# Logistic regression

## Logistic regression

- When response variable is measured/counted, regression can work well.
- But what if response is yes/no, lived/died, success/failure?
- Model probability of success.
- Probability must be between 0 and 1; need method that ensures this.
- Logistic regression does this. In R, is a generalized linear model with binomial "family":

```
glm(y ~ x, family="binomial")
```

Begin with simplest case.

## **Packages**

```
library(MASS)
library(tidyverse)
library(marginaleffects)
library(broom)
library(nnet)
library(conflicted)
conflict prefer("select", "dplyr")
conflict prefer("filter", "dplyr")
conflict prefer("rename", "dplyr")
conflict_prefer("summarize", "dplyr")
```

## The rats, part 1

• Rats given dose of some poison; either live or die:

dose status

- 0 lived
- 1 died
- 2 lived
- 3 lived
- 4 died
- 5 died

### Read in:

```
my_url <- "http://ritsokiguess.site/datafiles/rat.txt"
rats <- read_delim(my_url, " ")
rats</pre>
```

dose	status
0	lived
1	died
2	lived
3	lived
4	died
5	died

## Basic logistic regression

• Make response into a factor first:

```
rats2 <- rats %>% mutate(status = factor(status))
```

• then fit model:

```
status.1 <- glm(status ~ dose, family = "binomial", data = rats2)
```

## Output

```
summary(status.1)
##
## Call:
## glm(formula = status ~ dose, family = "binomial", data = rats2)
##
## Deviance Residuals:
##
## 0.5835 -1.6254 1.0381 1.3234 -0.7880 -0.5835
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 1.6841 1.7979 0.937 0.349
## dose -0.6736 0.6140 -1.097 0.273
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 8.3178 on 5 degrees of freedom
## Residual deviance: 6.7728 on 4 degrees of freedom
## AIC: 10.773
##
## Number of Fisher Scoring iterations: 4
```

## Interpreting the output

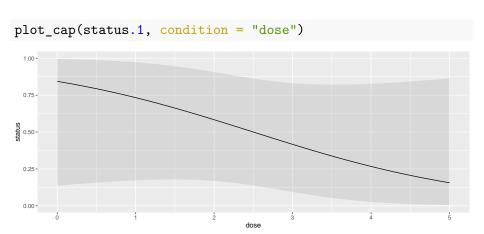
- ullet Like (multiple) regression, get tests of significance of individual x's
- Here not significant (only 6 observations).
- "Slope" for dose is negative, meaning that as dose increases, probability of event modelled (survival) decreases.

## Output part 2: predicted survival probs

```
cbind(predictions(status.1)) %>%
  select(dose, estimate)
```

dose	estimate
0	0.8434490
1	0.7331122
2	0.5834187
3	0.4165813
4	0.2668878
5	0.1565510

## On a graph



## The rats, more

- More realistic: more rats at each dose (say 10).
- Listing each rat on one line makes a big data file.
- Use format below: dose, number of survivals, number of deaths.

```
dose lived died
0 10 0
1 7 3
2 6 4
3 4 6
4 2 8
5 1 9
```

- 6 lines of data correspond to 60 actual rats.
- Saved in rat2.txt.

#### These data

rat2

## Rows: 6 Columns: 3

```
my_url <- "http://ritsokiguess.site/datafiles/rat2.txt"</pre>
rat2 <- read_delim(my_url, " ")</pre>
```

```
## Delimiter: " "
## dbl (3): dose, lived, died
```

##

## -- Column specification -----

## i Use `spec()` to retrieve the full column specification for this data. ## i Specify the column types or set `show\_col\_types = FALSE` to quiet this

lived died dose 10 0 0 6 4 6 8 5

## Create response matrix:

- Each row contains multiple observations.
- Create *two-column* response:
  - #survivals in first column,
  - #deaths in second.

```
response <- with(rat2, cbind(lived, died))
response</pre>
```

```
## lived died
## [1,] 10 0
## [2,] 7 3
## [3,] 6 4
## [4,] 4 6
## [5,] 2 8
## [6,] 1 9
```

Response is R matrix:

```
class(response)
```

```
## [1] "matrix" "array"
```

## Fit logistic regression

using response you just made:

```
rat2.1 <- glm(response ~ dose,
  family = "binomial",
  data = rat2
)</pre>
```

