BE7023 Homework 8

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```
#setwd("C:/Users/lapt3u/Box/UC/Fall_2018/BE7023_Adv_Biostats/adv_biostats/hw_8")
library(MatchIt)
dat <- lalonde
dim(dat)
## [1] 614 10
summary(dat)
##
        treat
                                           educ
                                                           black
                           age
##
                                             : 0.00
                                                              :0.0000
   Min.
           :0.0000
                     Min.
                            :16.00
                                      Min.
                                                       Min.
   1st Qu.:0.0000
                      1st Qu.:20.00
                                      1st Qu.: 9.00
                                                       1st Qu.:0.0000
    Median :0.0000
                     Median :25.00
                                      Median :11.00
                                                       Median :0.0000
##
##
    Mean
           :0.3013
                     Mean
                            :27.36
                                      Mean
                                            :10.27
                                                       Mean
                                                              :0.3958
    3rd Qu.:1.0000
##
                     3rd Qu.:32.00
                                      3rd Qu.:12.00
                                                       3rd Qu.:1.0000
##
    Max.
           :1.0000
                             :55.00
                                             :18.00
                                                       Max.
                                                              :1.0000
                     Max.
                                      Max.
##
        hispan
                        married
                                          nodegree
                                                              re74
##
           :0.0000
                     Min.
                             :0.0000
                                       Min.
                                               :0.0000
   Min.
                                                         Min.
    1st Qu.:0.0000
                      1st Qu.:0.0000
                                       1st Qu.:0.0000
                                                         1st Qu.:
                                                         Median: 1042
##
    Median :0.0000
                     Median :0.0000
                                       Median :1.0000
##
    Mean
           :0.1173
                     Mean
                             :0.4153
                                       Mean
                                              :0.6303
                                                         Mean
                                                                : 4558
    3rd Qu.:0.0000
##
                     3rd Qu.:1.0000
                                       3rd Qu.:1.0000
                                                         3rd Qu.: 7888
    Max.
           :1.0000
                             :1.0000
                                              :1.0000
                                                         Max.
                                                                :35040
##
         re75
                            re78
                                   0.0
##
    Min.
                0.0
                      Min.
                             :
    1st Qu.:
                0.0
                      1st Qu.: 238.3
                      Median: 4759.0
  Median : 601.5
## Mean : 2184.9
                            : 6792.8
                      Mean
    3rd Qu.: 3249.0
                      3rd Qu.:10893.6
  Max.
          :25142.2
                      Max.
                              :60307.9
sapply(dat, class)
##
       treat
                   age
                             educ
                                      black
                                               hispan
                                                         married nodegree
## "integer" "integer" "integer" "integer" "integer" "integer" "integer"
                  re75
                             re78
## "numeric" "numeric" "numeric"
head(dat)
##
        treat age educ black hispan married nodegree re74 re75
                                                                        re78
## NSW1
            1
               37
                    11
                            1
                                   0
                                           1
                                                     1
                                                          0
                                                               0
                                                                  9930.0460
## NSW2
               22
                     9
                            0
                                   1
                                           0
                                                          0
                                                               0
                                                                  3595.8940
            1
                                                     1
                                   0
## NSW3
               30
                    12
                            1
                                           0
                                                     0
                                                               0 24909.4500
## NSW4
            1
               27
                    11
                            1
                                   0
                                           0
                                                     1
                                                          0
                                                               Ω
                                                                  7506.1460
## NSW5
            1
               33
                     8
                                   0
                                           0
                                                     1
                                                          0
                                                                   289.7899
                            1
## NSW6
               22
                                   0
                                           0
                                                                  4056.4940
            1
                     9
                            1
                                                          0
```

```
# Optimal matching
opt <- matchit(treat ~ age + educ + black + hispan + married, data = dat,
               method = "optimal", ratio = 2)
summary(opt)
##
## Call:
## matchit(formula = treat ~ age + educ + black + hispan + married,
       data = dat, method = "optimal", ratio = 2)
##
##
## Summary of balance for all data:
            Means Treated Means Control SD Control Mean Diff eQQ Med eQQ Mean
                                             0.2305
                                                       0.3801 0.4592
## distance
                   0.5669
                                 0.1868
                                                                        0.3808
                                28.0303
                                            10.7867
                                                      -2.2141 1.0000
                                                                        3.2649
## age
                  25.8162
                                10.2354
                                            2.8552
                                                       0.1105 1.0000
                                                                        0.7027
## educ
                  10.3459
