```
In [238... # ECGR 4105
# Angelica Chica
# ID: 800 929 546
# Homework 5

In [238... %matplotlib inline
import numpy as np
import torch
import torch.nn as nn
import torch.optim as optim
from matplotlib import pyplot as plt

from sklearn.preprocessing import StandardScaler
from sklearn.model_selection import train_test_split
import numpy as np
import pandas as pd
```

Problem 1

```
In [239...
t_c = [0.5, 14.0, 15.0, 28.0, 11.0, 8.0, 3.0, -4.0, 6.0, 13.0, 21.0]
t_u = [35.7, 55.9, 58.2, 81.9, 56.3, 48.9, 33.9, 21.8, 48.4, 60.4, 68.4]

t_c = torch.tensor(t_c)
t_u = torch.tensor(t_u)

t_un_non = 0.1 * t_u
t_un_lin = 0.1 * t_u

w = torch.ones(())
w2 = torch.ones(())
w1 = torch.ones(())
b = torch.zeros(())
```

```
In [240... # Nonlinear model for regression.
         def model_nonlin(t_u, w2, w1, b):
             return w2 * t u ** 2 + w1 * t u + b
         def dmodel_dw2(t_u, w2, w1, b):
             return t_u**2
         def dmodel_dw1(t_u, w2, w1, b):
             return t u;
         def dmodel_db_nonlin(t_u, w2, w1, b):
             return 1.0
         def loss_fn(t_p, t_c):
             squared_diffs = (t_p - t_c)**2
             return squared_diffs.mean()
         def dloss_fn(t_p, t_c):
             dsq_diffs=2*(t_p - t_c) / t_p.size(0)
             return dsq_diffs
          def grad_fn_nonlin(t_u, t_c, t_p, w2, w1, b):
             dloss_dtp = dloss_fn(t_p, t_c)
             dloss_dw2 = dloss_dtp * dmodel_dw2(t_u, w2, w1, b)
             dloss_dw1 = dloss_dtp * dmodel_dw1(t_u, w2, w1, b)
```

```
return torch.stack([dloss dw2.sum(), dloss dw1.sum(), dloss db.sum()])
In [241... # linear model for regression
         def model_lin(t_u, w, b):
             return w * t u + b
         def dmodel_dw(t_u, w, b):
             return t_u
         def dmodel_db_lin(t_u, w, b):
             return 1.0
         def loss_fn(t_p, t_c):
             squared diffs = (t p - t c)**2
             return squared_diffs.mean()
         def dloss_fn(t_p, t_c):
              dsq_diffs=2*(t_p - t_c) / t_p.size(0)
             return dsq diffs
          def grad_fn_lin(t_u, t_c, t_p, w, b):
             dloss_dtp = dloss_fn(t_p, t_c)
             dloss dw = dloss dtp * dmodel dw(t u, w, b)
             dloss db = dloss dtp * dmodel db lin(t u, w, b)
             return torch.stack([dloss_dw.sum(), dloss_db.sum()])
In [242... # Training loop for nonlinear model.
          def training_loop_nonlin(n_epochs, learning_rate, params, t_u, t_c):
             for epoch in range(1, n epochs + 1):
                 w2, w1, b = params
                  t_p = model_nonlin(t_u, w2, w1, b)
                  loss = loss_fn(t_p, t_c)
                  grad = grad_fn_nonlin(t_u, t_c, t_p, w2, w1, b)
                  params = params - learning_rate * grad
                  if epoch % 500 == 0:
                      print('Epoch %d, Loss %f' % (epoch, float(loss)))
             return params
         # At different learning rates, print the loss over the 500th epoch.
In [243...
