using a U-Line H-1650 counting scale. The scale has an accuracy of 0.001 lbs and a maximum capacity of 30 lbs. The minimum capacity of the scale is 10 grams [18].

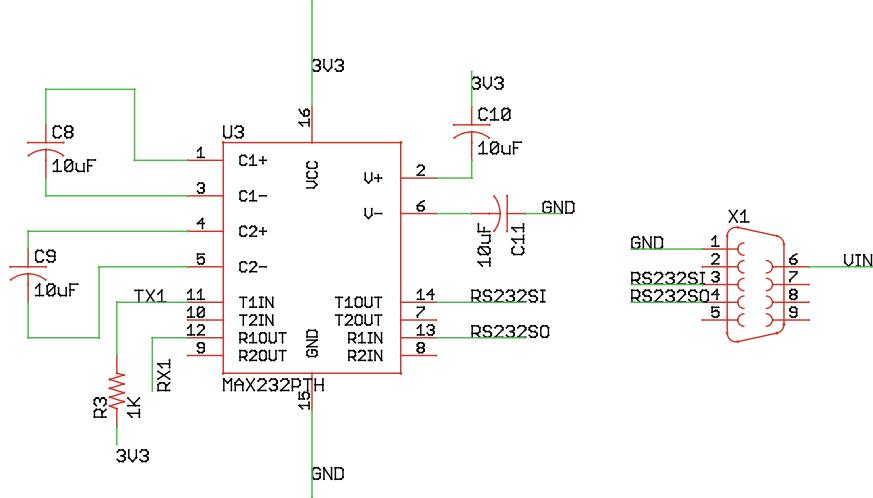
## Magnetometers

Two separate magnetometers were used for separate purposes. A Honeywell HMR-2300 3-D magnetometer, shown in Figure 1.13, is the main magnetometer. It is used when extremely accurate heading information is needed, or when GPS course is unavailable, such as during extremely slow or vertical flight.



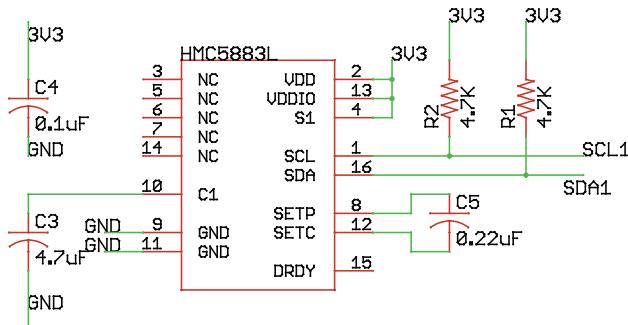
**Figure 1.13: Honeywell HMR-2300 3-D Magnetometer**

This magnetometer provides a RMS error of 0.1 milliGauss for all axes, using the 1 Gauss full-scale setting<sup>[19]</sup>. The HMR-2300 can be supplied with power between 6V and 15V, so the 3-cell 11.1V nominal LiPo battery that powers the Arduino also passes through to power the magnetometer. The HMR-2300 operates using an RS-232 serial interface. To properly interface with the Arduino Due, which uses 3.3V TTL logic levels, a Max-3232 IC was used. This IC, when combined with charge pump capacitors, translates TTL levels between 3V and 5.5V to RS-232 logic levels of  $\pm 6V$ .



**Figure 1.14:** HMR-2300 Logic Level Circuit

The second magnetometer is a Honeywell HMC-5883L, which comes in an LCC package that was surface mounted to the main sensor board. It was added to the system for two main reasons: it is much smaller for applications where size is critical, and it is much less expensive for testing with unproven vehicles. It communicates with the Arduino using an I<sup>2</sup>C interface and uses a 3.3V operating voltage<sup>[20]</sup>. The HMC-5883L has an accuracy of 2 milliGauss on each axis.



**Figure 1.15:** HMC-5883L Schematic

Both magnetometers were calibrated for both soft-iron and hard-iron effects<sup>[21]</sup>. To do this, data was acquired for 10 seconds with the magnetometer being swept through all directions. An ellipsoid was fit to the data using a ordinary least squares method available from the

MATLAB file exchange<sup>[22]</sup>. The least squares fit estimates the center and radius of each axis. The center values for each axis was subtracted from the readings to remove hard-iron effects. Each  $i$ -th axis is then scaled by  $\frac{1}{R_i}$  to reshape the ellipse into a circle, which removes soft-iron effects.

The surface-mounted HMC-5883L was assumed to be aligned with the surface-mounted accelerometer. Since the two magnetometers both measured the North vector, a rotation matrix that describes the difference in alignment between the two sensors can be calculated by

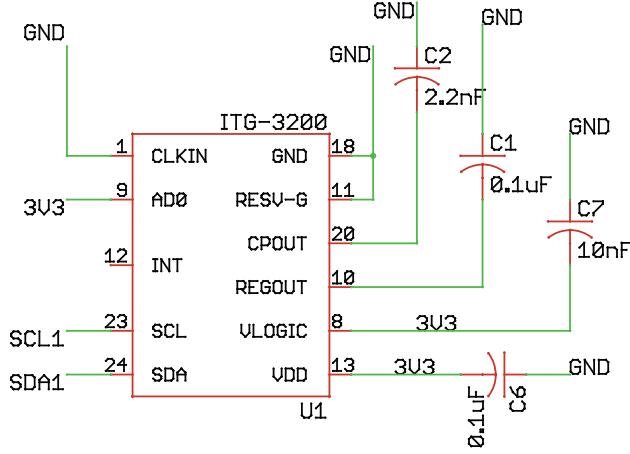
$$\vec{N}_{HMC5883} = \bar{R}_b^{M_1} \vec{N}_{HMR2300}. \quad (1.5.3)$$

The rotation matrix  $\bar{R}_b^{M_1}$  can then be used to align the HMR-2300's coordinate system with the body mounted accelerometers, using

$$\vec{N}_b = \bar{R}_b^{M_1} \vec{N}_{HMR2300}. \quad (1.5.4)$$

## Gyroscope

A three-axis gyroscope was also included in the system. The gyroscope chosen was the Invensense ITG-3200, which comes in a QFN package. This gyroscope has a total error of  $0.38^\circ/\text{s-rms}$ <sup>[23]</sup>, and uses a digital I<sup>2</sup>C interface on a 3.3V operating voltage. This gyroscope has a full-scale span of  $\pm 2000^\circ/\text{s}$ .



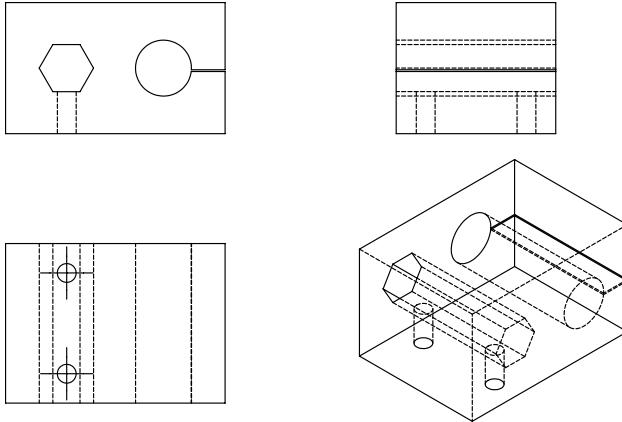
**Figure 1.16: ITG-3200 Eagle Schematic**

The gyroscope was calibrated in the same manner as the accelerometer. The device was placed in six orientations on a turn table which rotated at a constant  $33 \frac{1}{3}$  RPM. Slope and offset values for each axis were calculated using `fmincon`. Before each flight test, the offset values were re-calculated by taking 10 seconds of static readings.

## Air Data System

A five-hole probe was chosen to measure aerodynamic angles as they do not contain moving parts and can provide very accurate, repeatable data. The five-hole probe selected was the Aeroprobe Air Data probe. It is 6 inches long, has a diameter of 1/8 inch, and uses a 0.25" hexagonal section as its mounting section. The probe comes factory calibrated from angles to pressure readings, and was calibrated at an airspeed of 70 ft/s.

The probe was extended roughly one chord length in front of the leading edge of the wing by a 0.25" carbon fiber tube and an aluminum adapter which connected to the probe using set screws.



**Figure 1.17: Five-Hole Probe Adapter**

The adapter was manufactured to be square to itself and to have the reference flat of the probe's hexagonal section be parallel to one side of the adapter. An accelerometer was then glued to a side of the adapter, and the accelerometer was calibrated to the block using a level surface and the flat sides of the adapter. Before each flight test, three static readings are taken of the adapter's accelerometer and the main body-mounted accelerometer. Since the probe's orientation with respect to the adapter's accelerometer is known, this allows the wind angles measured by the probe to be calculated with respect to the body axes, and gives an accurate alignment of the wind reference frame to the body reference frame.

Each pair of lines of the five-hole air data probe is connected to an All Sensors digital differential pressure sensor with a full scale range of  $\pm 5$  in-H<sub>2</sub>O<sup>[24]</sup>. The static port of the five-hole probe was connected to an All Sensors BARO-DO digital barometric pressure sensor, which has a range of 600 to 1100 mBar<sup>[25]</sup>. The barometric pressure sensor comes in the same package and uses the same communication protocol as the differential pressure sensors.



**Figure 1.18: All Sensors 5-INCH-D-DO Pressure Sensor**

The differential pressure sensors have a total error band of 0.25% FSO, and the barometric pressure sensor has a nominal error of 1 mBar. They use a UART serial interface that operates on a 5V logic level, so the logic levels were converted to the 3.3V levels of the Arduino Due. The serial interface includes addressable read commands, which allows multiple devices on a single bus, and ensures all devices record pressure at the same time. The sensor can output both a 14-bit pressure reading and a 12-bit temperature reading, which the device uses to correct its pressure measurement.

A digital temperature sensor was combined with the barometric pressure sensor to estimate the air density, which allowed air speed to be calculated.



**Figure 1.19: Dallas Semiconductors' DS18B20 Digital Temperature Sensors**

The DS18B20 from Dallas Semiconductors was chosen for its relatively simple One-Wire interface. The device can be powered with the communication line and has a  $\pm 0.5^{\circ}\text{C}$  nominal accuracy<sup>[26]</sup>.

The differential pressure sensors were calibrated for slope using a Reference Pressure Recorder from Crystal Engineering<sup>[27]</sup>. This calibration unit is capable of 0.025% of reading. The zero offset of each differential pressure sensor was removed before each flight by taking 100 data samples in a no-wind condition. The barometric pressure transducer and the temperature sensor were calibrated for offset using a Paroscientific Model 745 Pressure Standard, capable of 0.008% FSO accuracy<sup>[28]</sup>.

### Wind Angle Kalman Filter

To improve the accuracy of the wind angle estimation, a discrete Extended Kalman filter was used. The state transition functions are

$$\dot{\alpha} = \frac{1}{V \cos \beta} (-a_x \sin \alpha + a_z \cos \alpha) + q - (p \cos \alpha + r \sin \alpha) \tan \beta \quad (1.5.5)$$

$$\dot{\beta} = \frac{1}{V} (-a_x \cos \alpha \sin \beta + a_y \cos \beta - a_z \sin \alpha \sin \beta) + p \sin \alpha - r \cos \alpha. \quad (1.5.6)$$

These state transition equations come from solving for the vehicle forces in wind axes instead of body axes<sup>[7]</sup>. The equations for the Kalman filter for the wind angles are

$$\begin{bmatrix} \alpha_k \\ \beta_k \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} \alpha_{k-1} \\ \beta_{k-1} \end{bmatrix} + \begin{bmatrix} \Delta T & 0 \\ 0 & \Delta T \end{bmatrix} \begin{bmatrix} \dot{\alpha}_k \\ \dot{\beta}_k \end{bmatrix} + \hat{w}_{k-1} \quad (1.5.7)$$

$$z_k = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} \alpha_k \\ \beta_k \end{bmatrix} + \hat{v}_{k-1}. \quad (1.5.8)$$

The process covariance matrix was calculated using the error propagation discussed in Section 1.3 and the standard deviation data from the zero offset calibration of each of the applicable sensors. The measurement noise covariance matrix was calculated based on the standard deviation data for the zero offset of each pressure transducer connected to the five-hole probe.

## GPS Receiver

A uBlox LEA-6T GPS receiver was included in the data acquisition system. This model was selected for its ability to output raw timing data, which can be used to get an extremely accurate inertial velocity estimate<sup>[29]</sup>. The receiver itself was integrated onto a breakout board sold by CSG Shop, which has UART, USB, and I<sup>2</sup>C interface options.



**Figure 1.20: CGS Shop Board for uBlox LEA-6T**

## Data Acquisition System Integration

The sensors were packaged into a main shield for the Arduino. This shield plugs directly into the Arduino, eliminating the need to disconnect and reconnect wiring. Header pins capable of reading commanded PWM signals to servos were also added on the main board. Future work could include stability derivative estimation, and the header pins provide PWM measurement, which can map to servo angles, if it is assumed the servo is not stalled. The servo signal breakout pins also allowed the data to be easily split into sections with and without commanded throttle for drag polar estimation without thrust.

A second board was developed to integrate the air data system with the main sensor board. This pressure board can be located near a wing tip and provides expandability should additional sensors be desired in the future. It also interfaces with the temperature sensor,

which is located in the air flow. Finally, all data was saved to a microSD card attached to the main sensor board. Data was saved in binary format for both increased speed and file size reductions. Once on the ground, the data is converted to meaningful values using a custom MATLAB data parser.

## 2.0 Flight Test

Flight testing was done at Cal Poly’s Educational Flight Range (EFR). The goal of flight testing was to validate the performance of the final system design. The drag polar estimation was chosen as the validation case, and was approached from each of the three coefficients. To this end, the final system was flown on multiple vehicles which each had a different role in the validation routine.

### 2.1 $C_{D_0}$ Validation

Validation of the parasite drag coefficient was completed using a Finwing Universal Penguin FPV R/C aircraft<sup>[30]</sup>.

This model was selected because it has a large internal payload bay which has plenty of room for the system and had enough excess power to overcome additional drag. The validation method involved flying the base model and measuring the drag polar. Then, parasite drag was added in the form of streamers, similar to those used in amateur rocketry recovery. The benefit of this technique is that it does not modify either of the other two drag polar coefficients. A power law fit to the expected drag coefficient of the streamers was given in [31]. The validation routine was flying the vehicle with and without streamers and seeing the horizontal shift in the drag polar.

### 2.2 $K_1$ Validation

The  $K_1$  term of the drag polar is mainly driven by the  $C_L$  for minimum drag. To validate this coefficient, a custom test vehicle was manufactured with two different wings of equal area. One wing had a NACA 63-014 airfoil cross section, which is a symmetric airfoil, meaning the vehicles  $K_1$  value should be zero. The next wing had a NACA 63-614 airfoil, which has a

design  $C_L$  for minimum drag of 0.6. The validation method was flying both of these wings on the same vehicle, and seeing the vertical shift in the drag polar.

### 2.3 $K_2$ Validation

The  $K_2$  drag polar coefficient is the inviscid drag due to lift term. This form of drag comes from the wing tip vortices of a finite wing, and is affected by both wing aspect ratio and lift distribution. Prandtl showed experimentally<sup>[12]</sup> that, for rectangular wings with aspect ratios between one and seven, the drag coefficient corresponding to one aspect ratio can be scaled to that of a different aspect ratio using the equation

$$C_{D,1} = C_{D,2} + \frac{C_L^2}{\pi e} \left( \frac{1}{AR_1} - \frac{1}{AR_2} \right) \quad (2.3.1)$$

The  $K_2$  validation uses this fact by flying the same test aircraft with two different sets of wings with the same area. The first wing has an aspect ratio of three, while the second wing has an aspect ratio of seven. The  $AR = 3$  wing was then corrected to the  $AR = 7$  wing and the resulting drag polar should fall on top of each other.

## 2.4 Results and Future Work

The system was built and tested to prove functionality. After functionality testing was complete, the system was integrated into a 0.40-size Piper Cub R/C aircraft.



**Figure 2.1:** System Integration into 0.40-size R/C Piper Cub

After integration, an initial test flight was conducted. Unfortunately, an electrical short-circuit caused the vehicle to crash and corrupted some data, so no aerodynamic force estimation has been conducted. However, the micro-SD card did survive the crash, and provided enough data to show the system was collecting data as expected before the short-circuit.



**Figure 2.2:** Pre-Flight System Checks



**Figure 2.3:** Crashed Vehicle in Water

The small amount of data collected was analyzed using a user interface developed to rapidly process the data acquisition system’s files. This user interface will allow designers to analyze data immediately following a test flight and make corrections to the test flight program while still at the test flight location.

Due to the vehicle crash, the accuracy of the system developed still needs to be extensively validated. The immediate future work following this paper will be quantifying the accuracy of the system, as well as verifying reliability and safe integration into multiple unmanned systems. Most of the accuracy estimation will be accomplished by measuring changes to a vehicle’s drag polar. The ability to measure parasite drag will be proven by adding payloads with a known drag coefficient to “dirty” the aircraft, and then measuring the change in the parasite drag coefficient of the test vehicle. To quantify the accuracy of drag-due-to-lift measurement, wings with different aspect ratios will be used on the vehicle, which should combine into a single equivalent curve<sup>[12]</sup>. Following the accuracy estimation, a sensor fusion algorithm will be developed to combine inertial sensors with the air data system and other available sensors in a manner similar to other current research,<sup>[32],[33]</sup> in order to give full situational awareness to the UAS. This situational awareness could allow stability and control derivative estimation, which the aircraft designer could use to size tail and control surfaces.

