# Statistical Machine Translation LING-462/COSC-482 Week 4:

Phrase-based statistical machine translation

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### Agenda

- Language in ten minutes: Janet Liu: German
- Planning further "Language in ten minutes" presentations
- Step-by-step walk trough IBM Model 1 word alignment
- Break -
- Phrase-based statistical machine translation
- MT internships?

#### IBM Model 1

- Generative model: break up translation process into smaller steps
  - IBM Model 1 only uses lexical translation
- Translation probability
  - for a foreign sentence  $\mathbf{f} = (f_1, ..., f_{l_f})$  of length  $l_f$
  - to an English sentence  $\mathbf{e}=(e_1,...,e_{l_e})$  of length  $l_e$
  - with an alignment of each English word  $e_j$  to a foreign word  $f_i$  according to the alignment function  $a:j\to i$

$$p(\mathbf{e}, a|\mathbf{f}) = \frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} t(e_j|f_{a(j)})$$

- parameter  $\epsilon$  is a normalization constant

### EM Expectation step ground work

 Deriving the formula to calculate the alignment probability based on word translation probabilities

$$p(a|e,f) = \frac{p(a,e,f)}{p(e,f)} = \frac{p(a,e,f)p(f)}{p(e,f)p(f)}$$
$$= \frac{p(e,a|f)}{p(e|f)} = \dots = \prod_{j=1}^{l_e} \frac{t(e_j|f_{a(j)})}{\sum_{i=0}^{l_f} t(e_j|f_i)}$$

#### IBM Model 1 and EM: Maximization Step

- Now we have to collect counts
- Evidence from a sentence pair **e**, **f** that word e is a translation of word f:

$$c(e|f; \mathbf{e}, \mathbf{f}) = \sum_{a} p(a|\mathbf{e}, \mathbf{f}) \sum_{j=1}^{l_e} \delta(e, e_j) \delta(f, f_{a(j)})$$

• With the same simplication as before:

$$c(e|f; \mathbf{e}, \mathbf{f}) = \frac{t(e|f)}{\sum_{i=0}^{l_f} t(e|f_i)} \sum_{j=1}^{l_e} \delta(e, e_j) \sum_{i=0}^{l_f} \delta(f, f_i)$$

#### IBM Model 1 and EM: Maximization Step

After collecting these counts over a corpus, we can estimate the model:

$$t(e|f; \mathbf{e}, \mathbf{f}) = \frac{\sum_{(\mathbf{e}, \mathbf{f})} c(e|f; \mathbf{e}, \mathbf{f})}{\sum_{e} \sum_{(\mathbf{e}, \mathbf{f})} c(e|f; \mathbf{e}, \mathbf{f}))}$$

# Walk-trough with Excel sheet

# Noisy channel model

$$argmax_f p(f|e) = argmax_f p(e|f)p(f)$$

# Language Model p(f)

Given the target language corpus

```
<s> la maison </s>
```

<s> une maison </s>

# Unigrams maximum likelihood probabilities

W	p(w)
<s></s>	0.25
la	0.167
maison	0.167
lune	0.084
une	0.084
	0.25

# Bigram counts

w1/w2	<b>&lt;</b> \$>	la	maison	lune	une		Total
<s></s>		2			1		3
la			1	1			2
maison						2	2
lune						1	1
une			1				1
							0

# Bigram maximum likelihood probabilities

p(w2 w1)	<s></s>	la	maison	lune	une		Total
<s></s>		0.667			0.333		1.000
la			0.500	0.500			1.000
maison						1.000	1.000
lune						1.000	1.000
une			1.000				1.000
							0.000

# Bigram maximum likelihood probabilities

- What happens if translation model suggests "une lune" to translate "a moon"?
- Bigram model estimates probability zero!
- Language model smoothing/ interpolation/backoff needed

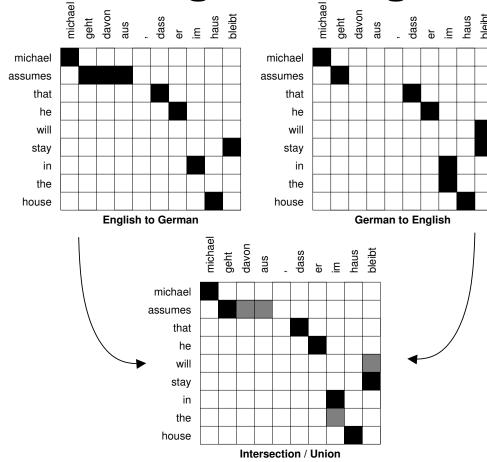
# Bigram add-one counts

w1/w2	<b>&lt;</b> \$>	la	maison	lune	une		Total
<s></s>	1	3	1	1	2	1	9
la	1	1	2	2	1	1	8
maison	1	1	1	1	1	3	8
lune	1	1	1	1	1	2	7
une	1	1	2	1	1	1	7
	1	1	1	1	1	1	6

