

(1[∞]) INDETERMINATION

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{x}\right)^x = e$$

(1)

$$\lim_{x \rightarrow \square} f(x) = \lim_{x \rightarrow \square} g(x) = \lim_{x \rightarrow \square} f(x) \cdot g(x)$$

224 or **3**

$$a) \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{\sqrt{x}}\right)^x = (1^\infty) \text{ IND.}$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{\sqrt{x}}\right)^{x \cdot \frac{1}{5} \cdot 5} = \lim_{x \rightarrow +\infty} \left[\left(1 + \frac{1}{\sqrt{x}}\right)^{\sqrt{x}} \right]^{1/5} = e^{1/5}$$

$$b) \lim_{x \rightarrow +\infty} \left(5 + \frac{1}{\sqrt{x}}\right)^{\sqrt{x}} = (1^\infty)$$

$$\lim_{x \rightarrow +\infty} \left[5 \left(1 + \frac{1}{25x}\right) \right]^{\sqrt{x}} = \lim_{x \rightarrow +\infty} 5^{\sqrt{x}} \left(1 + \frac{1}{25x}\right)^{\sqrt{x}} =$$

$$= \lim_{x \rightarrow +\infty} 5^{\sqrt{x}} \left(1 + \frac{1}{25x}\right)^{5x \cdot \frac{1}{5}} = \lim_{x \rightarrow +\infty} 5^{\sqrt{x}} \left[\left(1 + \frac{1}{25x}\right)^{25x} \right]^{1/5} =$$

$$= \lim_{x \rightarrow +\infty} 5^{\sqrt{x}} \cdot \lim_{x \rightarrow +\infty} \left[\left(1 + \frac{1}{25x}\right)^{25x} \right]^{1/5} =$$

$$= +\infty \cdot e^{1/5} = \underline{\underline{+\infty}}$$

$$c) \lim_{x \rightarrow +\infty} \left(5 + \frac{1}{\sqrt{x}}\right)^{-\sqrt{x}} = \lim_{x \rightarrow +\infty} \left[5 \left(1 + \frac{1}{25x}\right) \right]^{-\sqrt{x}} =$$

$$= \lim_{x \rightarrow +\infty} 5^{-\sqrt{x}} \cdot \left(1 + \frac{1}{25x}\right)^{-5x \cdot \frac{1}{5}} = \lim_{x \rightarrow +\infty} 5^{-\sqrt{x}} \cdot \left[\left(1 + \frac{1}{25x}\right)^{25x} \right]^{-1/5} =$$

$$= 0 \cdot e^{-1/5} = \underline{\underline{0}}$$

$$\lim_{x \rightarrow +\infty} 5^{-\sqrt{x}} = 5^{-\infty} = \frac{1}{5^\infty} = 0$$

$$d) \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{\sqrt{x}}\right)^5 = 1^5 = \underline{\underline{1}}$$

(2)

$$e) \lim_{x \rightarrow +\infty} \left(1 + \frac{5}{x}\right)^x = 1^\infty$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{x/5}\right)^x = \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{x/5}\right)^{\overbrace{x \cdot \frac{1}{5}}^5} = e^5$$

$$f) \lim_{x \rightarrow +\infty} \left(1 + \frac{5}{x}\right)^{-x} = (1^\infty)$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{x/5}\right)^{\overbrace{-x \cdot \frac{1}{5}}^{(-5)}} = \lim_{x \rightarrow +\infty} \left[\left(1 + \frac{1}{x/5}\right)^{x/5} \right]^{-5} = \underline{\underline{e^{-5}}}$$

$$g) \lim_{x \rightarrow +\infty} \left(5 + \frac{5}{x}\right)^{5x} = 5^{+\infty} = \underline{\underline{+\infty}}$$

$$\begin{aligned} \text{EDO} \quad \lim_{x \rightarrow +\infty} \left[5 \left(1 + \frac{1}{x}\right)\right]^{5x} &= \lim_{x \rightarrow +\infty} \underbrace{5^{5x}}_{5^{+\infty}} \cdot \underbrace{\left(1 + \frac{1}{x}\right)^x}_{e^5} \\ &= 5^{+\infty} \cdot e^5 = +\infty \cdot e^5 = \underline{\underline{+\infty}} \end{aligned}$$

$$h) \lim_{x \rightarrow +\infty} \left(1 - \frac{1}{x}\right)^{5x} = (1^\infty)$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{-x}\right)^{5x} = \lim_{x \rightarrow +\infty} \left[\left(1 + \frac{1}{-x}\right)^{-x \cdot (-5)} \right] = \underline{\underline{e^{-5}}}$$

$$i) \lim_{x \rightarrow +\infty} \left(1 - \frac{1}{x}\right)^{-5x} = (1^\infty)$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{-x}\right)^{-x \cdot 5} = \underline{\underline{e^5}}$$

216.007) [4] (1[∞])

(31)

$$a) \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{x}\right)^{3x-2} = (1^{+\infty})$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{x}\right)^{3x} \cdot \left(1 + \frac{1}{x}\right)^{-2} = e^3 \cdot 1^{-2} = \underline{\underline{e^3}}$$

$$b) \lim_{x \rightarrow +\infty} \left(1 - \frac{1}{2x}\right)^{4x} = (1^{+\infty})$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{-2x}\right)^{-2x \cdot \frac{2}{-1}} = \underline{\underline{e^{-2}}}$$

$$c) \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{5x}\right)^{3x} = (1^{+\infty})$$

$$= \lim_{x \rightarrow +\infty} \left(1 + \frac{1}{5x}\right)^{3x \cdot \frac{5}{5}} = \underline{\underline{e^{3/5}}}$$

$$d) \lim_{x \rightarrow +\infty} \left(1 + \frac{3}{2x}\right)^5 = 1^5 = 1$$

$$e) \lim_{x \rightarrow +\infty} \left(1 - \frac{1}{2x}\right)^{3x} = (1^{+\infty})$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{-2x}\right)^{3x \cdot \frac{-2}{2}} = \underline{\underline{e^{3/2}}}$$

$$f) \lim_{x \rightarrow +\infty} \left(1 + \frac{2}{5x}\right)^{5x} = (1^{+\infty})$$

$$\lim_{x \rightarrow +\infty} \left(1 + \frac{1}{5x/2}\right)^{5x \cdot \frac{2}{2}} = \underline{\underline{e^2}}$$