

## Solution to Homework 2

**name:** Brian Ackermann

**netids:** ackerma9

---

### Problem 1

(\*1\*)  $\rho_4 \rightarrow \{z \rightarrow 4, \text{plus\_}x \rightarrow < \text{fun } y \rightarrow x + y, x \rightarrow 2 >, x \rightarrow 2\}$

(\*2\*)  $\rho_6 \rightarrow \{y \rightarrow 0, \text{sub\_}z \rightarrow < \text{fun } x \rightarrow y - z + x, \rho_4 >\} + \rho_4$

(\*3\*)  $\rho_7 \rightarrow \{f\_z \rightarrow < \text{fun } x \rightarrow \text{if plus\_}x \ x < z \text{ then plus\_}x \ z \text{ else sub\_}z \ x, \rho_6\} + \rho_6$

### Problem 2

$\text{Eval}(f\_z \ x, \rho_6) =$

$\text{Eval}(\text{app } < x \rightarrow \text{if plus\_}x \ x < z \text{ then plus\_}x \ z \text{ else sub\_}z \ x, \rho_6 > (x), \rho_6) =$

$\text{Eval}(\text{app } < x \rightarrow \text{if plus\_}x \ \dots > (2), \rho_6) =$

$\text{Eval}(\text{app } < x \rightarrow \text{if } 2 < 4 \text{ then plus\_}x \ 4 \text{ else sub\_}z \ 2, \rho_6 > (2), \rho_6) =$

$\text{Eval}(\text{plus\_}x \rightarrow < \text{fun } y \rightarrow x + y, \{x \rightarrow 2\} >, (2), \rho_6) =$

$\text{Eval}(x + y, \{x \rightarrow 2, y \rightarrow 2\} + \{x \rightarrow 2\}) =$

$\text{Eval}(2 + 2, \{x \rightarrow 2, y \rightarrow 2\} + \{x \rightarrow 2\}) = 4$