

①

DERİBANAK.

8. Ortaokula.

$$1.) f(x) = 2x + 1 \rightarrow f'(x) = \boxed{2}$$

$$2.) f(x) = \frac{3x - 2}{4} = \frac{3x}{4} - \frac{2}{4} = \frac{3x}{4} - \frac{1}{2} \rightarrow f'(x) = \boxed{\frac{3}{4}}$$

$$3.) f(x) = \frac{3}{4} \rightarrow f'(x) = \boxed{0}$$

$$4.) f(x) = \frac{x}{2} + 3 = \frac{1}{2}x + 3 \rightarrow f'(x) = \boxed{\frac{1}{2}}$$

$$5.) f(x) = x^3 - 3x^2 + 2 \rightarrow f'(x) = \boxed{3x^2 - 6x}$$

$$6.) f(x) = \frac{3x^5}{5} - \frac{4x^3}{3} + 5 = \frac{3}{5}x^5 - \frac{4}{3}x^3 + 5 \rightarrow f'(x) = \frac{3}{5}x^4 - \frac{4}{3}x^2 = \boxed{3x^4 - \frac{4}{3}}$$

$$7.) f(x) = \frac{4\pi - 2}{3} \rightarrow f'(x) = \boxed{0}$$

$$8.) f(x) = \frac{4}{3}(x^2 - \frac{3}{4}x + 2) \rightarrow f'(x) = \frac{4}{3}(2x - \frac{3}{4}) = \boxed{\frac{8x}{3} - 1}$$

$$9.) \frac{x^2}{5} - \frac{x}{4} + \sqrt{5} \rightarrow f'(x) = \boxed{\frac{2x}{5} - \frac{1}{4}}$$

$$10.) \frac{x}{7} - \sqrt{7}x = \frac{1}{7}x - \sqrt{7} \cdot x^{1/2} \rightarrow f'(x) = \frac{1}{7} - \frac{\sqrt{7}}{2}x^{\frac{1}{2}-1} = \frac{1}{7} - \frac{\sqrt{7}x}{2} \cdot \frac{\sqrt{7}}{\sqrt{7}} \\ = \frac{1}{7} - \frac{\sqrt{7}x}{2x} = \frac{2x - 7\sqrt{7}x}{7x}$$

$$11.) f(x) = \frac{1}{x} = x^{-1} \rightarrow f'(x) = -1 \cdot x^{-2} = \boxed{-\frac{1}{x^2}}$$

$$12.) f(x) = \frac{3}{x^2} = 3x^{-2} \rightarrow f'(x) = 3(-2)x^{-3} = \boxed{-\frac{6}{x^3}}$$

$$13.) f(x) = \frac{5}{3x^3} = \frac{5}{3} \cdot x^{-3} \rightarrow f'(x) = \frac{5(-3)}{3}x^{-4} = \boxed{-\frac{5}{x^4}}$$

$$14.) f(x) = \sqrt[3]{x^4} = x^{4/3} \rightarrow f'(x) = \frac{4}{3}x^{\frac{4}{3}-1} = \frac{4}{3}x^{\frac{11}{3}} = \boxed{\frac{4\sqrt[3]{x}}{3}}$$

$$15.) f(x) = \frac{\sqrt{3x}}{x^2} = \frac{\sqrt{3} \cdot \sqrt{x}}{x^2} \rightarrow f'(x) = \sqrt{3} \left(\frac{3}{2} \right) \cdot x^{-3/2-1} \\ = \sqrt{3}x^{1/2-2} = \sqrt{3} \cdot x^{-3/2}$$

$$= -\frac{3\sqrt{3}}{2}x^{-5/2} = \frac{-3\sqrt{3}}{2\sqrt{x}} = \frac{-3\sqrt{3}}{2x^{2/2}} \cdot \frac{\sqrt{x}}{\sqrt{x}} = \boxed{-\frac{3\sqrt{3}x}{2x^3}}$$

$$16) f(x) = \frac{3\sqrt{x^3}}{2x^4} = \frac{3}{2} x^{\frac{3}{2}-4} = \frac{3}{2} x^{-\frac{5}{2}} \rightarrow f'(x) = \frac{3}{2} \left(-\frac{5}{2}\right) x^{-\frac{5}{2}-1} =$$

$$= -\frac{15}{4} x^{-\frac{7}{2}} = -\frac{15}{4\sqrt{x^7}} = \frac{-15}{4x^3\sqrt{x}} \cdot \frac{\sqrt{x}}{\sqrt{x}}$$

$$= \boxed{\frac{-15\sqrt{x}}{4x^4}}$$

$$17) f(x) = \frac{2}{x} + \frac{x}{2} = 2x^{-1} + \frac{1}{2}x \rightarrow f'(x) = 2 \cdot (-1)x^{-2} + \frac{1}{2} = \boxed{\frac{-2}{x^2} + \frac{1}{2}}$$

$$18) f(x) = \frac{\sqrt[3]{x^2}}{3} - \frac{x}{3} + \sqrt{5} = \frac{1}{3} x^{\frac{2}{3}} - \frac{1}{3}x + \sqrt{5}$$

$$f'(x) = \frac{1}{3} \cdot \frac{2}{3} x^{\frac{2}{3}-1} - \frac{1}{3} = \frac{2}{9} x^{-\frac{1}{3}} - \frac{1}{3} = \frac{2}{9\sqrt[3]{x}} \frac{\sqrt[3]{x^2}}{\sqrt[3]{x}} - \frac{1}{3} =$$

$$= \frac{2\sqrt[3]{x^2}}{9x} - \frac{1}{3} = \boxed{\frac{2\sqrt[3]{x^2} - 3x}{9x}}$$

$$19) f(x) = \sqrt[4]{\frac{1}{x^3}} = x^{-\frac{3}{4}} \rightarrow f'(x) = -\frac{3}{4}x^{-\frac{7}{4}} =$$