          rate = [1e-2, 1e-3, 1e-4, 1e-5]
         for learning_rate in rate:
              print(f'========= Learning Rate = {learning_rate} ==========================
             params = torch.tensor([1.0, 1.0, 0.0])
              params = training_loop_nonlin(
                  n = 5000,
                  learning_rate = learning_rate,
                  params = params,
                 t_u = t_un_non,
                 t_c = t_c
```

params

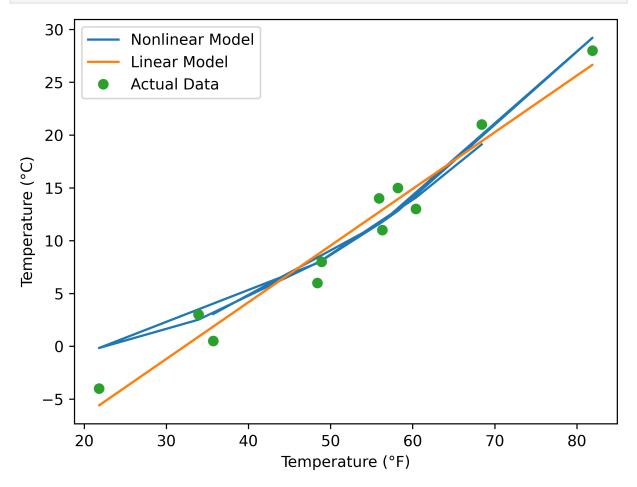
dloss_db = dloss_dtp * dmodel_db_nonlin(t_u, w2, w1, b)

```
Epoch 500, Loss nan
         Epoch 1000, Loss nan
         Epoch 1500, Loss nan
         Epoch 2000, Loss nan
         Epoch 2500, Loss nan
         Epoch 3000, Loss nan
         Epoch 3500, Loss nan
         Epoch 4000, Loss nan
         Epoch 4500, Loss nan
         Epoch 5000, Loss nan
         ====== Learning Rate = 0.001 ========
         Epoch 500, Loss nan
         Epoch 1000, Loss nan
         Epoch 1500, Loss nan
         Epoch 2000, Loss nan
         Epoch 2500, Loss nan
         Epoch 3000, Loss nan
         Epoch 3500, Loss nan
         Epoch 4000, Loss nan
         Epoch 4500, Loss nan
         Epoch 5000, Loss nan
         ======= Learning Rate = 0.0001 ========
         Epoch 500, Loss 10.708597
         Epoch 1000, Loss 8.642083
         Epoch 1500, Loss 7.171005
         Epoch 2000, Loss 6.123476
         Epoch 2500, Loss 5.377228
         Epoch 3000, Loss 4.845286
         Epoch 3500, Loss 4.465787
         Epoch 4000, Loss 4.194724
         Epoch 4500, Loss 4.000802
         Epoch 5000, Loss 3.861744
         ======= Learning Rate = 1e-05 =========
         Epoch 500, Loss 13.269526
         Epoch 1000, Loss 12.944256
         Epoch 1500, Loss 12.629864
         Epoch 2000, Loss 12.325988
         Epoch 2500, Loss 12.032271
         Epoch 3000, Loss 11.748377
         Epoch 3500, Loss 11.473977
         Epoch 4000, Loss 11.208754
         Epoch 4500, Loss 10.952396
         Epoch 5000, Loss 10.704611
In [244...
         params = torch.tensor([1.0, 1.0, 0.0])
         learning rate = 1e-4
         params = training loop nonlin(
             n_{epochs} = 5000,
             learning_rate = learning_rate,
             params = params,
             t_u = t_un_non,
             t_c = t_c
         params
```

======= Learning Rate = 0.01 =========

```
Epoch 500, Loss 10.708597
          Epoch 1000, Loss 8.642083
          Epoch 1500, Loss 7.171005
          Epoch 2000, Loss 6.123476
          Epoch 2500, Loss 5.377228
          Epoch 3000, Loss 4.845286
          Epoch 3500, Loss 4.465787
          Epoch 4000, Loss 4.194724
          Epoch 4500, Loss 4.000802
          Epoch 5000, Loss 3.861744
          tensor([ 0.5570, -0.8881, -0.8753])
Out[244]:
In [245... def training_loop_lin(n_epochs, learning_rate, params, t_u, t_c):
              for epoch in range(1, n_epochs + 1):
                  w, b = params
                  t_p = model_lin(t_u, w, b)
                  loss = loss_fn(t_p, t_c)
                   grad = grad_fn_lin(t_u, t_c, t_p, w, b)
                  params = params - learning rate * grad
                  if epoch % 500 == 0:
                      print('Epoch %d, Loss %f' % (epoch, float(loss)))
              return params
In [246...