## black
                   0.8432
                                 0.2028
                                            0.4026
                                                       0.6404 1.0000
                                                                        0.6432
## hispan
                   0.0595
                                 0.1422
                                             0.3497
                                                      -0.0827 0.0000
                                                                        0.0811
## married
                   0.1892
                                 0.5128
                                            0.5004
                                                     -0.3236 0.0000
                                                                        0.3243
##
            eQQ Max
## distance 0.6134
## age
            10.0000
## educ
             4.0000
## black
             1.0000
## hispan
             1.0000
## married
             1.0000
##
##
## Summary of balance for matched data:
            Means Treated Means Control SD Control Mean Diff eQQ Med eQQ Mean
## distance
                   0.5669
                                 0.2113
                                            0.2393
                                                       0.3556 0.4386
                                                                        0.3568
                  25.8162
                                           10.8854
                                                      -1.8730 2.0000
                                                                        3.3027
## age
                                27.6892
## educ
                  10.3459
                                10.6568
                                             2.7336
                                                      -0.3108 1.0000
                                                                        0.6649
## black
                   0.8432
                                 0.2351
                                             0.4247
                                                       0.6081 1.0000
                                                                        0.6108
## hispan
                   0.0595
                                 0.1649
                                            0.3716
                                                     -0.1054 0.0000
                                                                        0.1027
## married
                   0.1892
                                 0.4351
                                            0.4964
                                                     -0.2459 0.0000
                                                                        0.2432
##
            eQQ Max
## distance 0.5899
## age
            10.0000
## educ
             4.0000
## black
             1.0000
## hispan
             1.0000
## married
             1.0000
##
## Percent Balance Improvement:
##
            Mean Diff.
                         eQQ Med eQQ Mean eQQ Max
## distance
                6.4506
                          4.5021
                                   6.2939
                                           3.8419
                                  -1.1589
                                           0.0000
## age
               15.4065 -100.0000
                          0.0000
                                   5.3846
## educ
             -181.2393
                                           0.0000
## black
                5.0493
                          0.0000
                                   5.0420
                                           0.0000
                          0.0000 -26.6667
## hispan
              -27.4063
                                           0.0000
                          0.0000 25.0000 0.0000
## married
               24.0043
##
## Sample sizes:
```

```
Control Treated
## All
                 429
                         185
                 370
                         185
## Matched
## Unmatched
                  59
                           0
## Discarded
                   0
                           0
# So all of our treated samples we matched, we just have 59 extra controls that were not matched.
# Let's grab the match data
mat dat <- match.data(opt)</pre>
dim(mat_dat)
## [1] 555 13
summary(mat_dat)
##
                                          educ
                                                          black
        treat
                          age
           :0.0000
                     Min. :16.00
                                     Min.
                                            : 0.00
                                                             :0.0000
   Min.
                                                     Min.
   1st Qu.:0.0000
                     1st Qu.:19.00
                                     1st Qu.: 9.00
                                                     1st Qu.:0.0000
   Median :0.0000
                     Median :25.00
                                     Median :11.00
                                                     Median : 0.0000
##
   Mean
         :0.3333
                     Mean
                           :27.06
                                     Mean :10.55
                                                     Mean
                                                             :0.4378
##
   3rd Qu.:1.0000
                     3rd Qu.:31.50
                                     3rd Qu.:12.00
                                                      3rd Qu.:1.0000
##
   Max.
          :1.0000
                     Max.
                            :55.00
                                     Max.
                                           :18.00
                                                      Max.
                                                           :1.0000
##
       hispan
                        married
                                         nodegree
                                                           re74
##
   Min.
          :0.0000
                     Min.
                            :0.0000
                                      Min. :0.000
                                                      Min. :
                                                                   0.0
##
   1st Qu.:0.0000
                     1st Qu.:0.0000
                                      1st Qu.:0.000
                                                      1st Qu.:
                                                                   0.0
   Median :0.0000
                     Median : 0.0000
                                      Median :1.000
                                                      Median: 748.4
##
   Mean
         :0.1297
                     Mean
                           :0.3532
                                      Mean :0.591
                                                      Mean
                                                            : 4349.2
##
   3rd Qu.:0.0000
                     3rd Qu.:1.0000
                                      3rd Qu.:1.000
                                                       3rd Qu.: 7389.4
##
   Max.
          :1.0000
                     Max.
                            :1.0000
                                      Max.
                                             :1.000
                                                      Max.
                                                             :35040.1
##
        re75
                           re78
                                           distance
                                                              weights
##
   Min. :
                0.0
                      Min.
                           :
                                  0.0
                                        Min.
                                               :0.03231
                                                          Min.