$$= -\frac{3}{4\sqrt[4]{x^7}} = \frac{-3}{4x\sqrt[4]{x^3}} \cdot \frac{\sqrt[4]{x}}{\sqrt[4]{x}} = \boxed{\frac{-3\sqrt[4]{x}}{4x^2}}$$

$$20) f(x) = \sqrt{\frac{3}{x^5}} = \sqrt{3} \cdot x^{-\frac{5}{2}} \rightarrow f'(x) = \sqrt{3} \left(-\frac{5}{2}\right) x^{-\frac{5}{2}-1} =$$

$$= -\frac{5\sqrt{3}}{2\sqrt[3]{x}} \cdot \frac{\sqrt{x}}{\sqrt{x}} = \boxed{-\frac{5\sqrt{3}x}{2x^4}}$$

$$21) f(x) = \frac{2\sqrt{x}}{x} - \frac{3}{x^2} + \frac{1}{x} = 2x^{\frac{1}{2}-1} - 3x^{-2} + x^{-1} = 2x^{-\frac{1}{2}} - 3x^{-2} + x^{-1}$$

$$f'(x) = 2 \left(-\frac{1}{2}\right) x^{-\frac{1}{2}-1} - 3 \cdot (-2) \cdot x^{-2-1} + (-1) \cdot x^{-1-1} =$$

$$= -x^{-\frac{3}{2}} + 6x^{-3} - x^{-2} = -\frac{1}{\sqrt{x^3}} + \frac{6}{x^3} - \frac{1}{x^2} \quad \text{---}$$

$$= -\frac{1 \cdot \sqrt{x}}{x\sqrt{x}} + \frac{6}{x^3} - \frac{1}{x^2} = \boxed{-\frac{\sqrt{x}}{x^2} + \frac{6}{x^3} - \frac{1}{x^2}}$$

$$22.) f(x) = x - \frac{3\sqrt{5}}{4} + \frac{1}{x^2} = x - \frac{3\sqrt{5}}{4} + x^{-2}$$

$$f'(x) = 1 - 0 + (-2)x^{-2-1} = 1 - 2x^{-3} = \boxed{1 - \frac{2}{x^3}}$$

$$23.) f(x) = \frac{x^2}{3} - \frac{3}{x^2} + \frac{3\sqrt{5}}{2} = \frac{1}{3}x^2 - 3 \cdot x^{-2} + \frac{3\sqrt{5}}{2}$$

$$f'(x) = \frac{2}{3}x - 3(-2)x^{-3} + 0 = \boxed{\frac{2x}{3} + \frac{6}{x^3}}$$

$$24.) f(x) = \frac{x^3}{3} - 4\sqrt{x} - \frac{2}{x^3} - \underbrace{x^2\sqrt{x}}_{3/2} = \frac{1}{3}x^3 - 4x^{1/2} - 2x^{-3} - x^{2+1/2}$$

$$f'(x) = \cancel{\frac{1}{3}} \cancel{3} \cdot x^2 - \frac{4}{2}x^{\cancel{\frac{1}{2}}-1} - 2(5)\cancel{x} - \frac{5}{2}x^{\cancel{\frac{5}{2}}-1} = \boxed{x^2 - \frac{2}{\sqrt{x}} + \frac{6}{x^4} - \frac{5}{2}\sqrt{x^3}}$$

$$25.) f(x) = \frac{x^2 - 3x + 1}{x} = \frac{x^2}{x} - \frac{3x}{x} + \frac{1}{x} = x - 3 + \underbrace{\frac{1}{x}}_{x^{-1}}$$

$$f'(x) = 1 - 0 + (-1)x^{-1-1} = 1 - x^{-2} = 1 - \frac{1}{x^2} = \boxed{\frac{x^2 - 1}{x^2}}$$

10. omialdea

$$1.) f(x) = 3\sin x - 2\cos x \rightarrow f'(x) = 3\cos x + 2\sin x$$

$$2.) f(x) = 4\tan x + e^x \rightarrow f'(x) = \frac{4}{\cos^2 x} + e^x$$

$$3.) f(x) = x \cdot \ln x. \quad \text{Bidurkitia} \rightarrow f'(x) = \frac{f'g + fg'}{1 \cdot \ln x + x \cdot \frac{1}{x}} = \boxed{\ln x + 1}$$

$$4.) f(x) = x \cdot e^x \rightarrow f'(x) = 1 \cdot e^x + x \cdot e^x = \boxed{e^x(1+x)}$$

$$5.) f(x) = (x^2 + 1) \cdot \sin x \rightarrow f'(x) = 2x \cdot \sin x + (x^2 + 1) \cdot \cos x$$

$$6.) f(x) = 2^x \cdot \tan x \rightarrow f'(x) = 2^x \cdot \ln 2 \cdot \tan x + \frac{2^x}{\cos^2 x},$$

$$7.) f(x) = x^2 - \underbrace{\frac{x}{3} e^x}_{\text{BIDERK.}} \rightarrow f'(x) = 2x - \left(\frac{1}{3} e^x + \frac{x}{3} e^x \right)$$

$$\boxed{f'(x) = 2x - \frac{1}{3} e^x - \frac{x}{3} e^x}$$

$$8.) f(x) = \underbrace{(x^3 - 2x + 1)}_f \cdot \underbrace{\cos x}_g \rightarrow f'(x) = (3x^2 - 2) \cdot \cos x + (x^3 - 2x + 1) \cdot \sin x.$$

$$9.) f(x) = 3^x + \ln x - \frac{1}{x}^{x^{-1}}$$

$$f'(x) = 3^x \ln 3 + \frac{1}{x} - (-1) x^{-2} = \boxed{3^x \ln 3 + \frac{1}{x} + \frac{1}{x^2}}$$