### **3.0 Summary**

This is the summary chapter.

## A.0 System Usage

This section documents the steps required for correct usage of the data acquisition system.

### A.1 Zero Offset Calibration

Before installing the data acquisition system in the aircraft, wind-off zero calibration should be acquired for the pressure sensors. To do this, connect one port to the other on each of the differential pressure sensors, then acquire data for some amount of time. Take note of these values.

### A.2 Post Flight Zero Offset Calibration

After the flight is complete, a second round of zero offset calibration data should be acquired. This set ensures that any drift that occurred during the flight is accounted for. Repeat the steps outlined in Section A.1.

### A.3 Software Usage

Let's talk about how to use that sweet GUI of yours.

## B.0 Flight Test Procedure

This section documents the flight test procedure for using the data acquisition system. It is split into three time periods

1. Pre-Flight Preparation
2. Flying Field Procedure
3. Post-Flight

The testing procedure is split into these time categories to ensure the testing is efficient and that any unforeseen circumstances can be dealt with quickly. Specifically , this guide applies to the Cal Poly Flight Lab testing a vehicle at the Cal Poly Educational Flight Range. In general, it is better to flight test early in the morning, since there will be less people at the field, winds will be calmer, and the sun won't be as harsh in the pilot's eyes.

## B.1 Pre-Flight Preparation

The preparation work required for a test flight is often overlooked, and this section will documents how to effectively flight test a vehicle. The main purpose of pre-flight preparation is to minimize the possibility of problems that might force a test to be canceled after already going to the field.

### B.1.1 Day Before Test

The following should be done the day before a flight test:

1. Charge all flight battery packs, including any receiver or auxillary packs.
2. Charge the transmitter battery.

3. Ensure the airframe is structurally sound (wing tip test minimum.)
4. Verify radio system communicates properly, and the correct fail-safe is in place. **Important:** If the receiver has been used by Design/Build/Fly, the fail-safe should be changed to normal mode.
5. Verify control surface deflections matches desired directions, and all radio mixes work.
6. Verify the motor/propeller spin in the correct direction.
7. Pack a flight box, containing any necessary tools (recommend: screw drivers, various tapes, razor blades, CA glue, spare propeller, paper and pencil, as a minimum.)
8. Check the weather. The closest monitoring station to the field is KCASANLU17.
9. Check the SLO Flyers' flight schedule. Some days are reserved for certain events (glider competitions, etc.) and these need to be worked around.
10. Make sure all required personnel know when and where to meet, and there are sufficient rides to get to the field.
11. Create flight documentation that clearly lays out the test goals and how they will be accomplished. Print copies for all personnel.

### B.1.2 Day Of Test

The following should be done the morning of a flight test:

1. Pack flight batteries into flight box, including receiver and auxillary packs.
2. Pack battery charging equipment, with adapters and leads, if necessary.
3. Pack transmitter into box.
4. Double check control surface deflections and radio link.

5. Do a full system check, potentially including a short taxi test in the quad.
6. Do a final check that all equipment made it into vehicles, before leaving the lab.

## B.2 Flying Field Procedure

With the pre-flight preparation completed, the testing at the flying field should be fairly event free. Any problems that occur should be either fixable with the minimum supplies in the flight box, or the test should be canceled to minimize risk, and repairs done at the lab. Specific procedures at the flight field will depend on the test being conducted, but below are steps that apply to nearly all tests before flight.

1. Verify structural integrity using a wing tip test.
2. Verify motor/propeller are spinning in the correct direction.
3. Verify radio link and fail safe mode.
4. Verify control surface deflections match desired directions.
5. Verify center of gravity is at an appropriate location.
6. Create flight timer on the transmitter so the pilot knows how long the aircraft has been flying.

## C.0 $C_{D_0}$ Flight Test Card

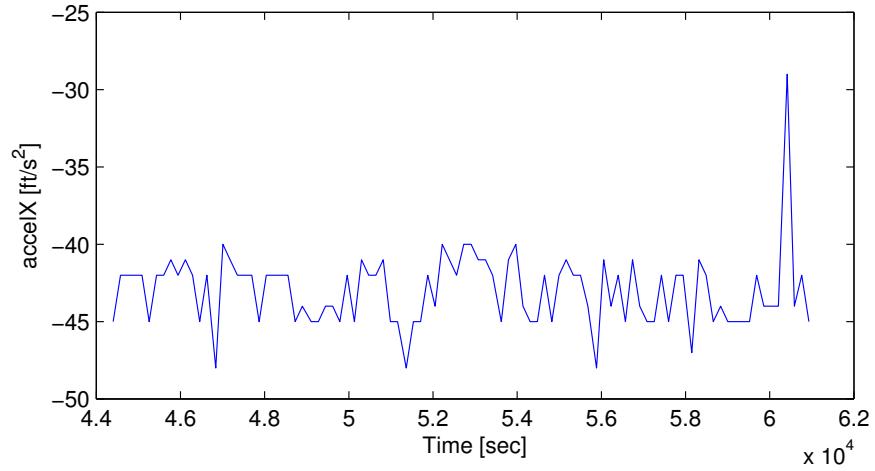
## D.0 $K_2$ Flight Test Card

## **E.0 Sample System Ouput**

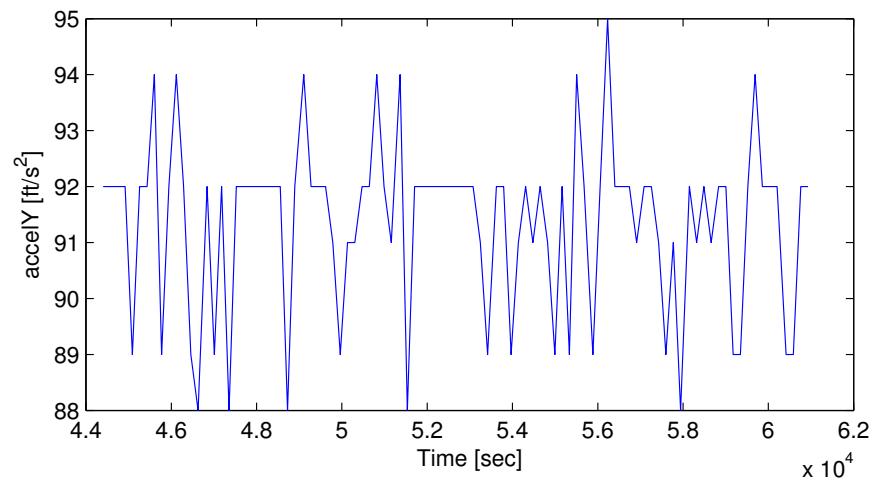
This appendix contains graphs representing typical outputs from the data acquisition system, shown in strip chart format.

