- 1. [10 pts] Consider the context-free grammar S  $\rightarrow$  ySx | yySx |  $\epsilon$ 
  - a. Show that the grammar is ambiguous.
  - b. Derive an equivalent unambiguous grammar.
- 2. [15 pts] Design a PDA for the following languages:

a. 
$$L_1 = \{0^{2k} \ 1^{3k} \mid k \ge 0\}$$
  
b.  $L_2 = \{ \ 0^a 1^b 2^c \mid a, b, c \ge 0 \ \text{and} \ a + b = c \ \}$ 

- 3. [15 pts] Prove or disprove the following statements:
  - a. The class of context-free languages are closed under the union operation.
  - b. The class of context-free languages are closed under the intersection operation. Hint: Consider the following two languages:

$$L_1 = \{a^m b^n c^n \mid m, n \ge 0\}$$
  

$$L_2 = \{a^n b^n c^m \mid m, n \ge 0\}$$

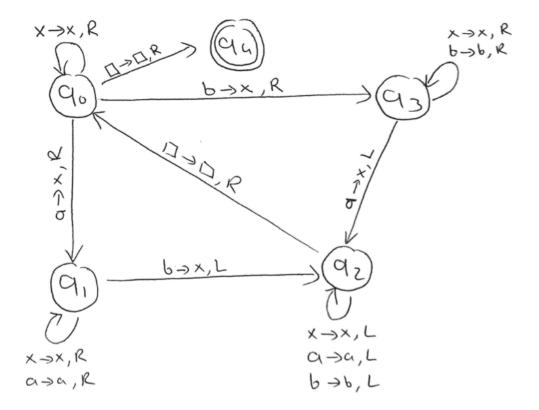
4. [10 pts] Given the following context-free grammar:

$$S \rightarrow XY \mid \varepsilon$$
  
 $X \rightarrow xY$   
 $Y \rightarrow SV$ 

- a. What is the language generated by this grammar?
- b. Draw the parse tree for the string xxyyyy.
- 5. [15 pts] Convert the following context-free grammar to an equivalent grammar in Chomsky Normal Form.

$$S \rightarrow ASA \mid A \mid \varepsilon$$
  
 $A \rightarrow 11 \mid \varepsilon$ 

6. [10 pts] What is the language on {a,b} recognized by the following Turing Machine (a,b,x, and box are the tape symbols where box denotes the empty cell)?



- 7. [10 pts] Prove or disprove the following statement:

  Turing-recognizable languages are closed under the intersection operation.
- 8. [15 pts] Prove that the following languages are decidable (give the deciders for each of the language):
  - a.  $L_1=\{< D,R>\mid D \text{ is a DFA},R \text{ is a regular expression and }L(D)=L(R)\}$ b.  $L_2=\{< N>\mid N \text{ is an NFA and }L(N)=\Sigma^*\}$

## Notes:

- You need to create only one pdf file with high resolution. Make sure that your pdf file is readable. (You can use a smartphone application for this purpose)
- Make sure that the pdf file's name contains your number. (yourNumber HW2.pdf)
- ullet Make sure that the all pages of your pdf file also contain your number. (for example, on upper right corner)
- ullet Note that in case of cheating, all parties involved will get zero grade.
- $\bullet$  If you submit your assignment late, for every day after the due date, your grade will be decreased by 10%. (If you submit the day

after the due date, you will get 90% of your actual grade, if you submit 2 days after, you will get 80% of your actual grade, etc.)

- Due date of the assignment is June 9, 2020, 23:59.
- Send your assignments to <a href="mailto:cse364.projects@gmail.com">cse364.projects@gmail.com</a>