$$10.) f(x) = 2^x + \log_2 x$$

$$f'(x) = \boxed{2^x \cdot \ln 2 + \frac{1}{x \ln 2}}$$

$$11.) f(x) = \underbrace{x^2 \cdot e^x}_f + \underbrace{2x \cdot \ln x}_g$$

$$f'(x) = \underbrace{2x \cdot e^x}_f + \underbrace{x^2 \cdot e^x}_g + \underbrace{2 \cdot \ln x}_g + \underbrace{2x \cdot \frac{1}{x}}_g = \\ = \boxed{2x \cdot e^x + x^2 \cdot e^x + 2 \ln x + 2}$$

$$12.) f(x) = \sqrt{x} \cdot \sin x - \log_3 5 = x^{\frac{1}{12}} \cdot \sin x - \log_3 5.$$

$$f'(x) = \frac{1}{2} x^{-\frac{11}{12}} \sin x + \sqrt{x} \cdot \cos x - 0$$

$$f' g + f g'$$

$$= \frac{1}{2\sqrt{x}} \sin x + \sqrt{x} \cdot \cos x = \frac{\sin x + 2\sqrt{x} \cdot \cos x}{2\sqrt{x}}$$

$$= \boxed{\frac{\sin x + 2x \cos x}{2\sqrt{x}}}$$

(5)

ZATIVKETA

$$13) f(x) = \frac{4x}{x+1} = \frac{F(x)}{G(x)} \quad f'(x) = \frac{F'G - FG'}{G^2}$$

$$f'(x) = \frac{4 \cdot (x+1) - 4x \cdot 1}{(x+1)^2} = \frac{4x + 4 - 4x}{(x+1)^2} = \frac{4}{(x+1)^2}$$

$$14) f(x) = \frac{x^2 - 1}{2x+2} \rightarrow f'(x) = \frac{2x(2x+2) - (x^2 - 1) \cdot 2}{(2x+2)^2} \dots$$

Erläutern! Faktor 2 ausrechnen & duplifizieren.

$$f(x) = \frac{x^2 - 1}{2x+2} = \frac{(x+1)(x-1)}{2(x+1)} = \frac{x-1}{2} = \frac{1}{2}(x-1)$$

$$\boxed{f'(x) = \frac{1}{2}}$$

$$15) f(x) = \frac{x+1}{x-2} \rightarrow f'(x) = \frac{1 \cdot (x-2) - (x+1) \cdot 1}{(x-2)^2} = \frac{x-2-x-1}{(x-2)^2}$$

$$\boxed{f'(x) = \frac{-3}{(x-2)^2}}$$

$$16) f(x) = \frac{\ln x}{x} \rightarrow f'(x) = \frac{\frac{1}{x} \cdot x - \ln x \cdot 1}{x^2} = \boxed{\frac{1-\ln x}{x^2}}$$

$$17) f(x) = \frac{e^x + e^{-x}}{2} = \frac{1}{2}(e^x + e^{-x}) \rightarrow \text{Kataren erreichen.}$$

$$f'(x) = \frac{1}{2}(e^x + (-1) \cdot e^{-x})$$

$$18) f(x) = \frac{1}{x^4+1} \rightarrow f'(x) = \frac{0 \cdot (x^4+1) - 1 \cdot 2x}{(x^4+1)^2} = \boxed{\frac{-2x}{(x^4+1)^2}}$$

$$19) f(x) = \frac{x^3}{x+2} \rightarrow f'(x) = \frac{3x^2(x+2) - x^3 \cdot 1}{(x+2)^2}$$

$$= \frac{3x^3 + 6x^2 - x^3}{(x+2)^2} = \boxed{\frac{2x^3 + 6x^2}{(x+2)^2}}$$

$$20.) f(x) = \frac{2x-1}{3x+2} \rightarrow f'(x) = \frac{2(3x+2) - (2x-1) \cdot 3}{(3x+2)^2} = \textcircled{6}$$

$$= \frac{6x+4 - 6x+3}{(3x+2)^2} = \frac{7}{(3x+2)^2}$$

$$21.) f(x) = \frac{x^2}{x^2-1} \rightarrow f'(x) = \frac{2x(x-1) - x^2(2x)}{(x^2-1)^2} =$$

$$= \frac{2x^2 - 2x - 2x^3}{(x^2-1)^2} = \frac{-2x}{(x^2-1)^2}$$

$$22.) f(x) = \frac{\sqrt{x}}{x+2} \rightarrow f' = \frac{\frac{1}{2\sqrt{x}}(x+2) - \sqrt{x} \cdot 1}{(x+2)^2} =$$

$$= \frac{\frac{x+2}{2\sqrt{x}} - \frac{\sqrt{x} \cdot 2\sqrt{x}}{2\sqrt{x}}}{(x+2)^2} = \frac{\frac{x+2-2x}{2\sqrt{x}}}{(x+2)^2} = \frac{\frac{2-x}{2\sqrt{x}}}{(x+2)^2 \cdot 2\sqrt{x}}$$

$$23.) f(x) = (x-1) \cdot \sqrt{x}$$

Brücke

$$f(x) = 2x \cdot \sqrt{x} + (x-1) \cdot \frac{1}{2\sqrt{x}} = \frac{2x\sqrt{x} \cdot 2\sqrt{x}}{2\sqrt{x}} + \frac{x^2-1}{2\sqrt{x}} =$$

$$= \frac{4x^2+x^2-1}{2\sqrt{x}} = \frac{5x^2-1}{2\sqrt{x}}$$

$$24.) f(x) = 3 \arcsin x \rightarrow f'(x) = \frac{3}{\sqrt{1-x^2}}$$

$$25.) f(x) = 2 \cdot \arccos x + e^x \rightarrow f'(x) = \frac{-2}{\sqrt{1-x^2}} + e^x$$

$$26.) y = 5 \operatorname{arctg} x \rightarrow f'(x) = \frac{5}{1+x^2}$$

$$27.) y = \frac{x \cdot e^x - \ln x}{2} \rightarrow f'(x) = \frac{1}{2} \cdot \left(1 \cdot e^x + x \cdot e^x - \frac{1}{x} \right) = \frac{x e^x + x e^x - 1}{2x}$$