### **E.1 Sample System Ouput - Raw Data**

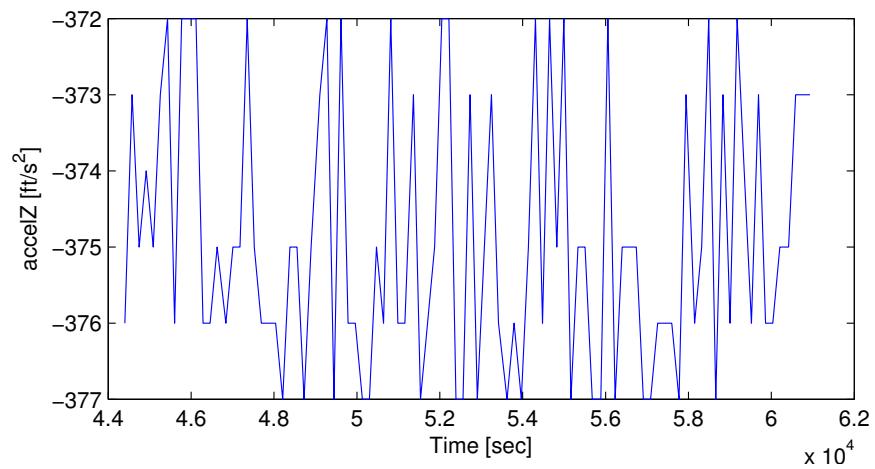
**Figure E.1: accelX vs. Time**



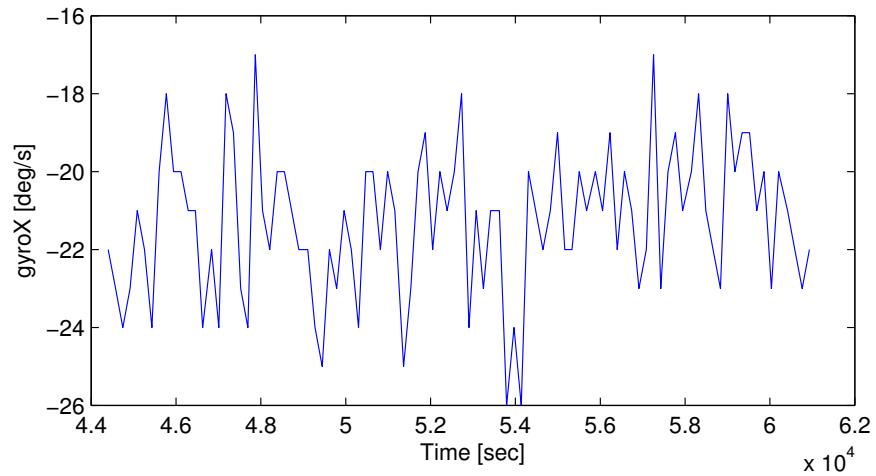
**Figure E.2: accelY vs. Time**



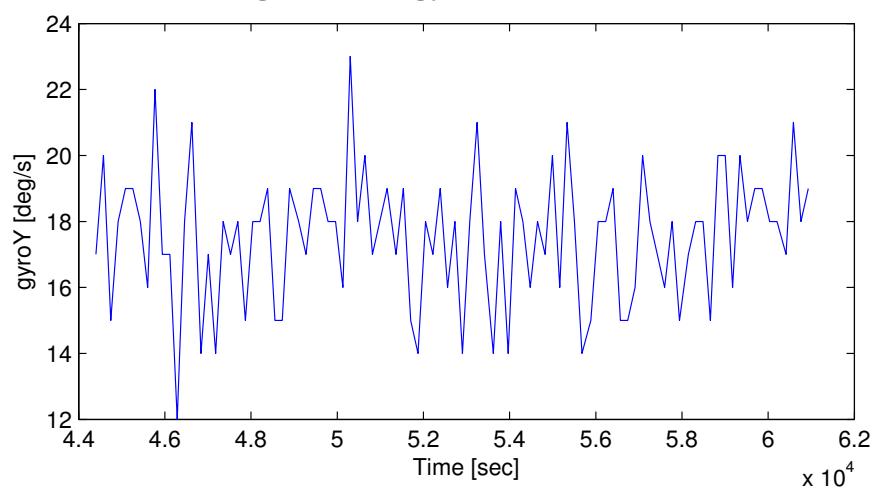
**Figure E.3: accelZ vs. Time**



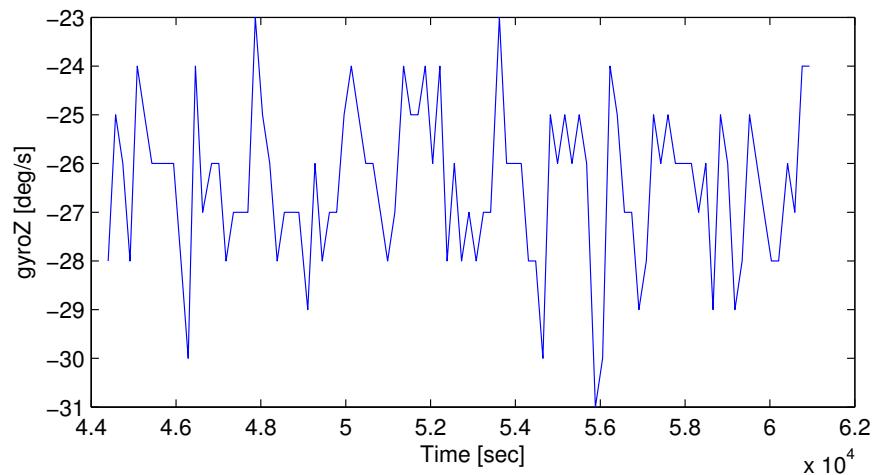
**Figure E.4: gyroX vs. Time**



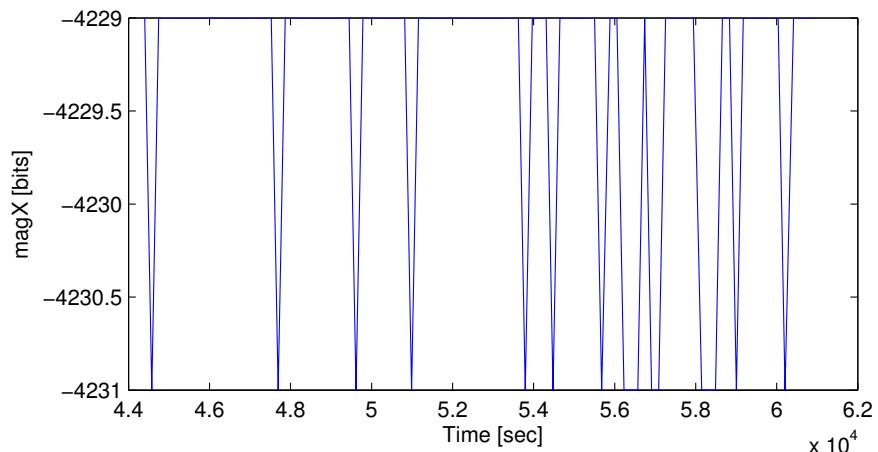
**Figure E.5: gyroY vs. Time**



**Figure E.6: gyroZ vs. Time**

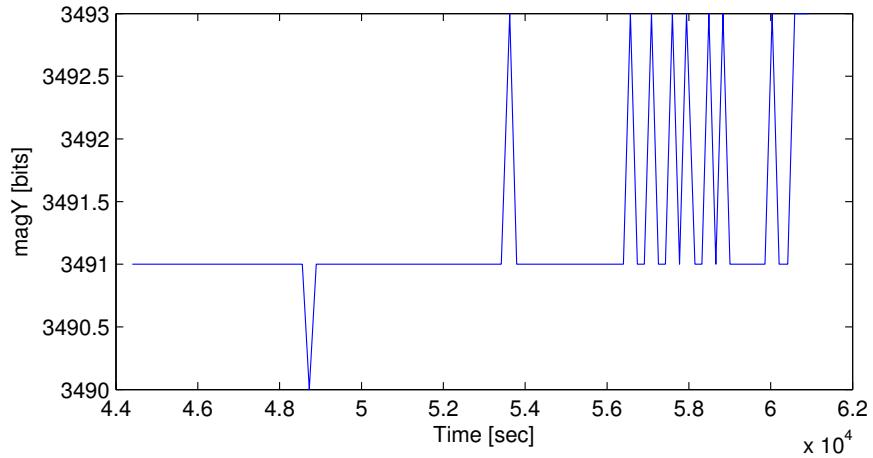


**Figure E.7: magX vs. Time**

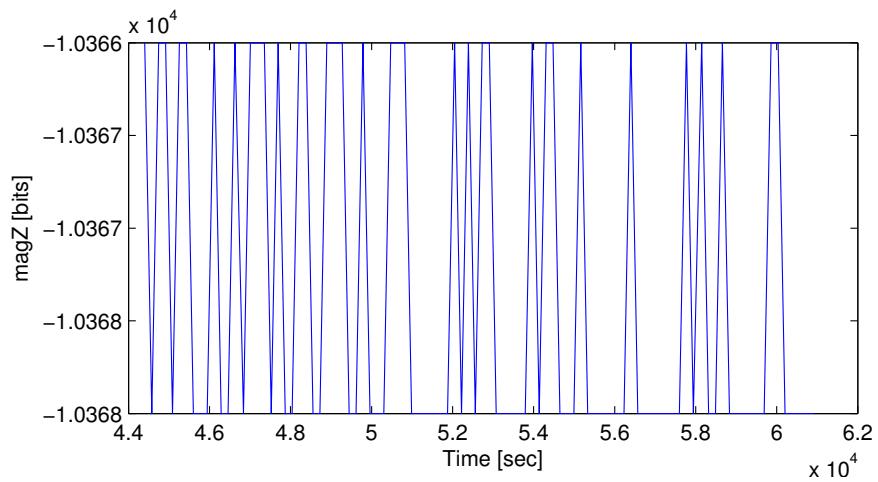


## E.2 Sample System Ouput - Units Data

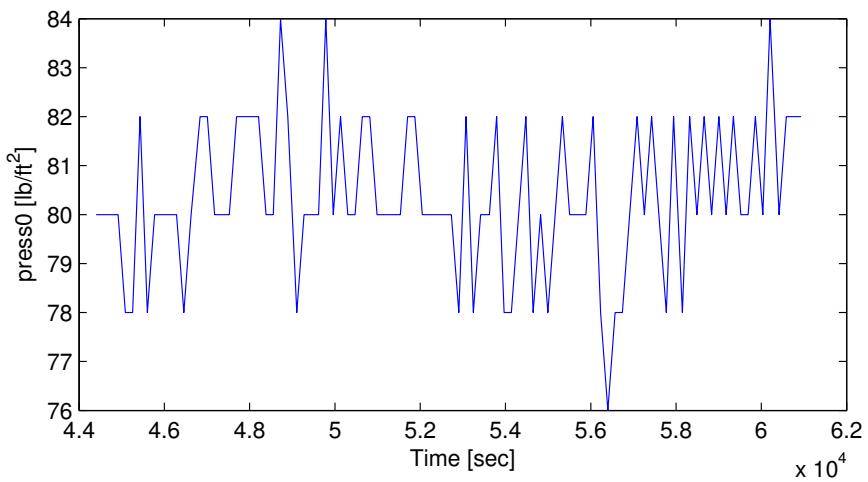
**Figure E.8: magY vs. Time**



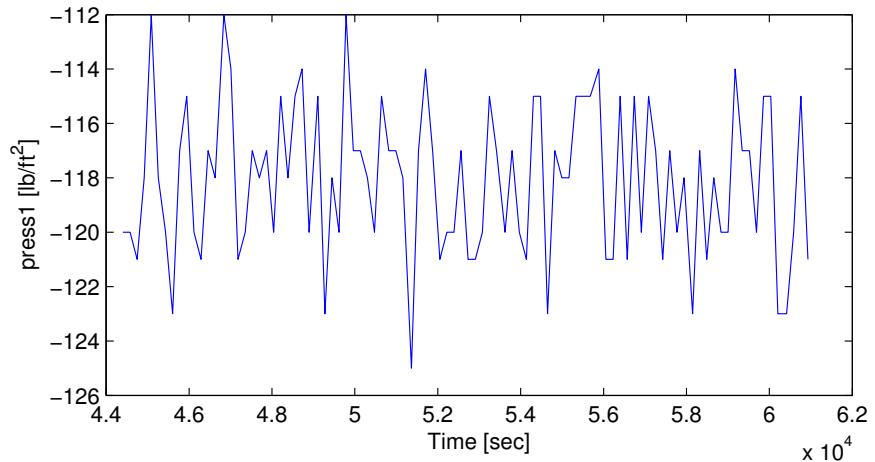
**Figure E.9: magZ vs. Time**



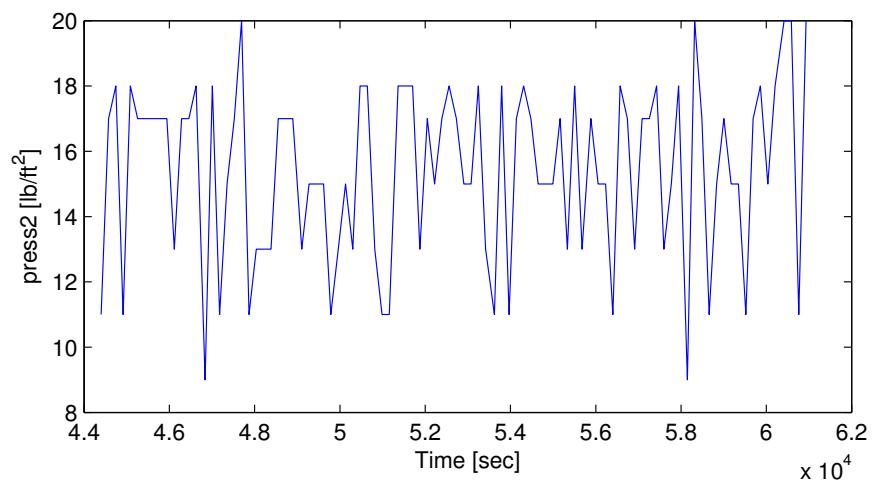
**Figure E.10: press0 vs. Time**



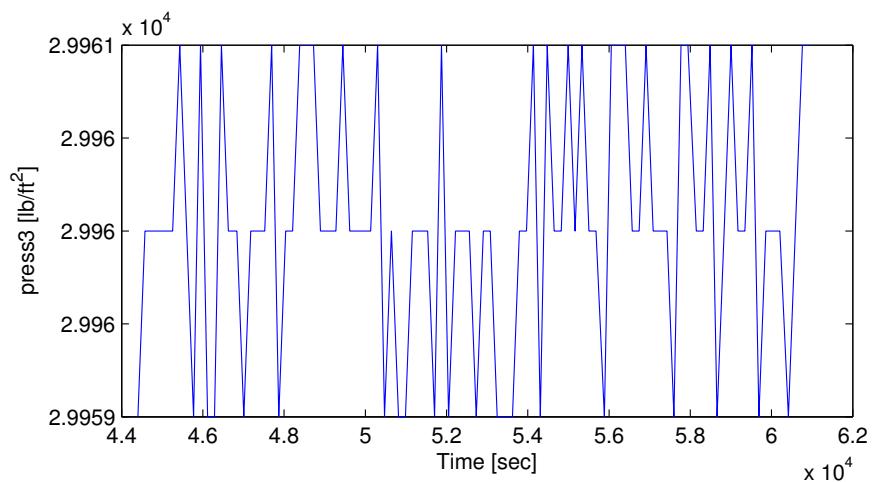
**Figure E.11: press1 vs. Time**



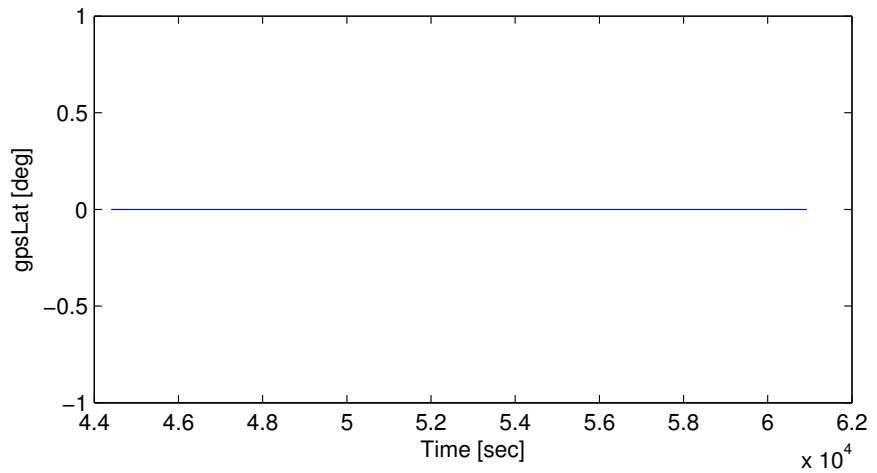
**Figure E.12: press2 vs. Time**



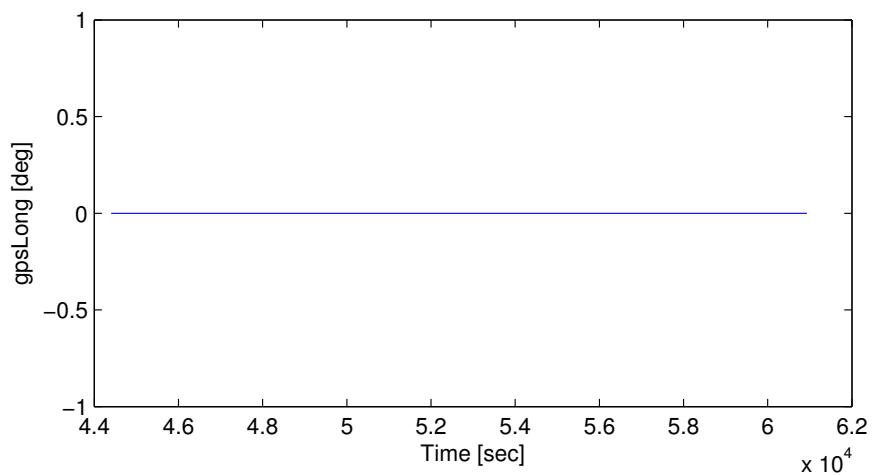
