

Model Documentation of the Two Mass Floating Bodies

1 Nomenclature

1.1 Nomenclature for Model Equations

m_1	mass of the iron ball
m_2	mass of the brass ball
k_1	geometry constant
k_2	air gap of magnet
k_f	spring constant
g	acceleration of gravity
I	current
s_1	position of the iron ball in x-direction
s_2	position of the brass ball in x-direction
v_1	velocity of the iron ball in x-direction
v_2	velocity of the brass ball in x-direction

2 Model Equations

State Vector and Input Vector:

$$\underline{x} = (x_1 \ x_2 \ x_3 \ x_4)^T = (s_1 \ s_2 \ v_1 \ v_2)^T$$
$$\underline{u} = u_1 = I$$

System Equations:

$$\dot{x}_1 = x_3 \tag{1a}$$

$$\dot{x}_2 = x_4 \tag{1b}$$

$$\dot{x}_3 = g - \frac{k_f}{m_1}(x_1 - x_2) - k_1 \frac{I}{m_1(x_1 + k_2)^2} \tag{1c}$$

$$\dot{x}_4 = g + \frac{k_f}{m_2}(x_1 - x_2) \tag{1d}$$

$$\tag{1e}$$

Parameters: $m_1 \ m_2 \ k_1 \ k_2 \ k_f \ g$

Outputs: s_2

2.1 Assumptions

1. Mass of the iron ball is a pointmass
2. Mass of the brass ball is a pointmass

2.2 Exemplary parameter values

Parameter Name	Symbol	Value	Unit
mass of the iron ball	m_1	0.05	kg
mass of the brass ball	m_2	0.04	kg
geometry constant	k_1	$4.0 \cdot 10^{-5}$	
air gap of magnet	k_2	0.005	m
spring constant	k_f	10	$\frac{N}{m}$
acceleration of gravity	g	9.8	$\frac{m}{s^2}$

3 Derivation and Explanation

Not available

4 Simulation

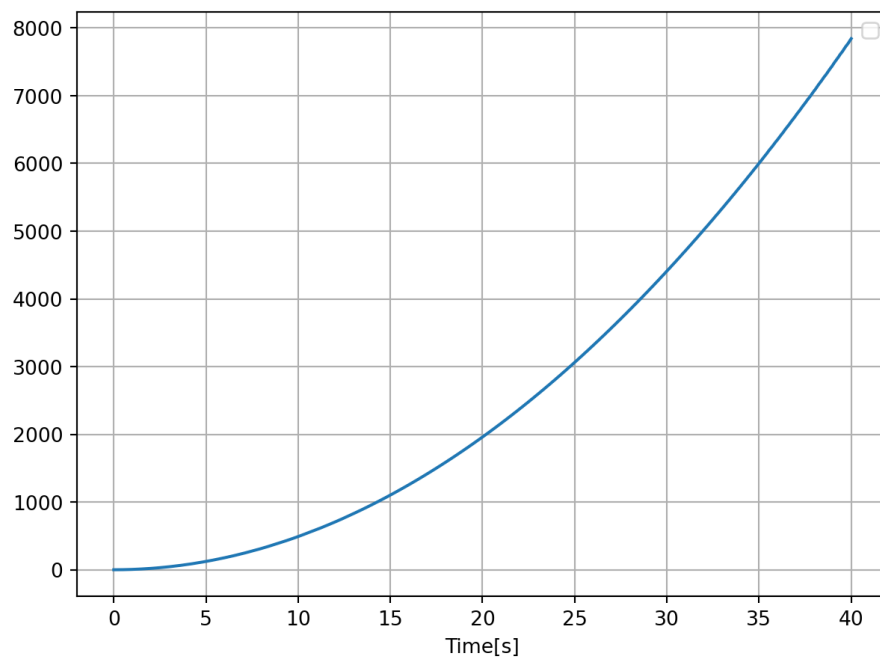


Figure 1: Simulation of the Two Mass Floating Bodies.

References

- [1] Xinyu Wang: *Erstellung eines Katalogs regelungstechnischer Problemstellungen mit ausführbaren Beispiellösungen*