(4)

$$28) f(x) = 3^x \cdot \sin x - \log_2 x$$

$$f'(x) = 3^x \cdot \ln 3 \cdot \sin x + 3^x \cdot \cos x - \frac{1}{x \ln 2}$$

KATEAREN ERREGEZA : Fn KONFSATNAK

13. omialdeez

$$1.) f(x) = (x^2 + 5)^6$$

$$f'(x) = 6 \cdot (x^2 + 5)^5 \cdot (x^2 + 5)' = 6(x^2 + 5)^5 \cdot 2x = \boxed{12x(x^2 + 5)^5}$$

$$2.) f(x) = \sin(x^2 - 1)$$

$$f'(x) = \cos(x^2 - 1) \cdot (x^2 - 1)' = \boxed{2x \cdot \cos(x^2 - 1)}$$

$$3.) f(x) = \cos(\ln x)$$

$$f'(x) = -\sin(\ln x) \cdot (\ln x)' = \boxed{-\frac{\sin(\ln x)}{x}}$$

$$4.) f(x) = \operatorname{tg}(2x - 3x^2)$$

$$\begin{aligned} f'(x) &= \left[1 + \operatorname{tg}^2(2x - 3x^2) \right] \cdot (2x - 3x^2)' \\ &= \boxed{(-6x + 2) \cdot [1 + \operatorname{tg}^2(2x - 3x^2)]} \end{aligned}$$

$$5.) f(x) = e^{3x^4 + 1}$$

$$f'(x) = e^{3x^4 + 1} \cdot (3x^4 + 1)' = \boxed{12x \cdot e^{3x^4 + 1}}$$

$$6.) f(x) = 2^{4x+1}$$

$$\begin{aligned} f'(x) &= 2^{4x+1} \ln 2 \cdot (4x+1)' = 2^{4x+1} \ln 2 \cdot 4 \\ &= \boxed{4 \cdot \ln 2 \cdot 2^{4x+1}} \end{aligned}$$

$$7.) f(x) = \cos^5 x$$

$$\begin{aligned} f'(x) &= 2 \cdot \cos x \cdot (\cos x)^1 = 2 \cdot \cos x \cdot (-\sin x) = \\ &= -2 \cos x \cdot \sin x = -\underline{\sin(2x)} \end{aligned}$$

8.

$$8.) f(x) = e^{3x}$$

$$f'(x) = e^{3x} \cdot (3x)^1 = \underline{3 \cdot e^{3x}}$$

$$\sin 2x = 2 \cdot \sin x \cdot \cos x$$

$$9.) f(x) = \ln(3x^2 - 6)$$

$$f'(x) = \frac{1}{3x^2 - 6} \cdot (3x^2 - 6)^1 = \frac{6x}{3x^2 - 6} = \frac{6x}{3(x^2 - 2)} = \underline{\frac{2x}{x^2 - 2}}$$

$$10.) f(x) = \ln\left(\frac{3x^2 - 1}{2}\right) = \ln(3x^2 - 1) - \ln 2.$$

$$\text{Logarit. Prop !! } \ln \frac{F(x)}{G(x)} = \ln F(x) - \ln G(x)$$

$$f'(x) = \frac{1}{3x^2 - 1} \cdot (3x^2 - 1)^1 - 0 = \underline{\frac{6x}{3x^2 - 1}}$$

$$11.) f(x) = \operatorname{arctg}(3x^2 + 2x)$$

$$\begin{aligned} f'(x) &= \frac{1}{1 + (3x^2 + 2x)^2} \cdot (3x^2 + 2x)^1 = \frac{6x + 2}{1 + (3x^2 + 2x)^2} \\ &= \underline{\frac{6x + 2}{9x^4 + 12x^3 + 6x^2 + 1}} \end{aligned}$$

$$12.) f(x) = \operatorname{arsin}(x^2)$$

$$f'(x) = \frac{1}{\sqrt{1 - (x^2)^2}} \cdot (x^2)^1 = \underline{\frac{2x}{\sqrt{1 - x^4}}}$$

$$13.) f(x) = \operatorname{arcos}(x^3 - 1)$$

$$f'(x) = \frac{-(x^3 - 1)^1}{\sqrt{1 - (x^3 - 1)^2}} = \frac{-3x^2}{\sqrt{1 - (x^3 - 1)^2}} =$$

$$= \underline{\frac{-3x^2}{\sqrt{x^6 + 2x^3}}}$$

$$18) f(x) = \left(\frac{x^2-1}{x+2} \right)^2$$

$$\begin{aligned} f'(x) &= 2 \cdot \frac{x^2-1}{x+2} \cdot \left(\frac{x^2-1}{x+2} \right)' = 2 \frac{x^2-1}{x+2} \cdot \frac{2x \cdot (x+2) - (x^2-1) \cdot 1}{(x+2)^2} \\ &= 2 \frac{x^2-1}{x+2} \cdot \frac{2x^2 + 4x - x^2 + 1}{(x+2)^2} = \frac{2(x^2-1)(x^2+4x+1)}{(x+2)^3} \end{aligned}$$

$$19) f(x) = \sqrt{x^2-4x} = (x^2-4x)^{1/2}$$

$$\begin{aligned} f'(x) &= \frac{1}{2} (x^2-4x)^{\frac{1}{2}-1} \cdot (x^2-4x)' = \frac{1}{2\sqrt{x^2-4x}} \cdot 2x-4 = \\ &= \frac{x-2}{\sqrt{x^2-4x}} \end{aligned}$$