**Figure E.13: press3 vs. Time**



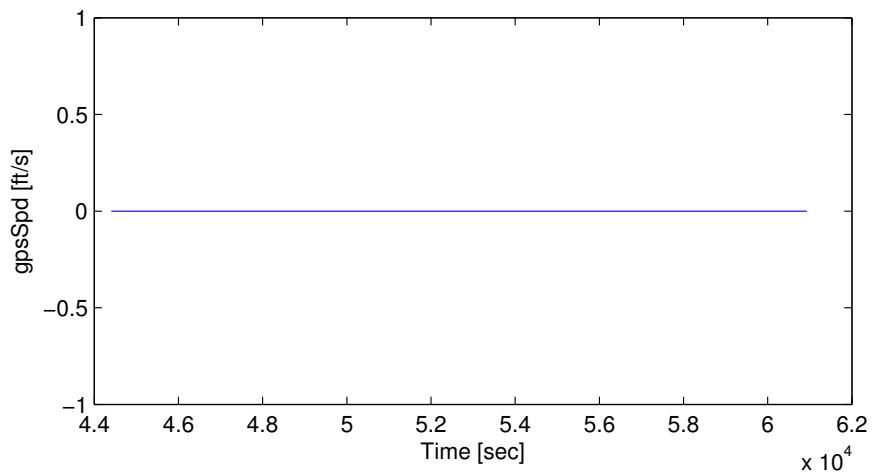
**Figure E.14: gpsLat vs. Time**



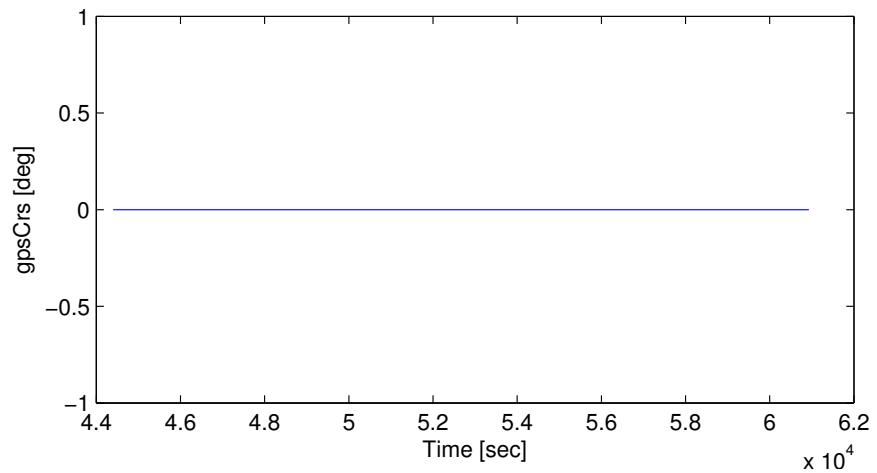
**Figure E.15: gpsLong vs. Time**



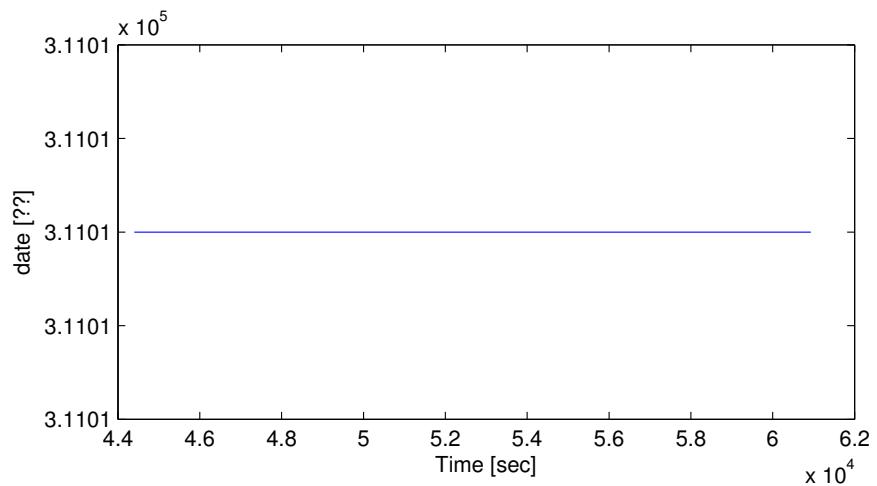
**Figure E.16: gpsSpd vs. Time**



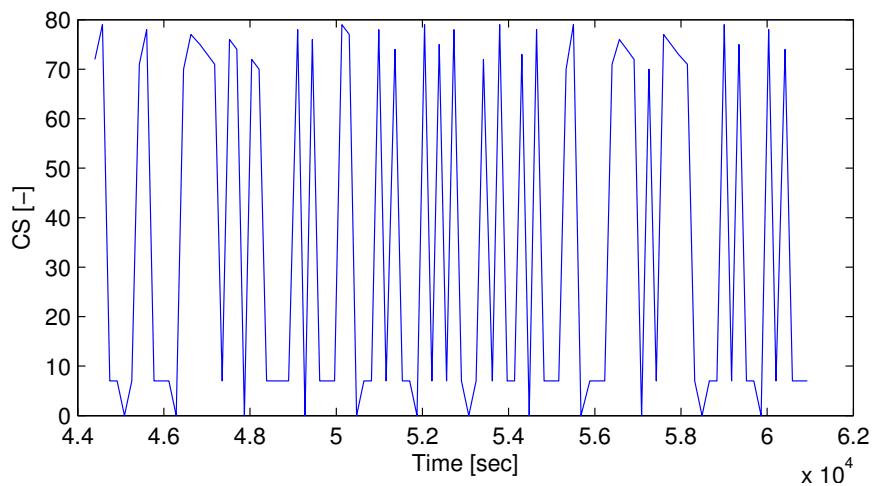
**Figure E.17: gpsCrs vs. Time**



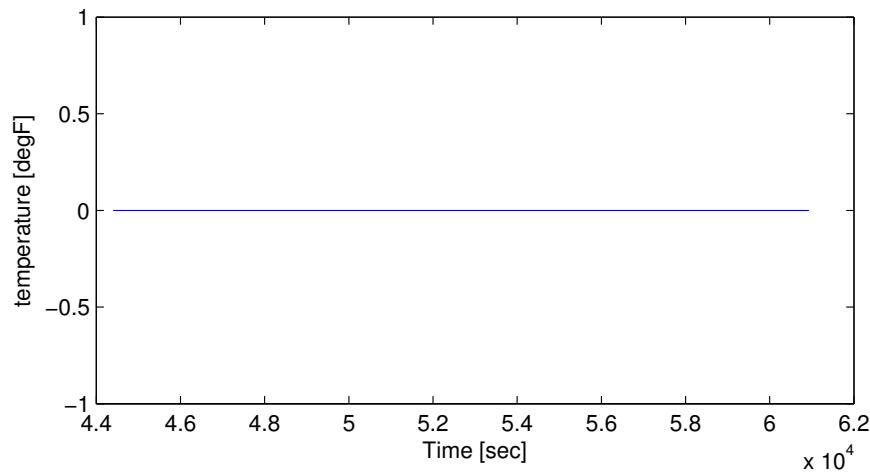
**Figure E.18: date vs. Time**



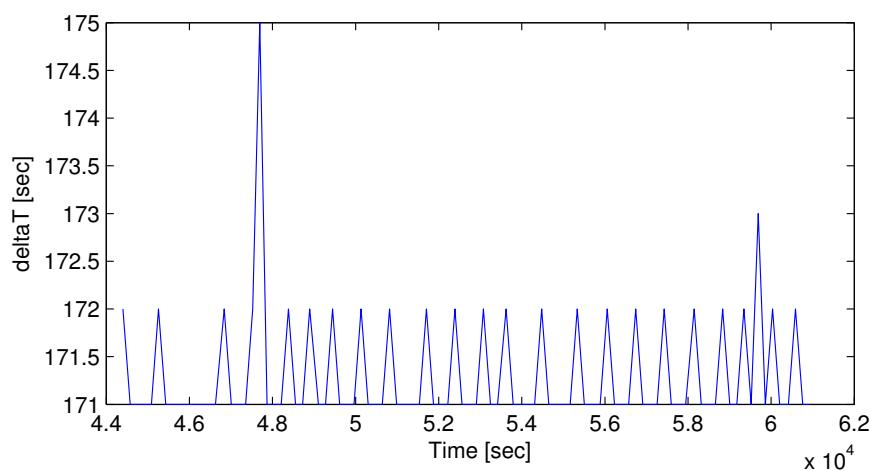
**Figure E.19: CS vs. Time**



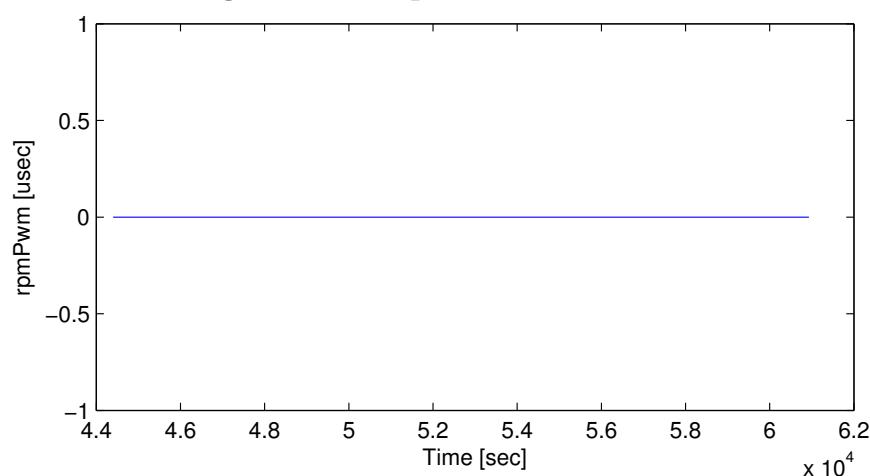
**Figure E.20: temperature vs. Time**



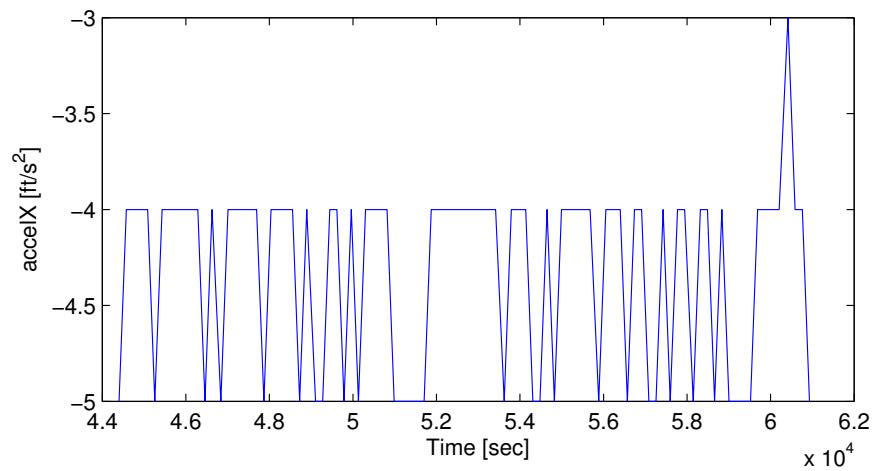
**Figure E.21: deltaT vs. Time**



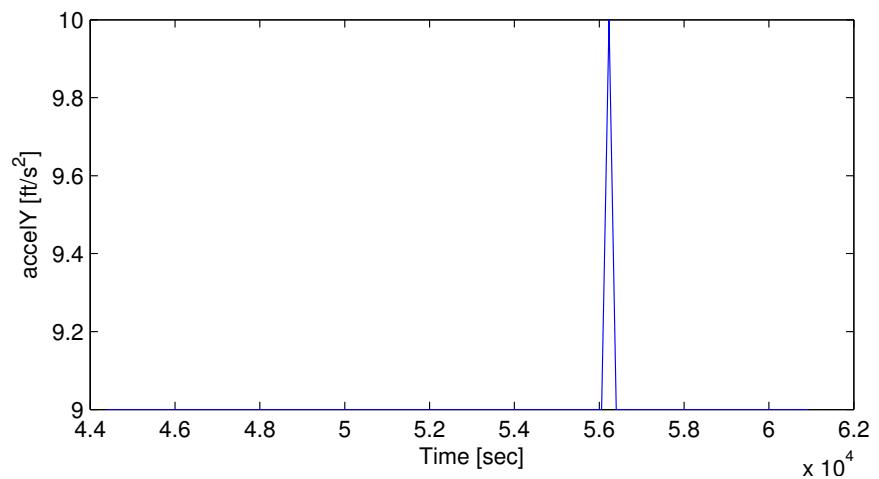
**Figure E.22: rpmPwm vs. Time**



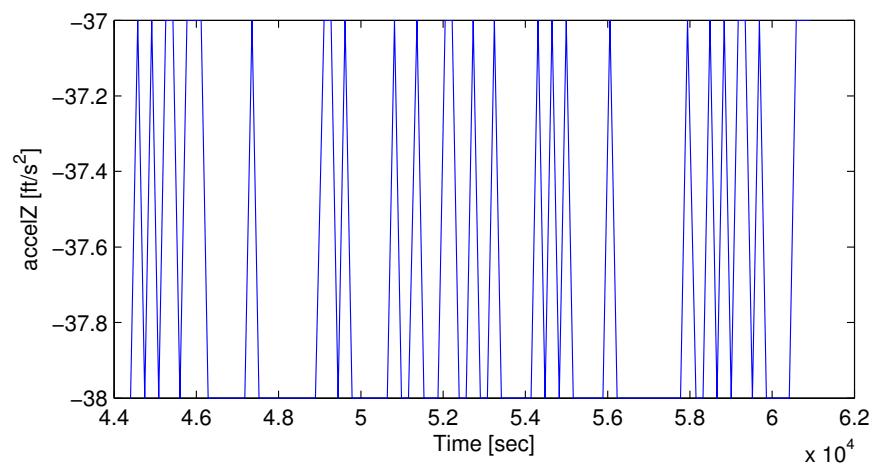
**Figure E.23: accelX vs. Time**



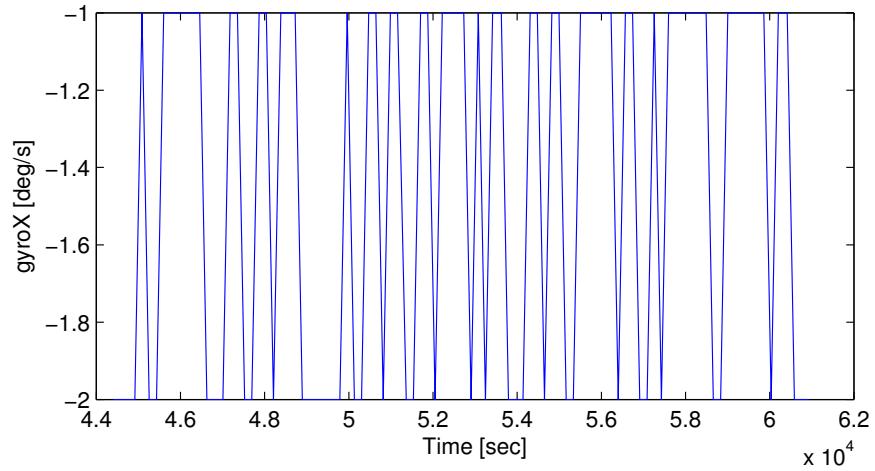
**Figure E.24: accelY vs. Time**



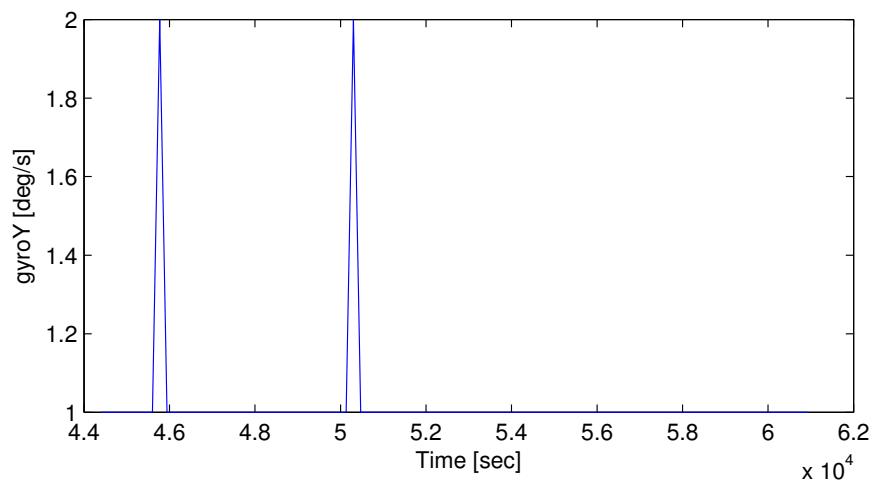
**Figure E.25: accelZ vs. Time**



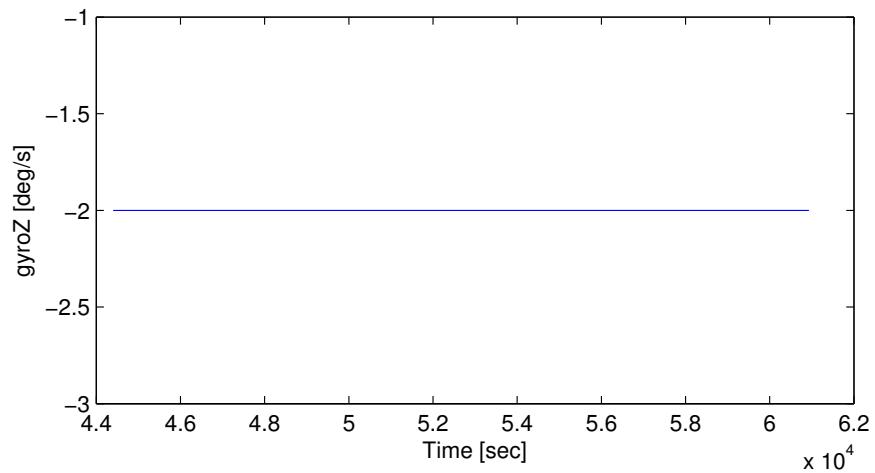
