Realizations of non-ergodic series