$$20) f(x) = \frac{x+1}{(x-2)^2}$$

$$\begin{aligned} f'(x) &= \frac{1 \cdot (x-2)^2 - 2(x-2) \cdot (x+1)}{(x-2)^4} = \\ &= \frac{(x-2)[(x-2) - 2(x+1)]}{(x-2)^4} = \frac{x-2-2x-2}{(x-2)^3} = \frac{x-4}{(x-2)^3} \end{aligned}$$

$$21) f(x) = \frac{(2x+1)^2}{x-1}$$

$$f'(x) = \frac{2(2x+1) \cdot (2x+1)' \cdot (x-1) - (2x+1)^2 \cdot \frac{1}{g'}}{(x-1)^2} =$$

$$= \frac{2(2x+1) \cdot 2 \cdot (x-1) - (2x+1)^2}{(x-1)^2} = \frac{4 \cdot (2x^2-2x+x-1) - 4x^2-4x-1}{(x-1)^2}$$

$$= \frac{8x^2-4x-4x^2-4x-1}{(x-1)^2} = \frac{4x^2-8x-5}{(x-1)^2}$$

$$14.) f(x) = \sin(3x^2 - 1)^2$$

$$f'(x) = \cos(3x^2 - 1)^2 \cdot (3x^2 - 1)^1$$

$$= \cos(3x^2 - 1)^2 \cdot 2 \cdot (3x^2 - 1) \cdot (3x^2 - 1)^1$$

$$= \cos(3x^2 - 1)^2 \cdot 2 \cdot (3x^2 - 1) \cdot 6x$$

$$= 12x(3x^2 - 1) \cdot \cos(3x^2 - 1)^2$$

$$15.) f(x) = \sin^2(3x^2 - 1) = [\sin(3x^2 - 1)]^2$$

$$f'(x) = 2 \cdot \sin(3x^2 - 1) \cdot (\sin(3x^2 - 1))^1 =$$

$$= 2 \cdot \sin(3x^2 - 1) \cdot \cos(3x^2 - 1) \cdot (3x^2 - 1)^1$$

$$= 2 \cdot \underbrace{\sin(3x^2 - 1)}_{\sin 2x} \cdot \cos(3x^2 - 1) \cdot 6x$$

$$= 6x \cdot \sin 2(3x^2 - 1)$$

$$= [6x \cdot \sin(6x^2 - 2)]$$

$$\sin 2x = 2 \sin x \cdot \cos x$$

$$16.) f(x) = 3^{\cos x}$$

$$f'(x) = 3^{\cos x} \cdot \ln 3 \cdot (\cos x)^1 = \ln 3 \cdot (-\sin x) 3^{\cos x}$$

$$17.) f(x) = \ln\left(\frac{x+1}{x-2}\right) \quad \text{Log Proprietät!} \quad \log \frac{F(x)}{G(x)} = \log F(x) - \log G(x)$$

$$f(x) = \ln(x+1) - \ln(x-2)$$

$$f'(x) = \frac{1}{x+1} - \frac{1}{x-2} = \frac{x-2-(x+1)}{(x+1)(x-2)} = \frac{-3}{(x+1)(x-2)}$$

$$22) f(x) = \frac{(3x-1)^2}{2x+1} \quad \text{Katia}$$

$$f'(x) = \frac{2(3x-1) \cdot (3x-1)' \cdot (2x+1) - (3x-1)^2 \cdot 2}{(2x+1)^2}$$

$$= \frac{2(3x-1) \cdot 3 \cdot (2x+1) - 2(3x-1)^2}{(2x+1)^2} =$$

$$= \frac{6(6x^2 + 3x - 2x - 1) - 2(9x^2 - 6x + 1)}{(2x+1)^2} =$$

$$= \frac{36x^2 + 18x - 12x - 6 - 18x^2 + 12x - 2}{(2x+1)^2} =$$

$$= \boxed{\frac{18x^2 + 18x - 8}{(2x+1)^2}}$$

$$23) f(x) = \frac{e^x}{(x-1)^2}$$

$$f'(x) = \frac{e^x (x-1)^2 - e^x \cdot 2(x-1) \cdot 1}{(x-1)^4} =$$

$$= \frac{e^x [x^2 - 2x + 1 - 2x + 2]}{(x-1)^4} = \frac{e^x (x^2 - 4x + 3)}{(x-1)^4} =$$

$$= \frac{e^x (x-1)(x-3)}{(x-1)^4} = \boxed{\frac{e^x (x-3)}{(x-1)^3}} \quad x^2 - 4x + 3$$

$$\begin{array}{r|rrr} & 1 & -4 & 3 \\ 1 & & 1 & -3 \\ \hline & & 1 & 0 \end{array}$$

14. ornaidea.

$$1.) y = \frac{x^3}{3} - \frac{x^2}{4} + \frac{2}{3} \rightarrow y' = \frac{3x^2}{3} - \frac{2x}{4} = x^2 - \frac{1}{2}x$$

$$2.) y = \frac{x^5}{3} - \frac{2}{x^2} + 3 \rightarrow y' = \frac{5x^4}{3} - 2(-2)x^{-3} = \frac{5x^4}{3} + \frac{4}{x^3}$$

$$3.) y = \frac{x^2 - 2x + 1}{5} \rightarrow y' = \frac{2x - 2}{5}$$

$$4.) y = (3x - 2) \cdot e^x \rightarrow y' = 3e^x + (3x - 2) \cdot e^x = (3x + 1) \cdot e^x$$