**Figure E.26:** gyroX vs. Time



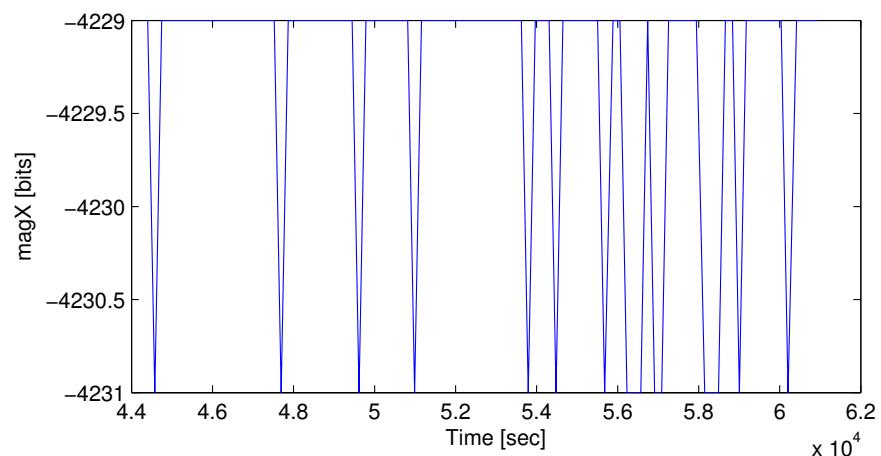
**Figure E.27:** gyroY vs. Time



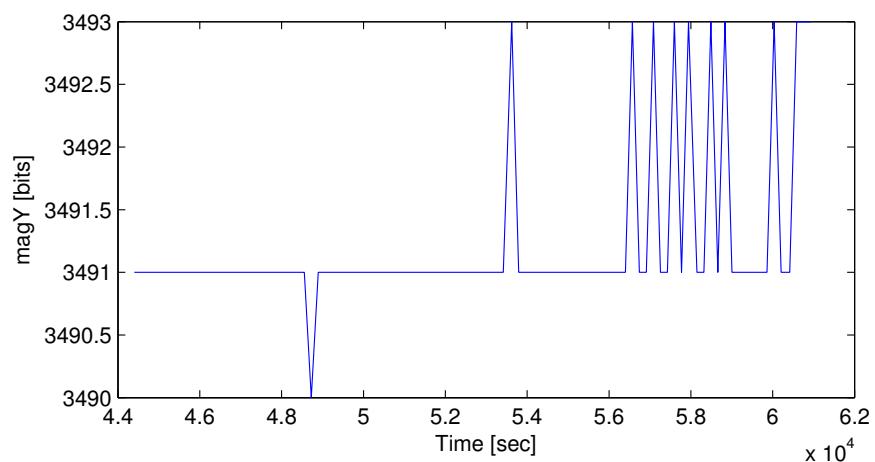
**Figure E.28:** gyroZ vs. Time



**Figure E.29: magX vs. Time**

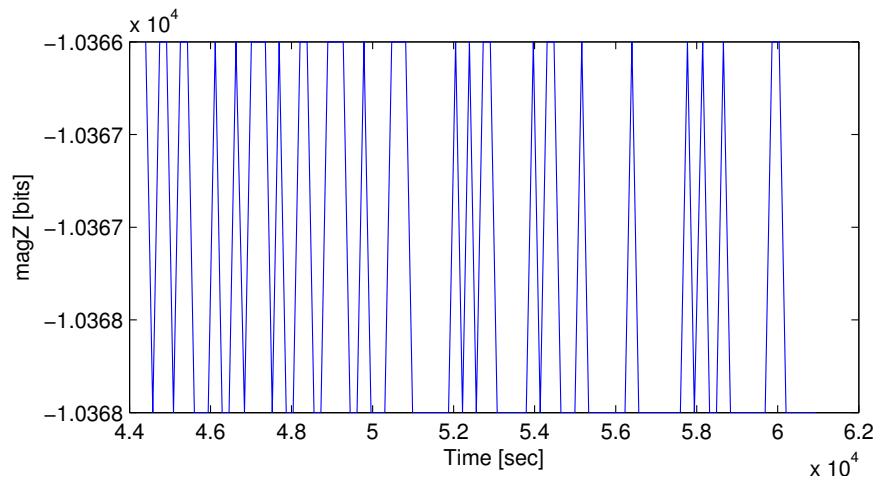


**Figure E.30: magY vs. Time**

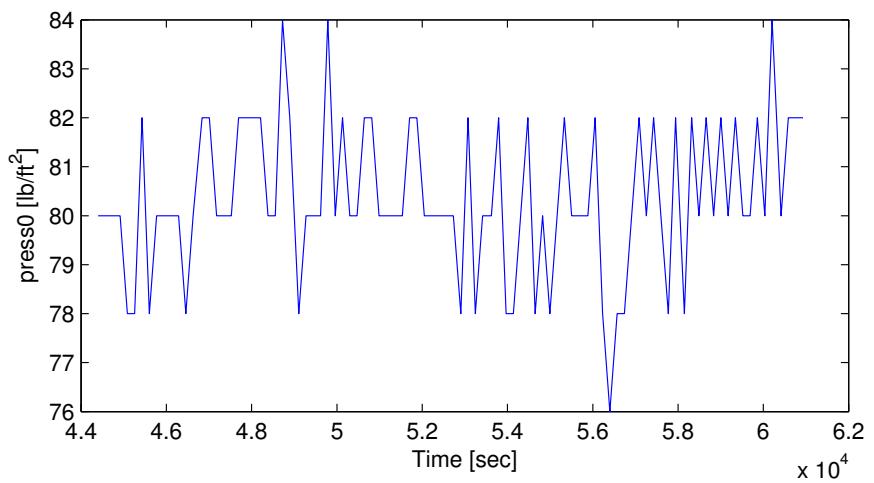


### E.3 Sample System Ouput - State Data

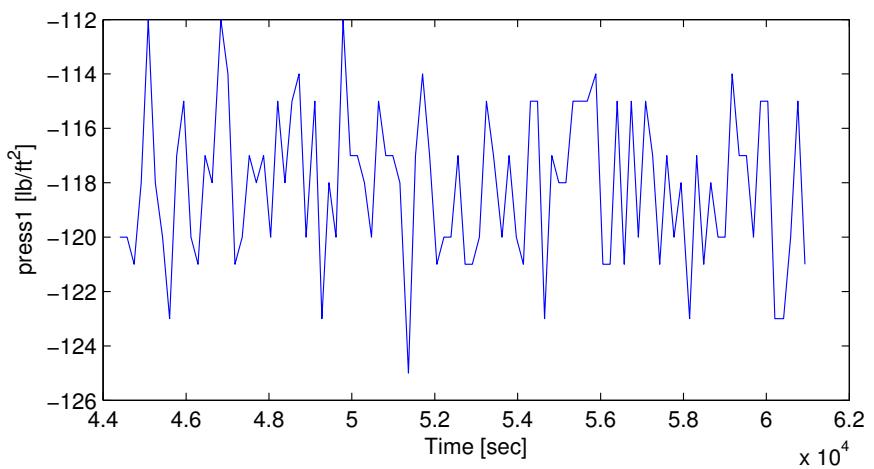
**Figure E.31: magZ vs. Time**



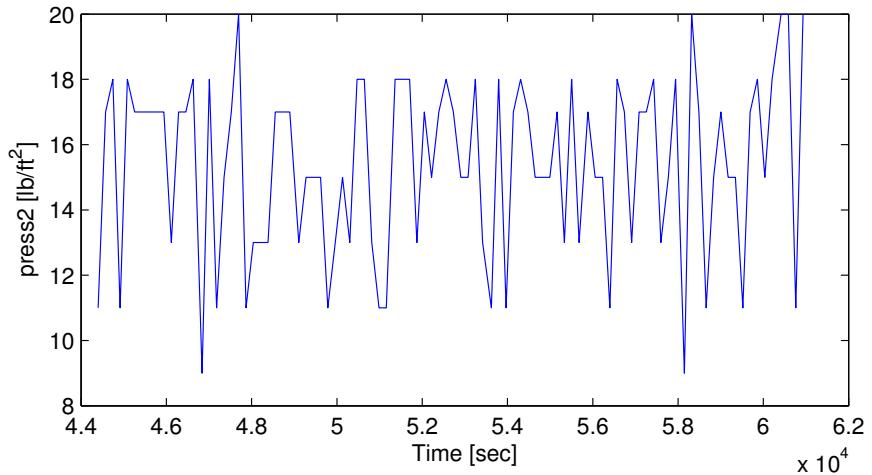
**Figure E.32: press0 vs. Time**



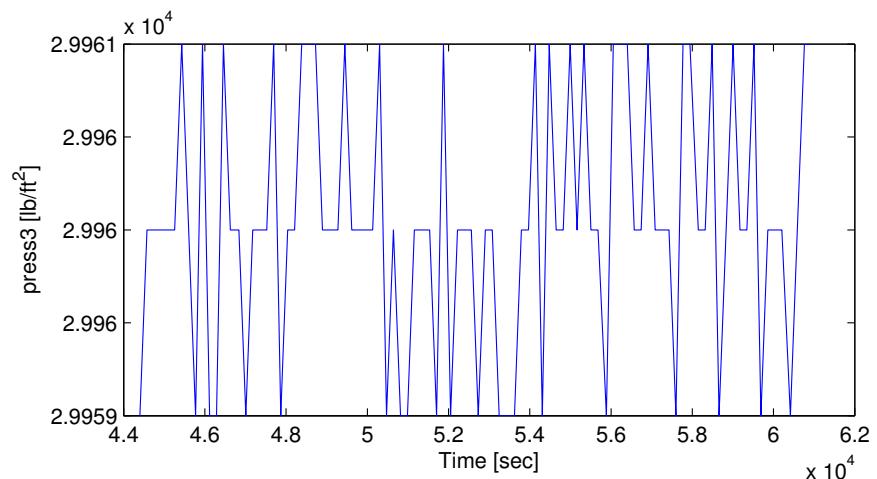
**Figure E.33: press1 vs. Time**



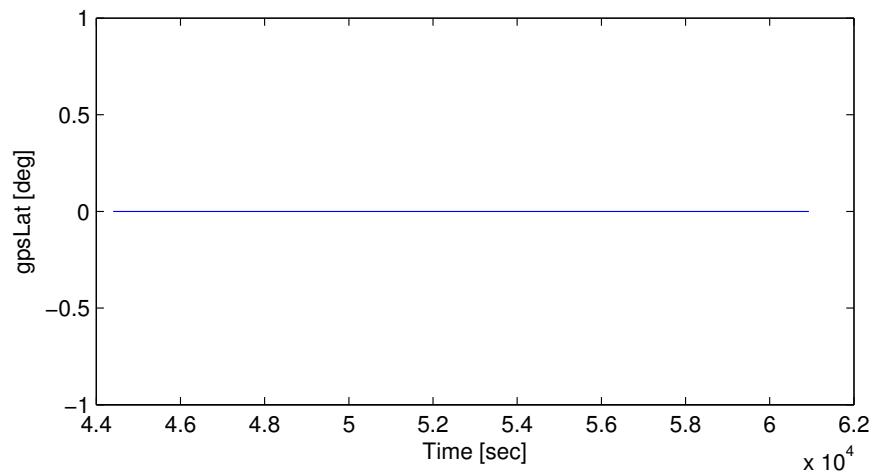
**Figure E.34: press2 vs. Time**



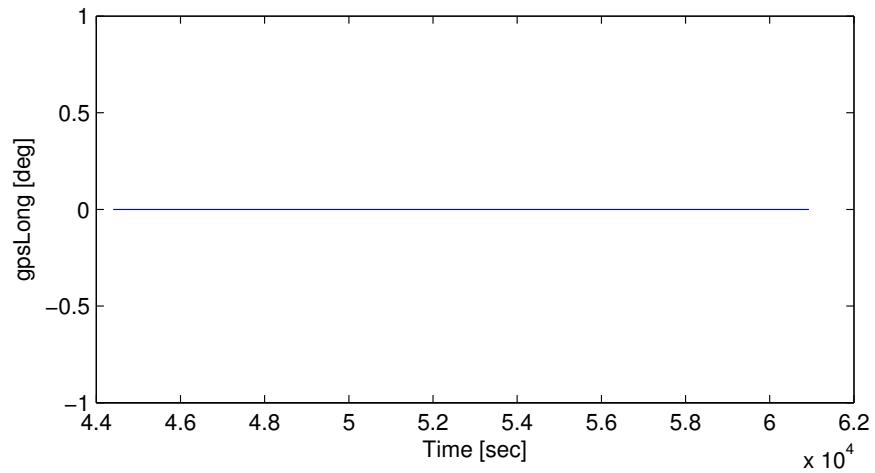
**Figure E.35: press3 vs. Time**



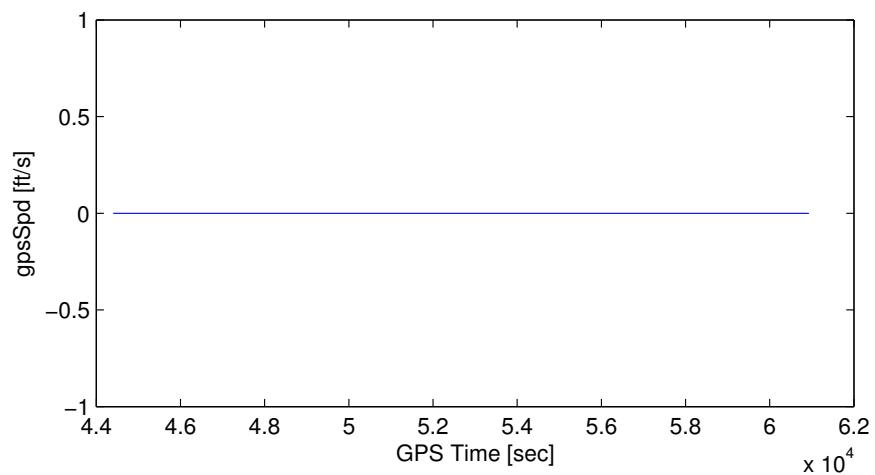
**Figure E.36: gpsLat vs. Time**



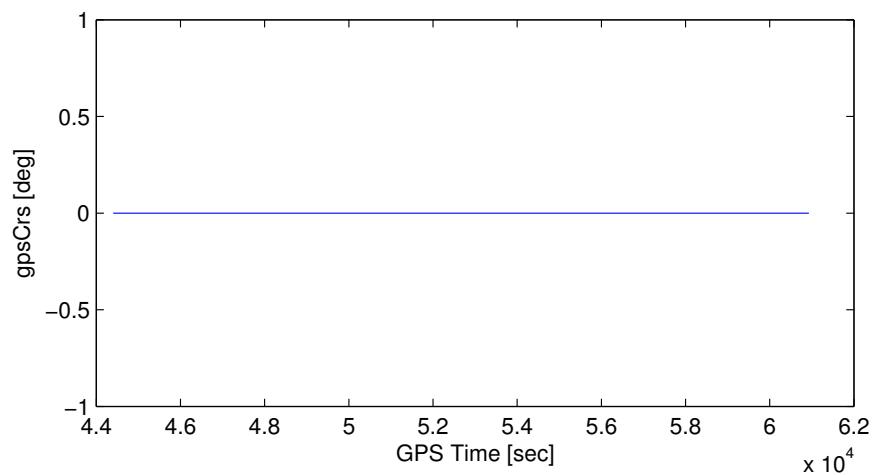
**Figure E.37: gpsLong vs. Time**



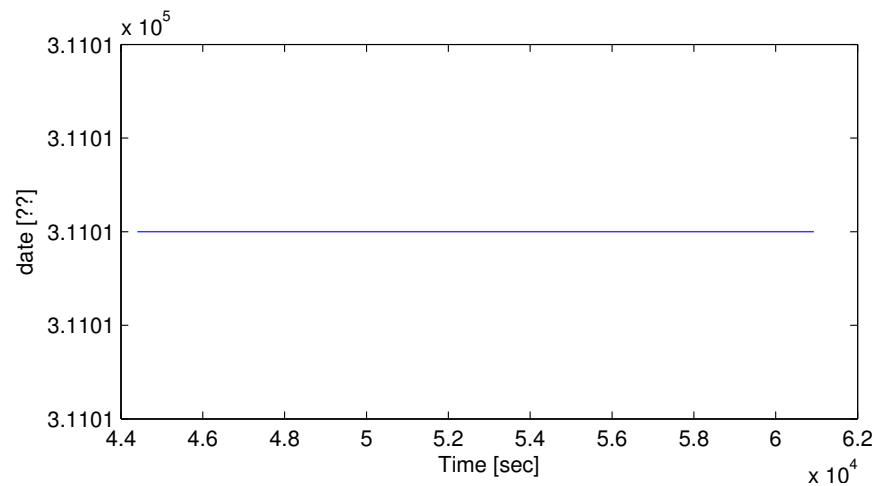