                                                                 : 1
   1st Qu.:
                      1st Qu.: 270.5
                                        1st Qu.:0.07828
##
                0.0
                                                           1st Qu.:1
##
   Median: 469.1
                      Median: 4787.8
                                        Median :0.18597
                                                          Median:1
          : 2075.3
   Mean
                      Mean
                            : 6822.9
                                        Mean
                                              :0.32982
                                                           Mean
                                                                  :1
   3rd Qu.: 3074.6
                                                           3rd Qu.:1
##
                      3rd Qu.:10746.7
                                        3rd Qu.:0.67423
##
   Max.
           :25142.2
                      Max. :60307.9
                                        Max.
                                              :0.75771
                                                          Max.
##
       subclass
## Min. : 1
  1st Qu.: 47
##
## Median: 93
## Mean : 93
##
   3rd Qu.:139
## Max.
          :185
head(mat dat)
                                                                      re78
        treat age educ black hispan married nodegree re74 re75
## NSW1
            1 37
                    11
                           1
                                  0
                                          1
                                                    1
                                                                 9930.0460
## NSW2
            1
               22
                     9
                           0
                                  1
                                          0
                                                         0
                                                              0
                                                                 3595.8940
                                                    1
## NSW3
            1
               30
                    12
                                  0
                                          0
                                                   0
                                                         0
                                                              0 24909.4500
                           1
## NSW4
              27
                                  0
                                          0
                                                         0
                                                              Ω
            1
                    11
                                                    1
                                                                 7506.1460
                           1
## NSW5
              33
                     8
                                          0
                                                   1
                                                                  289.7899
            1
                           1
                                          0
## NSW6
            1
               22
                     9
                           1
                                  0
                                                   1
                                                         0
                                                              0 4056.4940
         distance weights subclass
```

```
## NSW1 0.4938102
                                     1
## NSW2 0.1964210
                                   184
                           1
## NSW3 0.7127660
                           1
                                   12
## NSW4 0.6998489
                                   25
                           1
## NSW5 0.6769612
                           1
                                   37
## NSW6 0.6742263
                                   49
                           1
table(mat_dat$subclass)
##
##
          2
              3
                                7
                                                          13
                                                              14
                                                                       16
                                                                            17
     1
                   4
                       5
                            6
                                     8
                                         9
                                            10
                                                 11
                                                     12
                                                                   15
                                                                                 18
##
     3
          3
                   3
                       3
                            3
                                3
                                     3
                                         3
                                              3
                                                  3
                                                           3
                                                                3
                                                                    3
                                                                         3
                                                                             3
                                                                                  3
                                                       3
##
    19
        20
             21
                 22
                      23
                          24
                               25
                                   26
                                        27
                                             28
                                                 29
                                                      30
                                                          31
                                                               32
                                                                   33
                                                                       34
                                                                            35
                                                                                 36
##
     3
         3
              3
                   3
                       3
                            3
                                3
                                     3
                                         3
                                             3
                                                  3
                                                       3
                                                           3
                                                                3
                                                                    3
                                                                        3
                                                                             3
                                                                                  3
##
    37
                           42
        38
             39
                  40
                      41
                               43
                                   44
                                        45
                                             46
                                                 47
                                                      48
                                                          49
                                                               50
                                                                   51
                                                                       52
                                                                            53
                                                                                 54
##
     3
         3
              3
                  3
                       3
                            3
                                3
                                    3
                                         3
                                             3
                                                  3
                                                       3
                                                           3
                                                                3
                                                                    3
                                                                        3
                                                                             3
                                                                                 3
##
    55
        56
             57
                 58
                      59
                          60
                               61
                                   62
                                        63
                                            64
                                                 65
                                                     66
                                                          67
                                                               68
                                                                   69
                                                                       70
                                                                            71
                                                                                 72
##
     3
         3
              3
                  3
                       3
                           3
                                3
                                    3
                                         3
                                             3
                                                  3
                                                       3
                                                           3
                                                               3
                                                                    3
                                                                        3
                                                                             3
                                                                                 3
##
    73
        74
             75
                 76
                      77
                          78
                               79