$$5.) y = \sqrt{x} - \frac{2}{x^3} + \sqrt[3]{5} \\ = \frac{x^{1/2}}{1} - 2x^{-3} + \sqrt[3]{5} \rightarrow y' = \frac{1}{2}x^{\frac{1}{2}-\frac{1}{2}} - 2(-3)x^{-4} \\ = \frac{1}{2}\frac{\sqrt{x}}{\sqrt{x}\sqrt{x}} + \frac{6}{x^4} = \frac{\sqrt{x}}{2x} + \frac{6}{x^4}$$

$$6.) y = \frac{1}{x} - \frac{3\sqrt{x}}{3} + 2x^2 = x^{-1} - \frac{x^{1/3}}{3} + 2x^2$$

$$y' = (-1) \cdot x^{-2} - \frac{1}{3} \cdot \frac{x^{1/3-1}}{3} + 2 \cdot 2 \cdot x = -\frac{1}{x^2} - \frac{1}{9\sqrt[3]{x^2}} + 4x \\ = -\frac{1}{x^2} - \frac{1}{9x} + 4x = \frac{1}{9\sqrt[3]{x^2}} \cdot \frac{\frac{3\sqrt{x}}{3}}{\frac{3\sqrt{x}}{3}} = \frac{3\sqrt{x}}{9x}$$

$$= \frac{-9 - x + 36x^3}{9x^2}$$

$$7.) y = \frac{\sqrt[3]{x}}{x^2} - \frac{x^{2/3}}{3} = x^{\frac{1}{3}-2} - \frac{x^{\frac{2}{3}}}{3} = x^{-\frac{5}{3}} - \frac{x^{2/3}}{3} =$$

$$y' = -\frac{5}{3}x^{-\frac{5}{3}-1} - \frac{1}{3}2x = -\frac{5}{3}x^{-\frac{8}{3}} - \frac{2}{3}x =$$

$$= \frac{-5\sqrt[3]{x}}{3x} - \frac{2}{3}x =$$

$$= \frac{-5\sqrt[3]{x} - 2x^{\frac{1}{3}}}{3} //$$

$$x^{-\frac{8}{3}} = \frac{1}{\sqrt[3]{x^8}} = \frac{1}{x^{\frac{8}{3}}} \cdot \frac{\sqrt[3]{x}}{\sqrt[3]{x}} =$$

$$= \frac{\sqrt[3]{x}}{x^3}$$

$$8). y = \frac{x^3 - 3x^4 + 2x + 1}{x} = x^2 - 3x^3 + 2 + x^{-1} \quad 13$$

$$y' = 2x - 9x^2 - 1x^{-2} = \boxed{-9x^2 + 2x - \frac{1}{x^2}}$$

$$9.) y = \frac{3}{2x^4} - \frac{2x^2}{3} + 6x^5 = \frac{3}{2}x^{-2} - \frac{2}{3}x^2 + 6x^5$$

$$y' = \frac{3}{2} \cdot (-2)x^{-3} - \frac{2}{3} \cdot 2x + 0 = \frac{-3}{x^3} - \frac{4x}{3} = \boxed{\frac{-9 - 4x^4}{3x^3}}$$

$$10.) y = \sqrt{\frac{2}{x^3}} - \frac{x^2}{3} + \sqrt{2} = \sqrt{2}x^{-\frac{3}{2}} - \frac{1}{3}x^2 + \sqrt{2}$$

$$y' = \sqrt{2} \cdot \frac{3}{2}x^{-\frac{5}{2}} - \frac{1}{3} \cdot 2x + 0 = \frac{-3\sqrt{2}}{2} \cdot \frac{1}{\sqrt{x^5}} - \frac{2x}{3} = \boxed{\frac{-3\sqrt{2}x}{x^3} - \frac{2x}{3}}$$

$$11.) y = \frac{2\sqrt{3}}{4} + \frac{3\ln x}{2} \rightarrow \boxed{y' = \frac{3}{2x}}$$

$$\frac{1}{\sqrt{x^5}} = \frac{1}{x^2\sqrt{x}} \cdot \frac{\sqrt{x}}{\sqrt{x}} = \frac{\sqrt{x}}{x^3}$$

$$12.) y = \sin x \cdot \cos x \rightarrow y' = \cos x \cdot \cos x + \sin x (-\sin x)$$

$$= \boxed{\cos^2 x - \sin^2 x = \cos(2x)} \quad !!$$

$$13.) y = \frac{e^x}{x^2 - 1}$$

$$y' = \frac{e^x(x^2 - 1) - e^x \cdot 2x}{(x^2 - 1)^2} = \frac{e^x(x^2 - 2x - 1)}{(x^2 - 1)^2}$$

$$14.) y = \frac{x^2 - 1}{2x + 1} \rightarrow y' = \frac{2x(2x+1) - (x^2 - 1) \cdot 2}{(2x+1)^2} =$$

$$= \frac{4x^3 + 2x - 2x^2 + 2}{(2x+1)^2} = \frac{2x^3 + 2x + 2}{(2x+1)^2}$$

$$14.) y = \frac{x^2 - 1}{2x + 1} \rightarrow y' = \frac{2x(2x+1) - (x^2 - 1) \cdot 2}{(2x+1)^2} =$$

$$= \frac{4x^3 + 2x - 2x^2 + 2}{(2x+1)^2} = \frac{2x^3 + 2x + 2}{(2x+1)^2}$$

$$15.) y = (x^2 - 1) e^x - \ln x$$

$$y' = 2x \cdot e^x + (x^2 - 1) e^x - \frac{1}{x} = e^x (x^2 + 2x - 1) - \frac{1}{x}$$

$$16.) y = 2^x - 3 + g(x) \rightarrow y' = 2^x \ln 2 - 3(1 + f^2(x))$$

$$17.) y = x^3 \cdot e^x + x^2 \sin x \rightarrow$$

$$y' = 3x^2 \cdot e^x + x^3 \cdot e^x + 2x \cdot \sin x + x^2 \cos x$$

$$18.) y = \frac{x-1}{3x-2} \rightarrow y' = \frac{1 \cdot (3x-2) - (x-1) \cdot 3}{(3x-2)^2} =$$