**Figure E.38: gpsSpd vs. Time**



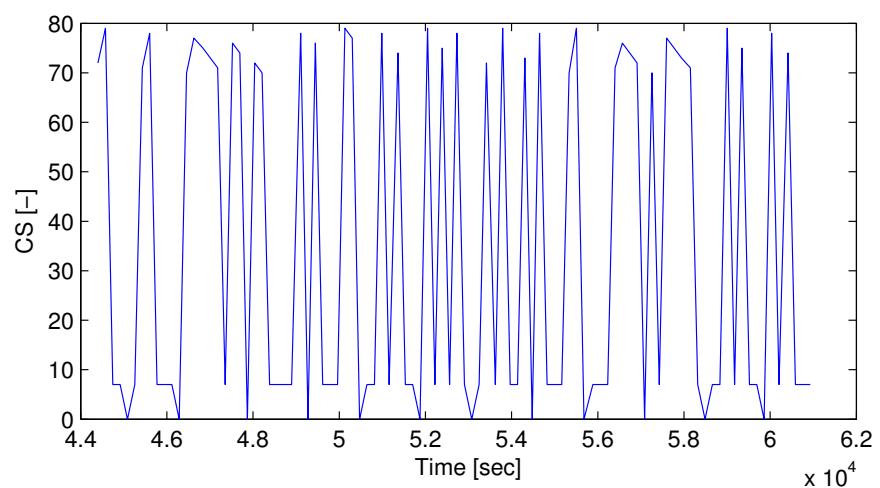
**Figure E.39: gpsCrs vs. Time**



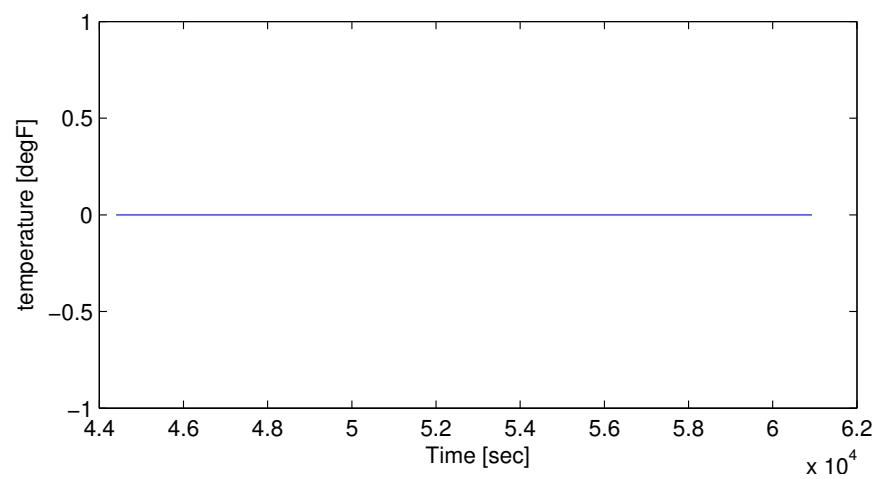
**Figure E.40: date vs. Time**



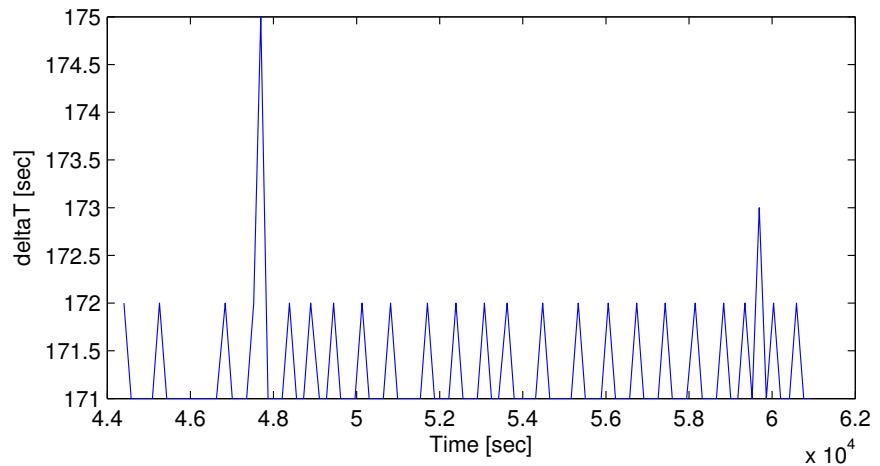
**Figure E.41: CS vs. Time**



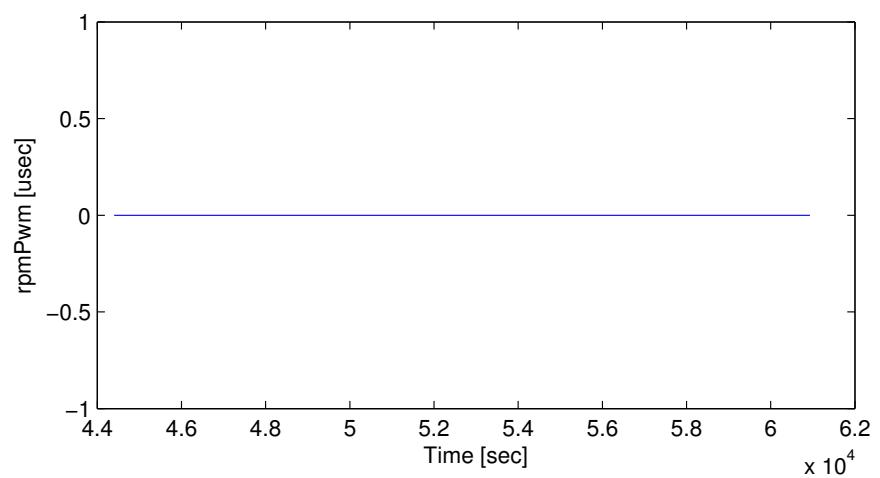
**Figure E.42: temperature vs. Time**



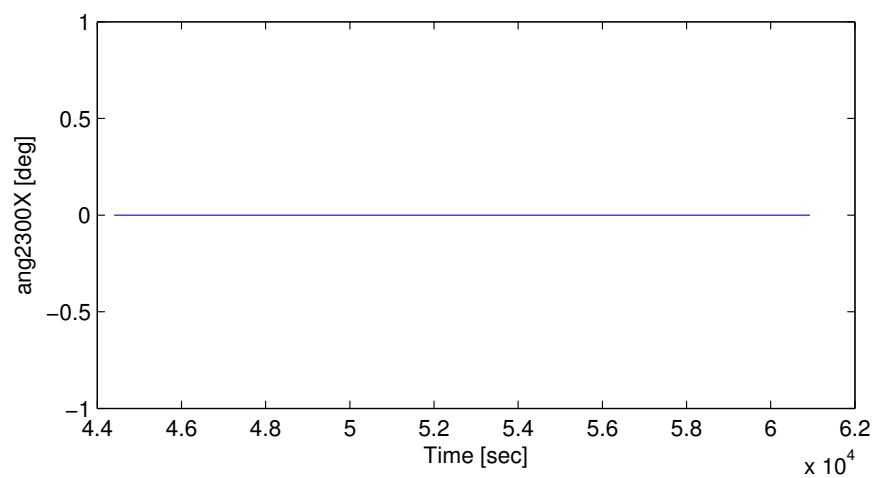
**Figure E.43: deltaT vs. Time**



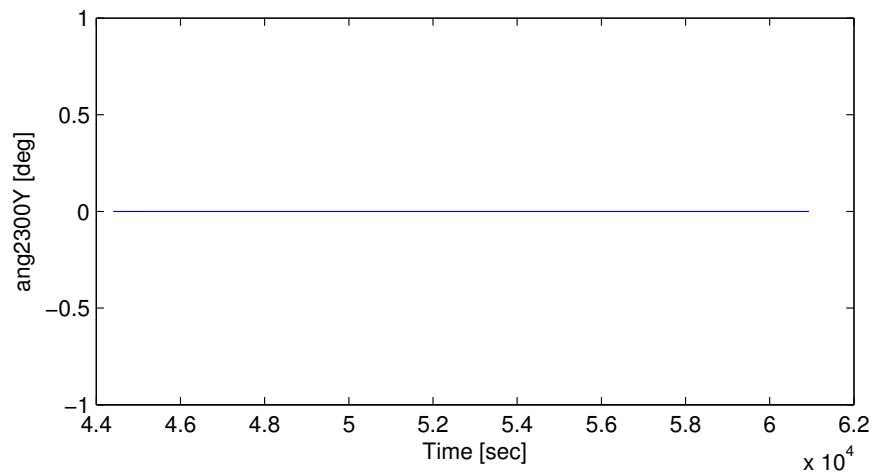
**Figure E.44: rpmPwm vs. Time**



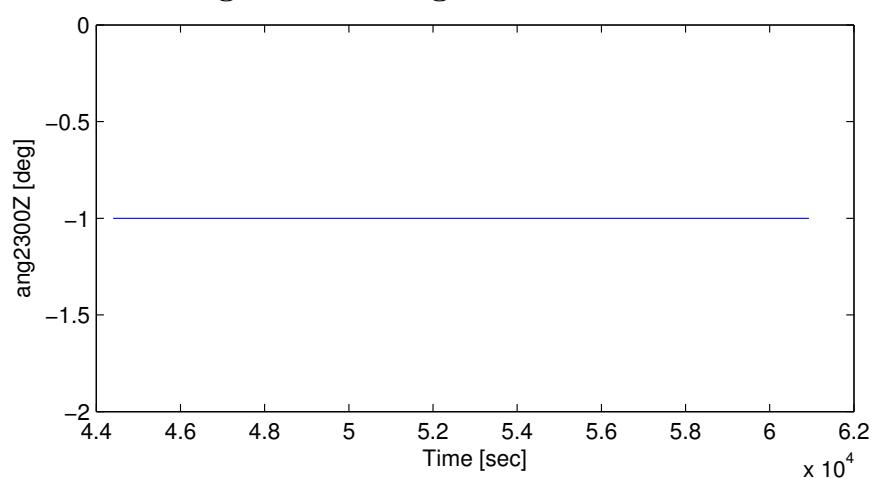
**Figure E.45: ang2300X vs. Time**



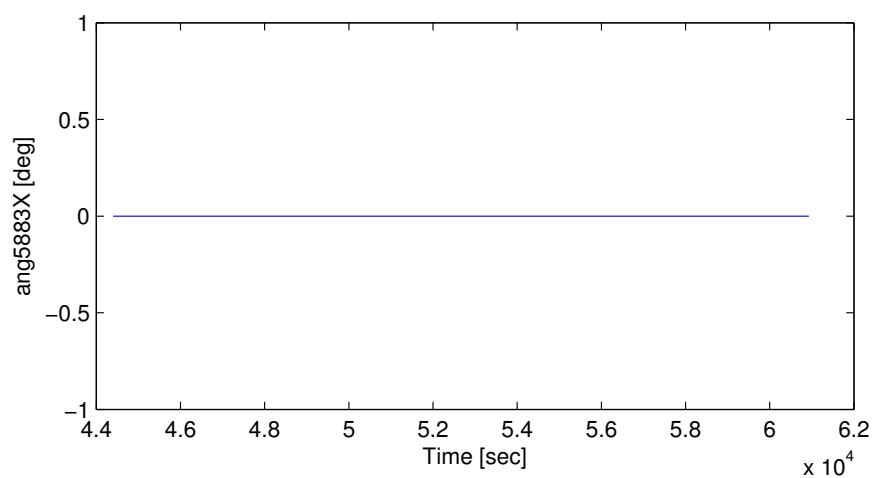
**Figure E.46: ang2300Y vs. Time**



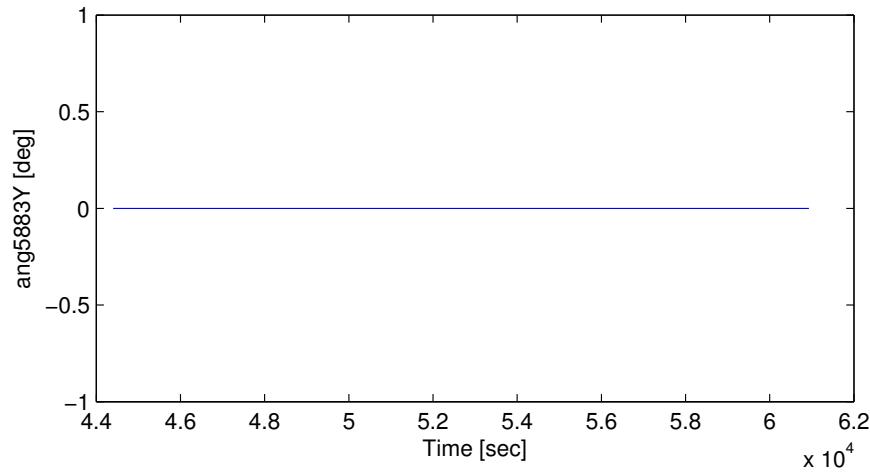
**Figure E.47: ang2300Z vs. Time**



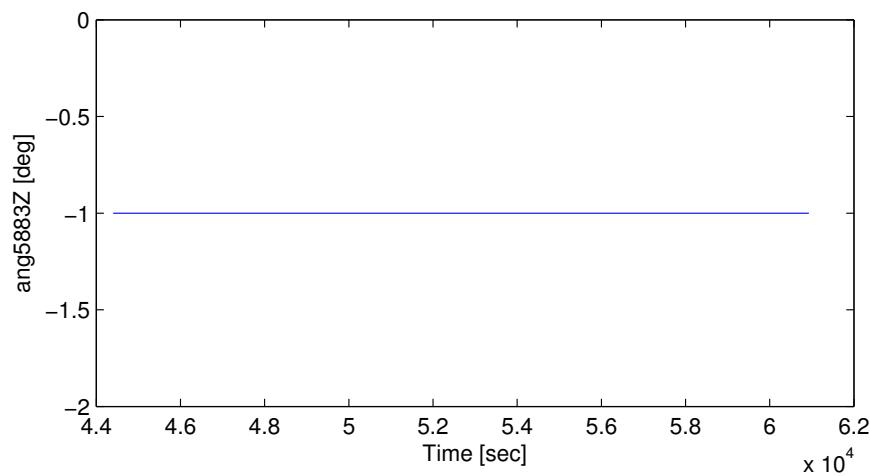
**Figure E.48: ang5883X vs. Time**



**Figure E.49: ang5883Y vs. Time**



**Figure E.50: ang5883Z vs. Time**



**Figure E.51: qbar vs. Time**

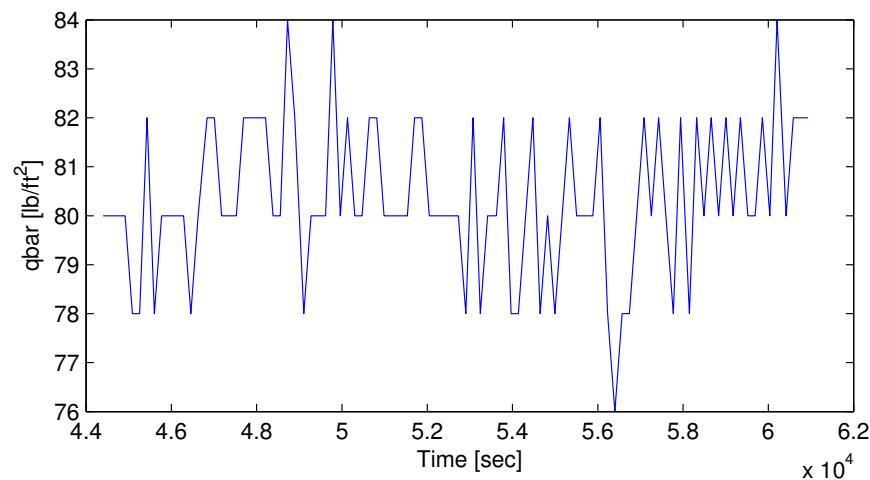
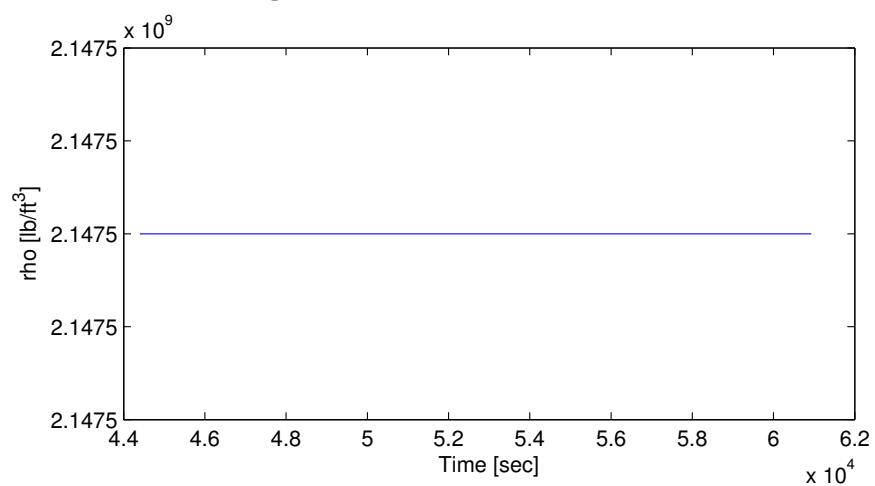
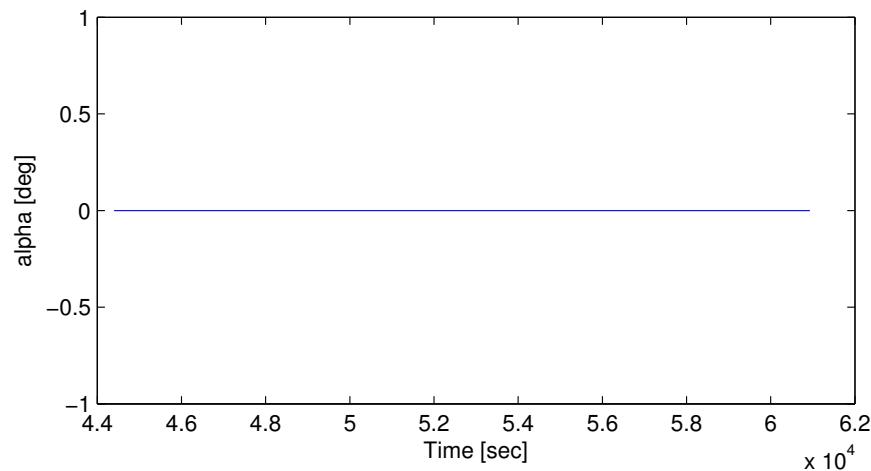


