

# Model Documentation of the Lotka-Volterra (Predator-Prey) Model

## 1 Nomenclature

### 1.1 Nomenclature for Model Equations

$x_1$  population of prey  
 $x_2$  population of predators

## 2 Model Equations

State Vector:

$$\underline{x} = (x_1 \ x_2)^T$$

System Equations:

$$\dot{x}_1 = \alpha x_1 - \beta x_1 x_2 \quad (1a)$$

$$\dot{x}_2 = \gamma x_1 x_2 - \delta x_2 \quad (1b)$$

Parameters:  $\alpha, \beta, \gamma, \delta$

### 2.1 Exemplary parameter values

| Parameter Name                          | Symbol   | Value | Range         |
|---|----------|-------|---------------|
| reproduction rate of prey alone         | $\alpha$ | 1.3   | $(0, \infty)$ |
| mortality rate of prey per predator     | $\beta$  | 0.9   | $(0, \infty)$ |
| mortality rate of predators             | $\gamma$ | 0.8   | $(0, \infty)$ |
| reproduction rate of predators per prey | $\delta$ | 1.8   | $(0, \infty)$ |

### 3 Simulation

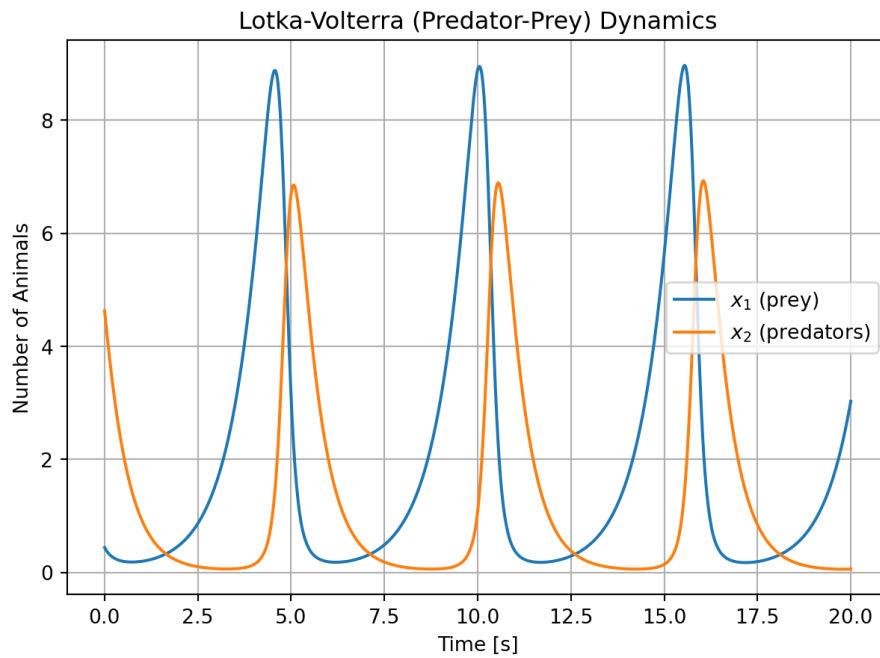


Figure 1: Simulation of the Lotka Volterra.

### References

- [1] Peter J. Wangersky: *Lotka-Volterra Population Models*, 1978, <https://www.jstor.org/stable/2096748>