          params linear = torch.tensor([1.0, 0.0])
          learning_rate = 1e-2
          params linear = training loop lin(
              n = 5000,
              learning_rate = learning_rate,
              params = params_linear,
              t_u = t_un_lin,
              tc = tc
          params_linear
          Epoch 500, Loss 7.860115
          Epoch 1000, Loss 3.828538
          Epoch 1500, Loss 3.092191
          Epoch 2000, Loss 2.957698
          Epoch 2500, Loss 2.933134
          Epoch 3000, Loss 2.928648
          Epoch 3500, Loss 2.927830
          Epoch 4000, Loss 2.927680
          Epoch 4500, Loss 2.927651
          Epoch 5000, Loss 2.927648
          tensor([ 5.3671, -17.3012])
Out[246]:
In [247... t_p_nonlinear = model_nonlin(t_un_non, *params)
          t_p_linear = model_lin(t_un_lin, *params_lin)
          fig = plt.figure(dpi=600)
          plt.xlabel("Temperature (°F)")
          plt.ylabel("Temperature (°C)")
          plt.plot(t_u.numpy(), t_p_nonlinear.detach().numpy(), label = "Nonlinear Model")
          plt.plot(t_u.numpy(), t_p_linear.detach().numpy(), label = "Linear Model")
          plt.plot(t_u.numpy(), t_c.numpy(), 'o', label = "Actual Data")
```

```
plt.legend()
plt.show()
```



Problem 2

```
In [249...
housing = pd.read_csv(r'C:\Users\achica1\Desktop\ML-DataSets\Housing.csv')
vars = ['area', 'bedrooms', 'bathrooms', 'stories', 'parking', 'price']
data = housing[vars]
data.head()
```

```
Out[249]:
                    bedrooms bathrooms stories parking
                                                              price
              area
           0 7420
                                       2
                                              3
                                                       2 13300000
                            4
           1 8960
                                       4
                                                       3 12250000
           2 9960
                            3
                                       2
                                              2
                                                       2 12250000
                                       2
           3 7500
                                                       3 12215000
           4 7420
                            4
                                       1
                                              2
                                                       2 11410000
```

```
In [250...
scaled = StandardScaler()
scaled_data_raw = scaled.fit_transform(data.values[:,:])
scaled_data = pd.DataFrame(scaled_data_raw)

X = scaled_data.values[:,0:5]
Y = scaled_data.values[:,5]
```

```
X train, X test, Y train, Y test = train test split(X, Y, test size=0.2, random state
```

```
In [251...