## Output

```
summary(rat2.1)
##
## Call:
## glm(formula = response ~ dose, family = "binomial", data = rat2)
##
## Deviance Residuals:
##
## 1.3421 -0.7916 -0.1034 0.1034 0.0389 0.1529
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 2.3619 0.6719 3.515 0.000439 ***
## dose -0.9448 0.2351 -4.018 5.87e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 27.530 on 5 degrees of freedom
##
## Residual deviance: 2.474 on 4 degrees of freedom
## AIC: 18.94
##
```

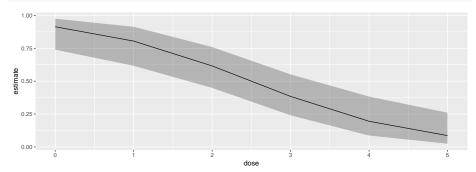
Logistic regression

## Predicted survival probs

```
new <- datagrid(model = rat2.1, dose = 0:5)
cbind(predictions(rat2.1, newdata = new))</pre>
```

rowid	estimate	p.value	conf.low	conf.high	dose
1	0.9138762	0.0004390	0.7398304	0.9753671	0
2	0.8048905	0.0031438	0.6169584	0.9135390	1
3	0.6159474	0.1721142	0.4487610	0.7595916	2
4	0.3840526	0.1721143	0.2404084	0.5512390	3
5	0.1951095	0.0031438	0.0864609	0.3830417	4
6	0.0861238	0.0004390	0.0246329	0.2601697	5

## On a picture



## Comments

- Significant effect of dose.
- Effect of larger dose is to decrease survival probability ("slope" negative; also see in decreasing predictions.)
- Confidence intervals around prediction narrower (more data).

# Multiple logistic regression

- With more than one x, works much like multiple regression.
- Example: study of patients with blood poisoning severe enough to warrant surgery. Relate survival to other potential risk factors.
- Variables, 1=present, 0=absent:
  - survival (death from sepsis=1), response
  - shock
  - malnutrition
  - alcoholism
  - age (as numerical variable)
  - bowel infarction
- See what relates to death.

#### Read in data

```
my url <-
  "http://ritsokiguess.site/datafiles/sepsis.txt"
sepsis <- read delim(my url, " ")
## Rows: 106 Columns: 6
## -- Column specification ---
## Delimiter: " "
## dbl (6): death, shock, malnut, alcohol, age, bowelinf
##
## i Use `spec()` to retrieve the full column specification for
## i Specify the column types or set `show col types = FALSE`
```

## Make sure categoricals really are

```
sepsis %>%
  mutate(across(-age, \(x) factor(x))) -> sepsis
```

# The data (some)

### sepsis

death	shock	malnut	alcohol	age	bowelinf		
0	0	0	0	56	0		
0	0	0	0	80	0		
0	0	0	0	61	0		
0	0	0	0	26	0		
0	0	0	0	53	0		
1	0	1	0	87	0		
0	0	0	0	21	0		
1	0	0	1	69	0		
0	0	0	0	57	0		
0	0	1	0	76	0		
1	0	0	1	66	1		
0	0	0	0	48	0		
0	0	0	0	18	0		
	Logistic regression						

22 / 83

## Fit model

```
sepsis.1 <- glm(death ~ shock + malnut + alcohol + age +
  bowelinf,
family = "binomial",
data = sepsis
)</pre>
```

## Output part 1

#### tidy(sepsis.1)

term	estimate	std.error	statistic	p.value
(Intercept)	-9.7539056	2.5416952	-3.837559	0.0001243
shock1	3.6738658	1.1648114	3.154044	0.0016103
malnut1	1.2165811	0.7282236	1.670615	0.0947978
alcohol1	3.3548846	0.9821026	3.416022	0.0006354
age	0.0921527	0.0303237	3.038968	0.0023739
bowelinf1	2.7975864	1.1639717	2.403483	0.0162397

- All P-values fairly small
- but malnut not significant: remove.

## Removing malnut

```
sepsis.2 <- update(sepsis.1, . ~ . - malnut)
tidy(sepsis.2)</pre>
```

term	estimate	std.error	statistic	p.value
(Intercept)	-8.8945899	2.3168948	-3.839013	0.0001235
shock1	3.7011932	1.1035347	3.353944	0.0007967
alcohol1	3.1859040	0.9172457	3.473338	0.0005140
age	0.0898318	0.0292153	3.074821	0.0021063
bowelinf1	2.3864685	1.0722662	2.225631	0.0260389

• Everything significant now.