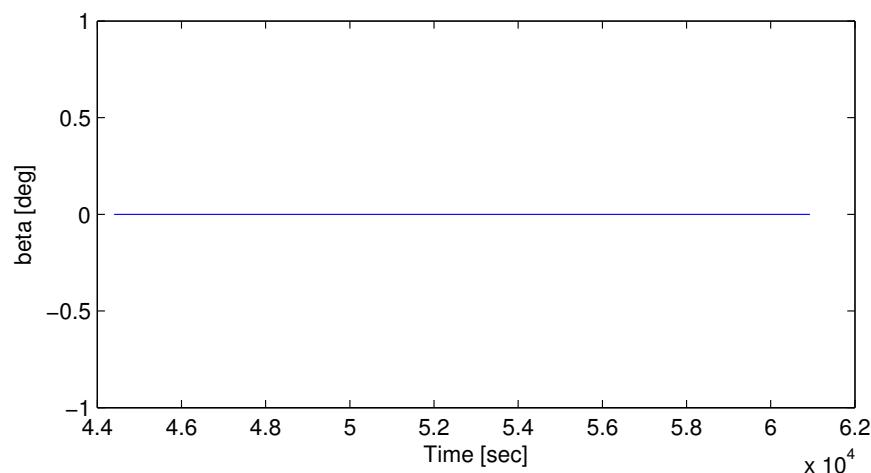
Figure E.52: rho vs. Time



**Figure E.53: alpha vs. Time**

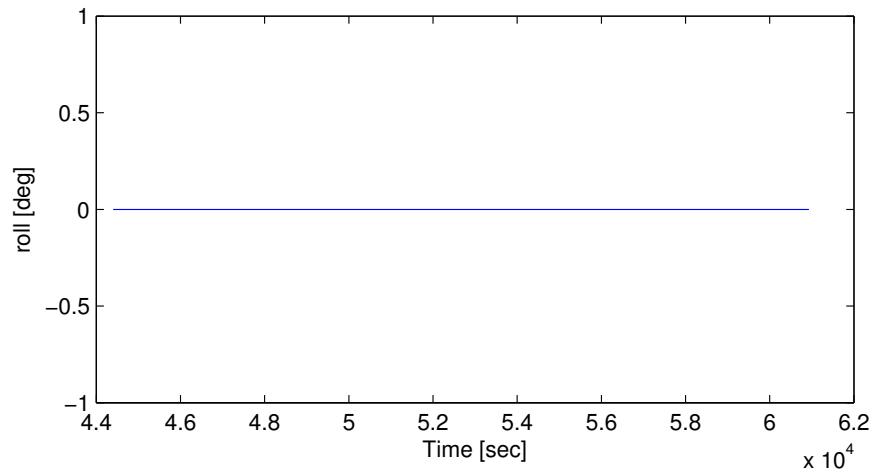


**Figure E.54: beta vs. Time**

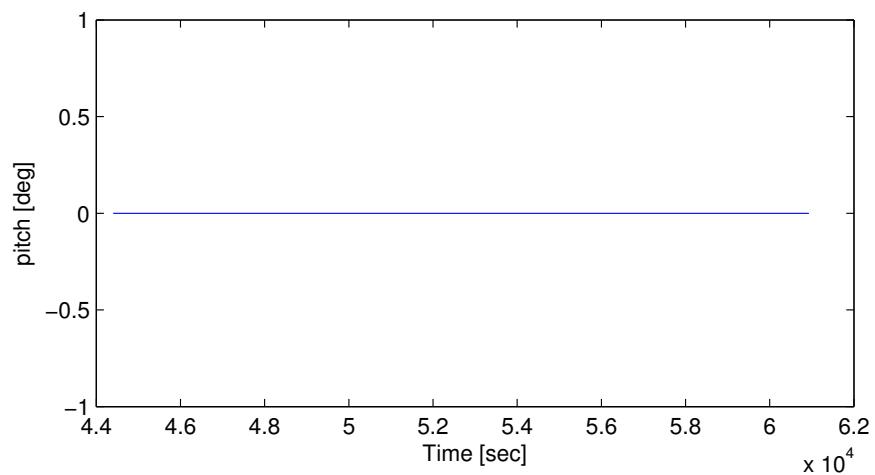


#### E.4 Sample System Ouput - Filtered Data

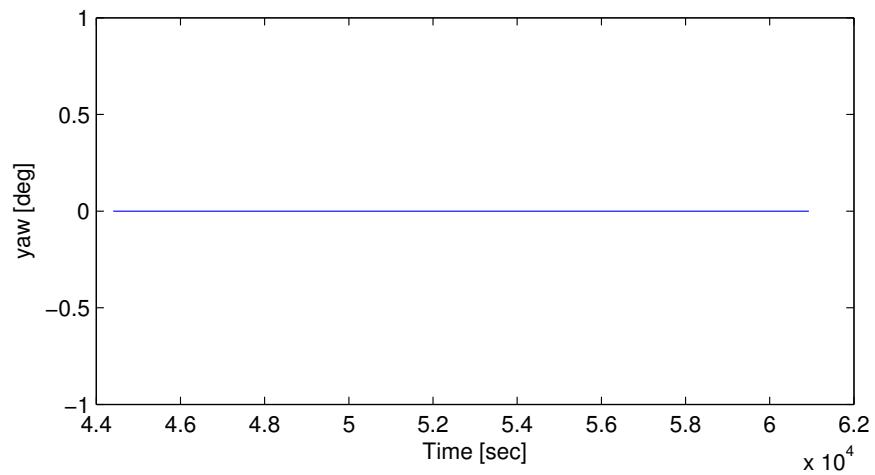
**Figure E.55: roll vs. Time**



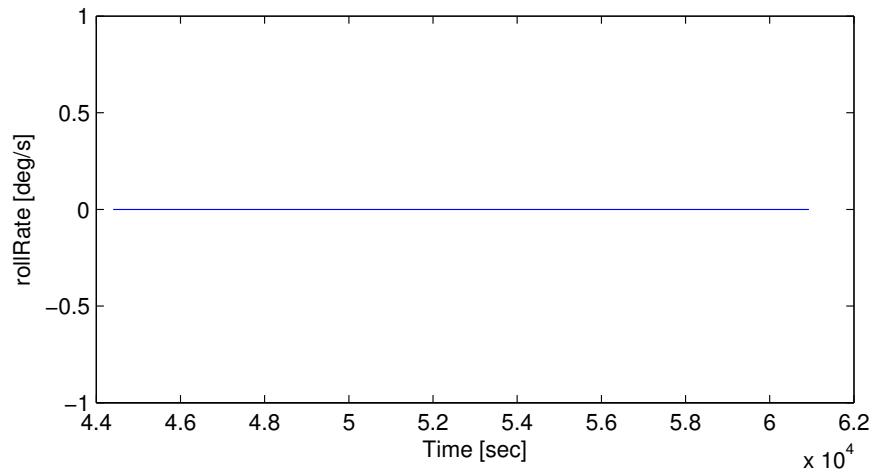
**Figure E.56: pitch vs. Time**



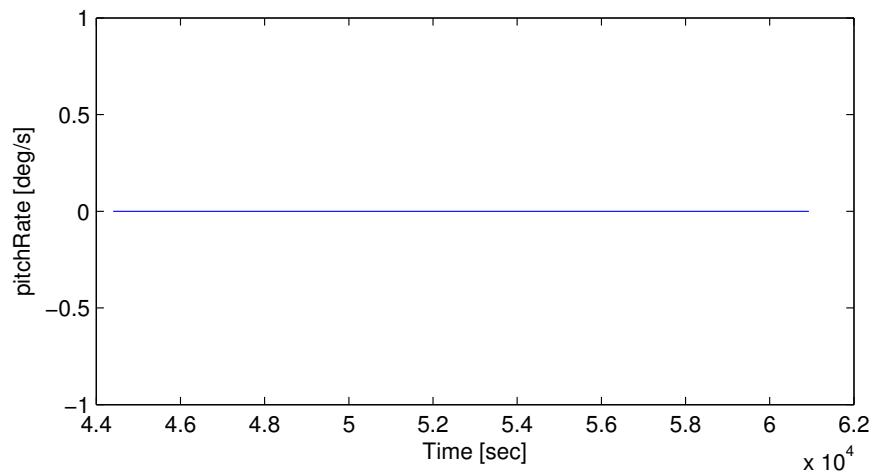
**Figure E.57: yaw vs. Time**



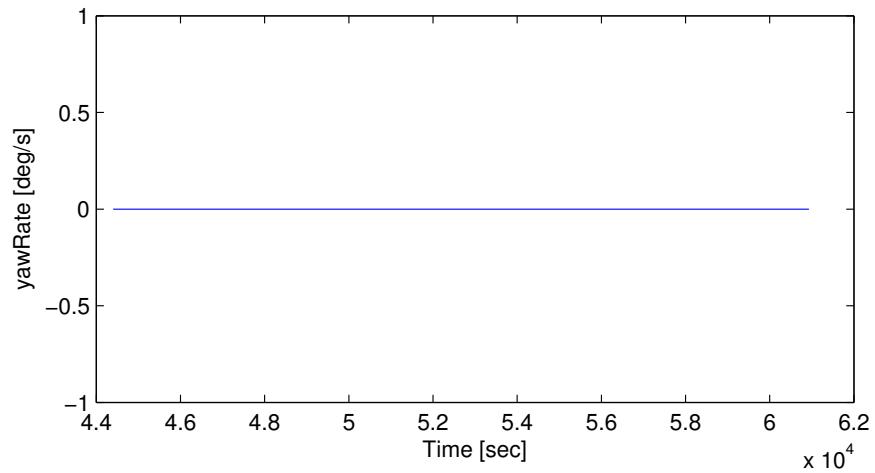
**Figure E.58: rollRate vs. Time**



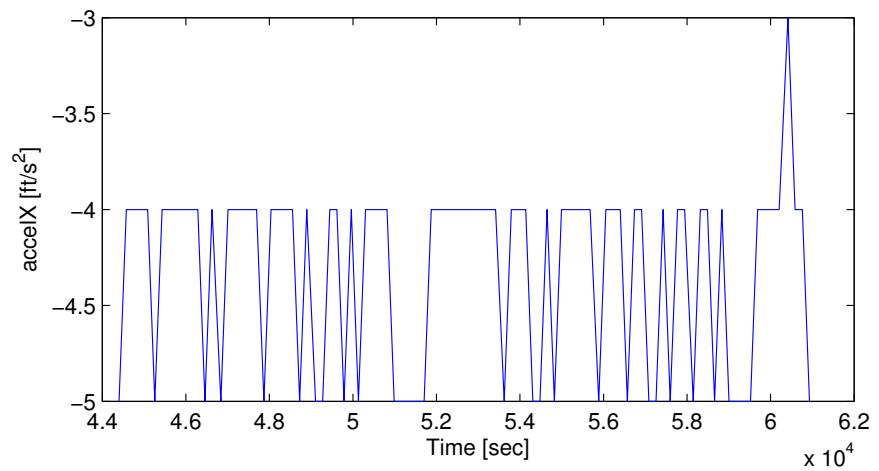
**Figure E.59: pitchRate vs. Time**



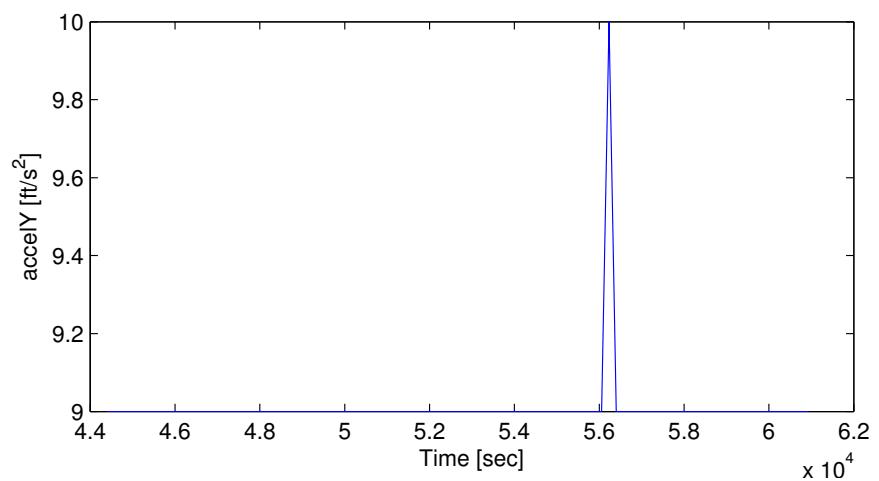
**Figure E.60: yawRate vs. Time**



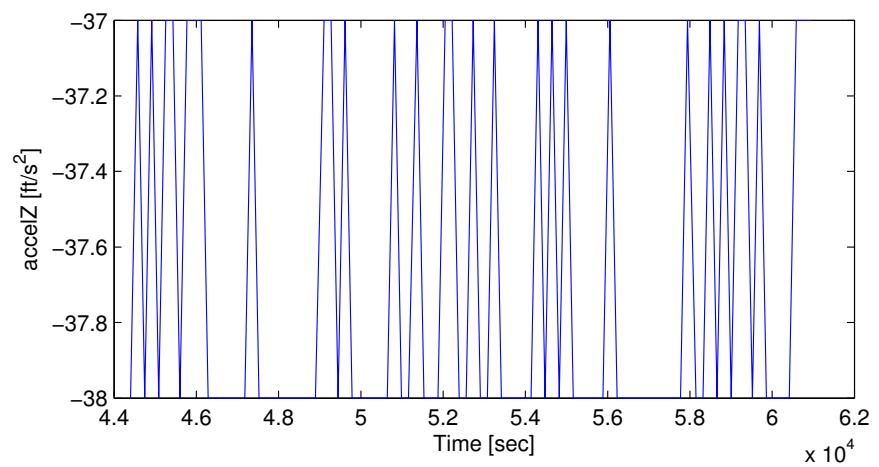
**Figure E.61: accelX vs. Time**



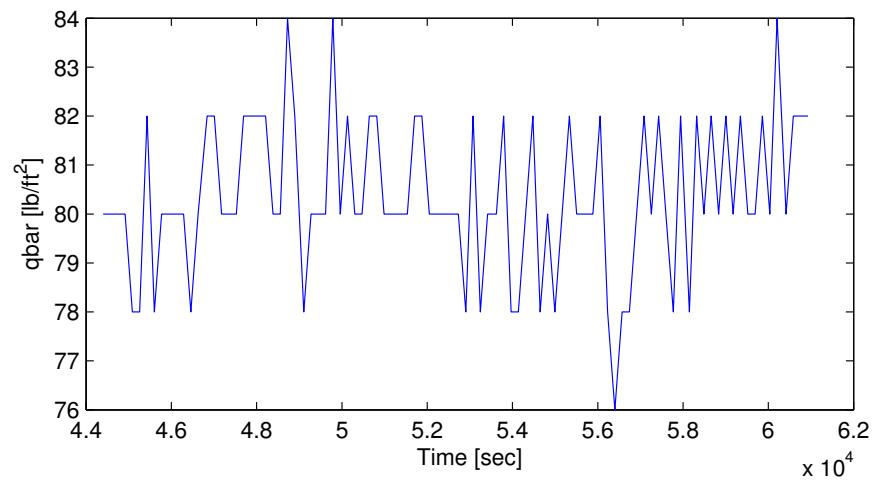
**Figure E.62: accelY vs. Time**



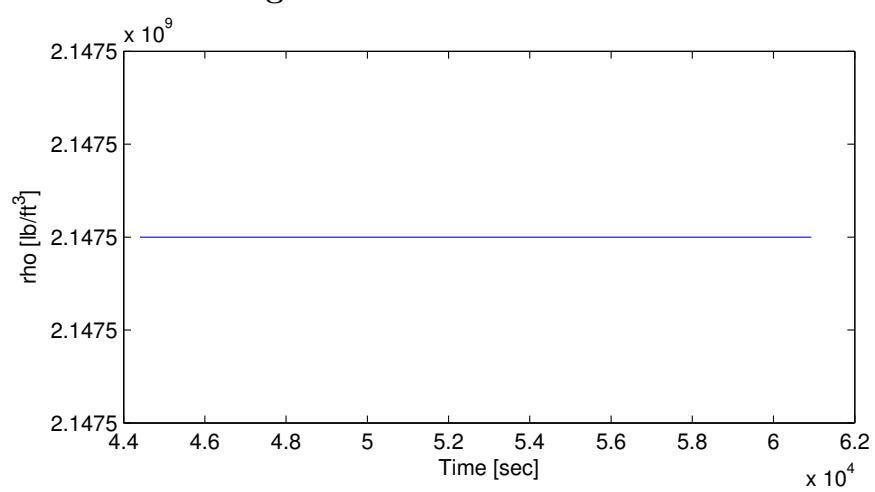
**Figure E.63: accelZ vs. Time**



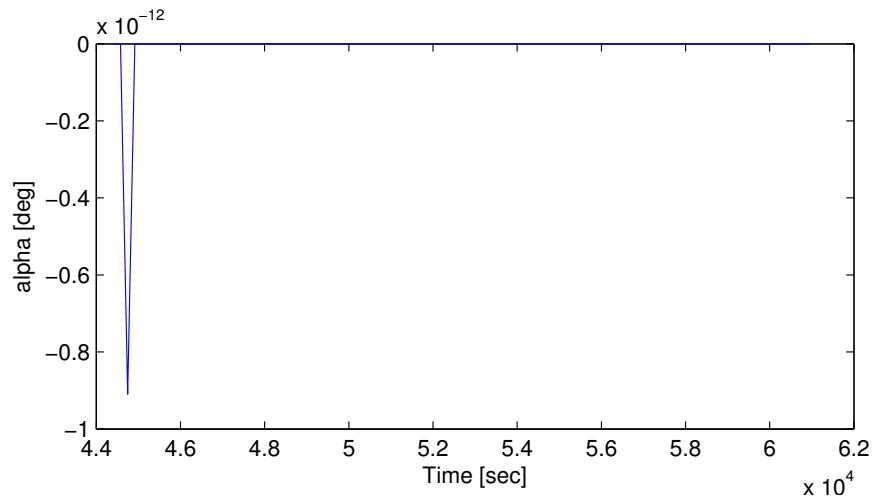
**Figure E.64: qbar vs. Time**



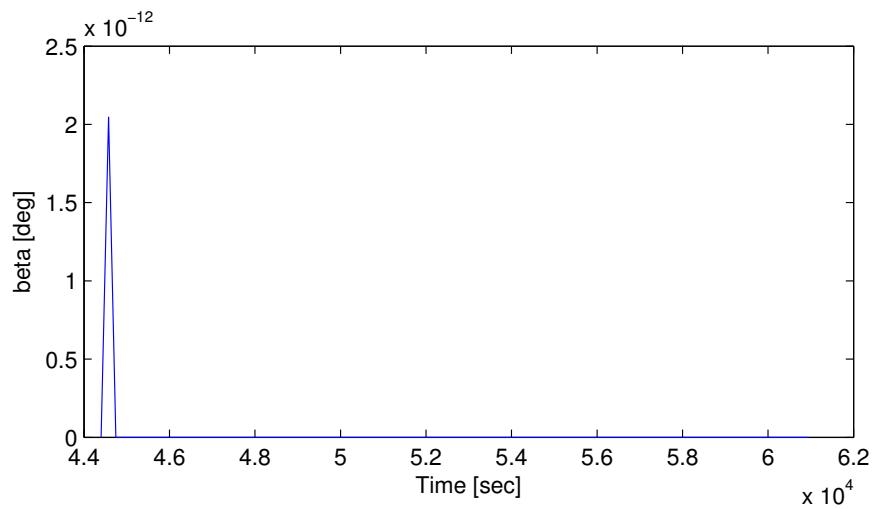
**Figure E.65: rho vs. Time**



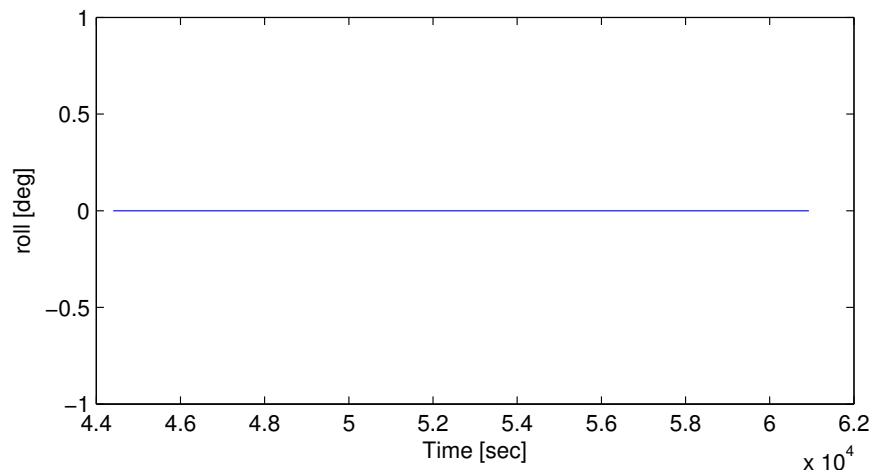
**Figure E.66: alpha vs. Time**



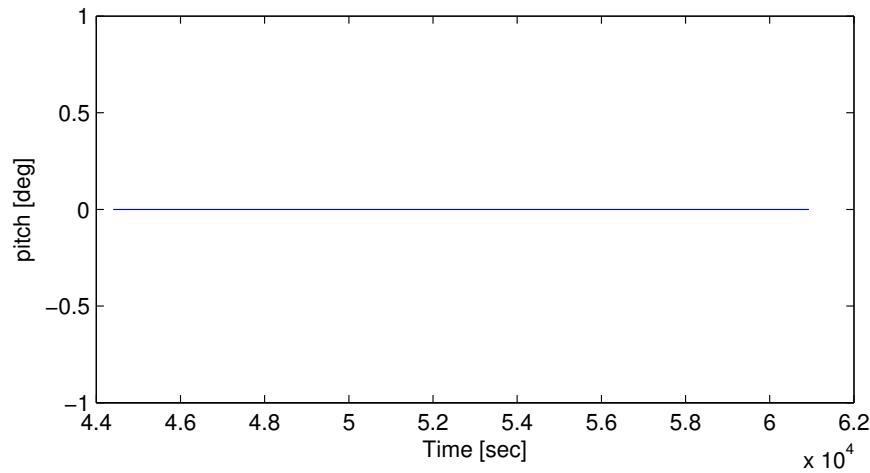
**Figure E.67: beta vs. Time**



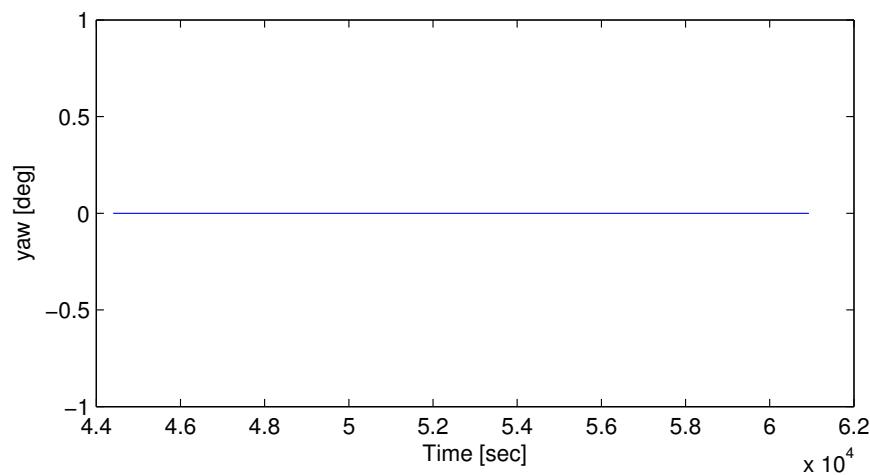
**Figure E.68: roll vs. Time**



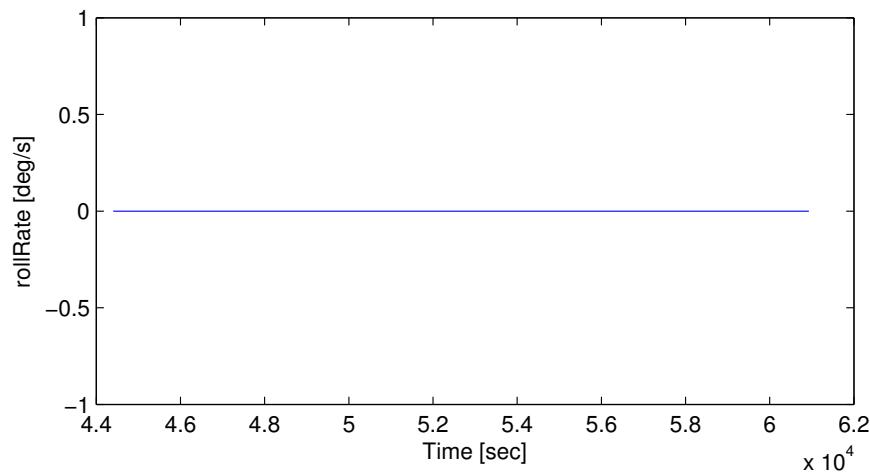
**Figure E.69: pitch vs. Time**



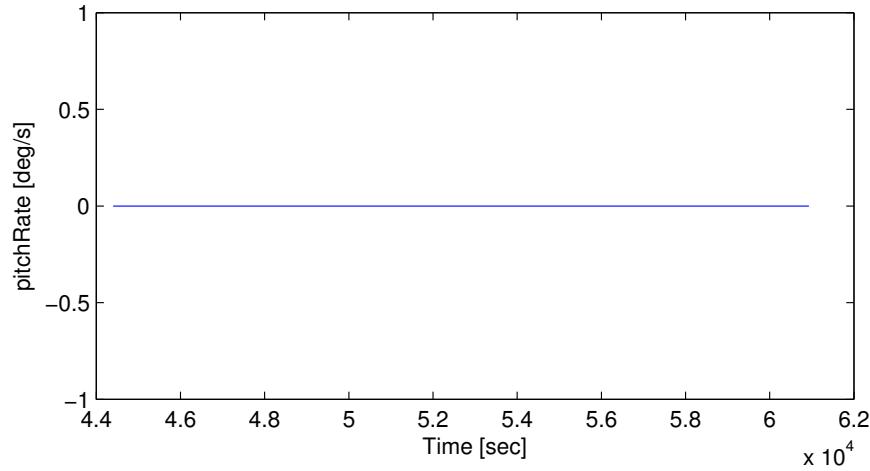
**Figure E.70: yaw vs. Time**



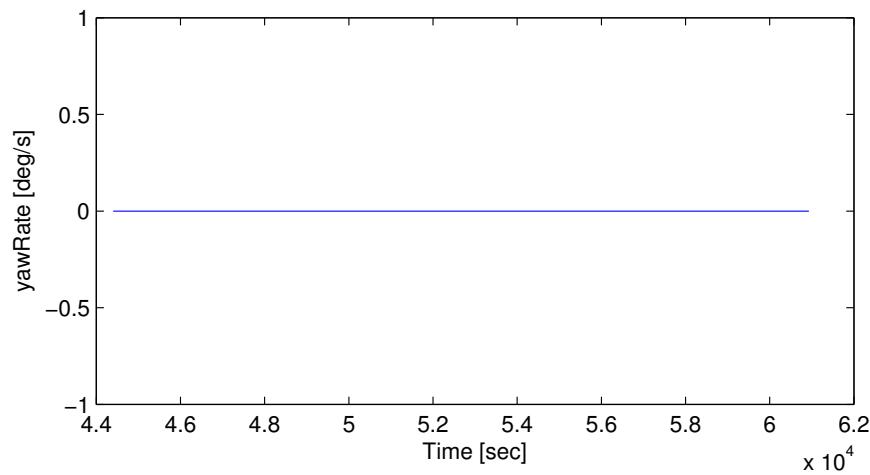
**Figure E.71: rollRate vs. Time**



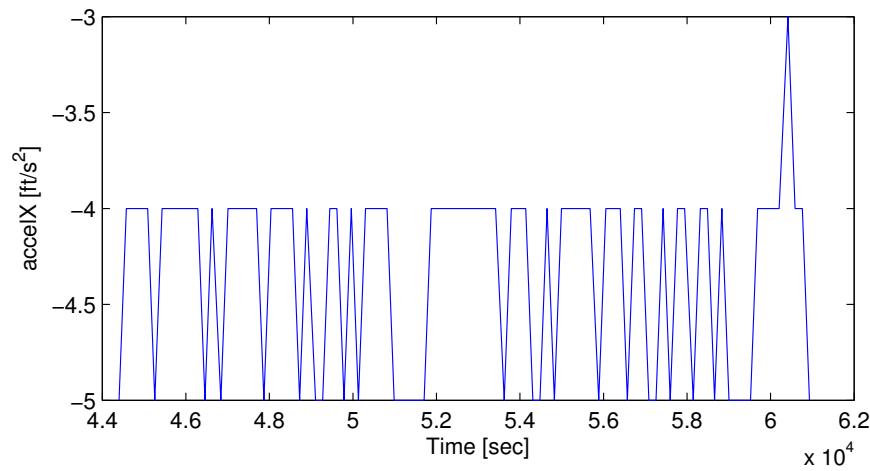
**Figure E.72: pitchRate vs. Time**



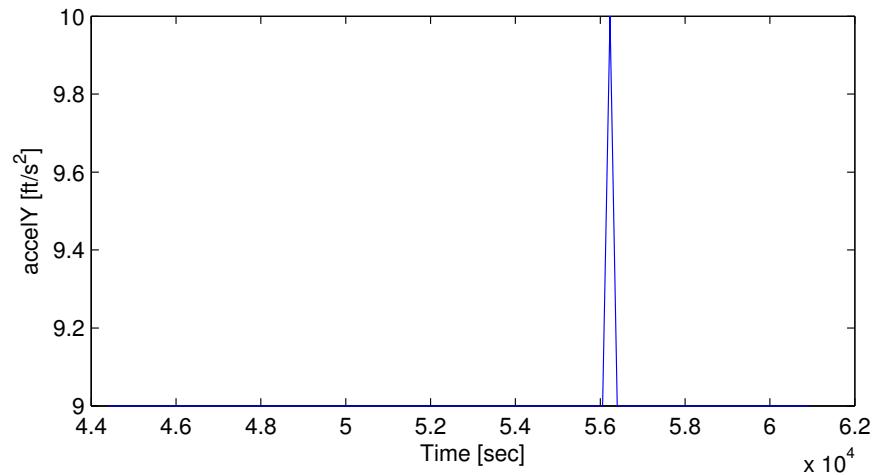