$$= \frac{3x-2 - 3x + 3}{(3x-2)^2} = \boxed{\frac{1}{(3x-2)^2}}$$

$$19.) y = \frac{\sqrt{x}}{\sin x} \rightarrow y' = \frac{\frac{1}{2} \cdot x^{-\frac{1}{2}} \cdot \sin x - \sqrt{x} \cdot \cos x}{\sin^2 x} =$$

$$= \frac{\sin x - \sqrt{x} \cos x}{2\sqrt{x} \cdot \sin^2 x} = \frac{\sin x - \sqrt{x} \cos x (2\sqrt{x})}{2\sqrt{x} \cdot \sin^2 x} =$$

$$= \boxed{\frac{\sin x - 2x \cos x}{2\sqrt{x} \cdot \sin^2 x}}$$

$$20.) y = (x^2 - 1)^4 \rightarrow y' = 4 \cdot (x^2 - 1)^3 \cdot 2x = \boxed{8x(x^2 - 1)^3}$$

$$21.) y = \left(\frac{x-1}{x+2}\right)^3 \rightarrow y' = 3 \left(\frac{x-1}{x+2}\right)^2 \cdot \left(\frac{x-1}{x+2}\right)' =$$

$$y' = 3 \left(\frac{x-1}{x+2}\right)^2 \cdot \frac{1 \cdot (x+2) - (x-1) \cdot 1}{(x+2)^2} = \frac{3(x-1)^2}{(x+2)^2} \cdot \frac{3}{(x+2)} =$$

$$= \boxed{\frac{9(x-1)^2}{(x+2)^4}}$$

$$\begin{aligned}
 22.) \quad & y = \frac{2x-1}{(x+1)^2} \rightarrow y' = \frac{2(x+1)^2 - (2x-1) \cdot 2(x+1)}{(x+1)^4} \\
 & = \frac{(x+1)[2(x+1) - (2x-1) \cdot 2]}{(x+1)^4} = \frac{2x+2 - 4x+2}{(x+1)^3} = \\
 & = \boxed{\frac{-2x+4}{(x+1)^3}}
 \end{aligned}$$

$$\begin{aligned}
 23.) \quad & y = \frac{x+1}{(x-1)^3} \rightarrow y' = \frac{1 \cdot (x-1)^3 - (x+1) \cdot 3(x-1)^2}{(x-1)^6} = \\
 & = \boxed{\frac{(x-1)^2[(x-1) - (x+1) \cdot 3]}{(x-1)^6} = \frac{(x-1) - 3x - 3}{(x-1)^4} = \boxed{\frac{-2x-4}{(x-1)^4}}}
 \end{aligned}$$

$$\begin{aligned}
 24.) \quad & y = \ln\left(\frac{x-1}{x+4}\right) \quad y = \ln(x-1) - \ln(x+4)
 \end{aligned}$$

$$y' = \frac{1}{x-1} - \frac{1}{x+4} = \frac{(x+4) - (x-1)}{(x-1)(x+4)} = \frac{5}{(x-1)(x+4)}$$

$$25.) \quad y = \cos^2(3x-2) = [\cos(3x-2)]^2$$

$$\begin{aligned}
 y' &= 2 \cdot \cos(3x-2) \cdot (\cos(3x-2))' = \\
 &= 2 \cdot \cos(3x-2) \cdot (-\sin(3x-2)) \cdot (3x-2)' = \\
 &= -2 \sin(3x-2) \cdot \cos(3x-2) \cdot (3x-2) \\
 &= -(3x-2) \sin(6x-4)
 \end{aligned}$$

$$\boxed{\sin 2x = 2 \cdot \sin x \cdot \cos x}$$

$$26.) y = \sqrt{\sin x} = (\sin x)^{1/2}$$

$$\begin{aligned} y' &= \frac{1}{2}(\sin x)^{1/2-1} \cdot (\sin x)' = \frac{1}{2}(\sin x)^{-1/2} \cos x = \\ &= \frac{1}{2} \frac{\cos x}{\sqrt{\sin x}} \cdot \frac{\sqrt{\sin x}}{\sqrt{\sin x}} = \boxed{\frac{\sqrt{\sin x} \cdot \cos x}{2 \sin x}} \end{aligned}$$

$$27.) y = \ln(\sin x^2)$$

$$\begin{aligned} y' &= \frac{1}{\sin x^2} \cdot (\sin x^2)' = \frac{1}{\sin x^2} \cos x^2 \cdot (x^2)' = \\ &= \frac{\cos x^2}{\sin x^2} \cdot 2x = \boxed{\frac{2x}{\tan x^2}} \end{aligned}$$

$$28.) y = e^{4x-1} \sin(3x^2) \quad f'g + fg'$$

$$\begin{aligned} y' &= (e^{4x-1})' \cdot \sin(3x^2) + e^{4x-1} \cdot (\sin 3x^2)' = \\ &= \underbrace{e^{4x-1} \cdot 4}_{f'} \cdot \underbrace{\sin(3x^2)}_{g} + \underbrace{e^{4x-1}}_f \underbrace{\cos 3x^2 \cdot 6x}_{g'} = \\ &= e^{4x-1} \left[4 \cdot \sin(3x^2) + 6x \cdot \cos(3x^2) \right] \end{aligned}$$

$$29.) y = 2^{4x^2-1} \ln(8x)$$

$$\begin{aligned} y' &= (2^{4x^2-1})' \cdot \ln(8x) + 2^{4x^2-1} \cdot (\ln(8x))' \\ &= \underbrace{2^{4x^2-1} \cdot \ln 2 \cdot 8x}_{f'} \cdot \underbrace{\ln(8x)}_g + \underbrace{2^{4x^2-1}}_f \underbrace{\frac{1}{8x} \cdot 8}_{g'} = \\ &= \ln 2 \cdot 8x \cdot 2^{4x^2-1} \cdot \ln(8x) + \boxed{\frac{2^{4x^2-1}}{x}} \end{aligned}$$