## Comments

- Most of the original x's helped predict death. Only malnut seemed not to add anything.
- Removed malnut and tried again.
- Everything remaining is significant (though bowelinf actually became less significant).
- All coefficients are positive, so having any of the risk factors (or being older) increases risk of death.

### Predictions from model without "malnut"

### • A few (rows of original dataframe) chosen "at random":

```
sepsis %>% slice(c(4, 1, 2, 11, 32)) -> new new
```

death	shock	malnut	alcohol	age	bowelinf
0	0	0	0	26	0
0	0	0	0	56	0
0	0	0	0	80	0
1	0	0	1	66	1
1	0	0	1	49	0

```
cbind(predictions(sepsis.2, newdata = new)) %>%
  select(estimate, conf.low, conf.high, shock:bowelinf)
```

estimate	conf.low	conf.high	shock	malnut	alcohol	age	bowelinf
0.0014153	0.0000627	0.0310305	0	0	0	26	0
0.0205524	0.0041025	0.0965660	0	0	0	56	0
0.1534168	0.0560684	0.3560344	0	0	0	80	0
0.9312901	0.5490986	0.9934148	0	0	1	66	1
0.2130010	0.0763906	0.4696795	0	0	1	49	0

## Comments

- Survival chances pretty good if no risk factors, though decreasing with age.
- Having more than one risk factor reduces survival chances dramatically.
- Usually good job of predicting survival; sometimes death predicted to survive.

## Another way to assess effects

of age:

```
new <- datagrid(model = sepsis.2, age = seq(30, 70, 10))
new</pre>
```

death	shock	alcohol	bowelinf	age
0	0	0	0	30
0	0	0	0	40
0	0	0	0	50
0	0	0	0	60
0	0	0	0	70

## Assessing age effect

```
cbind(predictions(sepsis.2, newdata = new)) %>%
  select(estimate, shock:age)
```

estimate	shock	alcohol	bowelinf	age
0.0020261	0	0	0	30
0.0049603	0	0	0	40
0.0120925	0	0	0	50
0.0291792	0	0	0	60
0.0687298	0	0	0	70

# Assessing shock effect

```
new <- datagrid(shock = c(0, 1), model = sepsis.2)
new</pre>
```

death	alcohol	age	bowelinf	shock
0	0	51.28302	0	0
0	0	51.28302	0	1

```
cbind(predictions(sepsis.2, newdata = new)) %>%
  select(estimate, death:shock)
```

estimate	death	alcohol	age	bowelinf	shock
0.0135497	0	0	51.28302	0	0
0.3574261	0	0	51.28302	0	1

# Assessing proportionality of odds for age

- An assumption we made is that log-odds of survival depends linearly on age.
- Hard to get your head around, but basic idea is that survival chances go continuously up (or down) with age, instead of (for example) going up and then down.
- In this case, seems reasonable, but should check:

## Residuals vs. age

```
sepsis.2 %>% augment(sepsis) %>%
  ggplot(aes(x = age, y = .resid)) +
  geom_point()
 3 -
 2-
resid
  0 -
 -1-
            25
                                                      75
                                 50
```

### Comments

- No apparent problems overall.
- Confusing "line" across: no risk factors, survived.

## Probability and odds

• For probability p, odds is p/(1-p):

	<u> </u>		
Prob.	Odds	log-odds	in words
0.5	0.5/0.5 = 1/1 = 1.00	0.00	"even money"
0.1	0.1/0.9 = 1/9 = 0.11	-2.20	"9 to 1"
0.4	0.4/0.6 = 1/1.5 = 0.67	-0.41	"1.5 to 1"
8.0	0.8/0.2 = 4/1 = 4.00	1.39	"4 to 1 on"

- Gamblers use odds: if you win at 9 to 1 odds, get original stake back plus 9 times the stake.
- Probability has to be between 0 and 1
- Odds between 0 and infinity
- Log-odds can be anything: any log-odds corresponds to valid probability.

## Odds ratio

- Suppose 90 of 100 men drank wine last week, but only 20 of 100 women.
- Prob of man drinking wine 90/100 = 0.9, woman 20/100 = 0.2.
- Odds of man drinking wine 0.9/0.1 = 9, woman 0.2/0.8 = 0.25.
- Ratio of odds is 9/0.25 = 36.
- Way of quantifying difference between men and women: "odds of drinking wine 36 times larger for males than females'."