# Bigram add-one probabilities

p(w2 w1	<s></s>	la	maison	lune	une		Total
/		ıa	maison	Idiic	arre	<b>1</b> /3/	Iotai
<s></s>	0.111	0.333	0.111	0.111	0.222	0.111	1.000
la	0.125	0.125	0.250	0.250	0.125	0.125	1.000
maison	0.125	0.125	0.125	0.125	0.125	0.375	1.000
lune	0.143	0.143	0.143	0.143	0.143	0.286	1.000
une	0.143	0.143	0.286	0.143	0.143	0.143	1.000
	0.167	0.167	0.167	0.167	0.167	0.167	1.000

#### **Symmetrizing Word Alignments**



- Intersection of GIZA++ bidirectional alignments
- Grow additional alignment points [Och and Ney, CompLing2003]

#### **Growing heuristic**

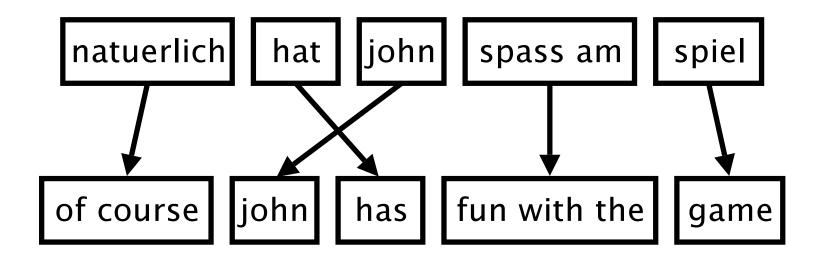
```
grow-diag-final(e2f,f2e)
 1: neighboring = \{(-1,0),(0,-1),(1,0),(0,1),(-1,-1),(-1,1),(1,-1),(1,1)\}
 2: alignment A = intersect(e2f,f2e); grow-diag(); final(e2f); final(f2e);
grow-diag()
 1: while new points added do
          for all English word e \in [1...e_n], foreign word f \in [1...f_n], (e, f) \in A do
 2:
              for all neighboring alignment points (e_{\text{new}}, f_{\text{new}}) do
 3:
 4:
                   if (e_{\text{new}} \text{ unaligned OR } f_{\text{new}} \text{ unaligned}) \text{ AND } (e_{\text{new}}, f_{\text{new}}) \in \text{union(e2f,f2e)} then
                       add (e_{\text{new}}, f_{\text{new}}) to A
 5:
                   end if
 6:
 7:
              end for
 8:
         end for
 9: end while
final()
 1: for all English word e_{\text{new}} \in [1...e_n], foreign word f_{\text{new}} \in [1...f_n] do
          if (e_{\text{new}} \text{ unaligned OR } f_{\text{new}} \text{ unaligned}) \text{ AND } (e_{\text{new}}, f_{\text{new}}) \in \text{union(e2f,f2e)} then
 3:
              add (e_{\text{new}}, f_{\text{new}}) to A
          end if
 4:
 5: end for
```

# PHRASE-BASED STATISTICAL MACHINE TRANSLATION

#### **Motivation**

- Word-Based Models translate words as atomic units
- Phrase-Based Models translate *phrases* as atomic units
- Advantages:
  - many-to-many translation can handle non-compositional phrases
  - use of local context in translation
  - the more data, the longer phrases can be learned
- "Standard Model", used by Google Translate and others

#### Phrase-Based Model



- Foreign input is segmented in phrases
- Each phrase is translated into English
- Phrases are reordered

#### **Phrase Translation Table**

- Main knowledge source: table with phrase translations and their probabilities
- Example: phrase translations for natuerlich

Translation	Probability $\phi(\bar{e} \bar{f})$
of course	0.5
naturally	0.3
of course,	0.15
, of course ,	0.05

#### Real Example

• Phrase translations for den Vorschlag learned from the Europarl corpus:

English	$\phi(ar{e} ar{f})$	English	$\phi(ar{e} ar{f})$
the proposal	0.6227	the suggestions	0.0114
's proposal	0.1068	the proposed	0.0114
a proposal	0.0341	the motion	0.0091
the idea	0.0250	the idea of	0.0091
this proposal	0.0227	the proposal,	0.0068
proposal	0.0205	its proposal	0.0068
of the proposal	0.0159	it	0.0068
the proposals	0.0159		

- lexical variation (proposal vs suggestions)
- morphological variation (proposal vs proposals)
- included function words (the, a, ...)
- noise (it)

#### **Linguistic Phrases?**

- Model is not limited to linguistic phrases
   (noun phrases, verb phrases, prepositional phrases, ...)
- Example non-linguistic phrase pair

spass am 
$$\rightarrow$$
 fun with the

- Prior noun often helps with translation of preposition
- Experiments show that limitation to linguistic phrases hurts quality

#### **Probabilistic Model**

Bayes rule

$$\mathbf{e}_{\mathsf{best}} = \mathsf{argmax}_{\mathbf{e}} \; p(\mathbf{e}|\mathbf{f})$$

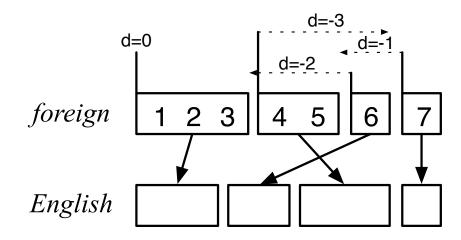
$$= \mathsf{argmax}_{\mathbf{e}} \; p(\mathbf{f}|\mathbf{e}) \; p_{\mathrm{LM}}(\mathbf{e})$$

- translation model  $p(\mathbf{e}|\mathbf{f})$
- language model  $p_{\rm LM}(\mathbf{e})$
- Decomposition of the translation model

$$p(\bar{f}_1^I | \bar{e}_1^I) = \prod_{i=1}^I \phi(\bar{f}_i | \bar{e}_i) \ d(start_i - end_{i-1} - 1)$$

- phrase translation probability  $\phi$
- reordering probability d

#### **Distance-Based Reordering**



phrase	translates	movement	distance
1	1–3	start at beginning	0
2	6	skip over 4–5	+2
3	4–5	move back over 4–6	-3
4	7	skip over 6	+1

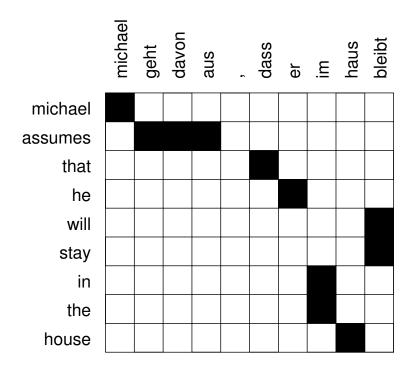
Scoring function:  $d(x) = \alpha^{|x|}$  — exponential with distance

#### Learning a Phrase Translation Table

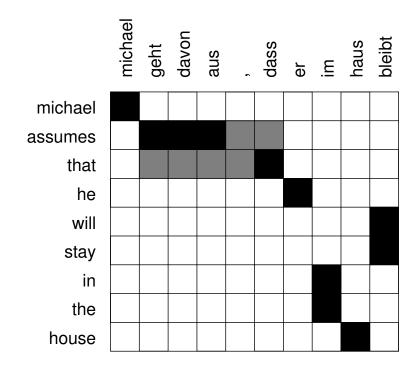
• Task: learn the model from a parallel corpus

- Three stages:
  - word alignment: using IBM models or other method
  - extraction of phrase pairs
  - scoring phrase pairs

#### **Word Alignment**



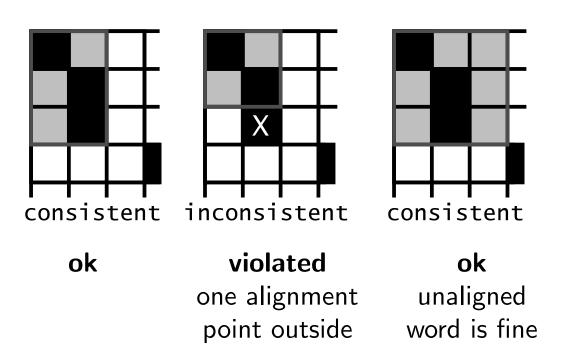
#### **Extracting Phrase Pairs**



extract phrase pair consistent with word alignment:

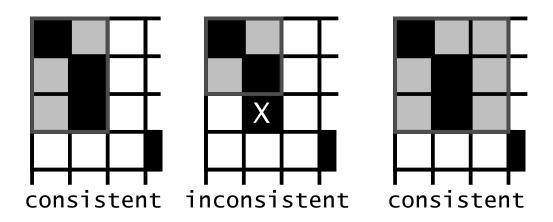
assumes that / geht davon aus, dass

#### Consistent



All words of the phrase pair have to align to each other.

