Matched pairs

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Some data:

subject	druga	drugb
1	2.0	3.5
2	3.6	5.7
3	2.6	2.9
4	2.6	2.4
5	7.3	9.9
6	3.4	3.3
7	14.9	16.7
8	6.6	6.0
9	2.3	3.8
10	2.0	4.0

Matched pairs 1/2

▶ Data are comparison of 2 drugs for effectiveness at reducing pain.

  ▶ 12 subjects (cases) were arthritis sufferers
  ▶ Response is #hours of pain relief from each drug.

▶ In reading example, each child tried only one reading method.

▶ But here, each subject tried out both drugs, giving us two measurements.

▶ Possible because, if you wait long enough, one drug has no influence over effect of other.

▶ Advantage: focused comparison of drugs. Compare one drug with another on same person, removes a lot of variability due to differences between people.

▶ Matched pairs, requires different analysis.

▶ Design: randomly choose 6 of 12 subjects to get drug A first, other 6 get drug B first.

Packages

```
library(tidyverse)
library(smmr) # for a sign test later
```

Reading the data

Values aligned in columns:

```
my_url <-
  "http://ritsokiguess.site/datafiles/analgesic.txt"
pain <- read_table(my_url)
pain
```

```
# A tibble: 12 x 3
   subject druga drugb
     <dbl> <dbl> <dbl>
 1       1   2     3.5
 2       2   3.6   5.7
 3       3   2.6   2.9
 4       4   2.6   2.4
 5       5   7.3   9.9
 6       6   3.4   3.3
 7       7  14.9  16.7
 8       8   6.6   6
 9       9   2.3   3.8
```

Paired *t*-test

```
with(pain, t.test(druga, drugb, paired = TRUE))
```

```
    Paired t-test

data:  druga and drugb
t = -2.1677, df = 11, p-value = 0.05299
alternative hypothesis: true mean difference is not equal t
95 percent confidence interval:
 -4.29941513  0.03274847
sample estimates:
mean difference
      -2.133333
```

▶ P-value is 0.053.
▶ Not quite evidence of difference between drugs.

t-testing the differences

▶ Likewise, you can calculate the differences yourself and then do a 1-sample t-test on them.

```
pain %>% mutate(diff = druga - drugb) -> pain
pain
```

```
# A tibble: 12 x 4
   subject druga drugb   diff
     <dbl> <dbl> <dbl>  <dbl>
 1       1     2   3.5   -1.5
 2       2   3.6   5.7   -2.1
 3       3   2.6   2.9 -0.300
 4       4   2.6   2.4  0.200
 5       5   7.3   9.9   -2.6
 6       6   3.4   3.3  0.100
 7       7  14.9  16.7  -1.80
 8       8   6.6     6  0.600
 9       9   2.3   3.8   -1.5
10      10     2     4     -2
```

t-test on the differences

▶ then throw them into t.test, testing that the mean is zero, with same result as before:

```
with(pain, t.test(diff, mu = 0))
```

```
    One Sample t-test

data:  diff
t = -2.1677, df = 11, p-value = 0.05299
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
 -4.29941513  0.03274847
sample estimates:
mean of x
-2.133333
```
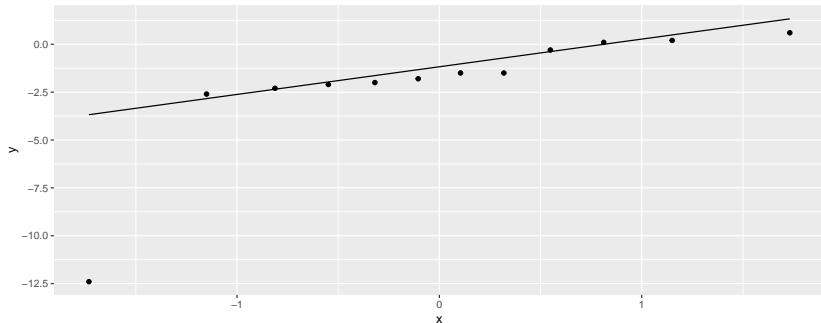
▶ Same P-value (0.053) and conclusion.

Assessing normality

- ▶ 1-sample and 2-sample t-tests assume (each) group normally distributed.
- ▶ Matched pairs analyses assume (theoretically) that differences normally distributed.
- ▶ How to assess normality? A normal quantile plot.

The normal quantile plot (of differences)

```
ggplot(pain,aes(sample=diff))+stat_qq()+stat_qq_line()
```


▶ Points should follow the straight line. Bottom left one way off, so normality questionable here: outlier.

What to do instead?

▶ Matched pairs t-test based on one sample of differences
▶ the differences not normal (enough)
▶ so do *sign test* on differences, null median 0:

```
sign_test(pain, diff, 0)

$above_below
below above
    9     3

$p_values
  alternative    p_value
1       lower 0.07299805
2       upper 0.98071289
3   two-sided 0.14599609
```
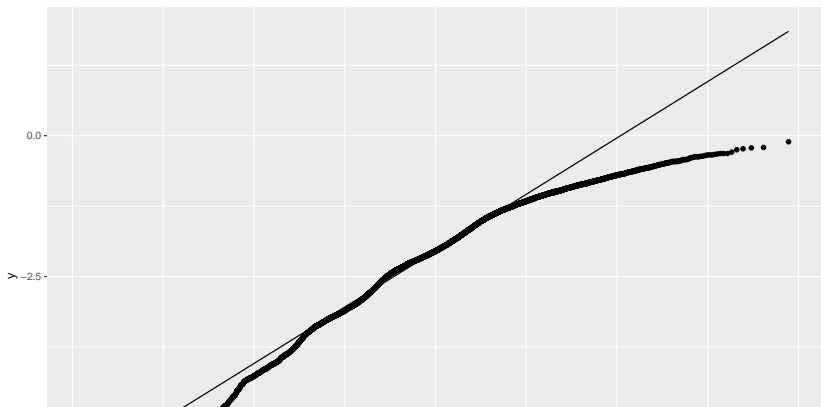
Did we need to worry about that outlier?

Bootstrap sampling distribution of sample mean differences:

```
tibble(sim = 1:10000) %>%
  rowwise() %>%
  mutate(my_sample = list(sample(pain$diff, replace = TRUE)
  mutate(my_mean = mean(my_sample)) %>%
  ggplot(aes(sample = my_mean)) + stat_qq() + stat_qq_line(
```

Comments

- no evidence of any difference between drugs (P-value 0.1460)
- in t-test, the low outlier difference pulled mean difference downward and made it look more negative than it should have been
- therefore, there really isn't any difference between the drugs.