### Sepsis data again

Recall prediction of probability of death from risk factors:

```
sepsis.2.tidy <- tidy(sepsis.2)
sepsis.2.tidy</pre>
```

term	estimate	std.error	statistic	p.value
(Intercept)	-8.8945899	2.3168948	-3.839013	0.0001235
shock1	3.7011932	1.1035347	3.353944	0.0007967
alcohol1	3.1859040	0.9172457	3.473338	0.0005140
age	0.0898318	0.0292153	3.074821	0.0021063
bowelinf1	2.3864685	1.0722662	2.225631	0.0260389

Slopes in column estimate.

## Multiplying the odds

• Can interpret slopes by taking "exp" of them. We ignore intercept.

```
sepsis.2.tidy %>%
  mutate(exp_coeff=exp(estimate)) %>%
  select(term, exp_coeff)
```

term	exp_coeff
(Intercept)	0.0001371
shock1	40.4955951
alcohol1	24.1891449
age	1.0939902
bowelinf1	10.8750206

### Interpretation

term	exp_coeff
(Intercept)	0.0001371
shock1	40.4955951
alcohol1	24.1891449
age	1.0939902
bowelinf1	10.8750206

- These say "how much do you multiply odds of death by for increase of 1 in corresponding risk factor?" Or, what is odds ratio for that factor being 1 (present) vs. 0 (absent)?
- Eg. being alcoholic vs. not increases odds of death by 24 times
- One year older multiplies odds by about 1.1 times. Over 40 years, about  $1.09^{40}=31$  times.

#### Odds ratio and relative risk

- Relative risk is ratio of probabilities.
- Above: 90 of 100 men (0.9) drank wine, 20 of 100 women (0.2).
- Relative risk 0.9/0.2=4.5. (odds ratio was 36).
- When probabilities small, relative risk and odds ratio similar.
- Eg. prob of man having disease 0.02, woman 0.01.
- Relative risk 0.02/0.01 = 2.

#### Odds ratio vs. relative risk

Odds for men and for women:

```
(od1 <- 0.02 / 0.98) # men

## [1] 0.02040816

(od2 <- 0.01 / 0.99) # women

## [1] 0.01010101

• Odds ratio
```

- od1 / od2
- ## [1] 2.020408
  - Very close to relative risk of 2.

# More than 2 response categories

- With 2 response categories, model the probability of one, and prob of other is one minus that. So doesn't matter which category you model.
- With more than 2 categories, have to think more carefully about the categories: are they
- ordered: you can put them in a natural order (like low, medium, high)
- nominal: ordering the categories doesn't make sense (like red, green, blue).
- R handles both kinds of response; learn how.

### Ordinal response: the miners

- Model probability of being in given category or lower.
- Example: coal-miners often suffer disease pneumoconiosis. Likelihood of disease believed to be greater among miners who have worked longer.
- Severity of disease measured on categorical scale: none, moderate, severe.

#### Miners data

#### • Data are frequencies:

Exposure	None	Moderate	Severe
5.8	98	0	0
15.0	51	2	1
21.5	34	6	3
27.5	35	5	8
33.5	32	10	9
39.5	23	7	8
46.0	12	6	10
51.5	4	2	5

### Reading the data

Severe = col double()

## ## )

Data in aligned columns with more than one space between, so:

```
my_url <- "http://ritsokiguess.site/datafiles/miners-tab.txt"
freqs <- read_table(my_url)

##
## -- Column specification -------
## cols(
## Exposure = col_double(),
## None = col_double(),
## Moderate = col_double(),</pre>
```

### The data

#### freqs

Exposure	None	Moderate	Severe
5.8	98	0	0
15.0	51	2	1
21.5	34	6	3
27.5	35	5	8
33.5	32	10	9
39.5	23	7	8
46.0	12	6	10
51.5	4	2	5

# **Tidying**

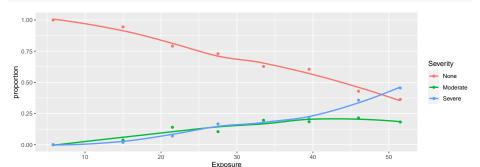
```
freqs %>%
  pivot_longer(-Exposure, names_to = "Severity", values_to = "
  mutate(Severity = fct_inorder(Severity)) -> miners
```