         area train = torch.tensor(X train[:,0])
          bedrooms_train = torch.tensor(X_train[:,1])
          bathrooms train = torch.tensor(X train[:,2])
          stories train = torch.tensor(X train[:,3])
          parking_train = torch.tensor(X_train[:,4])
          price_train = torch.tensor(Y_train)
         w1 = torch.ones(())
          w2 = torch.ones(())
         w3 = torch.ones(())
         w4 = torch.ones(())
          w5 = torch.ones(())
          b = torch.zeros(())
          area_test = torch.tensor(X_test[:,0])
          bedrooms_test = torch.tensor(X_test[:,1])
          bathrooms test = torch.tensor(X test[:,2])
          stories_test = torch.tensor(X_test[:,3])
          parking_test = torch.tensor(X_test[:,4])
          price_test = torch.tensor(Y_test)
          w1 = torch.ones(())
         w2 = torch.ones(())
         w3 = torch.ones(())
          w4 = torch.ones(())
         w5 = torch.ones(())
          b = torch.zeros(())
In [252... | def model(area, bedrooms, bathrooms, stories, parking, w1, w2, w3, w4, w5, b):
              return w5*parking + w4*stories + w3*bathrooms + w2*bedrooms + w1*area + b
          def loss fn(t p, price):
              squared_diffs = (t_p - price)**2
              return squared diffs.mean()
          def dloss_fn(t_p, price):
              dsq diffs=2* (t p - price) / t p.size(0)
              return dsq diffs
          def dmodel_dw5(parking, w5, b):
              return parking
          def dmodel_dw4(stories, w4, b):
              return stories
          def dmodel dw3(bathrooms, w3, b):
              return bathrooms
          def dmodel_dw2(bedrooms, w2, b):
              return bedrooms
          def dmodel dw1(area, w1, b):
              return area
          def dmodel_db(area, bedrooms, bathrooms, stories, parking, w1, w2, w3, w4, w5, b):
              return 1.0
```

```
def grad fn(area, bedrooms, bathrooms, stories, parking, price, t p, w1, w2, w3, w4, w
             dloss_dtp = dloss_fn(t_p, price)
             dloss dw5 = dloss dtp * dmodel dw5(parking, w5, b)
             dloss dw4 = dloss dtp * dmodel dw4(stories, w4, b)
             dloss_dw3 = dloss_dtp * dmodel_dw3(bathrooms, w3, b)
             dloss dw2 = dloss dtp * dmodel dw2(bedrooms, w2, b)
             dloss_dw1 = dloss_dtp * dmodel_dw1(area, w1, b)
             dloss_db = dloss_dtp * dmodel_db(area, bedrooms, bathrooms, stories, parking, w1,
             return torch.stack([dloss dw5.sum(),dloss dw4.sum(),dloss dw3.sum(),dloss dw2.sum(
         def training_loop(n_epochs, learning_rate, params, area, bedrooms, bathrooms, stories,
              print(f'========= Learning Rate = {learning_rate} ==========================
             for epoch in range(1, n_epochs + 1):
                 w1, w2, w3, w4, w5, b = params
                 t_p = model(area, bedrooms, bathrooms, stories, parking, w1, w2, w3, w4, w5, t
                  loss = loss_fn(t_p, price)
                  grad = grad fn(area, bedrooms, bathrooms, stories, parking, price, t p, w1, w2
                  params = params - learning rate * grad
                  if epoch == 1 or epoch % 500 == 0:
                      print('Epoch %d, Loss %f' % (epoch, float(loss)))
             return params, loss
In [253... rate = [1e-2, 1e-3, 1e-4, 1e-5]
         for learning rate in rate:
              params_train = torch.tensor([1.0, 1.0, 1.0, 1.0, 1.0, 0.0])
             learning_rate = learning_rate
             training loop(
                  n_{epochs} = 5000,
                  learning_rate = learning_rate,
                  params = params_train,
                  area = area_train,
                  bedrooms = bedrooms train,
                  bathrooms = bathrooms_train,
                  stories = stories_train,
                  parking = parking_train,
```

price = price train)

```
Epoch 1, Loss 5.965522
         Epoch 500, Loss 15429.993929
         Epoch 1000, Loss 8169457599.081010
         Epoch 1500, Loss 4544116725205980.000000
         Epoch 2000, Loss 2555540409318029393920.000000
         Epoch 2500, Loss 1440598518220296344276303872.000000