#### Consistent

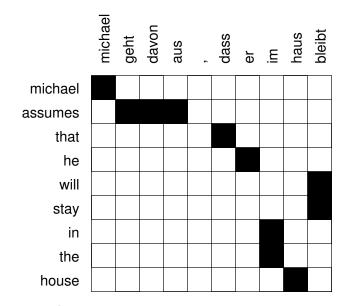


Phrase pair  $(\bar{e}, \bar{f})$  consistent with an alignment A, if all words  $f_1, ..., f_n$  in  $\bar{f}$  that have alignment points in A have these with words  $e_1, ..., e_n$  in  $\bar{e}$  and vice versa:

 $(\bar{e},\bar{f})$  consistent with  $A \Leftrightarrow$ 

$$\forall e_i \in \bar{e} : (e_i, f_j) \in A \to f_j \in \bar{f}$$
AND  $\forall f_j \in \bar{f} : (e_i, f_j) \in A \to e_i \in \bar{e}$ 
AND  $\exists e_i \in \bar{e}, f_j \in \bar{f} : (e_i, f_j) \in A$ 

#### **Phrase Pair Extraction**

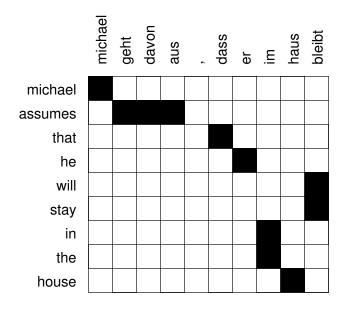


#### Smallest phrase pairs:

```
michael — michael
assumes — geht davon aus / geht davon aus ,
that — dass / , dass
he — er
will stay — bleibt
in the — im
house — haus
```

unaligned words (here: German comma) lead to multiple translations

#### **Larger Phrase Pairs**



```
michael assumes — michael geht davon aus / michael geht davon aus , assumes that — geht davon aus , dass er that he — dass er / , dass er ; in the house — im haus michael assumes that — michael geht davon aus , dass michael assumes that he — michael geht davon aus , dass er michael assumes that he will stay in the house — michael geht davon aus , dass er im haus bleibt assumes that he will stay in the house — geht davon aus , dass er im haus bleibt that he will stay in the house — geht davon aus , dass er im haus bleibt , he will stay in the house — er im haus bleibt ; will stay in the house — im haus bleibt
```

#### **Scoring Phrase Translations**

- Phrase pair extraction: collect all phrase pairs from the data
- Phrase pair scoring: assign probabilities to phrase translations
- Score by relative frequency:

$$\phi(\bar{f}|\bar{e}) = \frac{\mathsf{count}(\bar{e}, \bar{f})}{\sum_{\bar{f}_i} \mathsf{count}(\bar{e}, \bar{f}_i)}$$

#### Size of the Phrase Table

- Phrase translation table typically bigger than corpus
  - ... even with limits on phrase lengths (e.g., max 7 words)
- $\rightarrow$  Too big to store in memory?
  - Solution for training
    - extract to disk, sort, construct for one source phrase at a time
  - Solutions for decoding
    - on-disk data structures with index for quick look-ups
    - suffix arrays to create phrase pairs on demand

#### Weighted Model

- Described standard model consists of three sub-models
  - phrase translation model  $\phi(\bar{f}|\bar{e})$
  - reordering model d
  - language model  $p_{LM}(e)$

$$e_{\mathsf{best}} = \mathsf{argmax}_e \prod_{i=1}^I \phi(\bar{f}_i | \bar{e}_i) \ d(start_i - end_{i-1} - 1) \ \prod_{i=1}^{|\mathbf{e}|} p_{LM}(e_i | e_1 ... e_{i-1})$$

