Analysis of Covariance

Analysis of covariance

- ANOVA: explanatory variables categorical (divide data into groups)
- traditionally, analysis of covariance has categorical x's plus one numerical x ("covariate") to be adjusted for.
- 1m handles this too.
- Simple example: two treatments (drugs) (a and b), with before and after scores.
- Does knowing before score and/or treatment help to predict after score?
- Is after score different by treatment/before score?

Data

Treatment, before, after:

```
a 5 20
a 10 23
```

a 12 30

a 9 25 a 23 34

a 21 40

a 14 27

a 18 38

a 6 24

a U 24 - 12 21

a 13 31

b 7 19

b 12 26

b 27 33 b 24 35

b 18 30

b 22 31

b 26 34

b 21 28 b 14 23

b 9 22

Packages

```
library(tidyverse)
library(broom)
library(marginaleffects)
```

the last of these for predictions.

Read in data

```
url <- "http://ritsokiguess.site/datafiles/ancova.txt"
prepost <- read_delim(url, " ")
prepost</pre>
```

```
# A tibble: 20 x 3
  drug before after
  <chr> <dbl> <dbl>
              5
1 a
                    20
2 a
             10
                    23
3 a
             12
                    30
4 a
              9
                    25
             23
5 a
                    34
6 a
             21
                    40
7 a
             14
                    27
8 a
             18
                    38
9 a
              6
                    24
10 a
             13
                    31
11 b
              7
                    19
12 b
             12
                    26
13 b
             27
                    33
14 b
                    35
             24
15 b
             18
                    30
16 b
             22
                    31
17 b
             26
                    34
18 b
             21
                    28
19 b
             14
                    23
                    22
20 b
              9
```

Making a plot

```
ggplot(prepost, aes(x = before, y = after, colour = drug)) +
geom_point()

drug

25-
20-
before
```

Comments

- As before score goes up, after score goes up.
- Red points (drug A) generally above blue points (drug B), for comparable before score.
- Suggests before score effect and drug effect.

The means

```
1 a 13.1 29.2
2 b 18 28.1
```

- Mean "after" score slightly higher for treatment A.
- Mean "before" score much higher for treatment B.
- Greater *improvement* on treatment A.

Testing for interaction

```
prepost.1 <- lm(after ~ before * drug, data = prepost)</pre>
  anova(prepost.1)
Analysis of Variance Table
Response: after
            Df Sum Sq Mean Sq F value
                                          Pr(>F)
             1 430.92 430.92 62.6894 6.34e-07 ***
before
             1 115.31
                      115.31 16.7743 0.0008442 ***
drug
                       12.34 1.7948 0.1990662
before:drug 1 12.34
Residuals
            16 109.98
                         6.87
```

• Interaction not significant. Will remove later.

Predictions

Signif. codes:

Set up values to predict for:

```
summary(prepost)
```

drug	before	after
Length: 20	Min. : 5.00	Min. :19.00
Class :character	1st Qu.: 9.75	1st Qu.:23.75
Mode :character	Median :14.00	Median :29.00
	Mean :15.55	Mean :28.65
	3rd Qu.:21.25	3rd Qu.:33.25
	Max. :27.00	Max. :40.00

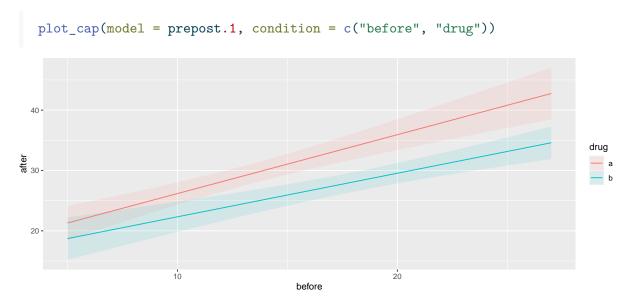
0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

and then

```
cbind(predictions(prepost.1, newdata = new)) %>%
    select(drug, before, estimate)

drug before estimate
1    a   9.75  25.93250
2    b   9.75  22.14565
3    a   14.00  30.07784
4    b   14.00  25.21304
5    a   21.25  37.14929
6    b   21.25  30.44565
```

Predictions (with interaction included), plotted



Lines almost parallel, but not quite.

Taking out interaction

- Take out non-significant interaction.
 - before and drug strongly significant.
 - Do predictions again and plot them.

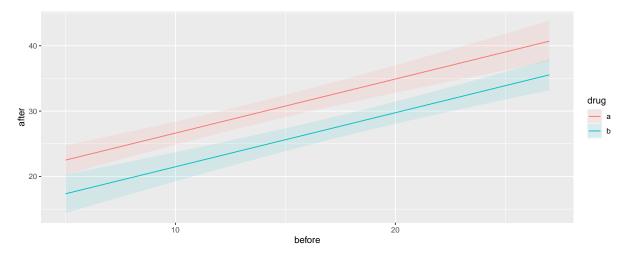
Predictions

```
cbind(predictions(prepost.2, newdata = new)) %>%
    select(drug, before, estimate)

drug before estimate
1    a   9.75  26.42794
2    b   9.75  21.27328
3    a   14.00  29.94473
4    b   14.00  24.79007
5    a   21.25  35.94397
6    b   21.25  30.78931
```

Plot of predicted values

```
plot_cap(prepost.2, condition = c("before", "drug"))
```



This time the lines are *exactly* parallel. No-interaction model forces them to have the same slope.

Different look at model output

summary(prepost.2)

- anova(prepost.2) tests for significant effect of before score and of drug, but doesn't help with interpretation.
- summary(prepost.2) views as regression with slopes:

```
Call:
lm(formula = after ~ before + drug, data = prepost)
Residuals:
    Min
            1Q Median
                            ЗQ
-3.6348 -2.5099 -0.2038 1.8871 4.7453
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 18.3600
                       1.5115 12.147 8.35e-10 ***
before
             0.8275
                        0.0955 8.665 1.21e-07 ***
drugb
             -5.1547
                        1.2876 -4.003 0.000921 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 2.682 on 17 degrees of freedom Multiple R-squared: 0.817, Adjusted R-squared: 0.7955 F-statistic: 37.96 on 2 and 17 DF, p-value: 5.372e-07

Understanding those slopes

- before ordinary numerical variable; drug categorical.
- 1m uses first category druga as baseline.
- Intercept is prediction of after score for before score 0 and drug A.
- before slope is predicted change in after score when before score increases by 1 (usual slope)
- Slope for drugb is *change* in predicted after score for being on drug B rather than drug A. Same for *any* before score (no interaction).

Summary

- ANCOVA model: fits different regression line for each group, predicting response from covariate.
- ANCOVA model with interaction between factor and covariate allows different slopes for each line.
- Sometimes those lines can cross over!
- If interaction not significant, take out. Lines then parallel.
- With parallel lines, groups have consistent effect regardless of value of covariate.