# Model Documentation of the Kapitza's Pendulum

#### 1 Nomenclature

#### 1.1 Nomenclature for Model Equations

- $\gamma$  Dampening factor
- l length of the pendulum
- g acceleration due to gravity
- $\varphi$  angle of deflection from the equilibrium position
- a magnitude of the harmonic oscillation of the suspension point
- $\omega$  frequency of the harmonic oscillation of the suspension point

## 2 Model Equations

State Vector and Input Vector:

$$\underline{x} = (x_1 \ x_2)^T = (\varphi \ \dot{\varphi})^T$$
$$u = \emptyset$$

System Equations:

$$\dot{x}_1 = x_2 \tag{1a}$$

$$\dot{x}_2 = -2\gamma x_2 - \left(\frac{g}{l} - \frac{a}{l}\omega^2 \cos(\omega t)\right) \sin(x_1) \tag{1b}$$

Parameters:  $\omega$ , a, l, g,  $\gamma$ 

Outputs:  $\varphi$ 

#### 2.1 Assumptions

1. Mass of the pendulum is a pointmass

#### 2.2 Exemplary parameter values

Parameter Name	Symbol	Value	Unit
Pendulum length	1	0.3	cm
acceleration due to gravitation	g	9.81	$\frac{m}{s^2}$
Amplitude of Oscillation	a	$0.2 \ 1$	$\mathrm{cm}$
Frequency of Oscillation	$\omega$	$16\omega_0$	$_{\mathrm{Hz}}$
Dampening Factor	$\gamma$	$0.1\omega_0$	$_{\mathrm{Hz}}$
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with  $\omega_0 = \sqrt{\frac{g}{l}}$ 

### 3 Derivation and Explanation

 $Not\ available$ 

## References

[1] Butikov, E. I.: Kapitza's Pendulum: A Physically Transparent Simple Treatment, published 2017