- Some sub-models may be more important than others
- Add weights  $\lambda_{\phi}$ ,  $\lambda_{d}$ ,  $\lambda_{LM}$

$$e_{\mathsf{best}} = \mathsf{argmax}_e \prod_{i=1}^{I} \phi(\bar{f}_i | \bar{e}_i)^{\lambda_\phi} \ d(start_i - end_{i-1} - 1)^{\lambda_d} \ \prod_{i=1}^{|\mathbf{e}|} p_{LM}(e_i | e_1 ... e_{i-1})^{\lambda_{LM}}$$

#### Log-Linear Model

• Such a weighted model is a log-linear model:

$$p(x) = \exp \sum_{i=1}^{n} \lambda_i h_i(x)$$

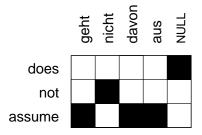
- Our feature functions
  - number of feature function n=3
  - random variable x = (e, f, start, end)
  - feature function  $h_1 = \log \phi$
  - feature function  $h_2 = \log d$
  - feature function  $h_3 = \log p_{LM}$

#### Weighted Model as Log-Linear Model

$$p(e, a|f) = \exp(\lambda_{\phi} \sum_{i=1}^{I} \log \phi(\bar{f}_i|\bar{e}_i) + \lambda_d \sum_{i=1}^{I} \log d(a_i - b_{i-1} - 1) + \lambda_{LM} \sum_{i=1}^{|\mathbf{e}|} \log p_{LM}(e_i|e_1...e_{i-1}))$$

#### **More Feature Functions**

- Bidirectional alignment probabilities:  $\phi(\bar{e}|\bar{f})$  and  $\phi(\bar{f}|\bar{e})$
- Rare phrase pairs have unreliable phrase translation probability estimates
  - → lexical weighting with word translation probabilities

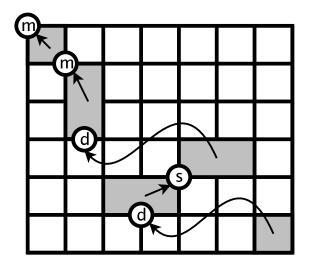


$$\operatorname{lex}(\bar{e}|\bar{f},a) = \prod_{i=1}^{\operatorname{length}(\bar{e})} \frac{1}{|\{j|(i,j)\in a\}|} \sum_{\forall (i,j)\in a} w(e_i|f_j)$$

#### **More Feature Functions**

- Language model has a bias towards short translations
  - $\rightarrow$  word count:  $wc(e) = \log |e|^{\omega}$
- We may prefer finer or coarser segmentation
  - $\rightarrow$  phrase count  $pc(e) = \log |I|^{\rho}$
- Multiple language models
- Multiple translation models
- Other knowledge sources

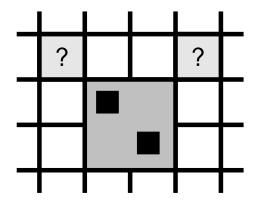
#### **Lexicalized Reordering**



- Distance-based reordering model is weak
  - → learn reordering preference for each phrase pair
- Three orientations types: (m) monotone, (s) swap, (d) discontinuous

orientation 
$$\in \{m, s, d\}$$
  
 $p_o(\text{orientation}|\bar{f}, \bar{e})$ 

#### **Learning Lexicalized Reordering**



- Collect orientation information during phrase pair extraction
  - if word alignment point to the top left exists → monotone
  - if a word alignment point to the top right exists → swap
  - if neither a word alignment point to top left nor to the top right exists
    - $\rightarrow$  neither monotone nor swap  $\rightarrow$  **discontinuous**

#### **Learning Lexicalized Reordering**

Estimation by relative frequency

$$p_o(\text{orientation}) = \frac{\sum_{\bar{f}} \sum_{\bar{e}} count(\text{orientation}, \bar{e}, \bar{f})}{\sum_{o} \sum_{\bar{f}} \sum_{\bar{e}} count(o, \bar{e}, \bar{f})}$$

ullet Smoothing with unlexicalized orientation model  $p(\mbox{orientation})$  to avoid zero probabilities for unseen orientations

$$p_o(\text{orientation}|\bar{f},\bar{e}) = \frac{\sigma \ p(\text{orientation}) + count(\text{orientation},\bar{e},f)}{\sigma + \sum_o count(o,\bar{e},\bar{f})}$$

### Summary

- What we have now: statistical models
  - Word-based translation models
  - Phrase-based translation models
  - N-gram language models
  - Noisy channel model
  - Log-linear model
- Next: decoding
  - How do we find the most-likely or top-n most likely translations?