#### Result

miners

Exposure	Severity	Freq
5.8	None	98
5.8	Moderate	0
5.8	Severe	0
15.0	None	51
15.0	Moderate	2
15.0	Severe	1
21.5	None	34
21.5	Moderate	6
21.5	Severe	3
27.5	None	35
27.5	Moderate	5
27.5	Severe	8
33.5	None	32
33.5	Moderate	10
33.5	Severe	9
39.5	None	23
39.5	Moderate	7
39.5	Severe	8
46.0	None	12
46.0	Moderate	6
46.0	Severe	10
51.5	None	4
51.5	Moderate	2
51.5	Severe	5

### Plot proportions against exposure



# Reminder of data setup

miners

Exposure	Severity	Freq
5.8	None	98
5.8	Moderate	0
5.8	Severe	0
15.0	None	51
15.0	Moderate	2
15.0	Severe	1
21.5	None	34
21.5	Moderate	6
21.5	Severe	3
27.5	None	35
27.5	Moderate	5
27.5	Severe	8
33.5	None	32
33.5	Moderate	10
33.5	Severe	9
39.5	None	23
39.5 Log	Moderate gistic regression	7

### Fitting ordered logistic model

Use function polr from package MASS. Like glm.

```
sev.1 <- polr(Severity ~ Exposure,
  weights = Freq,
  data = miners
)</pre>
```

### Output: not very illuminating

```
sev.1 <- polr(Severity ~ Exposure,</pre>
 weights = Freq,
 data = miners,
 Hess = TRUE
summary(sev.1)
## Call:
## polr(formula = Severity ~ Exposure, data = miners, weights = Freq,
      Hess = TRUE
##
##
## Coefficients:
            Value Std. Error t value
##
## Exposure 0.0959 0.01194 8.034
##
  Intercepts:
##
                  Value Std. Error t value
## None | Moderate 3.9558 0.4097 9.6558
## Moderate|Severe 4.8690 0.4411 11.0383
##
## Residual Deviance: 416.9188
## AIC: 422.9188
```

### Does exposure have an effect?

Fit model without Exposure, and compare using anova. Note 1 for model with just intercept:

```
sev.0 <- polr(Severity ~ 1, weights = Freq, data = miners)
anova(sev.0, sev.1)</pre>
```

Model	Resid. df	Resid. Dev	Test	Df	LR stat.	Pr(Chi)
1	369	505.1621		NA	NA	NA
Exposure	368	416.9188	1 vs 2	1	88.24324	0

Exposure definitely has effect on severity of disease.

### Another way

• What (if anything) can we drop from model with exposure?

	Df	AIC	LRT	Pr(>Chi)
	NA	422.9188	NA	NA
Exposure	1	509.1621	88.24324	0

• Nothing. Exposure definitely has effect.

### Predicted probabilities 1/2

```
freqs %>% select(Exposure) -> new
new
```

Exposure
5.8
15.0
21.5
27.5
33.5
39.5
46.0
51.5

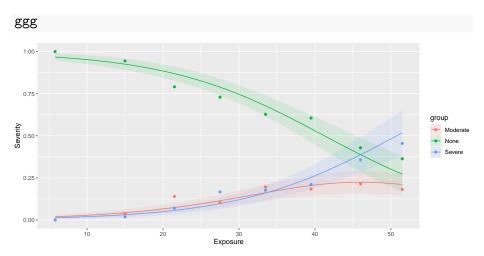
# Predicted probabilities 2/2

```
cbind(predictions(sev.1, newdata = new)) %>%
  select(group, estimate, Exposure) %>%
  pivot_wider(names_from = group, values_from = estimate)
```

Exposure	Moderate	None	Severe
5.8	0.0190891	0.9676920	0.0132189
15.0	0.0432993	0.9253445	0.0313561
21.5	0.0738586	0.8692003	0.0569411
27.5	0.1141300	0.7889290	0.0969409
33.5	0.1620715	0.6776641	0.1602644
39.5	0.2048420	0.5418105	0.2533476
46.0	0.2244155	0.3879962	0.3875883
51.5	0.2102501	0.2722543	0.5174956

### Plot of predicted probabilities

## The graph



#### Comments

- Model appears to match data well enough.
- As exposure goes up, prob of None goes down, Severe goes up (sharply for high exposure).
- So more exposure means worse disease.