         Epoch 3000, Loss 812497726786145530359950608433152.000000
         Epoch 3500, Loss 458297996344184245923247564556133728256.000000
         Epoch 4000, Loss 258513769954810306486788190018636348584361984.000000
         Epoch 4500, Loss 145821484133829767796344972890715910412771017097216.000000
         Epoch 5000, Loss 82254524482028267379183529462016773486862327513446612992.000000
         ======= Learning Rate = 0.001 ========
         Epoch 1, Loss 5.965522
         Epoch 500, Loss 0.723786
         Epoch 1000, Loss 0.947568
         Epoch 1500, Loss 2.219570
         Epoch 2000, Loss 6.920083
         Epoch 2500, Loss 24.304790
         Epoch 3000, Loss 88.795261
         Epoch 3500, Loss 328.680360
         Epoch 4000, Loss 1223.135553
         Epoch 4500, Loss 4565.388574
         Epoch 5000, Loss 17077.598883
         ======= Learning Rate = 0.0001 ========
         Epoch 1, Loss 5.965522
         Epoch 500, Loss 4.251940
         Epoch 1000, Loss 3.078354
         Epoch 1500, Loss 2.277433
         Epoch 2000, Loss 1.731910
         Epoch 2500, Loss 1.361596
         Epoch 3000, Loss 1.111678
         Epoch 3500, Loss 0.944710
         Epoch 4000, Loss 0.835139
         Epoch 4500, Loss 0.765556
         Epoch 5000, Loss 0.724139
         ======= Learning Rate = 1e-05 =========
         Epoch 1, Loss 5.965522
         Epoch 500, Loss 5.763471
         Epoch 1000, Loss 5.568562
         Epoch 1500, Loss 5.380926
         Epoch 2000, Loss 5.200294
         Epoch 2500, Loss 5.026404
         Epoch 3000, Loss 4.859006
         Epoch 3500, Loss 4.697859
         Epoch 4000, Loss 4.542730
         Epoch 4500, Loss 4.393396
         Epoch 5000, Loss 4.249641
         print("Loss from the Training model: Linear Regression")
In [254...
         params_train = torch.tensor([1.0, 1.0, 1.0, 1.0, 1.0, 0.0])
         learning rate = 1e-4
         params train = training loop(
             n = 5000,
             learning_rate = learning_rate,
             params = params train,
             area = area train,
             bedrooms = bedrooms_train,
             bathrooms = bathrooms train,
             stories = stories_train,
```

======= Learning Rate = 0.01 =========

```
parking = parking_train,
              price = price_train)
          params_train
          Loss from the Training model: Linear Regression
          ======= Learning Rate = 0.0001 ========
          Epoch 1, Loss 5.965522
          Epoch 500, Loss 4.251940
          Epoch 1000, Loss 3.078354
          Epoch 1500, Loss 2.277433
          Epoch 2000, Loss 1.731910
          Epoch 2500, Loss 1.361596
          Epoch 3000, Loss 1.111678
          Epoch 3500, Loss 0.944710
          Epoch 4000, Loss 0.835139
          Epoch 4500, Loss 0.765556
          Epoch 5000, Loss 0.724139
          (tensor([ 0.2746, 0.4192, 0.3749, 0.1775, 0.5251, -0.0031],
Out[254]:
                  dtype=torch.float64),
           tensor(0.7241, dtype=torch.float64))
In [255... # Validation Model
          rate = [1e-2, 1e-3, 1e-4, 1e-5]
          for learning_rate in rate:
              params_test = torch.tensor([1.0, 1.0, 1.0, 1.0, 1.0, 0.0])
              learning_rate = learning_rate
              training_loop(
                  n_{epochs} = 5000,
                  learning_rate = learning_rate,
                  params = params_test,
                  area = area_test,
                  bedrooms = bedrooms test,
                  bathrooms = bathrooms_test,
                  stories = stories_test,
                  parking = parking_test,
                  price = price_test)
```

```
======= Learning Rate = 0.01 =========
         Epoch 1, Loss 6.422749
         Epoch 500, Loss 3747.592104
         Epoch 1000, Loss 399885318.469560
         Epoch 1500, Loss 46542146546085.039062
         Epoch 2000, Loss 5631467045934208000.000000
         Epoch 2500, Loss 692293233971147963367424.000000
         Epoch 3000, Loss 85638702341912930729141993472.000000
         Epoch 3500, Loss 10619407736953381105360932159094784.000000