                                   80
                                        81
                                            82
                                                 83
                                                     84
                                                          85
                                                              86
                                                                   87
                                                                       88
                                                                            89
                                                                                 90
##
     3
          3
              3
                   3
                       3
                           3
                                3
                                     3
                                         3
                                              3
                                                  3
                                                       3
                                                           3
                                                                3
                                                                    3
                                                                         3
                                                                             3
                                                                                  3
##
    91
        92
             93
                 94
                      95
                           96
                               97
                                   98
                                        99 100 101 102 103 104 105
                                                                      106
                                                                           107
          3
                            3
                                                           3
##
     3
              3
                   3
                       3
                                3
                                     3
                                         3
                                              3
                                                  3
                                                       3
                                                                3
                                                                    3
                                                                         3
                                                                             3
   109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125
##
     3
          3
              3
                   3
                       3
                            3
                                3
                                     3
                                         3
                                              3
                                                  3
                                                           3
                                                                3
                                                                    3
                                                                         3
                                                                                  3
                                                       3
   127 128 129 130 131 132 133 134 135 136
                                               137 138 139 140 141 142 143
          3
                   3
                            3
                                3
                                     3
                                         3
                                                  3
                                                           3
                                                                    3
                                                                         3
                                                                                  3
                       3
                                              3
                                                       3
                                                                3
## 145 146 147 148 149 150 151 152 153 154
                                                    156 157 158
                                                                 159 160 161
                                               155
##
                       3
                            3
                                3
                                     3
                                         3
                                              3
                                                  3
                                                       3
                                                           3
                                                                3
                                                                    3
                                                                         3
  163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180
##
     3
          3
              3
                   3
                       3
                            3
                                3
                                     3
                                         3
                                              3
                                                  3
                                                       3
                                                           3
                                                                3
                                                                    3
                                                                         3
## 181 182 183 184 185
          3
              3
                   3
                       3
mat_dat <- mat_dat[order(mat_dat$subclass),]</pre>
head(mat dat)
##
            treat age educ black hispan married nodegree
                                                                     re74
                                                                                re75
## NSW1
                1
                    37
                         11
                                 1
                                         0
                                                  1
                                                                   0.0000
                                                                               0.000
## PSID10
                0
                    39
                         10
                                 0
                                         0
                                                            1 16767.4100 12022.020
                                                  1
## PSID115
                0
                    20
                         11
                                 0
                                         0
                                                  1
                                                               5822.9410
                                                                            3532.306
                                                            1
## NSW107
                1
                    27
                         13
                                 1
                                         0
                                                  0
                                                            0
                                                                   0.0000
                                                                               0.000
## PSID90
                0
                    29
                                 0
                                         0
                                                                 713.1731
                                                                            4542.048
                         10
                                                  1
                                                            1
## PSID163
                    48
                                                            1 16050.3100
                                                                            2116.161
                0
                          8
                                 0
                                         0
                                                  1
##
                 re78
                         distance weights subclass
             9930.046 0.49381018
## NSW1
                                          1
## PSID10
             4433.180 0.03835856
                                          1
                                                    1
## PSID115 11075.560 0.03637358
                                                    1
                                          1
                                                    2
## NSW107
            34099.280 0.71891686
                                          1
                                                    2
## PSID90
             7781.708 0.03643670
## PSID163 11600.150 0.03675183
                                          1
mat_dat$subclass <- as.factor(mat_dat$subclass)</pre>
mat_mod <- lm(re78 ~ treat + nodegree + re74 + re75 + subclass, data = mat_dat)</pre>
summary(mat_mod)
```

```
##
## Call:
## lm(formula = re78 ~ treat + nodegree + re74 + re75 + subclass,
##
       data = mat_dat)
##
## Residuals:
      Min
              10 Median
                             30
                                   Max
## -18416 -3756
                   -161
                           3063
                                 35727
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                7.165e+03
## (Intercept)
                           4.211e+03
                                         1.701
                                                 0.0897
## treat
                8.967e+02
                            6.756e+02
                                         1.327
                                                 0.1852
                            8.647e+02
## nodegree
               -2.109e+03
                                        -2.439
                                                 0.0152 *
## re74
                3.394e-01
                            7.155e-02
                                         4.744 3.01e-06 ***
## re75
                1.097e-01
                            1.433e-01
                                         0.765
                                                 0.4446
## subclass2
                9.629e+03
                            5.764e+03
                                                 0.0957 .
                                        1.671
## subclass3
               -4.778e+03
                            5.779e+03
                                        -0.827
                                                 0.4089
## subclass4
                1.464e+03
                            5.819e+03
                                        0.252
                                                 0.8015
## subclass5
               -1.718e+03
                            5.773e+03
                                        -0.298
                                                 0.7662
## subclass6
               -4.728e+03
                            5.776e+03
                                       -0.819
                                                 0.4135
## subclass7
                            5.783e+03
                                                 0.4836
                4.055e+03
                                        0.701
## subclass8
               -1.946e+03
                            5.778e+03
                                        -0.337
                                                 0.7365
## subclass9
                6.295e+02
                            5.774e+03
                                        0.109
                                                 0.9132
## subclass10
                4.988e+03
                            5.778e+03
                                         0.863
                                                 0.3885
## subclass11
                2.116e+03
                            5.814e+03
                                         0.364
                                                 0.7161
                                                 0.4237
## subclass12
                4.618e+03
                            5.767e+03
                                         0.801
## subclass13
                6.097e+03
                            5.747e+03
                                        1.061
                                                 0.2894
## subclass14
               -5.052e+03
                            5.778e+03
                                       -0.874
                                                 0.3825
## subclass15
               -6.292e+03
                            5.756e+03
                                       -1.093
                                                 0.2750
## subclass16
               -2.122e+03
                            5.779e+03
                                        -0.367
                                                 0.7137
## subclass17
                6.198e+02
                            5.777e+03
                                        0.107
                                                 0.9146
## subclass18
               -3.477e+03
                            5.823e+03
                                        -0.597
                                                 0.5508
## subclass19
               -3.044e+03
                            5.847e+03
                                        -0.521
                                                 0.6029
## subclass20
               -1.796e+01
                            5.837e+03
                                        -0.003
                                                 0.9975
## subclass21
               -1.246e+03
                            5.773e+03
                                       -0.216
                                                 0.8292
## subclass22
               -1.226e+03
                            5.781e+03
                                        -0.212
                                                 0.8321
## subclass23
                5.629e+03
                            5.784e+03
                                                 0.3311
                                        0.973
               -1.024e+03
                            5.771e+03
                                                 0.8592
## subclass24
                                        -0.178
## subclass25
                1.781e+03
                            5.759e+03
                                        0.309
                                                 0.7573
               -6.864e+03
## subclass26
                            5.803e+03
                                        -1.183
                                                 0.2376
## subclass27
                1.123e+03
                            5.821e+03
                                                 0.8472
                                        0.193
## subclass28
                6.525e+03
                            5.760e+03
                                        1.133
                                                 0.2580
## subclass29
                3.813e+03
                            5.763e+03
                                        0.662
                                                 0.5086
## subclass30
                6.043e+02
                            5.773e+03
                                        0.105
                                                 0.9167
## subclass31
               -2.378e+03
                            5.781e+03
                                        -0.411
                                                 0.6810
## subclass32
               -4.832e+03
                            5.798e+03
                                        -0.833
                                                 0.4052
## subclass33
                2.488e+03
                            5.768e+03
                                         0.431
                                                 0.6665
## subclass34
               -3.622e+02
                            5.771e+03
                                        -0.063
                                                 0.9500
## subclass35
               -3.577e+03
                            5.764e+03
                                        -0.621
                                                 0.5353
## subclass36
               -8.932e+01
                            5.764e+03
                                       -0.015
                                                 0.9876
## subclass37
               -4.984e+03
                            5.777e+03
                                       -0.863
                                                 0.3888
## subclass38
               -1.677e+03
                            5.836e+03
                                       -0.287
                                                 0.7741
## subclass39
               -3.518e+03 5.777e+03
                                       -0.609
                                                 0.5430
```

```
3.936e+03
                            5.802e+03
                                                  0.4980
## subclass40
                                          0.678
                                                  0.7999
## subclass41
                -1.465e+03
                             5.774e+03
                                        -0.254
## subclass42
                 3.453e+02
                             5.795e+03
                                          0.060
                                                  0.9525
## subclass43
                 8.396e+02
                             5.766e+03
                                          0.146
                                                  0.8843
##
   subclass44
                 1.789e+03
                             5.753e+03
                                          0.311
                                                  0.7560
   subclass45
                -1.817e+03
##
                             5.773e+03
                                         -0.315
                                                  0.7531
  subclass46
                -3.698e+03