#### Unordered responses

- With unordered (nominal) responses, can use generalized logit.
- Example: 735 people, record age and sex (male 0, female 1), which of 3 brands of some product preferred.
- Data in mlogit.csv separated by commas (so read\_csv will work):

```
my_url <- "http://ritsokiguess.site/datafiles/mlogit.csv"
brandpref <- read_csv(my_url)</pre>
```

```
## Rows: 735 Columns: 3
## -- Column specification ------
## Delimiter: ","
```

```
## dbl (3): brand, sex, age ##
```

## i Use `spec()` to retrieve the full column specification fo
## i Specify the column types or set `show\_col\_types = FALSE`

# The data (some)

 ${\tt brandpref}$ 

brand	sex	age
1	0	24
1	0	26
1	0	26
1	1	27
1	1	27
3	1	27
1	0	27
1	0	27
1	1	27
1	0	27
1	0	27
1	1	27
2	1	28
Logist	ic regressi	on

### Bashing into shape

• sex and brand not meaningful as numbers, so turn into factors:

### Fitting model

• We use multinom from package nnet. Works like polr.

```
brands.1 <- multinom(brand ~ age + sex, data = brandpref)
## # weights: 12 (6 variable)</pre>
```

```
## initial value 807.480032

## iter 10 value 702.990572

## final value 702.970704

## converged
```

## Can we drop anything?

• Unfortunately drop1 seems not to work:

```
drop1(brands.1, test = "Chisq", trace = 0)
```

```
## trying - age
```

## Error in if (trace)  $\{: argument is not interpretable as log$ 

 So, fall back on fitting model without what you want to test, and comparing using anova.

## Do age/sex help predict brand? 1/3

Fit models without each of age and sex:

brands.2 <- multinom(brand ~ age, data = brandpref)

## # weights: 9 (4 variable)

## initial value 807.480032

## iter 10 value 706.796323

## iter 10 value 706.796322

## final value 706.796322

## converged

```
## # weights: 9 (4 variable)
## initial value 807.480032
## final value 791.861266
## converged
```

brands.3 <- multinom(brand ~ sex, data = brandpref)</pre>

# Do age/sex help predict brand? 2/3

anova(brands.2, brands.1)

Model	Resid. df	Resid. Dev	Test	Df	LR stat.	Pr(Chi)
age	1466	1413.593	1 vs 2	NA	NA	NA
age + sex	1464	1405.941		2	7.651236	0.021805

anova(brands.3, brands.1)

Model	Resid. df	Resid. Dev	Test	Df	LR stat.	Pr(Chi)
sex	1466	1583.723	1 vs 2	NA	NA	NA
age + sex	1464	1405.941		2	177.7811	0

# Do age/sex help predict brand? 3/3

- age definitely significant (second anova)
- sex significant also (first anova), though P-value less dramatic
- Keep both.
- Expect to see a large effect of age, and a smaller one of sex.

### Another way to build model

• Start from model with everything and run step:

```
step(brands.1, trace = 0)
## trying - age
## trying - sex
## Call:
## multinom(formula = brand ~ age + sex)
##
## Coefficients:
##
     (Intercept) age sexmale
## 2 -11.25127 0.3682202 -0.5237736
## 3 -22.25571 0.6859149 -0.4658215
##
  Residual Deviance: 1405.941
## AIC: 1417.941
```

• Final model contains both age and sex so neither could be removed.

### Making predictions

Find age 5-number summary, and the two sexes:

summary(brandpref)

```
##
   brand
               sex
                            age
   1:207 female:466 Min. :24.0
##
##
   2:307 male :269 1st Qu.:32.0
##
   3:221
                       Median:32.0
                       Mean :32.9
##
##
                       3rd Qu.:34.0
##
                       Max. :38.0
```

Space the ages out a bit for prediction (see over).