         Epoch 4000, Loss 1318059036807454211138020616974345699328.000000
         Epoch 4500, Loss 163653292851367088010712139032497273677283328.000000
         Epoch 5000, Loss 20322364690552330273618344646039723414634857758720.000000
         ======= Learning Rate = 0.001 ========
         Epoch 1, Loss 6.422749
         Epoch 500, Loss 0.578541
         Epoch 1000, Loss 0.731333
         Epoch 1500, Loss 1.598271
         Epoch 2000, Loss 4.355404
         Epoch 2500, Loss 13.053470
         Epoch 3000, Loss 40.525670
         Epoch 3500, Loss 127.455068
         Epoch 4000, Loss 403.031064
         Epoch 4500, Loss 1278.185959
         Epoch 5000, Loss 4062.130062
         ======= Learning Rate = 0.0001 =========
         Epoch 1, Loss 6.422749
         Epoch 500, Loss 4.419614
         Epoch 1000, Loss 3.085965
         Epoch 1500, Loss 2.200358
         Epoch 2000, Loss 1.612678
         Epoch 2500, Loss 1.223355
         Epoch 3000, Loss 0.966349
         Epoch 3500, Loss 0.797858
         Epoch 4000, Loss 0.688848
         Epoch 4500, Loss 0.620083
         Epoch 5000, Loss 0.578841
         ======= Learning Rate = 1e-05 =========
         Epoch 1, Loss 6.422749
         Epoch 500, Loss 6.183709
         Epoch 1000, Loss 5.953785
         Epoch 1500, Loss 5.733079
         Epoch 2000, Loss 5.521221
         Epoch 2500, Loss 5.317858
         Epoch 3000, Loss 5.122647
         Epoch 3500, Loss 4.935263
         Epoch 4000, Loss 4.755390
         Epoch 4500, Loss 4.582729
         Epoch 5000, Loss 4.416989
In [256... # Linear Regression of the Validation model's loss
         params test = torch.tensor([1.0, 1.0, 1.0, 1.0, 1.0, 0.0])
         learning rate = 1e-4
         params test = training loop(
             n_{epochs} = 5000,
             learning rate = learning rate,
             params = params test,
             area = area_test,
             bedrooms = bedrooms test,
             bathrooms = bathrooms_test,
```

```
parking = parking_test,
              price = price_test)
          params_test
          ======= Learning Rate = 0.0001 ========
          Epoch 1, Loss 6.422749
          Epoch 500, Loss 4.419614
          Epoch 1000, Loss 3.085965
          Epoch 1500, Loss 2.200358
          Epoch 2000, Loss 1.612678
          Epoch 2500, Loss 1.223355
          Epoch 3000, Loss 0.966349
          Epoch 3500, Loss 0.797858
          Epoch 4000, Loss 0.688848
          Epoch 4500, Loss 0.620083
          Epoch 5000, Loss 0.578841
          (tensor([0.4858, 0.4767, 0.2127, 0.1545, 0.3222, 0.0085],
Out[256]:
                  dtype=torch.float64),
           tensor(0.5788, dtype=torch.float64))
          problem 3
In [259...
          housing = pd.read csv(r'C:\Users\achica1\Desktop\ML-DataSets\Housing.csv')
          vars = ['area', 'bedrooms', 'bathrooms', 'stories', 'parking', 'price']
          data = housing[vars]
          data.head()
Out[259]:
                  bedrooms bathrooms stories parking
                                                         price
          0 7420
                          4
                                    2
                                           3
                                                   2 13300000
          1 8960
                                                   3 12250000
                                    2
          2 9960
                          3
                                           2
                                                   2 12250000
                                    2
          3 7500
                                                   3 12215000
          4 7420
                          4
                                    1
                                           2
                                                   2 11410000
In [260...
          scaled = StandardScaler()
          scaled_data_raw = scaled.fit_transform(data.values[:,:])
          scaled data = pd.DataFrame(scaled data raw)
          X_data = torch.tensor(scaled_data.values[:,0:5], dtype=torch.float32)
          Y_data = torch.tensor(scaled_data.values[:,5], dtype=torch.float32)
In [261...