**Figure E.73: yawRate vs. Time**



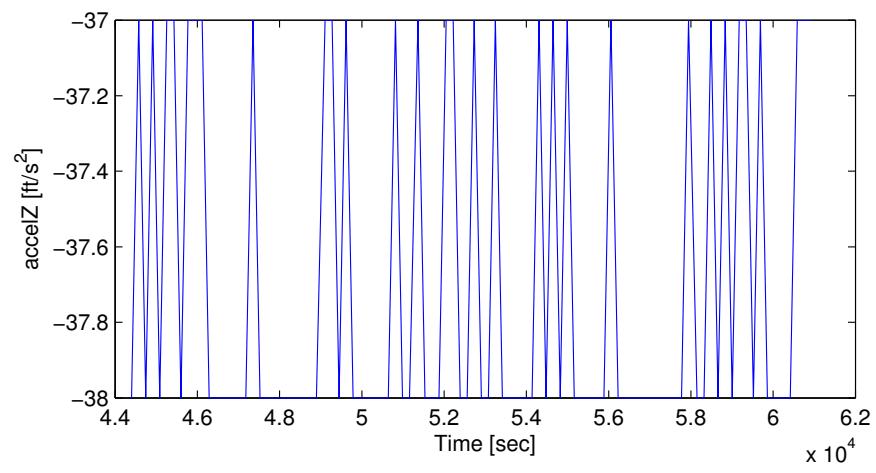
**Figure E.74: accelX vs. Time**



**Figure E.75: accelY vs. Time**

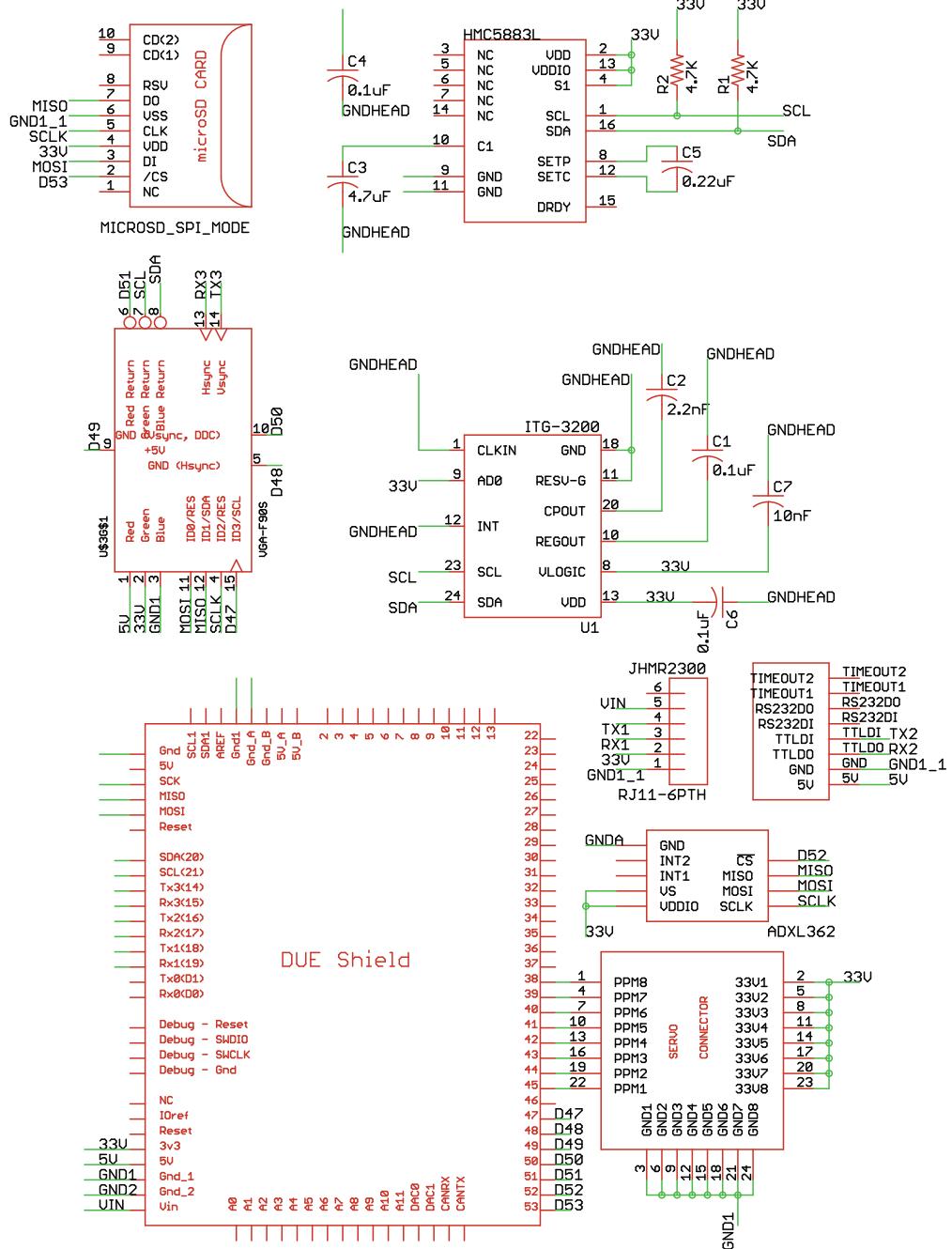


**Figure E.76: accelZ vs. Time**



## F.0 Wiring Schematics

Figure F.1: Arduino Due Flight Data Recorder Shield



**Figure F.2: Pressure Satellite Board Schematic**

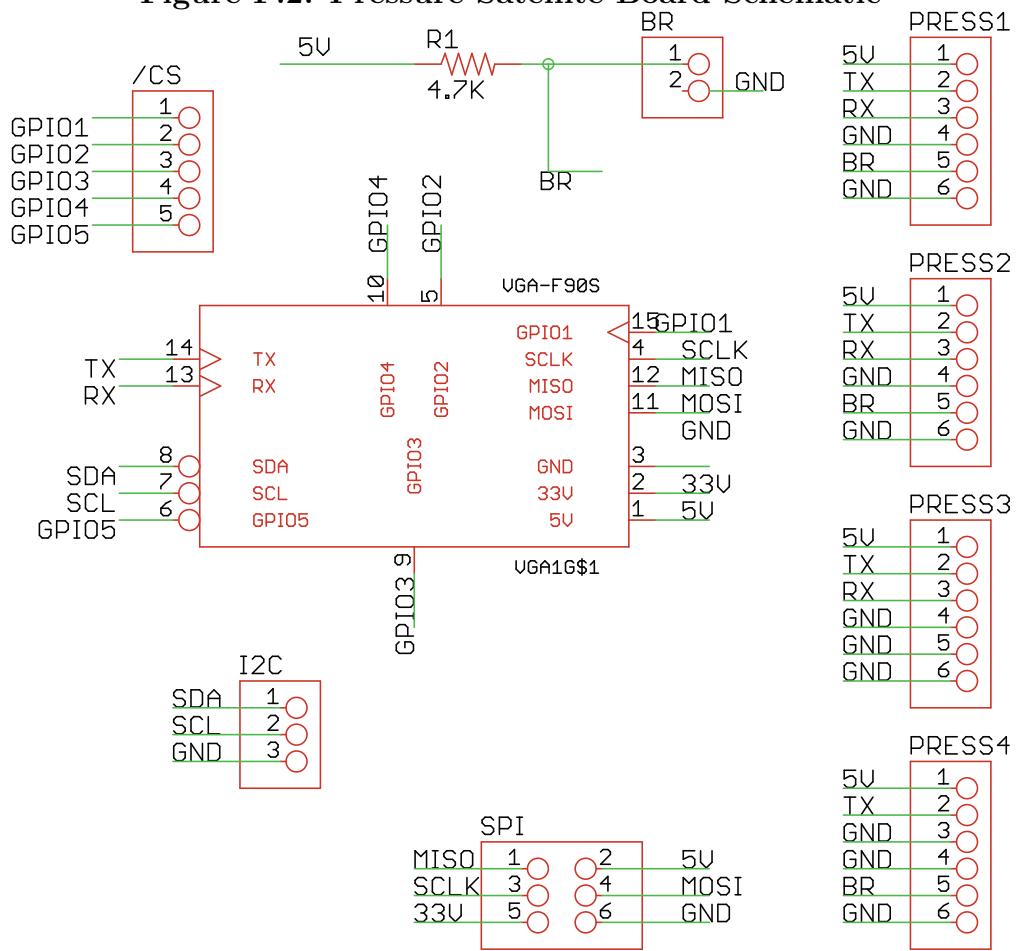
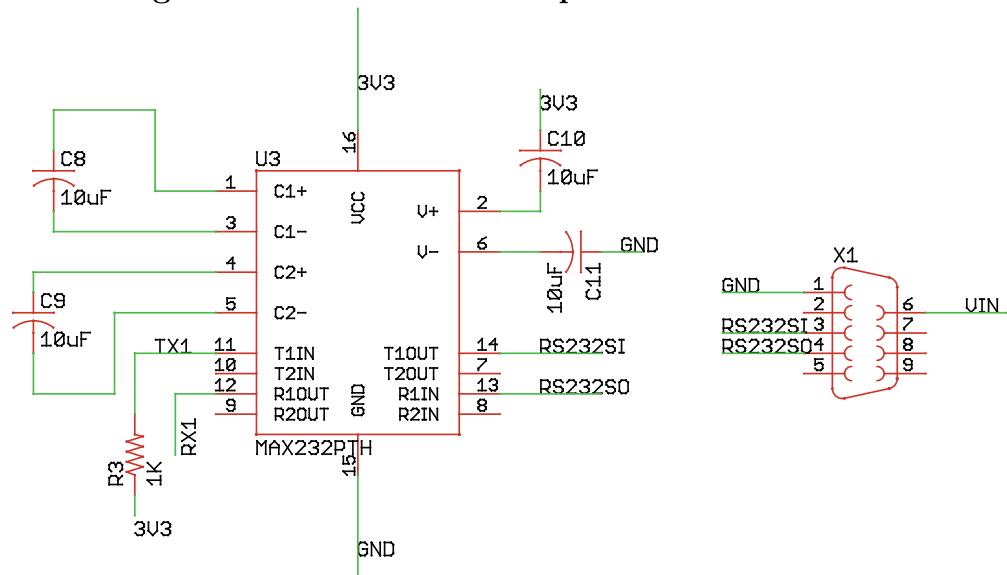


Figure F.3: HMR-2300 Adapter Board Schematic



## F.1 Future Work

The accuracy of the system developed still needs to be extensively validated. The immediate future work following this paper will be quantifying the accuracy of the system, as well as verifying reliability and safe integration into multiple UASs. Most of the accuracy estimation will be accomplished by measuring changes to a vehicle's drag polar. Parasite drag will be proven by adding a known quantity and measuring the change in the parasite drag coefficient of the test vehicle. To quantify the accuracy of drag-due-to-lift, wings with different aspect ratios will be used on the vehicle, which should combine into a single equivalent curve<sup>[12]</sup>. Following the accuracy estimation, a sensor fusion algorithm will be developed to combine inertial sensors with the air data system and other available sensors in a manner similar to other current research,<sup>[32],[33]</sup> in order to give full situational awareness to the UAS. This situational awareness could allow stability and control derivative estimation, which the aircraft designer could use to develop and simulate new control laws using actual stability derivatives.

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