#### **Combinations**

```
new <- datagrid(age = c(24, 30, 33, 35, 38),

sex = c("female", "male"), model = brands.1)
new
```

brand	age	sex
2	24	female
2	24	male
2	30	female
2	30	male
2	33	female
2	33	male
2	35	female
2	35	male
2	38	female
2	38	male

#### The predictions

```
cbind(predictions(brands.1, newdata = new)) %>%
  select(group, estimate, age, sex) %>%
  pivot_wider(names_from = group, values_from = estimate)
```

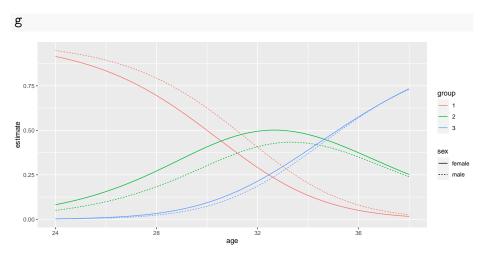
age	sex	1	2	3
24	female	0.9153281	0.0818834	0.0027886
24	male	0.9479605	0.0502270	0.0018126
30	female	0.4995959	0.4071307	0.0932733
30	male	0.6250637	0.3016944	0.0732418
33	female	0.2032060	0.4998037	0.2969903
33	male	0.2963797	0.4317571	0.2718632
35	female	0.0840409	0.4317037	0.4842554
35	male	0.1305674	0.3972445	0.4721880
38	female	0.0162307	0.2516401	0.7321292
38	male	0.0259786	0.2385542	0.7354671

#### Comments

- Young males prefer brand 1, but older males prefer brand 3.
- Females similar, but like brand 1 less and brand 2 more.
- A clear brand effect, but the sex effect is less clear.

# Making a plot

# The graph



# Digesting the plot

- Brand vs. age: younger people (of both genders) prefer brand 1, but older people (of both genders) prefer brand 3. (Explains significant age effect.)
- Brand vs. sex: females (solid) like brand 1 less than males (dashed), like brand 2 more (for all ages).
- Not much brand difference between genders (solid and dashed lines of same colours close), but enough to be significant.
- Model didn't include interaction, so modelled effect of gender on brand same for each age, modelled effect of age same for each gender. (See also later.)

#### Alternative data format

Summarize all people of same brand preference, same sex, same age on one line of data file with frequency on end:

#### brandpref

brand	sex	age
1	male	24
1	male	26
1	male	26
1	female	27
1	female	27
3	female	27
1	male	27
1	male	27
1	female	27
1	male	27
1 L	ogistic regression	77

### Getting alternative data format

```
brandpref %>%
  group_by(age, sex, brand) %>%
  summarize(Freq = n()) %>%
  ungroup() -> b
b
```

age	sex	brand	Freq			
24	male	1	1			
26	male	1	2			
27	female	1	4			
27	female	3	1			
27	male	1	4			
28	female	1	6			
28	female	2	2			
28	female	3	1			
28	male	1	4			
Logistic regression						

77 / 83

### Fitting models, almost the same

- Just have to remember weights to incorporate frequencies.
- Otherwise multinom assumes you have just 1 obs on each line!
- Again turn (numerical) sex and brand into factors:

```
b %>%
  mutate(sex = factor(sex)) %>%
  mutate(brand = factor(brand)) -> bf
b.1 <- multinom(brand ~ age + sex, data = bf, weights = Freq)
b.2 <- multinom(brand ~ age, data = bf, weights = Freq)</pre>
```

#### P-value for sex identical

anova(b.2, b.1)

Model	Resid. df	Resid. Dev	Test	Df	LR stat.	Pr(Chi)
age	126	1413.593		NA	NA	NA
age + sex	124	1405.941	1 vs 2	2	7.651236	0.021805

Same P-value as before, so we haven't changed anything important.

# Trying interaction between age and gender

```
brands.4 <- update(brands.1, . ~ . + age:sex)

## # weights: 15 (8 variable)
## initial value 807.480032
## iter 10 value 703.191146
## iter 20 value 702.572260
## iter 30 value 702.570900
## iter 30 value 702.570893
## iter 30 value 702.570893
## final value 702.570893
## converged</pre>
```

anova(brands.1, brands.4)

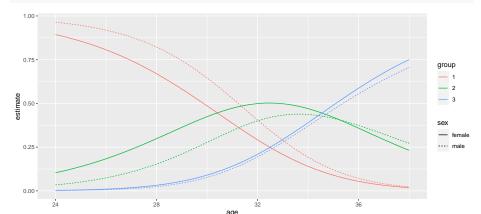
Model	Resid. df	Resid. Dev	Test	Df	LR stat.	Pr(Chi)
age + sex	1464	1405.941		NA	NA	NA
age + sex + age:sex	1462	1405.142	1 vs 2	2	0.7996223	0.6704466

 No evidence that effect of age on brand preference differs for the two genders.

## Make graph again

# Not much difference in the graph





### Compare model without interaction