$$30.) y = \frac{(2x+3)^2}{1-x} \rightarrow y' = \frac{2(2x+3)(1-x) - (2x+3)^2(-1)}{(1-x)^2} =$$

$$y' = \frac{2(2x-2x^2+3-3x) - (4x^2+12x+9)}{(1-x)^2} =$$

$$= \frac{4x-4x^2+6-6x-4x^2-12x-9}{(1-x)^2} = \frac{-8x^2-14x-3}{(1-x)^2}$$

$$31.) y = \operatorname{tg}\left(\frac{2}{x-3}\right) = \operatorname{tg}\left[2 \cdot (x-3)^{-1}\right]$$

$$y' = \left[1 + \operatorname{tg}^2\left(\frac{2}{x-3}\right)\right] \cdot \left(2(x-3)^{-1}\right)' =$$

$$= \left[1 + \operatorname{tg}^2\left(\frac{2}{x-3}\right)\right] \cdot 2 \cdot (-1) \cdot (x-3)^{-2} =$$

$$= \frac{-2}{(x-3)^2} \left[1 + \operatorname{tg}^2\left(\frac{2}{x-3}\right)\right]$$

$$32.) y = \frac{e^{5x+1}}{x+2}$$

$$y' = \frac{\left(e^{5x+1}\right)'(x+2) - e^{5x+1}(x+2)'}{(x+2)^2} =$$

$$= \frac{e^{5x+1} \cdot 5 \cdot (x+2) - e^{5x+1} \cdot 1}{(x+2)^2} = \frac{e^{5x+1}(5x+9)}{(x+2)^2}$$

$$33.) y = \frac{\ln x}{x} = \frac{(\ln x)^2}{x}$$

$$y' = \frac{2 \ln x (\ln x)' \cdot x - (\ln x)^2 \cdot x'}{x^2}$$

$$y' = \frac{2 \ln x \cdot \cancel{\frac{1}{x}} - (\ln x)^2}{x^2} = \frac{2 \ln x - (\ln x)^2}{x^2} = \frac{\ln x (2 - \ln x)}{x^2}$$

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$$34.) \quad y = \frac{x \cdot e^x}{x+2}$$

$$y' = \frac{(x \cdot e^x) \cdot (x+2) - x \cdot e^x \cdot (x+2)}{(x+2)^2} =$$

$$= \frac{(1 \cdot e^x + x \cdot e^x) \cdot (x+2) - x \cdot e^x \cdot 1}{(x+2)^2} =$$

$$= \frac{x \cdot e^x + 2 \cdot e^x + x^2 e^x + 2x \cdot e^x - x \cdot e^x}{(x+2)^2}$$

$$= \frac{e^x (x^2 + 2x + 2)}{(x+2)^2}$$

$$35.) \quad y = \frac{\sqrt{x-1}}{3x+4}$$

$$\frac{(x-1) \cdot 6}{3x+4 - \sqrt{x-1} \cdot 3 \cdot (2 \cdot \sqrt{x-1})} =$$

$$\frac{2\sqrt{x-1}}{(3x+4)^2}$$

$$y' = \frac{\frac{1}{2\sqrt{x-1}} \cdot (3x+4) - \sqrt{x-1} \cdot 3}{(3x+4)^2} =$$

$$= \frac{3x+4 - 6(x-1)}{2\sqrt{x-1} \cdot (3x+4)^2} = \frac{-3x+10}{2\sqrt{x-1} \cdot (3x+4)^2}$$

$$36.) \quad y = \sqrt{\frac{3x+1}{x+2}} = \left(\frac{3x+1}{x+2}\right)^{1/2}$$

$$y' = \frac{1}{2} \cdot \frac{3x+1}{x+2} \cdot \left(\frac{3x+1}{x+2}\right)' = \frac{1}{2} \cdot \frac{3x+1}{x+2} \cdot \frac{3(x+2) - (3x+1) \cdot 1}{(x+2)^2} =$$

$$= \frac{3x+1}{2(x+2)} \cdot \frac{3x+6 - 3x-1}{(x+2)^2} = \frac{5(3x+1)}{2(x+2)^3}$$

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37.) $y = \arctg(x^2 + 2)$

$$y' = \frac{1}{1 + (x^2 + 2)^2} \cdot (x^2 + 2)' = \frac{2x}{1 + x^4 + 4x^2 + 4} = \\ = \frac{2x}{x^4 + 4x^2 + 5}$$

38.) $y = \sqrt{\arctg x} = (\arctg x)^{\frac{1}{2}}$

$$y' = \frac{1}{2} (\arctg x)^{-\frac{1}{2}} \cdot (\arctg x)' = \frac{1}{2\sqrt{\arctg x}} \cdot \frac{1}{1+x^2}$$

39.) $y = \frac{3 \cdot \arcsin(2x-1)}{4}$

$$y' = \frac{3}{4} \cdot \frac{1}{\sqrt{1-(2x-1)^2}} \cdot (2x-1)' = \frac{3 \cdot 2}{4 \sqrt{1-(2x-1)^2}} = \\ = \frac{3}{2\sqrt{-4x^2+4x}}$$

40.) $f(x) = \arccos(\sqrt{x})$

$$y' = \frac{-1}{\sqrt{1-(\sqrt{x})^2}} \cdot (\sqrt{x})' = \frac{-1}{2\sqrt{x}\sqrt{1-x}} = \\ = \frac{-1}{2\sqrt{x(1-x)}} = \frac{-1}{2\sqrt{x-x^2}}$$