          # Splitting the dataset using training and validation split
          n samples = X data.shape[0]
          n_val = int(0.2 * n_samples)
          shuffled_indices = torch.randperm(n_samples)
          train indices = shuffled indices[:-n val]
          val_indices = shuffled_indices[-n_val:]
          X_train = X_data[train_indices]
```

stories = stories_test,

Y train raw = Y data[train indices]

```
Y_train = torch.reshape(Y_train_raw, (436,1))
         X_val = X_data[val_indices]
         Y_val_raw = Y_data[val_indices]
         Y val = torch.reshape(Y val raw, (109,1))
In [263... def training loop(n epochs, optimizer, model, loss fn, X train, X val, Y train, Y val,
             for epoch in range(1, n_epochs + 1):
                 t_p_train = model(X_train)
                  loss_train = loss_fn(t_p_train, Y_train)
                  t p val = model(X val)
                  loss_val = loss_fn(t_p_val, Y_val)
                  optimizer.zero grad()
                  loss_train.backward()
                  optimizer.step()
                  epochs.append(epoch)
                  train loss.append(loss train.item())
                  val_loss.append(loss_val.item())
                  if epoch == 1 or epoch % 40 == 0:
                      print(f"Epoch {epoch}, Training loss {loss_train.item():.4f},"
                            f" Validation loss {loss_val.item():.4f}")
         def loss_fn(t_p, t_c):
             squared_diffs = (t_p - t_c)**2
             return squared_diffs.mean()
In [267... # Problem 3a
         from collections import OrderedDict
          seq model one = nn.Sequential(OrderedDict([
              ('hidden_linear', nn.Linear(5, 8)),
              ('hidden_activation', nn.ReLU()),
              ('output_linear', nn.Linear(8, 1))
          ]))
         optimizer = optim.SGD(seq model one.parameters(), lr=0.07)
         one_epochs = []
         one_train_loss = []
         one val loss = []
         print("one hidden layer:")
          params_one = training_loop(n_epochs = 200, optimizer = optimizer, model = seq_model_or
             X_val = X_val, Y_train = Y_train, Y_val = Y_val, epochs = one_epochs, train_loss
         params_one
         one hidden layer:
         Epoch 1, Training loss 1.0766, Validation loss 1.2084
         Epoch 40, Training loss 0.4976, Validation loss 0.3323
         Epoch 80, Training loss 0.4657, Validation loss 0.3115
         Epoch 120, Training loss 0.4593, Validation loss 0.3035
         Epoch 160, Training loss 0.4570, Validation loss 0.2991
         Epoch 200, Training loss 0.4553, Validation loss 0.2967
In [268... seq_model_three = nn.Sequential(OrderedDict([
```

```
('hidden_linear_1', nn.Linear(5, 8)),
    ('hidden_activation_1', nn.ReLU()),
    ('hidden_linear_2', nn.Linear(8, 8)),
    ('hidden_activation_2', nn.ReLU()),
    ('hidden_linear_3', nn.Linear(8, 8)),
    ('hidden_activation_3', nn.ReLU()),
    ('output_linear', nn.Linear(8, 1))
]))
optimizer = optim.SGD(seq model three.parameters(), lr=0.095)
three_epochs = []
three_train_loss = []
three val loss = []
print("three hidden layers:")
params_three = training_loop(n_epochs = 200, optimizer = optimizer, model = seq_model_
    X_train = X_train, X_val = X_val, Y_train = Y_train, Y_val = Y_val, epochs = three
    val loss = three val loss)
params_three
three hidden layers:
Epoch 1, Training loss 1.0375, Validation loss 1.0815
Epoch 40, Training loss 0.6212, Validation loss 0.5867
Epoch 80, Training loss 0.4976, Validation loss 0.4057
Epoch 120, Training loss 0.4580, Validation loss 0.3547
Epoch 160, Training loss 0.4610, Validation loss 0.3519
Epoch 200, Training loss 0.4425, Validation loss 0.3395
```

In []: