

Berehalako integralen adierazpen konposatuak.

1.

$$\int u^r du = \frac{u^{r+1}}{r+1} + K = \cos^6 x \quad u = \cos x \quad du = -\sin x dx$$

a) $\int \cos^5 x (-\sin x) dx = \int (\cos x)^4 (-\sin x) dx =$
 $= \frac{\cos^6 x}{6} + K.$

b) $\int \sqrt[3]{\cos^2 x} (-\sin x) dx = \int (\cos x)^{2/3} (-\sin x) dx =$
 $\frac{(\cos x)^{2/3+1}}{2/3+1} + K = \frac{\sqrt[3]{\cos^5 x}}{5/3} = \frac{3}{5} \sqrt[3]{\cos^5 x} + K$

c) $\int e^{\cos x} \sin x dx = -e^{\cos x} + K$

d) $\int e^{x^3+x^2} (3x^2+2x) dx = e^{x^3+x^2} + K$

e) $\int \operatorname{tg} x^2 \cdot 2x dx = \int \frac{\sin x^2}{\cos x^2} 2x dx =$
 $-\ln |\cos x^2| + K$

f) $\int \frac{3x^2}{1+x^6} dx = \int \frac{3x^2}{1+(x^3)^2} dx = \operatorname{arctg} x^3 + K$

g) $\int \frac{-e^{-x}}{\sqrt{1-e^{-2x}}} dx = \int \frac{-e^{-x}}{\sqrt{1-(e^{-x})^2}} = \operatorname{arcsin}(e^{-x}) + K$

h) ~~$\int \frac{-e^{-x}}{\sqrt{1-e^{-2x}}} dx$~~ $\int \ln(x^2+1) \cdot 2x dx =$
 $(x^2+1)\ln(x^2+1) - (x^2+1) + K$ $u = x^2+1$
 $du = 2x dx$

i) $\int \sqrt[3]{(x^4+5x)^2} (4x^3+5) dx = \frac{3}{5} \sqrt[3]{(x^4+5x)^5} + K$
 $u = x^4+5x \quad du = (4x^3+5) dx \quad \int u^{2/3} du = \frac{3}{5} u^{5/3} = \frac{3}{5} \sqrt[3]{(x^4+5x)^5} + K$