                             5.791e+03
                                         -0.639
                                                  0.5235
## subclass47
                 2.227e+03
                             5.787e+03
                                          0.385
                                                  0.7006
   subclass48
                -3.725e+03
                             5.815e+03
                                         -0.641
                                                  0.5221
##
##
   subclass49
                 2.473e+03
                             5.852e+03
                                          0.423
                                                  0.6728
  subclass50
                -3.501e+02
                             5.779e+03
                                         -0.061
                                                  0.9517
   subclass51
                -3.843e+03
                             5.790e+03
                                         -0.664
                                                  0.5073
##
   subclass52
                -5.409e+03
                             5.787e+03
                                        -0.935
                                                  0.3505
   subclass53
                -1.032e+01
                             5.765e+03
                                         -0.002
                                                  0.9986
   subclass54
                -3.574e+03
                             5.784e+03
                                         -0.618
                                                  0.5371
   subclass55
                -5.182e+03
                             5.781e+03
                                         -0.896
                                                  0.3706
##
                 6.128e+01
                             5.777e+03
                                                  0.9915
##
   subclass56
                                          0.011
                -2.452e+03
                             5.762e+03
                                                  0.6707
   subclass57
                                         -0.426
                 1.037e+03
                             5.762e+03
                                                  0.8572
## subclass58
                                          0.180
##
   subclass59
                 9.964e+02
                             5.779e+03
                                          0.172
                                                  0.8632
## subclass60
                 2.307e+03
                             5.778e+03
                                          0.399
                                                  0.6899
## subclass61
                 3.317e+03
                             5.776e+03
                                          0.574
                                                  0.5661
                -2.490e+02
                             5.810e+03
                                         -0.043
## subclass62
                                                  0.9658
##
  subclass63
                 1.689e+03
                             5.792e+03
                                          0.292
                                                  0.7707
## subclass64
                -1.586e+03
                             5.809e+03
                                         -0.273
                                                  0.7850
  subclass65
                -5.398e+03
                             5.776e+03
                                         -0.934
                                                  0.3507
   subclass66
                -2.368e+03
                             5.794e+03
                                         -0.409
                                                  0.6829
   subclass67
                 2.419e+03
                             5.812e+03
                                         0.416
                                                  0.6775
##
   subclass68
                 7.431e+02
                             5.779e+03
                                          0.129
                                                  0.8978
                             5.778e+03
                                                  0.5584
   subclass69
                 3.385e+03
                                          0.586
   subclass70
                -2.438e+03
                             5.782e+03
                                         -0.422
                                                  0.6735
##
   subclass71
                -3.136e+03
                             5.772e+03
                                         -0.543
                                                  0.5872
                 8.610e+03
                             5.791e+03
                                                  0.1379
   subclass72
                                          1.487
                -7.638e+02
                             5.805e+03
                                                  0.8954
##
   subclass73
                                         -0.132
##
   subclass74
                -2.110e+03
                             5.777e+03
                                         -0.365
                                                  0.7151
##
   subclass75
                 1.760e+02
                             5.799e+03
                                         0.030
                                                  0.9758
  subclass76
                -8.214e+03
                             5.776e+03
                                         -1.422
                                                  0.1559
                -4.896e+03
## subclass77
                             5.844e+03
                                         -0.838
                                                  0.4028
## subclass78
                -7.262e+03
                             5.797e+03
                                        -1.253
                                                  0.2111
## subclass79
                -8.263e+03
                             5.764e+03
                                         -1.434
                                                  0.1526
  subclass80
                -6.157e+03
                             5.800e+03
                                         -1.062
                                                  0.2891
##
  subclass81
                -1.760e+03
                             5.763e+03
                                         -0.305
                                                  0.7603
##
   subclass82
                 2.454e+03
                             5.812e+03
                                         0.422
                                                  0.6731
##
   subclass83
                 5.169e+03
                             5.767e+03
                                         0.896
                                                  0.3706
   subclass84
                -5.915e+03
                             5.829e+03
                                         -1.015
                                                  0.3109
   subclass85
                -6.994e+03
                             5.847e+03
                                         -1.196
                                                  0.2324
                -3.056e+03
                                         -0.529
##
   subclass86
                             5.780e+03
                                                  0.5974
##
   subclass87
                 3.275e+03
                             5.776e+03
                                          0.567
                                                  0.5710
   subclass88
                -6.287e+03
