

Model Documentation of the Kapitza's Pendulum

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1 Nomenclature

1.1 Nomenclature for Model Equations

γ	Dampening factor
l	length of the pendulum
g	acceleration due to gravity
φ	angle of deflection from the equilibrium position
a	magnitude of the harmonic oscillation of the suspension point
ω	frequency of the harmonic oscillation of the suspension point

2 Model Equations

State Vector and Input Vector:

$$\underline{x} = (x_1 \ x_2)^T = (\varphi \ \dot{\varphi})^T$$
$$\underline{u} = \emptyset$$

System Equations:

$$\dot{x}_1 = x_2 \tag{1a}$$

$$\dot{x}_2 = -2\gamma x_2 - \left(\frac{g}{l} - \frac{a}{l} \omega^2 \cos(\omega t) \right) \sin(x_1) \tag{1b}$$

Parameters: ω , a , l , g , γ

Outputs: φ

2.1 Assumptions

1. Mass of the pendulum is a pointmass

2.2 Exemplary parameter values

Parameter Name	Symbol	Value	Unit
Pendulum length	l	0.3	cm
acceleration due to gravitation	g	9.81	$\frac{m}{s^2}$
Amplitude of Oscillation	a	$0.2l$	cm
Frequency of Oscillation	ω	$16\omega_0$	Hz
Dampening Factor	γ	$0.1\omega_0$	Hz

with $\omega_0 = \sqrt{\frac{g}{l}}$

3 Derivation and Explanation

Not available

References

- [1] Butikov, E. I.: *Kapitza's Pendulum: A Physically Transparent Simple Treatment*, published 2017