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# Berehalako integralen adierazpen kooposatua.

1.1.

$$\int u^5 du = \frac{u^6}{6} + K = \cos^6 x$$

$u = \cos x \quad du = -\sin x dx$

a)  $\int \cos^5 x \cdot (-\sin x) dx = \int (\cos x)^5 \cdot (-\sin x) dx =$

$$= \frac{\cos^6 x}{6} + K.$$

b)  $\int \sqrt[3]{\cos^2 x} \cdot (-\sin x) dx = \int (\cos x)^{\frac{2}{3}} \cdot (-\sin x) dx =$

$$\frac{(\cos x)^{\frac{2}{3}+1}}{\frac{2}{3}+1} + K = \frac{\sqrt[3]{\cos^5 x}}{\frac{5}{3}} = \frac{3}{5} \sqrt[3]{\cos^5 x} + K$$

c)  $\int e^{\cos x} \cdot \sin x dx = -e^{\cos x} + K$

d)  $\int e^{x^3+x^2} \cdot (3x^2+2x) dx = e^{x^3+x^2} + K$

e)  $\int \tan x \cdot 2x dx = \int \frac{\sin x}{\cos x} \cdot 2x dx =$

$$- \ln |\cos x| + K$$

f)  $\int \frac{3x^2}{1+x^6} dx = \int \frac{3x^2}{1+(x^3)^2} dx = \arctan x^3 + K$

g)  $\int \frac{-e^{-x}}{\sqrt{1-e^{-2x}}} dx = \int \frac{-e^{-x}}{\sqrt{1-(e^{-x})^2}} = \arcsin(e^{-x}) + K$

h)  ~~$\int -e^{-x} \cdot \ln(x^2+1) \cdot 2x dx =$~~

$$(x^2+1) \ln(x^2+1) - (x^2+1) + K$$

$$\begin{aligned} u &= x^2+1 \\ du &= 2x dx \end{aligned}$$

~~1.1.~~  $\int \sqrt[3]{(x^4+5x)^2} \cdot (4x^3+5) dx = \frac{3}{5} \sqrt[3]{(x^4+5x)^5} + K$

$$\begin{aligned} u &= x^4+5x \\ du &= (4x^3+5)dx \end{aligned}$$

$$\int u^{\frac{2}{3}} du = \frac{3}{5} u^{\frac{5}{3}} = \frac{3}{5} (x^4+5x)^{\frac{5}{3}} + K$$