                             5.771e+03
                                         -1.089
                                                  0.2767
   subclass89
                 2.138e+03
                             5.768e+03
                                         0.371
                                                  0.7110
##
                                                  0.7565
##
   subclass90
                -1.790e+03
                             5.770e+03
                                        -0.310
   subclass91
                -3.734e+03
                             5.777e+03
                                         -0.646
                                                  0.5184
## subclass92
                -5.305e+03
                             5.800e+03
                                         -0.915
                                                  0.3609
## subclass93
                 7.002e+02 5.846e+03
                                          0.120
                                                  0.9047
```

```
## subclass94
                4.669e+02 5.796e+03
                                        0.081
                                                 0.9358
                                                 0.5990
                                       -0.526
## subclass95
               -3.045e+03
                           5.786e+03
               -6.264e+03
## subclass96
                            5.784e+03
                                       -1.083
                                                 0.2795
               -4.953e+03
## subclass97
                            5.799e+03
                                       -0.854
                                                 0.3936
## subclass98
               -8.630e+02
                            5.841e+03
                                       -0.148
                                                 0.8826
## subclass99
                2.509e+02
                            5.839e+03
                                        0.043
                                                 0.9657
## subclass100 5.892e+03
                            5.791e+03
                                        1.017
                                                 0.3096
## subclass101 -1.109e+03
                            5.764e+03
                                       -0.192
                                                 0.8475
  subclass102 -1.336e+03
                            5.787e+03
                                       -0.231
                                                 0.8175
## subclass103 5.930e+03
                            5.781e+03
                                        1.026
                                                 0.3056
## subclass104 -4.930e+03
                            5.797e+03
                                       -0.850
                                                 0.3957
## subclass105 2.022e+03
                            5.761e+03
                                        0.351
                                                 0.7258
  subclass106 3.425e+03
                                                 0.5527
                            5.764e+03
                                        0.594
                            5.769e+03
  subclass107 8.577e+02
                                        0.149
                                                 0.8819
## subclass108 2.583e+03
                            5.812e+03
                                        0.444
                                                 0.6570
   subclass109 5.060e+03
                            5.788e+03
                                        0.874
                                                 0.3826
  subclass110 -2.995e+03
                            5.796e+03
                                                 0.6057
                                       -0.517
  subclass111 -4.460e+03
                            5.782e+03
                                                 0.4409
                                       -0.771
## subclass112 -8.593e+03
                            5.815e+03
                                                 0.1403
                                       -1.478
   subclass113 -3.481e+03
                            5.773e+03
                                       -0.603
                                                 0.5470
## subclass114 -7.742e+03
                            5.830e+03
                                       -1.328
                                                 0.1850
## subclass115 -6.478e+03
                            5.811e+03
                                       -1.115
                                                 0.2657
## subclass116 -7.127e+03
                            5.761e+03
                                       -1.237
                                                 0.2168
## subclass117 1.507e+03
                            5.768e+03
                                        0.261
                                                 0.7940
## subclass118 1.849e+04
                            5.779e+03
                                        3.199
                                                 0.0015 **
## subclass119 -5.812e+03
                            5.774e+03
                                       -1.007
                                                 0.3148
## subclass120 -2.875e+03
                            5.771e+03
                                       -0.498
                                                 0.6186
## subclass121 2.827e+02
                            5.782e+03
                                        0.049
                                                 0.9610
## subclass122 -4.600e+03
                            5.750e+03
                                       -0.800
                                                 0.4243
                                       -0.099
## subclass123 -5.709e+02
                            5.767e+03
                                                 0.9212
## subclass124 1.222e+03
                            5.773e+03
                                        0.212
                                                 0.8325
## subclass125 -4.504e+03
                            5.786e+03
                                       -0.778
                                                 0.4369
## subclass126 -5.240e+03
                            5.824e+03
                                       -0.900
                                                 0.3689
## subclass127 5.048e+03
                            5.765e+03
                                                 0.3819
                                        0.876
   subclass128 3.224e+03
                            5.770e+03
                                                 0.5766
                                        0.559
## subclass129 -5.348e+03
                            5.763e+03
                                       -0.928
                                                 0.3540
## subclass130 -4.894e+03
                            5.778e+03
                                       -0.847
                                                 0.3975
## subclass131 1.268e+03
                            5.772e+03
                                        0.220
                                                 0.8262
## subclass132 -5.194e+03
                            5.769e+03
                                       -0.900
                                                 0.3685
## subclass133 -1.469e+03
                            5.788e+03
                                       -0.254
                                                 0.7998
## subclass134 -3.418e+03
                            5.806e+03
                                       -0.589
                                                 0.5564
## subclass135 1.136e+03
                            5.751e+03
                                        0.198
                                                 0.8435
## subclass136 4.410e+03
                            5.764e+03
                                        0.765
                                                 0.4447
## subclass137 -8.340e+02
                            5.758e+03
                                       -0.145
                                                 0.8849
## subclass138 2.377e+03
                            5.754e+03
                                        0.413
                                                 0.6798
## subclass139 -5.472e+03
                            5.770e+03
                                       -0.948
                                                 0.3436
## subclass140 4.982e+03
                            5.762e+03
                                        0.865
                                                 0.3878
## subclass141 -5.543e+03
                            5.754e+03
                                       -0.963
                                                 0.3360
## subclass142 -2.850e+03
                            5.774e+03
                                       -0.494
                                                 0.6219
## subclass143 -5.494e+03
                            5.815e+03
                                       -0.945
                                                 0.3454
## subclass144 -2.523e+03
                            5.776e+03
                                       -0.437
                                                 0.6626
## subclass145 -1.512e+03
                            5.797e+03
                                       -0.261
                                                 0.7944
## subclass146 -6.996e+03
                           5.791e+03
                                       -1.208
                                                 0.2278
## subclass147 -4.791e+02 5.812e+03 -0.082
                                                 0.9343
```

```
## subclass148 -5.143e+03 5.762e+03 -0.893
                                              0.3727
## subclass149 4.578e+03 5.830e+03
                                      0.785
                                             0.4329
## subclass150 -1.044e+03 5.791e+03 -0.180
                                              0.8571
## subclass151 -4.558e+02 5.788e+03
                                             0.9373
                                    -0.079
## subclass152 -5.012e+03 5.771e+03
                                    -0.869
                                             0.3857
## subclass153 -2.152e+03 5.782e+03 -0.372
                                             0.7100
## subclass154 -8.478e+02 5.759e+03 -0.147
                                             0.8831
## subclass155 2.005e+03 5.787e+03
                                     0.347
                                             0.7291
## subclass156 -6.574e+03 5.776e+03
                                    -1.138
                                             0.2558
## subclass157 -5.476e+03 5.767e+03
                                    -0.950
                                             0.3429
## subclass158 -3.840e+03
                          5.769e+03
                                    -0.666
                                             0.5061
## subclass159 2.488e+03
                          5.765e+03
                                     0.432
                                             0.6663
## subclass160 -8.627e+02 5.786e+03 -0.149
                                             0.8816
## subclass161 -6.401e+02 5.746e+03 -0.111
                                             0.9114
## subclass162 -1.136e+03 5.796e+03 -0.196
                                             0.8447
## subclass163 -2.657e+03 5.845e+03
                                     -0.455
                                              0.6497
## subclass164 -3.285e+02 5.747e+03
                                    -0.057
                                             0.9544
## subclass165 -1.970e+03 5.757e+03
                                    -0.342
                                              0.7324
## subclass166 5.323e+03 5.753e+03
                                     0.925
                                             0.3554
## subclass167 -9.947e+03 5.813e+03
                                    -1.711
                                             0.0879 .
## subclass168 -6.623e+03 5.789e+03 -1.144
                                             0.2534
## subclass169 1.868e+03 5.759e+03
                                             0.7459
                                     0.324
## subclass170 -8.576e+03 5.791e+03 -1.481
                                             0.1395
## subclass171 -1.547e+03 5.771e+03 -0.268
                                             0.7888
## subclass172 1.796e+02 5.827e+03
                                      0.031
                                             0.9754
## subclass173 -3.214e+03 5.760e+03 -0.558
                                             0.5772
## subclass174 3.201e+02
                                             0.9558
                          5.776e+03
                                     0.055
## subclass175 -2.422e+03
                          5.775e+03 -0.419
                                             0.6752
## subclass176 -1.957e+02 5.763e+03
                                    -0.034
                                             0.9729
## subclass177 -2.225e+03 5.747e+03 -0.387
                                             0.6989
## subclass178 -3.365e+03 5.809e+03
                                     -0.579
                                             0.5628
## subclass179 4.838e+03 5.805e+03
                                      0.833
                                             0.4052
## subclass180 2.577e+02 5.747e+03
                                      0.045
                                              0.9643
## subclass181 -5.239e+02 5.765e+03
                                    -0.091
                                             0.9276
## subclass182 -9.141e+02 5.889e+03
                                     -0.155
                                             0.8767
## subclass183 -3.307e+03 5.828e+03
                                    -0.568
                                             0.5707
## subclass184 3.570e+02 5.762e+03
                                      0.062
                                              0.9506
## subclass185 1.993e+03 5.815e+03
                                      0.343
                                              0.7320
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7037 on 366 degrees of freedom
## Multiple R-squared: 0.4213, Adjusted R-squared: 0.1241
## F-statistic: 1.418 on 188 and 366 DF, p-value: 0.002504
# R2 is low but still significant, nodegree is significant, and re74 is very significant.
# Now lets do anova
an <- anova(mat_mod, test = "chisq")
## Analysis of Variance Table
##
## Response: re78
```

```
Df
                   Sum Sq
                            Mean Sq F value
                                             Pr(>F)
           1 6.2274e+07
                           62273832 1.2577 0.2628171
## treat
## nodegree 1 6.5809e+08 658086062 13.2912 0.0003053 ***
## re74
            1 3.6727e+09 3672707751 74.1766 < 2.2e-16 ***
             1 9.6719e+07 96718720 1.9534 0.1630675
## re75
## subclass 184 8.7057e+09 47313402 0.9556 0.6331507
## Residuals 366 1.8122e+10 49513010
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
# We can see that subclass is not significant and that nodegree and re74 are both significant.
```